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Dark matter and bubble nucleation in old neutron stars

A. Herrero,¹ M. A. Pérez-García⁽⁰⁾,^{1,*} J. Silk⁽⁰⁾,^{2,3,4,†} and C. Albertus^{(1),‡}

¹Department of Fundamental Physics, University of Salamanca, Plaza de la Merced S/N E-37008, Salamanca, Spain

 ²Institut d'Astrophysique, UMR 7095 CNRS, Sorbonne Université, 98bis Blvd Arago, 75014 Paris, France
 ³Department of Physics and Astronomy, The Johns Hopkins University, Baltimore Maryland 21218, USA
 ⁴Beecroft Institute of Particle Astrophysics and Cosmology, Department of Physics, University of Oxford, Oxford OX1 3RH, United Kingdom

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We study the probability for nucleation of quark matter droplets in the dense cold cores of old neutron stars induced by the presence of a self-annihilating dark matter component, χ . Using a parametrized form of the equation of state for hadronic and quark phases of ordinary matter, we explore the thermodynamical conditions under which droplet formation is facilitated by the energy injection from χ self-annihilations. We obtain the droplet nucleation time as a function of the dark matter candidate mass, m_{χ} . We discuss further observational consequences.

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I. INTRODUCTION

Neutron stars (NSs) are compact astrophysical stellar objects where the low temperature and high density regions of ordinary matter phase space can be explored [1]. Typically, their measured masses do not exceed a maximum value $M_* \sim 2 M_{\odot}$ and radii $R_* \sim 11-13$ km. They are thought to be composed out of nucleons, mainly neutrons, with a little fraction of protons and possibly other heavier baryons or even more exotic components [2] besides a leptonic fraction to keep electrical charge neutrality. Central nucleon number densities are thought to be several times that of nuclear saturation density, $n_0 \sim 0.17$ fm⁻³ and effective measured temperatures are in the range $T^{\infty} \sim$ $10^{5.3}$ – 10^6 K for old NSs with lifetimes $\tau_{\rm NS} \gtrsim 10^4$ yr [3]. Under these conditions ordinary matter is typically degenerate since baryonic Fermi energies are of the order of $E_{\rm FB} \sim 30$ MeV, whereas the internal temperature drops below $T \sim 1$ MeV ($k_{\rm B} = 1$) within ~100 seconds after the birth of the NS [4].

Although the usual description of the interior of these objects is based on effective nuclear degrees of freedom i.e., nucleons and mesons, other realizations based on quark

mperezga@usal.es

constituents could indeed happen in nature. Early since the pioneering work by Bodmer and Witten [5,6] the conjecture of the existence of a most fundamental, quark deconfined, state of matter in the NS core has remained an intriguing possibility. This has been explored in the literature, see for example [7–11] and references therein.

There are two principal mechanisms capable of triggering the deconfinement transition. One involves the increase of the central pressure [12] due to either the accretion of a small amount of hadronic matter or slowed rotation, while the other relies on temperature effects [13–17]. In [18], the concept of a limiting conversion temperature in the protohadronic star is introduced as an indicator of the thermal energy $\Theta \sim 10-30$ MeV that can induce nucleation, provided central densities (or stellar masses) are large enough. In brief, both rely on overcoming the hadronic potential barrier that confines quarks and tunneling out of the nucleon bag that is a few fm in size. Microscopically, the locally deconfined two-flavored *ud* quark phase (Q^*) first forms and later proceeds to a β -equilibrated threeflavored uds quark matter (QM). Note, however, that whether this former *ud* phase truly decays has been questioned by recent works relying on arguments of energetic stability [19].

Matter at such high densities can only be partially tested by terrestrial experiments. Sites such as the GSI with the FAiR accelerator, BNL with RHIC, and CERN with the LHC, can use heavy ion collisions (HIC) to produce the socalled quark-gluon plasma [20] consisting of a highly excited hadronic system several fm in size and a lifetime of approximately 20 fm/c. Although temperatures in the fireball that is produced are initially high $T \gtrsim 80$ MeV,

silk@iap.fr

albertus@usal.es

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HIC can test supra-saturation densities and provide tighter constraints on magnitudes such as the high-density behavior of the symmetry energy, the tidal deformability and the equation of state (EoS) of nuclear matter itself, thus linking different areas of interest ranging from astrophysics to nuclear and particle physics [21].

In this work, we are interested in the study of nucleation of quark droplets in a hadronic (nucleon) medium inside the NS core with a novel mechanism mediated by dark matter (DM). This type of matter is one of the key ingredients in our presently accepted cosmological model that remains as vet undetected. It is found to constitute $\sim 26\%$ of our Universe. There are nowadays plenty of candidates from extensions beyond the Standard Model (SM) of particle physics that have been proposed to populate the dark sector [22]. Experimental searches with different strategies try to put constraints on the mass and scattering cross section phase space $(m_{\gamma}, \sigma_{\gamma})$. For example, while the weakly interacting candidates (WIMPs) have been thoroughly searched for in the last decade with null results [23], other candidates have lately attracted much attention, see [24]. Within standard cosmology, the present relic density can be calculated reliably if the WIMPs were in thermal and chemical equilibrium with the hot SM particles after inflation. In this same context, scanning the $m_{\gamma} \sim$ 10–1000 GeV range (we use c = 1) has yielded some results. Direct detection generation II experiments based on nuclear recoils are currently approaching the $\sigma_{\gamma} \sim$ 10^{-47} cm² [25] close to the atmospheric/solar coherent neutrino interaction floor. In addition, they exclude some of the preferred regions arising from scans of SUSY models, see Fig 26.1 in [23] in the range $m_{\chi} \sim 30-60$ GeV and $m_{\gamma} \sim 10^2 - 10^3$ GeV. In indirect searches [26], products of DM annihilation including neutrinos, gamma rays, positrons, antiprotons, and antinuclei can be detected. There are additional sources with constraining power such as those arising from large-scale structure of the Universe that rule out a $m_{\gamma} \lesssim 400 \text{ eV}$ WIMP under the Tremaine-Gunn bound [27] along with others. It is generally believed that massive DM particles interact gravitationally and that any nongravitational couplings are expected to be weakly or strongly interacting in order to at least maintain equilibrium with luminous matter in our Universe.

The structure of this contribution is as follows. In Sec. II we present the effective field theory approaches to describe the hadronic content of the interior of the NS with a possible quark phase. We introduce the relativistic Lifshitz-Kagan theory used to describe the induced bubble nucleation due to the presence of a component of DM inside the NS. Later, in Sec. III, we present our results discussing the thermodynamical conditions along with model details more favorable for nucleation of QM bubbles in hadronic matter. We evaluate the nucleation time taking into account the mass of the DM candidate. We discuss the different sources of uncertainty in our modeling and possible further

astrophysical observable consequences. Finally, in Sec. IV, we give our conclusions.

II. MODELING THE NS INTERIOR WITH A DM COMPONENT

We assume that a nonvanishing component of DM is present in the NS. In an evolved NS, this may be the result of various processes taking place during the lifetime of the star, including its progenitor phase as well. In dense DM environments such as the Galactic center, where there is a high density of neutron stars, clumps of DM of typical mass corresponding to the free streaming mass, of order 10^{-6} M_{\odot} but possibly larger [28], can occasionally be accreted by NSs. This can provide a rare but substantial enhancement of the DM component of the NS.

As we explain below, gravitational capture and depletion processes (typically self-annihilation or decay [29,30]) modulate the DM population inside the star [31,32]. Complementary constraints on DM annihilation processes from additional isotropic gamma-ray or reionization and heating of the intergalactic gas backgrounds have been summarized in recent contributions [33]. We will consider DM that self-annihilates through reactions involving quark pairs $\chi \bar{\chi} \rightarrow q \bar{q} \rightarrow N \gamma$ producing photon final states. Note that although other channels are indeed available, for simplicity we will stick to this case in what follows but we will later discuss other possibilities. DM candidates (χ) of interest to us will be those with cross sections $\sigma_{\chi N}$ scattering off nucleons (N) and masses m_{χ} in nonexcluded regions of the currently available phase space [23].

We first consider the cold NS core as a system described by the well-known relativistic Lagrangian model from [34] consisting of a baryon sector B = n, p (neutrons and protons) interacting through mesonic fields $\mathcal{M} = \sigma, \omega$, ρ and a minimal leptonic sector l = e (electrons). Besides, the usual nonlinear self-interacting potential is included under the form

$$\mathcal{U}(\sigma) = \frac{1}{3}a_1m_B(m_B - m_B^*)^3 + \frac{1}{4}a_2(m_B - m_B^*)^4, \quad (1)$$

with m_B being the bare baryon mass and $m_B^* = m_B - g_{\sigma B}\sigma$ the effective baryon mass in the medium. Specific values for the couplings of the baryon and meson fields as well as particle masses used can be found in [35].

In the cold system, baryonic density can be expressed in terms of the Fermi momentum $k_{F,B}$ for each particle component as $n_b = \sum_B \frac{k_{F,B}^3}{3\pi^2}$. Similarly, for the leptons we have $n_l = n_e = \frac{k_{F,l}^3}{3\pi^2}$. The equations for the mesonic fields in the extended system are obtained using a mean field approach so that we replace a generic field $\phi(x) \rightarrow \langle \phi(x) \rangle = \phi$. By doing this the equations for the nonvanishing mesonic field components are obtained. For the $\omega_0 \equiv \omega$ field one obtains

$$m_{\omega}^2 \omega = \sum_B g_{\omega B} n_B, \qquad (2)$$

while for the $\rho_{03} \equiv \rho$ field

$$m_{\rho}^2 \rho = \sum_B g_{\rho B} \tau_{3B} n_B, \qquad (3)$$

being $\tau_{3B} = \text{diag}(1/2, -1/2)$ the isospin 3-rd component matrix operator. Finally for the σ field,

$$m_{\sigma}^{2}\sigma = -\frac{d\mathcal{U}(\sigma)}{d\sigma} + \frac{1}{2\pi^{2}}\sum_{B}g_{\sigma B}m_{B}^{*3}\left[t_{B}\sqrt{1+t_{B}^{2}}\right]$$
$$-\ln\left(t_{B}+\sqrt{1+t_{B}^{2}}\right), \qquad (4)$$

where we have defined $t_B = k_{F,B}/m_B^*$. We can also write the chemical potential for baryons as $\mu_B = \sqrt{k_{F,B}^2 + m_B^{*2}} + g_{\omega B}\omega + g_{\rho B}\tau_{3B}\rho$ while for leptons $\mu_l = \sqrt{k_{F,l}^2 + m_l^2}$. Additionally, imposing conditions for electrical charge neutrality $n_e = n_p$ and β -equilibrium $\mu_n = \mu_p + \mu_e$ (no neutrinos are trapped) we can obtain the solution for the mesonic fields, provided a n_b value is set. This allows to obtain the EoS from contribution of all particle species. From this, the total energy density and pressure to describe the interior of the old NS can be written as a sum of hadronic (Had) and leptonic (1) terms, $\epsilon = \epsilon_{\text{Had}} + \epsilon_l$ and $P = P_{\text{Had}} + P_l$, respectively. More explicitly,

$$\varepsilon = \frac{1}{8\pi^2} \sum_{i=B,l} m_i^{*4} \Big[(2t_i^2 + 1)t_i \sqrt{1 + t_i^2} - ln \Big(t_i + \sqrt{1 + t_i^2} \Big) \Big] + \mathcal{U}(\sigma) + \frac{1}{2} m_\sigma^2 \sigma^2 + \frac{1}{2} m_\omega^2 \omega^2 + \frac{1}{2} m_\rho^2 \rho^2,$$
(5)

and

$$P = -\sum_{i=B,l} \varepsilon_i + \sum_{i=B,l} n_i \mu_i.$$
(6)

We use $t_l = k_{F,l}/m_l$ and $m^*_l = m_l = m_e$.

Let us note that although a proper treatment of the hadronic (quark) system would require using the framework of quantum chromodynamics (QCD) at intermediate energies, this calculation is, in practice, technically infeasible. It is for this reason that phenomenologically different approaches using effective field theories with baryonic (mesonic) and more fundamental quark (gluon) degrees of freedom have been exploited in order to determine the EoS of both forms of matter consistently [36] and explore their thermodynamical conditions of stability. In this spirit, to describe the deconfined quark matter phase we use the MIT Bag model [37] where gluon fields are effectively considered through a vacuum pressure, B, including interactions through the strong coupling constant α_S [38]. The perturbative QCD parameter α_S characterizes the degree of the quark interaction correction, with $\alpha_S = 0$ corresponding to no QCD corrections (Fermi gas approximation). For our purposes we will explore values $\alpha_S = 0.4$, 0.5 in line with previous works [10]. In addition, these selected values are also included in the allowed range arising from gravitational wave and astrophysical constraints quoted in [39,40]. We use this model as it provides a tractable and meaningful way to describe a hypothetical more fundamental configuration of matter although other more refined approaches exist [41]. Regarding this aspect we expect no dramatic modification of the results we find.

For a cold *uds* quark system, the thermodynamical potential Ω_q for each light flavor with mass m_q and chemical potential μ_q (q = u, d, s), has a general form

$$\Omega_{q} = -\frac{1}{4\pi^{2}} \left[\mu_{q} p_{\mathrm{F},\mathrm{q}} \left(\mu_{q}^{2} - \frac{5}{2} m_{q}^{2} \right) + \frac{3}{2} m_{q}^{4} \ln \left(\frac{\mu_{q} + p_{\mathrm{F},\mathrm{q}}}{m_{q}} \right) \right] \\ + \frac{\alpha_{\mathrm{S}}}{2\pi^{3}} \left\{ 3 \left[\mu_{q} p_{\mathrm{F},\mathrm{q}} - m_{q}^{2} \ln \left(\frac{\mu_{q} + p_{\mathrm{F},\mathrm{q}}}{m_{q}} \right) \right]^{2} - 2 p_{\mathrm{F},\mathrm{q}}^{4} \right\},$$
(7)

where $p_{\rm F,q} = (\mu_q^2 - m_q^2)^{1/2}$. Here we use the approximation $m_u = m_d \equiv 0$ and $m_s = 150$ MeV. Thus for massless quarks Ω_q adopts the simplified form $\Omega_q = -\frac{\mu_q^4}{4\pi^2}(1-\frac{2\alpha_s}{\pi})$. The quark number density is obtained as $n_q = -\frac{\partial\Omega_q}{\partial\mu_q}$.

Finally, the energy density for *uds* matter includes the contribution from the effective bag constant *B* under the form $\varepsilon_{\text{Quark}} = \sum_{q} (\Omega_q + \mu_q n_q) + B$ or, more explicitly,

$$\varepsilon_{\text{Quark}} = \frac{3}{4\pi^2} \left(1 - \frac{2\alpha_s}{\pi} \right) (\mu_u^4 + \mu_d^4) + \frac{3}{8\pi^2} m_s^4 [x_s \eta_s (2x_s^2 + 1) - \ln(x_s + \eta_s)] - \frac{\alpha_s}{2\pi^3} m_s^4 \{2x_s^2 (x_s^2 + 2\eta_s^2) - 3[x_s \eta_s + \ln(x_s + \eta_s)]^2\} + B,$$
(8)

where $x_s = \sqrt{\mu_s^2 - m_s^2}/m_s$, $\eta_s = \sqrt{1 + x_s^2}$. Note that an additional lepton component ε_l must be present in the total ε contribution, analogous to that in Eq. (5). For the quark-gluon pressure we have

$$P_{\text{Quark}} = -\sum_{q} \Omega_q - B \tag{9}$$

and the total pressure is $P = P_{\text{Quark}} + P_l$. As before, the conservation of baryonic charge, weak equilibrium, and the additional constraint of electric charge neutrality in NS matter can be expressed for the quark phases as $n_b = \frac{1}{3}\sum_q n_q$, $\mu_d = \mu_u + \mu_e$, $\mu_s = \mu_d$ and $\frac{2}{3}n_u = \frac{1}{3}(n_d + n_s) + n_e$. In this model the actual first order phase transition comes

determined by the thermodynamical conditions of the cold NS interior [18]. For the multicomponent system under scrutiny the Gibbs criteria imposes the equality of baryonic chemical potentials at a given pressure P_0 where equilibrium holds,

$$\mu_b(P_0)|_{\text{Had}} = \mu_b(P_0)|_{\text{Quark}},\tag{10}$$

and $\mu_b = \frac{\varepsilon + P}{n_b}$ in the cold system.

Let us remark here that, on general grounds, the nature of the transition between the hadron-resonance gas (HRG) and quark-gluon plasma (QGP) phases of nuclear matter can be presented in terms of the phase diagram of QCD as a function of temperature T and baryon chemical potential μ_b . At large T and small μ_b , the transition is expected on the basis of lattice calculations to be a rapid crossover, whereas it is naturally expected that the phase transition along the μ_b -axis (with T = 0) is an actual first-order phase transition [42,43]. Somewhere along the phase transition line the point at which this occurs is commonly known as the QCD critical point that has not yet been experimentally confirmed nor predicted with theoretical certainty [44].

In our stellar scenario DM with $m_{\gamma} \gtrsim 10$ GeV and cross sections $\sigma_{\gamma N}$ in the currently allowed phase space can thermalize and display a radial distribution inside the NS, $\rho_{\chi,*}(r)$, built on top of that of ordinary baryonic matter. The ratio of gravitational to thermal energy makes DM to follow a Gaussian distribution $\rho_{\chi,*}(r) \sim e^{-(r/r_{\rm th})^2}$ with a radius $r_{\rm th} = \sqrt{\frac{3k_BT}{2\pi G\rho_B m_{\chi}}}$. This central region is where most DM annihilations will take place. We consider that the inner NS core has a baryonic mass density around three times that of nuclear saturation density, $\rho_B \sim 7 \times 10^{14} \text{ g/cm}^3$, and an internal temperature $T \sim 10^5$ K at a given galactic location with a corresponding ambient DM density, ρ_{χ} . Typical values in the solar neighbourhood are $\rho_{\chi,\text{local}} =$ (0.39 ± 0.03) GeV/cm³ [45] although NSs are found closer to the Galactic center where they can be higher by a factor of ~100. The NS captures DM, up to factors of order unity, at a rate C_{γ} [46,47]

$$C_{\chi} \simeq 1.8 \times 10^{23} \left(\frac{100 \text{ GeV}}{m_{\chi}}\right) \left(\frac{\rho_{\chi}}{\rho_{\chi,\text{local}}}\right) f_{\chi,N} \text{ s}^{-1}.$$
(11)

 $f_{\chi,N}$ denotes a phenomenological factor dealing with the opacity of stellar matter as it depends on the ratio of the leading contribution of χN scattering cross section $\sigma_{\chi N}$ to the minimum geometrical cross section defined as $\sigma_0 \sim \frac{m_B}{M_*} R_*^2 \sim 10^{-45} \text{ cm}^2$. Thus this factor saturates to unity $f_{\chi,N} \sim 1$ if $\sigma_{\chi N} \gtrsim \sigma_0$, whereas it decreases the capture rate otherwise. As current experimental efforts foresee sensitivities below σ_0 for some m_{χ} windows, this would imply lower amounts of DM inside the NS by this same factor. However this aspect is not critical as a tiny content

of DM can induce important changes in the NS EoS, as we will explain.

The DM particle population number inside the star, N_{χ} , will not only depend on the capture rate C_{χ} but also on the self-annihilation rate, C_a , in our scenario. This latter is model-dependent but we can estimate it to be $C_a \sim \langle \sigma_a v \rangle / r_{\text{th}}^2$. Numerically,

$$C_a = 1.1 \times 10^{-30} \left(\frac{\langle \sigma_a v \rangle}{3 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1}} \right) \\ \times \left(\frac{10^5 \text{ K}}{T} \frac{m_{\chi}}{100 \text{ GeV}} \right)^{3/2} \text{ s}^{-1}.$$
(12)

Therefore N_{χ} can be obtained as a function of time *t* by solving the differential equation for the NS core $\frac{dN_{\chi}}{dt} = C_{\chi} - C_a N_{\chi}^2$ considering the two competing processes of capture and self-annihilation. The solution can be written as

$$N_{\chi}(t) = \sqrt{\frac{C_{\chi}}{C_a}} \tanh\left[\frac{t}{\tau} + \gamma(N_{\chi,0})\right], \qquad (13)$$

where $N_{\chi,0}$ is the DM population in the final stage of its progenitor phase and $\gamma(N_{\chi,0}) = \tanh^{-1}(\sqrt{\frac{C_{\chi}}{C_a}}N_{\chi,0})$ with $\tau^{-1} = \sqrt{C_{\chi}C_a}$. For times large enough so that the system has reached the steady state, $t \gg \tau$, the asymptotic population is given by $N_{\chi}(t_{\infty}) \simeq \sqrt{\frac{C_{\chi}}{C_{\star}}}$.

Under such conditions, we model the average energy release from annihilation processes as obtained from the spectrum of the reaction $\chi\bar{\chi} \to q\bar{q} \to N\gamma$. Although other channels are indeed possible [48], we restrict our modeling to this one as the mechanism presented here will not be dramatically altered. The spectrum $\frac{dN_{\gamma}}{dE}$ provides the average energy release as $\langle E \rangle = \int_0^{m_\chi} E \frac{dN_\chi}{dE} dE$. Note that the upper limit in the integral is due to the fact that the center of mass energy is $E_{\rm CM} = \sqrt{s} = 2m_{\gamma}$ being s the Mandelstam variable and each quark (antiquark) carries a maximum value $E_{\rm q} = \sqrt{s}/2 = m_{\gamma}$. We have used the PYTHIA package [49] to obtain that as an indication, for light quarks approximately 67% of the DM mass m_{γ} is deposited in the medium in the form of photons. Heavier quarks, alternative channels or even corrections due to energy loss and final state kinematics from the most energetic photons would indeed change the size of the energy injection. Since the energetics of the microscopic particle physics event in the very dense medium inside the NS core with $\sim 10^{34}$ nucleons/cm³ is rather complex this treatment constitutes just an approximate description. However, we do not expect it dramatically alters the nucleation mechanism itself as exposed here.

Typically, the photons produced will be obtained from different highly energetic hadronic as well as electromagnetic showers involving inelastic interactions with the dense medium. In this way, the hadrons with a cross section σ_{Had} , which is largely uncertain but can be roughly estimated to be $\sigma_{\text{Had}} \sim 1 \text{ fm}^2$ will produce showers with typical sizes depending on the baryonic density in the NS core. Taking a density $n_b \sim (3-5)n_0$ and typical energies $E \sim 1 - 10^5 \text{ GeV}$ for each event we obtain a size $X_{\text{Had}} \sim \frac{1}{n_b \sigma_{\text{Had}}} \text{Log}(\frac{E}{10 \text{ MeV}}) \lesssim 10 \text{ fm}$ for the hadronic showers while $X_{\text{EM}} \sim 1 \text{ fm}$ for the electromagnetic showers [50]. The injected energy is mainly contained into the bubble region with radius *R* as long as $X_{\text{Had}} \lesssim 2R$.

The global picture is thus that of a central DM annihilation volume, where both types of matter coexist, and baryonic matter is subject to steady state energy injection from the quoted DM reactions. To explore whether this scenario could lead to induced quark bubble nucleation we use the relativistic Lifshitz-Kagan theory [51]. We aim to describe the microscopics of a locally induced phase transition from an effective (metastable) hadronic phase to a more fundamental deconfined state. In this formalism the relativistic Lagrangian that describes the formation of a fluctuation i.e., a spherical bubble of mass M and radius R is given by

$$\mathcal{L}(R, \dot{R}) = -M(R)\sqrt{1 - \dot{R}^2} + M(R) - U(R), \quad (14)$$

where $\dot{R} = dR/dt$ is the radial growth rate and U(R) is an effective potential depending on the thermodynamical conditions of the medium

$$U(R) = \frac{4}{3}\pi R^3 n_{\text{Quark}} (\mu_{\text{Quark}} - \mu_{\text{Had}}) + 4\pi\sigma R^2.$$
(15)

We label μ_{Had} (μ_{Quark}) as the chemical potentials of the hadronic (quark) phases of matter at fixed pressure value, *P*. n_{Quark} is the number density of the quark phase and σ is the surface tension among the two phases. Contributions from volume as well as surface terms are the most energetically relevant although more corrections can be included [52]. As written, this expression may be familiar to the reader as it also used in terrestrial experiments for DM searches such as PICO [53] at SNOLAB, with an analogous strategy based on detecting χ scattering events in bubble chambers filled with overheated liquids at much smaller densities.

When nucleated, QM bubbles can be characterized by a critical radius for stability,

$$R_c = \frac{3\sigma}{n_{\text{Quark}}(\mu_{\text{Quark}} - \mu_{\text{Had}})},$$
 (16)

fulfilling the relation $U(R_c) = 0$ such that for $R > R_c$, the bubble is energetically stable. The potential barrier maximum height to be tunneled is

$$U_{\rm max} = \frac{16}{27} \pi \sigma R_c^2.$$
 (17)

In order to drive further changes at the macroscopic level QM bubbles must have the capability to last sufficiently and, in any case, longer than the timescale for stellar dynamical collapse $\tau_D \sim \sqrt{2R_*^3/2GM_*} \sim 3 \times 10^{-5}$ s.

Making a transformation to the phase space canonical variables q, p one can obtain the Hamiltonian associated to the Lagrangian in Eq. (14) as $\mathcal{H}(q, p) = p\dot{q} - \mathcal{L}$. As explained in [10] by taking the *WKB* approximation [54], one can compute the energy of the ground state, E_0 . The associated oscillation frequency $\nu_0^{-1} = \frac{dI}{dE}|_{E=E_0}$ is obtained [10] using the expression

$$I(E) = 2 \int_0^{R_-} \sqrt{[2M(R) + E - U(R)][U(R) - E]} dR, \quad (18)$$

being R_{-} the smaller turn around radius. The action under the potential barrier

$$A(E) = 2 \int_{R_{-}}^{R_{+}} \sqrt{[2M(R) + E - U(R)][U(R) - E]} dR.$$
(19)

determines the tunneling probability $p_0 = \exp(-\frac{A(E)}{\hbar})$.

In this system, the average energy per quark injected into the nucleon bag from DM self-annihilation events necessary to create a stable spherical droplet of size $\sim R_c$ can be approximated by $E_{inj} \sim \frac{\langle E \rangle}{n_b 4\pi R_c^3}$. We assume that the energetic shower is contained into the bubble, however, if this is not the case a decreasing factor $\xi \sim (2R/X_{Had})$ must be included. Thus the photon yields from DM self-annihilation act effectively to raise the energy level of otherwise confined quarks.

The bubble formation time is obtained as $\tau^{-1} = \nu_0 p_0$. It is important to notice that the nucleation process may most probably happen over the whole DM thermal volume $\sim r_{\text{th}}^3$. Therefore a number of nucleation centers are available for this process and can be estimated as $N_C \sim (\frac{r_{\text{th}}}{R_c})^3$. In such a case the corrected nucleation time is given by $\tau_N = \tau/N_C$. As explained in the introduction section of this contribution, the nucleation of quark droplets relying on standard astrophysical mechanisms is highly suppressed. This means, in practice, that nucleation times may be much larger than stellar lifetimes. As we will explain below, as a result of an extra energy injection from DM selfannihilation the hadronic system can be driven into an excited configuration allowing the formation of stable quark droplets more easily.

In our description of the cold nuclear system we have not considered the possibility of the existence of a fraction or paired nucleons. Typically for the high densities and low temperatures in the NS core the paired nucleon fraction is less than $\sim 10\%$. At supranuclear densities the pairing gaps,

 Δ , for neutrons (${}^{3}P_{2}^{3}F_{2}$ channels) and for protons (${}^{1}S_{0}$ channel) have been estimated yielding sizes up to a few MeV. Instead, for quarks they may be as large as a hundred MeV, see for example [55] for a review. In brief, the density of paired nucleons depends on this gap [56] as well as the quantity $\sqrt{(E_N(k, m_N^*) - \mu_N^*)^2 + \Delta^2(k)}$ involving the nucleon single-particle energy E_N , effective mass m_N^* and effective chemical potential μ_N^* for a fixed momentum $k < k_{F,N}$. The existence of such a gapped fraction adds an extra amount of energy $(E_{\text{BCS pair break}} > 2\Delta(k_{F,N}))$ that must be overcome in order to break the correlated pair as dictated by the BCS theory [57]. In this sense, the possible existence of a paired fraction tends to suppress the nucleation process. However, it is worth noting that, safely, for nucleons $\Delta(k_{F,N})/m_{\chi} \ll 1$ for typical NS core densities and most of the m_{γ} range explored in our study and similar applies for quarks. Thus we expect that the possible corrections from kinematically blocked states in the final phase space or paired components will not have a dramatic impact and the scattered fermions will have energies above the Fermi level for DM masses larger than a few GeV. However, this fact must be carefully reconsidered for $m_{\gamma} \lesssim$ 1 GeV as this could be a competing effect quenching the efficiency of nucleation. For simplicity we have neglected this possibility leaving it for a future contribution.

III. RESULTS

In this section we present our results. We have used arbitrary values $B \in [70, 150]$ MeV fm⁻³ as usually done in the literature, however recent calculations [58] restrict stable solutions of T = 0 uds QM to a window $60 \lesssim B \lesssim 80 \text{ MeV fm}^{-3}$. In addition, if confirmed, quark stars having masses beyond ~2 M_{\odot} limit would imply even smaller B values [39]. In addition values of the surface tension are poorly known. This quantity is relevant for bubble nucleation in different already studied environments, for example quark matter in supernovae [59] and neutron star mergers [60]. It is also relevant for a possible quark-hadron mixed phase in the interior of neutron stars [61]. Some available calculations have estimated its value using different complementary approaches such as Nambu-Jona-Lasinio models, quark-meson models [62] or chiral models [63] where in the latter maximum values point toward $\sigma \sim 15 \text{ MeV fm}^{-2}$. For our purposes we will consider $\sigma \in [10, 30]$ MeV fm⁻².

In Fig. 1 we plot pressure as a function of the baryonic chemical potential $\mu_b - m_B$ for hadronic matter (Had) and deconfined *ud* matter. We use $\alpha_S = 0.4, 0.5, B = 70, 100, 150 \text{ MeV fm}^{-3}$, and $\sigma = 30 \text{ MeV fm}^{-2}$. As the baryonic chemical potential (density) grows the softer quark matter EoS overpasses that of hadronic matter at a transition point i.e., the crossing of both curves. The higher the *B* (α_S) the higher the chemical potential associated to the transition density. The transition pressures and baryonic densities for



FIG. 1. Pressure as a function of the baryonic chemical potential for hadronic matter (Had) and deconfined *ud* matter. We use $\alpha_s = 0.4$, 0.5, B = 70, 100, 150 MeV fm⁻³.

 $\alpha_S = 0.4 \text{ are } P_0 = 588,483,401 \text{ MeV fm}^{-3} \text{ and } n_b = 0.92,$ 0.87, 0.78 fm⁻³ for $B = 150,100,70 \text{ MeV fm}^{-3}$, respectively. These results do not depend on σ . If instead we use $\alpha_S = 0.5$ and $B = 100 \text{ MeV fm}^{-3}$, we find $P_0 = 600 \text{ MeV fm}^{-3}$, $n_{\text{Had}} = 0.95 \text{ fm}^{-3}$, $n_{\text{Quark}} = 1.80 \text{ fm}^{-3}$.

In Fig. 2 we plot the potential barrier U(R) as a function of radius for different parameter sets. Solid, dashed, and dotted lines depict $P = P_0 + 32$ MeV, $P = P_0 + 42$ MeV, $P = P_0 + 52$ MeV for each case. In the upper panel we fix $\alpha_S = 0.4, B = 120 \text{ MeV fm}^{-3}, \sigma = 10 \text{ MeV fm}^{-2}$ (black curves) and $\sigma = 30 \text{ MeV fm}^{-2}$ (red curves). The latter case (red lines) has been scaled a factor 1/20 in order to numerically compare on the same axis. The pressure at the transition point is $P_0 = 525 \text{ MeV fm}^{-3}$ while the density is $n_{\text{Had}} = 0.88 \text{ fm}^{-3}$, $n_{\text{Quark}} = 1.58 \text{ fm}^{-3}$. We can see that for higher σ values, larger bubbles are required for stability and, at the same time, more energetic barriers form. Instead, for increasing pressure, smaller bubbles can survive. In the lower panel we fix $B = 100 \text{ MeV fm}^{-3}$, $\sigma = 30 \text{ MeV fm}^{-2}$, $\alpha_S = 0.4$ (blue curves) and $\alpha_s = 0.5$ (green curves). We can clearly see that for larger α_S values, i.e., including less strong corrections, smaller bubbles are predicted.

In Fig. 3 we plot the logarithm (base 10) of the nucleation time as a function of the DM particle mass for different parameter sets used. The amount of DM for each m_{χ} value is obtained from the asymptotic population $N_{\chi}(t_{\infty})$ ranging from $N_{\chi} \sim 10^{30}$ for $m_{\chi} = 1$ GeV to $N_{\chi} \sim 10^{23}$ for $m_{\chi} = 10^6$ GeV. These values are in all cases below the critical value given by their fermionic or bosonic nature, see [30,64]. In addition, given the spread of the hadronic/ quark parameters scanned, the pressure values considered for evaluation are selected above their corresponding P_0 for each case.

For the first set we fix $\alpha_s = 0.4$, $B = 70 \text{ MeV fm}^{-3}$, $\sigma = 10 \text{ MeV fm}^{-2}$ and select $P = 406 \text{ MeV fm}^{-3}$ (long



FIG. 2. Potential barrier energy as a function of radius for different combinations of (α_S, B, σ) . Solid, dashed, and dotted lines depict $P = P_0 + 32$ MeV, $P = P_0 + 42$ MeV, $P = P_0 + 52$ MeV for B = 120 MeV/fm³ (upper panel) and B = 100 MeV/fm³ (lower panel). Red curves on the upper panel have been scaled a factor 1/20 to improve readability. See text for details.



FIG. 3. Nucleation time as a function of the DM particle mass for different cases. Colored bands depict old NS ages (blue horizontal) and SUSY favored regions (pink vertical). The Universe lifetime $\tau_U \sim 10^{17.6}$ s is also shown. See text for details.

dashed). For the second set (same α_S as before) $B = 120 \text{MeV}\text{fm}^{-3}$, $\sigma = 30 \text{ MeV}\text{fm}^{-2}$ with $P = 535 \text{MeV}\text{fm}^{-3}$ (short dashed), and third set $\sigma = 10 \text{MeV}\text{fm}^{-2}$ (solid). For the fourth one $B = 100 \text{MeV}\text{fm}^{-3}$, $\sigma = 30 \text{ MeV}\text{ fm}^{-2}$ with $P = 515 \text{ MeV}\text{ fm}^{-3}$ (dotted) and, finally, the ffith set is the same as the latter case but using $\alpha_S = 0.5$ (dot-dashed).

We plot additional colored regions with constraints coming from NS ages typically measured (blue horizontal), see Table I in [3] with $\tau_{NS} \sim 10^{9.5} - 10^{13.5}$ s. They can even reach ~4.9 Gyr as in PSR J04374715 [65], close to the upper limit provided by the Universe lifetime (yellow double dash-dotted line) with $\tau_U \sim 10^{17.6}$ s. We also plot the regions (pink vertical) denoting the preferred four typical SUSY models, CMSSM, NUHM1, NUHM2, pMSSM10 which integrates constraints set by ATLAS Run 1 [23].

We can see that nucleation times are critically dependent on the B, α_S , and σ values of the quark phase. The thermodynamical conditions (central pressure) produce a moderate impact on the results. Increasing the bubble critical radius, i.e., σ , produces a high energetic cost. The energy injection obtained from the self-annihilating χ pair signals the kink where probability of nucleation $p_0 \sim 1$. The results obtained for the $B = 70 \text{ MeV fm}^{-3}$ set properly belong to the quoted stability window of QM as obtained in earlier works [58]. This case requires a $m_{\gamma} \gtrsim$ 4×10^5 GeV to induce nucleation in the central thermal volume inside the NS. In this scenario, light DM candidates $(m_{\gamma} < 10 \text{ GeV})$ would less favor such a conversion in ordinary NSs. Baryonic densities at the transition point found for each case are indeed in the previously estimated interval $\sim (3-4)n_0$. Note that additional corrections due to final state limitations of the energy injected as well as hadronic cascade sizes versus bubble radius will correct the energy efficiency by factors $\mathcal{O}(1)$. Thermal energy loses are found to be negligible in a cold system. In addition, other basic channels into which DM particles may annihilate could happen, including heavy quarks, leptons, weak or Higgs bosons [33]. Besides, a direct neutrino/ antineutrino annihilation channel or neutrinos originating from the decays of the particles produced in the annihilation could take place. This could modify effectively the energy injected into the central hadronic region altering the efficiency of the process [66]. The hierarchy problem, also framed as requiring naturalness or the absence of fine tuning, prefers WIMP masses below about a few TeV, which is considerably more constraining than the WIMP coincidence which essentially allows particles from a few GeV to about 100 TeV [67]. Nevertheless in our analysis we have considered maximum values of $m_{\chi} \lesssim 10^3$ TeV in consistency with the wimplike scenario depicted here and with capture rates in accordance with a typical weakly interacting DM candidate being accreted by the NS, see results from CTA [68] or MAGIC [69]. If more massive DM candidates were considered additional corrections to several quantities, e.g., capture rates, effective hadronic potentials, corrections from final phase space multiple channels or excited states of quark degrees of freedom should be considered.

A remark is due at this point regarding the feasibility of the percolation transition in the macroscopic stellar object. The mechanism quoted for nucleation in the relativistic Lifshitz-Kagan theory involves matter undergoing this process is at a metastable state, i.e., at pressures larger than the transition pressure P_0 . Given an object with mass M_* and radius R_* it may happen that displays either pure hadronic or nuclear-quark hybrid mixed nature. As we mentioned in the introduction section we have focused on the nucleation mechanism for matter in NS cores under the hadronic state in consistency with the DM-nucleon scattering cross sections used in the capture rate in Eq. (11). Additional corrections would arise from a hybrid NS or even a quark star and will be treated elsewhere.

In the hadronic stellar object the existence of such a macroscopic percolated region is expected to convert the full NS as already explained in [12] producing an energetic $10^{51}-10^{53}$ erg gamma ray burst (GRB). On the other hand for some of the parameter sets explored in our work (see dot-dashed line curve in Fig. 3) this mechanism would induce a rapid nucleation that, if progressing to macroscopic, seems to be hardly reconcilable with the frequency of very short GRBs observed [70]. The correspondence of the m_{ν} to the probability of nucleation of quark droplets seems remarkably sensitive under this mechanism. At a microscopic level, a dynamical study of the droplet boundary once formed has not been studied in detail yet. If the full NS converts to a more compact QM star this exotic type of matter would be ejected leaving an imprint on the cosmic rays or scintillation patterns [71–73]. Boundary conditions for isolated clusters have been somewhat explored in [74] where, arising from the strange quark content, the name of *strangelet* is coined. If a strangelet is not in flavor equilibrium, it can decay via weak semileptonic decays, weak radiative decays and electron capture. Other modes of decay reduce the baryon number instead. Further work on this is under progress and will be reported elsewhere.

IV. CONCLUSIONS

We have studied the nucleation of quark droplets in the NS core facilitated by the energy injection due to a component of self-annihilating DM present inside neutron stars. We find that under the effective field theoretical description of the hadronic and quark phases, the latter using a MIT bag model, the dark matter candidate mass highly influences the nucleation time τ_N . Depending on the central pressure (density) conditions inside the star nucleation times may span 40 orders of magnitude. Within this scenario light dark matter is less favored to produce such a percolation phase transition inside the core central region. However, for parameter sets within a window of energetic stability for stellar mass-radius values of $m_{\gamma} \gtrsim$ 4×10^5 GeV are found capable of nucleating the macroscopic thermal DM core during the NS lifetime and drive a conversion into a more compact star. Emission of radiation (GRB) or chunks of matter (cosmic rays) is to be expected along with gravitational waves. To determine the temporal sequence of the multimessenger signal and magnitude of the effects presented here, detailed calculations of the central EoS instability are needed and are left for future work.

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