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# Polytopic reconfiguration: a graph-based scheme for the multiscale transformation of music segments and its perceptual assessment

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## ABSTRACT

Music is a sequential process for which relations between adjacent elements play an important role. Expectation processes based on alternations of similarity and novelty contribute to the structure of the musical flow. In this work, we explore a polytopic representation of music, which accounts for expectation systems developing at several time-scales in parallel. After recalling properties of polytopic representations for describing multi-scale implication processes, we introduce a scheme for recomposing musical sequences by simple transformations of their support polytope. A specific set of permutations (referred to as Primer Preserving Permutations or PPP) are of particular interest, as they preserve systems of analogical implications within musical segments. By means of a perceptual test, we study the impact of PPP-based transformations by applying them to the choruses of pop songs in midi format and comparing the result with Randomly Generated Permutations (RGP). In our test, subjects are asked to rate musical excerpts reconfigured by PPP-based transformations versus RGP-based ones in terms of musical consistency and of attractiveness. Results indicate that PPP-transformed segments score distinctly better than RGP-transformed for the two criteria, suggesting that the preservation of implication systems plays an important role in the subjective acceptability of the transformation. Additionally, from the perspective of building an automatic recomposition system for artistic creation purposes, we introduce, in appendix, the preliminary version of an automatic method for decomposing segments into low-scale musical elements, taking into account possible phase-shifts between the musical surface of the melody and the metrical information.

## 1. INTRODUCTION

Music is usually considered as a sequential process, where sounds, group of sounds and motifs are occurring chronologically, following the natural unfolding of time. Under this approach, music is considered as a flow of information, the organization of which is essentially governed by the relations that develop between adjacent elements. This property of sequentiality is indeed central to many models

of music description and generation, including musicological models such as Schenkerian analysis [1], generative theories based on tree-like structures such as GTTM [2], or computational automata such as Markov chains [3].

From a complementary perspective, it is also commonly accepted that the organization of music is widely based on alternations of similarity and novelty which create patterns and systems of expectation and surprise that ultimately contribute to the structure of the musical discourse from a cognitive point of view [4] [5] [6]. These can be represented as a Polytopic Graph of Latent Relations [7] where each node of the graph represents a low-scale musical segment and vertices correspond to their relation within the expectation systems.

The aim of this work is to explore the polytopic model in terms of its relevance to account for the inner structure of musical segments, by assessing its potential use for the structural recomposition of music. In fact, as presented in section 2, the polytopic representation of a musical segment enables a large range of transformations by applying various permutations to its nodes, thus generating multiple reconfigurations of its musical content, with the same elements in a different order.

Specific permutations, called Primer Preserving Permutations (PPP), are of particular interest, as they preserve systems of analogical implications between metrically homologous elements within the segment [8]. The central hypothesis of the present work is that the musical consistency of PPP-transformed segments will therefore be less affected than it would be by an “ordinary” (i.e. randomly generated) permutation.

In section 2, we describe the implementation of the polytopic reconfiguration process and we elaborate on the organizational properties of Primer Preserving Permutations as well as their potential impact on the inner structure of musical segments.

Then, in section 3, we assess the relevance of the reconfiguration scheme (and its underlying hypotheses): we report on a perceptual test where subjects are asked to rate musical properties of MIDI segments, some of them have been reconfigured with PPPs while others were transformed by Randomly Generated Permutations (RGPs) designed so as to possess a comparable number of discontinuities.

In appendix, we introduce an automatic method for decomposing segments into low-scale musical elements, taking into account possible phase-shifts between the musical surface and the metrical information (for instance, anacrusis).

## 2. BACKGROUND AND FORMALISM

### 2.1 Musical objects and time-scales

Before detailing the background and formalism aspects of this work, it is important to specify what musical objects are under consideration in our study. Following Snyder’s “levels of musical experience” [9], one may identify three ranges of time-scales in music: an *event-fusion* level, up to  $1/32^{th}$  second (corresponding to early processing), an *intermediate* “melodic and rhythmic grouping” level, between  $1/16^{th}$  and 8 sec. (governed by short-term memory) and a *form* level, 16 sec. or above (resorting to long-term memory).

In this work, we focus on sectional units (i.e. the first time-scale of the form level) and we study their inner organization as the result of the relations existing between successive constituents at the intermediate level, around 1 sec (i.e. typically half-bars). We put a particular focus on melody, with the consequence that our low-scale objects are small groups of a few notes with a common harmonic background.

### 2.2 Polytopic representations of implication systems

The basic concept of a sequential implication system is that the observation of a given event by a subject with no particular preconception will trigger (to that subject) the expectation that the next event is likely to be similar to the first one. This is considered as even more so, in the case of repetition, as is expressed by Narmour’s implication principles for the analysis of basic melodic structures [10]:

$$\begin{aligned} A + A &\longrightarrow A \\ A + B &\longrightarrow C \end{aligned}$$

thus meaning that the repetition of two similar patterns  $A$  induces the expectation of a third similar pattern  $A$ , whereas two different patterns  $A$  and  $B$  trigger the expectation of something different from both:  $C$ . Narmour’s principles can be understood as a cognitive model based on Gestalt Theory, as mentioned in [11].

This sequential implication principle can be extended by now considering a *system* of elements viewed as forming the base of an analogical induction process [12]. For instance, consider the matrices below, and imagine what could be the missing elements in terms of “logical” implications:

A	B	2	4	$\cap$	$\downarrow$
E	.	8	.	$\cup$	.

As developed in [6], such square systems trigger an expectation process which spans over 2 time-scales simultaneously and which writes, in a formalism compatible with Narmour’s:

$$A + f(A) + g(A) \longrightarrow g(f(A))$$

and in particular:

$$\begin{aligned} A + B + A &\longrightarrow B \\ A + A + B &\longrightarrow B \end{aligned}$$

These two prototypical cases of square implication systems are indeed the basis of two very frequent structural patterns,  $ABAC$  and  $AABC$ , which can be understood as the denial, in  $4^{th}$  position, of the implication system triggered by the first 3 elements. But quite a number of other such redundant patterns can be embedded in this framework.

Further generalizing this principle by encompassing more time-scales, as in [13], leads to cubic (3-scale), tesseract (4-scale) and more generally  $n$ -cubic systems where  $n$  time-scales are considered simultaneously (see Figure 1).

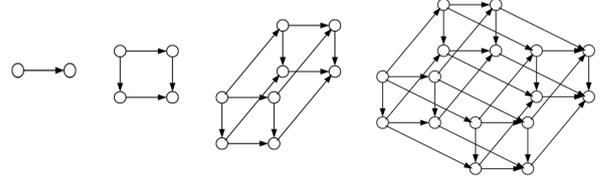


Figure 1. Graph representation of multi-scale implication systems. From left to right: segment, square, cube, tesseract.

When mapped with a sequence of musical events, these polytopic graphs can be used to represent analogical relations between musical objects in metrically homologous positions at different time-scales [7].

### 2.3 Structural reconfiguration by node permutations

There are many ways to define a permutation, but the most adequate one in the context of this work is to view it as a bijective function  $\varphi$  (i.e. a one-to-one correspondence) between the  $N$  time indexes of an original sequence  $x_0 \dots x_{N-1}$  and those of the permuted sequence  $x_{\varphi(0)} \dots x_{\varphi(N-1)}$ .

Applying a permutation to the time indexes creates a certain degree of disruption in the original flow of the sequence. In this paper, we characterize this fact by two properties:  $D$ , the number of *discontinuities* created by the permutation and  $E$ , the ( $\log_2$  of the) maximum time-interval (or *excursion*) between 2 consecutive elements in the permuted sequence.

$$\begin{aligned} D &= \#\{t \mid |\varphi(t) - \varphi(t-1)| \neq 1\}_{0 < t < N} \\ E &= \log_2 \max_{0 < t < N} |\varphi(t) - \varphi(t-1)| \end{aligned}$$

Among all possible permutations  $\varphi$ , a particular subset of them is focused on in this work. They are referred to as PPPs (for *Primer Preserving Permutations*) and were introduced by Louboutin et al. [8] as the set of permutations which preserve the systemic relations of the musical elements  $x_t$  in the sequence, by just interchanging the time-scales at which they develop. These permutations are therefore particularly interesting to investigate on the relevance of the implications systems (and their preservation) in the consistency of a musical segment.

In the case of a sequence of  $N=16$  elements, the polytope is a 4-cube, also called a *tesseract* (see Figure 2), and it can be viewed as being composed of 4 homologous lower-scale systems of 4 elements (formed by 4 parallel faces of the tesseract), themselves linked by an upper-scale system

PPP																		Disc.	Exc.
ORIG	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15		0	1
1	0	2	4	6	1	3	5	7	8	10	12	14	9	11	13	15		14	1
2	0	1	8	9	2	3	10	11	4	5	12	13	6	7	14	15		7	2
3	0	1	4	5	2	3	6	7	8	9	12	13	10	11	14	15		6	1
4	0	4	8	12	1	5	9	13	2	6	10	14	3	7	11	15		15	3
5	0	2	8	10	1	3	9	11	4	6	12	14	5	7	13	15		15	2

Table 1. Extensive definition of the 6 PPPs and their properties (discontinuity and excursion - see text).

RGP																		Disc.	Exc.
1	0	3	4	2	7	1	6	5	8	13	10	9	11	14	12	15		14	1
2	0	4	5	6	1	3	8	9	10	11	12	13	14	2	7	15		7	2
3	0	1	2	5	3	4	6	7	8	9	10	12	13	11	14	15		6	1
4	0	5	3	8	6	4	14	2	10	1	9	12	7	11	13	15		15	3
5	0	9	7	1	6	4	2	8	10	3	11	14	13	5	12	15		15	2

Table 2. Examples of RGPs and their properties (discontinuity and excursion - see text).

formed by the first element of each lower-scale system (on a face which is perpendicular to the 4 lower-scale ones) (see Figure 3).

Mapping these systems of faces by a permutation, while preserving time order within faces, yields 5 possibilities (plus the identity), which correspond to the PPPs defined in Table 1. Note that each PPP maps 0 to 0 and  $N-1$  to  $N-1$ .

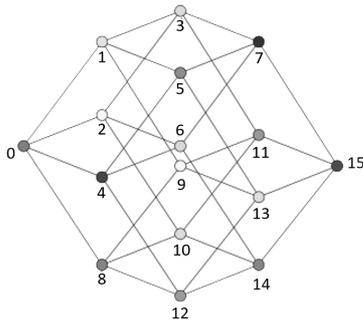


Figure 2. Example of the polytopal representation of a time sequence in the case of a tesseract.

By construction, PPPs preserve implication systems of 4 elements in the sense that sets of 4 parallel faces in the tesseract are mapped on another set of parallel faces. By doing so, analogical systems are preserved, and only the scales at which they develop are modified: for instance,  $[x_0x_1x_2x_3]$  in the original is “transferred” to  $[x_0x_4x_1x_5]$  with PPP1 and  $[x_0x_4x_8x_{12}]$  with PPP4. Moreover, the last element of a system never occurs before all the elements of all the systems it belongs to, have themselves occurred, therefore preserving a principle of causality in all the analogical implications.

For comparison purposes, Table 2 illustrates 5 *Randomly Generated Permutations* (RGPs), which also start with 0, end with  $N-1$ , and have the same profile as their corresponding PPPs in terms of discontinuity and excursion. It can be easily checked that, unless incidentally, analogical systems are not preserved by RGPs.

Ultimately, a given permutation is applied to a musical se-

quence of events by reading and copying (in the permuted order) the original musical material after having segmented into proper low-scale elements. Figure 4 illustrates this process on a 8-bar melodic line (original at the top), processed as a sequence of  $N=16$  half-bar (2-beat) elements, resulting in reconfigured melodic lines, the organization of which is either driven by PPPs or by RGPs.

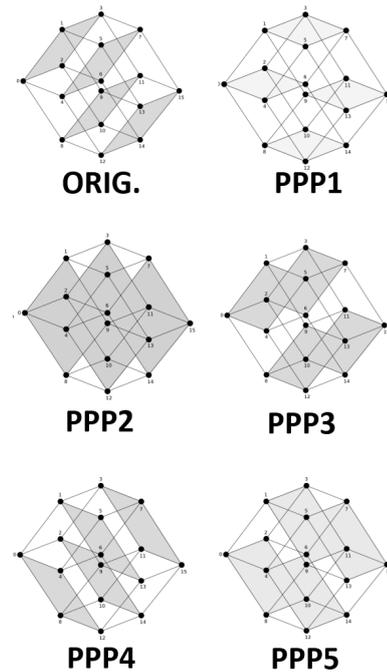


Figure 3. Representation of the 6 systems of parallel faces on the tesseract and their corresponding PPP in reference to the original.

## 2.4 Handling musical surface time-shifts

As a prerequisite to the application of a permutation to a sequence of musical objects, it is of primary importance to define precisely the location and boundaries of the objects that will be subjected to the transformation.

In this work, elementary objects are melodic fragments

Original  $\text{G} \text{A} \text{B} \text{C} \text{B} \text{A} \text{G} \text{F}\sharp$

PPP 1  $\text{G} \text{A} \text{B} \text{C} \text{B} \text{A} \text{G} \text{F}\sharp$

PPP 2  $\text{G} \text{A} \text{B} \text{C} \text{B} \text{A} \text{G} \text{F}\sharp$

PPP 3  $\text{G} \text{A} \text{B} \text{C} \text{B} \text{A} \text{G} \text{F}\sharp$

PPP 4  $\text{G} \text{A} \text{B} \text{C} \text{B} \text{A} \text{G} \text{F}\sharp$

PPP 5  $\text{G} \text{A} \text{B} \text{C} \text{B} \text{A} \text{G} \text{F}\sharp$

RGP 1  $\text{G} \text{A} \text{B} \text{C} \text{B} \text{A} \text{G} \text{F}\sharp$

RGP 2  $\text{G} \text{A} \text{B} \text{C} \text{B} \text{A} \text{G} \text{F}\sharp$

RGP 3  $\text{G} \text{A} \text{B} \text{C} \text{B} \text{A} \text{G} \text{F}\sharp$

RGP 4  $\text{G} \text{A} \text{B} \text{C} \text{B} \text{A} \text{G} \text{F}\sharp$

RGP 5  $\text{G} \text{A} \text{B} \text{C} \text{B} \text{A} \text{G} \text{F}\sharp$

Figure 4. Example of the 11 types of reorganized variants on a 8-bar melodic line.

of 1/2-bar long which correspond to 2 beats in the case of a 4-4 meter (as is the case in the example of Fig 4).

However, for reconfiguration purposes, these “objects” may not be optimal if they are blindly synchronized on downbeats (and sub-downbeats). In a number of cases, the musical surface of the “proper” low-scale melodic elements should be slightly shifted in order to correspond to an optimal grouping of the notes and therefore a better result after permutation.

This situation is illustrated in Figure 5 where the first melodic element should be considered as starting 1.5 beat before the first downbeat of the section.

In designing the perceptual test described in the next section, this optimal time-shift has been adjusted manually on a case-by-case basis. However, we present in the appendix, a preliminary algorithm that has been developed to estimate the time-shift automatically.

### 3. PERCEPTUAL EXPERIMENTS IN STRUCTURAL RECONFIGURATION

In this section, we present the details of the methodology which has been used for the evaluation of polytopic reconfigurations. The general principle has been to design a perceptual test where subjects are presented with musical excerpts which are either PPP-transformed or RGP-transformed, and where they are asked to rate (blindly) these excerpts both in terms of consistency and attractive-

ness. We then study the difference of ratings across subjects between the two types of transformations.

#### 3.1 Test data

The experiments are performed on the RWC POP corpus, a subset of the Real World Computing (RWC) music database created for scientific purposes by Goto et al. [14]. This dataset has been designed for researchers. It is available for a small fee and without restrictions.

The RWC POP set is made of 100 songs in WAV and MIDI formats. According to the authors, they were composed partly in the style of the 80s American hits and partly in the 90s Japanese style. This corpus is very commonly used in various task in Music Processing and Information Retrieval.

Using the RWC songs in our tests has an additional advantage: there is virtually no risk that subjects participating to the test already know the songs from which the excerpts are stemming. This is a favorable situation as the familiarity with a particular song could affect the rating of the transformed excerpts in an uncontrolled way.

For our experiments, a subset of 24 songs has been selected for which the first instance of chorus is exactly 8-bar long. The reconfiguration process is applied to the MIDI version of the chorus. The elements of interest are the melodic lines, the accompaniment (harmony and bass) and the drums. We consider that these elements provide an acceptable rendering of the structural information of the



Figure 5. Example of a melodic line starting 1.5 beat before the first downbeat of the section.

chorus and they all are transformed synchronously by the permutations. The average duration of a chorus is 19.5 seconds.

As presented in section 2, these transformations are performed on the original chorus after having segmented it into 16 elements (with a possible shift of the musical surface of the melody, as explained in section 2.4). Then, the 10 permutations (5 PPPs and 5 RGPs) are applied to the 16 elements, resulting in a re-ordering of the original choruses, i.e. 10 new musical contents (per chorus), which we will call “variants” of the original.

To summarize, for each of the 24 choruses, the following 11 variants are considered:

- the original version of the chorus
- 5 PPP-transformed variants (PPP<sub>1</sub> to PPP<sub>5</sub>)
- 5 RGP-transformed variants (RGP<sub>1</sub> to RGP<sub>5</sub>)

The perceptual test is therefore conducted on  $24 \times 11 = 264$  distinct excerpts.

### 3.2 Protocol

The perceptual experiments are performed with 66 subjects, selected among colleagues and relatives of the authors<sup>1</sup>. About 25% of the subjects are female and 75% male, aged between 22 and 55 years old.

In order to avoid the bias that could arise if a subject gets familiar with a particular chorus, each subject is presented with one and only one variant of each of the 24 choruses, in a random order. The total number of tests in our experiments is therefore equal to  $66 \times 24 = 1584$ , i.e. 144 tests per variant. Moreover, the 11 variants are distributed as evenly as possible for each subject, i.e. typically 2 (or occasionally 3) per subject.

After a brief general presentation of the test (during which the subjects are *not* provided with any detail on the scientific motivation of the test), they are asked to answer, for each excerpt, two questions formulated as follows:

1. “Please give your opinion as of the consistency of the musical construction of this passage”.
2. “Please give your opinion as of the degree of musical attractiveness of this passage”

The subjects must respond by placing a cursor on a 5-level scale corresponding to 5 different levels of evaluation (from *very bad consistency* to *very good consistency* and from *very unattractive* to *very attractive*). They also have the possibility to position the cursor between two graduations, thus offering them 9 levels of rating altogether.

<sup>1</sup> For obvious reasons, the authors themselves were not included in the panel of subjects.

Asking two different questions aims at leading subjects to decorrelate as much as possible their rating of the acceptability of the musical construction (question 1), from their own personal taste (which they can express in their response to question 2).

### 3.3 Scoring

For each subject, we thus collect 24 consistency ratings and 24 attractiveness ratings.

Let us denote as  $r$ , the generic variable which designates such ratings (ignoring for the moment whether it is *consistency* or *attractiveness*, for the sake of notations’ simplicity).

The 24 ratings  $r_{jk}$  produced by subject  $j$  ( $1 \leq j \leq 66$ ,  $1 \leq k \leq 24$ ) are distributed into the 11 variants:  $\mathcal{O}$  for original,  $\mathcal{P}_i$  for PPP <sub>$i$</sub>  ( $1 \leq i \leq 5$ ) and  $\mathcal{P}_i^*$  for RGP <sub>$i$</sub>  ( $1 \leq i \leq 5$ ). These individual ratings are averaged separately, thus leading to 11 mean ratings (one per type of variant):

$$\mu_{0j} = \frac{1}{m_{0j}} \sum_{\mathcal{O}} r_{jk} \quad \text{for the original choruses} \quad (1)$$

$$\mu_{ij} = \frac{1}{m_{ij}} \sum_{\mathcal{P}_i} r_{jk} \quad \text{for the 5 PPP variants} \quad (2)$$

$$\mu_{ij}^* = \frac{1}{m_{ij}^*} \sum_{\mathcal{P}_i^*} r_{jk} \quad \text{for the 5 RGP variants} \quad (3)$$

Note that, in practice,  $m_{0j}$ ,  $m_{ij}$  and  $m_{ij}^*$  are equal to 2 or 3 and their sum is equal to 24.

To evaluate the relative degradation created by the various reconfigurations of the music material, we can measure:

$$\delta_{ij} = \mu_{0j} - \mu_{ij} \quad (4)$$

$$\delta_{ij}^* = \mu_{0j} - \mu_{ij}^* \quad (5)$$

namely the signed difference, for a given subject  $j$ , between his/her ratings of the reconfigured variants and his/her ratings of the originals.

For each subject and variant, we can also compute:

$$\pi_{ij} = \mu_{ij} - \mu_{ij}^* = \delta_{ij} - \delta_{ij}^* \quad (6)$$

which measures the (positive or negative) preference of PPP <sub>$i$</sub> -transformed excerpts over RGP <sub>$i$</sub> -transformed ones, for speaker  $j$  (where PPP <sub>$i$</sub>  and RGP <sub>$i$</sub>  are comparable in terms of discontinuities  $D$  and excursion  $E$ ).

Ultimately, we focus on 3 scores:

$$\pi_j = \frac{1}{5} \sum_{i=1}^5 \pi_{ij} \quad (7)$$

$$\delta_i = \frac{1}{66} \sum_{j=1}^{66} \delta_{ij} \quad (8)$$

$$\delta_i^* = \frac{1}{66} \sum_{j=1}^{66} \delta_{ij}^* \quad (9)$$

where  $\pi_j$  provides a global preference score (positive or negative) on PPPs over RGP for each subject  $j$ , while  $\delta_i$  (resp.  $\delta_i^*$ ) provides a degradation score for each of the PPP- (resp. RGP-) reconfigured variants, averaged over all subjects.

These two quantities are calculated separately for consistency ratings and for attractiveness ratings.

### 3.4 Results

Figure 6 and 7 depict the distributions of consistency and attractiveness preference scores ( $\pi_j$ ), ranked from lowest to highest, over the panel of 66 subjects. In both cases, the distributions are visibly shifted towards positive values, especially for consistency ratings. Indeed, for consistency, 57.5 subjects have a positive preference for PPPs versus 8.5 having a negative preference<sup>2</sup> (i.e. 87.1% vs 12.9%). The average score for positive judgments amounts to +0.89 whereas it rests at -0.30 only, for negative judgments. For attractiveness, the proportions are still clearly in favor of PPPs, but not as contrasted (74.2% vs 25.8%), with average scores of +0.74 and -0.55 respectively.

Figure 8 and 9 represent the relative degradation scores ( $\delta_i$  and  $\delta_i^*$ ) for the 10 variants, ranked in increasing order of degradation. From the ranking of the permutations, it is noticeable that the degradation score is primarily correlated with the number of discontinuities of the permutations, as the two permutations with lower  $D$  show a smaller value of  $\delta$  as opposed to the three others.

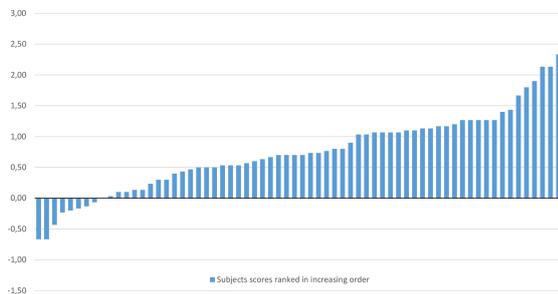


Figure 6. Musical consistency: relative PPP-preference  $\pi_j$  of the test subjects, ranked in increasing order

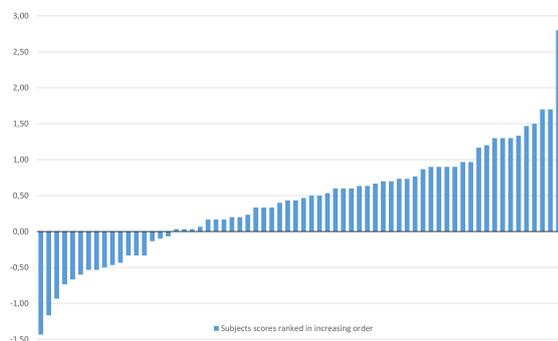


Figure 7. Musical attractiveness: relative PPP-preference  $\pi_j$  of the test subjects, ranked in increasing order

Globally, these results indicate that PPP-based reconfigurations tend to be less disruptive than RGPs against the

<sup>2</sup> counting as 0.5 in each category, the subject who scores exactly 0.

perceived consistency of musical segments, thus supporting the hypothesis that the preservation of expectation systems contributes to their inner structure.

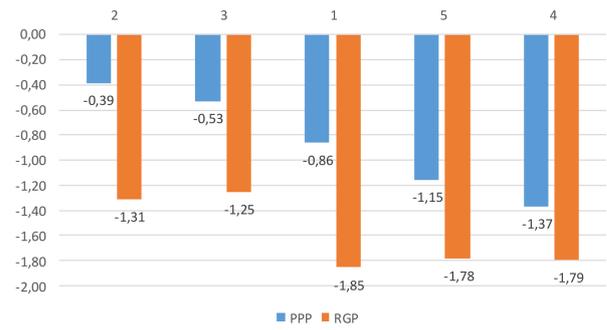


Figure 8. Musical consistency: degradation scores  $\delta_i$  and  $\delta_i^*$  for the different permutation variants (PPP and RGP)

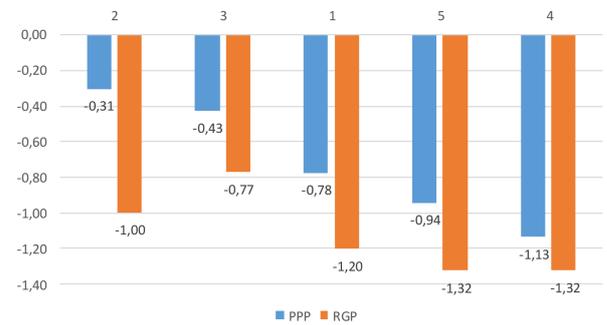


Figure 9. Musical attractiveness: degradation scores  $\delta_i$  and  $\delta_i^*$  for the different permutation variants (PPP and RGP)

## 4. CONCLUSIONS

Systems of relations between elements play a key role in structural constructions in many cognitive dimensions. The experiments reported in this paper constitute an initial investigation on the role of analogical systems (modeled by polytopic graphs) in the perception of segmental structure in pop music.

These results indicate a very noticeable trend towards the hypothesis that the preservation of the analogical implication systems in musical segments impacts positively the perception of their inner structure and hence, their acceptability. However, more extensive tests on a larger population and with more varied musical excerpts are certainly needed to consolidate these first results, and refine their precise scope.

In parallel, we intend to develop the proposed reconfiguration scheme into a music creation tool which could be used by composers to experiment new possibilities in employing musical material with multiple purposes, results and effects. In this context, the polytopic representation is an additional advantage, as it is bound to make manipulation interfaces more intuitive and easy to use.

Ultimately, the development of an automatic segmentation process is a complementary goal towards a fully operational concept.

## Appendix

### Melodic segmentation with a compressibility criterion

In order to perform a relevant permutation-based transformation to a sequence of musical objects, it is crucial to define precisely the location and boundaries of the objects on which the transformation is applied.

As mentioned in section 2.4, it is quite common that the structure of the melodic line is time-shifted with respect to the phase of the metrical pulsation. As a consequence, it is important to take into account this time-shift when defining the low-level melodic objects. In this section, we present a preliminary method to automatically estimate this time-shift.

For doing so, we estimate a segmentation of the melodic surface by optimizing the grouping of the notes using a compressibility criterion.

### Meter, segmentation and phase-shift

For simplicity and consistency with the rest of our work, we consider musical segments which are 8-bar long, and 4|4 meter, i.e  $L = 32$  beats, and we assume that we want to segment the excerpt in  $m$  elementary objects. In this work  $m = 16$ .

Let  $S$  be the sequence of instants where the strong beats fall, according to the meter and the bar:

$$S = (t_0, t_1, \dots, t_p, \dots, t_{m-1}) \quad (10)$$

Let us now denote as  $\Sigma$  another segmentation that is not necessarily synchronized with downbeats.

$$\Sigma = (\tau_0, \tau_1, \dots, \tau_p, \dots, \tau_{m-1}) \quad (11)$$

In the general case we can write:

$$\tau_p = t_p + \theta_p \quad (12)$$

where  $\theta_p$  is the phase-shift of the musical surface of segment  $p$  in relation to the strong beat location  $t_p$ .

In compliance with the work reported in the body of this article, we further assume that  $\theta_p$  does not depend on  $p$ :

$$\tau_p = t_p + \theta \quad (13)$$

### Properties of the phase-shift

When  $\theta = 0$ , the melodic segments are considered to be starting synchronously with the downbeat. If  $\theta > 0$ , this means that the melodic objects display some phase-delay with the beat, whereas if  $\theta < 0$ , they start in anticipation (as in the case of an anacrusis).

Let  $\alpha$  be the ‘‘size’’ of one elementary object in terms of the number of beats, i.e.:

$$\alpha = \frac{L}{m} \quad (14)$$

Here  $\alpha = 2$ .

Quite naturally, we assume that the phase-shift cannot exceed the size of the elementary objects, i.e.:

$$-\alpha \leq \theta \leq \alpha \quad (15)$$

Fig. 10, shows the segmentation of a 8-bar melody, represented in MIDI format. The first 3 notes of this section are located with a phase-shift of -1,5 (beat) with respect to the metric boundaries: the thick lines correspond to the downbeat instants and the thin ones correspond to the segmentation obtained with  $\theta = -1.5$  (beat).

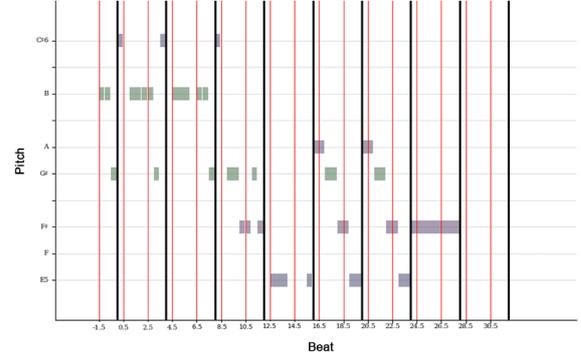


Figure 10. Example of a melodic line segmentation starting 1.5 beat before the first downbeat of the section ( $\theta = -1.5$  beat).

### A compressibility criterion for segmentation

In order to estimate an optimal value of  $\theta$ , we define a compressibility criterion which scores how redundant is the sequence of elements resulting from a given segmentation.

This approach is inspired from Kolmogorov’s information theory [15] and relates, in its spirit, to recent work exploring the potential of approaches based on complexity and compression for modeling music contents (for instance [16] [17]).

Let now  $\Sigma$  be a segmentation as in equation 11 and  $\sigma_p$  the elementary object of  $\Sigma$  within the time interval  $[\tau_p, \tau_{p+1}[$ .

We first define the *parallel run-length* between two melodic elements as the relative duration  $d \in [0, 1]$  during which they remain similar to each other (i.e. identical, up to a translation). We denote as  $b$  the translation between the two similar fragments and we assign to  $b$  a binary value of 0 (if no translation) or 1 (when a translation is observed).

We then define an elementary cross-compressibility score function  $c(\sigma_p, \sigma_q)$  between two melodic objects  $\sigma_p$  and  $\sigma_q$ , by combining  $d$  and  $b$ :

$$c(\sigma_p, \sigma_q) = d(\sigma_p, \sigma_q) - \lambda b(\sigma_p, \sigma_q) \quad (16)$$

For the time being,  $\lambda$  is tuned empirically.

We then define a compressibility score function for each elementary object  $\sigma_p$  within  $\Sigma$ , which depends on the previous objects in the segmentation, for instance:

$$z(\sigma_p) = \frac{1}{p} \sum_{h < p} c(\sigma_h, \sigma_p) \quad (17)$$

Finally, we compute the entire segmentation compressibility score  $Z(\Sigma)$  as:

$$Z(\Sigma) = \frac{1}{m} \sum_p z(\sigma_p) \quad (18)$$

Because  $\theta$  is the same across segments, all possible segmentations  $\Sigma$  can be tested exhaustively, and the optimal segmentation is chosen as the one with the highest compressibility score.

Fig. 11 depicts the behavior of  $Z$  for a particular example, with  $\theta$  ranging from  $-2$  to  $2$  by steps of  $0.25$  beat. Score values are normalized to 1 for the maximum value.

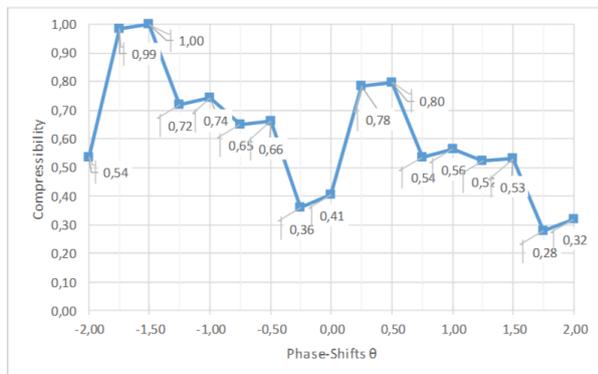


Figure 11. Behavior of the compressibility score  $Z$  for a particular 8-bar melody, with  $\theta$  ranging from  $-2$  to  $2$  beats.

### Current performance level

In its current version, the results provided by this algorithm have been evaluated over the 24 choruses used in the perceptual experiments, by comparing the automatic estimations of the melodic phase-shifts with those determined by a manual annotation: in 10 cases (out of 24), the automatic algorithm provided the same result as the expert.

This approach is currently being improved but the current results encourage us to further investigate the method, so as to evaluate its full potential.

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