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Comprehensive thermodynamic study of the calcium sulfate-water vapor system. Part 2: Physical modeling of adsorption phenomena.

João G. D. Preturlan^{±,†}, Loïc Favergeon^{±,*}, Laetitia Vieille[±], Sara Quiligotti[†]

[±]Mines Saint-Etienne, Univ Lyon, CNRS, UMR 5307 LGF, Centre SPIN, F - 42023 Saint-Etienne France

†Saint-Gobain Research Paris, 39 quai Lucien Lefranc, F-93000 Aubervilliers France

* E-mail: favergeon@emse.fr

ABSTRACT

The calcium sulfate-water vapor system is extremely relevant for a vast number scientific and industrial applications. Although the vast number of studies about this chemical system, some critical thermodynamic aspects seem to have been left aside. In this context, in the first part of this study, we investigated the thermodynamic equilibrium between two calcium sulfate polymorphs (AIII-CaSO₄ and CaSO₄ · 0.5 H₂O) and quantified the water vapor adsorption as a function of the temperature and water vapor partial pressure. In this second part, we employ a rigorous modeling approach to determine the thermodynamic nature of the water adsorption phenomena on these two polymorphs. We developed macroscopic solution models (ideal and non-ideal) for modeling monolayer adsorption on AIII-CaSO₄. This allowed the calculation of the energies of adsorption for this phenomenon, evidencing a physisorption mechanism. For the β -CaSO₄ · 0.5 H₂O, we interpreted the water adsorption using a multilayer adsorption model. For both materials, we showed that nitrogen adsorption data was not sufficient to represent their entire surface areas and porosity profiles compared to the water vapor sorption capacity of these materials.

KEYWORDS

adsorption, thermodynamics, phase equilibrium, calcium sulfate

1. Introduction

In the first part of this study, we reported an experimental study about the interaction between calcium sulfate polymorphs soluble anhydrite (AIII-CaSO₄) and calcium sulfate β -hemihydrate (β -CaSO₄ \cdot 0.5H₂O), both obtained from the dehydration of synthetic gypsum (CaSO₄ \cdot 2H₂O), and water vapor at atmospheric pressure. The equilibrium conditions between AIII-CaSO₄ and β -CaSO₄ \cdot 0.5H₂O in the presence of water vapor were confirmed and compared to available data in the literature. This equilibrium was also confirmed to be univariant. By thermogravimetric analysis under controlled temperature (T) and water vapor partial pressure (P_{H_2O}), we were also able to observe that compounds of the form CaSO₄ \cdot ϵ H₂O would show two bivariant zones as recalled in Figure 1. These two bivariant zones, a lower one (for $0 \le \epsilon \le 0.15$) and an upper one (for $\epsilon \ge 0.5$), were interpreted as caused by water adsorption on AIII-CaSO₄ and β -CaSO₄ \cdot 0.5H₂O, respectively. We observed that the extent of the water adsorption phenomena can be reasonably considerable when compared to the crystalline water content of both phases depending on the P_{H_2O} values. The lack of knowledge regarding these variations in water content could create uncertainties when manipulating or quantifying calcium sulfate based materials.

This second part of this study aims to analyze the nature of the water adsorption on each previously studied phase, AIII-CaSO₄ and β -CaSO₄ · 0.5H₂O, and to propose a physical interpretation for this phenomenon. For this, we plotted adsorption isotherms corresponding to each bivariant zone in Figure 1, and we compared the experimental data with thermodynamic models for monolayer and multilayer adsorption.

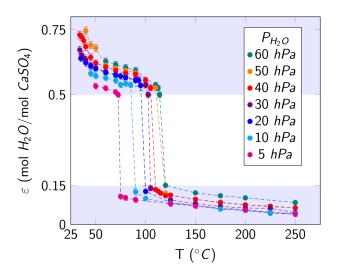


Figure 1. Isobars showing the overall water content ε of the calcium sulfate compounds as a function of the temperature (T) for fixed water vapor partial pressure (P_{H_2O}) values putting in evidence two bivariant zones (upper and lower) and a univariant transition zone (in the middle) (Shown in the first part of this study).

2. Thermodynamic models

Before analyzing the water adsorption phenomenon responsible for the bivariant behavior observed in the upper and lower bivariant zones in Figure 1, it is convenient to recall some principles. First of all, we consider the model for water vapor adsorption for which the gas molecules adsorb locally on identical points on the surface (adsorption sites) with no mobility within the adsorbed phase. That is, once the adsorbed molecule is fixed on an adsorption site, the surface of the solid becomes a network of free and occupied adsorption sites. At maximum surface coverage, all the adsorption sites are occupied forming a monomolecular layer. Everett also adds that considering the number of available adsorption sites to be independent of the temperature was observed as a satisfactory procedure to represent experimental data.^{2,3}

In this context, adsorption behaves like a surface solution of free and occupied adsorption sites for which the equilibrium equation writes⁴

$$S + G_{(g)} \rightleftharpoons SG_{(ads)}, \tag{1}$$

where S represents the free adsorption sites, $G_{(g)}$ the adsorbate in the surrounding gas phase, and $SG_{(ads)}$ the occupied adsorption sites. This equilibrium can be treated by a macroscopic solution model and the law of mass action for the equilibrium in (1 writes as follows

$$K_{eq} = \frac{x_{SG}\gamma_{SG}}{x_{S}\gamma_{S}P}$$
 (2)

where x_i and γ_i represent the molar fraction and the activity coefficient of the species i. The parameter P takes account of the pressure, and it is given by the ratio $P = P_G/P^\circ$, where P_G is the gas G partial pressure and P° is standard reference pressure (taken as the unit pressure).

This expression is usually simplified by the introduction of the surface coverage fraction θ . This parameter is given by the ratio between the concentration of occupied adsorption sites and the total concentration of adsorption sites. Therefore, the molar fractions in (2 can be expressed as $x_{SG} = \theta$ and $x_S = 1 - \theta$. Furthermore, for a first approximation, we consider the surface solution to be ideal. This approximation is often interpreted as the case for which there is no interaction between occupied adsorption sites. However, to be precise, this approximation assumes that interactions between occupied and free adsorption sites are identical to the interaction between two occupied adsorption sites. As a consequence, the activity coefficients are $\gamma_{SG} = \gamma_S = 1$ and (2 simplifies to the following expression where the pressure term P is homographic to the surface coverage

$$\theta = \frac{K_L P}{1 + K_L P} \tag{3}$$

This expression is similar to the well-known Langmuir isotherm equation used to interpret type I isotherms according to the classification of Brunauer, Deming, and Deming and Teller, normally

referred to as the BDDT or Brunauer classification, which was standardized by the IUPAC.⁵ For this reason, we replace the general equilibrium constant K_{eq} by K_L . The adsorption equilibrium constant K_L can then be written as follows

$$K_{L}(T) = K_{0} \exp\left(-\frac{E_{ads}}{RT}\right) \tag{4}$$

where R stands for the gas constant, K_0 represents a pre-exponential constant and E_{ads} accounts for the energy of adsorption. As an alternative, Everett considers this equilibrium constant as depending on the change in enthalpy and entropy of adsorption.^{2,5} For this case, the energy of adsorption would correspond to the change in enthalpy of adsorption $\Delta_a^0 H$, and the parameter K_0 would be a function of the change in entropy of adsorption $\Delta_a^0 S$. According to this approximation, these two parameters change with the surface coverage except for an assumption of an ideal surface solution and identical adsorption sites.⁶

Considering that surface coverage θ can also be defined as the ratio between the adsorbed molar quantity n_a per moles of solid and the monolayer capacity n_m per moles of solid, (3 can be rewritten as

$$\frac{n_a}{n_m} = \frac{K_L P}{1 + K_L P} \tag{5}$$

which is usually employed in its linear form

$$\frac{P}{n_a} = \frac{1}{K_L n_m} + \frac{P}{n_m} \tag{6}$$

These forms are useful to treat adsorption data because they allow the quick estimation of the energy of adsorption by using (4 from the fitted values of $K_L(T)$). The surface area S_σ of the solid in m^2/g is also easily assessed from the fitted values of monolayer capacity n_m and by considering the cross-sectional area σ of the adsorbing molecule according to the following expression

$$S_{\sigma} = \frac{n_{\rm m} \sigma N_{\rm Av}}{M_{\rm s}} \tag{7}$$

where N_{Av} is the Avogadro's number and M_s the molar mass of the solid.

Nevertheless, it is important to highlight that the physical meaning of the parameter n_m has to be considered with a degree of caution. This parameter was classically considered as a limiting adsorption uptake quantity due to a monolayer filling mechanism for type I isotherms. However, Rouquerol et al.⁵ and Gregg and Sing.⁷ discuss that in this context this value should preferentially be considered as a saturation capacity of the adsorbent due mostly to a micropore filling mechanism within pores that are accessible by the molecules of the adsorbate rather than the classic monolayer filling mechanism.

To address the issue of non-ideality of the surface solution into account and evaluate the validity of this hypothesis for the experimental data, we need a macroscopic solution model allowing the mathematical representation of the activity coefficients of surface solution species S and $SG_{(ads)}$ in (2. When the shift from ideal behavior is not large, it is reasonable to consider the approximation of regular solutions. Hence, the activity coefficients of each component of the surface solution can be expressed by the second-order Margules activity model as follows^{4,8,9}

$$\ln \gamma_{S} = B(T)x_{SG}^{2} = B(T)\theta^{2} \tag{8}$$

$$\ln \gamma_{SG} = B(T)x_S^2 = B(T)(1 - \theta)^2$$
 (9)

where B(T) is a parameter that depends on the temperature and the intermolecular lateral interactions within the solution. Using a microscopic approach from statistical physics, the coefficient B(T) of regular solutions is typically represented by⁴

$$B(T) = \frac{\alpha}{T} \tag{10}$$

where α is a temperature and composition dependent interaction term.

Substituting (8 and (9 in (2 gives the following expression:

$$K_{RS}P = \frac{\theta}{1 - \theta} \exp[B(T)(1 - 2\theta)] \tag{11}$$

where K_{eq} was replaced by K_{RS} (for the regular solution approximation) and the surface coverage is also given by $\theta = \frac{n_a}{n_m}$. This equation is also known as the Fowler-Guggenheim adsorption isotherm model. For this model, if B=0, we obtain the Langmuir adsorption model. For non-ideal solutions, the parameter B needs to be less than 2, otherwise, if $B \ge 2$, there is phase separation or no solution is formed at equilibrium (demixing case). Figure 2 shows a representation of adsorption isotherms for these different values of the parameter B. For $B \ge 2$ we observe that the same pressure P_{H_2O} show more than one θ value. This behavior has no physical meaning and indicates the case of solution demixing, as highlighted in zones D1 and D2.8-11

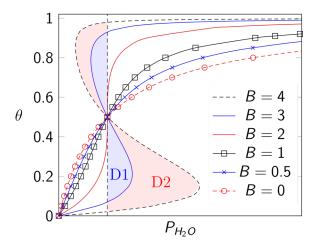


Figure 2. Water adsorption isotherms showing the evolution of the isotherm profile according to the value of the parameter B. Zones D1 and D2 indicate the cases for B > 2 in which there is demixing of the non-ideal solution.

The choice for the Margules activity coefficient model to express the non-ideality of the surface solution came from the use of the regular solution approach. As previously mentioned, this approach allows a relatively simple way of treating non-ideality of a solution when the behavior

does not differ much from the ideal one. However, there are many other more sophisticated and complicated activity coefficient models for liquid-vapor equilibrium (Redlich-Kister, Van Laar, NRTL, etc.) that can be used depending on the complexity of the system. ¹² Activity coefficients have also been expressed by temperature independent polynomial factors. ^{13,14}

Both models presented by (3 and (11 correspond to localized adsorption for which we consider the hypothesis of theoretical monolayer adsorption. These models are not adapted to represent adsorption isotherm profiles as for type II and type IV isotherms, which are normally interpreted as being produced by a multilayer adsorption mechanism for non-porous and mesoporous materials, respectively. For isotherms with these profiles, the Brunauer-Emmett-Teller (BET) theory for multilayer adsorption can then be employed to fit the adsorption curve and derive the BET area of the sample for each temperature condition. The BET equation is then given by the following expression

$$\frac{1}{n_{a}(1/P_{r}-1)} = \frac{1}{n_{m}C_{BET}} + \frac{C_{BET}-1}{n_{m}C_{BET}}P_{r}$$
 (12)

where P_r stands for the relative pressure (or relative humidity RH) and is given by the ratio $P_G/P_G^{sat}(T)$ ($P_G^{sat}(T)$) stands for the saturation pressure of the adsorbing gas for the isotherm temperature T). The coefficient C_{BET} is the BET parameter, and it is defined as an energetic term as follows

$$C_{BET} = \exp\left(\frac{-(E_{ads,1} - E_l)}{RT}\right)$$
 (13)

where $E_{ads,1}$ is the energy of adsorption of the first layer of adsorbed gas molecules, and E_l is the liquefaction energy for this adsorbed gas.

In rare cases, the adsorption isotherms profile is the product of only one type of adsorption phenomenon. That is, usually, adsorption isotherms are in fact an association of isotherms of

different types. For example, type II or type IV can commonly be associated with type I isotherms. This association means mean that pores with different size ranges are present within the analyzed sample. For instance, micropores could be present along with mesopores and macropores. For these cases, we observe the appearance of a classic "knee" in the isotherm profile indicating the filling of micropores (type I) before a change in concavity due to multilayer adsorption (type II or IV). The BET theory is typically applied for purely type II or type IV isotherms for the relative pressure range of $0.05 \le P_r \le 0.30$ and normally reaches its limitations for microporous materials. This would restrain the use of this theory to estimate the BET area of association of isotherms. However, some authors argued that this method can still give representative information about the pores and surface of the sample. Mooney et al. argued about the use of the BET theory to model combined type I and type II water vapor adsorption isotherms as long as the usual requirements (relative pressure ranges) are fulfilled. 16,17 According to the criteria published by Llewellyn et al., we are still able to consider the BET area as a "BET strong retention capacity" or "saturation capacity" of the material if two criteria are respected: (i) the value of C_{RET} must be positive for the range of points chosen for the calculation and (ii) the term $n_a \left(P_{H_2O}^{sat} - P_{H_2O}\right)$ must continuously increase (self-consistency criterion).¹⁸

The described methods were applied to interpret the adsorption phenomenon for AIII-CaSO₄ and β -CaSO₄ · 0.5H₂O. We chose isotherms for six temperature values in each bivariant zone in Figure 1 to analyze the nature of this phenomenon and have a broad description of each zone instead of working with adsorption at only one temperature as most of the studies aiming only at calculating specific surface areas.

3. Application of thermodynamic methods and discussion

3.1. Thermodynamic modeling of water adsorption on soluble anhydrite. The profiles of the adsorption isotherms for the AIII-CaSO₄ corresponding to the lower bivariant zone ($0 < \epsilon < 0.15$) in Figure 1 are shown in Figure 5 for six temperature values. These values were chosen to provide a relatively broad description of this bivariant zone. The isotherm profiles are analogous to homographic curves presenting a saturation plateau. This corresponds to type I isotherms according to the BDDT classification. Therefore, we initially evaluated the hypothesis of localized monolayer adsorption with ideal behavior. This case is represented by the Langmuir adsorption model shown by (3. The quantity of water ϵ is considered to correspond entirely to adsorbed water because the sample is constituted of the anhydrous crystalline phase AIII-CaSO₄. Therefore, we take $\epsilon = n_a$ for this data set.

Figure 3 shows the linear transform of the adsorbed quantity values and the fitted curves obtained by using (6. These linear transforms were used to fit the values of n_m and K_L shown in Table 1 and Figure 4. Overall, the localized monolayer ideal adsorption model represents the experimental data points and their trends with more dispersion between experimental and fitted values for higher temperatures. To better evaluate the overall validity of the assumptions taken into account by this model, we analyzed the values of the fitting parameters n_m and K_{eq} and the adsorption isotherms plotted in Figure 5.

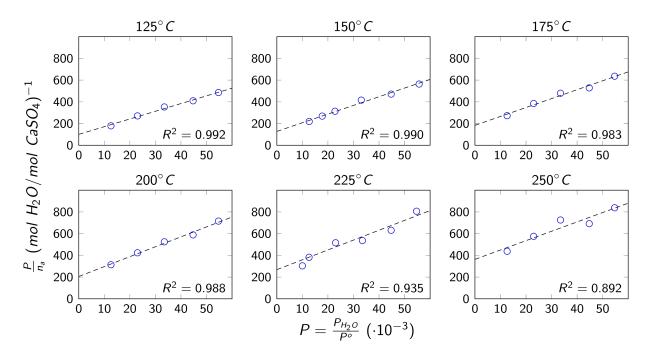


Figure 3. Langmuir linear transformation of the adsorption isotherms compared to the experimental points. The fitted curves represented by the dashed lines are used to calculate the parameters $n_{\rm m}$ and $K_{\rm L}$.

Table 1. Fitting parameters for the localized monolayer ideal adsorption hypothesis (Langmuir adsorption).

T (°C)	K_L	n _m (mol H ₂ O/mol CaSO ₄)	$S_{\sigma}(H_20) (g/m^2)$
125	70.6	0.141 ± 0.007	78 ± 4
150	62.5	0.125 ± 0.006	69 ± 3
175	44.7	0.122 ± 0.006	68 ± 3
200	44.4	0.109 ± 0.005	60 ± 3
225	33.8	0.110 ± 0.005	61 ± 3
250	23.7	0.116 ± 0.005	64 ± 3

The fitting parameter n_m is listed in Table 1 and plotted in Figure 4(a) as a function of the temperature. We observe a sensible decreasing trend for this parameter with stabilization between 200°C and 250°C. As previously mentioned, this parameter is usually assumed to be constant or independent of the temperature. Therefore, the variation observed for this parameter can perhaps be associated with the non-ideality of the surface solution (presence of interactions between molecules) or due to surface heterogeneities. The non-ideality effect is further evaluated. The monolayer capacity can be used to estimate specific surface area values ranging from $S_{\sigma}(H_20)$ = $(78 \pm 4) \text{ m}^2/\text{g}$ to $S_{\sigma}(H_2O) = (60 \pm 3) \text{ m}^2/\text{g}$ (considering an average cross-sectional area for the water molecule¹⁹ of $\sigma = 0.125 \text{ nm}^2$ and molar mass of anhydrous CaSO₄ as 136.14 g/mol). We can estimate an average surface area of $\overline{S_{\sigma}(H_2O)}=(66\pm5)\,\text{m}^2/\text{g}$. These surface area measurements can be compared to measurements obtained by nitrogen adsorption data and calculations performed using the BET theory. Figure S2 in the supporting information file shows the results of nitrogen adsorption and desorption isotherms obtained at 77K for one sample after dehydration at 200°C. As the isotherm presents a type II profile with an almost negligible hysteresis loop, we calculate the nitrogen BET area of the material as corresponding to $S_{BET}(N_2) = (14 \pm 1) \text{ m}^2/\text{g}$ ($C_{BET} = 63$). This value is almost 5 times inferior to the average value obtained from water vapor adsorption data. This difference can be associated with the fact that nitrogen might not access to the entire pore network because of its larger molecular size when compared to water vapor. Nitrogen molecules are considered to have a cross-sectional area of 0.162 nm², which is reasonably more significant than the water molecules cross-sectional area of 0.125 nm². Therefore, water molecules would more easily gain access to micropores with reduced dimensions (such as the supermicropores with a pore diameter between 2 and 0.7 nm) in contrast to nitrogen molecules.²⁰ This different behavior of the material in the presence of water compared

to the nitrogen is also sustainable considering the t-plot curve for the nitrogen adsorption data. The nitrogen adsorption results are indeed characteristic of non-porous materials and, as a consequence, they do not show the same textural properties as the water vapor adsorption data, which indicate the behavior of a microporous material. Furthermore, this kind of discrepancy in adsorption results obtained by different gases has been observed several times in the literature. Other authors such as Hagymassy et al.²¹, Mooney et al.^{16,17}, Médout-Marère et al.²², and Salles et al.23 have shown that porous materials such as concrete, cement, silica, and clays show more important sorption of water vapor than nitrogen. Gregg and Willing have also shown that during the decomposition of calcium sulfate dihydrate, different gases (oxygen, nitrogen, CCl₄, water, etc.) are adsorbed to different extents for the same material.^{24–26} As a consequence, the analysis of the surface area and the porosity by nitrogen adsorption at 77K, techniques that are typically employed and mastered for materials characterization, showed not to be sufficiently adapted to understand the water adsorption capabilities of AIII-CaSO₄. As a complement to the observations in this study, to verify the full porosity range water molecules have access to, it would be interesting to perform a full adsorption isotherm for water vapor. That is, analyzing the water adsorption capacity of the materials for a large P_{H2O} range, from almost completely dry conditions to near saturation pressure. However, this was not technically feasible using our experimental apparatus (which is limited to water vapor partial pressures up to 60 hPa) as detailed in the first part of this study. 1 Moreover, as phase transition towards CaSO₄ · 0.5H₂O can take place as the P_{H2O} increases, which would limit a full adsorption spectrum of the AIII-CaSO₄. Other interesting experiments to carry out to elucidate the different accessibility of gases in the pore network of AIII-CaSO₄ would be performing systematic adsorption experiments with different gases showing diverse cross-sectional areas and polarity.

Other reason that could explain the observed shift between water and nitrogen uptakes by adsorption could be that the partial pressure of water vapor can increase locally in pores and thus induce capillary condensation of water. This phenomenon could produce local hydration reactions near the surface of the solid and eventually locally hydrate the sample of AIII-CaSO₄ to CaSO₄ \cdot 0.5H₂O at pore walls increasing the retention capacity of water of the solid. This local effect would be complicated to measure experimentally, but the estimation of pore saturating pressures (based on pore dimensions) could be compared to the values of P_{H_2O} and T for phase transition to verify the plausibility of this phenomenon as further work.

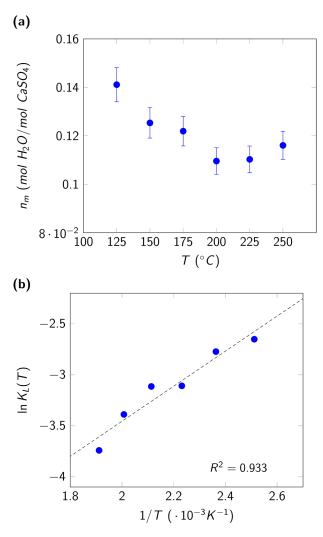


Figure 4. Fitting parameters n_m and K_L for the localized monolayer ideal adsorption model. (a) The monolayer capacity n_m is shown to decrease sensibly with temperature. (b) van't Hoff plot for the Langmuir adsorption equilibrium constant.

The second fitting parameter K_L is presented in the form of a van't Hoff plot in Figure 4(b). The energy of adsorption was estimated as $E_{ads} = -16.5 \text{ kJ} \cdot \text{mol}^{-1}$. As expected for an adsorption process, $E_{ads} < 0$ (evidencing an exothermic process). Moreover, the low value of $|E_{ads}| < 20 \text{ kJ} \cdot \text{mol}^{-1}$ confirms the hypothesis of a physisorption process as previously considered to develop this model. The overall quality of fit presented in the van't Hoff plot in Figure 4(b) shows

a linear trend with some dispersion. This can be caused by experimental effects combined with, as previously mentioned, non-ideal effects within the surface solution.

Finally, we chose to use the maximum value of monolayer coverage in Table 1 (i.e., $n_m = 0.141 \text{ mol H}_2\text{O/mol CaSO}_4$) to plot the adsorption isotherms and compare these curves as shown in Figure 5. The calculated curves represent the overall trend for each temperature, but with some shifts. These shifts are evidently produced by the difference between the used monolayer capacity value and the obtained fitted values for each temperature. To improve the quality of the fit for each curve, we evaluated the hypothesis of a non-ideal surface solution.

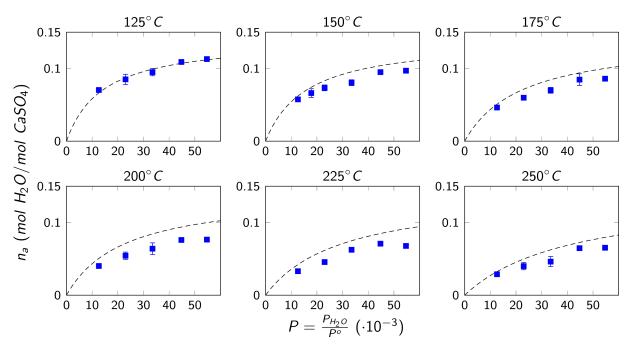


Figure 5. Isotherms for the adsorbed quantity of water n_a on AIII-CaSO₄ for temperatures between 125°C to 250°C. The results are presented as a function of P (the ratio between the water vapor partial pressure P_{H2O} and the reference unit pressure P^o, both in atm). The localized monolayer ideal adsorption model (dashed lines plotted using the maximum monolayer capacity fitted value) is compared to the experimental points (blue squares).

To address the issue of non-ideality of the surface solution into account and evaluate the validity of this hypothesis for interpreting the experimental data, we employed a macroscopic solution model to express the activity coefficients of its components. When the shift from ideal behavior is not considerably large (as observed in Figure 4 and Figure 5), it is reasonable to consider the approximation of regular solutions. We employed then the mathematical expression shown by (11, which is based on the Margules activity model. To evaluate this model for the presented adsorption isotherms, we considered the number of adsorption sites to be constant and took the maximum value of monolayer coverage, $n_{\rm m}=0.141~{\rm mol}~{\rm H_2O/mol}~{\rm CaSO_4}$, calculated for the ideal surface solution case. Figure 6 shows the comparison of the calculated surface coverage data plotted with the fitted curves. Table 2 shows the fitting parameters $K_{\rm RS}$ and B and also the calculated values of α according to (10. Parameters α and $K_{\rm RS}$ are graphically represented in Figure 7.

Initially, we observe that the fitted curves in Figure 6 correspond more adequately to the experimental points for each temperature value compared to the previous model. Therefore, the consideration of an additional fitting parameter that takes account of the non-ideality of the surface solution is suitable for the considered system. This parameter considers the interaction energies between adsorption sites not be equivalent.

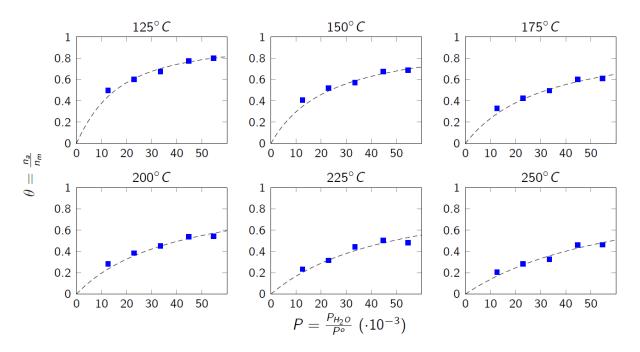


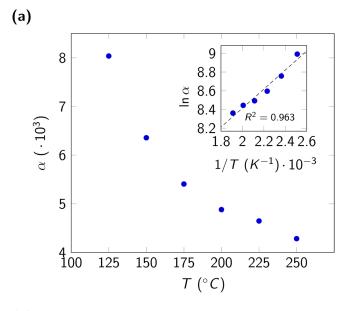
Figure 6. Adsorption isotherms for phase AIII-CaSO₄ for temperatures between 125°C to 250°C. The results are presented as a function of P (the ratio between the water vapor partial pressure P_{H2O} and the reference unit pressure P^o). The localized monolayer adsorption model combined with the regular solution approach (dashed-line fitted curves) is compared to the experimental points (blue squares).

Figure 7(a) shows that the interaction parameter α decreases with increasing temperature. This would indicate that the interaction forces between sites occupied with adsorbed molecules of the surface solution (and by consequence the shift from ideal behavior) are more important at lower temperatures. The miniature in Figure 7(a) shows the parameter α in Arrhenius coordinates. Due to the observed linearity, we can propose the following expression for α

$$\alpha = \alpha_0 \exp\left(\frac{\Gamma}{RT}\right)$$
 Eq. 14

where Γ is a thermal coefficient and α_0 a pre-exponential factor. This expression can be useful if we want to propose a predictive expression for α based on empirical observation ($\Gamma = 8.5 \text{ kJ} \cdot \text{mol}^{-1}$ and $\ln \alpha_0 = 6.4$).

Figure 7(b) shows the van't Hoff plot for K_{RS} . We observe that the experimental points show less dispersion than for the ideal surface solution approach. We can also estimate the energy of adsorption value as $E_{ads} = -18.0 \text{ kJ} \cdot \text{mol}^{-1}$. The negative and low value of this energy is following previous hypotheses of exothermic processes and physisorption. Besides, this value is not very different compared to the one obtained previously evidencing the small shift in behavior compared to the ideal surface solution hypothesis. Finally, we recall that the chosen regular solution model implies phase separation for B(T) > 2. Hence, the fitted values of B(T) shown in Table 1 confirm the thermodynamic feasibility of the surface solution.



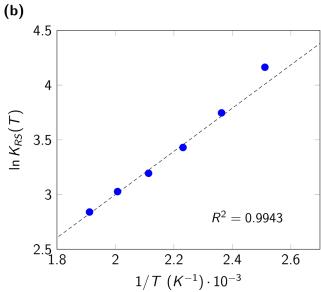


Figure 7. Fitting parameters α and K_{RS} for the localized monolayer non-ideal adsorption model: (a) α as a function of the temperature (miniature: Arrhenius coordinates) and (b) van't Hoff plot for the fitting parameters K_{RS} for the non-ideal surface solution model.

Overall, the hypothesis of the non-ideal surface solution represented by the regular solution hypothesis improves the quality of the fitted curves and fitted parameters compared to the ideal surface solution approach. The behavior of water adsorption on AIII-CaSO₄ is well described by

the hypothesis of monolayer adsorption where the heterogeneities within the interactions of the surface solution components play a part in this phenomenon. Depending on the objective of the analysis, a predictive equation giving the adsorbed quantity can be proposed to represent the experimental data in the given range respecting the experimental errors.

Table 2. Fitting parameters for non-ideal surface solution (regular solution approach)

T (°C)	K _{RS}	В	α
125	64.3	$2.31 \cdot 10^{-1}$	8040
150	42.4	$9.75 \cdot 10^{-3}$	6360
175	30.9	$6.13 \cdot 10^{-3}$	5410
200	24.4	$8.96 \cdot 10^{-4}$	4880
225	20.7	$3.46 \cdot 10^{-2}$	4650
250	17.2	$9.03 \cdot 10^{-2}$	4280

3.2. Thermodynamic modeling of water adsorption on β -hemihydrate. Figure 8(a) shows the isotherms representing the overall water contents for temperature values between 45°C and 90°C in the upper bivariant zone in Figure 1. Analogously as the previous section, we used six temperatures values to run through the different possible behaviors of the water vapor adsorption within the bivariant zone for which $\epsilon \geq 0.5$. Two main kinds of profiles can be distinguished. At first, the curves observed for temperature values from 45°C to 70°C present a change in concavity and recall the profiles for type II or type IV isotherms according to the BDDT classification. On the other hand, the curves for 80°C and 90°C do not present the same change in concavity and recall a homographic profile of type I (with a saturation plateau).

To analyze this observed behavior, we first consider the group of curves for which the profiles show a change in concavity, i.e., from 45°C to 70°C. Even though we are limited in terms of the

experimental pressure range (5 to 60 hPa), these isotherms seem to be typical of non-porous or mesoporous materials, corresponding to type II and IV isotherms, respectively. The BET theory for multilayer adsorption can then be employed to analyze the behavior of this material and derive the water vapor BET area $S_{BET}(H_2O)$ of the sample for each temperature condition. To apply this equation, we reasoned similarly as for water vapor adsorption on AIII-CaSO₄. The overall quantity of water ε measured in the upper bivariant region was considered to have two contributions: one by crystalline water content and the other by the adsorbed water content. For the $CaSO_4 \cdot 0.5H_2O$, the crystalline water content is equal to 0.5 mol H₂O/mol CaSO₄. Therefore, the adsorbed water content can be expressed as $n_a = \varepsilon - 0.5$. We then plotted these experimental values of the adsorbed water content na as a function of the relative pressure Pr as shown in Figure 8(b). As expected, we observe that with increasing temperature we reduce the relative pressure interval for the isotherm (because the saturation pressure value increases systematically). For this reason, for the lower temperature values, from 45°C to 70°C, we manage to apply the BET equation (cf. (12). However, for the higher values of temperature, 80°C and 90°C, the relative pressure interval is too reduced to consolidate the type II or IV behavior of the isotherm and apply the BET equation accordingly. Figure S4 in the supporting information section shows the BET plots for temperature values from 45°C to 70°C from which we obtained the parameters shown in Table 3. Figure S5 shows the self-consistency plots for this same temperature interval, and they respect the criteria recalled in the methods section.¹⁸ Using these parameters we could trace the BET adsorption isotherms from 45°C to 70°C as shown in Figure 8(a) and Figure 8(b) by the dashed lines. For the temperature values of 80°C and 90°C, the presented dotted lines in Figure 8(a) are only a guide for the eyes to evidence the different observed profile.

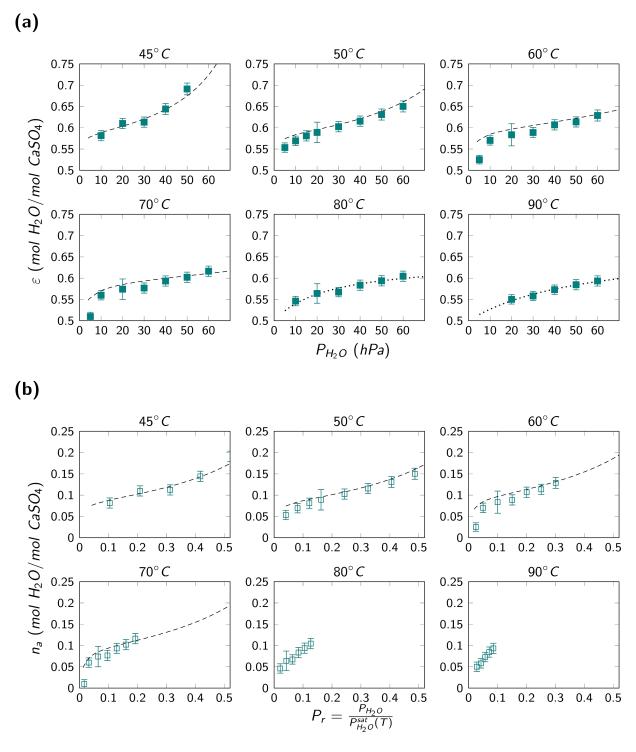


Figure 8. Isotherms for the (a) overall quantity of water of β- CaSO₄ \cdot 0.5H₂O and (b) adsorbed water contents on β- CaSO₄ \cdot 0.5H₂O for temperatures between 45°C to 90°C.

Overall, we observe that the BET equation represents well the experimental data for the temperature values from 45°C to 70°C. However, we observe a shift between the model and the experimental points for low relative pressure values. We can observe that the experimental curves present a sharp change in concavity for these low values of P_r (or a "knee", as usually referred to in the literature) at the beginning of the isotherm, and these profiles are normally associated with the phenomenon of micropore filling. This effect is more evident for the temperatures from 50°C to 70°C. This "knee" frequently represents that these isotherms are, in fact, an association of type II or type IV along with a type I isotherm. Usually, the BET theory reaches its physical limits for microporous materials. However, as the two criteria published by Llewellyn et al. ¹⁸ were verified, the n_m parameter and the calculated BET area do present a physical meaning and are suitable to represent the water retention capacity of the sample for each given temperature value.

We also observe that the calculated value for the monolayer capacity n_m and the BET area values increase with temperature. It ranges from $S_{BET}(H_2O) = 46 \text{ m}^2/\text{g}$ for 45°C to $S_{BET}(H_2O) = 61 \text{ m}^2/\text{g}$ for 70°C. This would mean that for higher temperatures, more water is required to completely fill the pores of the sample. This effect is may be that at higher temperatures the pores of the material are more available to water adsorption compared to lower temperatures. We also observed that the C_{BET} parameter decreases with increasing temperature. This would represent that the BET theory less adequately represents the behavior of the system at these temperatures. Finally, the non-ideality of the adsorbed layer (or surface solution) can also be compensated by these fitting parameters.

Finally, we notice a similar effect when comparing the water vapor and nitrogen adsorption phenomena, like the one observed for AIII-CaSO₄. Figure S3 in the supporting information document shows the results for one nitrogen adsorption and desorption isotherm obtained at 77K

for one sample of β -hemihydrate. This estimated BET area of the material was $S_{BET}(N_2)$ = $(7.3 \pm 1.6) \,\mathrm{m^2/g} \,(C_{BET} > 100)$. Therefore, we observed that the values of $S_{BET}(H_2O)$ in Table 3 are much superior to the nitrogen BET area S_{BET}(N₂). The t-plot for the hemihydrate shown in Figure S3 also shows the weak retention of nitrogen by micropores when compared to the water vapor adsorption. Therefore, the nitrogen adsorption data supports a non-porous material in contrast to water adsorption data that evidences the presence of micropores. These micropores would be preferentially accessible by molecules smaller than nitrogen, such as water. In other words, the water molecules seem to have access to a more extended surface than nitrogen molecules. Therefore, similar discussions as proposed for the adsorption on AIII-CaSO₄ are also convenient for the β -CaSO₄ · 0.5H₂O. For example, the broadly used nitrogen adsorption techniques seem to be insufficient to represent the whole extent of the β - CaSO₄ \cdot 0.5H₂O textural properties. To obtain more reliable and complete data about the surface area and the pore network of this material, it would also be interesting to perform complete water vapor adsorption isotherms for the given temperatures with relative water vapor pressure (or relative humidity) values up to near saturation values. Using different adsorbing gases could also increase the comprehension of the textural properties of β -hemihydrate.

Furthermore, we observe that the specific surface area values estimated by water adsorption for β -hemihydrate (between 46 and 61 m²/g) are sensibly inferior to the ones calculated for AIII-CaSO₄ (between 60 and 78 m²/g). This difference may be produced by the fact that the hydration reaction decreases the number of open pores for adsorption due to the increase in the crystalline water content. This also may be caused by the structural change taking place during the phase transition between these two polymorphs.

The main differences between the considerations for adsorption on AIII-CaSO₄ compared to the lower temperature isotherms obtained for β -CaSO₄ \cdot 0.5H₂O reside in the adsorption mechanism. Water vapor adsorption seems to proceed with a multilayer adsorption mechanism with the likely presence of micropores.

Finally, other mathematical models for adsorption on microporous-mesoporous materials can be found in the literature. However, they present little gain in physical interpretation compared to the BET model. For temperatures of 80°C and 90°C, we observe that due to restricted relative pressure range we could only obtain the beginning of their isotherms. This made it difficult to describe the general profile of the adsorption isotherms for these conditions.

Table 3. Parameters obtained from the application of the BET model for isotherms from 45°C to 70°C

٠	T (°C)	C_{BET}	n _m (mol H ₂ O/mol CaSO ₄)	$S_{BET}(H_2O) (m^2/g)$
	45	141	$8.40 \cdot 10^{-2}$	46
	50	144	$8.30 \cdot 10^{-2}$	45
	60	110	$9.40 \cdot 10^{-2}$	51
	70	77.5	$1.11\cdot 10^{-1}$	61

4. Conclusions

This was the second part of a two-part study about the thermodynamic aspects of the thermodynamic equilibrium between water vapor and two calcium sulfate polymorphs, AIII- $CaSO_4$ and β - $CaSO_4 \cdot 0.5H_2O$, obtained from the dehydration of gypsum. The first part consisted in the experimental determination of the equilibrium conditions between these two compounds and the quantification of the water adsorption phenomenon. The second part aim was to propose

physical interpretation for the observed adsorption phenomena by means of thermodynamic modeling of the experimental adsorption isotherms.

For AIII-CaSO₄, we proposed models of localized monolayer adsorption and the adsorbed layer was considered as a solution between free and occupied adsorption sites. Initially, we assumed ideal behavior of the surface solution and employed the Langmuir adsorption model to fit it. This model was not sufficient to represent the integrality of the adsorption isotherms and the fitted parameters presented some dispersion. Afterwards, the fitting was improved by the assumption of non-ideal behavior of the surface solution and the introduction of a parameter to take account of the interactions between the solution components. For both methods the values of the energy of adsorption were considerably low and confirmed an initial hypothesis of physisorption.

For β-CaSO₄ · 0.5H₂O, the water adsorption was modeled assuming multilayer adsorption. The adsorption isotherm profiles for temperature from 45°C to 70°C were not homographic as the ones for AIII-CaSO₄ and we employed the BET theory to analyze them. We observed shifts between the BET theory and the experimental points for low relative pressure ranges and attributed these effects to the presence of micropores in the matrix of the material. Isotherms for temperatures of 80°C and 90°C were left out of the modeling because they did not present a sufficiently large range of relative pressure to assess their characteristics.

For both materials, we observed an important effect concerning the differences between specific surface and profile of the adsorption isotherm for water vapor and nitrogen. The adsorption profiles obtained for water adsorption were typical of microporous materials. However, nitrogen adsorption data obtained at 77 K showed a profile for non-porous materials. Furthermore, the surface area values calculated from water adsorption data (either $S_{\sigma}(H_2O)$ for AIII-CaSO₄ or $S_{BET}(H_2O)$ for β -CaSO₄ · 0.5H₂O) were several times larger than the values $S_{BET}(N_2)$ obtained

by nitrogen adsorption data. This was interpreted as possibly caused by the fact that water molecules have reduced dimensions and may access smaller pores when compared to nitrogen molecules. Other effects of capillary condensation could also play a role in this phenomenon.

ASSOCIATED CONTENT

The following files are available free of charge.

Additional characterization data for the initial sample and for its dehydration product at 200°C is provided in **Support Preturlan JGD.PDF**

AUTHOR INFORMATION

Corresponding Author

E-mail: favergeon@emse.fr

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NOMENCLATURE

T Temperature (°C)

P_{H2O} Water vapor partial pressure (hPa)

S Free adsorption sites

 $G_{(g)}$ Adsorbing gas

SG_(ads) Adsorption site occupied by a gas molecule

K_{eq} Equilibrium constant

x_i Molar fraction of species i

γ_i Activity coefficient of species i

P Fugacity of gas

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P_G Partial pressure of adsorbing gas G

P° Reference pressure (normally taken as the unit pressure)

R Universal gas constant (= $8.314 \text{ J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$)

 θ Surface coverage fraction

K_L Langmuir equilibrium constant (ideal solution)

K_{L.0} Pre-exponential constant for Langmuir adsorption isotherm model

 E_{ads} Adsorption energy $(J \cdot mol^{-1} \cdot K^{-1})$

n_a Adsorbed quantity (mol H₂O/mol CaSO₄)

n_m Monolayer capacity (mol H₂O/mol CaSO₄)

 S_{σ} Specific surface area $(m^2 \cdot g^{-1})$

 $S_{BET}(N_2)$ BET area calculated from nitrogen adsorption data $(m^2 \cdot g^{-1})$

 $S_{BET}(H_2O)$ BET area calculated from water vapor adsorption data $(m^2 \cdot g^{-1})$

N_{Av} Avogadro's number

 M_s Molar mass $(g \cdot mol^{-1})$

B Margules interaction parameter

α Interaction parameter

 α_0 Pre-exponential factor

 Γ Thermal coefficient (kJ · mol⁻¹)

K_{RS} Equilibrium constant from regular solution approximation (non-ideal adsorption)

P_r Relative pressure

P_G^{sat}(T) Saturation pressure of gas G

C_{BET} BET constant

GREEK LETTERS

 ϵ Overall water content (mol H₂O/mol CaSO₄)

 σ Cross-sectional area of an adsorbing gas molecule (nm²)

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