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Sequential estimation of surface water mass changes from daily satellite gravimetry data

G. L. Ramillien · F. Frappart · S. Gratton · X. Vasseur

Abstract We propose a recursive Kalman filtering approach to map regional spatio-temporal variations of terrestrial water mass over large continental areas, such as South America. Instead of correcting hydrology model outputs by the GRACE observations using a Kalman filter estimation strategy, regional 2-by-2 degree water mass solutions are constructed by integration of daily potential differences deduced from GRACE K-band range rate (KBRR) measurements. Recovery of regional water mass anomaly averages obtained by accumulation of information of daily noise-free simulated GRACE data shows that convergence is relatively fast and yields accurate solutions. In the case of cumulating real GRACE KBRR data contaminated by observational noise, the sequential method of step-by-step integration provides estimates of water mass variation for the period 2004–2011 by considering a set of suitable a priori error uncertainty parameters to stabilize the inversion. Spatial and temporal averages of the Kalman filter solutions over river basin surfaces are consistent with the ones computed using global

monthly/10-day GRACE solutions from official providers CSR, GFZ and JPL. They are also highly correlated to in situ records of river discharges (70–95 %), especially for the Obidos station where the total outflow of the Amazon River is measured. The sparse daily coverage of the GRACE satellite tracks limits the time resolution of the regional Kalman filter solutions, and thus the detection of short-term hydrological events.

Keywords GRACE satellite gravimetry · Continental hydrology · Kalman filtering · Regional solutions

1 Introduction

Launched in March 2002, the Gravity Recovery and Climate Experiment (GRACE) mission has globally mapped the temporal variations of the Earth's gravity field at an unprecedented millimetre precision in terms of geoid height thanks to the accurate inter-satellite measurements made by the on-board K-band range (KBR) system (Tapley et al. 2004), and by now for more than 12 years. Pre-processing of Level-1 GRACE data consists of removing the effects of known a priori gravitational accelerations such as static gravity field, atmosphere and ocean mass changes, pole and oceanic tides from the measurements to produce Level-2 solutions that consist of “reduced” Stokes coefficients (i.e., dimensionless spherical harmonic coefficients of the geopotential—see theoretical aspects in Hofmann-Wellenhof and Moritz 2006) up to degree 90, or equivalently, of spatial resolutions of 200–300 km (Bettadpur 2007; Fletchner 2007; Chambers and Bonin 2012; Dahle et al. 2012). These global Level-2 solutions correspond to the gravity signatures of not modelled surface mass variations such as sudden earthquakes and continuous glacier melting, but mainly water mass transport

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over continental areas. North–south striping is particularly visible in the tropics where coverage of satellite tracks is poor due to (1) sparse GRACE track sampling in the latitudinal direction, (2) propagation of errors of the a priori correcting model accelerations (Han et al. 2004; Thompson et al. 2004; Ray and Luthcke 2006) and (3) numerical correlations generated while solving the undetermined systems of equations for high-degree Stokes coefficients (Swenson and Wahr 2006).

Short-term mass variability with periods from hours to days of ocean tides and atmosphere is removed using de-aliasing techniques of correcting model outputs. While the atmosphere pressure fields from ECMWF allow a reasonable de-aliasing of high frequency caused by non-tidal atmospheric mass changes, errors due to tide model appear in the GRACE solutions, especially from diurnal (S1) and semi-diurnal (S2) tides (Han et al. 2004; Ray and Luthcke 2006; Forootan et al. 2014). Thompson et al. (2004) showed that the degree error increased by a factor ~ 20 due to atmospheric aliasing, ~ 10 due to ocean model and ~ 3 due to continental hydrology, e.g., aliasing of the S2 tide has a strong impact on the determination of the C_{20} spherical harmonic coefficient of the geopotential (Seo et al. 2008). See, e.g., Guo et al. (2010) to know about the reduction of atmosphere aliasing by Gaussian smoothing.

A regional approach alternative to the classical global one has been more recently proposed to improve geographical localization of patterns of water storage change. This energy integral method consists of recovering equivalent-water thicknesses of juxtaposed 2-degree tiles from GRACE inter-satellite velocity residuals, by considering matrix regularization techniques for solving ill-posed problems, but without using spherical harmonics for representing water mass variations (see Ramillien et al. 2011, 2012). These multi-year series of 10-day regional solutions are comparable to independent datasets, such as local water level in the Amazon Basin, and thus they provide realistic amplitudes of water mass change from seasonal to inter-annual timescales over South America.

So far, global and regional solutions have been produced as weekly, 10-day and monthly averages from GRACE data, leading to a loss of resolution in time. In other words, global or regional averaging suppresses events with a gravity signature of a few days and thus does not enable us to capture them. Moreover, determining the regional equivalent-water heights for each separate time interval would neglect the temporal correlation between successive independent intervals imparted by the temporal dynamics of the water mass processes. While regional solutions computed as averages on constant 10-day intervals proved to be realistic snapshots of the surface water mass variability (Frappart et al. 2013a, b; Seoane et al. 2013), the next challenge is to attempt to improve the resolution of these regional solutions in time

for detecting more localized hydrological events lasting a few days.

Previously, Kurtenbach et al. (2009, 2012) and Sabaka et al. (2010) have proposed a recursive Kalman filter scheme for estimating daily Level-1B GRACE data taking into account statistical information on process dynamics and noise from geophysical models to gain in temporal resolution. Kurtenbach et al. (2009) have applied a Kalman filtering after having removed annual and semi-annual parts to obtain gravity variation time series of Stokes coefficients at daily intervals. These corrections have enabled them to consider a stationary isotropic process noise in time and space to derive an exponential covariance function of a first-order Markov process. In describing this process noise, Kurtenbach et al. (2009) have used a priori time and space covariances on Stokes coefficients. Unfortunately, daily spherical harmonics solutions remain smooth in space, due to the poor geographical coverage of the daily satellite tracks.

In this article, no a priori model is corrected by the GRACE observations, but the estimate is built iteratively by cumulating information of daily GRACE satellite tracks. As there are no daily GRACE satellite data to cover the surface of the Earth efficiently, we demonstrate that estimating regional time-cumulated solutions by the successive injection of daily GRACE tracks is achievable. The progressive integration of satellite observations has the advantage of avoiding inversion of large systems of equations in the determination of time-constant maps of water mass variation. The sequential method we propose is inspired from previous methods. However, our Kalman filter estimation is applied to regional solutions instead of global Stokes coefficients. First, the methodology of the two stages of the Kalman filter estimation (i.e., projection and correction) is presented, and secondly, its application for inverting simulated GRACE satellite data is shown. Thirdly, both the analysis of the convergence and the detection of short-term events are made by noise-free simulations from hydrology model outputs. This method is applied to invert along-track potential anomalies derived from real GRACE KBRR measurements to recover multi-year series of 2-by-2 degree solutions of water mass variations over South America. In the following, we use the term “regional averaged (or equivalently, cumulated) solutions computed at successive daily time steps”, but this does not imply a daily time resolution. Then, these estimates are confronted to the official global monthly GRACE solutions provided by CSR, GFZ and JPL (Release 5) filtered using the independent component analysis approach (Frappart et al. 2011), and 10-day regional solutions from Ramillien et al. (2012), 10-day global solutions from GRGS (Bruinsma et al. 2010), and GLDAS-NOAH (Rodell et al. 2004) and WGHM (Hunger and Döll 2008) outputs, as well as rapid events described by river discharge observations for validation. The possibility of detecting short-term water mass events is finally

discussed and tested by simulating localized water mass anomalies.

2 Datasets

2.1 Independent hydrological datasets

2.1.1 WGHM land water storage

The WaterGAP Global Hydrology model (WGHM) (Döll et al. 2003; Hunger and Döll 2008) is a conceptual model that simulates the water balance on continental areas at a spatial resolution of 0.5° . It describes the continental water cycle using several water storage compartments that include interception, soil water, snow, groundwater and surface water (rivers, lakes and wetlands). We consider the sum of all these contributions and called it Total Water Storage (TWS) to be comparable to GRACE observations, as these latter data correspond to the integrated continental hydrology change without distinguishing each compartment. WGHM has been widely used to analyse spatio-temporal variations of water storage globally and for large river basins (Günter et al. 2007). In this study, we use daily TWS grids from the model version WGHM 2.1f described by Hunger and Döll (2008) to simulate the GRACE hydrology-related geopotential anomalies, and recover the starting TWS variation grids, as accurately as possible from these modelled geopotential anomaly tracks over a region, to demonstrate the feasibility of the Kalman filter approach for estimating TWS change from GRACE observations.

2.1.2 GLDAS NOAH land water storage

The NOAH (NCEP, OSU, Air Force and Office of Hydrology) land surface model (LSM) simulates surface energy and water fluxes/budgets (including soil moisture) in response to near-surface atmospheric forcing and depending on surface conditions (e.g., vegetation state, soil texture and slope) (Ek et al. 2003). The data used in this study are soil moisture (SM) storage values from the NOAH LSM, with the NOAH simulations being driven (parameterization and forcing) by the Global Land Data Assimilation System (GLDAS) (Rodell et al. 2004). These SM estimates from GLDAS-NOAH version 2 have a spatial resolution of 1° and a temporal resolution of 3 h. They are accessible via the Hydrology Data Holdings page at the Goddard Earth Sciences Data and Information Services Center, <http://disc.sci.gsfc.nasa.gov/hydrology/data-holdings>. They were cumulated on the four soil layers representative of the top 2 m of the soil from the GLDAS-NOAH model and resampled at a daily timescale over the time period 2003–2010.

2.1.3 Measurements of river discharge

Time series of daily water discharges from in situ gauges located in Obidos (Amazon), Ciudad Bolivar (Orinoco), Tucurui (Tocantins), and Chapeton (La Plata) are used for comparisons to daily, 10-day and monthly anomalies of GRACE-based TWS over 2003–2010. These in situ records were downloaded for the period 2003–2010 from: (1) the Venezuelan water agency (Instituto Nacional de Meteorología e Hidrología—INAMEH) for Ciudad Bolivar ($63^\circ 36' 29''\text{W}$; $8^\circ 26' 20''\text{N}$); (2) the hydrological information system Hidroweb (<http://hidroweb.ana.gov.br/>) of the Brazilian water agency (Agência Nacional de Aguas—ANA) for Obidos ($55^\circ 39' 25''\text{W}$; $1^\circ 55' 23''\text{S}$), Manacapuru ($60^\circ 36' 32''\text{W}$; $3^\circ 18' 58''\text{S}$), Fazenda Vista Alegre ($60^\circ 01' 34''\text{W}$; $4^\circ 53' 53''\text{S}$), Porto Velho ($63^\circ 56' 46''\text{W}$; $8^\circ 47' 59''\text{S}$) and Tucurui ($49^\circ 40' 59''\text{W}$; $3^\circ 46' 59''\text{S}$) gauges; and (3) the Argentinian water agency (Instituto Nacional del Agua—INA) through the online database Base de Datos Hidrológica Integrada (BDHI—<http://www.hidricosargentina.gov.ar/>) for the Chapeton station ($60^\circ 16' 59''\text{W}$; $31^\circ 34' 26''\text{S}$).

2.1.4 Global GRACE solutions

Three processing centres including the Center for Space Research (CSR), Austin, Texas, USA, the GeoForschungs-Zentrum (GFZ), Potsdam, Germany and the Jet Propulsion Laboratory (JPL), Pasadena, California, USA, and forming the Science Data Center (SDC) are in charge of the processing of the GRACE data and the production of Level-1 and Level-2 products. These products are distributed by the GFZ's Integrated System Data Center (ISDC—<http://isdc.gfz-potsdam.de>) and the JPL's Physical Oceanography Distributive Active Data Center (PODAAC—<http://podaac-www.jpl.nasa.gov>). Pre-processing of Level-1 GRACE data (i.e., positions and velocities measured by GPS, accelerometer data and KBR inter-satellite measurements) is routinely made by the SDC, as well as monthly global GRACE gravity solutions (Level-2). These latter solutions consist of time series of monthly averages of Stokes coefficients (i.e., dimensionless spherical harmonics coefficients of geopotential) developed up to a degree between 50 and 120 that are adjusted from along-track GRACE measurements. A dynamical approach, based on the Newtonian formulation of the satellite's equation of motion in an inertial reference frame, centred at the Earth's centre of mass combined with a dedicated modeling of the gravitational and non-conservative forces acting on the spacecraft, is used to compute the monthly GRACE solutions. During the estimation process, atmospheric and ocean barometric redistribution of mass variations are removed from the GRACE coefficients using ECMWF and NCEP reanalysis for atmospheric mass variations and ocean tides, as well as global ocean circulation models (Bettadpur 2007;

Fletcher 2007). The GRACE coefficients are hence residuals that should include continental water storage change, and also signals from other geophysical phenomena and errors from correcting models and noise. The monthly GRACE solutions differ from one official provider to another due to the differences in the data processing, the choice of the correcting models and the data selection for computing the monthly averages.

A post-processing method based on independent component analysis (ICA) was applied to the Level-2 GRACE solutions from different official providers (i.e., CSR, GFZ, JPL), after a 400-km Gaussian pre-filtering. The separation is based on the assumption of statistical independence between the sources that compose the measured signals. The estimated contributors to the observed gravity field are forced not to be correlated numerically by imposing diagonal cross-correlations. The efficiency of ICA for separating land hydrology-related signals from noise by combining Level-2 GRACE solutions has previously been demonstrated in Frappart et al. (2010, 2011).

The GRGS-EIGEN GL04 models are derived from Level-1 KBR measurements and LAGEOS 1 and 2 data for enhancement of lower harmonic degrees and using an empirical stabilization; thus, these solutions do not require any low-pass filtering to get rid of striping (Lemoine et al. 2007; Bruinsma et al. 2010). Corresponding 10-day and monthly grids of TWS for the period 2003–2010 are available at: <http://grgs.obs-mip.fr>.

2.2 GRACE-based residual potential differences to be inverted

The K-band range (KBR) is the key science instrument of GRACE which measures the dual one-way range change of the baseline between the two coplanar, low-altitude satellites, with a precision of $\sim 0.1 \mu\text{m/s}$ on velocity difference, or equivalently, $10 \mu\text{m}$ in terms of line-of-sight (LOS) distance after integration versus time (Bruinsma et al. 2010). The average distance between the two GRACE vehicles is $\sim 220 \text{ km}$. The Level-1B KBR data represent the more precise measure of gravity variations sensed by the GRACE satellite tandem with a 10^{-7} m/s accuracy, that gives access to surface water mass transfers. Coupled with the accurate 3-axis accelerometers measuring the effects of non-conservative forces acting on the satellites (i.e., atmospheric drag and solar pressure) and a priori models for correcting atmosphere and ocean mass, oceanic and solid tides and polar tides, KBR rate residuals are computed by least-squares dynamical orbit determination of 1-day-long and 5-second sampled tracks. A priori gravitational force models for numerical orbit integration of the GRACE satellites A and B prepared at the GRGS centre in Toulouse (Bruinsma et al. 2010) are: (1) a static gravity field model EIGEN-GRGS.RL02.MEAN-FIELD to

degree and order 160; (2) 3D body perturbations DE403 of Sun, Moon and six planets (Standish et al. 1995); (3) solid Earth tides of the IERS conventions 2003 (McCarthy and Petit 2003); (4) solid Earth pole tide of the IERS conventions; (5) oceanic tides FES2004 to degree and order 100 (LeProvost et al. 1994); (6) Desai model of the oceanic pole tide (Desai 2002); (7) atmospheric pressure model ECMWF 3D grids per 6 h; and (8) oceanic response model MOG2D (Carrère and Lyard 2003). These KBR Rate (KBR) residuals represent the gravitational effects of non-modelled phenomena, and mainly the contribution of continental hydrology. They are easily converted into variations of along-track potential differences between the two GRACE satellites, following the energy integral method as proposed earlier by Jekeli (1999), Han et al. (2006) and lately Ramillien et al. (2011). Once corrected from known gravitational accelerations, along-track Residual Differences of Potential (RDP) mainly caused by hydrology variations in a selected continental region can reach $\pm 0.1 \text{ m}^2/\text{s}^2$ within a precision of $\sim 10^{-3} \text{ m}^2/\text{s}^2$ (see Ramillien et al. 2011). These form the initial data set for our Kalman filter approach.

3 Methodology

3.1 The forward problem

We suppose that the continental region consists of M juxtaposed surface elements ($j = 1, \dots, M$) of area S_j located at longitude λ_j and latitude θ_j , and characterized by an equivalent-water height h_j . The grid steps in longitude and latitude are $\Delta\lambda$ and $\Delta\theta$ respectively, in the case of a geographical grid. Let Γ_k be the N -by- M Newtonian matrix that relates the equivalent uniform water height h_j and the GRACE-based potential differences Y_i ($i = 1, \dots, N$) for each daily period of observation k . The coefficients of this matrix are simply deduced from the inverses of the Cartesian distances ξ between the surface element heights X_k and the successive positions of the GRACE satellites flying over the considered region (see Ramillien et al. 2011). Then, the observation equation can be written as:

$$\Gamma_k X_k = Y_k + v_k \quad (1)$$

where v_k is a zero-mean process noise usually drawn from a zero-mean multivariate normal distribution with covariance matrix R_k (i.e., $v_k \sim N(0; R_k)$). In the construction of the Newtonian matrix Γ_k , developing the inverse of the distance in sums of Legendre polynomials of $n = 300$ – 500 terms enables us to introduce the elastic Love numbers k_n , to take compensation of surface water masses by elastic response of the Earth's surface into account (Ramillien et al. 2011).

Additional information has to be included to find a stable mass variation estimate. In this study, we use a simple first-

order Gauss–Markov process to model the evolution of the current estimate X_k with time. More precisely, given $k > 1$, we use the simple prediction equation:

$$X_k = X_{k-1} + w_k \quad (2)$$

where w_k is a zero-mean process noise usually drawn from a zero-mean multivariate normal distribution with covariance matrix Q_k (i.e., $w_k \sim N(0; Q_k)$) describing the errors of the process. Although this dynamic is known to remain very crude, promising results will be shown in Sect. 4. The authors are well aware of the fact that this model can be improved by introducing an evolution model that might consist in exploiting outputs of hydrology models such as WGHM and GLDAS. Following Kurtenbach et al. (2009), a more sophisticated dynamical equation than Eq. 2 has been considered through a linearized dynamic (i.e., a finite difference matrix obtained from WGHM) that is described by the prediction equation (Eq. 2). Unfortunately, the results were not significantly different from the ones shown in Sects. 5 and 6. These disappointing results may be due to the use of a linearization technique or to the presence in the observations of effects not taken into account by the model. As the Newtonian operator Γ_k constructed from the relative Cartesian distances and applied to the unknown parameters (i.e., the equivalent-water heights) is completely linear (see Ramillien et al. 2011, 2012), for a given set of a priori uncertainty parameters, the Kalman filter estimate considering the entire GRACE-based RDP dataset is the same as the one obtained by summing all the separate Kalman filter estimates. This is the case if the complete RDP series are decomposed into pure dominant annual and semi-annual components plus any kind of RDP sub-dataset. In particular, the problem of recovering short-term hydrological events by tuning a priori uncertainty parameters is tackled in Sect. 6 by several simulations.

3.2 The inverse problem: sequential estimation—the Kalman filter equations

The observation equation (Eq. 1) and the prediction equation (Eq. 2) directly fit into the Kalman filter equation settings. The Kalman filter is a recursive estimator where one needs the knowledge of the previous state and new measurements to determine the actual state (Kalman 1960; Kalman and Bucy 1961; Evensen 2007). In our setting at iteration number k , the state of the estimator is represented by two variables: the current estimate X_k (i.e., the vector containing the equivalent-water heights) and its error covariance matrix P_k (i.e., the matrix of the uncertainties on the estimate).

The observations of the current state are used to correct the predicted variables to obtain a more precise estimate. First, the Kalman gain matrix is computed as:

$$K_k = P_k \Gamma_k^T \left[\Gamma_k P_k \Gamma_k^T + R_k \right]^{-1} \quad (3)$$

where R_k is the covariance of the measurements errors considered as independent (i.e., $R_k = \sigma_d^2 I$, where σ_d^2 is the error variance on the RDP Y_k , and I represents the identity matrix). Secondly, the updated a posteriori state estimate is obtained as:

$$X_k^* = X_k + K_k [Y_k - \Gamma_k X_k] \quad (4)$$

and the updated a posteriori error covariance matrix of the state estimate is computed as:

$$P_k^* = [I - K_k \Gamma_k] P_k \quad (5)$$

At the end of this step, X_{k+1} is deduced according to Eq. 2: $X_{k+1} = X_k^*$ and the resulting covariance matrix to be used at the next step is simply defined as:

$$P_{k+1} = P_k^* + Q_k \quad (6)$$

Note that for independent potential difference observations at time interval k , Q_k is often chosen as the diagonal matrix:

$$Q_k = \sigma_p^2 I \quad (7)$$

where σ_p^2 is the a priori variance of process errors. The Kalman gain appears as a measure of the relative uncertainty of the measurements and the current state estimate, and it can be “tuned” to achieve particular performance. When the gain is high, it places more weight on the observations and thus follows them more closely, whereas when it is low, the Kalman filtering follows the model prediction, smoothing noise out. In the extreme case of gain of zero, the measurements are completely ignored.

4 Application

4.1 Inversion of potential differences simulated from hydrology model outputs

4.1.1 Recovery of a piece-wise time-constant water mass anomaly map

First, we need to validate the proposed sequential method of estimation by recovering “static” 30-day averaged water mass anomaly maps from GRACE-type potential differences simulated using daily outputs from WGHM, over large continental areas. For this purpose, regular 2-by-2 degree grids of equivalent-water heights over South America [90°W–30°W, 60°S–20°N] are averaged onto monthly periods from daily WGHM outputs. GRACE-type ascending and descending tracks of 5-second sampling are easily generated by the GINS software from the satellite ephemeris data and for the region of interest. Along-track potential differences are simply computed at each satellite position using Eq. 1 without noise (i.e.,

$v_k = 0$). The test consists of recovering, as precisely as possible, the static 30-day averaged water mass anomaly map by applying the Kalman filter integration (Eqs. 2–7) of successive synthetic daily potential differences. The first guess is assumed to contain no hydrological signals (i.e., $X_{k=0} = 0$ for all elements of this vector for “cold start”), and in the case of no starting cross-error covariances between equivalent-water heights to recover, so we start with: $P_{k=0} = \sigma_m^2 I$. Then, the solution is progressively built by accumulation of information from the daily GRACE RDP tracks.

As illustrated on the top row of Fig. 1, the process of estimation converges rapidly to a stable solution, which is identical to the starting water mass anomaly after 30 days of integration. Root mean square error is typically less than 10 mm after the first iteration, 1 mm after the fifth iteration, 0.1 mm after the 10th iteration, and finally 0.01 mm of equivalent-water height after a month of integration, compared to amplitude of ± 300 mm of the hydrological patterns. Even short-wavelength details are revealed in the final Kalman filter solution, confirming that this noise-free recovery from simulated GRACE data is successful. A posteriori uncertainties on the fitted equivalent-water heights (i.e.,

square root of the diagonal elements of P_k) decrease, following the north–south direction of the tracks during the first iterations. Then they tend to be homogeneous on the whole region at the end of the fit. They are finally less than 0.1 mm, when the starting value is $\sigma_m = 1$ mm.

Different intervals (1, 2 or 5 days) of integration yield to the same final solution in the case of recovering a noise-free 30-day constant map of water mass anomaly. Several combinations of σ_d and σ_m have been tested on the simulated case of recovery from 10^{-9} to 10^{-2} m^2/s^2 , and 10 and 800 mm, respectively. A priori uncertainty on observations σ_d acts as a regularization parameter and makes the inversion of the linear system for getting the Kalman gain (Eq. 3) possible. Large values of this uncertainty parameter enable substantial improvements of the solution at each integration step and thus accelerate the convergence to the final estimate. On the contrary, the convergence is slow and the final estimate is smooth when σ_m is low (Fig. 2). In this latter case, low values of this parameter correspond to less weight of the GRACE observations in the Kalman gain K during the refreshing process of the solution. The final errors of a constant-time (monthly) map of water mass (i.e., difference between the estimate and

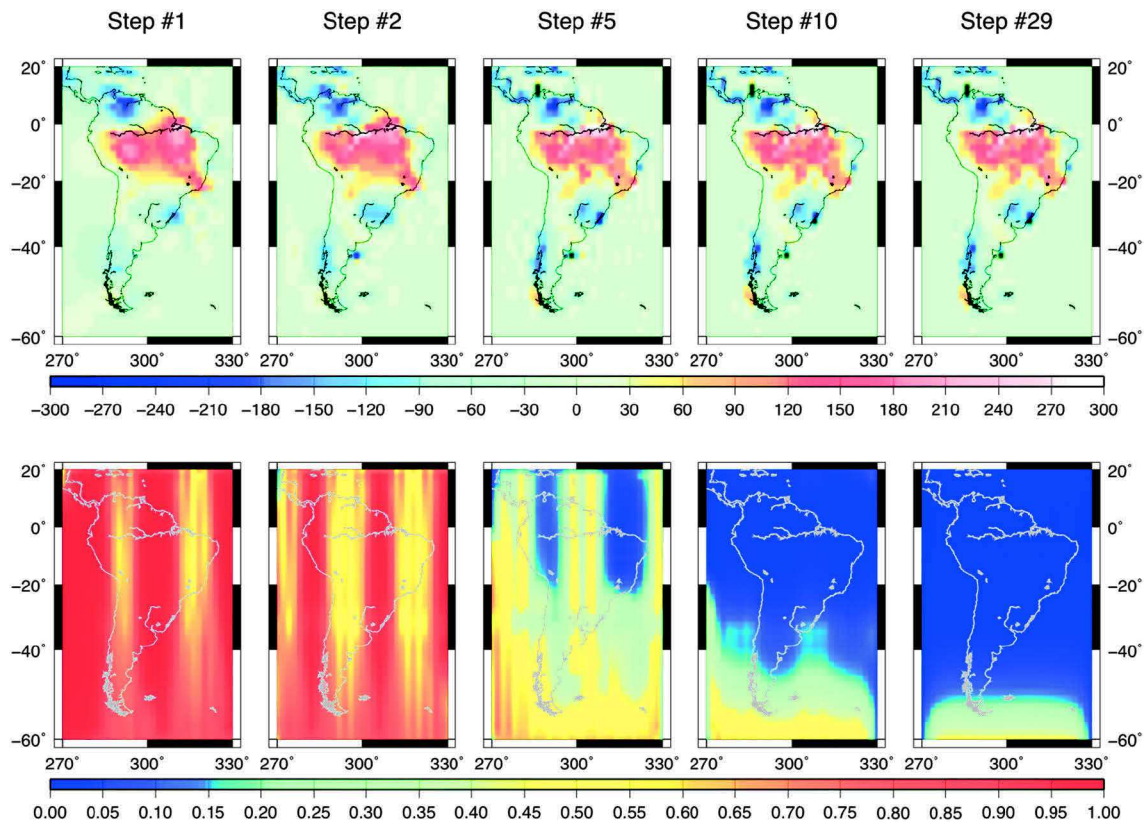


Fig. 1 Recovery of monthly mass variations over South America for March 2005 from simulated along-track RDP. Units are mm of equivalent-water height. Estimated regional maps obtained by accumulation of 1-day data that converge to a stable solution (*top row*), and the decreasing of the corresponding a posteriori uncertainties on the

water heights, starting from 1 mm down to <0.05 mm (*bottom row*). Final absolute error is around 0.01 mm after 30 steps (i.e., 30 days) of integration. Note the residual edge effect on the Southern boundary due to geographical truncation

Fig. 2 Convergence analysis of the recovery using a priori potential anomaly standard deviation of $\sigma_d = 10^{-9} \text{ m}^2/\text{s}^2$ (i.e., exact observations) and different a priori parameter uncertainties σ_m : 1 mm (circles), 10 mm (triangles), 100 mm (squares), 500 mm (stars)

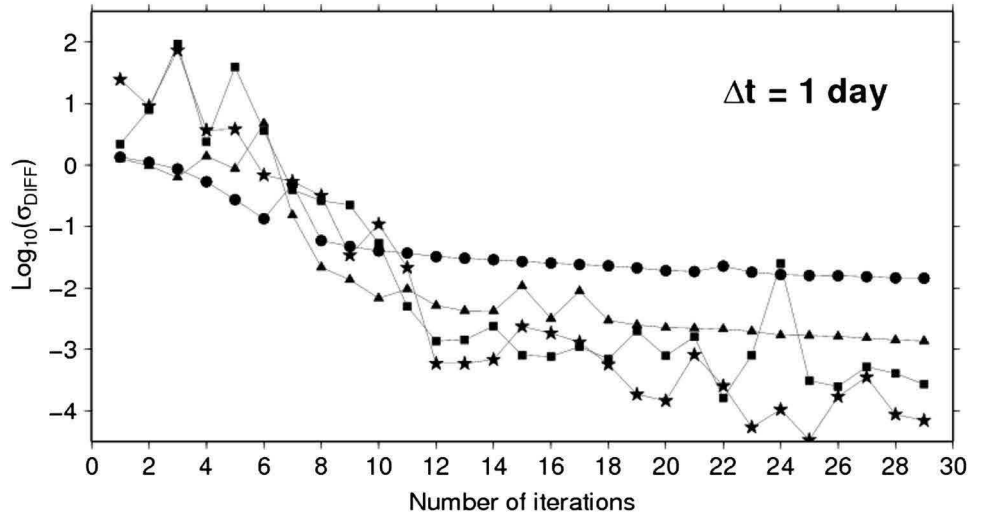
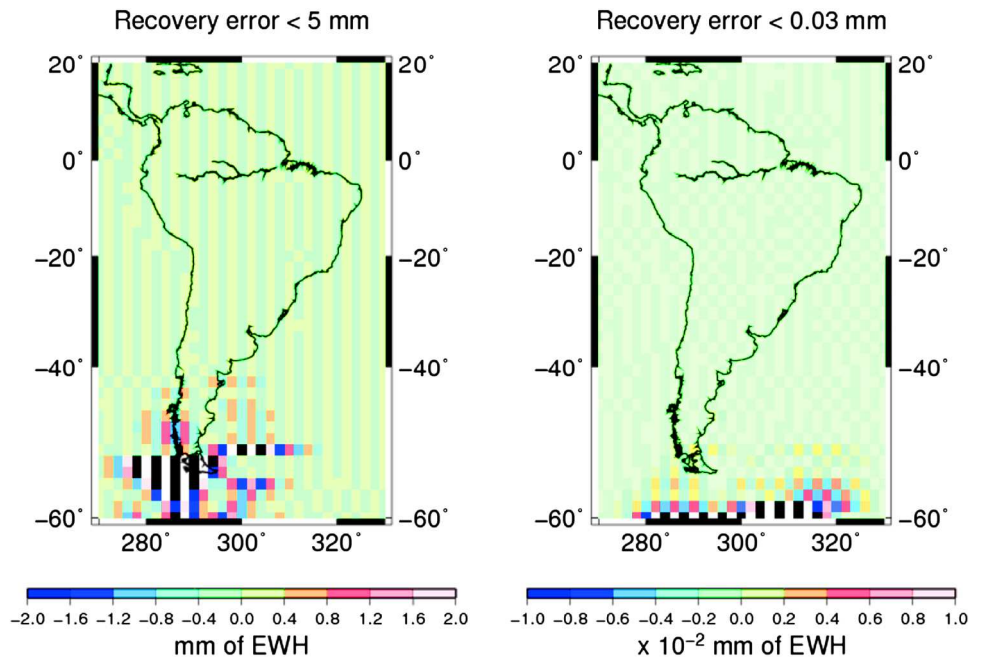


Fig. 3 Final error after cumulating $k = 30$ days of simulated RDP data when recovering a time-constant (monthly) water mass map from daily RDP over South America for $\sigma_m = 1$ mm (left) and $\sigma_m = 500$ mm (right)



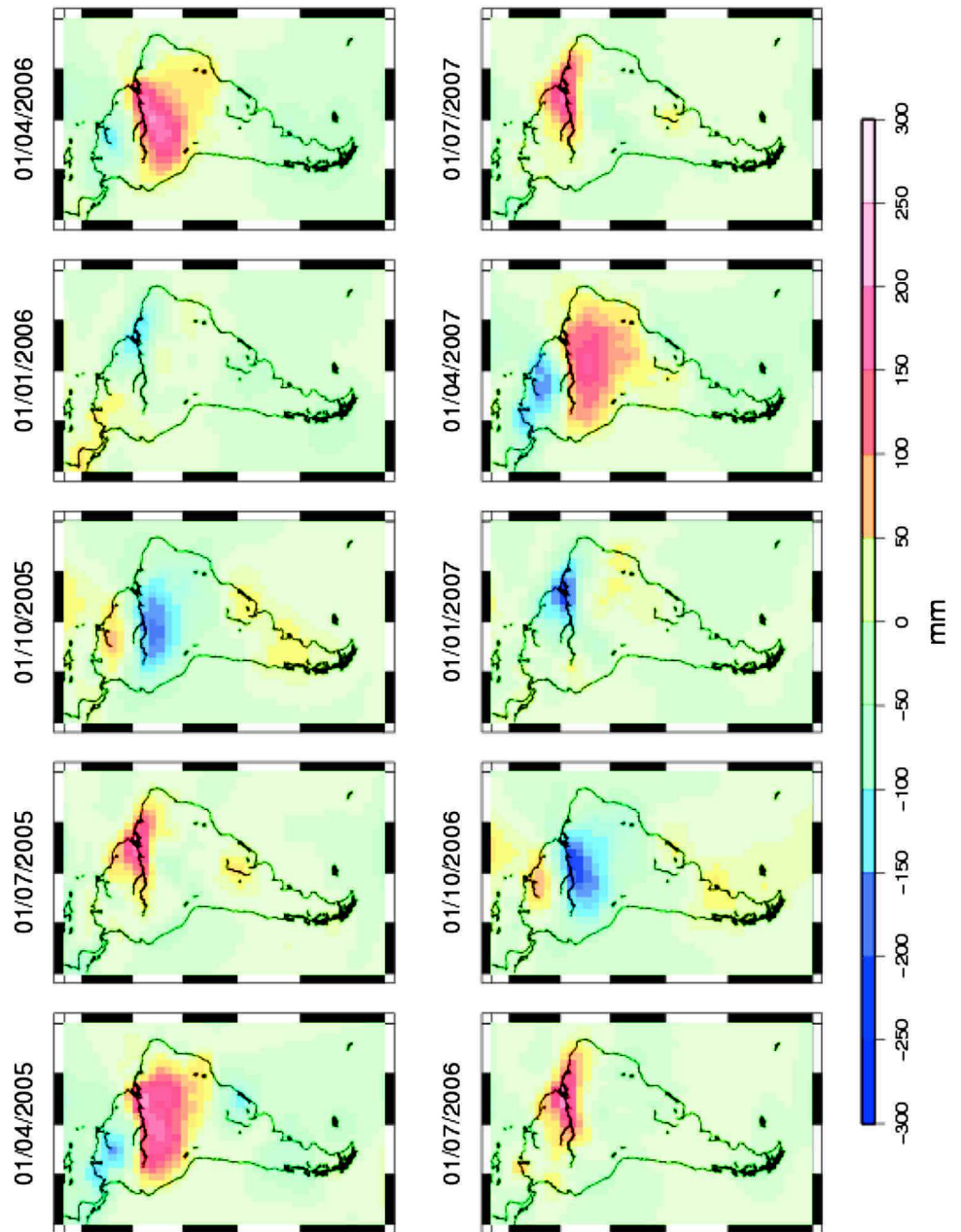
the reference WGHM water mass used for simulating RDP data) remain particularly small (Fig. 3), especially if σ_m is large (e.g., 500 mm), suggesting that the recovery is successful.

4.1.2 Recovery of water mass change maps by daily updates

While the recovery of a water mass solution from RDP simulated from a 30-day constant WGHM map is successful (see previous part), the next test is to estimate cumulated solutions from RDP computed using daily-varying hydrology. GRACE RDP tracks passing over South America are simulated each day at 5-second sampled orbit positions and from the WGHM (or GLDAS) total water storage (TWS) outputs for the period 2005–2007, using Eq. 1 without noise

(i.e., $v_k = 0$). Complete series of regional solutions of water mass variation can be estimated by a Kalman filter integration strategy on daily sampling intervals and tuning a priori error parameters. Figure 4 presents regional solution when considering $\sigma_d = 0.01 \text{ m}^2/\text{s}^2$ and $\sigma_m = 200$ mm, and obtained by cumulating WGHM-simulated daily along-track differences of potential. These solutions reveal realistic seasonal amplitudes in the drainage basins of South America. Absolute errors are defined as the differences between input and recovered 2-by-2 degree water mass grids for the same day. In this case of considering very accurate RDP data (i.e., σ_d very small) and in the absence of additional noise, the main hydrological structures of ± 300 mm of EWH are retrieved and quite well located on the main river basins of South America.

Fig. 4 Daily 2-by-2 degree regional maps of TWS over South America plotted at monthly intervals [units: mm of equivalent-water height (EWH)]



In particular, Fig. 5 shows the water mass time series for the surface element corresponding to Manaus ($60^{\circ}01'32''\text{W}$, $3^{\circ}08'06''\text{S}$), located in the centre of the Amazon basin. In our tests for Manaus tile and using model-simulated data, a priori error uncertainty ranges from $\sigma_d = 10^{-6} \text{ m}^2/\text{s}^2$ to $\sigma_d = 0.1 \text{ m}^2/\text{s}^2$ while the parameter $\sigma_m = 200 \text{ mm}$ is constant during the Kalman filter integration. As in the case of recovery of a time-constant map, the error of recovery of sub-monthly time-varying signals appears small when the RDP data are considered accurate (i.e., σ_d very small). However, this strong assumption permits the development of numerical instabilities. Representing the series of estimated water mass maps shows that using a priori error uncertainty σ_d less than

$0.001 \text{ m}^2/\text{s}^2$ creates unrealistic meridian striping in these maps that increases with the number of days integrated into the current solution.

Tests of recovery of a “static” water mass grid, made in the previous Sect. 4.1.1, show that σ_m controls the amplitude of information by the RDP tracks each day. In the case of recovering time-varying water mass maps with different starting values of σ_m , the Kalman filter process progressively converges to the same series of daily sampling step estimates (Fig. 6), and the time taken by the integration to reach this common solution (or “spin up”) from a cold start (i.e., no starting information: $X_{k=0} = 0$) is ~ 3 months. This “spin up” is of 1 month for recovering a constant-time water mass

Fig. 5 Multi-year time series of TWS for the surface tile number 357 centred over Manaus, that are obtained by integration of WGHM-simulated daily GRACE RDP data for several a priori error uncertainties, and a constant a priori error uncertainty on the parameters to be retrieved (i.e., the equivalent-water heights) first guess is $X_{k=0} = 0$ (i.e., “cold start”)

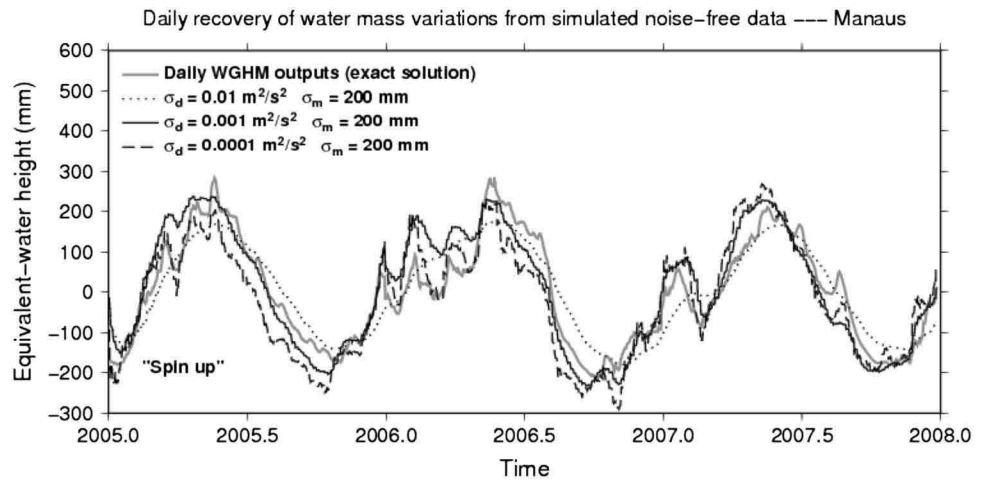
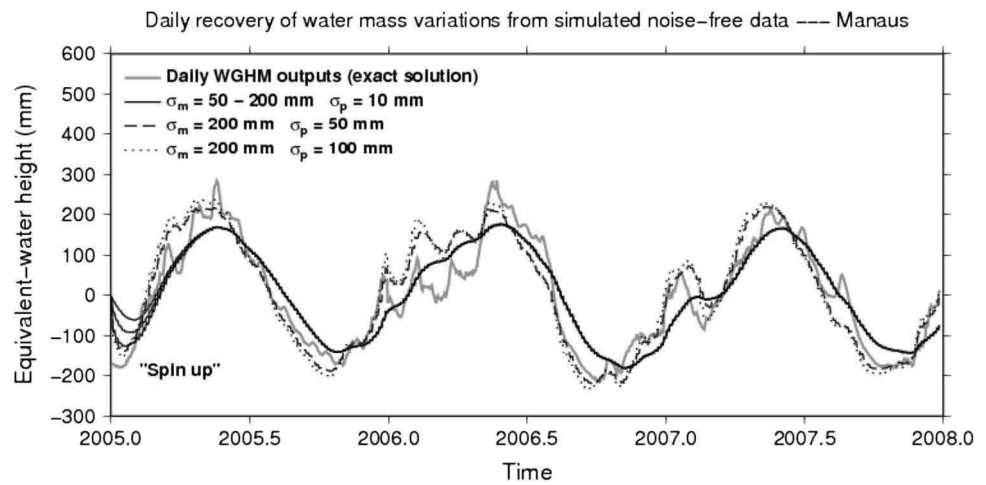


Fig. 6 Multi-year time series of TWS for the surface tile number 357 (Manaus) obtained for several a priori error uncertainties on the process (i.e., σ_p) and the equivalent-water heights (i.e., σ_m)



map, as the simulated RDP data are more consistent to each other on the period of integration and reinforce the same “static” surface distribution of water mass to be retrieved (see Sect. 4.1.1). Considering daily WGHM-based water mass variations, RDP data partly contain unexpected time-varying signals that perturb the convergence of the integration process and make the “spin up” longer. As for the a priori error σ_d on the RDP observations, important values of a priori process error σ_p (i.e., >50 mm) generate unrealistic meridian stripes in the estimated water mass maps.

For approaching more realistic conditions of data acquisition, high-frequency random noise can be added to the model-simulated GRACE RDP, but its effect is highly amplified if considered real and accurate signals (e.g., when a random noise of $0.001 \text{ m}^2/\text{s}^2$ amplitude is added in the simulated GRACE data, the daily Kalman filter solutions are only slightly degraded but smoothed if $\sigma_d = 0.01 \text{ m}^2/\text{s}^2$ or $\sim 10\%$ of hydrology-related RDP according to Ramillien et al. 2011). Unfortunately, the recovery errors reach tens of mm when the level of noise is greater than $0.01 \text{ m}^2/\text{s}^2$. To cancel the effect of noise amplification in the inversion, we

found that the best compromise is to consider that σ_d and σ_m are about $10^{-3} - 10^{-2} \text{ m}^2/\text{s}^2$ and $100 - 200$ mm, respectively, with value of a priori process error σ_p as small as possible.

4.2 Recovery of maps from real GRACE RDP

Inversion of real potential differences for continental hydrology appears complicated because of contaminating instrumental noise, even if potential anomalies should be smooth at satellite altitude as the result of upward continuation. In return, downward continuation associated to the recovery of surface water mass anomaly amplifies the high frequencies of the signal, in particular noise of any kind. Moreover, important errors from pre-treatment such as correcting by imperfect models still remain in the orbit observations and aliased with space and time (see Sect. 2.2). Another problem arises as KBR rate residuals contain unrealistic long-term variations at fractions of the satellite revolution period. The strategy lately proposed by Ramillien et al. (2011, 2012) is to remove a linear trend to each potential difference track crossing the considered regions for each day before inversion, so that

a recovery of medium- and high-frequency regional water mass variations is made, but at least without adding erroneous spatial long wavelengths. These missing wavelengths are added back from GRGS global solutions to complete the inverted signals afterwards.

2-by-2 degree water mass solutions after Kalman filter integration of daily GRACE RDP over South America for 2004–2010 are displayed on Fig. 7a, b. Starting parameters of Kalman filter estimation are $\sigma_d = 0.005 \text{ m}^2/\text{s}^2$ and $\sigma_d = 0.01 \text{ m}^2/\text{s}^2$ $X_{k=0} = 0$ (i.e., “cold start”), $P_{k=0} = \sigma_m^2 I$ with $\sigma_m = 200 \text{ mm}$ of equivalent-water height, and no a priori process errors. When $\sigma_d = 0.005 \text{ m}^2/\text{s}^2$, meridian striping and edge effects rapidly dominate the Kalman filter

solutions after ~ 1 year of integration of daily RDP tracks and till the end of the total period (Fig. 7a). Increasing slightly this a priori parameter up to $0.01 \text{ m}^2/\text{s}^2$ for an efficient regularization enables us to avoid the development of such unrealistic numerical instabilities in the time series of smoother solutions (Fig. 7b) where seasonal amplitudes are comparable to the ones of the global CSR solutions (Fig. 7c) (see also Tables 1, 2). Besides, additional runs for testing different a priori errors have been made to compute multi-year series of regional Kalman filter solutions that show the seasonal alternating of the large water mass amplitudes in the Amazon and Orinoco river basins. Figure 8 illustrates the case of the time series for the surface tile centred on Manaus. It reveals realis-

Fig. 7 Snapshots of 2-by-2 degree regional solutions of TWS over South America estimated from real GRACE RDP data and assuming $\sigma_m = 200 \text{ mm}$ and $\sigma_p = 10 \text{ mm}$, and plotted at 3-month intervals revealing the dominant seasonal amplitudes of water mass over South America: Kalman filter solutions for a priori error uncertainty **a** $\sigma_d = 0.005 \text{ m}^2/\text{s}^2$ and **b** $\sigma_d = 0.01 \text{ m}^2/\text{s}^2$, and **c** corresponding 400-km low-pass filtered CSR solutions (monthly averages) for the same periods for comparison

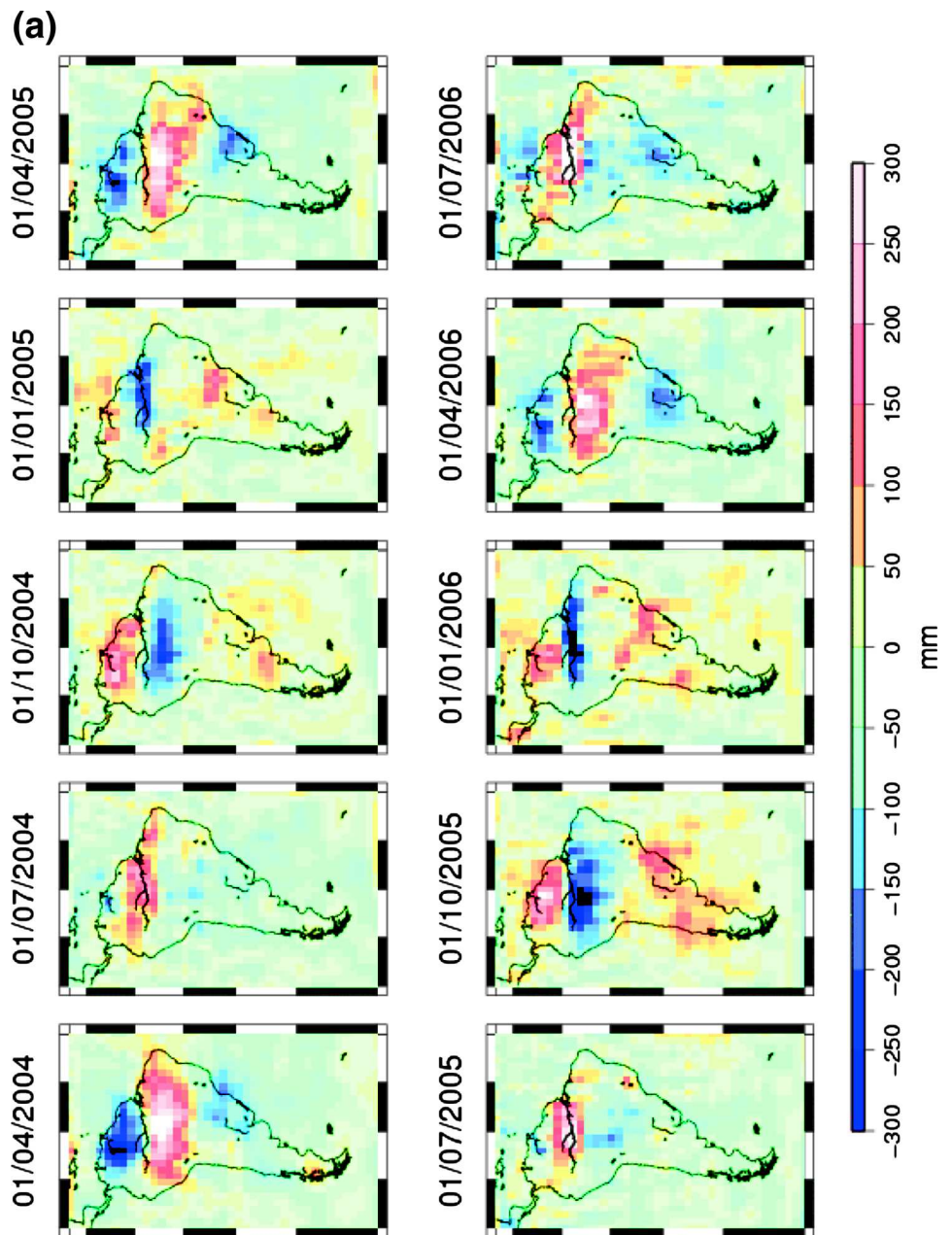
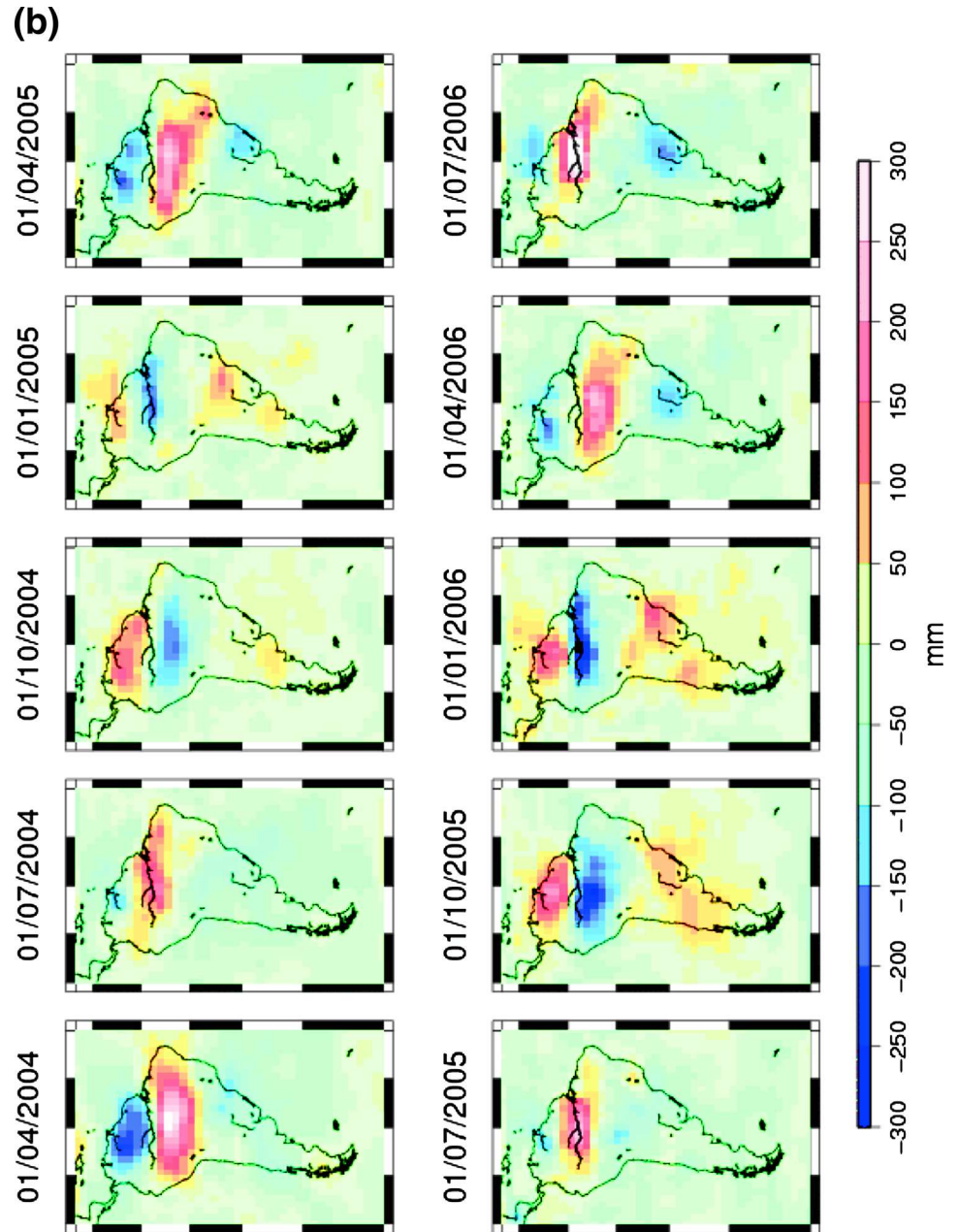


Fig. 7 continued



tic seasonal oscillations of 300–600 mm of EWH, which are clearly modulated by inter-annual variations. As expected, smooth estimates versus time are obtained when considering not precise GRACE RDP data (i.e., $\sigma_d = 0.1 \text{ m}^2/\text{s}^2$), but we found that values of σ_d lesser than $0.007 \text{ m}^2/\text{s}^2$ significantly amplify the noise contained the real GRACE RDP. The time series of these estimated Kalman filter maps will be validated in Sect. 5.

4.3 Errors due to spatio-temporal aliasing

Figure 9 is a visualization of the extra information brought by the GRACE satellite tracks computed as two successive

Kalman filter solutions. It shows that the Kalman filter estimate is daily updated in the very close neighbourhood under the satellite tracks—in a surface radius of about 600–800 km (e.g., see the numerical tests made in Ramillien et al. 2012)—just under the satellite tracks where the new information is brought. While the covariance function of the RDP data is smooth at satellite altitude (~ 400 km), the one of the corresponding water mass (i.e., the source of anomaly) is also much localized on the Earth’s surface due to downward continuation. This new along-track information represents a few tens of mm of EWH. Consequently, nothing is refreshed elsewhere, in areas which are not surveyed by the GRACE satellite during the considered day. This partial sampling explains

Fig. 7 continued

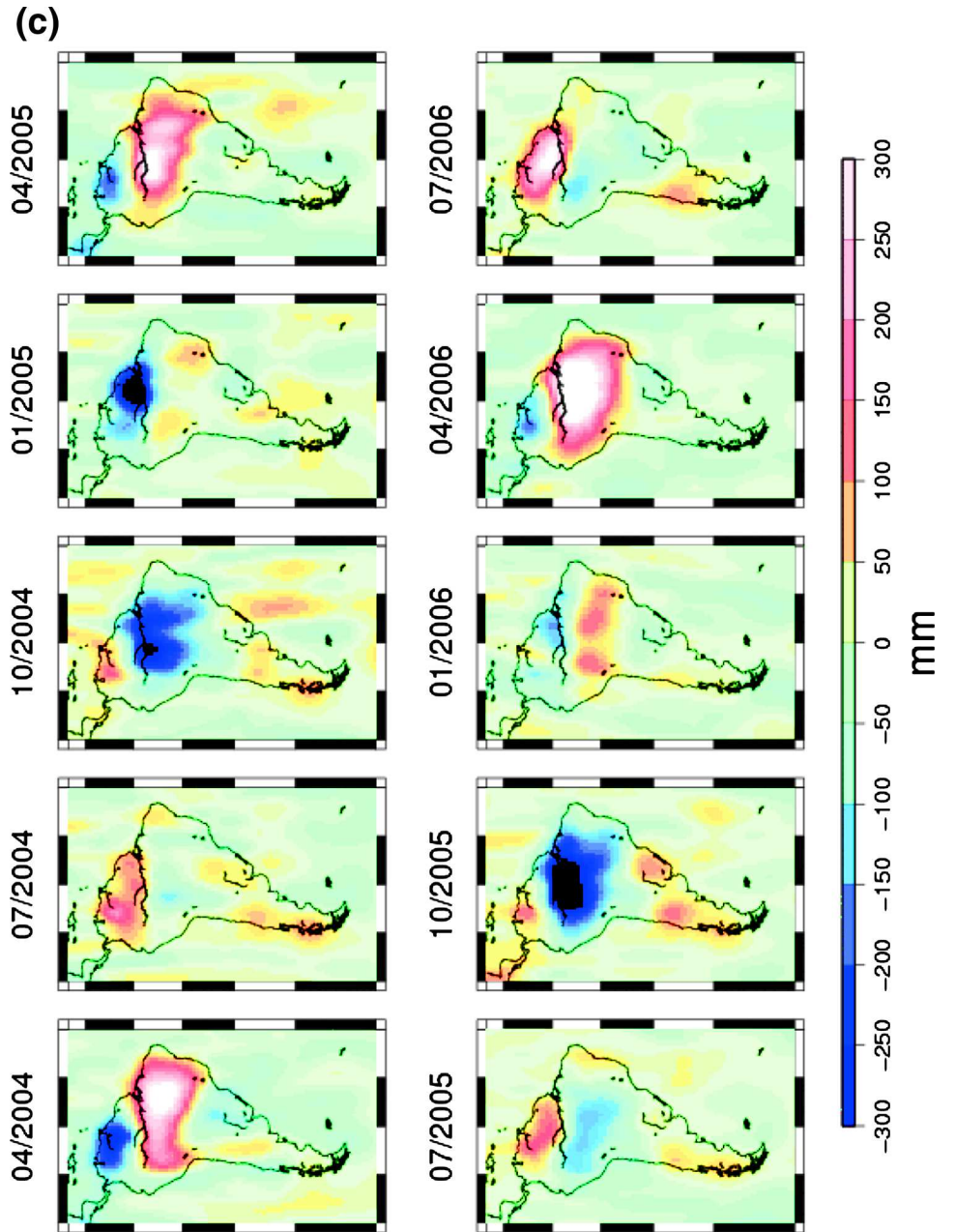


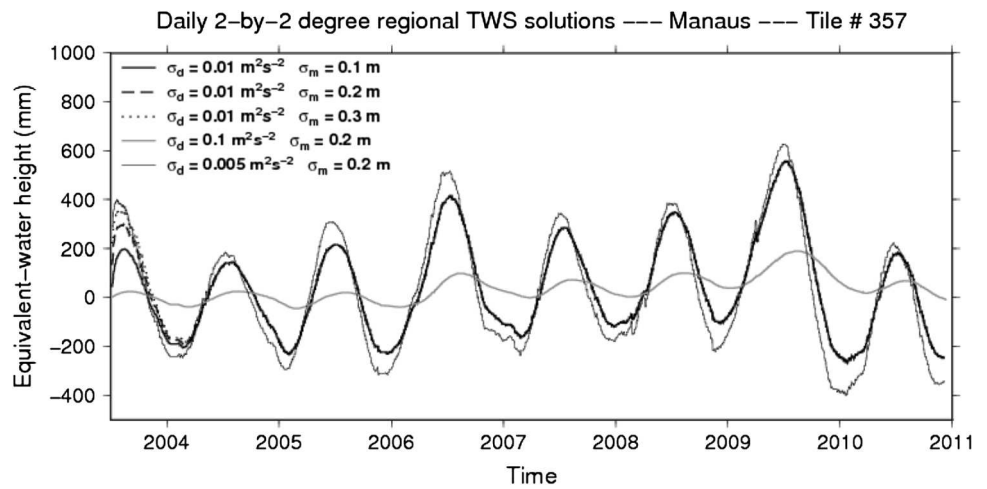
Table 1 Root mean square of the absolute differences between daily Kalman filter solutions and different TWS datasets for spatial averages over the main drainage basins of South America [units: mm of equivalent-water height (EWH)]

	Amazon	Paraná	Orinoco	Tocantins
WGHM 2005–2006–2007 (daily)	68.1	26.9	79.7	75.6
GLDAS NOAH 2005–2006–2007 (daily)	71.7	26.6	96.7	98.2
Regional solutions (Ramillien et al. 2012) (10-days)	18.2	22.7	62.6	42.2
GRGS (10-days)	27.5	26.6	70.7	61.7
Global CSR (monthly)	51.3	20.9	45.9	57.1
Global GFZ (monthly)	47.1	17.8	47.3	55.3
Global JPL (monthly)	51.0	19.8	47.2	54.9

Table 2 Linear correlations (%) between time series of GRACE solutions and of river discharge variations measured different stations

	Obidos (Amazon)	Chapeton (Paraná)	Ciudad Bolivar (Orinoco)	Turucui (Tocantins)
Kalman filter solutions				
$\sigma_d = 0.01 \text{ m}^2/\text{s}^2$ (daily)	92 (18.2)	68 (22.8)	78 (62.6)	81 (42.2)
Kalman filter solutions				
$\sigma_d = 0.001 \text{ m}^2/\text{s}^2$ (daily)	95 (29.6)	61 (31.3)	64 (91.3)	69 (52.5)
Regional solutions				
(Ramillien et al. 2012) (10-days)	87	75	92	81
Root mean square (RMS) values of the differences with Kalman filter solutions are indicated between parenthesis				
Global GRGS (10-days)	87	67	92	83
Global CSR (monthly)	85	74	93	85
Global GFZ (monthly)	86	75	92	91
Global JPL (monthly)	84	75	91	86

Fig. 8 Time series of TWS for Manaus obtained by integration of real daily GRACE RDP data for several a priori error uncertainties



that the reconstruction of a “static” map takes at least 10 days of data before the Kalman integration has a sufficient spatial coverage of the satellite tracks at the end (see previous Sect. 4.1.1). It also explains residual errors of recovery in the series of regional Kalman filter solutions, even if noise-free model-simulated RDP data are inverted (e.g., differences with model TWS values in Fig. 5), since off-track small and rapid hydrological features cannot be recovered, or partly retrieved, alternatively their signatures remain in the following Kalman filter solutions. Detection of sudden and localized hydrological events by tuning a priori error uncertainties and considering different cases of data coverage is explored with synthetic RDP data in the discussion of Sect. 6.

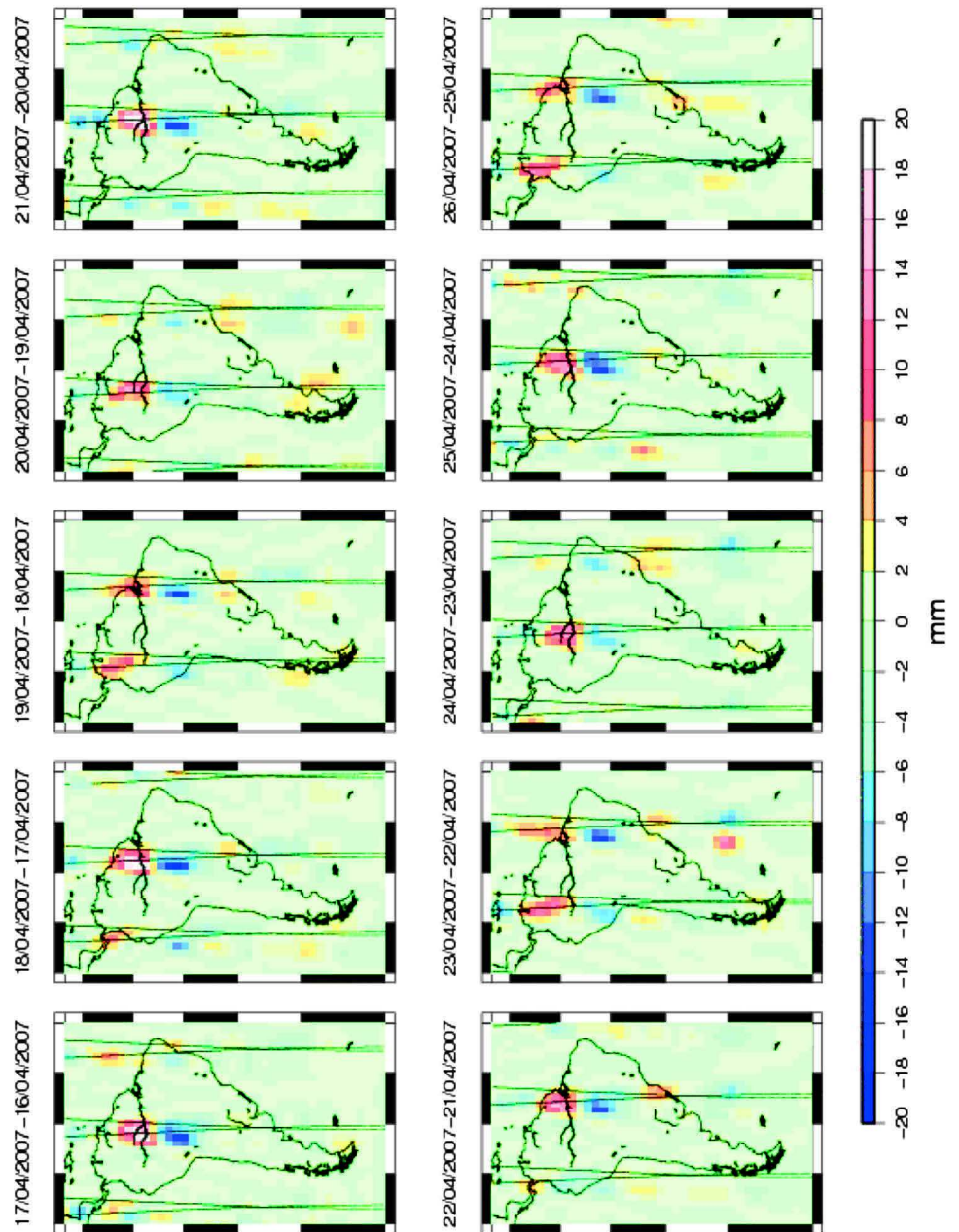
5 Validation of the Kalman filter solutions

Validation consists of confronting regional estimates of TWS obtained by integration of Kalman filter to existing GRACE-based products and independent datasets. For this purpose, we consider different sources of information presented in

Sect. 2: daily WGHM and GLDAS land waters outputs, monthly global GRACE solutions computed by the official providers CSR, GFZ and JPL, as well as local records of river discharge. Comparisons with the 10-day regional solution of water mass variation over South America lately proposed by Ramillien et al. (2012) have been also performed. Global Release 5 monthly solutions from CSR, JPL and GFZ have been low-pass filtered using a classical 400-km Gaussian filter (Wahr et al. 1998) and an ICA approach (Frappart et al. 2010, 2011) to reduce striping. To make the sampling of Kalman filter solutions comparable with the other GRACE solutions in space and time, they have been averaged over both the 10-day and monthly intervals, and over the largest drainage basins of South America: Amazon (~ 6 millions of km^2), Paraná (~ 2.6 millions of km^2), Orinoco (~ 1 million of km^2) and Tocantins (~ 0.8 million of km^2).

Statistical results of the comparisons of averages are summarized in Table 1. It shows that the Kalman filter solutions are statistically closer to the 10-day regional solutions from Ramillien et al. (2011) than the monthly global solutions.

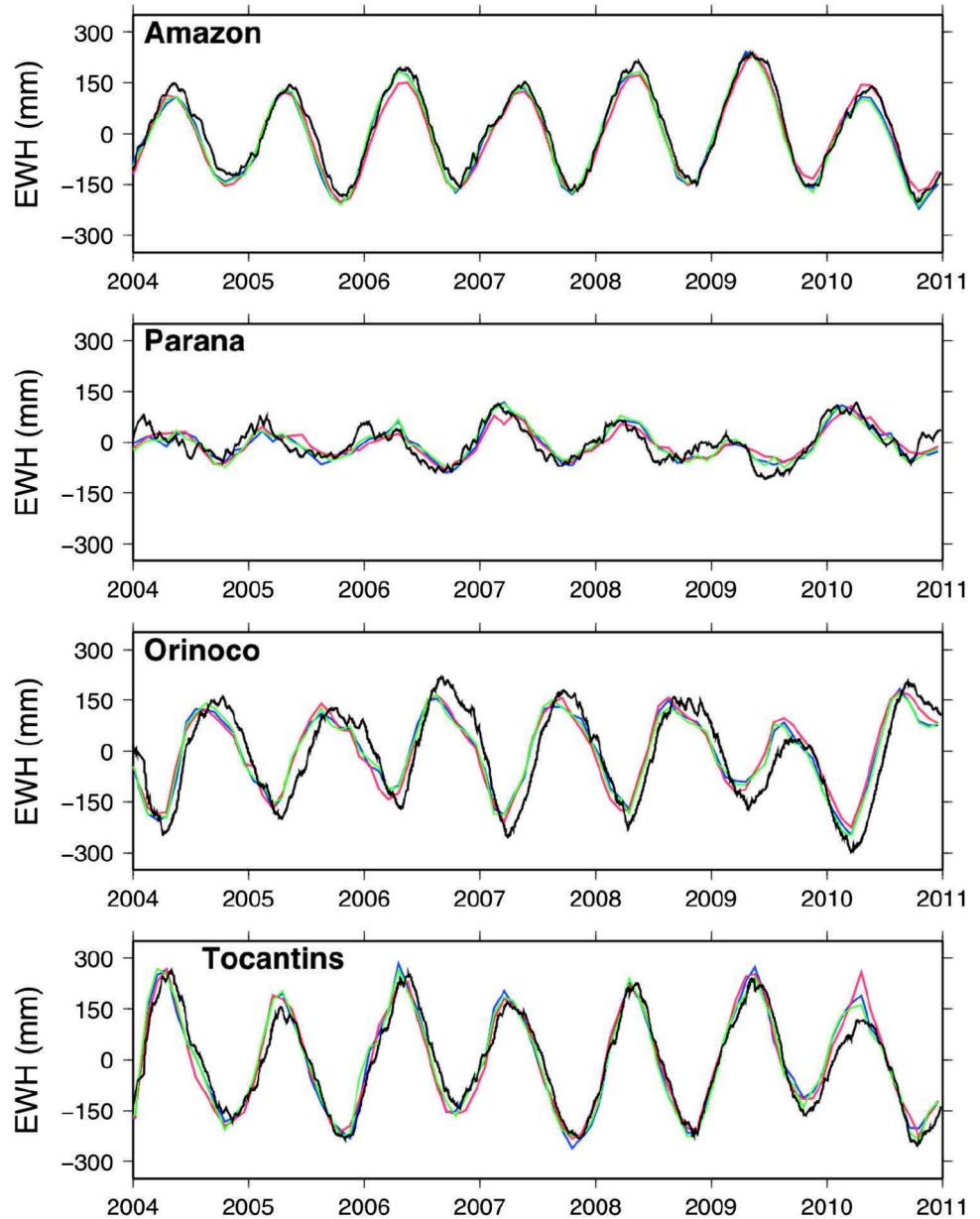
Fig. 9 Maps of the differences between successive Kalman filter solutions and the coverage of the corresponding GRACE satellite tracks used for the daily refreshing



Because of lower seasonal hydrological dynamics, there is less difference for the Parana basin (i.e., <27 mm of EWH RMS) and much difference for the Tocantins river (i.e., up to 98 mm of EWH RMS). Figure 10 shows a superposition of the monthly averages of the Kalman filter solutions and the global GRACE solutions. This proves that the Kalman filter method succeeds in recovering amplitudes and phases of TWS. Indeed, they are consistent to the ones of 10-day and monthly global GRACE solutions (for instance, see Frappart et al. 2013a, b), when they are averaged over large areas. In the comparison, RMS differences are more important for the two hydrological models. Figure 11 presents the TWS time series of the Kalman filter solutions and of WGHM and

GLDAS-NOAH outputs at daily timescale. Significant time shifts and large differences of amplitude can be observed between GRACE-based and simulated TWS, especially on the Amazon, Orinoco and Tocantins basins. In these basins, a large part of the hydrological signal comes from slow reservoirs as floodplains (see Frappart et al. 2012 in the case of the Amazon) and groundwater (see Chen et al. 2010 in the case of the La Plata basin, Gleeson et al. 2012 and Frappart et al. 2013b for their signatures in 10-day regional solutions) that are either not or not well modelled. As a consequence, significant differences and time-lags are likely to occur between model outputs and GRACE estimates (Alkama et al. 2010) (not shown here). Larger differences in amplitude and phase

Fig. 10 Time series of TWS for the largest drainage basins of South America obtained by averaging monthly CSR (*blue*), GFZ (*red*), JPL (*green*) and daily Kalman filter solutions (*black*)

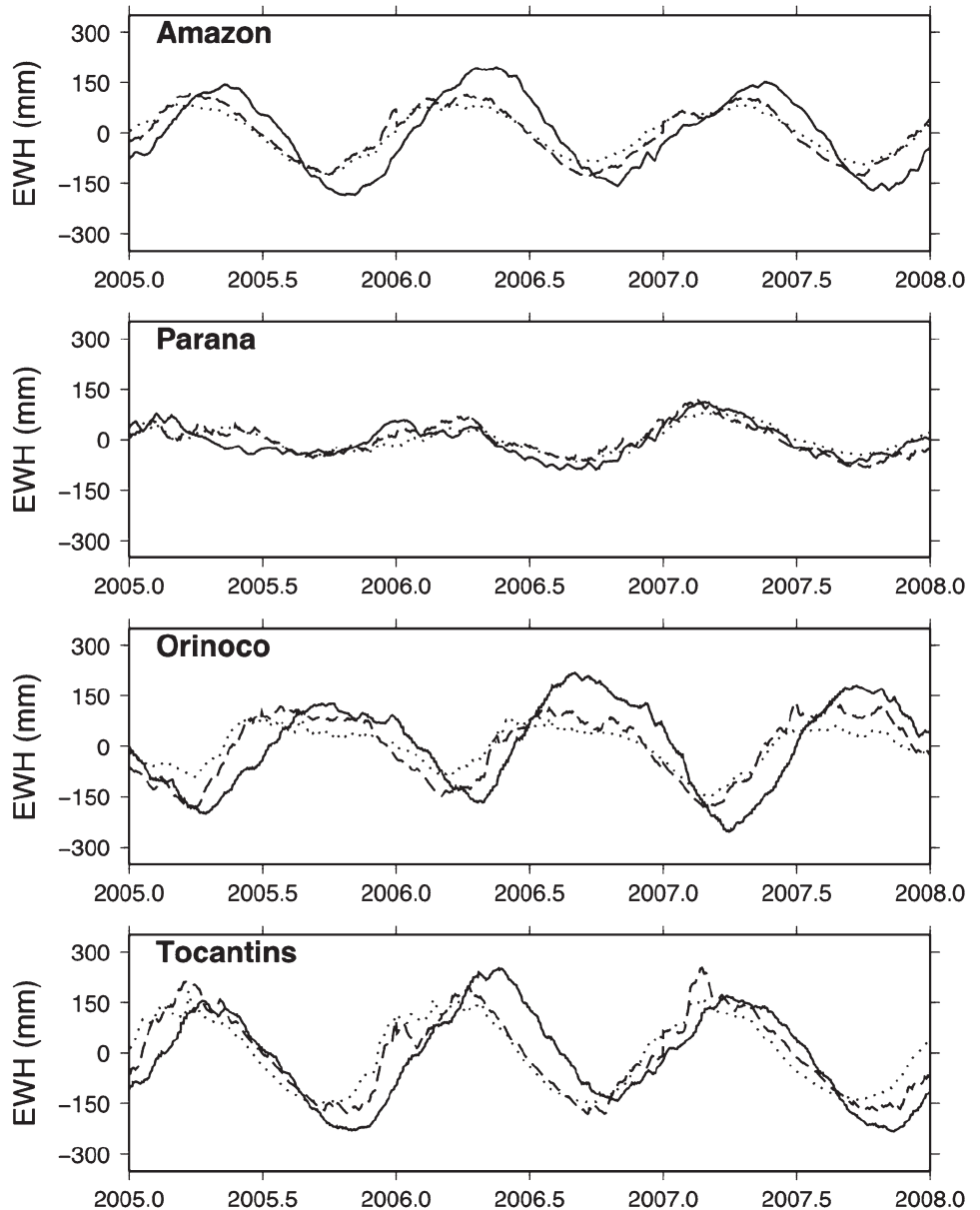


are observed with GLDAS outputs, as this model (NOAH), contrary to WGHM, does not consider neither surface storage (water stored in the rivers and the floodplains) nor the routing of the surface runoff into the river network which contributes to surface storage in the downstream grid points. The contribution of surface storage to TWS represents 40–50 % in the Amazon basin (see Han et al. 2009, 2010; Frappart et al. 2012; Paiva et al. 2013). So incorporation of total runoff outputs is likely to reconcile the GLDAS TWS variations to the GRACE-based amplitudes.

Comparisons were also achieved between 10-day and monthly GRACE and daily river discharges in the four largest drainage basins of South America (i.e., Amazon,

La Plata, Orinoco and Tocantins). They are presented in Fig. 12 and Table 2. An overall good agreement is found between GRACE-derived TWS and river discharge variations for all the basins (linear correlation greater than 70 % for the Kalman filter solutions for zero time-lag). Except in the case of Amazon basin where the values of correlation with discharge records reach 95 % for regional Kalman filter solutions, important linear correlations of 80–90 % are found at monthly and 10-day timescales. As TWS is the sum of the contributions all the hydrological reservoirs in a soil column (i.e., surface, soil moisture and groundwater storages), the rapid fluctuations of the discharge at daily timescale have a small impact on the TWS that contains slow

Fig. 11 Time series of TWS over the largest drainage basins of South America computed using WGHM model (*dashed line*) and GLDAS model (*dots*) outputs, as well as daily Kalman filter solutions (*solid line*)



changes in groundwater and other residual signals (e.g., from atmosphere and oceans mass corrections). This is why the correlations are slightly lower at daily timescale.

As they are sensitive to the input a priori error uncertainty parameters, the amplitudes of the regional Kalman filter solutions can be overestimated (e.g., if the RDP data are optimistically considered too accurate: $\sigma_d < 0.001 \text{ m}^2/\text{s}^2$) or underestimated (see Fig. 13 for comparison of the energy spectra of solutions from daily WGHM-simulated RDP data, in particular for the smoothing parameter $\sigma_d = 0.01 \text{ m}^2/\text{s}^2$). This sensitivity also explains important time shifts, as it is shown by previous results obtained with simulated RDP data (Figs. 5, 6), when the a priori error uncertainty of the observations is high and gives smooth estimates (i.e., $\sigma_d > 0.01 \text{ m}^2/\text{s}^2$).

Recovery from real GRACE-derived RDP confirms the low predicted seasonal amplitudes and time shifts with river discharge variations if σ_d is high (Fig. 12): the a priori error matrix R dominates the other terms of Eq. 3, so the Kalman gain K is small and minimizes the weights of the input RDP data. Consequently, the current solution is constructed very slowly versus time, is not refreshed efficiently by the daily RDP data, and thus existing water mass structures in this solution are more persistent, creating delay, in other words time shifting. As the satellite tracks bring local information (Fig. 9), this impossibility of catching any information versus time has an important impact on spatial averaging over relatively small Orinoco and Tocantins River basins (see Fig. 10).

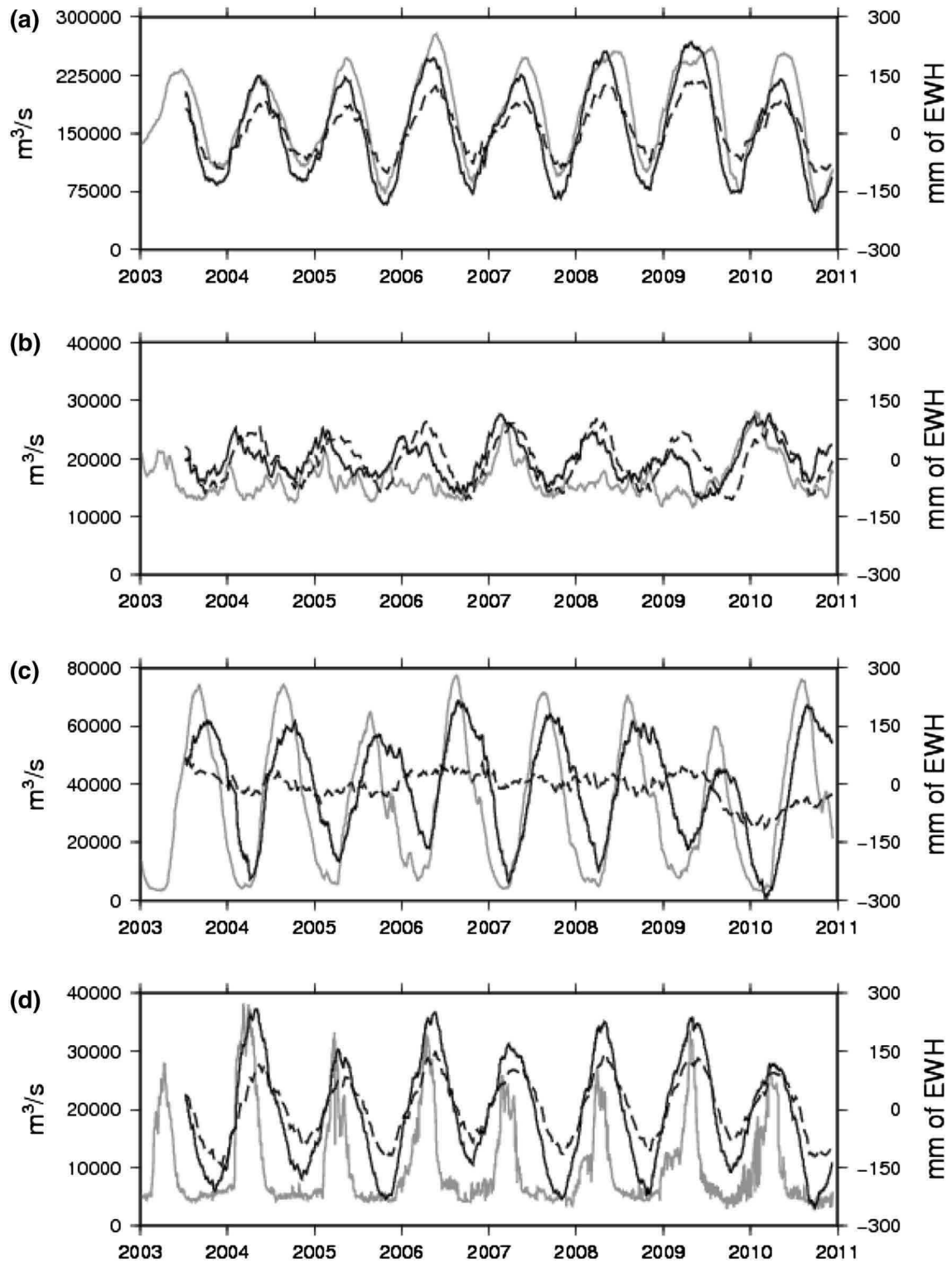
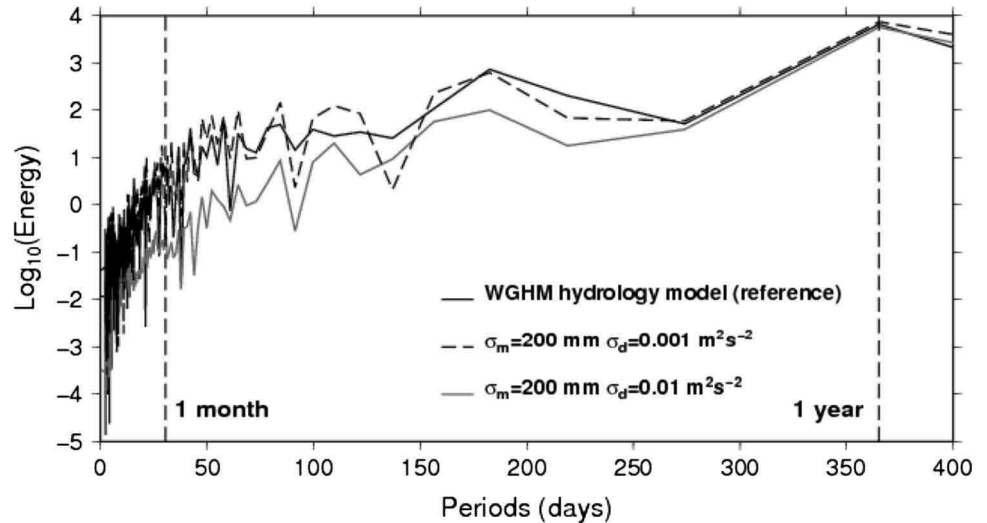


Fig. 12 River discharge variations (grey) measured at different in situ stations: **a** Obidos (Amazon), **b** Chapeton (Paraná), **c** Ciudad Bolívar (Orinoco) and **d** Tucuruí (Tocantins), as well as time series of daily Kalman filter solutions: $\sigma_d = 0.1 \text{ m}^2/\text{s}^2$ (dashed line) and $\sigma_d = 0.01 \text{ m}^2/\text{s}^2$ (solid line) when $\sigma_m = 200 \text{ mm}$

Fig. 13 Energy spectra of the time series (2004–2011) of the regional day-step solutions for different a priori uncertainty parameters and of reference hydrology model for the 2-degree tile centred over the city of Manaus



6 Discussion

While the long periods of water mass variations (>1 month) can be well recovered (see the previous section), we propose in the following discussion to perform numerical tests for exploring the ability of our sequential integration of daily WGHM-simulated RDP in recovering sub-monthly and geographically localized water mass variations. For this purpose, we model the spatio-temporal characteristics of a water mass anomaly as a time and space Gaussian-type varying function of length of a few days and placed at the centre of a 2-by-2 degree grid. Then, we simulate RDP using Eq. 1 from this error-free water mass variation model but with no use of propagated errors since no error information is really available. The challenge is to detect both the geographical location and the magnitude of such a time and space located anomaly by tuning input parameters, mainly the satellite track density (i.e., number of days of observation) and the a priori uncertainties. Once a set of these parameters are chosen and the error covariance matrices constructed, the process of integration is run (Eqs. 2–7). The errors of recovery are estimated at each step of integration as the differences between the current Kalman-cumulated solutions and the daily reference model maps. Note that the solutions may be biased towards the reference dataset. The sensitiveness of the input a priori uncertainty parameters and the impact of critical satellite track coverage are examined through different values of these a priori parameters. This trial-and-error approach helps us finding the best combination of parameters for the detection of the modelled water mass event, if the minimum RMS value of the recovery error is used as a criterion.

6.1 Searching for the best a priori parameters for inverting error-free RDP data

Tests on Kalman-type filtering of simulated error-free GRACE data show a quite rapid convergence from zero first guesses of surface mass density (i.e., an exact solution is found after a few days of data integration, as presented in Fig. 1 for South America). However, inversion of real along-track potential difference data remains difficult because of the presence of high-frequency noise and correcting model errors, effects of which have to be canceled in the inversion, or at least minimized. Thus, even if the convergence is fast to recover a 30-day constant map of equivalent-water heights, suitable a priori input values have to be chosen to build the Kalman gain (i.e., Eq. 3). The choice of parameters for constructing the Kalman gain is necessary to obtain the lower errors and to stabilize the final estimate to cope with noise and outliers in the real GRACE-derived RDP. Inversion of noise-free model-simulated RDP confirms that errors of recovery over South America are less than 1 mm of EWH RMS when using suitable a priori error parameters. In the presence of noise, these aliasing errors represent a few mm of EWH, as already shown by Encarnação et al. (2009). Considering large a priori uncertainties on potential observations (e.g., $\sigma_d > 10^{-2} \text{ m}^2/\text{s}^2$) leads to recovery errors greater than 2 mm RMS in terms of equivalent-water height, as smoothing is important. Besides, considering artificially very accurate observations (e.g., $\sigma_d < 10^{-4} \text{ m}^2/\text{s}^2$) makes the Kalman gain, and thus the cumulated solution at step number k very unstable. The problem of instability is also due to the sparse sampling of the GRACE satellite tracks whose spatial coverage is not sufficient to access cumulated solutions with a daily

Fig. 14 Maximum error of recovery versus a priori parameter σ_m after 30 days of Kalman filter integration in the case of a simulated 200-mm amplitude water mass anomaly centred at time $k = 15$, and assuming an a priori error uncertainty of the observations of $0.001 \text{ m}^2/\text{s}^2$

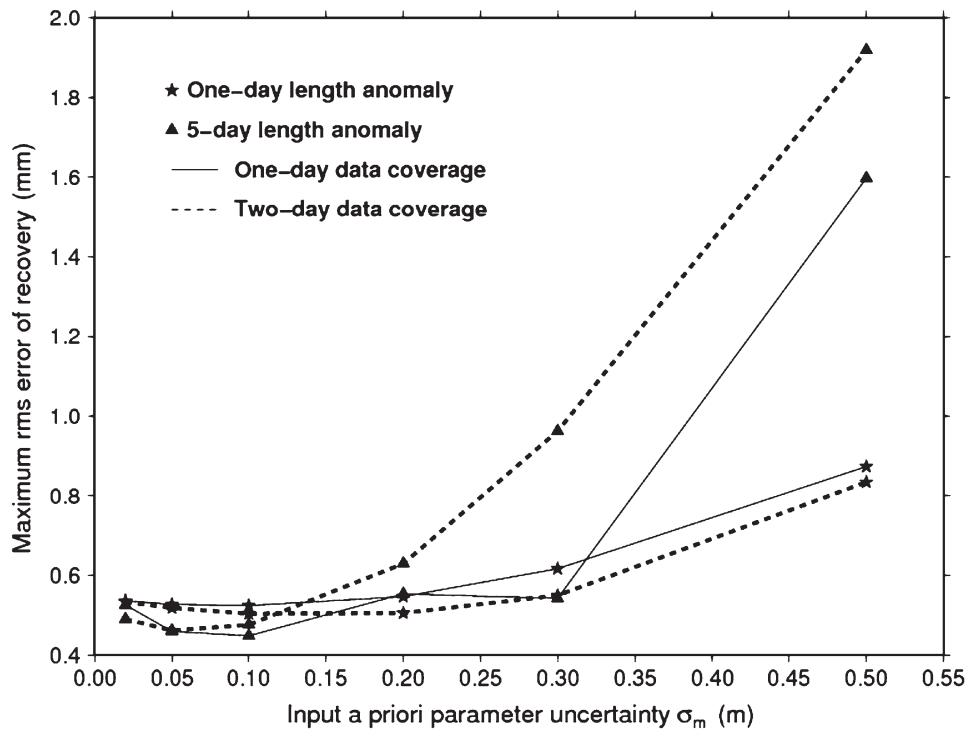
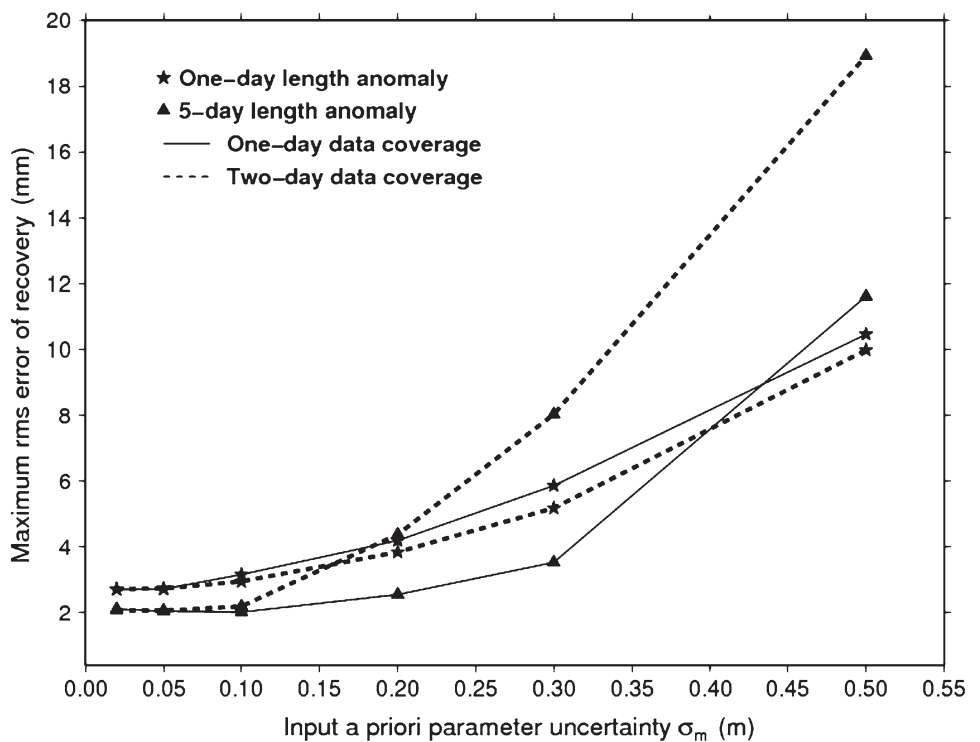


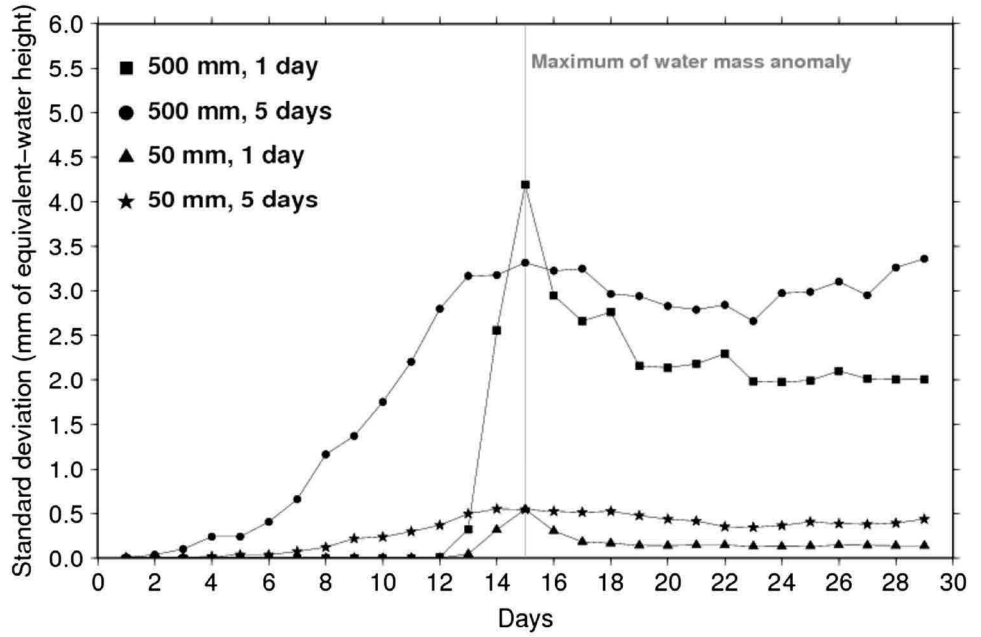
Fig. 15 Maximum error of recovery versus a priori parameter σ_m after 30 days of Kalman filter integration in the case of a simulated 1,200-mm amplitude water mass anomaly centred at time $k = 15$, and assuming an a priori uncertainty of the observations of $0.001 \text{ m}^2/\text{s}^2$



resolution. For these limitations of not using accurate RDP data, we deemed that using $\sigma_d = 10^{-2} - 10^{-3} \text{ m}^2/\text{s}^2$, which corresponds to the level of noise of the GRACE-based potential differences, represents a good compromise (see Ramillien et al. 2011, 2012).

Several simulations have revealed that the error of recovery increases with a priori model uncertainty σ_m as well as the duration of the water mass anomaly (Figs. 14, 15). This recovery error is ten times more important for water mass amplitude of 1,200 mm than considering a 200-mm water

Fig. 16 Geographical variability of the error of recovery versus iteration number to the final estimate. Total integration period is 30 days. The true water mass solution is Gaussian and centred at $t = 15$ days, with amplitudes of 50 mm (duration: *triangles*: 1 day, *stars*: 5 days) and 500 mm (durations: *squares*: 1 day, *circles*: 5 days)



mass anomaly. It reaches low values when a priori model uncertainty σ_m ranges from 10 to 50 mm. In this domain of small model uncertainty, the Kalman filter strategy provides less error than least-squares integration of one day of sparse RDP data, since its advantage is, by construction, to inherit (or cumulate) information from the previous stage $k - 1$ to build an averaged solution at the following stage k .

Obviously, the error of recovery in our final cumulated solution is lower when the data coverage at each stage is twice, indicating that the Kalman filtering is well adapted to estimate time-constant water mass map by progressive integration of RDP. Unfortunately, it is a particular case as hydrological signals surely vary in time from a day to another. This suggests that these unavoidable variations of water mass during the total period of integration (e.g., ~ 30 days) create errors of time aliasing by accumulation of rapid successive hydrological events. While considering constant monthly intervals produces no noticeable aliasing error for averages over large surfaces, quantification of time aliasing errors proposed by Encarnaçao et al. (2009) shows that GRACE satellite orbit configuration permits an optimal detection of hydrological events of at least 11–15 days, like in the case of the 3,300- to 4,400-km-wide Zambezi river basin.

6.2 Aliasing effects polluting the final estimate

According to the previous results, even if GRACE observations contain time-varying hydrological signals, the proposed method provides estimations of water mass anomaly that are considered constant over 10–30 days. Hence, the main source of error, excepting the presence of spurious noise that creates

numerical instabilities in the inversion, is the aliasing of fast-moving water mass events at periods shorter than the total integration period.

As the method cumulates all the hydrological signals, including the very short-term ones that can occur during the integration process, the final average corresponds to a mixing of events. We consider a synthetic Gaussian water mass anomaly located at the center of the region with varying amplitude from 50 to 500 mm of EWH, radius from 200 to 1200 km, and duration lasting from 1 to 5 days. Along-track RDP have been simulated from this reference model of water mass anomaly using Eq. 1, and used as input to build iteratively a Kalman filter solution. The error of recovery is then evaluated as the difference between the computed Kalman-based and reference water mass anomalies. These errors versus the number of days of integration are represented in Fig. 16. Persistent errors clearly appear after the water mass anomaly maximum occurring at day #15, and we note that they are not attenuated afterwards, even in the case of a sudden event. This error of aliasing increases drastically with amplitude of the water mass anomaly, by a factor 9 from 50 to 500 mm. In the particular case of water mass anomalies centred over the integration period, the final aliasing error should tend to zero after 30 days of integration. As it is presently built, the scheme keeps any water mass change “in memory” up to the final water mass estimate which is equivalent to an average of cumulated signals over the total period of integration. Due to the poor daily distribution of the GRACE satellite tracks, it is clear that the process cannot update the solution efficiently enough. Fortunately, in the case of long period of integration, high-frequency and

Fig. 17 Same as Fig. 16, but the total integration period is 1 day, instead of 30 days, to gain in temporal resolution and avoid persistent signals

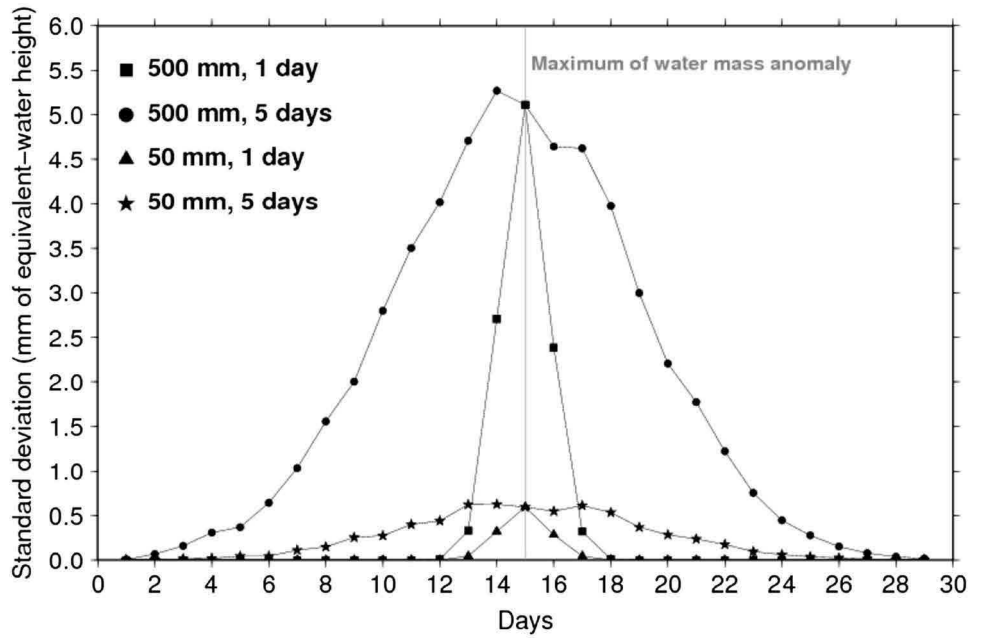
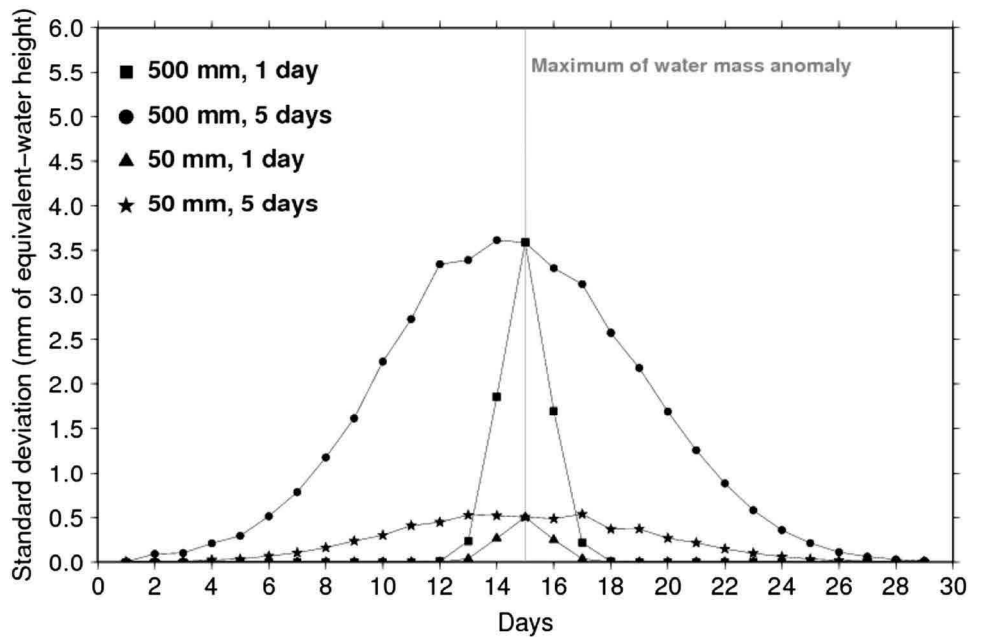


Fig. 18 Same as Fig. 17 (i.e., integration of one day data), but with a twice-denser coverage (i.e., 2-day steps) of the GRACE satellite tracks at each iteration



zero-mean noise should cancel out, and thus have a reduced impact on the final cumulated solution.

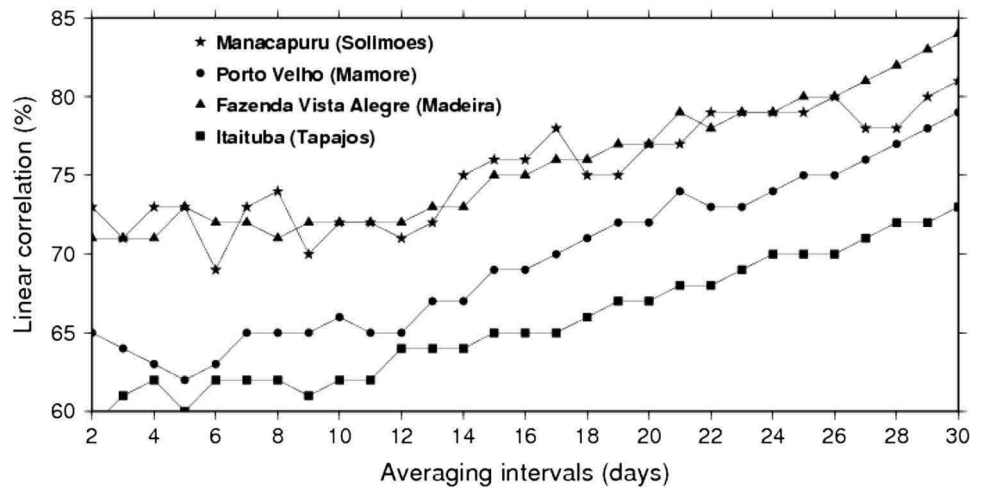
6.3 Reduction of aliasing error

Without including time correlations (or constraints) through hydrology model outputs, decreasing the period of integration is the only way of gaining in temporal resolution. As illustrated in Fig. 17, in the case of integration of daily RDP, the persistency of aliasing error is reduced after the maximum of anomaly is reached at $k = 15$. However, when the integration is made over 30 days (see Fig. 16), the amplitude of error

is slightly less than independent daily integrations, thanks to heritage of useful information from the previous iteration to the next one. Obviously, coverage of the daily GRACE tracks made artificially denser would make the aliasing error decrease significantly, as presented in Fig. 18.

According to the uncertainty principle, it is not possible to benefit from temporal and spatial resolutions at the same time, as previously mentioned by [Freedan and Schreiner \(2009\)](#), or equivalently, any representation cannot provide a precise localization of a particular event in both space and time. This is well illustrated by the previous results of [Kurtenbach et al. \(2009, 2012\)](#) who have used a similar Kalman filter

Fig. 19 Linear correlation between sub-monthly time averages of the regional Kalman filter solutions and the river discharge variations measured at four in situ stations versus the time interval used for averaging these two datasets



approach to estimate the dominant trend, annual and semi-annual cycles of the low-degree smooth spherical harmonics of the geopotential from daily GRACE data, with no access to the shorter time periods of the water mass variations. Comparing sub-monthly variations of Kalman filter solutions and in situ river discharge in terms of residuals (i.e., difference between average of TWS and discharge over Δt varying from 1 to 30 days and monthly respective quantities) reveals that their linear correlation increases with the interval of averaging from 10 to 15 days at a rate of 0.5–0.7 % per day (Fig. 19). This correlation remains greater than 65–70 % for averaging intervals greater than 10 days. Below this interval of time, the correlation rate flattens, suggesting that the regional Kalman filter solutions are not refreshed enough by the sparse coverage of the daily GRACE tracks to be compared to the local discharge measurements.

7 Conclusion

A new sequential approach for estimating regional 2-by-2 degree variations of water mass has been developed by integrating successive days of GRACE-type potential difference data. This method is based on cumulating satellite information to build progressively stable regional time averages over large continental areas. Recovering piece-wise time-constant maps of water mass is probably the most adapted case for the proposed method, as the permanent hydrological structures are reinforced during the iterative Kalman filter estimation. This sequential estimation was applied to estimate time-varying regional solutions over South America by daily updates using real GRACE potential differences. Series of regional cumulated solutions were derived at daily intervals by refreshing using real daily (and thus sparse) GRACE RDP, and testing ranges of sensitive a priori error uncertainties on the parameters and observations, before being analysed and confronted to other GRACE-based datasets.

These long time series of daily-step Kalman filter solutions have been validated by comparing them to GRACE-based and independent datasets (i.e., model outputs and in situ discharge observations). The seasonal amplitudes of TWS and their inter-annual modulations are well restored on the daily sampling solutions compared with regional/global GRACE solutions and model outputs. High correlations (>0.7) were found between daily TWS and in situ discharge data in the four largest drainage basins of South America, but were generally lower than these obtained at 10-day or monthly averages.

While long periods of the hydrological variations are well recovered by the sequential accumulation (e.g., by choosing suitable high values for σ_m to allow strong seasonal signals to be easily retrieved), the construction of sub-monthly hydrological events remains problematic because of the poor per-day coverage of the GRACE satellite tracks. According to the simulations we made, the refreshing process is efficient for accumulation of RDP information of 10–15 days, but fails to reach the daily resolution of the Kalman filter solutions and even a resolution of a few days. The detection of sub-monthly events can be slightly improved by tuning a priori error uncertainty parameters; however, the spatial distribution of the satellite tracks is the most limiting factor.

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