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# Fall-back time for photo-ionized Cs atoms attached to superfluid $^4\text{He}$ nanodroplets

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**Abstract.** We have studied the dynamic evolution of a Cs atom photo-excited from 6s to 6p and 7s states on a helium droplet using time-dependent  $^4\text{He}$ -DFT simulations. Depending on the excited electronic state, the Cs impurity remains on the droplet surface or it is ejected. Upon subsequent photo-ionization of the excited Cs atom the resulting  $\text{Cs}^+$  cation may either be ejected or come back to the droplet, depending on the time delay between photo-excitation and photo-ionization. We have calculated the critical time delay separating these two different behaviors, as well as final ion velocities. These observables will be used for future comparison with planned pump-probe experiments.

**PACS.** 36.40.-c Atomic and molecular clusters – 78.40.-q Absorption spectra of impurities

## 1 Introduction

He nanodroplets are often considered the “ideal spectroscopic matrix” owing to their extraordinary properties [1]. Their extremely low intrinsic temperature (0.37 K) leads to efficient cooling of embedded impurities (atoms, molecules, clusters, nanostructures); their chemical inertness makes He nanodroplets a weakly perturbing environment that allows to record highly resolved molecular spectra [2]; due to their superfluid nature, embedded impurities are mobile and readily aggregate into clusters and complexes inside He nanodroplets. However, this concept of a weakly perturbing environment is challenged when impurities are electronically excited or ionized using visible up to extreme ultraviolet radiation [3]. Absorption spectra of droplet-embedded atoms and molecules are often massively blue-shifted and broadened due to Pauli repulsion of the excited orbital from the surrounding helium. This repulsion tends to induce the formation of a void bubble around the excited dopant and even its ejection out of the droplet [4–7].

Alkali (Ak) atoms attached to superfluid helium droplets are known to reside in a dimple at the surface of the droplet, an experimental fact well reproduced by Density Functional Theory (DFT) calculations [8–10]. Electronic excitation of the impurity triggers a rich relaxation dynamics in the  $\text{Ak}@^4\text{He}_N$  complex. Owing to the repulsion of the excited electron from the helium droplet, most alkali

disassociate from the droplet under  $np \leftarrow ns$  excitation, either as a bare atom or with one or a few atoms attached to it (so-called “exciplexes”) [3, 11, 12]. The heavier ones, Rb and Cs, exhibit a more complex behavior. A Cs atom photo-excited from the 6s to the 6p state or a Rb atom upon  $5p \leftarrow 5s$  excitation can be ejected as a bare atom or as an exciplex, or remain at the droplet surface [13, 14].

If the excited cesium atom, here denoted as  $\text{Cs}^*$ , is ejected and it is subsequently photo-ionized, the  $\text{Cs}^+$  cation can keep dissociating as a bare cation or as a  $\text{He}_n\text{Cs}^+$  complex, or fall back onto the droplet, eventually sinking into it [15, 16]. Whether the cation is ejected or sinks into the droplet interior depends on the delay time  $\tau_D$  between excitation and ionization. Helium-positive charge interaction is attractive, hence the cation tends to be solvated. This is the case if ionization occurs at short  $\tau_D$ , when  $\text{Cs}^*$  is still close enough to feel the attraction from the droplet and has not acquired too much kinetic energy. On the other hand, for large  $\tau_D$ ,  $\text{Cs}^+$  will keep dissociating because  $\text{Cs}^*$  has already traveled a long distance and acquired a large amount of kinetic energy, so that the attractive He-cation interaction is not strong enough to make it turn around. The critical time  $\tau_c$  separating both processes has been termed fall-back time [17].

The real-time dynamics of the photo-excitation of Rb atoms to the 5p and 6p states and their subsequent photo-

ionization has been investigated using femtosecond imaging spectroscopy and helium time-dependent density functional theory (He-TDDFT) [18]. It was shown that the desorption dynamics of the  $\text{Rb}^*$  excited atom proceeded on very different time scales depending on the excited state, about  $\sim 1$  ps for  $6p$   $\text{Rb}^*$  and  $\sim 100$  ps for  $5p$   $\text{Rb}^*$ . Comparison between theory and experiment indicated that desorption was either impulsive ( $6p$ ) or in an intermediate regime between impulsive dissociation and complex desorption ( $5p$ ). These studies have stressed the interpretation of the pump-probe dynamics in terms of competition between the repulsion of the excited Rb atom from the droplet on the one hand, and the attraction of the  $\text{Rb}^+$  ion to the droplet on the other [17, 18]. The combination of femto-second pump-probe spectroscopy and velocity map imaging has proved crucial to disentangle the process of complex formation, desorption and ion solvation dynamics.

He-TDDFT has naturally become the tool of choice for the analysis of real-time processes involving impurities in helium droplets [7, 12, 19, 20], emerging as a compromise between accuracy and numerical feasibility. The aim of this work is to extend our theoretical study on Rb atoms on  $^4\text{He}$  droplets [17, 18, 21], to the next heavier Ak, namely Cs, as both species can be studied within the same approach. In particular, we address here Cs atoms excited to the  $6p$  and  $7s$  states. So far, there is no experimental information available for the photo-excitation of Cs atoms followed by their photo-ionization in order to determine the fall-back time. The present calculations may help guide these experiments.

This work is organized as follows. In Sec. 2 we describe the model employed to address the statics and real-time dynamics of a Cs atom photo-excited on the surface of a He droplet. Results for the two excited states ( $6p$  and  $7s$ ) studied here are discussed in Sec. 3, and a short summary is presented in Sec. 4.

## 2 Model

### 2.1 Statics

We have considered a droplet made of  $N = 1000$  helium atoms and have first obtained the structure of the neutral Cs-droplet complex in the ground state. Due to the large mass of cesium compared to that of helium, we describe the Cs atom and its cation as classical particles. As a result, their effect on the statics amounts to an external field acting upon the droplet [21, 22].

Within the He-DFT approach at zero temperature ( $T$ ), the energy of a  $N$  atoms helium droplet  $^4\text{He}_N$  is written as a functional of the helium particle density including an impurity-helium interaction term

$$E[\Psi] = \int d\mathbf{r} \left\{ \frac{\hbar^2}{2m_{\text{He}}} |\nabla\Psi|^2 + \mathcal{E}_c(\rho) \right\} + \int d\mathbf{r} \rho(\mathbf{r}) V_X(|\mathbf{r}_{\text{Cs}} - \mathbf{r}|), \quad (1)$$

where  $\mathbf{r}_{\text{Cs}}$  is the impurity location,  $\Psi(\mathbf{r})$  is the effective wave function of the superfluid such that  $\rho(\mathbf{r}) = |\Psi(\mathbf{r})|^2$ , and the functional  $\mathcal{E}_c(\rho)$  contains the interaction term within the Hartree approximation and additional terms describing non-local correlation effects [12]. The  $\mathcal{E}_c[\rho]$  functional used in the present work is a modified version of the Orsay-Trento functional [23] able to handle very structured helium configurations such as those expected to appear around fairly attractive impurities [24]. The Cs-He ground state pair potential  $V_X$  has been taken from [25].

Upon variation of Eq. (1) one obtains the equation to determine the equilibrium density  $\rho_0(\mathbf{r})$  of the droplet and the location of the dopant atom  $\mathbf{r}_{\text{Cs}_0}$

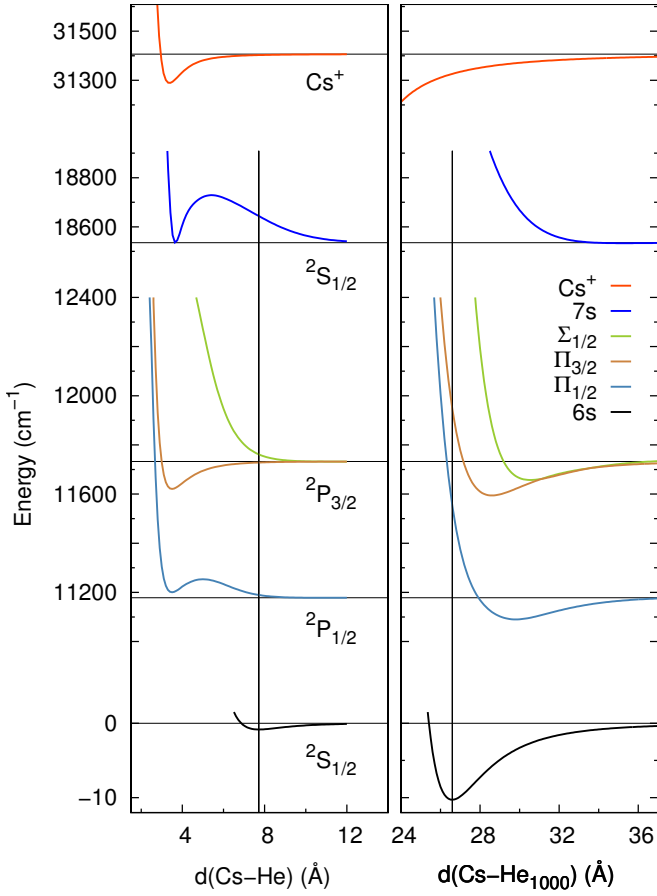
$$\left\{ -\frac{\hbar^2}{2m_{\text{He}}} \nabla^2 + \frac{\delta\mathcal{E}_c}{\delta\rho} + V_X(|\mathbf{r}_{\text{Cs}} - \mathbf{r}|) \right\} \Psi_0(\mathbf{r}) = \mu \Psi_0(\mathbf{r}), \quad (2)$$

where  $\mu$  is the chemical potential of the He droplet. Equation (2) has been solved in Cartesian coordinates using the  $^4\text{He}$ -DFT BCN-TLS computing package [26], see [12, 27] and references therein for additional details. We have used a space-step of  $0.4 \text{ \AA}$ .

A two-dimensional view of the dimple state configuration of the Cs atom can be seen in Fig. 3 of [9]. The Cs atom is located  $26.6 \text{ \AA}$  away from the center of mass of the droplet, whose sharp density radius is  $22.2 \text{ \AA}$ .

Since Cs detachment will be caused by photo-excitation, it is convenient to evaluate the  $6p \ ^2P \leftarrow 6s \ ^2S$  and the  $7s \ ^2S \leftarrow 6s \ ^2S$  absorption spectra to have a precise idea of the energetics of the process. This was done using the DF sampling method [28] with the He-Cs\*  $6p \ \Sigma$  and  $\Pi$  and the  $7s$  pair potentials of [29]. In the case of  $6p$  excitation spin-orbit (SO) coupling had to be taken into account. It was assumed to be independent of the He-Cs distance [30, 31], its intensity being set to reproduce the spin-orbit splitting of bare Cs in the  $6p \ ^2P$  state, namely  $554.0 \text{ cm}^{-1}$  [32]. The resulting pair potentials are depicted in the left part of Fig. 1 together with the  $6s$  pair potential. The resulting absorption spectra are shown in Fig. 2. The  $6p \leftarrow 6s$  absorption spectrum shown in the top plot is similar to that obtained in [9], which was in good agreement with experiment (see also [15]). The  $7s \leftarrow 6s$  absorption spectrum is shown in the bottom plot. It is forbidden in the isolated atom and becomes allowed here because of the symmetry breaking introduced by the helium droplet, as in *e.g.* [19]. It is somewhat blue-shifted, as compared to existing experimental and theoretical information [33, 34], see Fig. 2 of [34].

The position of the absorption bands with respect to the corresponding atomic lines can be rationalized by looking at the right part of Fig. 1, which displays the potential energy curves for Cs interacting with a  $^4\text{He}_{1000}$  droplet with density frozen at that of the ground electronic state equilibrium. All the absorption maxima are blue shifted compared to the atomic lines, as expected from the position of the Franck-Condon region. The largest blue shift is for  $7s \leftarrow 6s$  absorption, followed by absorption to the  $^2\Sigma_{1/2}$  state of the  $6p$  manifold. In both cases the Cs atom is given a large initial kinetic energy. Absorption to the



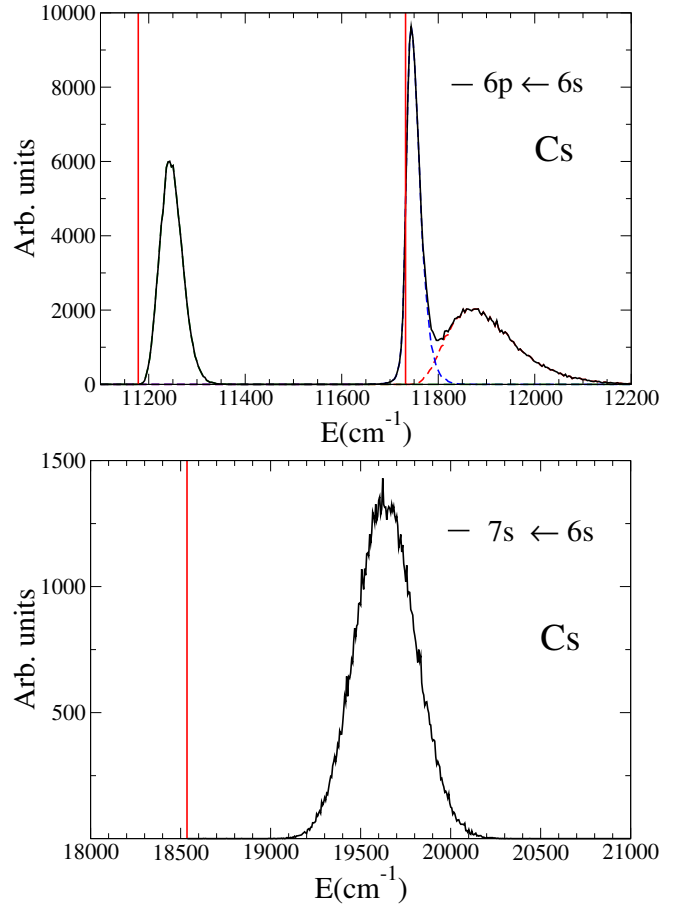
**Fig. 1.** Left part: He-Cs pair potentials used in this work. Right part: He<sub>1000</sub> droplet-Cs interaction potentials with the droplet density frozen at its equilibrium value with Cs in its ground electronic state. In both cases a vertical line is drawn from the ground electronic state equilibrium position in order to help visualize the Franck-Condon region.

$6p \ ^2\Pi_{3/2}$  state is rather close to the atomic  $^2P_{3/2}$  line, with a small initial kinetic energy given to the Cs atom. Absorption to the  $6p \ ^2\Pi_{1/2}$  state is intermediate, with a non-negligible recoil kinetic energy. These observations already give a hint of what to expect from the photodissociation dynamics on each of these states.

## 2.2 Dynamics

The simulations presented in this work have been carried out within the He-TDDFT approach [35] briefly outlined here. We introduce a complex effective wave function  $\Psi(\mathbf{r}, t)$  representing the helium droplet, such that  $|\Psi(\mathbf{r}, t)|^2 = \rho(\mathbf{r}, t)$ . It is evolved following the He-TDDFT prescription, while the motion of the excited Cs atom  $\mathbf{r}_{\text{Cs}^*}(t)$  is treated classically.

In the case of  $6p$  excitation the evolution of the  $\text{Cs}^*$  electronic state has to be also described. To this end, we introduce a six-component normalized vector  $|\lambda\rangle$  written in terms of a product basis of spin and angular momentum functions. The electron angular momentum is written in



**Fig. 2.** Top: Dipole absorption spectrum of  $\text{Cs}@^4\text{He}_{1000}$  around the  $6p \leftarrow 6s$  transition (arbitrary units). The vertical thin lines represent the free Cs atom transitions; the low energy D1 line comes entirely from excitation to the  $^2\Pi_{1/2}$  state. The high energy D2 line is decomposed into its  $^2\Pi_{3/2}$  (blue dashed line) and  $^2\Sigma_{1/2}$  (red dotted line) components. Bottom: same as top for the  $7s \leftarrow 6s$  transition.

cartesian basis functions  $i = x, y, z$  (standing for  $p_x, p_y$  and  $p_z$  orbitals) and the spin state as  $s = \uparrow$  ( $m_s = 1/2$ ),  $\downarrow$  ( $m_s = -1/2$ )

$$|\lambda\rangle = \sum_{is} \lambda_{is} |i, s\rangle. \quad (3)$$

The complete set of dynamical variables characterizing the system thus consists of a complex effective wave function for helium  $\Psi(\mathbf{r}, t)$ , a vector position for the impurity,  $\mathbf{r}_{\text{Cs}^*}(t)$ , and a 6-dimensional complex vector  $|\lambda(t)\rangle$ . The total energy of the  $\text{Cs}@^4\text{He}_{1000}$  complex suddenly excited to the  $^2P$  manifold is written as

$$E[\Psi, \mathbf{r}_{\text{Cs}^*}, \lambda] = \int d\mathbf{r} \frac{\hbar^2}{2m_{\text{He}}} |\nabla\Psi|^2 + \frac{p_{\text{Cs}^*}^2}{2m_{\text{Cs}}} + \int d\mathbf{r} \mathcal{E}_c[\rho] + \langle \lambda | V_{SO} | \lambda \rangle + \int d\mathbf{r} \rho(\mathbf{r}) V_\lambda(\mathbf{r} - \mathbf{r}_{\text{Cs}^*}). \quad (4)$$

The  $V_\lambda(\mathbf{r} - \mathbf{r}_{\text{Cs}^*})$  potentials are direction-dependent combinations of the  $\Pi$  and  $\Sigma$  potentials [35]

$$V_\lambda(\mathbf{r}) = \langle \lambda | \mathcal{V}(\mathbf{r}) | \lambda \rangle = \sum_{ijss'} \lambda_{is}^* \mathcal{V}^{ijss'}(\mathbf{r}) \lambda_{js'} \quad , \quad (5)$$

where the components of the six-dimensional matrix operator  $\mathcal{V}$  are [31]

$$\mathcal{V}^{ijss'}(\mathbf{r}) = \left\{ V_\Pi(r) \delta_{ij} + [V_\Sigma(r) - V_\Pi(r)] \frac{r_i r_j}{r^2} \right\} \delta_{ss'} \quad . \quad (6)$$

The dynamical evolution of the system is obtained by solving the following coupled 3D, time-dependent system

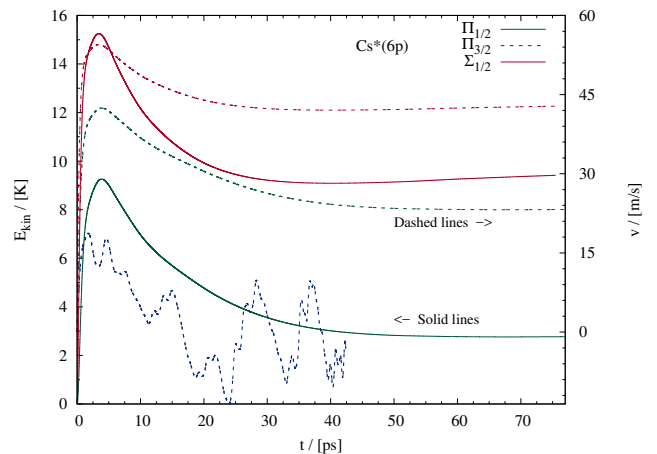
$$\begin{aligned} i\hbar \frac{\partial}{\partial t} \Psi &= \left[ -\frac{\hbar^2}{2m_{\text{He}}} \nabla^2 + \frac{\delta \mathcal{E}_c}{\delta \rho} + V_\lambda(\mathbf{r} - \mathbf{r}_{\text{Cs}^*}) \right] \Psi \\ i\hbar \frac{\partial}{\partial t} |\lambda\rangle &= \mathcal{H} |\lambda\rangle \\ m_{\text{Cs}} \ddot{\mathbf{r}}_{\text{Cs}^*} &= - \int d\mathbf{r} [\nabla \rho(\mathbf{r})] V_\lambda(\mathbf{r} - \mathbf{r}_{\text{Cs}^*}) \end{aligned} \quad (7)$$

The electronic Hamiltonian  $\mathcal{H}$  is a  $6 \times 6$  matrix with elements

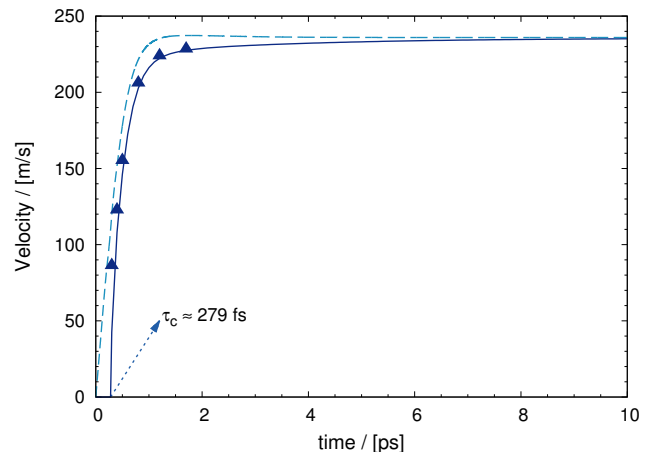
$$H^{ijss'} = \int d\mathbf{r} \rho(\mathbf{r}) \mathcal{V}^{ijss'}(\mathbf{r} - \mathbf{r}_{\text{Cs}^*}) + V_{SO}^{ijss'} \quad (8)$$

Equations (7) have been solved with the  $^4\text{He}$ -DFT-BCN-TLS computing package, using a time step of 0.5 fs and the same grid as for the static problem. The initial conditions were chosen to reflect as closely as possible femtosecond pump-probe experimental conditions. In this context the exciting laser pulse is short enough that the nuclei do not have time to move and the excitation process can be described as instantaneous. As a result the initial conditions were taken as: the equilibrium position of Cs at the surface dimple; the associated helium density  $\rho_0(\mathbf{r})$  –or effective wave function  $\Psi_0(\mathbf{r})$ – and atom position  $\mathbf{r}_{\text{Cs}_0^*}$  with initial velocity  $\dot{\mathbf{r}}_{\text{Cs}^*} = 0$ .

Moreover, the energy width associated with pulses of the order of several hundred femtoseconds is of the order of several tens of  $\text{cm}^{-1}$ , which is small enough to be able to select one initial eigenstate (see right part of Fig. 1). Hence the initial  $|\lambda\rangle$  state is taken as one of the eigenstates of the Hamiltonian  $\mathcal{H}$  at the time of excitation. Diagonalization of  $\mathcal{H}$  yields six eigenstates two-fold degenerate due to Kramer's theorem [36,37]. The dominant term of the electronic Hamiltonian Eq. (8) for  $\text{Cs}^*$  on the helium droplet is the spin-orbit interaction  $V_{SO}$ , as was the case for *e.g.* excited Ag atoms [35],  $\text{Ba}^+$  cations [38] and Rb atoms [21]. Hence the eigenstates can be arranged in two sets depending on their expectation value of  $\langle V_{SO} \rangle$ : the first set is the doublet correlating to the  $J = 1/2$  manifold, and the second set consists of the two doublets (four states) that correlate to the  $J = 3/2$  manifold. Evolution corresponding to  $^2\Pi_{1/2}$  state excitation was therefore started with  $|\lambda\rangle$  equal to one of the eigenstates correlating to the



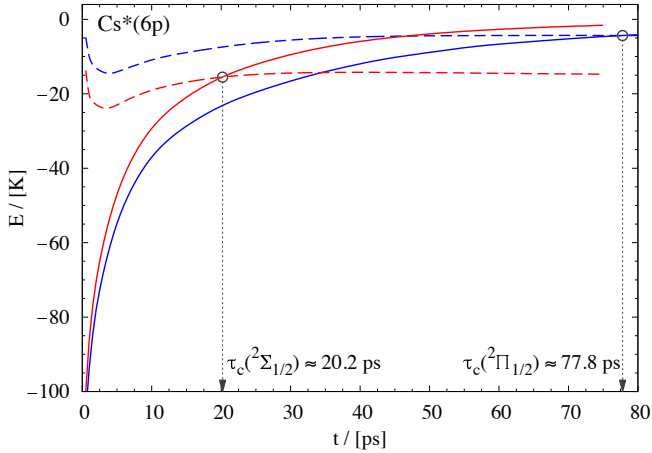
**Fig. 3.** Velocity (dashed lines, right scale) and kinetic energy (solid lines, left scale) of the Cs atom excited to the 6p state as a function of time. For the  $^2\Sigma_{1/2}$  and  $^2\Pi_{1/2}$  states the asymptotic velocities would correspond to the largest ion velocities. The kinetic energy of the  $^2\Pi_{3/2}$  state is not given as this state is not ejected.



**Fig. 4.** Dashed line: velocity of the Cs atom excited to the 7s  $\Sigma$  state as a function of time. Solid line: velocity of the  $\text{Cs}^+$  ion as a function of the delay time obtained from Eq. (14). The triangles are the result of the actual dynamic evolution of the  $\text{Cs}^+$  cation.

$J = 1/2$  manifold. To select the eigenstate corresponding to  $^2\Pi_{3/2}$  or  $^2\Sigma_{1/2}$  excitation we have proceeded as follows. Diagonalization of the  $J_z$  operator in the fourfold vector space correlating to the  $J = 3/2$  manifold results in two doublets with  $J_z = \pm 3/2$  or  $J_z = \pm 1/2$ . Either state of the former doublet was used to start the evolution corresponding to  $^2\Pi_{3/2}$  excitation, and either of the latter for  $^2\Sigma_{1/2}$  excitation.

Since  $\text{Cs}^*(6p) \rightarrow \text{Cs}^+$  ionization is also performed with femtosecond probe pulses, it is described as an instantaneous process: the nuclei do not change position and only the potential electronic surface is suddenly switched to the ionized state at the time of ionization  $\tau_D$ . The dynamics then proceeds by simulating the time evolution of  $\text{Cs}^+$  and of the helium density. Since  $\text{Cs}^+$  is in its ground electronic



**Fig. 5.**  $U^+(t)$  for Cs in the  $6p\ ^2\Sigma_{1/2}$  and  $2\Pi_{1/2}$  states (solid lines). Also shown are the Cs\* kinetic energies of Fig. 3 changed of sign (dashed lines). The intersection of the  $U^+(t)$  and  $-E_{kin}(t)$  curves corresponding to the same state yields the fall-back time  $\tau_c$  [Eq. (12)] for that state.

state the equations of motion reduce to

$$i\hbar \frac{\partial}{\partial t} \Psi = \left[ -\frac{\hbar^2}{2m_{\text{He}}} \nabla^2 + \frac{\delta \mathcal{E}_c}{\delta \rho} + V^+(|\mathbf{r} - \mathbf{r}_{\text{Cs}^+}|) \right] \Psi$$

$$m_{\text{Cs}} \ddot{\mathbf{r}}_{\text{Cs}^+} = - \int d\mathbf{r} [\nabla \rho(\mathbf{r})] V^+(|\mathbf{r} - \mathbf{r}_{\text{Cs}^+}|) \quad (9)$$

with initial conditions for  $\mathbf{r}_{\text{Cs}^+}$  and  $\dot{\mathbf{r}}_{\text{Cs}^+}$  given by the corresponding values for the Cs\* atom at the delay time, *i.e.*  $\mathbf{r}_{\text{Cs}^+}(\tau_D) = \mathbf{r}_{\text{Cs}^*}(\tau_D)$ ,  $\dot{\mathbf{r}}_{\text{Cs}^+}(\tau_D) = \dot{\mathbf{r}}_{\text{Cs}^*}(\tau_D)$  while  $\Psi$  at  $\tau_D$  is taken as equal to  $\Psi$  for the Cs\* dynamics at  $\tau_D$ . The Cs<sup>+</sup>-He pair potential has been taken from [16], which sensibly coincides with that of [39]. It is represented as the top curve in the left part of Fig. 1.

Excitation to the 7s state and subsequent ionization are simulated in the same way as for 6p excitation. The sole difference is that the time evolution of Cs\* is much simpler, as there is only one electronic state involved in the photo-excitation. Hence Eqs. (7) reduce to

$$i\hbar \frac{\partial}{\partial t} \Psi = \left[ -\frac{\hbar^2}{2m_{\text{He}}} \nabla^2 + \frac{\delta \mathcal{E}_c}{\delta \rho} + V_{7s}(|\mathbf{r} - \mathbf{r}_{\text{Cs}^*}|) \right] \Psi$$

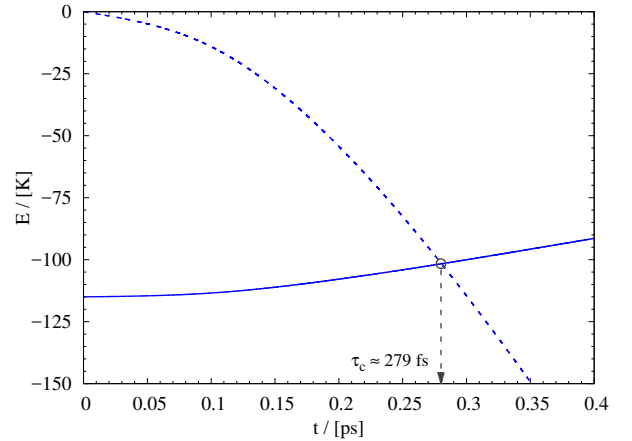
$$m_{\text{Cs}} \ddot{\mathbf{r}}_{\text{Cs}^*} = - \int d\mathbf{r} [\nabla \rho(\mathbf{r})] V_{7s}(|\mathbf{r} - \mathbf{r}_{\text{Cs}^*}|) \quad (10)$$

The 7s Cs\*-He pair potential has also been taken from [29]. It is represented in the left part of Fig. 1.

## 3 Results

### 3.1 Dynamics of Cs\* ejection

Figure 3 shows the velocity of Cs\* in the center of mass reference system of the Cs@ $^4\text{He}_{1000}$  complex for the three possible excited states corresponding to 6p Cs. Due to the



**Fig. 6.**  $U^+(t)$  for Cs in the  $7s\ \Sigma$  state (solid line). Also shown is the Cs\* kinetic energy changed of sign (dashed line). The intersection of the  $U^+(t)$  and  $-E_{kin}(t)$  curves yields the fall-back time  $\tau_c$  [Eq. (12)].

large mass difference between the atom and the droplet, this reference system sensibly coincides with the proper reference system of the helium droplet, where it is at rest. As can be seen in this figure,  $6p\ ^2\Sigma_{1/2}$  and  $6p\ ^2\Pi_{1/2}$  excitation leads to Cs\* dissociation. The overshoot in Cs\* velocity observed at short times when Cs\* dissociates is due to the existence of an attractive well in the excited state potentials. At longer times the Cs\* velocity reaches its asymptotic value: 43.6 m/s for  $6p\ ^2\Sigma_{1/2}$  and 23.8 m/s for  $6p\ ^2\Pi_{1/2}$  states. Our result for Cs in the  $6p\ ^2\Pi_{1/2}$  state is not in contradiction with the finding in [15] that Cs excited to this state is not desorbed, as these results correspond to exciting the Cs atom to the low energy tail of the D1 line and ours to the peak energy. A similar situation appeared for Rb\* [18, 40].

Figure 3 also shows that upon excitation to the  $6p\ ^2\Pi_{3/2}$  state, Cs\* is not ejected but remains on the droplet surface and oscillates around some kind of equilibrium position about 1 Å above that of the neutral atom at the dimple.

Notice that the largest velocity of the Cs<sup>+</sup> cation obtained by photo-ionization from these states is just the asymptotic velocity displayed for the corresponding Cs\* atom. Indeed, photo exciting Cs\* away from the droplet yields escaping Cs<sup>+</sup> cations whose velocity is little affected by the droplet. Hence, they keep the velocity of Cs\* before ionization.

The dynamics of the photoexcited Cs\* can be easily understood from the shape of the  $V_\lambda$  potentials defined in Eq. (5). An approximate representation of these potentials as a function of the droplet-Cs\* distance is given in Fig. 1. They are obtained by diagonalizing the electronic Hamiltonian of Eq. (8) for a helium density  $\rho(\mathbf{r})$  frozen at the ground state equilibrium. The Cs\*-He<sub>1000</sub> interaction potentials corresponding to the  $6p\ ^2\Sigma_{1/2}$  and  $6p\ ^2\Pi_{1/2}$  states are very repulsive in the Franck Condon region, and as a consequence when the Cs atom is excited to either of them it is quickly ejected. At variance, exciting to the  $6p\ ^2\Pi_{3/2}$

state brings the  $\text{Cs}^*\text{He}_{1000}$  system only slightly above the dissociation limit, so that the droplet can easily dissipate the excess energy and the Cs atom remains bound. In addition, as revealed by the corresponding pair potential in the left part of Fig. 1, a  $\text{He-Cs}^*$  excimer can be formed with no barrier. In 3 dimensions there are two deep attractive wells along the symmetry axis of the system, one between the droplet and the  $\text{Cs}^*$  and the other on the other side of the  $\text{Cs}^*$  with respect to the droplet. The former one is rapidly filled by helium atoms due to the absence of a barrier, leading to the formation of a linear exciplex [38]. By visual inspection of the  $\text{He-TDDFT}$  simulation, we have determined that this exciplex is formed in about 25 ps. The potential well is so deep that, once formed, the exciplex does not detach from the droplet. However, dissociation can occur upon relaxation to the  $^2\Pi_{1/2}$  state. This possibility, already identified for  $5p\text{Rb}^*$  [18],  $4p\text{K}^*$  [43], or  $6p\text{Ba}^{+*}$  [44] is discussed below.

Figure 4 shows the velocity of  $\text{Cs}^*$  upon excitation to the  $7s$  state as a function of time. The calculated maximum velocity of  $\text{Cs}^*$  is 235.9 m/s. In this case, the excited Cs is submitted to a highly repulsive interaction with He (see the corresponding potential curve in the right part of Fig. 1) and is ejected impulsively. This repulsion between He and  $7s\text{Cs}^*$  also yields a large blue-shift in the absorption spectrum, see the bottom panel of Fig. 2.

### 3.2 $\text{Cs}^+$ dynamics

Upon ionization at a given time delay  $\tau_D$ , the  $\text{Cs}^+$  ion at  $\mathbf{r}_{\text{Cs}^+}(t)$  evolves submitted to the potential

$$U^+(\mathbf{r}_{\text{Cs}^+}(t)) = \int d\mathbf{r}' V^+(|\mathbf{r}_{\text{Cs}^+}(t) - \mathbf{r}'|) \rho(\mathbf{r}', t) \quad (11)$$

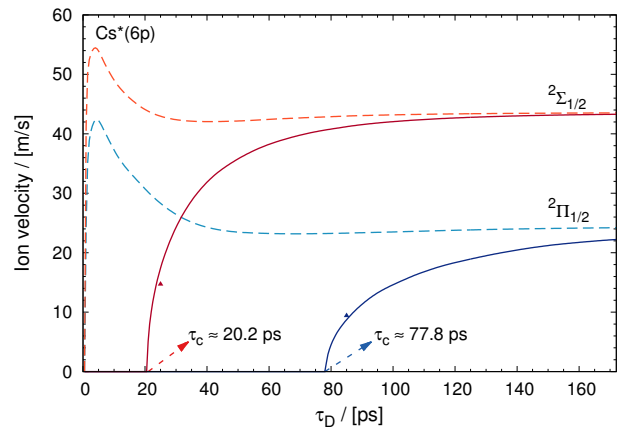
Notice that  $U^+(\mathbf{r}_{\text{Cs}^+}(t))$  depends on the state from which  $\text{Cs}^*$  has been photo-ionized (since  $\rho(\mathbf{r}, t)$  does).

The fall-back time  $\tau_c$  has been defined in the introduction as the critical value of the time delay  $\tau_D$  between excitation and ionization which separates the two possible outcomes for the ion: if  $\tau_D > \tau_c$ ,  $\text{Cs}^+$  will keep dissociating, whereas if  $\tau_D < \tau_c$ ,  $\text{Cs}^+$  will turn around and get solvated in the helium droplet. Since Cs is treated as a classical particle, the fall-back time  $\tau_c$  for a given  $\text{Cs}^*$  state is the solution of the equation

$$E_{kin}(\tau_c) + U^+(\tau_c) = 0, \quad (12)$$

where  $E_{kin}(t)$  is the kinetic energy of  $\text{Cs}^*$  at time  $\tau_D$ , which is taken to be equal to the initial kinetic energy for the ion [see text preceding Eq. (9)]. This condition defines the escape point of the ion; if ionization takes place at  $\tau_D > \tau_c$ ,  $\text{Cs}^+$  will go away from the system carrying some kinetic energy. The fall-back times for the  $6p$  states are  $\tau_c = 20.2$  ps ( $^2\Sigma_{1/2}$ ) and  $\tau_c = 77.8$  ps ( $^2\Pi_{1/2}$ ), see Fig. 5. In the case of  $7s$  Cs, we have obtained  $\tau_c = 279$  fs, see Fig. 6.

Due to the long range of the ion-He interaction (in  $1/r^4$ ), determining the asymptotic velocity of the ejected



**Fig. 7.** Velocity of the  $\text{Cs}^+$  ion in the  $6p^2\Sigma_{1/2}$  and  $6p^2\Pi_{1/2}$  states vs. delay (solid lines), and velocity of the neutral  $\text{Cs}^*$  in the corresponding state (dashed lines). The triangles represent the result of two explicit evolutions of the cation in the  $6p^2\Sigma_{1/2}$  and  $6p^2\Pi_{1/2}$  states for a delay of 25 ps and 85 ps, respectively.

ion for a given delay  $\tau_D > \tau_c$  is a very cumbersome task, because it requires to simulate the evolution of  $\text{Cs}^+$  for hundreds or even thousands picoseconds. This has been done only for a few test cases, as we did for  $\text{Rb}^+$  [18]. In general, we have used the method described below, which is accurate and efficient.

We have followed the actual evolution of the cation from the chosen  $\tau_D$  up to a rather long time  $t_{fr}$  at which the  $\text{Cs}^+$  cation is far enough from the droplet that the droplet density can safely be considered as frozen. Energy conservation for the  $\text{Cs}^+$  cation gives then its asymptotic energy  $[E_{kin}(\text{Cs}^+)]_{t_\infty}$  as its total energy at  $t_{fr}$ :

$$[E_{kin}(\text{Cs}^+) + U(\text{Cs}^+)]_{t_{fr}} = [E_{kin}(\text{Cs}^+)]_{t_\infty} \quad (13)$$

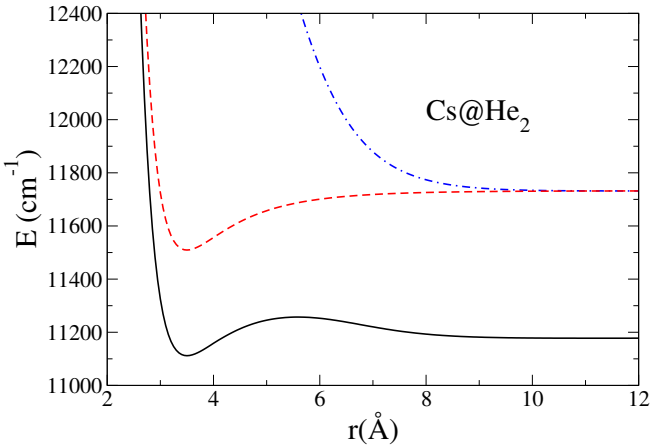
Hence, the asymptotic velocity of the ion  $\text{Cs}^+$  as a function of the time delay is determined as

$$v_{\text{Cs}^+}(\tau_D) = \sqrt{\frac{2}{m_{\text{Cs}}} [E_{kin}(\text{Cs}^+) + U(\text{Cs}^+)]_{t_{fr}}} \quad (14)$$

Notice that the maximum velocity of the ion obtained from Eq. (14) coincides with the asymptotic velocity of the excited neutral Cs atom, as it should be.

Figure 7 shows the velocity of the  $\text{Cs}^+$  ion in the  $6p^2\Sigma_{1/2}$  and  $6p^2\Pi_{1/2}$  states as a function of the time delay between excitation and ionization. The velocities of the neutral  $\text{Cs}^*$  atoms are displayed in dashed lines. Also shown in the figure is the result of two actual evolutions of the  $\text{Cs}^+$  ion in the  $6p^2\Sigma_{1/2}$  and  $6p^2\Pi_{1/2}$  states for a delay of 25 ps and 85 ps, respectively; the results for  $7s$  Cs are shown in Fig. 4. One can see that the agreement of the actual dynamics of  $\text{Cs}^+$  with the result obtained from Eq. (14) is good. We have found that the  $\text{Cs}^*$  atom has traveled 11.8 Å before ionization from the  $6p^2\Sigma_{1/2}$  state, 23.0 Å before ionization from the  $6p^2\Pi_{1/2}$  state, and 10.2 Å before ionization from the  $7s$  state.





**Fig. 8.** Energy of the linear symmetric Cs-He<sub>2</sub> configuration for Cs\* 6p states:  $^2I_{3/2}$  (red dashed line),  $^2I_{1/2}$  (black solid line), and  $^2\Sigma_{1/2}$  (blue dot-dashed line), as a function of the Cs-He distance. The wells in the  $^2I_{3/2}$  and  $^2I_{1/2}$  curves correspond to the exciplex.

### 3.3 Role of exciplex formation in the Cs\* ejection

As already discussed [see also Fig. 3], Cs excitation to the  $^2I_{3/2}$  state yields a linear exciplex, due to the existence of two deep wells in the  $V_\lambda(I_{3/2})$  potential [12]. The linear exciplex built on the droplet surface feels a strong attraction by the droplet and remains trapped at its surface. The same has been found for Ag [35], Ba<sup>+</sup> [38], and Rb [18].

This finding seems to be in contradiction with the experiments that observe exciplex formation and desorption at energies in the range where  $^2I_{3/2}$  and  $^2\Sigma_{1/2}$  states have some overlap. For the Rb( $^2I_{3/2}$ ) excitation [21], the disagreement was solved by adding a model for spin-orbit relaxation of likely broader applicability. We illustrate it as follows in the case of Cs.

The 6p  $^2I_{3/2}$  and 6p  $^2I_{1/2}$  energy curves of the Cs-He<sub>2</sub> linear symmetric exciplex calculated using the method of [38,42] are displayed in Fig. 8 as a function of the He-Cs\* distance. No exciplex can be formed around the 6p  $^2\Sigma_{1/2}$  state as there is no local minimum in the corresponding pair potential (see Fig. 1). The energy curves in Fig. 8 are similar to the ones found for Rb [21] and consequently, the mechanism for Cs\* ejection from the 6p  $^2I_{3/2}$  state must be similar. Upon Cs 6p  $I_{3/2}$  excitation, the system evolves in time for some tens of picoseconds, during which an exciplex is formed in a barrierless process as shown by Fig. 8. The Cs-He equilibrium position is thus moved from 7.7 Å in the 6s  $^2\Sigma_{1/2}$  state of the potential of [25] to 3.5 Å in the 6p  $^2I_{3/2}$  exciplex state. Subsequently, the 6p  $^2I_{3/2}$  exciplex relaxes non-radiatively to the 6p  $^2I_{1/2}$  state with the same equilibrium distance, some 387 cm<sup>-1</sup> below (see Fig. 8). Part of the available energy is dispersed into the droplet and the rest goes into initial kinetic energy for the exciplex. As a consequence, the exciplex dissociates from the droplet if it receives enough initial kinetic energy to overcome the attraction from the

droplet. Unfortunately, our model does not yield how the available energy is shared between the droplet and the impurity. Experimental information on the velocity of Cs<sup>+</sup> ions arising from the excitation of Cs to the 6p  $^2I_{3/2}$  state is needed to determine this ratio, as in the case of Rb\*(5p) [21]. Depending on its value, Cs\* in the 6p  $I_{1/2}$  state will remain on the droplet surface or be ejected as a bare Cs\* atom or as a HeCs\* exciplex that will be subsequently photo-ionized.

## 4 Summary

We have conducted a study of Cs 6p and 7s excitation dynamics on a He<sub>1000</sub> droplet using He-TDDFT simulations. The dynamics in the (pump) excited states as well as in the (probe) ionic states are determined.

Excitation to the 7s state leads to direct, impulsive dissociation, as expected from the repulsive He-Cs(7s) interaction potential. The same occurs upon excitation to the 6p  $^2\Sigma_{1/2}$  state. Excitation to the 6p  $^2I_{1/2}$  also leads to Cs\* desorption because the Cs\* interaction with the droplet is repulsive in the Franck-Condon region for that state. The apparent disagreement with experiment [15] is easily solved by realizing that our simulation corresponds to exciting at the maximum intensity of the  $^2I_{1/2}$  absorption peak whereas the non-dissociating Cs\* observed by Theisen *et al* [15] was for excitation at the low energy tail of the D1 line. This can be seen in the right part of Fig. 1, where the potential well in the  $^2I_{1/2}$  state can be accessed if the Franck-Condon region extends to about 0.5 Å further from the ground state equilibrium distance, which is very plausible. Finally, excitation to the 6p  $^2I_{3/2}$  state leads to barrierless formation of an exciplex which remains bound to the droplet. Eventually spin-orbit relaxation is expected to take place, as surmised and modeled in Rb\* 5p  $^2I_{3/2}$  [21]. As a consequence, Cs\* will dissociate, either as a bare atom or as an exciplex.

We have also simulated the dynamics in the ionic state corresponding to the probe process as a function of the delay time between excitation and ionization. This way the critical time delay  $\tau_c$  separating ion escape from ion turn back and solvation could be determined. This could be tested against planned experiments.

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## 5 Authors contributions

Most calculations were carried out by F. Coppens, A. Leal, and M. Pi. J. von Vangerow carried out experiments on



Rb that have motivated this work and clarified basic aspects of the problem. All the authors were involved in the discussions leading to the completion of this work and the preparation of the manuscript, that was mainly written by M. Barranco, N. Halberstadt, M. Mudrich, and F. Stienkemeier. All the authors have read and approved the final manuscript.

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