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# True density of combustion emitted particles: A comparison of results highlighting the influence of the organic contents

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#### **Abstract**

A validation of the ISO 787-23 method for measuring true density on reference black carbon samples and combustion emitted particles is proposed and compared to alternative methods. New measurements of true density on samples representative of fire emissions at different scales are presented and discussed, according to their respective experimental uncertainties. These results are compared to the values of soot true densities reported in the literature. An interesting correlation between the true density of combustion emitted particles and the Organic Carbon (OC) content is observed and commented: the true density significantly decreases as OC content increases. Three different ranges of true densities are then proposed as a function of the OC/Total Carbon (TC) ratio of combustion emitted particles. For low OC contents (i.e. below 5%) and high OC contents (i.e. above 20%), respective mean values of 1834 +/- 187 kg/m<sup>3</sup> and 1285 +/- 217 kg/m<sup>3</sup> are proposed. For intermediate OC content values, a fit is applied based on a mixing law. Finally, there is a discussion on the relevance of using these values for true densities of combustion emitted particles for temperatures representative of those reported in industrial fires, ranging from 25°C to 240°C.

#### **Introduction**

True density is the density of the condensed material as opposed to the effective density (density of porous particles or agglomerates/aggregates of nanoparticles, McMurry, Wang, Park, & Ehara, 2002). For aggregates of primary spheres, true density refers to the density of the primary spheres. For soot particles, defined by Petzold et al. (2013) as agglomerates of monomers consisting solely of carbon with small amounts of hydrogen and oxygen, true density of primary particles is generally assumed to be lower than graphite density of 2200 kg/m<sup>3</sup> due to a less dense microstructure. True density of powders has been widely measured since the last century using Helium pycnometry<sup>1</sup> and volume displacement methods such as ISO 787-23<sup>2</sup>. In most cases, with these methods, at least 500 mg of powder is needed to perform a relevant density analysis. This kind of analysis is suitable for industrial applications in the field of powder production, for which powder quantity is not a limiting factor. For research applications, and specifically within the aerosol and soot scientific community, retrieving several hundred milligrams of nanostructured carbonaceous particles from a burner, a diffusion flame or automotive/aircraft engines is a tremendous task. Nevertheless, beyond these experimental limitations, soot true density is an important property of such particles since it is needed for many measurement techniques (light extinction (Choi et al., 1995), laser induced incandescence (Michelsen et al., 2007), morphological analysis according to effective density measurement and computation of mass concentration according to size distribution measurement devices (Yon et al., 2015)) and for describing their physical behavior (cake formation during filtration processes, see Thomas et al., 2014, and soot formation prediction, see Kennedy, 1997). Furthermore, this parameter has been recently used for the development of an automatic analysis software (Bourrous et al., 2018) able to determine the specific surface area of soot samples directly from their TEM images.

<sup>&</sup>lt;sup>1</sup> https://www.astm.org/Standards/B923.htm

<sup>&</sup>lt;sup>2</sup> https://www.iso.org/standard/5102.html

Usually, the true density of freshly emitted soot particles is assumed to be close to 1800-1900 kg/m<sup>3</sup> (Bond et al., 2013; Dobbins, Mulholland, & Bryner, 1994). In fact, due to the lack of sample mass, limited numbers of experimental values are reported in the literature and they are often determined by Helium pycnometry (Roessler & Faxvog, 1980). Recently, several authors have proposed coupling a differential mobility analyzer (DMA) with a mass to mobility classifier (e.g. the Aerosol Particle Mass APM analyzer (Ehara et al., 1996) to the Centrifugal Particle Mass Analyzer CPMA (J. S. Olfert & Collings, 2005)) for computing the inherent density of diesel (Park et al., 2004) or propane/air soot (Yon et al., 2015). However, these new approaches are indirect measurement methods and need validation.

The aim of the present paper is to review values of soot true density reported in the literature and to propose additional values for particles emitted from materials relevant to fire emission studies at several scales. The reported values are mainly obtained using the ISO 787-23 method. DMA-CPMA approach was preferred for samples whose required mass cannot be reasonably obtained. The influence of the organic content of combustion emitted particles is then demonstrated, showing a significant decrease in true density as OC content increases. Finally, reference densities are proposed for low (less than 5%) and high (more than 20%) OC content of combustion emitted particles.

#### **Experimental method and validation**

The ISO 787-23 method is based on measurement of the liquid displacement induced by the immersion of a known mass of powder. The mass-to-volume ratio of the analyzed particles is determined by means of Archimedes thrust. A sketch of the principle and the measurement procedure is presented in Figure 1.

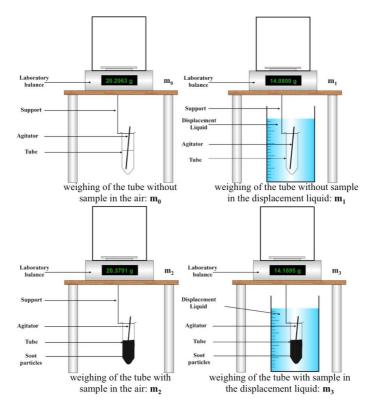


Figure 1: experimental protocol of powder true density measurement according to ISO 787-23

Four weighings (using a Mettler Toledo AE 240 analytical balance with a considered resolution of 0.001 g) are carried out: two in the air and two in the displacement liquid. Ethanol is used as the displacement liquid; its reference density at 20°C is 789 kg/m<sup>3</sup> (CRC, 2002). The first two weighings are of the sampling tube while the next two are of the sampling tube plus the powder sample. The measurements in the air determine the mass of powder while the measurements in ethanol give its volume. Due to the high porosity of nanostructured powders, it is necessary to compact the sample as much as possible. For this purpose, high-speed centrifugation (3000)

RPM) is applied for 15 minutes to the samples immerged in the displacement liquid. The measurement protocol is based on the 7 following steps:

- weighing of the tube without sample in the air: **m**<sub>0</sub>,
- weighing of the tube without sample in the displacement liquid: m<sub>1</sub>,
- drying of the tube and filling of ½ of the tube with the sample,
- weighing of the tube with sample in the air: **m**<sub>2</sub>,
- filling of <sup>3</sup>/<sub>4</sub> of the tube with the displacement liquid,
- high-speed centrifugation (3000 RPM) for 15 minutes,
- weighing of the tube with sample in the displacement liquid: m<sub>3</sub>.

Sample true density ( $\rho_{sample}$ ) is defined as the ratio of the sample mass ( $m_{sample}$ ) to the sample volume ( $V_{sample}$ ):

$$\rho_{\text{sample}} = \frac{m_{\text{sample}}}{V_{\text{sample}}} \tag{1}$$

The sample mass (m<sub>sample</sub>) is determined by weighing the tube in the air, with and without the sample:

$$\mathbf{m}_{\text{sample}} = \mathbf{m}_2 - \mathbf{m}_0 \tag{2}$$

The volume of the sample is determined by weighing the tube in the displacement liquid, with and without the sample. The difference between these two masses is associated with the liquid displacement induced by the Archimedes thrust applied by the liquid to the volume of the sample.

First, the displacement associated with the volume of the tube  $(V_{tube})$  must be determined by weighing the empty tube in the air  $(m_0)$  and in the displacement liquid  $(m_1)$ . The following relationship can be then considered:

$$m_1 = m_0 - V_{tube} \cdot \rho_{eth} \tag{3}$$

The density of the displacement liquid ( $\rho_{eth}$ ), i.e. ethanol, is then computed at the measurement temperature T (expressed in °C), considering the reference ethanol density  $\rho_0$  equal to 806.34 kg/m<sup>3</sup> at 0°C and applying a linear fit to the data reported in Dean (1990):

$$\rho_{eth} = -0.8462T + \rho_0$$
 (4)

Then, the displacement induced by the volume of sample in the tube can be determined by weighing the system (tube + sample) in the air  $(m_2)$  and in ethanol  $(m_3)$ .

$$m_3 = m_2 - (V_{tube} + V_{sample}) \cdot \rho_{eth} = m_2 - V_{tube} \cdot \rho_{eth} - V_{sample} \cdot \rho_{eth}$$
(5)

According to equations (3) and (5), the mass m<sub>3</sub> is defined as:

$$m_3 = m_2 - (m_0 - m_1) V_{sample} \rho_{eth}$$
 (6)

The volume of the sample is determined by:

$$V_{sample} = \frac{m_2 - m_3 - m_0 + m_1}{\rho_{eth}}$$
(7)

Finally, the sample density is defined by:

$$\rho_{\text{sample}} = \frac{m_{\text{sample}}}{V_{\text{sample}}} = \frac{(m_2 - m_0) \cdot \rho_{\text{eth}}}{m_2 - m_3 - m_0 + m_1} = \frac{(m_2 - m_0) \cdot \rho_{\text{eth}}}{(m_2 - m_0) - (m_3 - m_1)} = \frac{\rho_{\text{eth}}}{1 - \frac{(m_3 - m_1)}{(m_2 - m_0)}}$$
(8)

In the present study, sample densities were determined N times and a  $\chi^2$  test was carried out for each sample in order to discuss the dispersion of the experimental results. This dispersion is estimated by using the standard

deviation  $s(\rho_{sample})$ , according to the mean values of the uncertainties  $u(\rho_{sample})$ . Finally, the mean value of sample density  $\bar{\rho}_{sample}$  is determined by considering the N values obtained, and the uncertainties associated with this mean value are computed (for details see Annex I):

$$\overline{\rho_{\text{sample}}} = \frac{1}{N} \sum_{i=1}^{N} \rho_{(i)\text{sample}}$$
(9)

Before it was applied to real soot particles, this method was validated on several powder samples and carbonaceous particles with well-known true densities considered in the present article as "references". Table 1 presents the properties of the reference samples and Figure 2 presents the comparison between currently measured densities based on the ISO 787-23 method and the reference true densities corresponding to the values reported in the literature. At least three density measurements were made for each reference sample, and their mean values are presented in Table 1. As previously mentioned, before computing the mean values, a  $\chi^2$  test was also applied to the density results in order to verify the dispersion of the experimental values. This dispersion is explained by the experimental measurement process (see Annex II). The agreement between measured and reference densities appears to be quasi-perfect with a discrepancy of less than 5%. This confidence interval is in good agreement with the uncertainty determined for the entire measurement protocol and detailed in Annex I.

 Table 1: properties of reference samples used for the validation of the ISO 787-23 and DMA-CPMA methods of determining powder and aerosol samples

Nature	Name	Diameter	Reference true density (kg/m <sup>3</sup> )	OC content (%)	Measured true density (kg/m <sup>3</sup> )	Source			
Glass marbles	Glass	-	2500	n.r.	2369 +/- 39	-			
Alumina	Al <sub>2</sub> O <sub>3</sub>	-	3950 <sup>1</sup>	3950 <sup>1</sup> n.r.		<sup>1</sup> Durmax			
	LB 101	95 nm <sup>2</sup>	1770 <sup>3</sup>	$\begin{array}{c} 0.8 \ \%^2 \\ 0.8 \ \% \ \text{+/-} \ 0.1 \ \%^4 \end{array}$	1717 +/- 49	<sup>2</sup> (Saber et al., 2012) <sup>3</sup> manufacturer <sup>4</sup> present study			
Black carbon	Printex 90	14 nm <sup>5</sup>	1800 <sup>5</sup>	2.0 % <sup>6</sup> 1.3 % +/- 0.1 % <sup>4</sup>	1791 +/- 15	<sup>5</sup> (De Temmerman et al., 2014) <sup>6</sup> (Ferge et al., 2006) <sup>7</sup> (Pawlyta et al., 2015)			
	Printex 25	49 nm <sup>7</sup>	1800 <sup>3</sup>	$0.9 \%^3$	1878 +/- 15				
Glassy carbon	Glassy C.	0.4-12 μm <sup>8</sup>	14008	-	1402 +/- 17	<sup>8</sup> Good-fellow			
		Samples use	ed for validation of	f the DMA-CPMA ap	oproach				
Spark discharge carbonaceous aggregates	GFG1000	7 <sup>9</sup> – 8.6 <sup>10</sup> nm	$2000^{10}$ $2250^{09}$	$4.0~\%^{11}$	215011	<sup>9</sup> (Charvet et al., 2014) <sup>10</sup> (Schnaiter et al., 2003)			
Propane diffusion flame	CAST 16.2% OC	27 nm <sup>11</sup>	1631 +/- 132*	16.2 %	154311	<sup>11</sup> (Yon et al., 2015)			
n.r.: OC content measurement is not relevant for glass marbles and alumina *reference true density for CAST sample determined according to ISO 787-23									

As mentioned above, the main disadvantage of the ISO 787-23 method is the need for a significant sample mass (at least 100 mg). For soot sources such as a gaseous burner (miniCAST) and aircraft engine, the minimum amount of particles needed to apply the ISO 787-23 method is difficult to achieve. Consequently, for these particles, the DMA-CPMA method linked to TEM analysis of primary particle size distribution in terms of diameter, was considered (Park et al., 2004). Further details regarding the feasibility of this approach for determining soot true density could be retrieved in Yon et al. (Yon et al., 2015). Validation of this method has been performed for spark discharge nanoparticle aggregates (GFG1000) and propane diffusion flame soot

particles (CAST with an OC/TC content of 16.2%), and their physico-chemical properties are also reported in Table 1. Reference true density was considered from previous studies (Charvet et al., 2014; Schnaiter et al., 2003) for GFG1000 and from direct measurements based on previously validated ISO 787-23 for CAST. A good agreement (within +/- 5%) is also reported in Figure 2 for the DMA-CPMA approach, confirming the relevance of this alternative method for measuring soot true density.

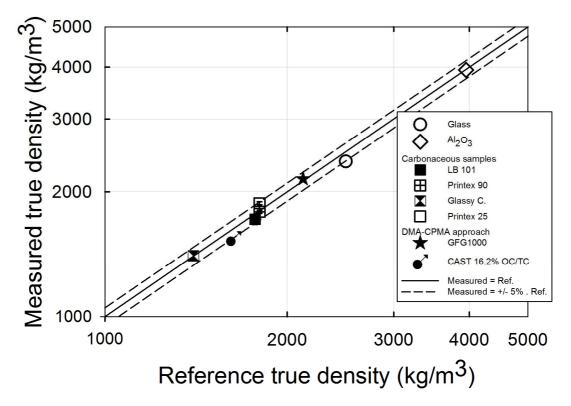


Figure 2: validation of the true density measurement methods ISO 787-23 and DMA-CPMA with reference powders

#### Experimental results: evidence of the influence of organic carbon content

The  $\chi^2$  test confirmed the homogeneity of the reference sample composition. However, several soot samples did not pass the  $\chi^2$  test (see Annex III), demonstrating, statistically, that the composition of these soot samples was not homogeneous. Nevertheless, final uncertainties were estimated taking into account this dispersion, enabling the associated mean values to be discussed.

The properties of the analyzed samples are summarized in Table 2. Since complex fire conditions were considered in the present work, clarification of the different definitions associated with combustion emitted particles is needed. Following Petzold et al. (2013), in the present study soot will refer to samples mostly consisting of carbon, with small amounts of hydrogen and oxygen and, for the present study, with an OC/TC ratio below 5%. Combustion emitted particles will refer to all other samples, denoting significant amounts of organic content and metals.

Soot true densities obtained by previous authors are also reported in Table 2 for comparison. In addition to true density, OC content is reported, corresponding to the organic to total carbon ratio OC/TC determined, in the present study with a thermo-optical device (Sunset Lab) using the improved protocol (Chow et al., 2007). Soot particles were sampled on pre-baked (at 850°C for 1 hour) quartz fiber filters (Pall Tissuquartz 2500 QAT-UP, 47 mm in diameter) and three punches of 1.5 cm<sup>2</sup> each were analyzed for each sample. Sampling flowrates were dependent on experimental conditions (from 1 to 5 L/min). Furthermore, samplings were carried out close to the emission point (in order to be as representative as possible of fresh combustion aerosol without any ageing effect), at temperatures near 100°C. For this reason, semivolatile vapor adsorption was not considered to be

significant within our experimental conditions (Turpin & Huntzicker, 1994). For samples identified from the literature for which OC/TC is not available, OC content is associated with carbon-to-oxygen ratio C/O or oxygen content O, determined by elemental analysis.

Within the present work, soot and combustion emitted particles are produced by different means at different scales: analytical test bench based on miniCAST soot generator (Yon et al., 2015), cone calorimeter (Mocho & Ouf, 2011; Ouf et al., 2015; Ouf et al., 2008), large-scale fires in over-ventilated/open (SATURNE facility) or under-ventilated/confined (DIVA facility) conditions (Ouf et al., 2014) and even during an aircraft engine test (Delhaye et al., 2017). Soot particles are generally pneumatically retrieved from previously clogged High Efficiency Particulate Air Filters installed in the ventilation networks of test benches.

In the case of laboratory gaseous diffusion flames, except for the miniCAST burner (Yon et al., 2015), the results reported in the literature and in the present study are in close agreement. According to values reported for gaseous burners, associated with low levels of organic content (i.e. below 5%, marked in Table 2 by an "\*" and previously defined as soot particles), a mean value of 1834 +/- 187 kg/m<sup>3</sup> is proposed for particles produced by gaseous fuels (acetylene, propylene, ethylene, methane, propane) and liquid fuels (toluene, n-heptane, diesel).

For other diffusion flames of liquids or polymers (samples marked by \*\* or no asterisk in Table 2), combustion emitted particles denote higher OC/TC ratios and significantly lower true densities than the previously reported mean value of 1834 kg/m<sup>3</sup>. A similar trend is also noticed for the miniCAST and aircraft particles, which also denote a high OC content.

Figure 3 presents the evolution of the true density of the samples considered, reported in Table 2 as a function of the organic carbon content (OC/TC ratio). Since the soluble organic fraction of the OC/TC fraction of the samples considered could be dissolved by ethanol, some of the samples were analysed in terms of OC/TC ratio before and after this centrifugation step. The corresponding variation in the OC/TC ratio was added in Figure 3 as dispersion bars for this property; more details are available in Annex IV.

Source	Fuel	OC content	Method	True density (kg/m <sup>3</sup> )	<u>Reference</u>		
	Acetylene ( $C_2H_2$ )	C/O: 107		1870*			
	Propylene $(C_3H_6)$	C/O: 57.6		1850*			
	Ethylene ( $C_2H_4$ )	-	Helium	1930*	(Wu, Krishnan, & Faeth, 1997)		
	Propane $(C_3H_8)$	-	pycnometry	1900*			
D:00 : 0	Acetylene $(C_2H_2)$	2.3 % O		2050*	(Roessler & Faxvog, 1980)		
Diffusion flame	Acetylene $(C_2H_2)$	-		1740 +/- 100*	(Choi et al., 1995)		
	Toluene (C <sub>7</sub> H <sub>8</sub> )	C/O: 7.52 +/- 0.74	Helium	1800 +/- 20*			
	Propane (C <sub>3</sub> H <sub>8</sub> )	C/O : 9.43 +/- 0.03	displacement	1770 +/- 20*			
	n-Heptane (C <sub>7</sub> H <sub>16</sub> )	C/O: 8.35 +/- 0.73	with BET	1780 +/- 20*	(Mullins & Williams, 1987)		
	Methane (CH <sub>4</sub> )	C/O: 5.66 +/- 0.30	apparatus	1830 +/- 20*			
		30		1270 for soot size 50 nm**	(Park et al., 2004)		
Automotive	Diesel fuel	10	DMA-APM	1780 for soot size 220 nm			
engine	Diesel fuel			1770 +/- 70 for soot at 300°C*	(Sakurai et al., 2003)		
	Acetylene $(C_2H_2)$ (BANCO)	5		1719 +/- 30*			
ŀ	Toluene ( $C_7H_8$ ) 450 (BANCO)	16.3		1515 +/- 191			
Diffusion	Toluene ( $C_7H_8$ ) 100 (BANCO)	25.0	Volume	1483 +/- 100**			
Flame	PMMA <sup>1</sup> (C <sub>5</sub> H <sub>8</sub> O <sub>2</sub> ) 450 (BANCO)	10.1	displacement	1648 +/- 78	Present study		
(cone calorimeter)	PMMA <sup>1</sup> (C <sub>5</sub> H <sub>8</sub> O2)100 (BANCO)	15.3	method ISO 787-23	1492 +/- 12	-		
calofineter)	2/3 PMMA <sup>1</sup> + 1/3 PVC <sup>1</sup> (BANCO)	14.8 +/- 2.3	130 787-25	1315 +/- 82			
	TBP <sup>2</sup> / TPH <sup>2</sup> (PARIS)	15.0 +/- 1.4		1534 +/- 78 <sup>†</sup>			
		16.2		1543			
miniCAST	Propane with different	58.3		1234**			
diffusion flame	fuel to air ratios	87	DMA-CPMA	1321**	(Yon et al., 2015)		
		22		1227**			
Aircraft engine	Kerozene	25.8 +/- 1.5		1174**	Present study		
	Electrical elements (BANCO)	37.6 +/- 1.7		1762 +/- 6 <sup>††</sup>	· · · · ·		
	Electrical cabinet (DIVA)	37.6 +/- 1.7		1672 +/- 29 <sup>††</sup>			
	Electrical cables (CFS)	55.3 +/- 2.8 <sup>††</sup>	Volume	2000 +/- 68 <sup>††</sup>			
Real scale fire	Electrical cable with PVC (CORE)	8.4 +/- 1.0 <sup>††</sup>	displacement method	1768 +/- 39 <sup>††</sup>	Present study		
	Hydraulic oil (FES)	10.3 +/- 0.4	ISO 787-23	1665 +/- 164			
	Gloves box (SATURNE)	6.2 +/- 0.6	150 707-25	1749 +/- 82	]		
	Gloves box (DIVA)	48.1 +/- 3.4**		2069 +/- 35 <sup>††</sup>			
densities considered for	or soot particles**densities considered for high ( solvant composed by tributyl phosphate and te	•					

**Table 2:** properties and true density of combustion emitted particle samples

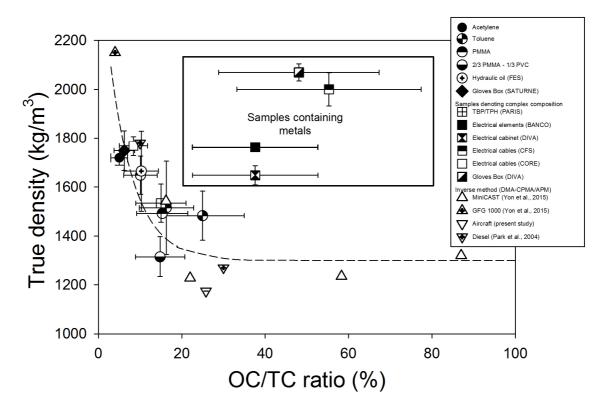


Figure 3: evolution of combustion emitted particle true density as a function of OC/TC ratio (dashed line is a guide to the eye)

High true density values are observed for several samples (electrical elements, electrical cabinet, electrical cables and glove box soot produced within the DIVA facility), even with a significant OC content. This discrepancy with other samples is mainly due to the significant metal content (iron, copper, etc.) reported for these samples, which tends to significantly enhance the true density of the mixing of carbonaceous particles with metallic particles.

For low OC contents (below 5%), the true density could be considered constant with a corresponding mean value of 1834 +/- 187 kg/m<sup>3</sup> as previously proposed (see samples marked by an "\*" in Table 2). For OC contents above 20 % (miniCAST and aircraft soot), the true density is almost constant and close to a mean value (calculated using the samples marked "\*\*" in Table 2) of 1285 +/- 217 kg/m<sup>3</sup>. By assuming that OC is mainly composed by Polycyclic Aromatic Hydrocarbons (PAH), then higher OC content could be associated with heavier PAHs formed by the miniCAST burner (Mueller et al., 2015), the present asymptotic density value is in close agreement with the density of several PAHs reported in the literature (i.e. from 980 kg/m<sup>3</sup> for phenanthrene to 1351 kg/m<sup>3</sup> for benzo[ $\alpha$ ]pyrene, ATSDR, 1995).

In between, a straight decrease of true inherent density is observed as OC mass fraction increases. As reported by several authors (Park et al., 2004; Sakurai et al., 2003), the density of diesel particles is strongly affected by the organic content and tends to decrease from the true density of the elemental carbon (EC) (close to 2000 kg/m<sup>3</sup>, CRC, 2002) to the density of the organic matter condensed on the diesel soot particles (OC). Those authors also proposed, based on a mixing law approach, defining the inherent true density  $\rho_{inherent}$  as a function of the respective density of these two carbonaceous fractions:

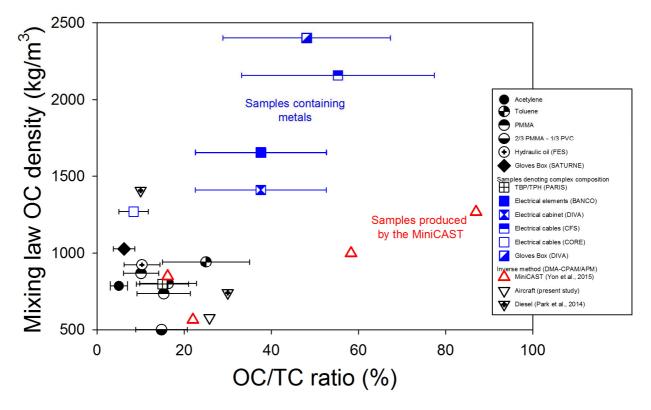
$$\rho_{\text{inherent}} = \frac{M_{\text{OC}} + M_{\text{EC}}}{V_{\text{OC}} + V_{\text{EC}}} = \frac{M_{\text{OC}} + M_{\text{EC}}}{\frac{M_{\text{OC}}}{\rho_{\text{OC}}} + \frac{M_{\text{EC}}}{\rho_{\text{EC}}}} = \frac{x + (1 - x)}{\frac{x}{\rho_{\text{OC}}} + \frac{1 - x}{\rho_{\text{EC}}}},\tag{10}$$

where  $M_{OC}$ ,  $V_{OC}$  and  $\rho_{OC}$  are, respectively, the mass, the volume and the density of organic condensed carbon,  $M_{EC}$ ,  $V_{EC}$  and  $\rho_{FC}$  are respectively the mass, the volume and the density of elemental carbon, and x is the mass

fraction of organic carbon  $\left(x = \frac{M_{OC}}{M_{OC}+M_{EC}}\right)$  as determined by thermo-optical analysis. However, this type of equation fails to reproduce the observed trend shown in Figure 3 since the composition of OC content could evolve as OC/TC ratio increases. By considering the measured inherent density and  $\rho_{EC} = 1834 \text{ kg/m}^3$  in the mixing law (eq. 10), the density of the organic phase ( $\rho_{OC}$ ) could be calculated (eq. 11). For samples containing metals, this density will also take into account the density of the metallic fraction of particles.

$$\rho_{\rm OC} = x \left( \frac{1}{\frac{1}{\rho_{\rm measured}} - \frac{(1-x)}{\rho_{\rm EC}}} \right)$$
(11)

The trend obtained for the density of the OC fraction as a function of the OC/TC ratio is presented in Figure 4.



**Figure 4:** evolution, as a function of OC/TC ratio, of the density of the OC fraction of the sample, determined by assuming equation 10 as a mixing law for describing the inherent density of combustion emitted particles

High density values computed for particles emitted during electrical cable/element fires (BANCO, DIVA, CFS) and in ventilated glove box (DIVA) fires, confirm the significant presence of metallic compounds in addition to a high OC fraction (expected to have a density significantly lower than  $\rho_{EC}$ ). For such samples, a mixing law based on two phases (EC and OC) is not relevant and should be improved by taking into account a metal-containing phase fixed on the particle surface.

For samples with lower OC content (OC < 20%) no specific trend can be identified. This could be explained by the variety of particle production conditions (fuels, ventilation, etc.), producing different types of organic component associated with different densities (from 500 to 1400 kg/m<sup>3</sup>).

Such discrepancies are not noticeable in the case of the miniCAST soot, where the density of the OC fraction appears to increase with the OC/TC ratio. This evolution agrees with recent findings reported for miniCAST soot particles (Mueller et al., 2015). The authors then demonstrated that flames denoting a higher fuel-to-air equivalence ratio tend to produce soot with a higher OC/TC content associated with heavier PAHs denoting higher density. By assuming the elemental carbon soot density, the present approach means that it is then possible to reasonably compute the density of the organic fraction of the soot samples. Such findings are also in

agreement with a recent review by Olfert & Rogak (2019), which aims to propose "universal relations between soot effective density and primary combustion sources". It should be borne in mind that such an approach, to be fulfilled for large range of combustion sources, requires soot density to be uniform (as reported in the present study) and, consequently, OC density to be approximately the same for different sources. The present experimental method of determination of OC density, linked to effective density measurements, could potentially pave the way for the extension of these "universal relations" to other combustion emitted particles.

#### Experimental results: temperature effect on the true density of combustion emitted particles

Considering the previously reported strong influence of potentially volatile OC content on the true density of combustion emitted particles, it could be suspected that this property must be strongly affected by temperature through OC desorption from the surface of the particles. Such an assumption is essential for fire applications since the temperature within a ventilated fire room could range from ambient temperature up to 200-300°C. With the aim of confirming the significant influence of the carbonaceous organic content on the true density of samples and the effect of temperature on the same property, density measurements were carried out in accordance with ISO 787-23, on four samples at ambient temperatures and after 24 hours of heat treatment in a furnace at 120°C and 240°C respectively. Figure 5 presents the true density of the samples as a function of the post-treatment temperature. For all samples treated under these conditions, the true density does not significantly evolve and remains close to the values determined at ambient temperature. Such a conclusion demonstrates that the organic compounds in the samples considered are stable up to 240°C, a temperature representative of those encountered during a fire in a confined and poorly ventilated facility. This finding is in good agreement with Ferraro et al. (2016) who reported, based on the TGA analysis of soot particles, that the decomposition of such particles starts at 300°C. Supporting this assumption, Figure A2 (Annex V) presents the evolution of the fraction of OC analyzed at the different temperature steps of the EC/OC analyzer (140, 280, 480 and 580°C based on the IMPROVE\_A protocol). For all samples, the fraction of OC denoting the highest volatility (desorbed below 280°C) represents less than 30% of the entire OC content, confirming the limited effect of temperature on the true densities of samples even after 24 hours at 240°C, shown in Figure 5. These organic materials can be strongly bonded to the particle surface by chemisorption and can be transported from their point of emission into ventilation ducts, eventually being found on High Efficiency Particulate Air filters as mentioned by Mocho & Ouf (2011).

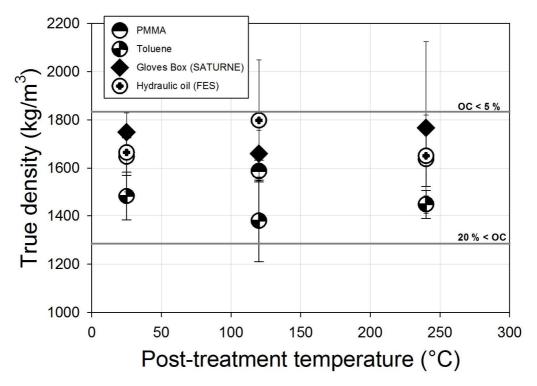


Figure 5: sample true density as a function of post-treatment temperature

#### **Conclusions**

The measurement of powder true density using the ISO 787-23 method was validated on carbonaceous particles with micronic and nanometric size distribution. Agreement within +/- 5%, explained by the experimental uncertainty associated with the measurement protocol, was reported for reference samples, confirming that this method, initially used specifically for micronic powders, is also suitable for measuring the true density of nanostructured samples such as soot particles. The agreement of the true density of the reference samples with DMA-CPMA methods is also found to be good.

True densities were determined for 13 soot samples using the ISO 787-23 method and were compared to values previously reported in the literature or indirectly obtained by DMA-CPMA analysis. Mean values of 1834 +/-187 kg/m<sup>3</sup> and 1285 +/- 217 kg/m<sup>3</sup> were proposed for soot, respectively denoting low (<5 %) and high (> 20%) OC contents. For intermediate OC contents, a mixing law was proposed for prediction of soot density. Larger true densities were determined for soot produced in complex fires, which consequently include metals in their composition.

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### Annex I: Uncertainty analysis

The uncertainty propagation law can be used to compute the relative uncertainty associated with the determined

sample density value 
$$\left(\frac{u(\rho_{sample})}{\rho_{sample}}\right)$$
:

$$\left[\frac{u(\rho_{sample})}{\rho_{sample}}\right]^{2} = \left[\frac{u(\rho_{eth})}{\rho_{eth}}\right]^{2} + \left[\frac{u\left(1 - \frac{(m_{3} - m_{1})}{(m_{2} - m_{0})}\right)}{1 - \frac{(m_{3} - m_{1})}{(m_{2} - m_{0})}}\right]^{2} = \left[\frac{u(\rho_{eth})}{\rho_{eth}}\right]^{2} + \left[\frac{u\left(1 - \frac{(m_{3} - m_{1})}{(m_{2} - m_{0})}\right)}{\frac{\rho_{sample}}{\rho_{eth}}}\right]^{2}.$$

Assuming that the sample and the liquid displacement are independent:

$$\frac{u\left(\rho_{\text{sample}}\right)}{\rho_{\text{sample}}}\right]^{2} = \left[\frac{u(\rho_{\text{eth}})}{\rho_{\text{eth}}}\right]^{2} + \frac{1}{\left[\frac{\rho_{\text{sample}}}{\rho_{\text{eth}}}\right]^{2}} \cdot \left[u(1)^{2} + u\left(\frac{(m_{3}-m_{1})}{(m_{2}-m_{0})}\right)^{2}\right] ,$$

$$\left[\frac{u\left(\rho_{\text{sample}}\right)}{\rho_{\text{sample}}}\right]^{2} = \left[\frac{u(\rho_{\text{eth}})}{\rho_{\text{eth}}}\right]^{2} + \frac{1}{\left[\frac{\rho_{\text{sample}}}{\rho_{\text{eth}}}\right]^{2}} \cdot u\left(\frac{(m_{3}-m_{1})}{(m_{2}-m_{0})}\right)^{2}$$

$$= \left[\frac{u(\rho_{eth})}{\rho_{eth}}\right]^{2} + \frac{\left(\frac{(m_{3}-m_{1})}{(m_{2}-m_{0})}\right)^{2}}{\left[\frac{\rho_{sample}}{\rho_{eth}}\right]^{2}} \cdot \frac{u\left(\frac{(m_{3}-m_{1})}{(m_{2}-m_{0})}\right)^{2}}{\left(\frac{(m_{3}-m_{1})}{(m_{2}-m_{0})}\right)^{2}}$$

$$= \left[\frac{u(\rho_{eth})}{\rho_{eth}}\right]^{2} + \frac{\left(\frac{(m_{3}-m_{1})}{(m_{2}-m_{0})}\right)^{2}}{\left[\frac{\rho_{sample}}{\rho_{eth}}\right]^{2}} \cdot \left[\frac{u(m_{3}-m_{1})^{2}}{(m_{3}-m_{1})^{2}} + \frac{u(m_{2}-m_{0})^{2}}{(m_{2}-m_{0})^{2}}\right]$$

$$= \left[\frac{u(\rho_{eth})}{\rho_{eth}}\right]^2 + \frac{\left(\frac{(m_3-m_1)}{(m_2-m_0)}\right)^2}{\left[\frac{\rho_{sample}}{\rho_{eth}}\right]^2} \cdot \left[\frac{u(m_3)^2}{(m_3-m_1)^2} + \frac{u(m_1)^2}{(m_3-m_1)^2} + \frac{u(m_2)^2}{(m_2-m_0)^2} + \frac{u(m_0)^2}{(m_2-m_0)^2}\right]$$

$$u\left(\rho_{\text{sample}}\right)^{2} = \left[\frac{\rho_{\text{sample}} \cdot u(\rho_{\text{eth}})}{\rho_{\text{eth}}}\right]^{2} + \left(\rho_{\text{eth}} \cdot \frac{(m_{3} - m_{1})}{(m_{2} - m_{0})}\right)^{2} \cdot \left[\frac{u(m_{3})^{2}}{(m_{3} - m_{1})^{2}} + \frac{u(m_{1})^{2}}{(m_{3} - m_{1})^{2}} + \frac{u(m_{2})^{2}}{(m_{2} - m_{0})^{2}} + \frac{u(m_{0})^{2}}{(m_{2} - m_{0})^{2}}\right]$$

$$u\left(\rho_{\text{sample}}\right) = \left[\left(\frac{\rho_{\text{sample}}.u(\rho_{\text{eth}})}{\rho_{\text{eth}}}\right)^{2} + \left(\rho_{\text{eth}}.\frac{(m_{3}-m_{1})}{(m_{2}-m_{0})}\right)^{2}.\left(\frac{u(m_{3})^{2}}{(m_{3}-m_{1})^{2}} + \frac{u(m_{1})^{2}}{(m_{3}-m_{1})^{2}} + \frac{u(m_{2})^{2}}{(m_{2}-m_{0})^{2}} + \frac{u(m_{0})^{2}}{(m_{2}-m_{0})^{2}}\right]^{\frac{1}{2}}.$$

The relative uncertainty associated with the ethanol density  $\left(\frac{u(\rho_{eth})}{\rho_{eth}}\right)$  is defined by:

$$\left[\frac{u(\rho_{\text{eth}})}{\rho_{\text{eth}}}\right]^2 = \left[\frac{u(\rho_0)}{\rho_0}\right]^2 + \left[\frac{u(273.15+20)}{(273.15+20)}\right]^2 + \left[\frac{u(T+273.15)}{(T+273.15)}\right]^2 \approx \left[\frac{u(T+273.15)}{(T+273.15)}\right]^2$$

where: u(T), is the uncertainty associated with the temperature measured under experimental conditions. In the present study, this uncertainty was considered to be 1°C while the ethanol reference density  $\rho_0$  at 273.15 K was assumed to be perfectly well-known (with negligible uncertainty).

The compound uncertainty  $u(m_i)$  associated with the respective weighings of masses  $m_0$ ,  $m_1$ ,  $m_2$  and  $m_3$  is considered equal to a third (k=3) of the permissible maximum error (PME) for the measured mass, assumed in the present study to be 1 mg, added to the repeatability error determined by performing 3 measurements for each mass:

$$u(\mathbf{m}_{i}) = \left[ \left( \frac{PME_{m}}{\sqrt{3}} \right)^{2} + \left( \frac{s(\mathbf{m}_{i})}{\sqrt{3}} \right)^{2} \right]^{\frac{1}{2}}$$

The uncertainty associated with the experimental measurement of sample density is then defined as:

$$u\left(\rho_{\text{sample}}\right) = \left[ \left( \frac{\rho_{\text{sample}} \cdot u(T)}{\rho_{\text{eth}} \cdot (T + 273.15)} \right)^2 + \left( \rho_{\text{eth}} \cdot \frac{(m_3 - m_1)}{(m_2 - m_0)} \right)^2 \cdot \left( \frac{2 \cdot PME_m^2 + s(m_1)^2 + s(m_3)^2}{3 \cdot (m_3 - m_1)^2} + \frac{2 \cdot PME_m^2 + s(m_2)^2 + s(m_0)^2}{3 \cdot (m_2 - m_0)^2} \right) \right]^2$$

It should be noted that correlated errors, associated with mass measurements performed on the same scale have been ignored, since they represent less than 1% of the overall uncertainty (determined on one typical experimental data set).

The uncertainty for the mean sample density value is computed by taking into account the dispersion and the

mean value of the uncertainties associated with N experimental measurements:

$$u_{c}(\bar{\rho}_{\text{sample}}) = \sqrt{\left(\frac{s(\rho_{\text{sample}})}{\sqrt{N}}\right)^{2} + \frac{1}{N}\sum_{s=1}^{N}u(\rho_{\text{sample}})^{2}},$$

where s ( $\rho_{sample}$ ), is the standard deviation associated with N measurements of sample density.

The confidence interval with a probability level of 95% is determined by multiplying the uncertainty by a weighting factor k=2:

$$IC(\overline{\rho_{\text{sample}}}) = 2. u_c(\overline{\rho_{\text{sample}}})$$

#### Annex II: Statistical analysis of experimental values of soot density

Considering several measurements, N, of sample density, the dispersion of the corresponding densities was compared using a  $\chi^2$  test.

For this purpose, the standard deviation associated with N measurements of sample density  $(\rho_{sample})$  was calculated first. The discriminant factor  $K\chi^2$  of the  $\chi^2$  test was then introduced as the ratio between this standard deviation and the mean sample density value  $\overline{\rho_{sample}}$ :

$$K_{\chi 2} = \frac{s\left(\rho_{\text{sample}}\right)}{\overline{\rho_{\text{sample}}}}$$

Finally, considering a probability of 95% (5% of chance of drawing a false conclusion) the  $K\chi^2$  factor was compared with values reported below in the  $\chi^2$  reference table associated with N measurements (or degrees of freedom).

The test is considered to be successful if  $K_{X-2}$  is lower than the value reported in the  $\chi^2$  table, confirming that the dispersion of the N values of sample density is fully explained by the measurement uncertainty and is not due to any heterogeneity of the sample.

<b>Table AII-1:</b> $\chi^2$ values as a function of probability P and degrees of freedom v (from Neuilly & CETAMA,
1000

1998)

VP	0.005	0.01	0.025	0.05	0.1	0.25	0.5	0.75	0.9	0.95	0.975	0.99	0.995
1	0.0000	0.0002	0.0010	0.0039	0.0158	0.102	0.455	1.32	2.71	3.84	5.02	6.63	7.88
2	0.0100	0.0201	0.0506	0.103	0.211	0.575	1.39	2.77	4.61	5.99	7.38	9.21	10.6
3	0.0717	0.115	0.216	0.352	0.584	1.21	2.37	4.11	6.25	7.81	9.35	11.3	12.8
4	0.207	0.297	0.484	0.711	1.06	1.92	3.36	5.39	7.78	9.49	11.1	13.3	14.9
5	0.412	0.554	0.831	1.15	1.61	2.67	4.35	6.63	9.24	11.1	12.8	15.1	16.7
6	0.676	0.872	1.24	1.64	2.20	3.45	5.35	7.84	10.6	12.6	14.4	16.8	18.5
7	0.989	1.24	1.69	2.17	2.83	4.25	6.35	9.04	12.0	14.1	16.0	18.5	20.3
8	1.34	1.65	2.18	2.73	3.49	5.07	7.34	10.2	13.4	15.5	17.5	20.1	22.0
9	1.73	2.09	2.70	3.33	4.17	5.90	8.34	11.4	14.7	16.9	19.0	21.7	23.6
10	2.16	2.56	3.25	3.94	4.87	6.74	9.34	12.5	16.0	18.3	20.5	23.2	25.2
11	2.60	3.05	3.82	4.57	5.58	7.58	10.3	13.7	17.3	19.7	21.9	24.7	26.8
12	3.07	3.57	4.40	5.23	6.30	8.44	11.3	14.8	18.5	21.0	23.3	26.2	28.3
13	3.57	4.11	5.01	5.89	7.04	9.30	12.3	16.0	19.8	22.4	24.7	27.7	29.8
14	4.07	4.66	5.63	6.57	7.79	10.2	13.3	17.1	21.1	23.7	26.1	29.1	31.3
15	4.60	5.23	6.26	7.26	8.55	11.0	14.3	18.2	22.3	25.0	27.5	30.6	32.8
16	5.14	5.81	6.91	7.96	9.31	11.9	15.3	19.4	23.5	26.3	28.8	32.0	34.3
17	5.70	6.41	7.56	8.67	10.1	12.8	16.3	20.5	24.8	27.6	30.2	33.4	35.7
18	6.26	7.01	8.23	9.39	10.9	13.7	17.3	21.6	26.0	28.9	31.5	34.8	37.2
19	6.84	7.63	8.91	10.1	11.7	14.6	18.3	22.7	27.2	30.1	32.9	36.2	38.6
20	7.43	8.26	9.59	10.9	12.4	15.5	19.3	23.8	28.4	31.4	34.2	37.6	40.0
21	8.03	8.90	10.3	11.6	13.2	16.3	20.3	24.9	29.6	32.7	35.5	38.9	41.4
22	8.64	9.54	11.0	12.3	14.0	17.2	21.3	26.0	30.8	33.9	36.8	40.3	42.8
23	9.26	10.2	11.7	13.1	14.8	18.1	22.3	27.1	32.0	35.2	38.1	41.6	44.2
24	9.89	10.9	12.4	13.8	15.7	19.0	23.3	28.2	33.2	36.4	39.4	43.0	45.6
25	10.5	11.5	13.1	14.6	16.5	19.9	24.3	29.3	34.4	37.7	40.6	44.3	46.9
26	11.2	12.2	13.8	15.4	17.3	20.8	25.3	30.4	35.6	38.9	41.9	45.6	48.3
27	11.8	12.9	14.6	16.2	18.1	21.7	26.3	31.5	36.7	40.1	43.2	47.0	49.6
28	12.5	13.6	15.3	16.9	18.9	22.7	27.3	32.6	37.9	41.3	44.5	48.3	51.0
29	13.1	14.3	16.0	17.7	19.8	23.6	28.3	33.7	39.1	42.6	45.7	49.6	52.3
30	13.8	15.0	16.8	18.5	20.6	24.5	29.3	34.8	40.3	43.8	47.0	50.9	53.7
40	20.7	22.2	24.4	26.5	29.1	33.7	39.3	45.6	51.8	55.8	59.3	63.7	66.8
50	28.0	29.7	32.4	34.8	37.7	42.9	49.3	56.3	63.2	67.5	71.4	76.2	79.5
60	35.5	37.5	40.5	43.2	46.5	52.3	59.3	67.0	74.4	79.1	83.3	88.4	92.0
70	43.3	45.4	48.8	51.7	55.3	61.7	69.3	77.6	85.5	90.5	95.0	100.4	104.2
80	51.2	53.5	57.2	60.4	64.3	71.1	79.3	88.1	96.6	101.9	106.6	112.3	116.3
90	59.2	61.8	65.6	69.1	73.3	80.6	89.3	98.6	107.6	113.1	118.1	124.1	128.3
100	67.3	70.1	74.2	77.9	82.4	90.1	99.3	109.1	118.5	124.3	129.6	135.8	140.2
<u>y                                    </u>	0.005	0.01	0.025	0.05	0.1	0.25	0.5	0.75	0.9	0.95	0.975	0.99	0.995

Samaa	<u>Fuel</u>		True density values (kg/m <sup>3</sup> ) +/- Uncertainty (k=1)								
Source			<u>#1</u>	<u>#2</u>	<u>#3</u>	#4	<u>#5</u>	<u>#6</u>	<u>#7</u>	<u>#8</u>	$\chi^2$ test
References	Glass		2432 +/- 3	2388 +/- 3	2367 +/- 3	-	-	-	-	-	FALSE
	Al <sub>2</sub> O <sub>3</sub>		3957 +/- 4	3906 +/- 4	3933 +/- 4	3953 +/- 4	-	-	-	-	TRUE
	LB 101		1759 +/- 2	1674 +/- 2	1718 +/- 2	-	-	-	-	-	FALSE
	Printex 90		1788 +/- 2	1788 +/- 2	1777 +/- 2	1815 +/- 2	1807 +/- 3	1768 +/- 2	-	-	TRUE
Samples	Printex 25		1891 +/- 2	1882 +/- 2	1849 +/- 2	1884 +/- 2	1885 +/- 2	-	-	-	TRUE
	Glas	sy C.	1382 +/- 2	1383 +/- 2	1396 +/- 2	1398 +/- 2	1415 +/- 2	1437 +/- 2	-	-	FALSE
	CAST 16.2	2% OC/TC	1526 +/- 5	1752 +/- 5	1614 +/- 3	-	-	-	-	-	FALSE
	Acetylene (C2	H <sub>2</sub> ) (BANCO)	1734 +/- 3	1704 +/- 3	-	-	-	-	-	-	FALSE
	Toluene (C7H8)	450 (BANCO)	1610 +/- 4	1419 +-/ 5	-	-	-	-	-	-	FALSE
Diffusion	Toluene (C7H8)	100 (BANCO)	1472 +/- 8	1404 +/- 5	1574 +/- 4	-	-	-	-	-	FALSE
Flame (cone	PMMA (C <sub>5</sub> H <sub>8</sub> O <sub>2</sub> ) 450 (BANCO)		1772 +/- 4	1671 +/- 4	1644 +/- 3	1616 +/- 3	1533 +/- 5	-	-	-	FALSE
calorimeter)	PMMA (C5H8O2)100 (BANCO)		1494 +/- 7	1489 +/- 5	-	-	-	-	-	-	TRUE
···· ,	2/3 PMMA + 1/3 PVC (BANCO)		1281 +/- 6	1340 +/- 8	1322 +/- 96	-	-	-	-	-	TRUE
	TBP / TPI	H (PARIS)	1495 +/- 2	1573 +/- 2	-	-	-	-	-	-	FALSE
	Electrical elements (BANCO)		1762 +/- 6	-	-	-	-	-	-	-	-
	Electrical cabinet (DIVA)		1681 +/- 2	1692 +/- 2	1644 +/- 2	-	-	-	-	-	FALSE
Real	Electrical cables (CFS)		1867 +/- 2	2050 +/- 2	2024 +/- 2	2016 +/- 2	2041 +/- 2	-	-	-	FALSE
scale	Electrical cable with PVC (CORE)		1812 +/- 6	1723 +/- 7	1760 +/- 6	1777 +/- 5	-	-	-	-	TRUE
fire	Hydraulic oil (FES)		1578 +/- 6	1382 +/- 4	1757 +/- 6	1800 +/- 6	1806 +/- 4	-	-	-	FALSE
	Gloves box (SATURNE)		1641 +/- 5	1687 +/- 2	1811 +/- 9	2006 +/- 11	1746 +/- 4	1717 +/- 3	1694 +/- 3	1688 +/- 3	FALSE
	Gloves box (DIVA)		2063 +/- 2	2032 +/- 2	2132 +/- 2	2073 +/- 2	2042 +/- 2	-	-	-	FALSE
	<u>Fuel</u>	<u>Temperature</u>							-		
	Gloves box (SATURNE)	120°C	1650 +/- 3	1582 +/- 2	1748 +/- 3	-	-	-	-	-	FALSE
		240°C	2120 +/- 4	1545 +/- 3	1636 +/- 3	-	-	-	-	-	FALSE
Temperature	Hydraulic oil	120°C	2043 +/- 4	1722 +/- 4	1628 +/- 4	-	-	-	-	-	FALSE
	(FES)	240°C	1822 +/- 4	1885 +/- 7	1462 +/- 6	1548 +/- 5	1540 +/- 5	-	-	-	FALSE
Effect	PMMA 450 (BANCO)	120°C	1630 +/- 4	1560 +/- 4	1574 +/- 12	-	-	-	-	-	TRUE
		240°C	1774 +/- 5	1507 +/- 6	1672 +/- 6	1600 +/- 5	-	-	-	-	FALSE
	Toluene 100	120°C	1381 +/- 5	1232 +/- 4	1526 +/- 4	-	-	-	-	-	FALSE
	(BANCO)	240°C	1393 +/- 4	1458 +/- 4	1493 +/- 8	-	-	-	-	-	FALSE

Annex III: raw values of sample true density measured in accordance with ISO 787-23 and results of their statistical analysis

#### Annex IV: Potential effect of organic fraction dissolution in ethanol

In order to evaluate the magnitude of this bias, we performed EC-OC measurements for samples suspected to be the most sensitive to organic fraction dissolution during centrifugation in ethanol. After this treatment, samples were then dried in a furnace at 40°C for 48 hours and EC-OC measurements were then performed. Figure A1 presents a comparison between EC-OC before and after this treatment. The influence appears to be limited for most samples and agreement between the two analyses could be reported in a 95% confidence interval of 40% of the OC/TC ratio. To take into account the potential effect of the soluble organic fraction (SOF) being dissolved in ethanol, this confidence interval for 40% has been reported in Figure 3.

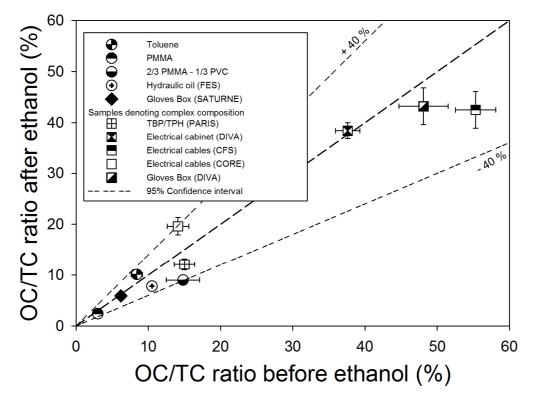
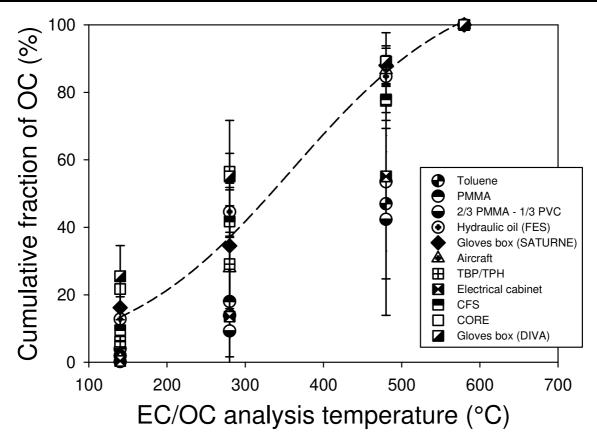


Figure A1: comparison of OC/TC ratio before and after ethanol treatment



Annex V: Evolution of the OC fraction as a function of the EC/OC analysis temperature

Figure A2: evolution of the cumulative mass fraction of OC as a function of EC/OC analysis temperature

