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# 1 Experimental and theoretical study of bumped characteristics 2 obtained with cylindrical Langmuir probe in magnetized Helium 3 plasma

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Cylindrical Langmuir probe measurements in a Helium plasma were performed and analysed in the presence of a magnetic field. The plasma is generated in the ALINE device, a cylindrical vessel 1 m long and 30 cm in diameter using a direct coupled RF antenna ( $v_{\text{RF}} = 25$  MHz). The density and temperature are of the order of  $10^{16} \text{ m}^{-3}$  and 1.5 eV, respectively, for 1.2 Pa Helium pressure and 200 W RF power. The axial magnetic field can be set from 0 up to 0.1 T, and the plasma diagnostic is a RF compensated Langmuir probe, which can be tilted with respect to the magnetic field lines. In the presence of a magnetic field,  $I(V)$  characteristics look like asymmetrical double probe ones (tanh-shape), which is due to the trapping of charged particles inside a flux tube connected to the probe on one side and to the wall on the other side. At low tilting angle, high magnetic field amplitude, power magnitude and low He pressure, which are the parameters scanned in our study, a bump can appear on the  $I(V)$  in the plasma potential range. We then compare different models for deducing plasma parameters from such unusual bumped curves. Finally, using a fluid model, the bump rising on the characteristics can be explained, assuming a density depletion in the flux tube, and emphasizing the role of the perpendicular transport of ions.

## 9 I. INTRODUCTION

10 Cylindrical Langmuir probes are one of the sim-  
11 plest device to investigate plasma properties as they  
12 consist of a small metallic wire of length  $L_p$  and  
13 radius  $r_p$ , usually made of tungsten, immersed into  
14 the plasma, and submitted to a ramp of voltage. The  
15 collected current by the tip vs. the applied voltage  
16 yields an  $I(V)$  probe characteristics, from which  
17 electron density  $n_e$ , ion density  $n_i$  and temperature  
18  $T_e$  can be derived.

19 An  $I(V)$  curve can be divided in three parts :  
20 the “ion saturation current” part, the “electron sat-  
21 uration current” and the exponential part<sup>1,2</sup>. For  
22 strongly negative potentials  $V$  applied to the probe  
23 (with respect to plasma potential  $\phi_p$ ) electrons are  
24 repelled and ions accelerated towards the probe, the  
25 collected current being the ion saturation current  $I_i$ .  
26 In the opposite case,  $V \gg \phi_p$ , only electrons are  
27 collected and the measured current at the probe is  
28 the electron saturation one  $I_e$ . These regions are so  
29 called “saturation current” because their mean ve-  
30 locities saturate at  $\langle v \rangle_{\text{max}}$ , deduced from their veloc-  
31 ity distribution. Actually even in the saturation part,  
32  $I$  keeps on increasing with  $V$ , because the sheath  
33 surrounding the probe is growing with the applied  
34 potential. Thus, the collecting surface for the accel-  
35 erated species in the sheath is not the probe surface,  
36 but the sheath one. Within the transition region,  
37 electrons are repelled according to the Boltzmann  
38 factor and  $n_e e^{-E/k_B T_e}$ , with  $E = -e(V - \phi_p)$ . An-  
39 other important point of the  $I(V)$  characteristic is  
40 the floating potential,  $\phi_{\text{fl}}$ , defined as the probe po-

41 tential for which the same amount of ion and elec-  
42 tron are collected, *i.e.* for  $I = 0$ . Note that the con-  
43 vention is to count ion current as negative, and elec-  
44 tron current as positive on  $I(V)$  plots.

45 Determining the plasma parameters on differ-  
46 ent regions listed above requires to use the most  
47 appropriate theory for each species. Mott-Smith  
48 and Langmuir<sup>3</sup> proposed the first model to extract  
49 temperature and density from characteristics using  
50 the OML theory (Orbital Motion Limited). This  
51 theory exploits mainly the ion part of the charac-  
52 teristics and was developed with the assumption  
53 of large sheaths ( $r_p/\lambda_D \ll 1$ , for  $\lambda_D$  the Debye  
54 length of the repelled species), large ion mean-free-  
55 path ( $\lambda_{i,\text{mfp}}/L_p \ll 1$ ) and cold ions ( $T_i/T_e \rightarrow 0$ ).  
56 Allen and Bernstein<sup>4-6</sup> improved this theory, solv-  
57 ing the Poisson equation within the sheath, which  
58 was omitted in the OML theory. But it can lead to  
59 an overestimation of the ion density by a factor of  
60 ten<sup>7</sup>. Laframboise extended the model assuming a  
61 velocity distribution function for ions<sup>8</sup>, but this so-  
62 phisticated approach does not improve the fits of the  
63 experimental ion current with respect to the ABR  
64 (Allen Boyd Reynolds) model<sup>5</sup>.

65 The presence of a magnetic field changes  
66 strongly the way particles are collected on the  
67 probe: the motion of charged particles can be di-  
68 vided into a longitudinal ( $\parallel \mathbf{B}$ ) and a perpendic-  
69 ular ( $\perp \mathbf{B}$ ) components, with their own tempera-  
70 ture. In such magnetized conditions, OML the-  
71 ory still holds<sup>9-11</sup> for ions, but the electron part is  
72 hardly interpretable<sup>12</sup> due to the distortion of the  
73  $I(V)$  curve, leading to an uncertainty on the deter-

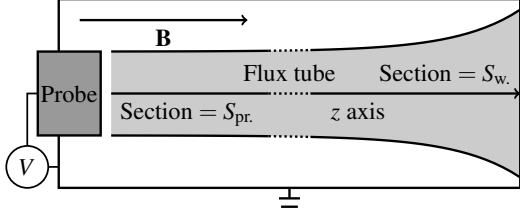


FIG. 1. Illustration of the double probe model : the widening of the flux tube is here to model the fact that at the end of the vessel magnetic field lines drive away each other.

74 mination of  $\phi_p$  and, thus, to a wrong  $T_e$  and  $n_e$ . Sev-  
 75 eral authors<sup>11,13</sup> emphasized the distortion of the  
 76 characteristics in the presence of  $\mathbf{B}$ , showing that  
 77  $I_e$  is much lower compared to the unmagnetized  
 78 case, because electrons are stuck along magnetic  
 79 field lines, with a low level of perpendicular trans-  
 80 port due to collisions<sup>14</sup> and drain diffusion<sup>11</sup> for in-  
 81 stance.

82 In several papers it was also reported that, in  
 83 some cases, a bump on the characteristics can ex-  
 84 ist between the exponential part and the electron  
 85 saturation part<sup>15-18</sup>. It was assumed that the bump  
 86 was caused by a density depletion of the flux tube  
 87 during the probing. Dote developed an OML-like  
 88 model to explain the presence of the bump<sup>19,20</sup> and  
 89 suggested the plasma potential to be the bump posi-  
 90 tion; his model however does not match quite well  
 91 with experimental results.

92 The shape of a  $I(V)$  characteristic in a mag-  
 93 netized plasma can be approached, excluding the  
 94 eventual bump, by a double probe model: the per-  
 95 fectly confined flux tube (which is  $\parallel \mathbf{B}$ ) is connected  
 96 to one hand to the probe, and on the other hand, to  
 97 the wall of the reactor as shown in Fig. 1.

98 The collected electron current is mainly paral-  
 99 lel to  $\mathbf{B}$  while the ion current is perpendicular to  
 100  $\mathbf{B}$  so that the lateral surface of the flux tube plays  
 101 the role of the wall in a classic unmagnetized dis-  
 102 charge. The magnetized double probe model can  
 103 then be seen as a classic asymmetric double probe  
 104 model without magnetic field<sup>21</sup>. The effect of these  
 105 ionic perpendicular currents both in DC<sup>22,23</sup> and in  
 106 RF<sup>24,25</sup> have already been studied for planar probes.  
 107 It was shown that the shape of the  $I(V)$  curve was  
 108 changed by feeding or pumping the flux tube and  
 109 that I-Vs are really sensitive to the  $r_p/r_L$  ratio.

110 Here simple asymmetric model is 1D in the  $z$  di-  
 111 rection (see sketch fig.1), the probe is located at  
 112  $z_{pr} = 0$  and the wall at  $z_w = L_t$ , the length of the  
 113 flux tube is then  $L_t$  and  $\mathbf{B} = B \mathbf{e}_z$ . The probe po-  
 114 tential is at  $V$ , the space potential is  $\phi_t$  and the wall  
 115 is grounded. The section of the tube on the wall  
 116 side is  $S_w$ , and the section at the probe is  $S_{pr}$  with

117  $S_{pr} \leq S_w$ . We assume constant density in the tube,  
 118  $n_t$ , and no loss in the perpendicular direction. Thus,  
 119 the stationary ( $\partial_t n = 0$ ) continuity equation writes :

$$\nabla \cdot \mathbf{J}_{\text{Tot.}} = 0 \quad \text{where } \mathbf{J}_{\text{Tot.}} = \mathbf{J}_e + \mathbf{J}_i \quad (1)$$

120 For homogeneous current density across both ends,  
 121 using Gauss's theorem by integrating eq.(1) over  
 122 the whole flux tube gives :

$$J_{\text{Tot.}}(z=0) \times S_{pr} + J_{\text{Tot.}}(z=L_t) \times S_w = 0 \quad (2)$$

Ion current density is the Bohm flux,

$$J_i = 0.61 \times en_t c_s \quad \text{where } c_s = \sqrt{\frac{k_B T_e}{m_i}},$$

and for electron it is given the Boltzmann equilib-  
 rium with the local potential,

$$J_e = -\frac{1}{4} en_t \langle v_e \rangle \times \exp \left[ e \frac{\phi(z) - \phi_t}{k_B T_e} \right]$$

$$\text{where } \langle v_e \rangle = \sqrt{\frac{8k_B T_e}{\pi m_e}}.$$

123 Introducing the electron saturation current as  
 124  $J_{e,\text{sat.}} = en_t \langle v_e \rangle / 4$  and the floating potential,  $\phi_{fl.} =$   
 125  $k_B T_e \ln(J_i / J_{e,\text{sat.}}) / e$ , eq.(2) becomes :

$$\phi_t = \frac{k_B T_e}{e} \ln \left[ \frac{\Sigma + \exp(eV/k_B T_e)}{\Sigma + 1} \right] - \phi_{fl.}, \quad (3)$$

126 where  $\Sigma = S_w / S_{pr}$ . Finally, the collected current on  
 127 the probe is

$$J_{pr}(V) = J_{e,\text{sat.}} \exp \left[ e \frac{V - \phi_t(V)}{k_B T_e} \right] - J_i. \quad (4)$$

128 Thus, using eq.(3) in eq.(4) one will get :

$$J_{pr}(V) = J_i \times \frac{\exp(eV/k_B T_e) - 1}{1 + \frac{1}{\Sigma} \exp(eV/k_B T_e)} \quad (5)$$

129 The asymmetric double probe  $I(V)$  characteristics  
 130 from eq.(5) is plotted in fig.2.

131 In this paper, we investigate the general be-  
 132 haviour of "bumped characteristics" with respect  
 133 to several parameters, such as the amplitude of the  
 134 magnetic field, the gas pressure or the RF power  
 135 input. We also propose a new explanation of  
 136 the bump, with the aim of a better understanding  
 137 of Langmuir probe measurements in magnetized  
 138 plasma. In the first part sect.II, the experimental  
 139 set-up and the plasma parameters (mean free paths,  
 140 Larmor radii, etc.) are detailed. Then the main ex-  
 141 perimental results are shown in section III, where  
 142 the behaviour of the bumps was studied with respect  
 143 to the amplitude of the magnetic field in sect.III A,  
 144 the angle  $\vartheta$  between the probe and  $\mathbf{B}$  in sect.III B,  
 145 the RF-power input in sect.III C, the probe position

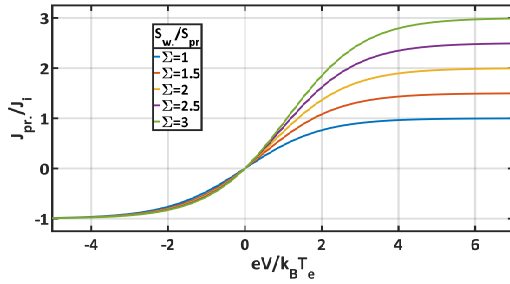


FIG. 2. Theoretical and normalized double probe characteristics for several values of  $\Sigma$ . For  $\Sigma \neq 1$  the characteristics are called “asymmetric”, and for  $\Sigma \rightarrow \infty$  they are very similar to classical Langmuir characteristics ( $S_w$  is the surface of the whole vessel in that case).

146 with respect to the RF-antenna in sect.III D and fi-  
 147 nally the He pressure in sect.III E. In the follow-  
 148 ing, sect.III, a method is proposed to determine the  
 149 plasma temperature and density with conventional  
 150 methods (when no magnetic field is present). Fi-  
 151 nally, the origin of the bump characteristics is ex-  
 152 plained thanks to a fluid model in the last section.

## 153 II. EXPERIMENTAL SETUP

154 Experiments were performed in the ALINE<sup>26,27</sup>  
 155 (A LINEar plasma device) reactor (see figure 3 and  
 156 4). The cylindrical chamber is 1 m long and 30 cm  
 157 diameter. The typical discharges presented here are  
 158 generated by a RF-antenna at  $\nu_{RF} = 25$  MHz (but  
 159 the amplifier frequency can be tuned from 10kHz  
 160 to 250 MHz), and the RF-power is in the range 20  
 161 - 200 W (though 0 to 600 W is achievable). The  
 162 amplifier is directly connected to the antenna (direct  
 163 coupling, so the average potential on the antenna is  
 164 0 V). The cathode is at the center of the vessel has  
 165 a radius of 4 cm and is 1 cm thick.

166 Six circular coils generate an axial magnetic field  
 167 from 0 to about 100 mT (the current in the coils is  
 168 in the range 0–200 A). Helium gas was used for  
 169 all discharges with a pressure in the range between  
 170 1.2 and 40 Pa for this study, which allows the study  
 171 from collisionless to collisional regimes.

172 The cylindrical Langmuir probe Tungsten tip  
 173 used in measurements has a length  $L_p$  of 1 cm and a  
 174 radius  $r_p$  of 75 microns. To enable measurements in  
 175 a RF plasma, the probe is RF-compensated<sup>7,28</sup>. For  
 176 each  $I(V)$  characteristics, a voltage ramp from  $-70$   
 177 to 70 V is swept 20 times at a frequency of the order  
 178 of 65 kHz. Hence, the measurement frequency  
 179 is much slower than RF-oscillations and all plasma  
 180 frequencies ( $\omega_e$  and  $\omega_p$ ), and thus, can be seen as  
 181 “stationary” with respect to the plasma dynamics.

182 The position of the probe tip is given with re-  
 183 spect to the middle of the antenna ( $y = 0$  and  $z = 0$ ).

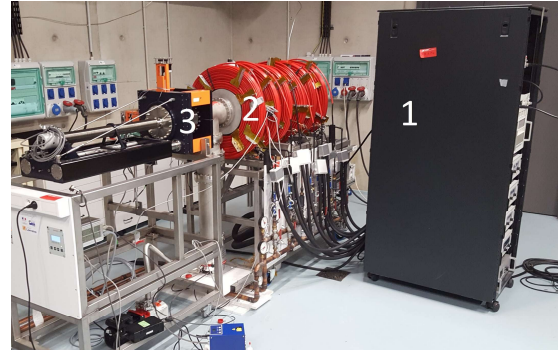


FIG. 3. Photograph of the ALINE plasma device. The cylindrical vessel (2) is 1m long and 30 cm diameter. Six coils (in red) are placed equidistantly along the axis, around the chamber to generate a quasi-homogeneous and uniaxial magnetic field along the axis of the cylinder. The power supplies for the coils and the RF antenna are placed in the rack (1). The antenna is in the middle of the vessel. The arm (3) holding the Hidden Langmuir probe along the vessel’s axis was developed by Cryoscan and is able to perform 3D translations (along the axis, up/down and left/right). Note that the arm is always parallel to the axis of the cylinder.

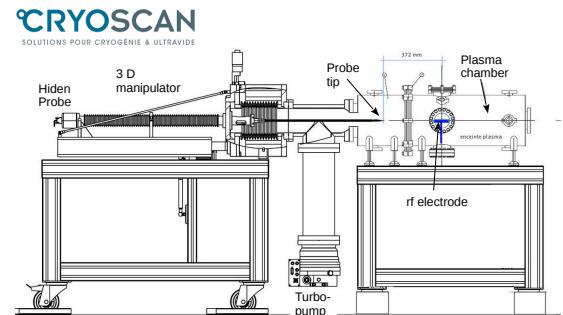


FIG. 4. Schematic representation of the plasma device designed by Cryoscan. The gas inlet is on the top-right end of the device (on the opposite of the pump).

184 All measurements were performed at  $z = -60$  mm  
 185 along the axis of the cylindrical chamber and  $y = 40$   
 186 mm above the antenna. The arm holding the probe  
 187 is parallel to the axis of the cylindrical vessel, and  
 188 only the tip is tilted  $\vartheta$  with respect to the magnetic  
 189 field lines (see fig.5).  $\vartheta \in [0, 6, 12, 18, 40, 94]^\circ$   
 190 angles were used for the study.

191 Moreover, the arm (see (3) in figure 3) is able  
 192 to move the probe tip inside a volume (see the red  
 193 dashed box in figure 6) to get three-dimensional  
 194 measurements of plasma parameters. Solving Biot-  
 195 Savart law in the whole vessel gives the magnetic  
 196 field topology. Figure 6 shows the result of the  
 197 computation. Let  $\langle B \rangle_{\text{meas.}}$  be the averaged modulus  
 198 inside the workable volume : in this paper we as-  
 199 sume uniaxial (along  $z$ , the axis of the reactor) and



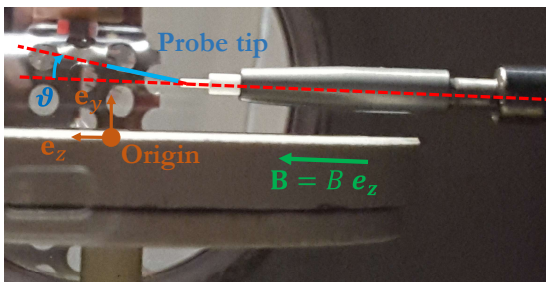


FIG. 5. Tilted cylindrical Langmuir probe with an angle  $\vartheta = 12^\circ$  with respect to  $\mathbf{B}$  (which is assumed homogeneous and constant in the whole probed volume,  $\mathbf{B} = B\mathbf{e}_z$ ). The position of the probe is  $z = 0$  and  $y = 5$  mm on this photograph. The value of the angle with respect to the antenna was measured thanks to the open source GeoGebra software.

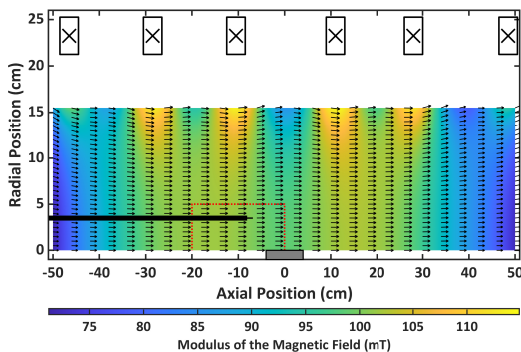


FIG. 6. Magnetic topology in the ALINE plasma device. The gray rectangle at the bottom represents the RF cathode, the long black rectangle and the narrow line at its end at  $r = 4$  cm represents the probe and its arm at probing position  $(x, y, z) = (0, 40, -60)$  mm. The red dashed box delimits the workable volume. White arrows represent the local magnetic field vectors.

constant magnetic field (the deviation from the averaged value being less than 3% in the probed volume). In the following  $B = \|\mathbf{B}\| = \langle B \rangle_{\text{meas.}}$ , and  $\mathbf{B} = B\mathbf{e}_z$ .

In low pressure conditions,  $p = 1.2$  Pa, the plasma can be considered as collisionless. Indeed after the values listed in table I, electron mean free path is greater than the probe dimensions<sup>6</sup>, *i.e.*  $\lambda_{e,\text{mfp}} \gg r_p$  and  $L_p$ . Ions can be considered as unmagnetized for the probe since  $\rho_{ci} \gg r_p$ . Note that an electron needs a parallel velocity over  $L_p \omega_{ce}/2\pi \approx 2.8 \times 10^7$  m/s to overfly the probe without completing a cyclotron period: at this velocity the  $f_e(\mathbf{v}) \sim 0$ , which means that almost all electrons complete an entire turn over the length of the probe. The electron collection can thus be seen as the intersection of the “cyclotron disk” ( $\pi\rho_{ce}^2$ ) with the probe for parallel inclination in collisionless regimes.

TABLE I. Plasma parameters for  $\|\mathbf{B}\| = 100$  mT and  $p = 1.2$  Pa. Note that probe dimensions are  $r_p = 75$   $\mu\text{m}$  and  $L_p = 1$  cm,  $\rho_c$  is the Larmor radius,  $\lambda_{\text{mfp}}$  is the mean-free-path for charged particle/neutral collisions,  $\nu_c$  the cyclotron frequency ( $\omega_c/2\pi$ ),  $\nu_p$  the plasma frequency and  $\nu_{\text{col}}^N$  the charged particle/neutral collision frequency<sup>29,30</sup>.

Quantity	Ions $\text{He}^+$	Electrons $e^-$
$T$ (eV)	0.026	2 – 4
$n$ ( $\text{m}^{-3}$ )	$5 - 50 \times 10^{15}$	$5 - 50 \times 10^{15}$
$\rho_c$ ( $\mu\text{m}$ )	400	37 – 83
$\lambda_{\text{mfp}}$ (cm)	1.50	2 – 4.5
$\nu_c$ (Hz)	$380 \times 10^3$	$3 \times 10^9$
$\nu_p$ (Hz)	$7 - 23 \times 10^6$	$635 - 2000 \times 10^6$
$\nu_{\text{col}}^N$ (Hz)	$88 \times 10^3$	$38 - 85 \times 10^6$

### III. EXPERIMENTAL STUDY

Scans over  $B$ ,  $\vartheta$ , RF-power,  $y$ -position and pressure were performed and main results are presented here. If not specified the probe tip position is set by default at  $y = 40$  mm and  $z = -60$  mm, and the pressure at 1.2 Pa.

#### A. Influence of the magnetic field

$I(V)$  Characteristics for all inclinations of the probe tip have been plotted for several values of  $\|\mathbf{B}\|$  and for a 200 W-RF power input in fig.7. Without magnetic field (fig.7-(a)), the “classical”  $I(V)$  is recovered, because the plasma is an isotropic medium and the orientation of the probe unimportant. The slight differences between all six curves come from small variations on the plasma conditions, due to the fact that the change of inclination requested to open the chamber between each measurement (uncertainties within 5% due to the gas pressure gauge, thus the RF coupled power which is sensitive to the pressure may not be exactly the same).

The shape of the  $I(V)$  changes drastically in the presence of a magnetic field as depicted in fig.7-(b) to (d). The slope of the exponential part and the electron saturation current one as well as the ratio  $I_e/I_i$  are strongly affected by the addition of a magnetic field<sup>11</sup>. Note that the increase of  $I_e$  with the magnetic field is due to a better coupling of the RF power and to better confinements. More generally, it can be seen that the overall shape of the characteristics are qualitatively close to the double probe/tanh-shape ones modelled by eq.(5). For small angles ( $\vartheta \leq 12^\circ$ ), the characteristics even display a bump between the exponential and the saturation parts. The bump’s overshoot amplitude and the change in the slope between the exponential part

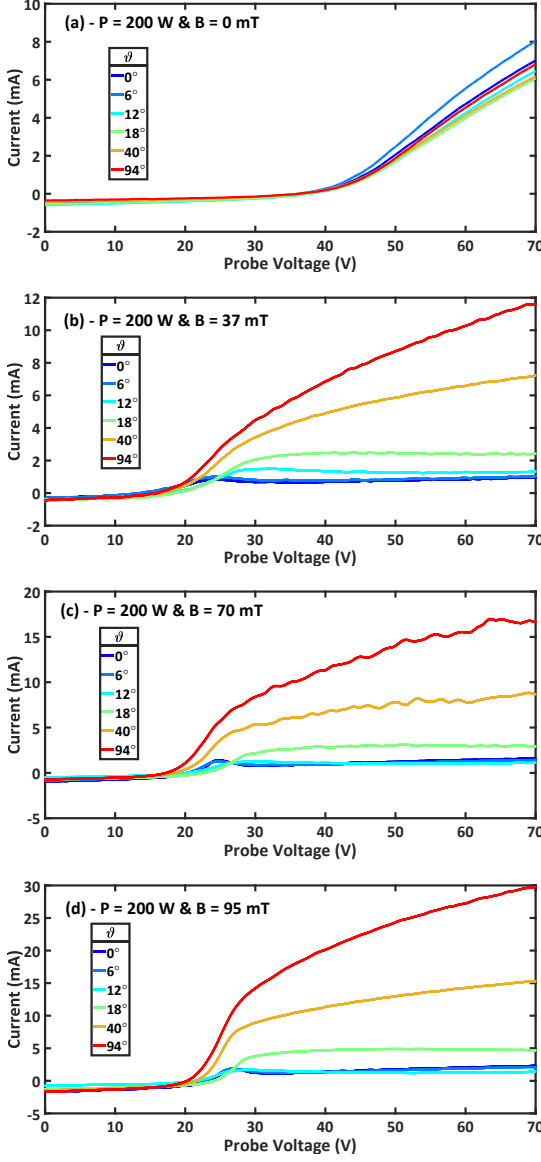


FIG. 7. Evolution of the  $I(V)$  characteristics at 200 W-RF power, at position  $y = 40/z = -60$  mm with increasing  $\|\mathbf{B}\|$  from 0 (a) to 95 mT (d) for all six  $\vartheta$  inclinations, 1.2 Pa He. Potential range of the measurements were  $-70$  to  $+70$  V, but the purpose of the study is not the ion part so only the range  $[0, 70]$  V is displayed here. Note that the current range changes for each graphs.

256 and the electron saturation regime is emphasized  
257 and steeper with larger  $\|\mathbf{B}\|$ .

## 258 B. Influence of probe inclination

259 For a probe inclination of  $18^\circ$ , the measured  $I(V)$   
260 characteristic looks like the “tanh-shape” as ex-  
261 plained previously. For higher inclination angle, the  
262 electron current does not saturate (due to sheath ex-

263 pansion) and for lower inclination angle, there is a  
264 bump. The only difference between all these dif-  
265 ferent cases is the width of the flux tube that scales  
266 as  $\sim L_p \sin \vartheta$ . The probe area facing magnetic field  
267 lines (see fig.5) is written as follows :

$$S_{\text{face}} = \pi r_p^2 \cos \vartheta + \pi L_p r_p \sin \vartheta \quad (6)$$

268 which can be scaled as  $S_{\text{face}} \sim \sin \vartheta$  because  $L_p \gg$   
269  $r_p$ .

270 For  $\vartheta = 0^\circ$  at 100 mT,  $r_p \approx 2\rho_{ce}$ , therefore, the  
271 probe surface facing the magnetic flux tube is compar-  
272 able to the “cyclotron area” ( $S_{ce} = \pi\rho_{ce}^2$ ) : in  
273 this case of grazing incidence, a bump arises on  
274 the measured characteristics. By increasing the angle,  
275 the facing surface increases (whereas the cyclotron  
276 area remains constant) and the amplitude of the bump  
277 decreases, and even disappears for larger angles.  
278 One can suggest that the flux tube narrowness compar-  
279 able to the cyclotron area could explain the bump. However,  
280 it remains even if  $S_{\text{face}} \gg S_{ce}$  (when  $\vartheta > 5^\circ$ ), therefore  
281 another mechanism should be invoked in order to explain  
282 the presence of the bump.  
283

284 We performed a series of experiments with a  
285 power input in the range 20 - 200 W in order to  
286 quantify the evolution of the characteristics with re-  
287 spect to  $\vartheta$ . Fig.8 shows the evolution of the current  
288 at 70 V,  $I(V = V_{\text{max}} = 70 \text{ V})$  or the “end-current”,  
289 against  $\sin \vartheta$ . This end value is used, because the  
290 plasma potential is actually unknown, so the compar-  
291 ison of the current at plasma potential is not possi-  
292 ble for now.

293 Without magnetic field (fig.8-(a)), the *end-*  
294 *current* is constant for any inclination as explained  
295 previously. Moreover by increasing the RF-power,  
296 the overall collected end-current also increases, be-  
297 cause the power also increases the plasma density  
298 ( $I \propto n_e$ ) as expected.

299 In the presence of a magnetic field of 95 mT  
300 (fig.8-(b)) two regimes are evidenced : the region  
301 where there is a bump ( $\vartheta \leq 12^\circ \Leftrightarrow \sin \vartheta \leq 0.21$ )  
302 and the region with an asymmetric double probe  
303 behaviour (above  $12^\circ$ ). In the former region, the  
304 end current is proportional to  $\sin \vartheta$ , as the width  
305 of the magnetic flux tube : the sine dependence of  
306 the current collection is verified. But in the “bump  
307 region”, the collected end-current remains approxi-  
308 mately constant with  $\vartheta$  for any RF-power. Since  
309 the collected current is proportional to the product  
310 of the density with the collecting surface,  $n_e S_{\text{coll}}$ ,  
311 (assuming  $\langle v_e \rangle \sim \langle v_{e,\parallel} \rangle \approx \text{Cte.}$ ), the increase of the  
312 angle also increases  $S_{\text{coll}}$ , so to keep constant col-  
313 lected current, the electron density in the flux tube  
314 should decrease. This is in a good agreement with  
315 figure 9-(b): in the presence of a magnetic field, and  
316 if there is a bump on the characteristic, the density  
317 is lower than in the absence of a bump (going from

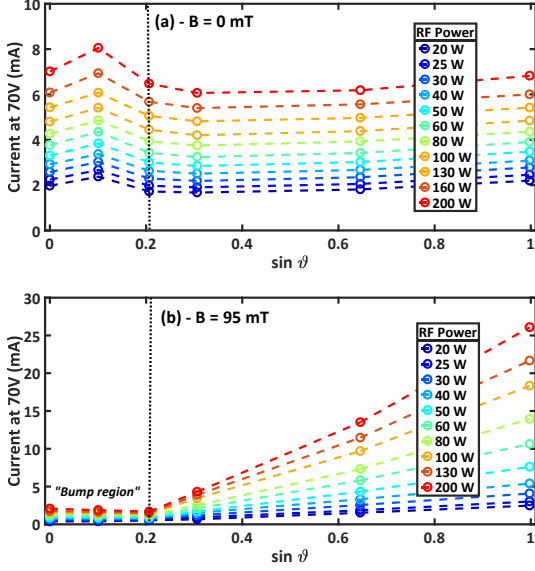


FIG. 8. Evolution of the collected current at 70 V with the sine of the inclination angle  $\vartheta$  without magnetic field (a), and with magnetic field (b) of amplitude 95 mT, 1.2 Pa He. The left region is the “bump region”, where a bump is measured ( $\vartheta \leq 12^\circ \Leftrightarrow \sin \vartheta \leq 0.21$ ). The line is a guide for the eye.

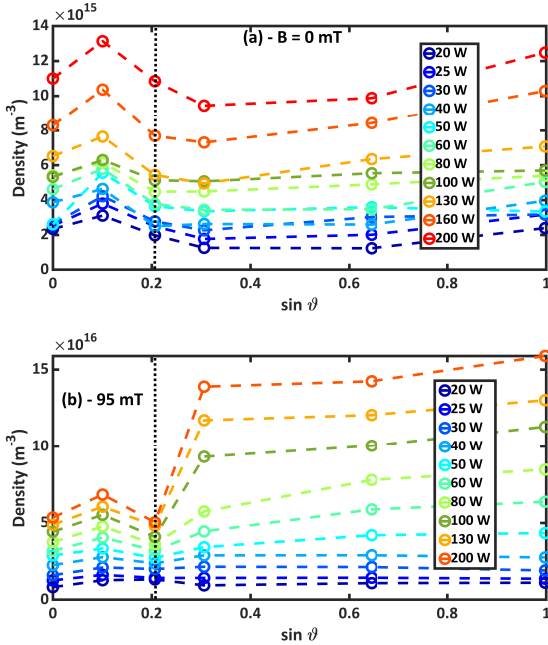


FIG. 9. Evolution of the density measured with the method described in the next section, in same conditions as in figure 8 with magnetic field (a) and without magnetic field (b) of 95 mT. As expected, the density is kept approximatively constant in the absence of magnetic field, but we notice a sharp change in the density between the “bump-” and the “no-bump-region” in the presence of magnetic field at higher power. The line is a guide for the eye.

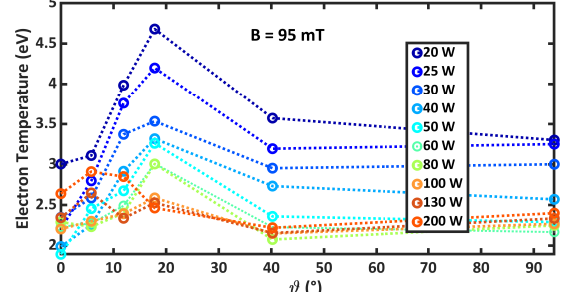


FIG. 10. Evolution of the computed electron temperature (see next section for the used algorithm) with respect to the inclination of the probe at 95 mT magnetic field amplitude. The line is a guide for the eye.

318  $n_e \approx 5 \times 10^{15} \text{ m}^{-3}$  with a bump to  $n_e \approx 15 \times 10^{15}$   
 319  $\text{m}^{-3}$  without a bump at 200 W RF power). This  
 320 density difference is enhanced for higher power.  
 321 However, for lower power the density remains ap-  
 322 proximately constant at all inclinations.

323 However, the evolution of the electron tempera-  
 324 ture with respect to the inclination angle (figure  
 325 10) is impossible to explain straightforwardly. In-  
 326 deed the electron flow collected by the probe is the  
 327 combination of two populations: the parallel and  
 328 the perpendicular to B flow, having each its own  
 329 temperature (i.e.  $T_{e\parallel}$  and  $T_{e\perp}$  resp.). Our method  
 330 gives a kind of average of both. Unfortunately, the  
 331 electron energy distribution function, which could  
 332 help us to understand the plot, is too noisy to be ex-  
 333 ploited (even after some filtering such as Stavitzky  
 334 Golay, or Fourier analysis). The explanation of this  
 335 plot is still an opened question for further studies.

336 Nevertheless, constant end-current in bump -  
 337 region can also mean there is a surrounding electron  
 338 sheath assuming the probe potential is higher than  
 339 the plasma potential, and then the effective collect-  
 340 ing radius is higher than the probe radius.

### C. Influence of the RF-power

342 As shown in the last subsection, increasing RF-  
 343 power also increases the overall density. To track  
 344 the bump evolution with RF-power regardless to  
 345 the density change, it is convenient to normalize  
 346 the  $I(V)$  to the end-current value  $I(V)/I(70 \text{ V})$ . In  
 347 fig.11 are depicted the normalized probe character-  
 348 istics at  $\|\mathbf{B}\| = 95 \text{ mT}$  for all inclinations and for  
 349 several input RF-power, fig.11-(a) to (c).

350 Although the end current is proportional to the  
 351 collecting surface (which is  $\propto \sin \vartheta$ ), the normal-  
 352 ization removes this dependence and all angles can  
 353 be compared. The electron saturation part, directly  
 354 connected to the sheath extension, is then the same  
 355 for every angles, as shown in fig.11. In fig.11-(a),

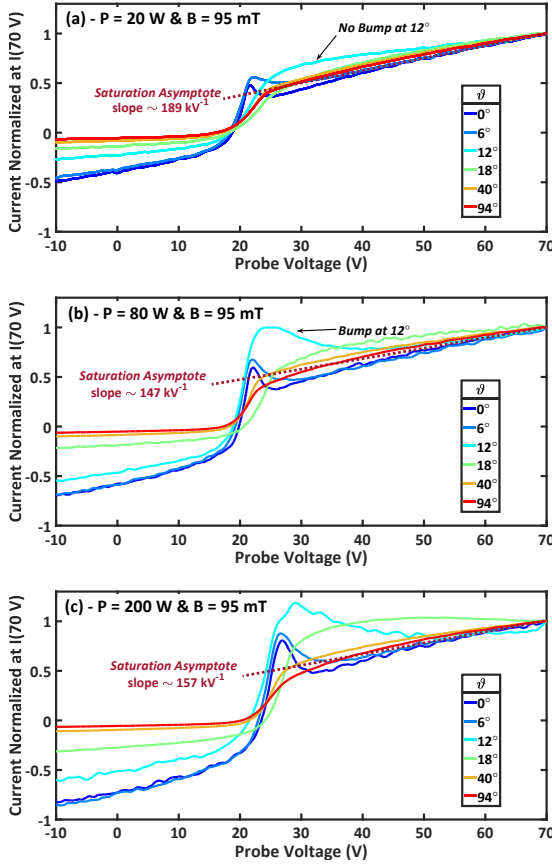


FIG. 11. Normalized  $I(V)/I(V_{\max})$  characteristics at 95 mT, for every inclination angles, 1.2 Pa He. RF-power is fixed at (a) 20 W, (b) 80 W and (c) 200 W. On each graph is also plotted (on dashed lines) the mean saturation linear curve with its slope.

356 for 20 W there is no bump at  $12^\circ$ , contrary to fig.11-  
 357 (b) for 80 W. The current at the bump position is  
 358 also larger than the end-current in fig.11-(c). More-  
 359 over, the increase of the power increases the ampli-  
 360 tude of the bump and its width.

361 One can suppose the existence of perpendicular  
 362 (to  $\mathbf{B}$ ) RF currents, pumping the flux tube con-  
 363 nected to the probe: this idea is used to derive  
 364 a fluid model in section IV to recover the bump  
 365 analytically. In addition, as depicted in fig.8-(b),  
 366 increasing the power does not increase the end-  
 367 current in the “bump region”, corroborating the for-  
 368 mer assumption. These RF currents, when averaged  
 369 over one RF period, exhibit a net DC perpendicular  
 370 contribution<sup>31</sup>, acting as perpendicular DC cur-  
 371 rents, which have already been investigated in pre-  
 372 vious models<sup>22,23</sup> to explain the depletion and satu-  
 373 ration currents of biased flux tubes.

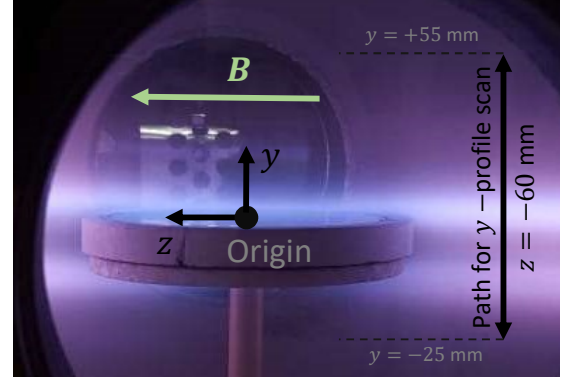


FIG. 12. Photograph from 1.2 Pa He pressure plasma around the RF antenna operating at 100 W with  $\|\mathbf{B}\| = 80$  mT magnetic field. The magnetic confinement generates this double player plasma aspect around the probe. Far enough from the antenna the density is homogeneous.

#### 374 D. Influence of the probe position

375 The position of the probe is also an important  
 376 parameter. It is initially placed relatively far from  
 377 the antenna to have a homogeneous plasma around  
 378 the probe. Indeed, near the antenna, the  $\mathbf{E} \times \mathbf{B}$   
 379 effect is larger and the plasma denser. That is why,  
 380 there is a thin plasma layer above, and below the  
 381 antenna (see photograph in fig.12). Moreover, at  
 382 this RF-pulsation ions do not react to the quick po-  
 383 tential change near the antenna, whereas electrons  
 384 do<sup>32</sup> ( $\omega_{pe} > \omega_{RF} > \omega_{pi}$ ).

385 To make sure that the inclination of the probe  
 386 does not scan different slices of plasma (i.e. that  
 387 the plasma is homogeneous in a range of  $\pm L_p \sin \vartheta$   
 388 around the probing position in the y direction), mea-  
 389 surements along the y axis were performed at fixed  
 390  $z = -60$  mm position and for  $\vartheta = 0^\circ$ . Power was  
 391 fixed at 100 W-RF,  $\|\mathbf{B}\| = 80$  mT in 1.2 Pa He  
 392 plasma. All characteristics in Fig.13 depicted a  
 393 bump, where the plotted parameters are the float-  
 394 ing potential  $\phi_{fl}$ , the bump potential  $V_{bump}$  and the  
 395 bump current  $I_{bump}$ . Dote suggested the bump po-  
 396 tential to be near the plasma one<sup>15,19,20</sup>. According  
 397 to Dote’s assumption and using the combined po-  
 398 tential drops in the sheath and the collisionless pre-  
 399 sheath<sup>1</sup>, one can write the potential drop between  
 400 the plasma and the floating probe potential for cold  
 401 ions ( $T_i/T_e \rightarrow 0$ ) as:

$$\phi_p - \phi_{fl} = \frac{T_e}{2e} \ln \left[ \frac{m_i}{2\pi m_e} \right] + \frac{T_e}{2e} = 4.03 \times T_e, \quad (7)$$

402 with  $T_e$  in eV. For all previous measurements at  
 403 ( $z = -60$  mm,  $y = 40$  mm), using the approxima-  
 404 tion  $\phi_p \approx V_{bump}$  gives  $T_e \approx 1.30$  eV (which is a typ-  
 405 ical value in ALINE magnetized, plasma<sup>26,27</sup>).



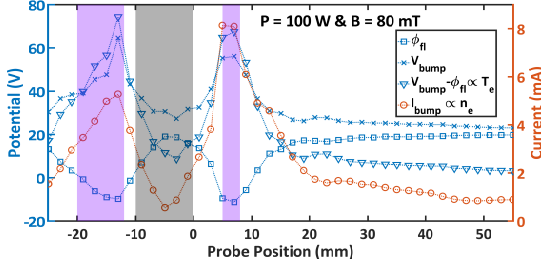


FIG. 13. Evolution of measured parameters (floating potential  $\phi_f$ , bump potential  $V_{\text{bump}}$  and bump current  $I_{\text{bump}}$ ) along the  $y$  axis at  $z = -60$  mm, 100 W-RF, 80 mT and 1.2 Pa (see double arrow  $\leftrightarrow$  in fig.12). The gray region represents the region where the probe faces the antenna (antenna extension is  $z \in [-40, 40]$  mm and  $y \in [-10, 0]$  mm), the purple regions represent the denser plasma region (see photograph in fig.12). For comparison  $T_e \propto V_{\text{bump}} - \phi_f$  is also plotted.

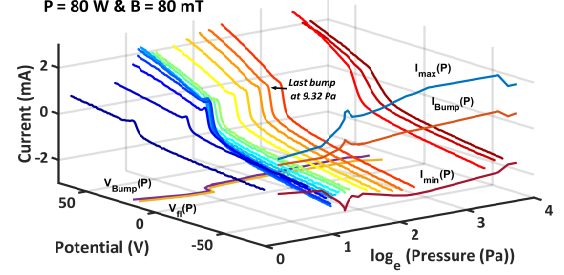


FIG. 14. Tridimensional representation of the  $I(V)$  characteristics in all considered He pressures from 1.2 to 40 Pa for 80 W-RF power and  $||\mathbf{B}|| = 80$  mT. In the  $V = 80$  V plane are plotted the end currents at  $\pm 70$  V and the bump current. In the  $I = -3$  mA plane are plotted the floating and the bump potentials. Last bump is measured at 9.32 Pa. If no bump is measured,  $I_{\text{bump}}$  corresponds to the point where  $dI/dV = \max(dI/dV)$ , i.e. the current at “classical” plasma potential.

407 The tilting of the probe does not scan “different  
408 slices” of plasma and different inclination angles  
409 can be compared as shown in fig.13: 1 cm around  
410 the  $y = 40$  mm position, all cited parameters are  
411 almost constant. Therefore, the homogeneity hypo-  
412 thesis (almost constant  $T_e$  and  $n_e$  in the probing  
413 area) can be applied in the experimental conditions.  
414 Finally, this last figure also highlights the fact that  
415 current and temperature (as defined in eq. 7) in-  
416 creases by a factor of  $\sim 7$  in the bright regions (see  
417 photograph depicted in fig.12), near the antenna.

#### 418 E. Influence of the pressure

419 For a magnetic field of 80 mT, and an input  
420 power of 80 W-RF, measurements were performed  
421 with a probe parallel to the field line ( $\vartheta = 0^\circ$ ) in a  
422 He pressure range from 1.2 to 40 Pa. All character-  
423 istics are plotted Fig. 14.

424 When pressure increases, the bump gets narrower  
425 and its amplitude diminishes. Above 9.32 Pa, the  
426 bumps disappear and the  $I(V)$  characteristic turns  
427 into an asymmetric double probe one.

428 That’s why one can separate the pressure range  
429 in 2 regimes :

430 The low collisional regime from 1 Pa to 10  
431 Pa. At these pressures the electron-neutral col-  
432 lision frequency  $\nu_{\text{col}}^{eN}$  is lower than the electron  
433 plasma frequency  $\nu_{pe}$ , and lower than the electron  
434 cyclotron frequency  $\nu_{ce}$  (see table I) and of the same  
435 order than the RF frequency. For example at 1 Pa  
436  $\nu_{\text{col}}^{eN} \approx 17$  MHz<sup>29</sup>. In the same way the ion-neutral  
437 collision frequency  $\nu_{\text{col}}^{iN}$  is much lower than the ion  
438 plasma frequency  $\nu_{pi}$ , and lower than the ion cy-  
439 clotron frequency  $\nu_{ci}$  up to 4 Pa so that ions are  
440 considered as magnetized in the first half of the low  
441 collisional pressure range. In this range the classi-

442 cal perpendicular diffusion falls down and perpen-  
443 dicular currents are able to deplete strongly the flux  
444 tube while the typical scale length of these current  
445 is higher than the radius of the probe, which is the  
446 case here because  $\rho_{ci} \gg r_p$ . In a quiet plasma, as  
447 we have in ALINE, such a behaviour can be seen,  
448 while in Tokamak edge plasma anomalous transport  
449 can still prevent the biased flux tubes to deplete.

450 In the collisional regime ( $P > 10$  Pa),  $\nu_{\text{col}}^{eN}$  re-  
451 mains lower than  $\nu_{ce}$  and  $\nu_{pe}$ , but much higher than  
452 the RF frequency. RF electron current are then low-  
453 ered by collisions. And ions are no more magne-  
454 tized because  $\nu_{\text{col}}^{iN} > \nu_{ci}$ , which favours their per-  
455 pendicular diffusion while ion perpendicular cur-  
456 rent are lowered in the same time, filling the lack  
457 of density caused by the probe collection and can-  
458 celling the bump on the characteristics. For the  
459 highest pressures, the flux tube for ions disappears  
460 and the  $I(V)$  looks like an unmagnetized one<sup>14</sup>.

461 In the intermediate case of partially magnetized  
462 ions, the  $I(V)$  looks like a double symmetric probe  
463 characteristics. The electron saturation current col-  
464 lected by the probe depends also on the competition  
465 between perpendicular DC and RF currents and the  
466 cross diffusion of ions due to collisions.

467 Another remarkable result depicted in fig.14 is  
468 that, when the pressure is increased by a factor of  
469 40, the maximal current at probe position only in-  
470 creases by a factor 2. This behaviour denotes a good  
471 confinement of the plasma around the antenna by  
472 the magnetic field. Indeed, increasing the pressure  
473 brightens the plasma shown in fig.12; however out-  
474 side this region the plasma remains more or less the  
475 same. The only thing that changes is the collision  
476 rate with neutrals at higher density.

#### 477 IV. THEORETICAL APPROACHS

478 In the first part of this section, we provide a quan-  
 479 titative comparison of three different methods used  
 480 to extract both  $n_e$  and  $T_e$  from bumped character-  
 481 istics. In a second part, we show by using a fluid  
 482 model that, the bump in the  $I(V)$  curves in a pres-  
 483 ence of a magnetic field, can be explained by mean  
 484 of density depletion within the tube flux connected  
 485 to the probe and to the opposite wall of the reactor.

##### 486 A. Density and temperature data processing

487 Extracting electron density and temperature from  
 488  $I(V)$  characteristics is far from simple. But if  
 489 the measurements are done in the presence of  
 490 a magnetic field, the exploitation are even more  
 491 difficult. The challenge lies on the presence of  
 492 the bump, whose existence, shape, location and  
 493 amplitude depend on several plasma parameters  
 494 ( $|\mathbf{B}|$ ,  $\vartheta$ ,  $P_{\text{wr.}}$ ,  $y$ ,  $p$ ) (see sections III A to III E).

495 The first problem with bumped characteristics is  
 496 the uncertainty on the position of the plasma po-  
 497 tential. It is usually found by assuming that, at the  
 498 plasma potential  $V = \phi_p$ ,  $dI/dV|_{\phi_p} = \max(dI/dV)$ ,  
 499 which is equivalent to  $d^2I/dV^2|_{\phi_p} = 0^{2,3}$  (this is  
 500 called the ‘‘classical method’’ in the following). An-  
 501 other method based on the intersection of the linear  
 502 fits of the exponential part and the electron sat-  
 503 uration one has also been suggested and used in a pre-  
 504 vious study<sup>17</sup>. It was finally suggested that, in the  
 505 context of bumped characteristics, the bump po-  
 506 tential is at the plasma potential<sup>15,19</sup>. Thus, three meth-  
 507 ods are available, in order to determine the plasma  
 508 potential and we propose to compare them, for dif-  
 509 ferent inclinations, in a single 100 W-RF plasma,  
 510 with  $|\mathbf{B}| = 80$  mT and  $p = 1.2$  Pa, whose charac-  
 511 teristics are depicted in fig.15-(a).

512 We assume that the best method is the one which  
 513 would exhibit the lowest deviation of the plasma pa-  
 514 rameters with respect to  $\vartheta$ . We suppose indeed that  
 515 the probed plasma slice is the same for all inclina-  
 516 tions.

517 In the context of the ‘‘intersection method’’  
 518 we linearised the exponential growth as  $I(V) \approx$   
 519  $a_{\text{exp.}}V + b_{\text{exp.}}$ , and fitted the electron saturation cur-  
 520 rent with the formula:

$$I_e(V) \approx a_{\text{sat.}}V + b_{\text{sat.}} + c_{\text{sat.}}\sqrt{V}. \quad (8)$$

521 with the  $\sqrt{V}$  term similar to one of the OML ap-  
 522 proach, which gives a relatively good fit with exper-  
 523 imental curves. This equation is only able to fit  
 524 the saturation part, *i.e.* the end of the  $I(V)$  — far  
 525 from the bump potential range. Only the last 20  
 526 volts of each  $I(V)$  were used for the fitting, see fig.  
 527 15-(a).

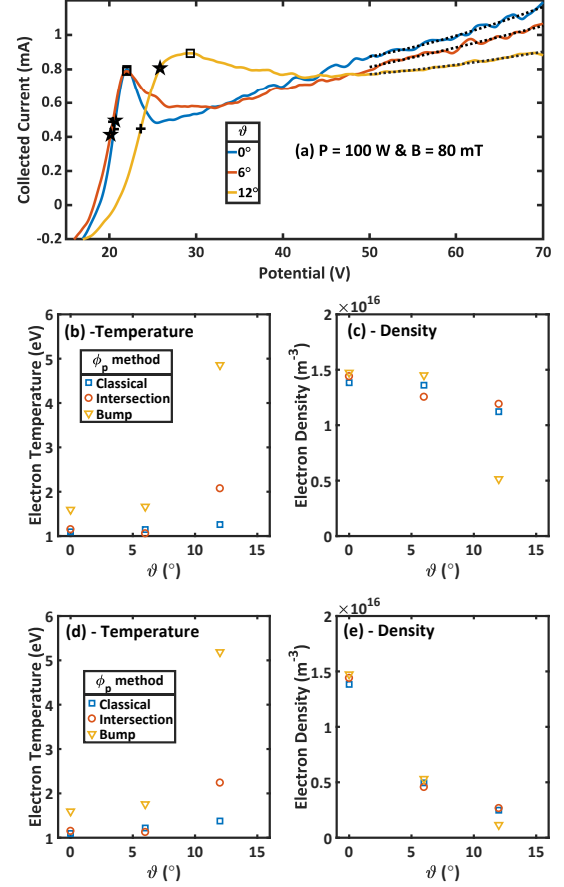


FIG. 15. Results of the electron temperature and density calculation on bumped characteristics with the described iterative model : (a)  $I(V)$  of plasma at 100 W-RF, 80 mT and 1.2 Pa for different probe inclinations and all methods are represented for the position of  $\phi_p$  (+ classical,  $\star$  intersection,  $\square$  bump). The dashed line is the fit of the electron saturation current with respect to equation (8) – (b) and (c)  $T_e$  and  $n_e$  against inclination angle with collecting surface correction – (d) and (e)  $T_e$  and  $n_e$  against inclination angle without collecting surface correction,  $S_{\text{coll.}} = S_{\text{probe}}$  ( $T_e$  remains the same though).

528 We used an iterative method, in order to deter-  
 529 mine both  $n_e$  and  $T_e$  with the plasma potential  $\phi_p$ ,  
 530 the current at plasma potential  $I_p$ , floating po-  
 531 tential  $\phi_{\text{fl.}}$ , magnetic field and probe inclination as  
 532 input parameters. First, a raw approximation of  
 533 electron temperature is done, supposing  $I \sim I_e \propto$   
 534  $\exp(eV/k_B T_e)$  for  $V \leq \phi_p$  in the exponential part.  
 535 Applying a linear fit on  $\ln I(V)$  one will find a first  
 536 value of  $T_e$ . From now one starts the iterative loops:  
 537 this electron temperature value allows a computa-  
 538 tion of a gross value of  $n_e$  since, at plasma potential,  
 539  $I_p = en_e(v)S_e/4$ . The value of  $S_e$  is not the probe  
 540 surface, even at plasma potential (where there is no  
 541 sheath), because of the cyclotron motion. That is  
 542 why it is assumed that the collecting surface is the

543 probe surface facing  $\mathbf{B}$  plus a layer thick of  $N_{\text{elr.}}\rho_{ce}$   
 544 (i.e. some Larmor radii –  $N_{\text{elr.}}$  being the number of  
 545 electron Larmor radii connected to the probe) :

$$S_e = \pi \cos \vartheta \times (r_p + N_{\text{elr.}}\rho_{ce})^2 + \pi L_p \sin \vartheta \times (r_p + N_{\text{elr.}}\rho_{ce}) \quad (9)$$

546 by replacing  $r_p \rightarrow r_p + N_{\text{elr.}}\rho_{ce}$  in eq.(6). It is as-  
 547 sumed that this equation takes into account the per-  
 548 pendicular motion of electrons along the magnetic  
 549 field lines connected to the probe.

550 With  $T_e$  and  $n_e$ , it is possible to compute the elec-  
 551 tron Debye length  $\lambda_{\text{De}}$  and the ion sheath thickness  
 552 using the Child-Langmuir law (since  $\rho_{ci} \gg r_p \sim \rho_{ce}$   
 553 and that Zhu's corrections<sup>33</sup> for cylindrical geome-  
 554 try only bring minor changes in opposition to its  
 555 complexity), knowing,

$$\ell_{\text{CL}} = \frac{\sqrt{2}}{3} \lambda_{\text{De}} \left( 2e \frac{|\phi_p - V|}{k_B T_e} \right)^{3/4} \quad (10)$$

556 for  $V \leq \phi_p$ . Since ions are supposed unmagnetized,  
 557 the collecting area for ions is

$$S_i = \pi(r_p + \ell_{\text{CL}})^2 + 2\pi L_p(r_p + \ell_{\text{CL}}). \quad (11)$$

558 It is then possible to compute the ion current  
 559 for  $V \leq \phi_p$ , using the Bohm flux formula,  $I_i =$   
 560  $0.61 \times en_e c_s S_i$ . So, the updated electron current  
 561  $I_e = I(V) - I_i$  can be calculated. Taking again the  
 562 log-scale of this new electron current gives a new  
 563 more accurate value of  $T_e$ . The loop starts over  
 564 again, and ends if temperature values converge (i.e.  
 565  $|T_e^{\text{new}} - T_e^{\text{old}}| \leq \varepsilon$ ,  $\varepsilon$  being given by the user).

566 Equations giving  $S_e$  and  $S_i$  (eqs. (9) and (11)  
 567 resp.) take into account the sheath extension for  
 568 magnetized electrons and unmagnetized ions. To  
 569 take into account the inclination of the probe, and  
 570 find reliable plasma parameters, one should also  
 571 multiply the total current by a geometric factor of  
 572  $\pi r_p^2 / S_{\text{face}}$  from eq.(6) giving a dimensionless fac-  
 573 tor of  $1/(\cos \vartheta + [L_p/r_p] \times \sin \vartheta)$ . This allows the  
 574 recovering of the same amplitude for all bumped  
 575  $I(V)$ . The extracted values of  $n_e$  and  $T_e$  are plot-  
 576 ted in fig.15-(b) and (c) using this correction, and  
 577 plotted in fig.15-(d) and (e) without the correc-  
 578 tion ( $n_e$  strongly decreases with the angle). From  
 579 Fig. 15-(b) and (c) it is clear that the classical  $\phi_p$ -  
 580 determination method gives the more reliable val-  
 581 ues of temperature and density (the deviation of  $T_e$   
 582 values between each inclination is negligible com-  
 583 pared to other methods). We have then  $T_e \approx 1.2$  eV  
 584 and  $n_e \approx 1.3 \times 10^{16} \text{ m}^{-3}$ . Since the OML model  
 585 remains valid in RF-plasmas<sup>34</sup>, and that ions are  
 586 unmagnetized, we extracted  $n_i^{\text{OML}} = 1.74 \times 10^{17}$   
 587  $\text{m}^{-3}$  (which is within the typical errorbar for OML  
 588 model) and  $T_e^{\text{OML}} = 2.69$  eV, which are overesti-  
 589 mated compared to the previous method.

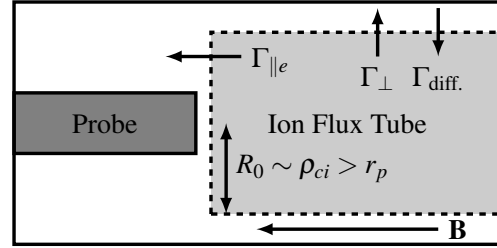


FIG. 16. Sketch of the fluid model. The flux tube is de-  
 limited by the dashed line. The inclination  $\vartheta$  is  $0^\circ$ .

590 By comparison, in the absence of magnetic field,  
 591 the bump method to find the plasma potential makes  
 592 no sense (since there is no bump) and both classi-  
 593 cal and intersection methods are alike and give the  
 594 same value of the plasma potential. Therefore the  
 595 self-consistent algorithm gives an electron density  
 596 of the order of  $5.32 \times 10^{15} \text{ m}^{-3}$  and an electron tem-  
 597 perature of 3.47 eV (for the same discharge param-  
 598 eters as with  $\|\mathbf{B}\| \neq 0$ ).

## 599 B. Fluid model approach

600 As suggested by Mihaila and Rozhansky<sup>16,23</sup>, the  
 601 bump on  $I(V)$  characteristics could be induced by  
 602 density depletion within the flux tube.

603 The cylindrical flux tube connected from the  
 604 probe to the reactor's wall is filled by electrons us-  
 605 ing a single channel, which is the lateral area of  
 606 the cylinder. Due to magnetic confinement and for  
 607 grazing incidences, the perpendicular current arises  
 608 thanks to collisions with neutrals. During a  $I(V)$   
 609 measurement for  $V > \phi_p$ , one pumps the electrons  
 610 inside the flux tube, which makes the local elec-  
 611 tron density decreases. If the pumped electron cur-  
 612 rent is larger than the refill perpendicular one, then  
 613 the collected current at the probe decreases with  
 614 phi (the bump origin). But when the probe poten-  
 615 tial is increased further, the sheath extent around it  
 616 also increases, which artificially makes the cylindri-  
 617 cal flux tube diameter wider. Consequently, when  
 618  $V \gg \phi_p$ , the electron perpendicular current com-  
 619 pensate the pumped one and the collected current  
 620 increases again. Now for larger incidences, the per-  
 621 pendicular current always overcomes the pumped  
 622 one, which explains the experimentally observed  
 623 disappearance of the bump for  $\vartheta > 12^\circ$ .

624 In the meantime, there is another mechanism in-  
 625 volving mainly ions: it is the plasma pumping via  
 626 perpendicular ion current due to the positive bias-  
 627 ing of the flux tube with respect to the surround-  
 628 ing plasma potential. This mechanism has already  
 629 been invoked to explain the early electron satur-  
 630 ation of the  $I(V)$  characteristics in the case of planar



631 probe<sup>23</sup> in magnetized plasmas. The typical scale  
632 length of these perpendicular ion currents is the ion  
633 gyroradius. To explain the bump, this mechanism  
634 can be divided in three regimes occurring when the  
635 probe potential overcomes the plasma potential:

- 636 1. When the transverse (perpendicular to  $\mathbf{B}$ )  
637 ion current is lower than the electron satura-  
638 tion current collected by the probe, the  
639 space charge of the sheath is electropositive  
640 and consequently the flux tube potential “fol-  
641 lows” the probe potential. The density deple-  
642 tion can first appear in that regime.
- 643 2. When the transverse ion current is exactly  
644 equal to the electron saturation current col-  
645 lected by the probe, the sheath between the  
646 probe and the flux tube disappears and the  
647 collected current can decrease because the  
648 flux tube density decreases with the probe po-  
649 tential.
- 650 3. Finally when the transverse ion current is  
651 higher than the electron saturation current  
652 collected by the probe, electrons must be ac-  
653 celerated in the sheath to balance the ion cur-  
654 rent and thus the sheath drop is reversed. The  
655 sheath space charge becomes electronegative  
656 and the flux tube potential tends to saturate  
657 compared to the probe potential. This regime  
658 accounts for long and thin flux tube.

659 Nevertheless, plasma diffusion is more and more  
660 efficient as the flux tube is widening. So in the third  
661 regime, with the saturation of the flux tube poten-  
662 tial, the pumping also saturates and the density de-  
663 pletion can be cancelled resulting in a classical in-  
664 crease of the current in the last part of the  $I(V)$  char-  
665 acteristics (beyond the bump).

666 Finally there is an optimum point for which the  
667 pumping is maximum compared to cross diffusion,  
668 and this is at this working point the bump appears to  
669 be the higher because of the strong negative slope  
670 just following the maximum of the bump. Actu-  
671 ally, the bump does not mean there is an increase of  
672 current compared to an  $I(V)$  characteristics with no  
673 bump, on the contrary it means a decrease of cur-  
674 rent.

675 The complexity of the phenomenon can only be  
676 explained by a mass and current conservation tak-  
677 ing into account the growing of the flux tube radius  
678 with the potential.

### 679 The model:

680 Rozhansky *et al.*<sup>23</sup> showed that the ion flux tube  
681 has a characteristic radius of  $R_0 \sim \rho_{ci}$ , and a length  
682  $L$  (this ion flux tube connected to the probe also

683 contains the electron flux tube of radius  $\rho_{ce} \ll \rho_{ci}$ ).  
684 Due to their cyclotron motion, electrons are trapped  
685 in both ion and electron tubes and can only leave  
686 them through the ends, producing a parallel net cur-  
687 rent of  $J_{e,\text{sat.}} \times \pi R_0^2$ . To ensure current and quasi-  
688 neutrality conservation in the ion tube, there must  
689 be a perpendicular ion flux through the cylindrical  
690 surface so that,  $J_{i,\text{sat.}} \times 2\pi R_0 L \approx J_{e,\text{sat.}} \times \pi R_0^2$ . In  
691 this regime, where the perpendicular current can  
692 be higher than the electron saturation current on  
693 the probe, the potential gap can reverse in front  
694 of the probe (electronegative sheath) accelerating  
695 electrons and repelling ions. Thus, one can ne-  
696 glect the parallel ion flux on the probe side (in the  
697 case of an electropositive sheath, the ion current on  
698 the probe surface can also be neglected compared  
699 to electron current, still assuming that the electron  
700 current is close to its saturation value).

701 In the following we use current continuity for  
702 ions in order to obtain a first order ODE that gives  
703 the density of the flux tube with respect to the probe  
704 potential. Using Laframboise’s theory, this tube  
705 density (or “local plasma density”) gives the elec-  
706 tron fraction that will be collected by the probe re-  
707 garding its potential  $V$ . An analytic expression of  
708 the collected current can be then provided.

709 As shown in the last sections, the pumping is  
710 enhanced by perpendicular (to  $\mathbf{B}$ ) RF and DC  
711 currents<sup>21,22</sup>. But periodic RF current can be re-  
712 duced to an averaged DC over one a period. That is  
713 why the model is steady state, and only DC quan-  
714 tities are considered. Finally, to prevent the tube  
715 density to drop to zero, we assume the presence of  
716 a source term  $S_0$ , so that,

$$\iiint_{\text{tube}} S_0 \, d\tau = 2 \times \pi R_0^2 \times \frac{1}{2} n_0 \langle v_e \rangle, \quad (12)$$

717 where  $n_0$  is the bulk plasma density (outside the ion  
718 flux tube region) and  $n_t$ , the ion flux tube density  
719 ( $n_0 \geq n_t$ ). This term fills the tube at the same rate  
720 electrons leave it from both ends (which is an over-  
721 estimation of the “real”  $S_0$  source term).

722 From the stationary ion continuity equation, we  
723 have  $\nabla \cdot \mathbf{\Gamma}_i \sim \nabla \cdot \mathbf{\Gamma}_{i,\perp} = S_0$ . Perpendicular ion flux  
724 is separated in two parts: lateral mobility  $-\mu_i n_t \nabla \phi$   
725 and the diffusion flux  $-D_\perp \nabla n_t$ . Integration of all  
726 ion fluxes through the whole tube using Gauss’s law  
727 gives:

$$\frac{n_0 \langle v_e \rangle}{2L} R_0 = - \left( D_\perp \frac{\partial n_t}{\partial r} \Big|_{R_0} + n_t \mu_i \times \frac{\partial \phi}{\partial r} \Big|_{R_0} \right) \quad (13)$$

728 In the presence of a strong radial electric field (and  
729 especially in a cold plasma), the ion drift veloc-  
730 ity is larger than the thermal velocity, thus  $\rho_{ci} =$   
731  $v_\perp / \omega_{ci} = (v_{\text{drift}}^2 + v_{i,\text{Th.}}^2)^{1/2} / \omega_{ci} \sim |v_{\text{drift}}| / \omega_{ci} =$   
732  $-\partial_r \phi / B \omega_{ci}$  (all at  $R_0$ ). Recalling that  $R_0 \sim \rho_{ci}$ ,

733 equation (13) rewrites as,

$$\frac{n_0 \langle v_e \rangle}{2LB\omega_{ci}} \times \frac{\partial \phi}{\partial r} \Big|_{R_0} = \left( D_{\perp} \frac{\partial n_t}{\partial r} \Big|_{R_0} + n_t \mu_i \times \frac{\partial \phi}{\partial r} \Big|_{R_0} \right) \quad (14)$$

734 Now using the chain rule,  $\partial n_t / \partial r|_{R_0} = \partial n_t / \partial \phi \times$   
 735  $\partial \phi / \partial r|_{R_0}$ , one will get the following first order  
 736 ODE at the radius  $r = R_0$  :

$$\frac{\partial n_t}{\partial \phi} = -\frac{\mu_i}{D_{\perp}} n_t + \frac{n_0 \langle v_e \rangle}{2\omega_{ci}BLD_{\perp}} \quad (15)$$

737 The perpendicular mobility can also be written as a  
 738 conductivity depending on the current nature (col-  
 739 lision, inertial, viscosity, anomalous,...). With the  
 740 initial condition of  $n_t(\phi = \phi_p) = n_e$  since there is  
 741 no sheath nor spatial potential variation at plasma  
 742 potential, one will get :

$$n_t(V) = n_{\infty} + (n_0 - n_{\infty}) \exp \left[ \frac{\mu_i}{D_{\perp}} (V - \phi_p) \right], \quad (16)$$

743 where  $V$  is the probe potential and  $n_{\infty} = n_0 \times$   
 744  $\langle v_e \rangle / 2\mu_i B \omega_{ci} L$ . Here we assumed that the flux tube  
 745 potential equals the probe one. Although generally,  
 746  $\phi_t = f(V) \geq V > \phi_p$ .

747 Equation 16 exhibits an exponential decay of the  
 748 density with  $V$ . This strong depletion of the flux  
 749 tube as soon as the biased potential of the tube  
 750 is higher than the surrounding plasma potential is  
 751 needed to see the bump rising. For lower decay  
 752 (for ex.  $\sim 1/(V - \phi_p)$  or  $\sim 1/(V - \phi_p)^2$ ) the bump  
 753 does not appear because of the expansion of the  
 754 sheath which increases the lateral surface of the flux  
 755 tube and hence the total perpendicular current more  
 756 rapidly that the density is depleted. This also  
 757 explains why at higher probe potential value, when  
 758 the exponential decay saturates, the current rises up  
 759 again due to sheath expansion. Actually there is a  
 760 competition between the diffusion  $D_{\perp}$  across the  
 761 lateral surface of the tube versus the perpendicular  
 762 current due to ion mobility  $\mu_i$  as it can be seen in  
 763 equation 16.

764 Next to fit the sheath expansion above  $V_p$  in a  
 765 magnetic field parallel to the probe, one uses the  
 766 Laframboise<sup>9</sup> model which showed that the portion  
 767 of plasma density actually touching a probe and  
 768 thus collected,  $n_{\text{eff}}$ , is given by the relation,

$$n_{\text{eff}}(\xi) = \frac{2n_t(\xi)}{\sqrt{\pi}} \left[ \sqrt{\xi} + \frac{\sqrt{\pi}}{2} e^{\xi} \text{erfc} \sqrt{\xi} \right] \quad (17)$$

769 for  $\xi = e(V - \phi_p) / k_B T_e$ . Finally, the collected cur-  
 770 rent on the probe is simply given by

$$I_e(V) = \frac{1}{2} e n_{\text{eff}}(V) \times \langle v_e \rangle S_e \quad (18)$$

771 where  $S_e$  is given by eq.(9), and the number of elec-  
 772 tron Larmor radii ( $N_{\text{elr}}$ ) is given as fitting param-  
 773 eter.

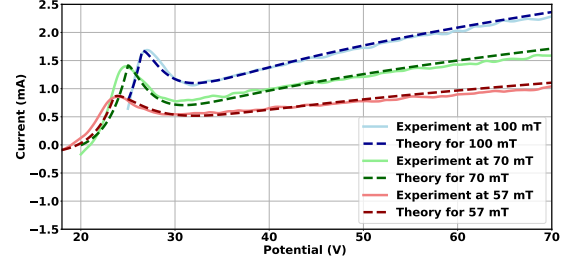


FIG. 17. Comparison of the 1D fluid model with the experiment. Probe had  $\vartheta = 0^\circ$  inclination angle in 200 W-RF plasma at 1.2 Pa for several  $\|\mathbf{B}\|$ .

744 This model is compared with the experimental  
 745 data in figure 17 for a magnetic field of 57, 70 and  
 746 100 mT in a 200 W-RF and 1.2 Pa Helium plasma  
 747 (the probe was parallel to  $\mathbf{B}$ ). For  $V < \phi_p$  the expo-  
 748 nential  $J_{e,\text{sat}} \times \exp(e(V - \phi_p) / k_B T_e) S_e$  part of the  
 749 electronic current is considered.

750 The number of Larmor radii,  $N_{\text{elr}}$ , goes from 0.1  
 751 to 5 with increasing  $\|\mathbf{B}\|$  in Eq. (9). The limit den-  
 752 sity in the flux tube,  $n_{\infty}$  is close to  $n_0 / 10$  : that  
 753 means that the measurement heavily depletes the  
 754 magnetic flux tube. Moreover, the model suggests  
 755 that the plasma potential is on the top of the bump  
 756 as proposed by Dote and Mihaila : the pumping  
 757 mechanism starts when  $V > \phi_p$  according to the  
 758 theory. Since electrons are way much mobile than  
 759 ions along  $B$ , as soon as the probe potential is above  
 760 the plasma potential, electrons of the flux tube are  
 761 flushed towards the probe. Moreover, as pointed out  
 762 by eq.(3), the flux tube itself has its own potential  
 763 (slightly above the bulk plasma potential) since it is  
 764 connected to the probe and thus somehow biased.

765 Finally, according to this theory, the prior param-  
 766 eter is actually the probe surface facing the mag-  
 767 netic field lines (i.e. the width of the magnetic flux  
 768 tube). Therefore, a bump could appear on a plane  
 769 probe characteristics or a spherical probe characteris-  
 770 tics as well, if the facing surface is small enough  
 771 corresponding more or less to a disk surface having  
 772 a radius of the order of  $\rho_{ce}$ .

## 803 V. CONCLUSION

804 Langmuir probe measurements in the presence of  
 805 a magnetic field are of a paramount importance in  
 806 plasma physics. Understanding and exploiting  $I(V)$   
 807 characteristics from a cylindrical Langmuir probe  
 808 in such conditions is difficult, especially due to the  
 809 presence of a bump in the curves for grazing inci-  
 810 dences of the cylindrical probe with respect to the  
 811 magnetic field lines. In this paper, the evolution of  
 812 the  $I(V)$  characteristics with respect to several dis-  
 813 charge parameters (magnetic field amplitude, probe  
 814 inclination, and pressure) was studied, in order to

815 provide a better understanding of cylindrical Lang-  
816 muir probe measurements in magnetized plasmas.

817 We showed that the presence of the magnetic  
818 field changes the general shape of the  $I(V)$  curves,  
819 because of the breaking-up of the plasma isotropy:  
820 the particles are not collected by the probe from all  
821 possible directions anymore but from a flux tube,  
822 connected to it from one end, and to the reactor's  
823 wall to the other. That is why the general shape  
824 of the characteristics tends to an asymmetric double  
825 probe (or tanh-shaped) one. We also showed  
826 that for grazing incidences of the probe with re-  
827 spect to  $B$ , a bump arises between the exponential  
828 part and the electron saturation current one. The  
829 bump vanishes as the probe inclination is increased,  
830 or if the magnetic field amplitude is reduced. It  
831 is also dependent on collisional processes, because  
832 its amplitude decreases, when the gas pressure in-  
833 creases. Finally, increasing the RF-power at the an-  
834 tenna heightens the bump amplitude, and can even  
835 make one appearing on the characteristics.

836 We argued that a probe measurement pumps  
837 electrons from their flux tube while ions are ex-  
838 pelled in the perpendicular direction (the electron  
839 current is mainly parallel to magnetic field lines).  
840 This density depletion as soon as probe potential  
841  $V$  overcomes the plasma one  $\phi_p$  (*i.e.* as the probe  
842 starts to attract electrons) can explain the presence  
843 of the bump. This hypothesis is strengthened by  
844 the pressure effects on the probe measurements:  
845 increasing the gas pressure (thus increasing colli-  
846 sions and therefore, perpendicular diffusion fluxes),  
847 makes the bump vanish. By using a fluid model,  
848 we corroborated the pumping mechanism of den-  
849 sity (due to a competition between mobility and  
850 diffusion) and validated the assumption of density  
851 depletion in the flux tube connected to the probe.  
852 Nevertheless this assumption is not enough to make  
853 appear the bump, the density decay in the flux tube  
854 must be stronger than the perpendicular expansion  
855 of the flux tube with  $V$ , that is why the exponential  
856 decay from our model is needed.

857 We have finally compared different methods for  
858 extracting both  $n_e$  and  $T_e$  from bumped charac-  
859 teristics, which are not very usual in the con-  
860 text of probe measurements. We showed that the  
861 classical method of plasma potential determination  
862 (where  $dI/dV$  is maximum) stays the most repro-  
863 ducible method to access this important parameter,  
864 although previous studies argued that the plasma  
865 potential coincides with the bump one. A lot of  
866 work is still needed to provide a complete theory  
867 that exploits bumped characteristics, especially to  
868 know the good collecting surfaces of the probe, and  
869 the good mobility and diffusion parameters to put  
870 in the model.

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