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Effects of contaminants and trophic cascade regulation on food chain stability: application to cadmium soil pollution on small mammals - raptor systems

Virgile Baudrot^{1,2,*}, Clémentine Fritsch¹, Antoine Perasso¹, Malay Banerjee³ and Francis Raoul¹

¹Université Bourgogne Franche-Comté - UMR CNRS 6249 Chrono-environnement, 25030 Besançon, France ²Université Lyon 1 - UMR CNRS 5558 LBBE, 69300 Villeurbanne, France ³Department of Mathematics and Statistics, IIT Kanpur. Kanpur 28016, India

E-mail addresses Virgile Baudrot: virgile.baudrot@univ-fcomte.fr; Clémentine Fritsch: clementine.fritsch@univ-fcomte.fr; Antoine Perasso: antoine.perasso@univ-fcomte.fr; Malay Banerjee: malayb@iitk.ac.in; Francis Raoul: francis.raoul@univ-fcomte.fr

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Corresponding author Virgile Baudrot Mail: virgile.baudrot@posteo.net Phone Number: +33(7)-82-11-60-69

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Abstract

Within the current context of global change, ecosystems face simultaneously multiple stres-2 sors such as environmental pollution, excessive enrichment, and additional disturbances affecting population dynamics. Numerous theoretical and empirical studies explored the transfer of contaminants by food ingestion between trophic levels, and how contaminant effects on survival and fecundity may change regime shifts of classical predator-prey dynamics. However, the extent to which those contaminants may influence the cascade effect of external stressors. as a change in resources (bottom-up cascade) or a variation in predator abundance (top-down cascade) is still poorly understood. We develop a data-driven model to explore how soil contamination modulate the food chain stability and resilience to changes in prey nutrient and in 10 the apex predator mortality rate. We particularly focus on the ecotoxicological impact of the 11 trace metal, cadmium, on a widespread raptor, the barn owl (Tyto alba), feeding on several 12 prey distinct by their trophic positions: herbivores (*Microtus* spp), omnivores (wood mouse 13 Apodemus sylvaticus and bank vole Myodes glareolus) and insectivores (shrews: Crocidura spp 14 and *Sorex* spp). Our model reveals the alternative steady states in population dynamics and 15 the occurrence and position of regime shifts where a subtle change in conditions causes a 16 sudden shift in the ecological system. Based on mathematical modelling and bifurcation anal-17 ysis, the results show for instance that under toxicity threshold, where no population decline 18 is observed, the contaminant weakens food-chain resilience. Then at higher contamination, 19 the toxic effects on predator releases the top-down control over prey that may increase. This 20 range of chemical stress overturns the paradox of enrichment, a central concept in trophic cas-21 cade theory. The transition phase at the highest contamination, where the whole community 22 collapse, exhibits multiple patterns, from smooth to abrupt, depending on external stressors 23 and the prey population. Thus, this work provides a methodology to identify ecological traits 24 of preys that are critical for transferring adverse effects of contaminants across the whole 25 community. 26

27 **1** Introduction

Across the globe, anthropogenic activities increase the input of contaminants in ecosystems, dis-28 turbing their regime and potentially threaten their health. One of the most widely observable 29 impact is the lost of apex predators (Estes et al., 2011; Heath et al., 2014). As a consequence, 30 there is a surge in attention concerning the effect of pollution at the food web scale. The response 31 of a food-chain to external disturbances may be gradual (i.e., from a fixed state to another or to 32 an oscillating pattern), or remains inert until a sudden regime shift, a critical transition, where 33 the food-chain structure and composition are drastically altered (Scheffer, 2009). These sudden 34 changes often correspond to abrupt degradation of ecosystem services which are difficult, if not impossible, to recover (Rockström et al., 2009). Due to their socio-economical importances, analysis 36 of discontinuous transitions (i.e., regime shift) have been widely studied (Scheffer et al., 2015), but 37 very few theoretical works have considered terrestrial food-chain impacted by the combination of 38

³⁹ a chemical contaminant and external disturbances (i.e., trophic cascades). This lack of a mathe⁴⁰ matical description on how polluted ecosystems respond to external stressors (e.g., eutrophication,
⁴¹ climate change, diseases) is due to the combination of many direct and indirect effects (Fleeger
⁴² et al., 2003; Rohr et al., 2006; Relyea and Hoverman, 2006; De Laender et al., 2015)

Direct effects of severe contaminant exposure as population declines (by increasing mortality or 43 reproductive failure) are possibly predictable from controlled laboratory toxicity tests. Those tests 44 are the classical approach to assess the potential risk of contaminants in ecosystems, and most 45 of them use one single species and one chemical compound, and quantify the toxicological effect 46 through several threshold of exposure concentration (i.e., NOAEL, LOAEL, LC_{50}) (Villeneuve 47 and Garcia-Reyero, 2011). However, there is a difficulty in predicting the ecological effects of 48 an environmental pollution from those laboratory results (Mineau, 2005; Villeneuve and Garcia-49 Reyero, 2011). 50

Indeed, the exposure of vertebrate wildlife to environmental contaminants integrates complex 51 interactions between the routes of exposure (inhalation, ingestion, dermal absorption and maternal 52 transfer), the intensity (concentration in the vector agent and bioavailability), the frequency and 53 duration of the exposure, and the life history traits of exposed organisms (Smith et al., 2007). For 54 instance, among factors affecting metals body burden in small mammals, several field studies en-55 lightened the critical role of the feeding behavior and the habitat use (Veltman et al., 2007b; Fritsch et al., 2010a; Van Den Brink et al., 2011). In addition to this great variability in the exposure, 57 the fate of a contaminant within the organism (i.e., toxicokinetics) and its toxicological effect (i.e., 58 toxicodynamics) differ greatly between and within species (Rainbow, 2002; Burger, 2008; Fritsch 59 et al., 2010a). This complexity in exposure and in the response of organisms induces a dispro-60 portional impact on the constituent species of a community and therefore many indirect effects 61 (e.g., changes in the diversity of resources and/or consumers) (Rohr et al., 2006). For instance, a 62 non-sensitive species may still be affected when one of its resource, predator, mutualistic species 63 or competitor is affected by the contaminant (Fleeger et al., 2003; Clements and Rohr, 2009). 64

One of the most known type of propagation of indirect effects in food web is the "trophic 65 cascade" where the food chain is disturbed by either a change in the abundance of the highest 66 trophic level (i.e., top-down cascade) or by a change in the resources (i.e., bottom-up cascade) 67 (Carpenter et al., 1985; Heath et al., 2014). For instance, a top-down cascade initiated by a 68 decrease in predator abundance releases the pressure on its prey which consequently increase 69 in density and subsequently induce more pressure on prey resources. The reverse process of a 70 bottom-up cascade in a three-level food chain, may start by an increase/decrease of prey resources 71 favoring/constraining in first prey density and then its predator (Heath et al., 2014). Another 72 well-known bottom-up effect is the "paradox of enrichment" where the increase of prey resources 73 (i.e., the carrying capacity) has a destabilizing effect where population dynamics of prey and 74 predators shift from a fixed stable state to an oscillating behavior (Rosenzweig, 1971). However, 75 recent studies in aquatic systems showed that exposure to contaminants may inhibit the paradox 76

of enrichment by reducing oscillations and driving the system back to a fixed equilibrium (Prosnier
et al., 2015; Huang et al., 2015).

Many individual-based models for exposure of terrestrial wildlife to contaminants have been 79 proposed (Loos et al., 2010b; Schipper et al., 2012; Schmitt et al., 2015). Those highly detailled 80 models are very efficient for the management of a specific ecosystem (Schmitt et al., 2015; DeAngelis 81 and Grimm, 2014), but the wide variety of components and mechanisms induces a black box effect 82 hiding more or less the possibility of an analytical description of critical transitions (Gómez-Mourelo 83 and Ginovart, 2009). Therefore, in order to achieve a stability analysis of steady state(s) (i.e., 84 namely a bifurcation analysis) (Kooi et al., 2008; Huang et al., 2015), we develop an ODE model 85 including the ecological dynamics of a two-level food chain with a soil compartment, small mammals 86 (rodents and shrews) as preys of the raptor barn owl (Tyto alba) contaminated by the trace metal 87 cadmium (Cd). Presence of Cd occurs in the Earth's crust at relatively low concentration (0.1-0.5)88 ppm), and Cd is well-known to be highly toxic since non-biodegradable and because of its ability 89 to bind with many organic molecules that distribute it in all or part of the organism (Hopkin et 90 al., 2012). The main anthropogenic sources are non-ferrous metal mining and refining, application 91 of phosphate fertilizers and byproducts of battery manufacturer (Burger, 2008; Faroon et al., 2012). 92 Mammals are mainly contaminated through oral consumption of contaminated water and food 93 items (Smith et al., 2007). Moreover, there is a great variety of small mammal diet composition with a gradient from herbivores to carnivores by including omnivores species which can induce 95 various patterns of exposure and responses to environmental contaminants within this mammal 96 group and shape the exposure of their predators. Similarly, while birds may be contaminated 97 by direct unintentional ingestion of the contaminant (human poisoning, chemically treated seeds, 98 polluted water), secondary poisoning through the consumption of contaminated food items is 99 more common (Smith et al., 2007). Due to their high trophic positions, their scavenging activities, 100 their large spatial living area and long lifespan over which to accumulate contaminants raptor 101 species are highly exposed to persistent and/or bioacumulative contaminants (Gómez-Mourelo 102 and Ginovart, 2009; Bustnes et al., 2013; Espín et al., 2016). 103

Based on empirical scenarios and data, our aims are to provide a theoretical model on how 104 external stressors distributed in food chains by trophic cascades modulate the occurrence and 105 strength of regime shifts emerging in polluted ecosystems. We first explore different exposure sce-106 narios of the predator according to trophic position of preys (herbivores, carnivores or omnivores). 107 Then, we analyze the occurrence and position of regime shifts in the predator-prey dynamics with 108 variations in Cd concentration in soils. Finally, we test the sensitivity of the system to external 109 disturbance inducing trophic cascade effects: variations in prey resources and in intrinsic predator 110 mortality rate. 111

112 2 Methods

¹¹³ 2.1 Formulation of the general model

Contaminants are commonly measured in concentration per biomass of an individual, $[\mu g.g^{-1}]$ 114 denoted ppm. In the terrestrial ecotoxicological system, we consider a soil with contaminant con-115 centration denoted by C_s in $[\mu g.g^{-1}]$. Cadmium being a persistent contaminant (neither degra-116 dation nor metabolization), we assumed C_s to be constant since the transfer of contaminant to prey species cannot significantly change the soil concentration (i.e., negligible over the considered 118 period owing to the quantities in respectively the soil and biomass compartments, and included in 119 a balanced uptake/release cycle), and no external inputs of Cd in soils can be expected since the 120 main point source is no longer emitting cadmium. Also, in the system under consideration, several 121 publications showed the same order of magnitude of soil contamination in samplings from 1995 to 122 2006 (while not exactly on the same locations) (Sterckeman et al., 2000; Sterckeman et al., 2002; 123 Pruvot et al., 2006; Douay et al., 2009). 124

Then, the contaminant is transferred to a barn owl's preys (i.e., small mammal species), which 125 are exposed to the environmental contaminant mainly through ingestion of contaminated foodstuffs 126 (i.e., trophic transfer), and Cd accumulates in their tissues. We denote x the density of the prey 127 species and B_x the mean biomass of an individual of that species. The notation C_x holds for the 128 mean concentration of the contaminant in one individual, commonly called the body burden of the 129 prey. The growth function of the prey population is a function $g_x(x, C_x)$ in $[day^{-1}]$ depending on 130 the population density x and the concentration of the contaminant C_x . The additional mortality 131 due to pollution is a function $\mu_x(C_x)$ in $[day^{-1}]$. The dose-response curve $\mu_x(C_x)$ is defined by a log-132 normal cumulative distribution function as in Loos et al. (2010a) (see detailled parameterization 133 hereafter, section 2.2.2 and Supporting Information). We denote $\kappa(C_s)$ the rate of transfer of 134 the contaminant from soil to prey which follow a log-log linear regression (i.e., $\ln(C_x) = a +$ 135 $b\ln(C_s)$ defined from data, see section 2.2.1). The rate of excretion of the contaminant in the prey 136 population is a constant denoted by $k_{out.x}$. 137

The highest level of the food chain is the predator with density z. The predator feeds on prey at 138 a rate $\Phi(x)$, which is called the functional response. We assume that predator is only contaminated 139 through this trophic interaction with an absorption coefficient η (i.e., bioavailability). The excretion 140 rate of the contaminant by the predator is denoted $k_{out,z}$. Previous ecotoxicological model based 141 on ODEs were considered in aquatic system, where every prey species, whatever their trophic 142 level, are exposed to the contaminant present in the water compartment (Kooi et al., 2008; Bontje 143 et al., 2009; Huang et al., 2015). In our terrestrial ecotoxicological system, we assume the predator 144 not to be exposed directly to soil contaminant. We call $\psi(C_z)$ the stepwise linear function, equation 145 (4), of reproduction efficiency of the predator depending on contaminant concentration within the 146 predator denoted C_z , m the natural death rate of the predator, and $\mu_z(C_z)$ the linear function, 147 equation (5), standing for the additional mortality rate due to the contaminant. 148

With all the previous assumptions, the model for the transfer of contaminant is given in 149 Supporting Informations S1.1. Also, a classical growth function for rodents is the logistic type 150 growth rate. We then assume that the contaminant affects the intrinsic growth rate: $g_x(x, C_x) =$ 151 $\pi(C_x)(1-x/K)$, with $\pi(C_x)$ following a log-normal cumulative distribution function (Loos et 152 al., 2010a) (see parameterization in section 2.2.2 and Supporting Information). The carrying ca-153 pacity K represents the resource of prey and is used as the parameter for bottom-up cascade in the 154 bifurcation analysis. For top-down cascade effect, we used the natural mortality rate of the preda-155 tor, m. Prey-dependent functional response satisfies the properties: $\Phi(0) = 0$ and $\Phi'(x) > 0, x > 0$. 156 Thus, it is straightforward to express the dynamics as: 157

$$\begin{cases} \frac{dx}{dt} = x\pi(C_x)\left(1 - \frac{x}{K}\right) - \overset{\text{additional mortality predation}}{\mu_x(C_x)x} - \Phi(x)z \\ \frac{dC_x}{dt} = \overbrace{\kappa(C_s)}^{\text{exposure}} - C_x \left(\overbrace{k_{out,x} + \pi(C_x)\left(1 - \frac{x}{K}\right)}_{\text{excretion}}\right) \\ \frac{dz}{dt} = \overbrace{z\psi(C_z)\Phi(x)}^{\text{growth rate}} - \overbrace{z(\mu_z(C_z) + m)}^{\text{mortality rate}} \\ \frac{dC_z}{dt} = \overbrace{\eta\frac{B_x}{B_z}\Phi(x)C_x}^{\text{intake rate}} - C_z \left(\overbrace{k_{out,z} + \psi(C_z)\Phi(x)}_{\text{excretion}}\right) \end{cases}$$
(1)

2.2 Parameterization of transfers and effects of cadmium in a soil-small mammals-raptor food chain

For parameterization, we consider the case of cadmium (Cd) transfer in a trophic chain from soil to small mammals and finally to a raptor feeding on these preys (see Fig. 1). Cadmium does not appear to have biological function in small mammals and birds, but is well-known to be one of the most mobile toxic metals (Cooke et al., 2011; Wayland et al., 2011). In this section, we parameterize model (1) to obtain five food chains corresponding to five different small mammal prey species (herbivores: *Microtus* spp ; omnivores: *Apodemus sylvaticus* and *Myodes glareolus* ; carnivores: *Sorex* spp and *Crocidura* spp) and one raptor predator, the barn owl (*Tyto alba*).

¹⁶⁷ 2.2.1 Prey exposure to the contaminant

When Cd is ingested through the diet, the absorption is around 1 to 5 % (Andersen et al., 1994; Schipper et al., 2008; Cooke et al., 2011). Many study use a fixed contaminant absorption efficiency at 2% which is also used in the present study (Schipper et al., 2008; Loos et al., 2010a). Exposure to cadmium is mainly chronic (a gradual accumulation from diet). The excretion rate of cadmium is long because of the binding to metallothionein (MT) (Fritsch et al., 2010a; Cooke et al., 2011). The half-lifes of Cd is in the range of [100 - 300] days in rats (Cooke et al., 2011) what would give an excretion rate of: $-\ln(1/2)/[100 - 300] \approx [0.0023, 0.0069]$ day⁻¹. Most of the studies (Gorree et al., 1995; Veltman et al., 2007a; Van Den Brink et al., 2010) use an excretion rate based on Friberg et al. (1986) which estimates the half-time for the whole body to be around 200 days, which gives an excretion rate of $k_{out,x} = 0.0035 \text{ day}^{-1}$.

To parameterize the function of transfer from soil to prey, denoted $\kappa(C_s)$, we use data collected 178 from 2006 to 2010 in a 40 km^2 area surrounding the former smelter "Metaleurop-Nord", north of 179 France (see publications Fritsch et al. (2010b); Fritsch et al. (2011); Tête et al. (2013); Fritsch 180 et al. (2010a)). Soil Cd level ranges from 0.1 ppm to 2402.1 ppm of dry matter based on more 181 than 260 samples of composite $0-25 \ cm$ soil (Douay et al., 2009; Fritsch et al., 2010a). Small 182 mammals were captured in sub-samples of 500×500 squares selected along a soil pollution gradient. 183 Small mammals were identified at the species level using morphometric, skull and teeth criteria. 184 Total body concentration in the different small mammal species were calculated from kidney and 185 liver concentrations measured in the animals Veltman et al. (2007a). From those data, we define 186 the function $\kappa(C_s)$ by a log-log linear regression (i.e., $\ln(C_x) = a + b \ln(C_s)$) as previously used 187 (Veltman et al., 2007a; Fritsch et al., 2010a) (see Table S1 in Supplementary Information and 188 Fig. 2.A). 189

¹⁹⁰ 2.2.2 Toxicity effect of Cd on reproduction and mortality of prey

The effect of Cd on the small mammals organism are, among others, a reduction of food and water 191 intake, growth depression, renal dysfunction, hypertension, anemia and cancer (Cooke et al., 2011). 192 According to Świergosz-Kowalewska (2001), the reproductive organs are more sensitive than other 193 organs and a low doses may affect spermatogenesis and ovulation. In the report of US-EPA (2005), 194 the NOAEL for reproduction and growth is a diet with a concentration of $1.86\mu g.g^{-1}.day^{-1}$, that 195 is $10.63 \,\mu g.g^{-1}$ in the whole body. Using data and methodology of the same report, the LOAEL 196 (Lowest Observed Adverse Effect Level) for reproduction is estimated at $6.27 \mu g.g^{-1}.day^{-1}$, that 197 is $35.83 \mu g.g^{-1}$ which is in the range estimated previously from Shore and Douben (1994). Again, 198 with the data provided by US-EPA (2005) we obtain a NOAEL (Non Observed Adverse Effect 199 Level) for mortality of $6.72 \,\mu g.g^{-1}.\text{day}^{-1}$ (i.e., $38.4 \,\mu g.g^{-1}$), and from the same report, a LOAEL 200 of $9.72 \,\mu g.g^{-1}$.day⁻¹ (i.e., $55.54 \,\mu g.g^{-1}$). 201

$$\pi(C_x) = r\left(1 - \frac{1}{2}\left(1 + \operatorname{erf}\left[\frac{\ln(C_x) - \mu_r}{\sigma_r\sqrt{2}}\right]\right)\right)$$
(2)

where the function erf() is the Gauss error function defined as: $\operatorname{erf}(x) = \frac{2}{\sqrt{\pi}} \int_0^x e^{-t^2} dt$.

For parameterization, we use the equivalence NOAEL= EC_{10} and LOAEL= EC_{30} (Greenberg et al., 2014), and then a least square regression to estimate parameters of the log-normal curve. For reproduction, we estimate $EC_{50} = 82.91 \mu g. g^{-1}$, the parameter of the log-normal curve, equation (3) are $\mu_r = 4.418$ and $\sigma_r = 1.601$ (see Fig. 2.A in Supporting Information). Combination of soil-prev contamination (i.e., $\kappa(C_s)$ described in Table S1 in Supporting Information) with the dose-response function (i.e., $\pi(C_x)$) gives the probability of prey to reproduce in function of concentration in soil (see curves plotted in Fig. 2.B in Supporting Information). The equation of the dose-response curve for prey reproduction is given by the cumulative distribution function of a log-normal law: The reproduction rate of small mammals are well-known to be high. From Quéré and Le Louarn (2011), we estimate the maximal growth rate of preys r around [1/365 - 25/365]per day, and fixed it at r = 20/365 for every prey species.

For mortality, we infer on a log-normal cumulative function, equation (3), with $\mu_{m_x} = 4.272$ and $\sigma_{m_x} = 0.486$ (see Fig. 2.A in Supporting Information).

$$\mu_x(C_x) = m_x \frac{1}{2} \left(1 + \operatorname{erf}\left[\frac{\ln(C_x) - \mu_{m_x}}{\sigma_{m_x}\sqrt{2}}\right] \right)$$
(3)

The combination of soil-prey transfer with dose-response curve for mortality, $\mu_x(C_x)$ gives the 217 probability of prey mortality as a function of concentration in soil (see curves plotted in Fig. 2.B 218 in Supporting Information when assuming the maximum of mortality rate due to Cd at $m_x = 1$). 219 Compared to rodents, the insectivores shrews have often highest exposure to cadmium but they are 220 able to tolerate high concentrations of Cd in their kidney and liver without adverse effect (Cooke 221 et al., 2011), what is confirmed with the data of US-EPA (2005) where shrews have highest NOAEL 222 and/or LOAEL for growth and survival than other species. However the set of data was too small 223 to give specifics NOAEL and LOAEL for shrews. Therefore, we gave different maximum rate of 224 mortality due to contamination: $m_x = 2/365$ for rodents (*Microtus, Apodemus* and *Myodes*), and 225 $m_x = 0.5/365$ for shrews (*Crocidura* and *Sorex*). 226

227 2.2.3 Exposure of raptors to cadmium

As for small mammals, birds accumulate Cd mainly through their diet (Wayland et al., 2011; Burger, 2008). While there are some works on avian toxicity of Cd, few concern raptors. In the review of US-EPA (2005), the species are mainly herbivores and insectivores. From these species, US-EPA (2005) estimates the NOAEL for reproduction and growth at $1.47\mu g.g^{-1}.day^{-1}$ and the LOAEL at $6.35 \mu g.g^{-1}.day^{-1}$. For mortality, the NOAEL is estimated at $10.33\mu g.g^{-1}.day^{-1}$ and the LOAEL around $22.97 \mu g.g^{-1}.day^{-1}$.

Also, from Gorree et al. (1995) (on kestrel and barn owl) we assume an excretion rate for bird $k_{out,z} = 0.0035 \,\mathrm{day}^{-1}$. From Wayland et al. (2011), the absorption rate, denoted η in the model, is in the range of [0.01-0.07], that we fixed at 2% (Schipper et al., 2008; Loos et al., 2010a). Therefore, to estimate the whole body concentration, we use the same equation as for small mammals, and we obtain for reproduction: NOAEL= $8.4 \,\mu g.g^{-1}$ and LOAEL= $36.28 \,\mu g.g^{-1}$, and for mortality, we have: NOAEL= $59.03 \,\mu g.g^{-1}$ and LOAEL= $131.26 \,\mu g.g^{-1}$.

240 2.2.4 Toxicity effect of Cd on reproduction and mortality in raptors

The natural mortality rate of the barn owl, denoted m, is based on the usual life span which is about 4 years, so $m = 1/(365 \times 4)$ in day⁻¹. For barn owl dynamics, the bifurcation analysis constraints the use of a log-normal distribution for the energy conversion and the predator's mortality rate. As a consequence, for the function of energy conversion in predator, we therefore use the following stepwise linear function:

$$\psi(C_z) = \varepsilon \max\{\alpha C_z + 1, 0\} \tag{4}$$

We estimate α in function of NOAEL and LOAEL. Using a classical linear regression model, we get $\alpha = -0.008$, and therefore, reproduction is not possible for the threshold concentration $C_z > T_R = 118.287 \mu g.g^{-1}$, where T_R is the threshold concentration such as $\alpha T_R + 1 = 0$. We set the conversion efficiency to $\varepsilon = 0.001$. Indeed, if we assume that 4 to 8 prey are eaten every day (around 70 to 100 grams of prey see Table S1 in Supplementary Information), we obtain a reproduction rate of $0.001 \times [4 - 10] \times 365 = [1.46 - 3.65]$ on an annual basis.

252

For mortality function, we compute a linear regression based on NOAEL and LOAEL giving:

$$\mu_z(C_z) = m_z \gamma C_z, \quad \text{with} \quad \gamma = 0.002 \tag{5}$$

$_{254}$ 3 Results

²⁵⁵ 3.1 Bifurcation diagram on soil concentration

A classical summary of the long-term behavior of populations dynamics is with bifurcation diagram. 256 Fig. 3 represents the steady points of the prey populations for Cd concentration in soil ranging from 257 0.4 to 2402.1 ppm with carrying capacity fixed at K = 1121.8 (see also Fig. S2.A in Supplementary 258 Information), and the natural mortality rate of predator at $m = 10/(4 \times 365)$. When external 259 changes occur, here Cd concentration in soil, C_s , ecosystems changes can be in a continuous way 260 or exhibit a sudden discontinuity. On a certain domain of parameters, ecosystems may have 261 several stable points (i.e., bistability for 2 stables points) where stochastic disturbances may drive 262 the system toward a different steady state. 263

For prey densities (see Fig. 3), we observe three situations: at low concentration, depending on 264 initial condition, prey tends to a prey-only equilibrium E_1 (predator is extirpated), a prey-predator 265 coexistence equilibrium E_* (with limit cycle) or a no-species steady point E_0 . Prey-only steady 266 point starts at the carrying capacity and decreases faster and faster with the increase in C_s . For 267 the prey-predator coexistence, prey point starts lower and increases slightly with the increase of 268 soil contamination. This point of coexistence is unstable but with a limit cycle, and the amplitude 269 of the limit cycle decreases until the Hopf-bifurcation point, denoted HB. Simultaneously, predator 270 population is either extirpated or decreases slightly (see Fig. 3.A-B). Again, predator oscillates 271

around the coexistence point decreasing with the increase in contaminant. At the coexistence point, oscillation stops at HB but prey still increases and predator decreases until the transcritical bifurcation (TB) at concentration $C_{s,2}$ where predator are extirpated and only prey-only steady point is feasible. Finally, prey is also extirpated by a TB at concentration $C_{s,1}$ (see Fig. 3.C) where no species can survive. For some range of parameter values, we may observe a homoclinic bifurcation when the periodic orbit collides with the prey-only saddle steady point.

To better understand the resilience of the system, the "marble-in-a-cup" diagram in Fig. 3.C represents the stability landscape where valleys are stable zone and top of hills are unstable points. In this graph, the concentration of Hopf bifurcation, $C_{s,H}$, and transcritical bifurcation $C_{s,1}$ and $C_{s,2}$ are represented.

²⁸² 3.2 Cascade effects with different small mammals species

In order to study at the bottom-up and top-down cascade effects on the steady points for the five 283 groups of small mammals, we analyse and compute 2D bifurcation digrams in Fig. 4 and Fig. 5. 284 Fig. 4 represents bottom-up cascade effect by an increase in prey resources parameterized with the 285 carrying capacity K ranging from 0 to 5000. The predator mortality rate is fixed at $m = 1/(4 \times 365)$. 286 Fig. 5 represents top-down cascade effect by an increase in the predator mortality rates, m, ranging 287 from 0 to $20/(4 \times 365)$. The carrying capacity is fixed at K = 2500. In both Fig. 4 and Fig. 5, panels 288 A are the null models where the concentration in the prey is the concentration is the soil $C_x = C_s$ 289 with a maximal intrinsic prey mortality rate fixed at $m_x = 2/365$. For a better distinction of 290 bifurcation zones, for each panel of Fig. 4 and Fig. 5 the y-axes (i.e., carrying capacity or predator 291 death rate) are square-root scaled and the x-axis (i.e., concentration in soil) are log-transformed 292 in the range 0.4 to 2402.1 ppm as for data representation in Fig. 2.A. 293

²⁹⁴ 3.2.1 Bottom-up cascade effects

The null model of Fig. 4 shows that at a very low carrying capacity, the increase in contaminant 295 changes the system from prey-only to no-species steady point through a transcritical bifurcation. 296 The resources of preys are sufficient to maintain the prey population but without predation. In 297 this situation, there is no limit cycle since the predator is extirpated. Limit cycle can only appears 298 with coexistence. When the carrying capacity increases, coexistence is possible (prey-only and no-299 species are unstable points). Then, prey-only equilibrium is stable, and the predator is extirpated. 300 Finally, after ≈ 80 ppm, no-species can survive, the soil contamination is too high. The two changes 301 in steady states stability are called transcritical bifurcations (green lines). When the carrying 302 capacity increases, the coexistence point becomes unstable with a limit cycle. This represents 303 the famous "paradox of enrichment" showed by Rosenzweig (1971). However, the increase of 304 contaminant stabilizes the system since the oscillation of the coexistence points disappears at 305 the Hopf bifurcation (red lines). And then, as previsouly, the system undergoes two transcritical 306 bifurcations. The fourth dynamic is the one described previously in Fig. 3 with bistability of 307

coexistence and prey-only steady point. When carrying capacity is low, the ecosystem changes 308 are continuous between steady points. But at high carrying capacity bistability occurs, where 309 discontinuous changes happen at the tipping points represented by fold bifurcations (blue lines). 310 For other panels of Fig. 4, for every species, the increase in K has a destabilizing effect. At low 311 carrying capacity, there is no limit cycle, and a limit cycle appears in every chain when K increases. 312 Also, the increase in Cd has a stabilizing effect since we observe a change from oscillations to stable 313 coexistence, prey-only steady point and finally extinction of species. At high carrying capacity, 314 we observe a zone of alternative stable (or limit cycle) states of coexistence and prey-only. This 315 illustrates that the enrichment in prev resources favors the occurrence of regime shifts. 316

317 3.2.2 Top-down cascade effects

In Fig. 5, we observe that m has a stabilizing effect. At low predator mortality, every system 318 exhibits oscillation when soil concentration is low. The oscillations disappears with the increase 319 in m. As for bottom-up bifurcation diagrams (Fig. 4), the increase in Cd in soil has a stabilizing 320 effect with the decline of oscillations until their disappearances. When the predator mortality 321 rate is high, the transition from coexistence to prey-only are smoother. Under this condition, 322 the predator fitness is weak and a slight increase in contaminant reducing the fitness drives the 323 predator to extinction. Then at intermediate predator mortality rate, there are tipping points due 324 to bistable zone (see Fig. 5.A-B,F). Finally, at low predator mortality rate, there is no transition 325 from coexistence to prey-only but directly from coexistence to no-species. This last pattern means 326 that the predator survival is not driven by the contaminant but by the presence of prey. 327

328 3.2.3 Predator and prey extirpation

The transcritical bifurcation from prey-only to no-species happens at the threshold value $C_{s,1}$ where the mortality rate of a prey population is greater than its reproduction rate leading to the extinction of prey. Since the prey is extincted, predator cannot survive. For the null model where concentration in prey is the same that the Cd concentration in the soil $C_x = C_s$, the threshold is $C_{s,Null Model,1} \approx 74.1$ ppm. For the herbivores *Microtus* spp, $C_{s,Mi,1} \approx 79.5$ ppm. This transcritical bifurcation for omnivores and for *Sorex* spp is not in the range considered for Cd soil concentration [0.4 - 2402.1] ppm. For *Crocidura* spp $C_{s,Cr,1} \approx 62.9$ ppm.

336 4 Discussion

This work provides a set of conditions on stressors (e.g., environmental pollution, excessive enrichment, predator depletion) that may introduce regime shifts in small mammals-raptor dynamics taking place in metal-polluted ecosystems. Along the soil contaminant concentration gradient, the food chain exhibits four types of outcomes: (i) predator-prey coexistence, (ii) prey-only, (iii) population extinction and (iv) a bistable state where a coexistence point and a prey-only steady

point form two stable valleys separated by an unstable coexistence area. This last case means that 342 a slight change in populations densities, due to stochastic variations, may lead the system to a 343 totally different state (i.e., from coexisting predator-prey state to a prey-only state where predators 344 are extirpated). Also, we observed oscillations when prey and predator coexist even in a bistable 345 context. These results provide a conceptual framework, with its limitations discussed hereinafter, 346 to modelize and analyze the effect of chemical pollution in the classical trophic cascade theory, in 347 term of stability (i.e., resilience and oscillations) and strength of transition between states (i.e., 348 smooth transition or abrupt change due to tipping point). For environmental risk management, 349 predicting alternative stable states and system sensitivity to external variations is essential to 350 anticipate or prevent abrupt changes in ecosystem (Scheffer, 2009). 351

4.1 Gradient of soil contamination

Within the range of low contamination of soil, the observation of population densities reveals no 353 impact of Cd pollution at the ecosystem level, but the bifurcation diagrams shows that when the 354 contamination increases, the resilience of the system decreases as the system moves closer to prev-355 only or no-species stable states. Also, when the Cd concentration increases, there is an increase in 356 prey densities simultaneous with a decrease in predator population. The reason is that the decrease 357 in predator due to the contaminant releases the pressure on prey population. The prey population 358 is also impacted by the contaminant but the balance between the release of predation and the stress 359 of contamination is beneficial for the prey. Then, at a higher level of contaminant concentration 360 in the soil, predator population goes extinct. This leads the system to a prey-only steady point where the contaminant concentration is the only external factor affecting prey survival until its 362 extinction. If prey is more sensitive and/or more exposed to the contaminant than the predator, 363 then, a transition from coexisting predator-prey steady state to a total extinction without the 364 transition at a prey-only equilibrium may occur. 365

4.2 Combined effects of trophic cascades and contamination

The transition from predator-prey coexistence to prey-only state is different according to bottomup and top-down pressures: it may change smoothly, strongly around a threshold concentration or exhibits tipping points with two alternative stable states.

Several theoretical and empirical studies predicted that enrichment (i.e., increase in resources) 370 leads to oscillation of population dynamics, what is known as the "paradox of enrichment" (Rosen-371 zweig, 1971; Fussmann et al., 2000; Roy and Chattopadhyay, 2007b). The system we consider 372 shows also an increase in oscillation amplitude with the increase in resource enrichment (i.e., 373 carrying capacity of prey). But we also show that the increase in soil contamination overturns 374 oscillating dynamics. Indeed, the transfer of contaminant in the food-chain, affecting the repro-375 duction and mortality of the species involved a stabilizing effect. In the same way, considering a 376 one predator-two preys model, where one prey is toxic while the other is palatable, Roy and Chat-377

topadhyay (2007a) showed that the introduction of a toxic prey reduces oscillations. In aquatic 378 ecosystem, Kooi et al. (2008); Prosnier et al. (2015); Huang et al. (2015) made the same ob-379 servations for respectively persistent toxicant-bacterium-ciliate, copper-Scenedesmus-Daphnia and 380 methylmercury-aquatic insects-rainbow trout systems. These models, showing that contaminant 381 may contribute to reduce oscillations in the community dynamics, concern chronic exposure to con-382 taminant in bi-trophic food chain. However, the theoretical work of Garay-Narváez et al. (2013) 383 showed that more complex systems (i.e., with a greater species richness) are destabilized in terms of reduction of food-web connectance, by the pulsed introduction of a contaminant into the envi-385 ronment. Therefore, further works are necessary to understand the different effects between pulsed 206 and chronic exposure, from low to high species richness including variations in both structure and 387 composition of the food web. 388

We show that a decrease in predator mortality rate, that is a decrease in top-down regulation, 389 has also a destabilizing effect on the predator-prey dynamics. This result means that when top-390 down pressure effect is high (i.e., high intrinsic predator mortality rate), the predator survival is 391 very sensitive to contaminant variation until a point where contaminant concentration drives the 392 predator population toward extinction. While with a low intrinsic mortality rate of the predator, 393 it is the density of prey that drives predator to extinction, and no more the contaminant. Also, 394 similarly to the paradox of enrichment, at low top-down regulation, contaminant has a stabilizing 395 effect. To our knowledge, the observation of this pattern is new and could be important for envi-396 ronmental management. Indeed, if empirical studies confirm our prediction, we could argue that 397 to prevent the extinction of apex predators, when the ecosystem contamination is high, manager 308 should focus on reducing exposure to contamination first, and then, when contaminant level is 399 lower, care has to be taken on prey population. Our model also shows that the strength of steady 400 state transitions increases with the decrease of the top-down regulation. Again, this illustrates 401 that predator survival is more dependent on prey density and less on its intrinsic mortality rate. 402

403 4.3 Trophic level of prey

In this study, we consider five groups of prey pooled according to their diet (i.e., herbivores, 404 omnivores and insectivores). We compare these five models to a null model using a null-prey 405 having the same body burden as the concentration in the soil. From field data, the five groups can 406 be clearly distinguished by their responses along the pollution gradient in terms of bioaccumulation. 407 At low concentration of the contaminant in soil, the herbivores (i.e. *Microtus* spp) are the least 408 contaminated, and the insectivores (i.e., shrews) are the most contaminated. Cd body burden 409 in the omnivores are in between. This ranking follows previous studies (Veltman et al., 2007a; 410 Fritsch et al., 2010a) suggesting a biomagnification of Cd in food chain, where the species at the 411 highest trophic level is the most contaminated. However, when Cd increases in soil, responses of 412 the various groups are different: *Microtus* spp are the most sensitive, with a positive response 413 which is accentuated with an increase in soil contamination. As a consequence, for bottom-up and 414

top-down cascades, the bifurcation diagram of *Microtus* spp is similar with the null model. This 415 similarity is due to the elasticity of exposure close to one (1.56, see Table S1 in Supplementary 416 Information), meaning that the Cd body burden in *Microtus* spp varies with the similar amplitude 417 that soil concentration. Omnivores rodents, A. sylvaticus and M. glareolus, are the least sensitive 418 to soil contamination since they have also a positive response, but this response diminishes with 419 the increase of Cd in soil. Therefore, at the food-chain level, omnivores preys have a buffer effect. 420 Those results reflects previous observations that the body burden of Cd in more related to diet 421 preferences for mobile species as A. sylvaticus rather than soil concentration, and is the opposite 422 for a nonmobile species as *Microtus* spp (Van Den Brink et al., 2011). Finally, as expected, 423 insectivore have the highest level of contamination but the response to contaminant level variation 424 are not the same between the two groups. While *Sorex* spp present a high Cd body burden at low 425 concentration in soil, field data did not exhibit an increase of Cd body burden along the pollution 426 gradient. So, as for omnivores, this buffers the impact of contamination when its level increases. 427 For the other insectivores, *Crocidura* spp, the response to contaminant level variations is similar to 428 that of *Microtus* spp species, but the body burden is higher. Therefore, *Crocidura* spp are the most 429 risky species to consume for a predator. This knowledge about critical prey species is important to 430 assess the exposure of apex predators to environmental contaminants (Schipper et al., 2008; Loos 431 et al., 2010a). Also, the position of raptor at the top of food webs informs on the bioavailability of 432 a wide range of contaminants and on the exposure of species at lower trophic levels and is therefore 433 an important challenge for environmental risk assessment (Bustnes et al., 2013). 434

435 4.4 Limitations and perspectives

Our model explore the changes in the balance between the necessity for a predator to feed on 436 prey and the damaging consequences of predation in terms of exposure to contaminants. This 437 modeling of prey-predator relationships under a panel of pollution stress scenarios allows not 438 only predicting long-term direct and indirect effects of contaminants on populations, but also, 439 it shows how extinctions may occur within communities free-living in polluted sites. The model 440 reveals the occurrences and the positions of bifurcation points where a small change in parameters 441 (i.e., soil contaminant concentration, prey carrying capacity, predator mortality rate) induces a 442 sudden change in the food chain dynamics. The analysis of these bifurcations helps to identify 443 which prey ecological traits are critical for propagating adverse effects across trophic levels, how 444 a whole community is sensitive to contaminant. It also provides inputs for concepts about how 445 contaminants modulate trophic cascades, and further how multiple stressors can shape population 446 dynamics and tipping points in ecosystem functioning. 447

However, in this simplified model, the complexity of trophic interactions is reduced to only one prey-one predator system even if different functional responses have been considered. Yet, a variation in the diet of a species is likely to change the exposure of that species to contaminants. The direct next step is therefore the inclusion of multi-prey predation to explore the influence of the adaptive foraging behavior of the predator (Baudrot et al., 2016) on similar ecotoxicological systems, and the role of biodiversity in prey community on shaping the responses of food-webs to environmental disturbances such as environmental pollution. Among many complexification of the models, since collection of data have been thought into a landscape approach, we suggest to take this spatial heterogeneity of habitats into account (Fritsch et al., 2012).

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463 **References**

- ⁴⁶⁴ Andersen, Ole, Jesper Bo Nielsen, Jens Ahm Sorensen, and Leif Scherrebeck (1994). "Experimen-
- tal localization of intestinal uptake sites for metals (Cd, Hg, Zn, Se) in vivo in mice." In:
 Environmental Health Perspectives 102(Suppl 3), p. 199.
- ⁴⁶⁷ Auger, Pierre and Rafael Bravo De La Parra (2000). "Methods of aggregation of variables in
 ⁴⁶⁸ population dynamics". In: Comptes Rendus de l'Académie des Sciences-Series III-Sciences de
 ⁴⁶⁹ la Vie 323(8), pp. 665–674.
- 470 Baudrot, Virgile, Antoine Perasso, Clémentine Fritsch, Patrick Giraudoux, and Francis Raoul
- (2016). "The adaptation of generalist predators diet in a multi-prey context: insights from
 new functional responses". In: *Ecology* 97, pp. 1832–1841.
- ⁴⁷³ Bontje, D, BW Kooi, M Liebig, and SALM Kooijman (2009). "Modelling long-term ecotoxicological
- effects on an algal population under dynamic nutrient stress". In: *Water Research* 43(13), pp. 3292–3300.
- ⁴⁷⁶ Burger, Joanna (2008). "Assessment and management of risk to wildlife from cadmium". In: Science
 ⁴⁷⁷ of the Total Environment 389(1), pp. 37–45.
- ⁴⁷⁸ Bustnes, Jan O, Bård-J Bårdsen, Georg Bangjord, Syverin Lierhagen, and Nigel G Yoccoz (2013).
- "Temporal trends (1986–2005) of essential and non-essential elements in a terrestrial raptor in
 northern Europe". In: Science of The Total Environment 458, pp. 101–106.
- 481 Carpenter, Stephen R, James F Kitchell, and James R Hodgson (1985). "Cascading trophic inter-
- actions and lake productivity". In: *BioScience*, pp. 634–639.
- ⁴⁸³ Clements, William H and Jason R Rohr (2009). "Community responses to contaminants: using
 ⁴⁸⁴ basic ecological principles to predict ecotoxicological effects". In: *Environmental Toxicology*
- 485 and Chemistry 28(9), pp. 1789–1800.
- Cooke, JA, WN Beyer, and JP Meador (2011). "Cadmium in small mammals". In: *Environmental contaminants in biota: interpreting tissue concentrations. CRC Press, Boca Raton*, pp. 627–642.
- ⁴⁸⁸ De Laender, F, M Morselli, H Baveco, PJ Van Den Brink, and A Di Guardo (2015). "Theoretically ⁴⁸⁹ exploring direct and indirect chemical effects across ecological and exposure scenarios using
- ⁴⁹⁰ mechanistic fate and effects modelling". In: *Environment International* 74, pp. 181–190.
- ⁴⁹¹ DeAngelis, Donald L and Volker Grimm (2014). "Individual-based models in ecology after four ⁴⁹² decades". In: *F1000prime Reports* 6(39), p. 6.
- ⁴⁹³ Douay, F., C. Pruvot, C. Waterlot, C. Fritsch, H. Fourrier, A. Loriette, G. Bidar, C. Grand, A. De
- ⁴⁹⁴ Vaufleury, and R. Scheifler (2009). "Contamination of woody habitat soils around a former lead
- smelter in the North of France". In: Science of the Total Environment 407(21), pp. 5564–5577.
- 496 Espín, S, AJ García-Fernández, D Herzke, RF Shore, B Van Hattum, E Martínez-López, M Coeur-
- dassier, I Eulaers, C Fritsch, P Gómez-Ramírez, et al. (2016). "Tracking pan-continental trends
- ⁴⁹⁸ in environmental contamination using sentinel raptors—what types of samples should we use?"
- ⁴⁹⁹ In: *Ecotoxicology* 25(4), pp. 777–801.

- ⁵⁰⁰ Estes, James A, John Terborgh, Justin S Brashares, Mary E Power, Joel Berger, William J Bond,
- ⁵⁰¹ Stephen R Carpenter, Timothy E Essington, Robert D Holt, Jeremy BC Jackson, et al. (2011).

⁵⁰² "Trophic downgrading of planet Earth". In: *Science* 333(6040), pp. 301–306.

- Faroon, Obaid, Annette Ashizawa, Scott Wright, Pam Tucker, Kim Jenkins, Lisa Ingerman, and
 Catherine Rudisill (2012). Toxicological profile for cadmium.
- ⁵⁰⁵ Fleeger, John W, Kevin R Carman, and Roger M Nisbet (2003). "Indirect effects of contaminants

in aquatic ecosystems". In: Science of the Total Environment 317(1), pp. 207–233.

- Friberg, Lars, Carl-Gustaf Elinder, Tord Kjellström, and GF Nordberg (1986). *Cadmium and health: a toxicological and epidemiological appraisal.* Vol. 2. CRC Press Boca Raton, FL:
- 509 Fritsch, Clémentine, Richard P Cosson, Michaël Cœurdassier, Francis Raoul, Patrick Giraudoux,
- ⁵¹⁰ Nadia Crini, Annette De Vaufleury, and Renaud Scheifler (2010a). "Responses of wild small
- mammals to a pollution gradient: host factors influence metal and metallothionein levels". In: *Environmental Pollution* 158(3), pp. 827–840.
- 513 Fritsch, Clémentine, Patrick Giraudoux, Michaël Cœurdassier, Francis Douay, Francis Raoul,

⁵¹⁴ Christelle Pruvot, Christophe Waterlot, Annette De Vaufleury, and Renaud Scheifler (2010b).

- ⁵¹⁵ "Spatial distribution of metals in smelter-impacted soils of woody habitats: Influence of land-⁵¹⁶ scape and soil properties, and risk for wildlife". In: *Chemosphere* 81(2), pp. 141–155.
- Fritsch, Clémentine, Michaël Cœurdassier, Patrick Giraudoux, Francis Raoul, Francis Douay, Dominique Rieffel, Annette De Vaufleury, and Renaud Scheifler (2011). "Spatially explicit analysis
- of metal transfer to biota: influence of soil contamination and landscape". In: *PloS ONE* 6(5), e20682.
- Fritsch, Clémentine, Michaël Coeurdassier, Bruno Faivre, Pierre-Emmanuel Baurand, Patrick Giraudoux, Nico W Van Den Brink, and Renaud Scheifler (2012). "Influence of landscape composition and diversity on contaminant flux in terrestrial food webs: A case study of trace metal
 transfer to European blackbirds *Turdus merula*". In: *Science of the Total Environment* 432,
 pp. 275–287.
- ⁵²⁶ Fussmann, Gregor F, Stephen P Ellner, Kyle W Shertzer, and Nelson G Hairston Jr (2000). "Cross⁵²⁷ ing the Hopf bifurcation in a live predator-prey system". In: *Science* 290(5495), pp. 1358–1360.
 ⁵²⁸ Garay-Narváez, Leslie, Matías Arim, José D Flores, and Rodrigo Ramos-Jiliberto (2013). "The
 ⁵²⁹ more polluted the environment, the more important biodiversity is for food web stability". In:
 ⁵³⁰ Oikos 122(8), pp. 1247–1253.
- Gómez-Mourelo, Pablo and Marta Ginovart (2009). "The differential equation counterpart of an
 individual-based model for yeast population growth". In: Computers & Mathematics with Applications 58(7), pp. 1360–1369.
- Gorree, M, WLM Tamis, TP Traas, and MA Elbers (1995). "BIOMAG: a model for biomagnification in terrestrial food chains. The case of cadmium in the Kempen, The Netherlands". In: *Science of the Total Environment* 168(3), pp. 215–223.

- Greenberg, Marc S, Ilse Schoeters, Randall S Wentsel, David W Charters, Ian A Mitchell, and 537
- Barry Zajdlik (2014). "Regulatory considerations for the potential development and application 538
- of metal cleanup values". In: Integrated Environmental Assessment and Management 10(3), 539
- pp. 401–414. 540

544

- Heath, Michael R., Douglas C. Speirs, and John H. Steele (2014). "Understanding patterns and 541 processes in models of trophic cascades". In: *Ecology Letters* 17(1), pp. 101–114. 542
- Hopkin, S.P., D.B Peakall, R.M Sibly, and C.H Walker (2012). Principles of Ecotoxicology, Fourth 543 Edition. 4th ed. CRC Press.
- Huang, Qihua, Hao Wang, and Mark A Lewis (2015). "The impact of environmental toxins on 545 predator-prey dynamics". In: Journal of Theoretical Biology 378, pp. 12–30. 546
- Kooi, BW, D Bontje, GAK Van Voorn, and SALM Kooijman (2008). "Sublethal toxic effects in a 547 simple aquatic food chain". In: *Ecological Modelling* 212(3), pp. 304–318. 548
- Loos, Mark, Ad MJ Ragas, Rinus Plasmeijer, Aafke M Schipper, and A Jan Hendriks (2010a). "Eco-540
- SpaCE: an object-oriented, spatially explicit model to assess the risk of multiple environmental 550
- stressors on terrestrial vertebrate populations". In: Science of the Total Environment 408(18), 551 pp. 3908-3917. 552
- Loos, Mark, Aafke M Schipper, Uwe Schlink, Kathrin Strebel, and Ad MJ Ragas (2010b). "Receptor-553
- oriented approaches in wildlife and human exposure modelling: a comparative study". In: En-554 vironmental Modelling & Software 25(4), pp. 369–382. 555
- Mineau, Pierre (2005). "A review and analysis of study endpoints relevant to the assessment of "long 556
- term" pesticide toxicity in avian and mammalian wildlife". In: Ecotoxicology 14(8), pp. 775–799. 557
- Prosnier, Loïc, Michel Loreau, and Florence D Hulot (2015). "Modeling the direct and indirect ef-558
- fects of copper on phytoplankton–zooplankton interactions". In: Aquatic Toxicology 162, pp. 73– 559 81. 560
- Pruvot, Christelle, Francis Douay, Fourrier Hervé, and Christophe Waterlot (2006). "Heavy metals 561
- in soil, crops and grass as a source of human exposure in the former mining areas (6 pp)". In: 562
- Journal of soils and sediments 6(4), pp. 215–220. 563
- Quéré, Jean-Pierre and Henri Le Louarn (2011). Les rongeurs de France Faunistique et biologie. 564 Editions Quae. 565
- Rainbow, Philip S (2002). "Trace metal concentrations in aquatic invertebrates: why and so what?" 566
- In: Environmental Pollution 120(3), pp. 497–507. 567
- Relyea, Rick and Jason Hoverman (2006). "Assessing the ecology in ecotoxicology: a review and 568 synthesis in freshwater systems". In: Ecology Letters 9(10), pp. 1157–1171. 569
- Rockström, Johan, Will Steffen, Kevin Noone, Åsa Persson, F Stuart Chapin, Eric F Lambin, 570
- Timothy M Lenton, Marten Scheffer, Carl Folke, Hans Joachim Schellnhuber, et al. (2009). "A 571 safe operating space for humanity". In: Nature 461(7263), pp. 472–475. 572
- Rohr, Jason R, Jacob L Kerby, and Andrew Sih (2006). "Community ecology as a framework for 573
- predicting contaminant effects". In: Trends in Ecology & Evolution 21(11), pp. 606–613. 574

- ⁵⁷⁵ Rosenzweig, Michael L et al. (1971). "Paradox of enrichment: destabilization of exploitation ecosys-
- tems in ecological time". In: *Science* 171(3969), pp. 385–387.
- Roy, Shovonlal and J Chattopadhyay (2007a). "Enrichment and ecosystem stability: effect of toxic
 food". In: *BioSystems* 90(1), pp. 151–160.
- Roy, Shovonlal and J Chattopadhyay (2007b). "The stability of ecosystems: a brief overview of the paradox of enrichment". In: *Journal of biosciences* 32(2), pp. 421–428.
- Scheffer, Marten (2009). Critical transitions in nature and society. Princeton University Press.
- Scheffer, Marten, Stephen R. Carpenter, Vasilis Dakos, and Egbert H. Van Nes (2015). "Generic
- Indicators of Ecological Resilience: Inferring the Chance of a Critical Transition". In: Annual
- Review of Ecology, Evolution, and Systematics 46(1), pp. 145–167.
- Schipper, Aafke M, Mark Loos, Ad MJ Ragas, João PC Lopes, Boris T Nolte, Sander Wijnhoven,
- and Rob SEW Leuven (2008). "Modeling the influence of environmental heterogeneity on heavy
- metal exposure concentrations for terrestrial vertebrates in river floodplains". In: *Environmental*
- ⁵⁸⁸ Toxicology and Chemistry 27(4), pp. 919–932.
- ⁵⁸⁹ Schipper, Aafke M, Sander Wijnhoven, Hans Baveco, and Nico W Van Den Brink (2012). "Con-
- taminant exposure in relation to spatio-temporal variation in diet composition: A case study
- of the little owl Athene noctua". In: Environmental Pollution 163, pp. 109–116.
- Schmitt, W, D Auteri, F Bastiansen, M Ebeling, C Liu, R Luttik, S Mastitsky, D Nacci, CJ
 Topping, and M Wang (2015). "An example of population-level risk assessments for small
 mammals using individual-based population models". In: Integrated Environmental Assessment
 and Management.
- Shore, Richard F and Peter ET Douben (1994). "The ecotoxicological significance of cadmium
 intake and residues in terrestrial small mammals". In: *Ecotoxicology and Environmental Safety* 29(1), pp. 101–112.
- 599 Smith, Philip N, George P Cobb, Céline Godard-Codding, Dale Hoff, Scott T McMurry, Thomas R
- Rainwater, and Kevin D Reynolds (2007). "Contaminant exposure in terrestrial vertebrates".
- In: Environmental Pollution 150(1), pp. 41–64.
- Sterckeman, T, F Douay, N Proix, and H Fourrier (2000). "Vertical distribution of Cd, Pb and Zn
 in soils near smelters in the North of France". In: *Environmental Pollution* 107(3), pp. 377–389.

504 Sterckeman, T., F. Douay, N. Proix, H. Fourrier, and E. Perdrix (2002). "Assessment of the contam-

ination of cultivated soils by eighteen trace elements around smelters in the North of France".

- ⁶⁰⁶ In: Water, Air, and Soil Pollution 135(1-4), pp. 173–194.
- ⁶⁰⁷ Świergosz-Kowalewska, Renata (2001). "Cadmium distribution and toxicity in tissues of small ⁶⁰⁸ rodents". In: *Microscopy research and technique* 55(3), pp. 208–222.
- ⁶⁰⁹ Tête, Nicolas, Clémentine Fritsch, Eve Afonso, Michaël Coeurdassier, Jean-Claude Lambert, Patrick
- Giraudoux, and Renaud Scheifler (2013). "Can body condition and somatic indices be used to
- evaluate metal-induced stress in wild small mammals?" In: *PloS ONE* 8(6), e66399.
- ⁶¹² US-EPA (2005). Ecological Soil Screening Levels for Cadmium.

- Van Den Brink, Nico, Dennis Lammertsma, Wim Dimmers, Marie-Claire Boerwinkel, and Annema-613 riet Van Der Hout (2010). "Effects of soil properties on food web accumulation of heavy metals 614 to the wood mouse Apodemus sylvaticus". In: Environmental Pollution 158(1), pp. 245–251. 615 Van Den Brink, Nico W, Dennis R Lammertsma, Wim J Dimmers, and Marie Claire Boerwinkel 616 (2011). "Cadmium accumulation in small mammals: species traits, soil properties, and spatial 617 habitat use". In: Environmental Science and Technology 45(17), pp. 7497–7502. 618 Veltman, Karin, Mark AJ Huijbregts, Timo Hamers, Sander Wijnhoven, and A Jan Hendriks 619 (2007a). "Cadmium accumulation in herbivorous and carnivorous small mammals: Meta-analysis 620 of field data and validation of the bioaccumulation model optimal modeling for ecotoxicological 621 applications". In: Environmental Toxicology and Chemistry 26(7), pp. 1488–1496. 622 Veltman, Karin, Mark AJ Huijbregts, Martina G Vijver, Willie JGM Peijnenburg, Peter HF Hobbe-623 len, Josee E Koolhaas, Cornelis AM Van Gestel, Petra CJ Van Vliet, and A Jan Hendriks 624 (2007b). "Metal accumulation in the earthworm Lumbricus rubellus. Model predictions com-625 pared to field data". In: Environmental Pollution 146(2), pp. 428–436. 626 Villeneuve, Daniel L and Natàlia Garcia-Reyero (2011). "Vision & strategy: Predictive ecotoxicol-627 ogy in the 21st century". In: Environmental Toxicology and Chemistry 30(1), pp. 1–8. 628 Wayland, M, AM Scheuhammer, WN Beyer, and JP Meador (2011). "Cadmium in birds". In: En-629
- vironmental contaminants in biota: interpreting tissue concentrations. CRC Press, Boca Raton,
- ⁶³¹ pp. 645–666.



Figure 1: Flow diagram of the transmission of a contaminant along a trophic chain. The plain line is the trophic interaction, dashed lines are transfers of the contaminant and dotted lines are population intrinsic dynamics. Grey elements are bottom-up and top-down regulation parameterized with respectively the carrying capacity K and the predator mortality rate m.



Figure 2: (A) Log-log linear model with 95% credible interval from data from Metaleurop. Whole body concentration in fresh weight and concentration in soil (dry weight). See equation in Table S1 in Supplementary Information. (B) Rate of reproduction with $r = 2/365 \text{ day}^{-1}$, and rate of mortality with $m_{Mi,Ap,My} = 2/365$ (maximal reproduction rate r) and $m_{Cr,So} = 0.5/365$ (1/4 of maximal reproduction rate to have reproduction greater than mortality at $C_s = 0$ for Sorex spp).

Symbols	Definitions	Values [References]
$\pi(C_x)$	Contaminant effect on prey reproduction	equation (2)
r	Maximal reproduction rate of prey	2/365 [a]
$\mu_x(C_x)$	Mortality in prey due to the contaminant	equation (3)
m_x	Maximal prey mortality due to contaminant	2/365 rodents, $0.5/365$ shrews
K	Carrying capacity in prey	[0 - 5000]
$\kappa(C_s)$	Function of prey exposure	data in Table S1 in Sup. Inf. [b]
$k_{out,x}$	Excretion rate of contaminant in prey	$0.0035 \ [c]$
B_x	Mean biomass of prey individual	data in Table S1 in Sup. Inf.
$\Phi(x)$	Ingestion rate of prey: Holling III	a = 0.003 and $h = 0.3$
$\psi(C_z)$	Contaminant effect on predator reproduction	see text
ε	Maximal predator reproduction efficiency	0.001
$\mu_z(C_z)$	Contaminant effect on predator mortality	1/100
η	Percentage of absorption of ingested Cd	0.02 [d]
$k_{out,z}$	Excretion rate of contaminant in predator	$0.0035 \ [c]$
m	Natural mortality rate of predator	$1/(4 \times 365)$
B_z	Mean biomass of individual predator	350 grams

Table 1: Definition of parameters and their values. References are [a] Quéré and Le Louarn (2011); [b] Fritsch et al. (2010a) ; [c] Friberg et al. (1986) ; [d] Schipper et al. (2008)



TB: transcritical bifurcation. HB: Hopf Bifurcation. FB: Fold bifurcation. (A-B) Bifurcation diagram of predator and prey densities with respect to contaminant level Figure 3: 1D-Bifurcation diagram illustrating smoothly changes and tipping points in the null model (prey Cd-concentration is equal to soil Cd-concentration $C_x = C_s$). in soil C_s . (C) "Marble-in-a-cup" representation of bifurcation diagram in the range [45 – 80] ppm. The marble rolls towards the bottom of valleys (stable steady points) moving away from top of hills (unstable steady points).



Figure 4: 2D-Bifurcation diagram of bottom-up forcing for the five preys. (A) Null model (B) *Microtus* spp, (C) *Apodemus sylvaticus*, (D) *Myodes glareolus*, (E) *Sorex* spp and (F) *Crocidura* spp.



Figure 5: 2D-Bifurcation diagram of top-down forcing for the five preys. (A) Null model (B) *Microtus* spp, (C) *Apodemus sylvaticus*, (D) *Myodes glareolus*, (E) *Sorex* spp and (F) *Crocidura* spp.

⁶³² S1 Supporting Information

⁶³³ Supporting Information provides all mathematical developments done in the present study.

634 S1.1 General model

With all the assumptions made in the manuscript (see also description of notations in the manuscript), especially the assumption that individuals of a same population have the same biomass and the same amount of contaminant in their bodies, the model for the transfer of a contaminant is given by:

$$\frac{dB_{Tx}}{dt} = B_{Tx}g_x(x, C_x) - \mu_x(C_x)B_{Tx} - B_x\Phi(x)z$$
(S1a)

$$\frac{dw_x}{dt} = \kappa(C_s)B_{Tx} - k_{out,x}w_x - w_x\,\mu_x(C_x) - C_xB_x\Phi(x)z + \gamma_xw_xg_x(x,C_x)$$
(S1b)

$$\frac{dB_{Tz}}{dt} = B_{Tz} \left(\psi(C_z) \Phi(x) - m - \mu_z(C_z) \right)$$
(S1c)

$$\frac{dw_z}{dt} = -k_{out,z}w_z - w_z\left(m + \mu_z(C_z)\right) + \eta C_x B_x \Phi(x)z + \gamma_z w_z \psi(C_z)\Phi(x)$$
(S1d)

$$w_x = C_x B_{Tx}$$
 and $C_z = w_z / B_{Tz}$ (S1e)

$$x = B_{Tx}/B_x$$
 and $z = B_{Tz}/B_z$ (S1f)

635

In the general model (S1), the equations (S1a) and (S1c) present the dynamic of the total biomass of prey and the predator respectively. The equations (S1b) and (S1d) stand for the dynamics of contaminant concentrations within individuals for respectively the prey and the predator, where the death of individuals (prey and predator) implies a decrease of amounts of the contaminant, respectively $-w_x\mu_x(C_x)$ and $-w_z(m + \mu_z(C_z))$. The transfer of the contaminant through the predation is express by the term $C_x B_x \Phi(x) z$, which is removed in prey (S1b), and added in the predator (with a factor of transfer efficiency η) (S1d).

While we could consider the population dynamic in term of biomasses, it is more convenient to use density of population as suggested by the change of variable presented in equations (S1f) which give directly the following equalities:

$$\frac{dx}{dt} = \frac{1}{B_x} \frac{dB_{Tx}}{dt} \quad \text{and} \quad \frac{dz}{dt} = \frac{1}{B_z} \frac{dB_{Tz}}{dt}$$
(S2)

⁶⁴⁶ S1.2 Dimensional transformation of variables

From the change of variables in equations (S1e), it is straightforward to give the contaminant dynamics for the prey:

$$\frac{dC_x}{dt} = \frac{dw_x/B_{Tx}}{dt} = \frac{1}{B_{Tx}^2} \left(\frac{dw_x}{dt} B_{Tx} - w_x \frac{dB_{Tx}}{dt} \right)
= \frac{1}{B_{Tz}^2} (B_{Tx}(\kappa(C_s)B_{Tx} + w_x(w_x\gamma_xg_x(x,C_x) - k_{out,x} - \mu_x(C_x)) - C_x\Phi(x)z) - w_zB_{Tz}(\psi(C_z)\Phi(x) - m - \mu_z(C_z)))
= \kappa(C_s) - k_{out,x}C_x - C_x\mu_x(C_x) - \frac{C_xB_x}{B_{Tx}}\Phi(x)z - C_xg_x(x,C_x) + C_x\mu_x(C_x) + \frac{C_xB_x}{B_{Tx}}\Phi(x)z
= \kappa(C_s) - C_x(k_{out,x} + g_x(x,C_x))$$
(S3)

and for the predator:

$$\frac{dC_z}{dt} = \frac{1}{B_{Tz}^2} \left(\frac{dw_z}{dt} B_{Tz} - w_z \frac{dB_{Tz}}{dt} \right)
= \frac{1}{B_{Tz}^2} (B_{Tz}(-k_{out,z}w_z + w_z (\psi(C_z)\Phi(x)\gamma_z - m - \mu_z(C_z)) + \eta C_x B_x \Phi(x)z) - w_z B_{Tz} (\psi(C_z)\Phi(x) - m - \mu_z(C_z)))
= -k_{out,z} C_z - C_z (m + \mu_z(C_z)) + \eta C_x \Phi(x) \frac{B_x}{B_z} - C_z (\psi(C_z)\Phi(x) - m - \mu_z(C_z)))
= \eta C_x \Phi(x) \frac{B_x}{B_z} - C_z (k_{out,z}\psi(C_z)\Phi(x))$$
(S4)

650 S1.3 Reduction of system using slow-fast dynamics

⁶⁵¹ With ξ the low parameter, system (1) becomes:

$$\begin{cases} \frac{dx}{dt} = x \left(\pi(C_x) \left(1 - \frac{x}{K} \right) - \mu_x(C_x) \right) - \Phi(x)z \\ \xi \frac{dC_x}{dt} = \kappa(C_s) - C_x \left(k_{out,x} + \xi \pi(C_x) \left(1 - \frac{x}{K} \right) \right) \\ \frac{dz}{dt} = z \left(\psi(C_z) \Phi(x) - \mu_z(C_z) - m \right) \\ \xi \frac{dC_z}{dt} = \eta \frac{B_x}{B_z} \Phi(x) C_x - C_z \left(k_{out,z} + \xi \psi(C_z) \Phi(x) \right) \end{cases}$$
(S5)

and letting $\xi \to 0$, we obtain:

$$\Rightarrow \begin{cases} \frac{dx}{dt} = x \left(\pi(C_x) \left(1 - \frac{x}{K} \right) - \mu_x(C_x) \right) - \Phi(x)z \\ C_x = \frac{\kappa(C_s)}{k_{out,x}} \\ \frac{dz}{dt} = z \left(\psi(C_z) \Phi(x) - \mu_z(C_z) - m \right) \\ C_z = \frac{\eta B_x}{k_{out,z} B_z} \Phi(x) C_x \end{cases}$$
(S6)

⁶⁵³ S1.4 Elasticity of the regression

⁶⁵⁴ Note that we have:

$$\ln(C_x) = b\ln(C_s) + a \qquad \Leftrightarrow \qquad C_x = e^a C_s^b \qquad \Leftrightarrow \qquad \frac{\partial C_x}{\partial C_s} = e^a b C_s^{b-1} \qquad \Leftrightarrow \qquad b = \frac{C_s}{C_x} \times \frac{\partial C_x}{\partial C_s}$$
(S7)

Therefore, the parameter b is the elasticity of our model, that is a measure of the proportional change in C_x in response to a proportional change in C_s .

⁶⁵⁷ **Biomagnification:** The reduction formulation of system (S9) gives the following coefficient of ⁶⁵⁸ biomagnification (BMF):

$$BMF = \frac{\eta B_x}{k_{out,z}B_z} \Phi(x) = \frac{0.02 \times [70 - 100]}{0.0035 \times 350} = [1.14 - 1.63], \text{ for 70 to 100 grams ingested daily}$$
(S8)

⁶⁵⁹ S1.5 Parameterization for probability of reproduction and mortality

Species	Mean individual biomass B_x (Std. Error)	Function of $\ln(C_x)$: Estimate (Std. Error)
Microtus spp Apodemus sylvaticus Myodes glareolus Sorex spp Crocidura spp	$\begin{array}{c} 16.33 \ (1.03) \\ 17.28 \ (0.13) \\ 19.29 \ (0.27) \\ 7.06 \ (0.25) \\ 9.81 \ (0.12) \end{array}$	$\begin{split} & 1.56(0.33)\times\ln(C_s)-2.52(0.72)\\ & 0.23(0.03)\times\ln(C_s)+0.32(0.08)\\ & 0.25(0.04)\times\ln(C_s)+1.83(0.10)\\ & -0.03(0.09)\times\ln(C_s)+5.11(0.14)\\ & 0.65(0.10)\times\ln(C_s)+2.82(0.23) \end{split}$

Table S1: Log-log linear model of internal concentration in small mammals depending on soil concentrations (see Figure 2). In the log-log linear regression, $\ln(C_x) = a + b \ln(C_s)$, *a* is the intercept and *b* is the elasticity of the model (see Supporting Informations S1.4), which is a measure of proportional change in prey concentration, C_x , in response to a proportional change in soil concentration C_s .

⁶⁶⁰ S1.6 Description of a 2D bifurcation diagram

661 S1.7 Mathematical analysis

The ecotoxicological model (1) is a 4-dimensional system resulting from the coupling of contaminant 662 and population dynamics. This complexity involving a great number of variables and parameters 663 challenges the mathematical stability analysis. We therefore take advantage of the two time scales 664 included in the system, to reduce the model (1) to a 2-dimensional system where fast events are 665 neglected (Auger and De La Parra, 2000). In our context, we consider the common assumption 666 (Kooi et al., 2008; Huang et al., 2015) that the contaminant dynamics are faster than the dynamic 667 of population growth. This assumption means that the time scale of population growth and the 668 efficiency to convert ingested prey into new-born are much slower than the intake and elimination of 669 contaminants and which approaches a quasi-steady state. Due to this slow-fast dynamics process, 670 we assume a constant concentration rate in populations (Kooi et al., 2008; Huang et al., 2015). 671



Figure S1: (A) Log-normal probabilities of reproduction and mortality for prey depending on the concentration in the species individuals. (B) Log-normal probabilities of reproduction and mortality depending on the concentration in the soil. We use same parametirization than in graph A.



Figure S2: (A) 2D-Bifurcation diagram illustrating smoothly changes and tipping points in the null model (prey concentration is equal to soil concentration $C_x = C_s$). This diagram results from 500 1D-bifurcation diagram along a range of carrying capacity $K \in [0, 5000]$. (B) 1D-Bifurcation diagram showing a continuous change in ecosystem when the concentration in the soil increase.

Therefore, with ξ the low parameter, and letting $\xi \to 0$, system (1) becomes (see appendix S1.3

673 for details):

$$\frac{dx}{dt} = \underbrace{x\pi(\overline{C_x})\left(1 - \frac{x}{K}\right)}_{\text{additional mortality}} - \underbrace{\Phi(x)z}_{\mu_x(\overline{C_x})x} - \Phi(x)z$$

$$\frac{dz}{dt} = \underbrace{z\psi(\overline{C_z})\Phi(x)}_{\text{excretion}} - \underbrace{z\left(\mu_z(\overline{C_z}) + m\right)}_{k_{out,x}} - \underbrace{\Phi(x)z}_{\text{additional mortality}} - \underbrace{\Phi(x)z}_{\text{additional mortality}} - \underbrace{\Phi(x)z}_{\mu_x(\overline{C_x})x} - \underbrace{\Phi(x)z}_{\mu$$

Cadmium excretion is very low compared to other pollutant $(k_{out,\{x,z\}} = 0.0035)$. Also, from the parameterization done in the previous section (see Table 1), we have $\pi(C_x) \leq r = 2/365 \approx$ 0.0055 and $\psi(C_z) \leq \varepsilon = 0.001$, and since reproduction rates are decreasing with the increase in contaminant, there is a range of contamination where the slow-fast process is relevant. Also, the prey reproduction is reduced with the saturating part of the logistic growth rate, (1 - x/K).

⁶⁷⁹ S1.8 Steady states and their stability

The contamination of prey population and the transmission of contaminating substance through the predation is described in model (S9). It is important to mention here that the properties of π , ψ , μ_x and μ_z can not be prescribed beforehand since it varies from case to case. From now and onwards, we use the notation $\overline{\pi}(C_s)$, $\overline{\mu_x}(C_s)$, $\overline{\psi}(C_s, x)$ and $\overline{\mu_z}(C_s, x)$ instead of respectively $\pi(\overline{C_x})$, $\mu_x(\overline{C_x})$, $\psi(\overline{C_z})$ and $\mu_z(\overline{C_z})$. Hence, the change in the system dynamics can be studied with C_s as bifurcation parameter (see part S1.1):

$$\begin{cases} \frac{dx}{dt} = x \left(\overline{\pi}(C_s) \left(1 - \frac{x}{K} \right) - \overline{\mu}_x(C_s) \right) - \Phi(x)z \\ \frac{dz}{dt} = z \left(\overline{\psi}(C_s, x) \Phi(x) - \overline{\mu}_z(C_s, x) - m \right) \end{cases}$$
(S10)

686 S1.8.1 Existence of steady states

Above system possesses two axial equilibrium points, $E_0(0,0)$ and $E_1\left(K\left(1-\frac{\overline{\mu_x}(C_s)}{\overline{\pi}(C_s)}\right),0\right)$. The second one is feasible if $\overline{\mu_x}(C_s) < \overline{\pi}(C_s)$. At the critical magnitude $C_s = C_{s,1}$, system undergoes a transcritical bifurcation and the threshold of this bifurcation is given by:

$$\overline{\mu_x}(C_{s,1}) = \overline{\pi}(C_{s,1}) \tag{S11}$$

Graphical representation of $C_{s,1}$ is given by Fig. 2.B. An example of the bifurcation behavior of the prey-only steady point $(x_1, 0)$ is given by the bifurcation diagram Fig. 3.

We denote $E_*(x_*, z_*)$ the non-trivial steady point where prey and predator coexist. The interior equilibrium point E_* bifurcates from the axial equilibrium point E_1 at the bifurcation threshold ⁶⁹¹ $C_s = C_{s,2}$ where $C_{s,2}$ is a positive root of the equation $K\left(1 - \frac{\overline{\mu_x}(C_s)}{\overline{\pi}(C_s)}\right) = x_*$, that is when

Steady points	Conditions of existence and stability
$E_0 = (0,0)$	Always feasible. Stable when $C_s > C_{s,1}$, that is when only E_0 is feasible. Saddle for $C_s < C_{s,1}$, and transcritical bifurcation with E_1 at $C_{s,1}$.
$E_1 = (x_1, 0)$	Feasible for $C_s < C_{s,1}$. Unstable when E_* is feasible, that is for $C_s < C_{s,2}$. Stable for $C_{s,2} < C_s < C_{s,1}$.
$E_* = (x_*, z_*)$	Feasible for $C_s < C_{s,2}$. See text.

 $x_1 = x_*$ (see appendix S1.10 for details).

Table S2: Steady points with conditions of existence and stability.

⁶⁹³ S1.8.2 Stability of the steady states

The analysis of stability of the steady points E_0 , E_1 and E_* is totally given in the appendix S1.11. Here, we describe the mains results.

From the Jacobian matrix for the system (S10) around the trivial equilibrium point E_0 , one eigenvalue is always negative and E_0 is stable if $\overline{\pi}(C_s) < \overline{\mu_x}(C_s)$ and is a saddle-point if $\overline{\pi}(C_s) > \overline{\mu_x}(C_s)$. The first eigenvalue becomes zero when $C_s = C_{s,1}$ and the model under consideration undergoes first transcritical bifurcation. The transversality condition has to be satisfied, that is the real part of the eigenvalues have to be non-zero.

For the second steady point E_1 where only the predator is extirpated, we know this point rot is feasible when $\overline{\mu_x}(C_s) < \overline{\pi}(C_s)$ and hence one eigenvalue is always negative. Then, using the condition of feasibility of E_* , the point E_1 is locally asymptotically stable whenever E_* is not feasible, that is when $C_s > C_{s,2}$. Conversely, E_1 is a saddle-point when E_* is feasible.

For the coexisting point E_* , since the determinant of the Jacobian matrix of system (S10), denoted J_* , is positive at this point, the stability of E_* is determined by the trace of the matrix as whenever E_* is feasible. Consequently, E_* is stable if $Tr(J_*) < 0$, is unstable if $Tr(J_*) > 0$ and undergoes Hopf-bifurcation if $Tr(J_*) = 0$. We call $C_{s,H}$ the Hopf-bifurcation threshold. With Holling type II functional response, the sign of $Tr(J_*)$ is the same as:

$$-2ahx_*\overline{\pi}(C_s) + ahK(\overline{\pi}(C_s) - \overline{\mu_x}(C_s)) - \overline{\pi}(C_s)$$
(S12)

S1.9 Explicit formulation of threshold concentration for predator-prey coexistence

For the predator dynamics, substituting equations (4) and (5) into system (S10), we obtain:

$$\frac{dz}{dt} = z \left(\varepsilon \alpha \frac{\eta B_x}{k_{out,z} B_z} \Phi(x)^2 C_x + \varepsilon \Phi(x) - m_z \gamma \frac{\eta B_x}{k_{out,z} B_z} \Phi(x) C_x - m \right)$$
(S13)

Then, as demonstrated in appendix S1.12, E_* has two solutions for $C_s < C_{s,3}$, denoted $E_{*,a}$ and $E_{*,b}$, one solution for $C_s = C_{s,3}$ and no solution otherwise. The threshold contamination $C_{s,3}$ is defined by:

$$C_{s,3} = e^{-a/b} \times \left[\frac{k_{out,z} B_z \varepsilon}{\eta B_x (m_z \gamma)^2} \left(m_z \gamma - 2\alpha m \pm 2\sqrt{\alpha m (\alpha m - m_z \gamma)} \right) \right]^{1/b}$$
(S14)

If $C_s > C_{s,3}$, there is no equilibrium. If $C_s \le C_{s,3}$, then there is two (or one if equal) possible steady points E_* appearing at $C_{s,3}$. If $C_{s,3} > C_{s,2}$ then the two points E_* appears when crossing the point E_1 at different level of contamination (case of the Fig. 3). When $C_{s,3} \le C_{s,2}$, the point coexisting E_* appears at $C_{s,3}$ and then is divided into the two possible points.

However, the last condition required for the feasibility of $E_{*,\{a,b\}}$ is that $x_{i,*,\{a,b\}} < x_1$. Therefore, under the previous necessary conditions for coexistence, there are three possible situations: (1) If $x_{i,*,\{a,b\}} < x_1$, then there is two coexistence points (i.e., $E_{*,a}$ and $E_{*,b}$). (2) If $x_{i,*,a} < x_1 < x_{i,*,b}$, then there is only one coexistence point (i.e., $E_{*,a}$ or $E_{*,b}$). (3) Finally when $x_{i,*,\{a,b\}} > x_1$, then there is no coexistence point.

725 S1.10 The coexisting point E_*

Since $E_*(x_*, z_*)$ is the coexisting equilibrium point, then x_* is the root of:

$$\overline{\psi}(C_s, x_*)\Phi(x_*) - \overline{\mu_z}(C_s, x_*) - m = 0$$
(S15)

and z_* is:

$$z_* = \frac{x_*}{\Phi(x_*)} \left(\overline{\pi}(C_s) \left(1 - \frac{x_*}{K} \right) - \overline{\mu_x}(C_s) \right)$$
(S16)

Therefore, if x_* is a positive root of (S15), then $z_* > 0$ is positive when $x_* < K\left(1 - \frac{\overline{\mu}_x(C_s)}{\overline{\pi}(C_s)}\right)$. Feasibility condition for E_* is given by

$$0 < x_* < K\left(1 - \frac{\overline{\mu_x}(C_s)}{\overline{\pi}(C_s)}\right) := x_1 \quad \text{with} \quad \overline{\mu_x}(C_x) < \overline{\pi}(C_s) \tag{S17}$$

The interior equilibrium point E_* bifurcates from the axial equilibrium point E_1 at the bifurration threshold $C_s = C_{s,2}$ where $C_{s,2}$ is a positive root of the equation $K\left(1 - \frac{\overline{\mu}_x(C_s)}{\overline{\pi}(C_s)}\right) = x_*$, that is when $x_1 = x_*$. Note also that $x_* < x_1$ when $C_s < C_{s,2}$, otherwise, $x_* > x_1$ but in this situation E_* is no more feasible. One requires $x_* > 0$ and functions $\overline{\pi}(C_s)$ is a decreasing function and $\overline{\mu}_x(C_s)$ is an increasing function. Therefore, we have $C_{s,2} < C_{s,1}$. Now we can find the local asymptotic stability conditions for various equilibrium of the system (S10).

⁷³⁶ S1.11 Stability of equilibria

737 Stability conditions for point $E_0 = (0,0)$

738

⁷³⁹ First we calculate the Jacobian matrix for the system (S10) around the trivial equilibrium point

740 E_0 and find:

$$J_0 = \begin{bmatrix} \overline{\pi}(C_s) - \overline{\mu}_x(C_s) & 0\\ 0 & -m \end{bmatrix}$$
(S18)

One eigenvalue is always negative and E_0 is stable if $\overline{\pi}(C_s) < \overline{\mu_x}(C_s)$ and is a saddle-point if $\overline{\pi}(C_s) > \overline{\mu_x}(C_s)$. The first eigenvalue becomes zero when $C_s = C_{s,1}$ and the model under consideration undergoes first transcritical bifurcation. The transversality condition has to be satisfied, that is the real part of the eigenvalues have to be non-zero.

745 Stability conditions for point $E_1 = (x_1, 0)$

746

Now we evaluate the Jacobian matrix for the system (S10) around E_1 to obtain:

$$J_{1} = \begin{bmatrix} -\overline{\pi}(C_{s}) + \overline{\mu_{x}}(C_{s}) & -\Phi(x_{1}) = -\Phi\left(K\left(1 - \frac{\overline{\mu_{x}}(C_{s})}{\overline{\pi}(C_{s})}\right)\right) \\ 0 & \overline{\psi}(C_{s}, x_{1})\Phi(x_{1}) - \overline{\mu_{z}}(C_{s}, x_{1}) - m \end{bmatrix}$$
(S19)

The eigenvalues of this matrix are given by the diagonal elements of the above matrix. For feasible existence of E_1 , we need $\overline{\mu_x}(C_s) < \overline{\pi}(C_s)$ and hence the first eigenvalue is negative.

Next we know that E_* is not feasible for $x_* > K\left(1 - \frac{\overline{\mu_x}(C_s)}{\overline{\pi}(C_s)}\right)$. Then using the relation that x_* is the positive root of the equation $\overline{\psi}(C_s, x_*)\Phi(x_*) - \overline{\mu_z}(C_s, x_*) - m = 0$, then we have $x_* = \Phi^{-1}\left(\frac{\overline{\mu_z}(C_s, x_*) + d}{\overline{\psi}(C_s, x_*)}\right)$, and we can derive that E_* is not feasible for:

$$\Phi^{-1}\left(\frac{\overline{\mu_z}(C_s, x_*) + d}{\overline{\psi}(C_s, x_*)}\right) > K\left(1 - \frac{\overline{\mu_x}(C_s)}{\overline{\pi}(C_s)}\right)$$
(S20)

Since $\Phi(.)$ is an increasing function and $\overline{\psi}(.) > 0$, the last inequality is equivalent to:

$$\overline{\mu_{z}}(C_{s}, x_{*}) + m > \overline{\psi}(C_{s}, x_{*}) \times \Phi\left(K\left(1 - \frac{\overline{\mu_{x}}(C_{s})}{\overline{\pi}(C_{s})}\right)\right)$$
(S21)

And therefore, we can derive that $\overline{\psi}(C_s, x_*) \Phi(x_*) - \overline{\mu_z}(C_s, x_1) - m < 0$ whenever E_* is not feasible. Hence E_1 is locally asymptotically stable whenever E_* is not feasible, when $C_s > C_{s,2}$.

If the condition $\overline{\psi}(C_s, x_1)\Phi(x_1) = \overline{\mu_z}(C_s, x_*) + m$ is satisfied then one eigenvalue of J_1 is zero and E_1 loses stability through another Transcritical bifurcation. Proceeding with the similar argument we can prove that E_1 is a saddle-point if E_* is feasible.

759 Stability conditions for point $E_* = (x_*, z_*)$

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Finally we consider the local asymptotic stability of the coexisting equilibrium point E_* . Evaluating the Jacobian matrix around E_* we find:

$$J_{*} = \begin{bmatrix} \overline{\pi(C_{s})} - \frac{2\overline{\pi(C_{s})}x_{*}}{K} - \overline{\mu_{x}}(C_{s}) - z_{*}\frac{\partial\Phi(x)}{\partial x}\Big|_{x_{*}} & -\Phi(x_{*}) \\ z_{*}\left(-\frac{\partial\overline{\mu_{z}}(C_{s},x)}{\partial x}\Big|_{x=x_{*}} + \overline{\psi}(C_{s},x_{*}) \times \frac{\partial\Phi(x)}{\partial x}\Big|_{x=x_{*}} + \Phi(x_{*})\frac{\partial\overline{\psi}(C_{s},x)}{\partial x}\Big|_{x=x_{*}}\right) & 0 \end{bmatrix}$$
(S22)

Since the determinant is positive (i.e., $Det(J_*) > 0$), the stability of E_* is determined by the trace of the matrix J_* as whenever E_* is feasible. Consequently, E_* is stable if $Tr(J_*) < 0$, is unstable if $Tr(J_*) > 0$ and undergoes Hopf-bifurcation if $Tr(J_*) = 0$. Solving the equation $Tr(J_*) = 0$ for C_s , we find the Hopf-bifurcation threshold $C_{s,H}$. Then satisfaction of the condition $\frac{d}{dC_s}Tr(J_*)\Big|_{C_s=C_{s,H}} \neq 0$ ensures that system undergoes Hopf-bifurcation at $C_s = C_{s,H}$. We need to keep in mind that the occurrence of Hopf-bifurcation is related to the existence of a positive root of the equation $Tr(J_*) = 0$ in terms of C_s , apart from the satisfaction of transversality condition.

Threshold for Hopf-Bifurcation: $C_{i,H}$

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Let $F_i(x) = x \left(\overline{\pi}(C_s) \left(1 - \frac{x}{K}\right) - \overline{\mu_x}(C_s)\right)$. At E_* , we have $z_{i*} = \frac{F_i(x_*)}{\Phi(x_*)}$. Therefore, the trace is equivalent to:

$$Tr(J_*) = \frac{\partial F_i}{\partial x} - z_{i*} \frac{\partial \Phi(x)}{\partial x} = \frac{\partial F_i}{\partial x} - \frac{F_i(x_*)}{\Phi(x_*)} \times \frac{\partial \Phi(x)}{\partial x} = \Phi(x_*) \times \frac{\partial}{\partial x} \left(\frac{F_i(x)}{\Phi(x)}\right)$$
(S23)

Since $\Phi(x_*) > 0$ when $E_* = (x_*, z_*)$ is feasible, then the sign of $Tr(J_*)$ is the sign of

$$\frac{\partial}{\partial x} \left(\frac{F_i(x)}{\Phi(x)} \right) \tag{S24}$$

The case where $\frac{\partial}{\partial x} \left(\frac{F_i(x)}{\Phi(x)} \right) < 0$ means that if we move a little from the point E_* , then the number of prey eaten is greater than the number of prey produced, and therefore, the system goes back to the steady point E_* . However, after a little change, if $\frac{\partial}{\partial x} \left(\frac{F_i(x)}{\Phi(x)} \right) > 0$, then the number of prey produce will be greater than the number of prey eaten, and the system moves away from the steady point E_* . With Holling's type functional response, the sign of $Tr(J_*)$ is the sign of:

Holling type I:
$$= -\overline{\pi}(C_s) \leq 0$$

Holling type II: $= -2ahx_*\overline{\pi}(C_s) + ahK(\overline{\pi}(C_s) - \overline{\mu_x}(C_s)) - \overline{\pi}(C_s)$ (S25)
Holling type III: $= -2ahx_*^3\overline{\pi}(C_s) + (K - ahKx_*^2)(\overline{\mu_x}(C_s) - \overline{\pi}(C_s))$

780 S1.12 Explicit formulation of threshold concentration: $C_{s,3}$

⁷⁸¹ For the predator dynamic, we have:

$$\frac{dz}{dt} = z \left(\psi(C_s) \Phi(x) - \mu_z(C_z) - m \right)$$

$$= z \left(\varepsilon \left(\alpha C_z + 1 \right) \Phi(x) - m_z \gamma C_z - m \right)$$

$$= z \left(\varepsilon \left(\alpha \frac{\eta B_x}{k_{out,z} B_z} \Phi(x) C_x + 1 \right) \Phi(x) - m_z \gamma \frac{\eta B_x}{k_{out,z} B_z} \Phi(x) C_x - m \right)$$

$$= z \left(\varepsilon \alpha \frac{\eta B_x}{k_{out,z} B_z} \Phi(x)^2 C_x + \varepsilon \Phi(x) - m_z \gamma \frac{\eta B_x}{k_{out,z} B_z} \Phi(x) C_x - m \right) := z G_i(x, C_x)$$
(S26)

We define ϕ the roots of the polynomial $G_i(x, C_x)$ giving:

$$\varepsilon \alpha \frac{\eta B_x}{k_{out,z} B_z} C_x \phi^2 + \left(\varepsilon - m_z \gamma \frac{\eta B_x}{k_{out,z} B_z} C_x\right) \phi - m = 0 \tag{S27}$$

⁷⁸³ Since $\varepsilon \alpha \frac{\eta B_x}{k_{out,z} B_z} C_x < 0$, to have solution for the functional response, ϕ , we have to satisfy the ⁷⁸⁴ positivity of the discriminant we denote $\Delta \ge 0$ with:

$$\Delta := \left(\varepsilon - m_z \gamma \frac{\eta B_x}{k_{out,z} B_z} C_x\right)^2 + 4\varepsilon \alpha \frac{\eta B_x}{k_{out,z} B_z} C_x m > 0 \tag{S28}$$

The roots of $\Delta = 0$ according to C_x are:

$$C_{i,a}^* = \frac{\varepsilon k_{out,zB_z}}{\eta B_x (m_z \gamma)^2} \left(m_z \gamma - 2\alpha m - 2\sqrt{\alpha m (\alpha m - m_z \gamma)} \right)$$
(S29)

786 and

$$C_{i,b}^* = \frac{\varepsilon k_{out,zB_z}}{\eta B_x (m_z \gamma)^2} \left(m_z \gamma - 2\alpha m + 2\sqrt{\alpha m (\alpha m - m_z \gamma)} \right)$$
(S30)

Note that the part under the square root is positive since $\alpha < 0$.

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Now, since
$$\left(m\gamma \frac{\eta B_x}{k_{out,z}B_z}\right)^2 > 0$$
, then $\Delta > 0$ for $C_x \not\in]C_{i,a}^*, C_{i,b}^*[$.

The solution of the equation
$$(S27)$$
 are:

$$\phi_{i,1} = \frac{k_{out,z}B_z}{2\varepsilon\alpha C_x\eta B_x} \left(\frac{\gamma m_z C_x\eta B_x}{k_{out,z}B_z} - \varepsilon - \sqrt{\Delta}\right) \quad \text{and} \quad \phi_{i,2} = \frac{k_{out,z}B_z}{2\varepsilon\alpha C_x\eta B_x} \left(\frac{\gamma m_z C_x\eta B_x}{k_{out,z}B_z} - \varepsilon + \sqrt{\Delta}\right) \tag{S31}$$

In the expression of Δ , we have $\varepsilon \alpha D_i C_x m < 0$, so there are always two positive solutions, and we have:

$$\varepsilon - \frac{\gamma m_z C_x \eta B_x}{k_{out,z} B_z} - \sqrt{\left(\varepsilon - m_z \gamma \frac{\eta B_x}{k_{out,z} B_z} C_x\right)^2 + 4\varepsilon \alpha \frac{\eta B_x}{k_{out,z} B_z} C_x m} > 0$$

$$\Leftrightarrow \quad \varepsilon - \frac{\gamma m_z C_x \eta B_x}{k_{out,z} B_z} - 2\sqrt{-\varepsilon \alpha \frac{\eta B_x}{k_{out,z} B_z} C_x m} > 0$$
(S32)

⁷⁹³ So the previous inequality (S32) implies that:

$$\varepsilon - \frac{\gamma m_z C_x \eta B_x}{k_{out,z} B_z} > 0 \quad \Leftrightarrow \quad C_x < \frac{k_{out,z} B_z}{m_z \gamma \eta B_x} \varepsilon \tag{S33}$$

Also, let us define the equation $P(C_x) := \varepsilon - \frac{\gamma m_z C_x \eta B_x}{k_{out,z} B_z} - 2 \sqrt{-\varepsilon \alpha \frac{\eta B_x}{k_{out,z} B_z} C_x m}$. The function P is decreasing with C_x . Then, solving $P(C_{i,c}^*) = 0$ we get:

$$C_{i,c}^* = \frac{k_{out,z} B_z \varepsilon}{(m_z \gamma)^2 \eta B_x} \left(\gamma m_z - 2\alpha m \pm 2\sqrt{\alpha d(\alpha m - \gamma m_z)} \right)$$
(S34)

Therefore, for $C_x < \frac{k_{out,z} B_z \varepsilon}{m_z \gamma \eta B_x}$, we get:

$$C_{i,c}^* = \frac{k_{out,z} B_z \varepsilon}{(m_z \gamma)^2 \eta B_x} \left(\gamma m_z - 2\alpha m - 2\sqrt{\alpha d(\alpha m - \gamma m_z)} \right)$$
(S35)

⁷⁹⁷ Also, we previously found the threshold values:

$$C_{i,a}^* = \frac{\varepsilon}{D(m_z \gamma)^2} \left(m_z \gamma - 2\alpha m - 2\sqrt{\alpha m(\alpha m - m_z \gamma)} \right)$$
(S36)

798 and

$$C_{i,b}^* = \frac{\varepsilon}{D(m_z \gamma)^2} \left(m_z \gamma - 2\alpha m + 2\sqrt{\alpha m(\alpha m - m_z \gamma)} \right)$$
(S37)

As a consequence, we define $C_{i,3} = \min\{C_{i,a}, C_{i,b}, C_{i,c}\} = C_{i,c} = C_{i,a}$, which is the threshold value of prey concentration for the existence of E_* .

We defined the soil concentration threshold $C_{s,3}$ the point:

$$C_{i,3}^* = e^a \times C_{s,3}^b \qquad \Leftrightarrow \qquad C_{s,3} = e^{-a/b} (C_{i,3}^*)^{1/b}$$
(S38)

As a consequence, if $C_s < C_{s,3}$, then $G_i(x, C_x) > 0$ has two positive solutions on $\Phi(x)$ denoted $\phi_{i,1}$ and $\phi_{i,2}$. And if $C_s > C_{s,3}$, then $G_i(x, C_x)$ has no solution.

⁸⁰⁴ S1.13 Positivity of the determinant

Determinant of the Jacobian matrix at the coexistence steady point E_* is:

$$\det(J_*) = \Phi(x_*)z_* \left(-\frac{\partial\overline{\mu_z}(C_s, x)}{\partial x} \big|_{x=x_*} + \overline{\psi}(C_s, x_*) \times \frac{\partial\Phi(x)}{\partial x} \big|_{x=x_*} + \Phi(x_*) \frac{\partial\overline{\psi}(C_s, x)}{\partial x} \big|_{x=x_*} \right)$$
(S39)

806 We have:

$$\frac{\partial \Phi(x)}{\partial x} > 0 \tag{S40}$$

and since $\psi(.)$ is an increasing function:

$$\frac{\partial\overline{\psi}(C_s,x)}{\partial x} = \frac{\partial\psi\left(\frac{\eta B_x}{k_{out,z}B_z}\Phi(x)C_x\right)}{\partial x} = \frac{\eta B_x}{k_{out,z}B_z}C_x\frac{\partial\psi\left(\Phi(x)\right)}{\partial x} > 0$$
(S41)

Finally, since $\mu(.)$ is a decreasing function:

$$\frac{\partial \overline{\mu_z}(C_s, x)}{\partial x} = \frac{\eta B_x}{k_{out, z} B_z} C_x \frac{\partial \mu_z(\Phi(x))}{\partial x} < 0$$
(S42)