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Algorithms for the Sequential Reprogramming of Boolean Networks

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Abstract—Cellular reprogramming, a technique that opens huge opportunities in modern and regenerative medicine, heavily relies on identifying key genes to perturb. Most of the existing computational methods for controlling which attractor (steady state) the cell will reach focus on finding mutations to apply to the *initial* state. However, it has been shown, and is proved in this article, that *waiting* between perturbations so that the update dynamics of the system prepares the ground, allows for new reprogramming strategies. To identify such *sequential* perturbations, we consider a qualitative model of regulatory networks, and rely on Binary Decision Diagrams to model their dynamics and the putative perturbations.

Our method establishes a set identification of sequential perturbations, whether permanent (mutations) or only temporary, to achieve the existential or inevitable reachability of an arbitrary state of the system. We apply an implementation for temporary perturbations on models from the literature, illustrating that we are able to derive sequential perturbations to achieve trans-differentiation.



1 INTRODUCTION

REGENERATIVE medicine has gained traction with the discovery of cell reprogramming, a way to change a cell phenotype to another, allowing tissue or neuron regeneration techniques. After proof that cell fate decisions could be reversed [21], scientists need efficient and trustworthy methods to achieve cell reprogramming. Instead of producing induced pluripotent stem cells and force the cell to follow a distinct differentiation path, new methods focus on *trans-differentiating* the cell, without necessarily going (back) through a multipotent state [7], [6].

This paper addresses the formal prediction of perturbations for cell reprogramming from computational models of gene regulation. We consider qualitative models where the genes and/or the proteins, notably transcription factors, are variables with an assigned value giving the level of activity, e.g., 0 for inactive and 1 for active, in a Boolean abstraction. The value of each variable can then evolve in time, depending on the value of its regulators.

In qualitative models of gene regulation, *attractors* of the dynamics, which represent the long term dynamics, are typically associated with differentiated and/or stable states of the cell [14], [22]. In such a setting, cell reprogramming can be interpreted as triggering a change of attractor: starting within an initial attractor, perform perturbations which would de-stabilize the network and lead the cell to a different attractor.

Current experimental settings and computational models mainly consider cell reprogramming by applying the set of perturbations simultaneously in the initial state. However, as suggested in [18] and as we will demonstrate formally in this paper, one finds novel reprogramming strategies, potentially requiring fewer interventions and / or achieving more objectives, by using *sequential* reprogram-

ming, i.e., where perturbations are applied at particular points in time, and in a particular *ordering*.

Contribution: This paper establishes the formal characterization of all possible reprogramming paths leading from one state of an asynchronous Boolean network to another, by means of a bounded number of either permanent (mutations) or temporary perturbations. We will account for whether the target state *may* be reached, or will be reached *inevitably*.

Our method relies on the exploration of the asynchronous dynamics of a perturbed Boolean network. A general algorithm is given to explore the perturbed transition graph. In the case of temporary perturbations, binary decision diagrams are used to model both perturbations and the dynamics of the system. We apply our approach to biological networks from the literature, and show that the *sequential* application of perturbations yields new reprogramming solutions.

This article extends the conference article [12] by generalizing the algorithm, and making experimentations on bigger models thanks to a new implementation.

Outline: Sect. 2 details an example of Boolean network which motivates sequential reprogramming. Sect. 3 gives formal definitions and an algorithm relying on set operations for sequential reprogramming. Sect. 4 Explains how BDDs are used to encode the dynamics of temporary sequential perturbations and how the reprogramming paths can be extracted. Sect. 5 applies it to biological networks from the literature. Sect. 6 concludes the paper.

Notations: For (k, n) two integers such that $k < n$, the set $\{k, k + 1, \dots, n - 1, n\}$ is denoted $[k, n]$. For a given $x \in \{0, 1\}^n$ and $i \in [1, n]$, $\bar{x}^{\{i\}} \in \{0, 1\}^n$ is defined as follows:

for all $j \in [1, n]$, $\bar{x}_j^{\{i\}} \triangleq \neg x_j$ if $j = i$ and $\bar{x}_j^{\{i\}} \triangleq x_j$ if $j \neq i$.

2 BACKGROUND AND MOTIVATING EXAMPLE

This section illustrates the benefits of *sequential* vs initial-state reprogramming on a small Boolean network in order to trigger a change of attractor. We show that, in this example, initial-state programming requires at least three perturbations, whereas the sequential approach necessitates only two. But first some preliminaries.

2.1 Boolean networks

A Boolean Network (BN) is a tuple of Boolean functions giving the future value of each variable with respect to the global state of the network.

Definition 1. A Boolean Network (BN) of dimension n is a function f such that:

$$f : \{0, 1\}^n \rightarrow \{0, 1\}^n \\ x = (x_1, \dots, x_n) \mapsto f(x) = (f_1(x), \dots, f_n(x))$$

The dynamics of a Boolean network f are modelled by *transitions* between its states $x \in \{0, 1\}^n$. In the scope of this paper, we consider the *fully asynchronous semantics* of Boolean networks: a transition updates the value of only one variable $i \in [1, n]$. Notice that examples for the relevance of sequential reprogramming can easily be exhibited in the synchronous update semantics as well.

Thus, from a state $x \in \{0, 1\}^n$, there is one transition for each vertex i such that $f_i(x) \neq x_i$. The *transition graph* (Def. 2) is a digraph where vertices are all the possible states $\{0, 1\}^n$, and edges correspond to asynchronous transitions. The transition graph of a Boolean network f can be denoted as STG(f).

Definition 2 (Transition graph). *The transition graph (also known as state graph) is the graph having $\{0, 1\}^n$ as vertex set and the edges set $\{x \rightarrow \bar{x}^{\{i\}} \mid x \in \{0, 1\}^n, i \in [1, n], f_i(x) = \neg x_i\}$. A path from x to y is denoted $x \rightarrow^* y$.*

The terminal strongly connected components of the transition graph can be seen as the long-term dynamics, phenotypes or “fates” of the system; throughout, we will refer to them as *attractors*. An attractor may model a unique state, referred to as a *fixpoint*, $f(x) = x$, or sustained oscillations (*cyclic attractor*) among several states.

Definition 3 (Attractor).

$$A \subseteq \{0, 1\}^n \text{ is an attractor} \Leftrightarrow \\ A \neq \emptyset \\ \text{and } \forall x \in A, \forall y \in \{0, 1\}^n \setminus A, x \not\rightarrow^* y \\ \text{and } \forall x, y \in A, x \rightarrow^* y$$

If $|A| = 1$ then A is a fixpoint. Otherwise, A is a cyclic attractor.

Let $\mathcal{A}(f)$ be the set of all attractors of the BN f .

The transition relation can be viewed as a Boolean function $T : 2^{2^n} \rightarrow \{0, 1\}$, where values 1 and 0 indicate a valid and an invalid transition, respectively.

The computation of the predecessors and successors utilize two basic functions: $Preimage(X, T) = \{s' \in \mathcal{S} \mid \exists s \in X \text{ such that } (s', s) \in T\}$, which returns the direct predecessors of X in T , i.e. $pre(X)$; $Image(X, T) = \{s' \in \mathcal{S} \mid \exists s \in X \text{ such that } (s, s') \in T\}$, which returns the direct successors of $X \subseteq \mathcal{S}$ in T , i.e. $post(X)$. To simplify the presentation, we define $Preimage^i(X, T) = \underbrace{Preimage(\dots(Preimage(X, T)))}_i$ with $Preimage^0(X, T) =$

X and $Image^i(X, T) = \underbrace{Image(\dots(Image(X, T)))}_i$ with

$Image^0(X, T) = X$. In this way, the set of all predecessors of X via transitions in T is defined as an iterative procedure $pre^*(X) = \bigcup_{i=0}^n Preimage^n(X, T)$ such that $Preimage^n(X, T) = Preimage^{n+1}(X, T)$. Similarly, the set of all successors of X via transitions in T is defined as an iterative procedure $post^*(X) = \bigcup_{i=0}^n Image^n(X, T)$ such that $Image^n(X, T) = Image^{n+1}(X, T)$.

The (strong) basin of X is the set of states that always eventually reach a state in X . It should be noted that X can be any set of states, not necessarily an attractor.

Definition 4 (Basin). *Let X be a set of nodes. The basin of X is the biggest set Y such that $X \subseteq Y$ and $\forall y \in Y \setminus X, post(y) \subseteq Y \wedge \exists x \in X, y \rightarrow^* x$.*

Basins are usually related to attractors, and are particularly interesting in this case: the basin of an attractor is the set of all states that will end up in the attractor. In most cases, the target of a reprogramming is an attractor, as explained in Sect. 1.

2.2 The advantage of sequential reprogramming

By taking advantage of the natural dynamics of the system, sequential reprogramming can provide additional strategies which may require fewer perturbations than with the initial state only reprogramming.

Let us consider the following BN

$$f_1(x) = x_1 \qquad f_2(x) = x_2 \\ f_3(x) = x_1 \wedge \neg x_2 \qquad f_4(x) = x_3 \vee x_4$$

Fig. 1 gives the transition graph of this BN, and the different perturbation techniques. To understand the benefit of sequential perturbations, let us consider the fixpoint 0000 as starting point and fixpoint 1101 as target.

Obviously, because 0000 is a fixpoint, there can be no sequence of updates from 0000 to 1101. It can also be seen that if one or two vertices are perturbed *at the same time*, by giving them new values, 1101 is not reachable, as shown in Fig. 1(top). However, if two vertices are perturbed, but the system is allowed to follow its own dynamics between the changes, 1101 can be reached, as shown in Fig. 1(bottom), by using the path $0000 \xrightarrow{x_1=1} 1000 \rightarrow 1010 \rightarrow 1011 \xrightarrow{x_2=1} 1111 \rightarrow 1101$, i.e. we first force the activation of the first variable, then wait until the system reaches (by its own dynamics) the state 1011 before activating variable 2. From the perturbed state, the system is guaranteed to end up in the desired fixpoint, 1101.

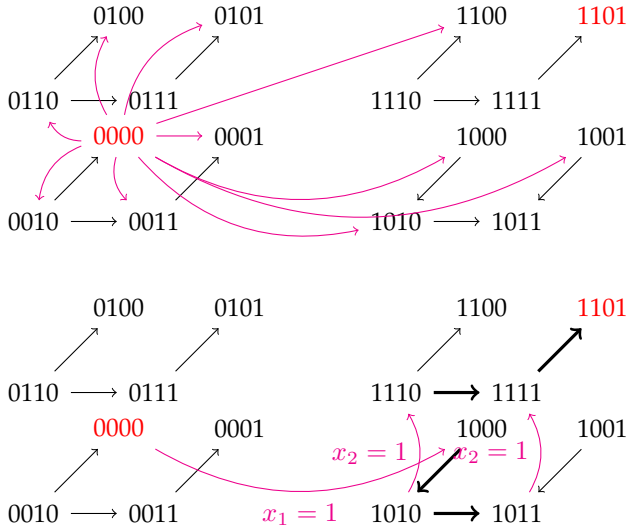


Fig. 1: Transition graph of f and candidate perturbations (magenta) for the reprogramming from 0000 to 1101: (top) none of candidate perturbations of one or two variables in the initial state allow to reach 1101; (bottom) sequences of two sequential perturbations allow to reach 1101.

In this case and almost every other case of sequential reprogramming, the ordering of perturbations is crucial. For example, if the perturbations were done in a different order in this example, the first perturbation to be made would be $x_2 = 1$, then only 0100 would be reachable. From this state, perturbing with $x_1 = 1$ allows 1100 to be reachable, and it is the only attractor reachable. 1101 is still unreachable, meaning the perturbations failed to make the target reachable.

Inevitable and existential reprogramming

This example shows that some otherwise unattainable attractors may be reached when the changes of values of vertices are coordinated in a particular order, and using the transient dynamics between perturbations. We remark that there exists another reprogramming path, where variable 2 is perturbed when the system reaches 1010. Note that, in this case, after the second perturbation, the system can reach 1101, but it is not guaranteed. We say that, in the first reprogramming path, the reprogramming is *inevitable*, whereas it is only *existential* in the second case.

Permanent and temporary perturbations

We also have to consider the sequential characteristics of how *individual* perturbations act. The system may either only be temporarily perturbed, by changing the value of a vertex i for a time (setting i to 0 or 1), or the change can be permanent, i.e. a modification of the *update function* of the vertex (setting f_i to 0 or 1). On our example, making permanent changes would yield the solutions given above. However, if the initial state is 1011 and the target state is 1100, then it has different solutions (Fig. 2).

Indeed, if the objective is to go from 1011 to 1100 in the same transition graph using only permanent perturbations, then their order does not matter. Perturbing x_2 and x_4 from

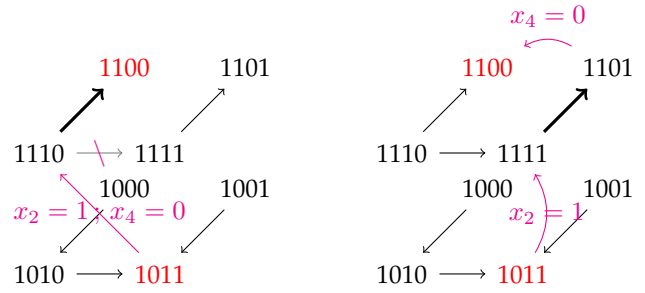


Fig. 2: Right part of the transition graph of f from initial state 1011 to 1100, with permanent perturbations (left) and temporary ones (right).

the initial state is enough to make 1100 the only reachable state. On the other hand, if the perturbations are temporary, x_2 has to be perturbed first, then when 1101 is reached, x_4 can be perturbed. If this order is not followed, 1101 is reachable as well as 1100.

In most cases, the perturbations done in permanent reprogramming and the ones done in temporary reprogramming can be on different variables.

3 CHARACTERIZATIONS OF REPROGRAMMING STRATEGIES

This section brings a formal definition of dynamical models adding perturbations to BN dynamics, and the characterization of sequential reprogramming. It also explains an algorithm to find all inevitable reprogramming solutions, given a maximum number of perturbations k , and applies the algorithm to the example from Sect. 2.

3.1 Perturbed model

Given a BN, perturbations can be added by allowing the variables to change value (temporary or permanently). We introduce the notion of *Perturbed Transition Graph* (Def. 5) which encompasses the transitions allowed by the BN and transitions due to perturbations. Moreover, a variable v_k tracks the number of applied perturbations. It should be noted that how the perturbations are made, which variables can be perturbed, and other details are all part of the model. The model is an input from the user, and should conform to the following definition in order for the properties and algorithm to work on it. An example of perturbed transition graph to model temporary perturbations is given in Sect. 4.

Definition 5 (Perturbed Transition Graph). *Given a BN f of dimension n , its transition graph $STG(f)=(\mathcal{S}, \mathcal{E}_f)$, and a maximum number of allowed perturbations k , the Perturbed Transition Graph \mathcal{G} is a pair $(\mathcal{S}_p, \mathcal{E}_p)$ where*

- $\mathcal{S}_p = \mathcal{S} \times [0, k]$ is the set of states, \mathcal{S} is the set of states of the transition graph with states possibly added to account for the perturbations, times a perturbation counter v_k ranging from 0 to k ;
- $\mathcal{E}_p \subseteq \{(s, i) \rightarrow (s', i) \mid i \in [0, k], (s \rightarrow s') \in \mathcal{E}_f\} \cup \{(s, i) \rightarrow (s', i+1) \mid i \in [0, k-1], s, s' \in \mathcal{S}\}$, is the set of transitions, which accounts both for a subset of

asynchronous transitions of $STG(f)$ and for perturbations (which increase the perturbation counter by one).

Graph layers and layer subsets

The transition graph can be layered by regrouping all states having the same perturbation count in the same layer. Let $\mathcal{N}_j = V_p \times \{j\}$ be the set of all states in layer j . A subset $A \subseteq \mathcal{S}_p$ restricted to a layer j is denoted $A_j := A \cap \mathcal{N}_j$. A subset $A \subseteq V_p$ of $STG(f)$ times a layer j is $A_j := A \times \{j\}$.

Property 1. Given a Perturbed Transition Graph \mathcal{G} of a BN f with temporary perturbations, for all $i \leq k$, the subgraph \mathcal{N}_i of \mathcal{G} is isomorphic to $STG(f)$, the original network's transition graph.

Property 2. If $i > j$, then $(s, j) \in \mathcal{S}_p$ cannot be reached from $(s', i) \in \mathcal{S}_p$, regardless of s and s' . That is, the perturbation counter can only increase.

From the definition of basin (Def. 4), the basin of a set of nodes X restricted to a layer considers only the transitions in the layer.

Definition 6 (Basin restricted to a layer). The basin of X restricted to a layer j , denoted by $bas_j(X)$, is the biggest set Y such that $X \subseteq Y \subseteq \mathcal{N}_j$ and $\forall y \in Y \setminus X, (post(y) \cap \mathcal{N}_j) \subseteq Y \wedge \exists x \in X, y \rightarrow^* x$.

3.2 Set characterization of inevitable reprogramming

Given a Perturbed Transition Graph $(\mathcal{S}_p, \mathcal{E}_p)$ of a BN f with a maximum number of perturbations k (temporary or permanent), let $\phi \subseteq \mathcal{S}$ be a set of states of the original $STG(f)$. States in ϕ are the targets of the inevitable reprogramming. \mathcal{W} is the solution set, the set of all states that have inevitable reprogramming from them to one of the target states.

As a reminder, ϕ_j is the set of states in ϕ in $STG(f)$ which are in layer j in the perturbed transition graph.

In order to compute \mathcal{W} , two other sets ψ_j and W_j for each layer are computed. ψ_j is the set of states in layer j that need to be reached in order to reach one of the target states in ϕ . Thus, ψ_j contains states of ϕ_j and states allowing one or multiple perturbations to a lower layer, where ϕ can be reached. W_j is the basin, restricted to the layer j , of ψ_j . Hence, W_j is the set of states, in layer j , that reach one of the states in ϕ , whether the state is in layer j or not.

The sets ψ_j and W_j are defined as follows:

$$\psi_k = \{x \mid x \in \mathcal{N}_k \wedge x \in \phi_k\}$$

$$W_k = bas_k(\psi_k)$$

For j between $k-1$ and 0 :

$$\psi_j = \{x \mid x \in \mathcal{N}_j \wedge (x \in \phi_j \vee x \in pre(W_{j+1}))\}$$

$$W_j = bas_j(\psi_j)$$

Since ψ_k exists and is defined, all ψ_j and W_j are defined.

The set describing the solution is $\mathcal{W} = \bigcup_{j \in [1, k]} W_j$.

If the initial state s_0 is in \mathcal{W} , then there exist inevitable reprogramming solutions, and all reprogramming solutions are in \mathcal{W} .

Property 3. By construction, the set of all attractors reachable in the graph restricted to \mathcal{W} is a subset of $\phi \times [0, k]$.

Algorithm using the state set characterization

Algorithm 1 is given in pseudo-code using the set characterization explained previously. The notations are

the same. A loop invariant is that \mathcal{W} corresponds to the set of states from layer j to layer k that have inevitable reprogramming to a state in ϕ .

The inputs of the algorithm are a Perturbed Transition Graph $(\mathcal{S}_p, \mathcal{E}_p)$, a set of states ϕ , an initial state s_0 , and the maximal number of perturbations, k .

The first step is to set W_{k+1} to the empty set, as there are no states in layer $k+1$ (line 2), and \mathcal{W} is the set of all possible solutions, hence $\mathcal{W} = \emptyset$ at the beginning.

Then, for each layer j , ψ_j has to be computed. ψ_j is the set of states either in ϕ_j or being direct predecessors of the solution states of the lower layer, the layer $j+1$. The basin of ψ_j is then computed. These states are the solution states of layer j , and are added to the set of all solution states, \mathcal{W} .

When the computation has reached the first layer, either the initial state is not among the solution states, in which case there is no solution for this reprogramming (line 7), or, if $s_0 \in W_0$, then the set of states containing all inevitable reprogramming paths is returned (line 9).

Algorithm 1 Inevitable Reprogramming relying on the Set Characterization

```

1: function REPROGRAMMING( $\mathcal{G}, \phi, s_0, k$ )
2:    $W_{k+1} = \emptyset$ .
3:    $\mathcal{W} = \emptyset$ 
4:   for  $j = k$  to  $0$  do
5:      $\psi_j = \{x \in \mathcal{N}_j \mid x \in \phi_j \vee x \in pre(W_{j+1})\}$ 
6:      $W_j = bas_j(\psi_j)$ 
7:      $\mathcal{W} = \mathcal{W} \cup W_j$ 
8:   if  $s_0 \notin W_0$  then
9:     Return  $\emptyset$ 
10:  else
11:    Return  $\mathcal{W}$ 

```

One could be surprised by the definition of ψ_j : in W_j , we use the basin of ψ_j , where the system will always reach one of the state in ψ_j , and on the other hand, in ψ_j , only the preimage of W_{j+1} is used. However, in this case, we want to control the system, meaning the perturbations are chosen by the controller. As a consequence, the controller only needs to choose one perturbation among all possible ones in order to reach W_{j+1} .

Complexity

Given a transition graph G from a network with n variables, and the possibility of doing up to k perturbations, $k \times m$ can be defined as the number of states of G , with $m = O(e^n)$.

Since the algorithm relies on the exploration of subparts of the graph, and the distance between basins of attraction and other layers, the complexity, both in space and time, will vastly depend on the graph properties.

In the worst case, all $\ln(m)$ perturbations from a state in ψ_j have to be explored, and all $k \times m$ states are in different ψ_j . Hence, the worst time complexity is in $O(k \times m \times \ln(m))$, or, if we use the size of the network as the entry, $O(k \times n \times e^n)$.

As for space complexity, the algorithm returns \mathcal{W} , which is the set of explored states mentioned for time complexity, giving the same complexity.

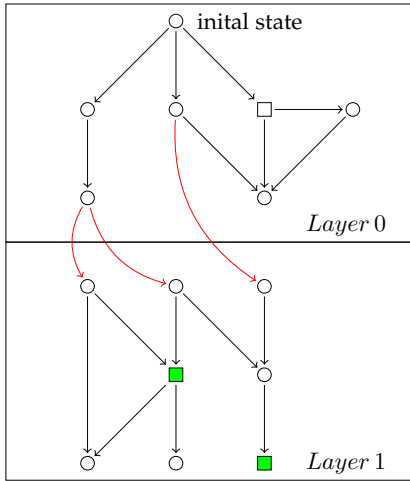


Fig. 3: Computing ψ_1 , in green.

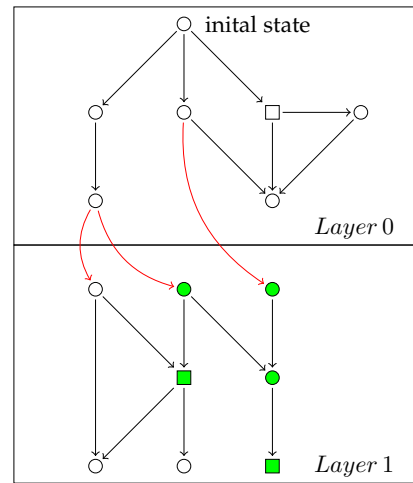


Fig. 4: Computing $W_1 = \text{bas}(\psi_1)$, in green.

However, these worst cases happen only if there are only perturbations in the transition graph, meaning there is no inherent dynamics to the model. Typical cases would have a lower time and space complexity.

Visual explanation of the set algorithm

Figures 3 to 7 show an example of the algorithm applied to a transition graph, with the states in ϕ marked as squares, and perturbation transitions in red. In this example, there are only two layers. Note that each layer of the transition graph should always be the same that layer 0, except for some transitions removed in the case of permanent or durable¹ perturbations. Here the two layers are different, it could be a different part of the original transition graph.

Figures 3 and 4 represent the first iteration of the **for** loop, respectively computing ψ_1 and then its basin to have the solution states in the layer 1: $W_1 = \text{bas}(\psi_1)$.

The next two figures, 5 and 6, represent the second iteration of the **for** loop, computing (in green) ψ_0 , by using some states in W_1 (in blue), and then computing $W_0 = \text{bas}(\psi_0)$.

Figure 7 represents the last step of the algorithm: since the initial state is in W_0 , the different perturbations to reach ϕ are computed.

The algorithm then returns \mathcal{W} , the set of states in green in figure 7. From this set, the perturbations can be extracted using the perturbation counter and by comparing the states. An example on how to do so is given in Sect. 4.

Existential Reprogramming

The algorithm and experiments focus on inevitable reprogramming as it is the most relevant for applications in cellular reprogramming. However, existential reprogramming can be easily achieved with the same algorithm by changing $\text{bas}_j(X)$ to $\text{pre}_j^*(X)$ on line 6.

As a reminder, in Sect. 2 the definition for $\text{pre}_j^*(X)$ is the set of states that can lead to X . This set can then be restricted to states only being in layer j .

Existential Reprogramming is the existence of a path to the

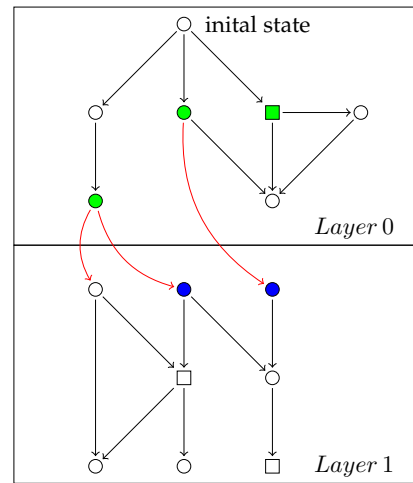


Fig. 5: In green, ψ_0 in the layer 0, and in blue the successors in W_1 .

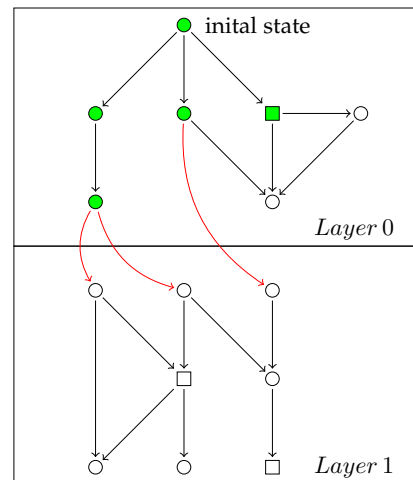


Fig. 6: Computing in green $W_0 = \text{bas}(\psi_0)$.

1. One could imagine a model where perturbations change the functions of the graph for a given time. In this case, the model and hence the perturbed transition graph are changed.

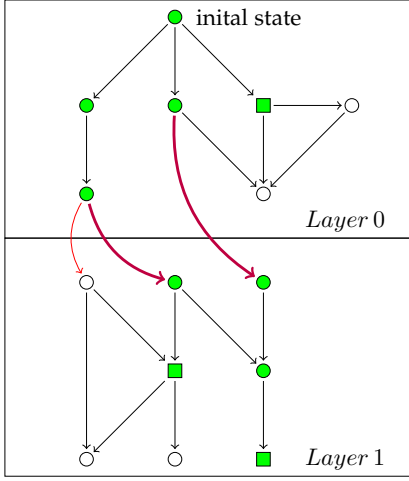


Fig. 7: Marking in green \mathcal{W} , and in purple the perturbations possible.

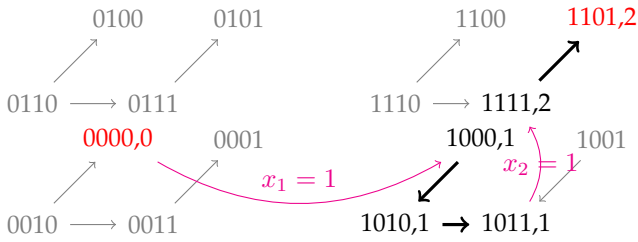


Fig. 8: The perturbation path returned by the algorithm on the example of Sect. 2.

solution. By using the set of predecessors instead of the basin, the algorithm no longer guarantees the reprogramming, but still guarantees the target to be reachable with the perturbations returned.

3.3 Example

Applied on the example of Sect. 2 for the inevitable reprogramming from 0000 to 1101 with $k = 2$, \mathcal{W} is the set of highlighted states, meaning all states not in gray in Fig. 8, and the algorithm returns $(x_1 = 1, x_2 = 1)$ as the only solution. The perturbation count is the number after the comma in the state.

The sequential reprogramming path identified in Sect. 2 is the only strategy for inevitable reprogramming.

A more complete explanation is given in sub-sect. 4.3, with the implemented version of the algorithm.

4 COMPUTATION OF THE TEMPORARY SEQUENTIAL REPROGRAMMING PATHS

In Sect. 3, we have introduced a general algorithm to compute all the inevitable reprogramming solutions for the temporary and the permanent sequential control. In this section, we focus on the temporary sequential control, and we propose an algorithm to find the minimal number of perturbations and the associated reprogramming paths.

4.1 Encoding BNs with temporary perturbations in BDDs

Binary decision diagrams (BDDs) were introduced by Lee in [10] and Akers in [2] to represent Boolean functions [10], [2]. BDDs have the advantage of memory efficiency and have been applied in many model checking algorithms to alleviate the state space explosion problem.

A BN with temporary perturbations, denoted as $G(V_p, f_p)$ is constructed by adding a variable v_k to V , whose value denotes the number of perturbations, and adding functions to f to enable the perturbations of the variables V . These functions allow any variable to change value at the cost of increasing the perturbation counter v_k . It can be modeled as a perturbed transition graph $\mathcal{G}(\mathcal{S}_p, \mathcal{E}_p)$ as described in Sect. 3, which can then be encoded in a BDD. Each variable in V_p can be represented by a BDD variable. Specifically, the Boolean variables $V \in V_p$ are binary BDD variables and the perturbation counter v_k is a bounded integer variable, whose value is in $[0, k]$. By slight abuse of notation, we also use V_p to denote the set of BDD variables. In order to encode the transition relations, another set V'_p of BDD variables, which is a copy of V_p , is introduced: V_p encodes the possible current states, i.e., $\mathbf{x}(t)$, and V'_p encodes the possible next states, i.e., $\mathbf{x}(t+1)$.

4.2 Method for the computation of the temporary sequential reprogramming paths

In Sect. 3, we described Algorithm 1 to compute inevitable reprogramming solutions with k perturbations. In this section, we modify Algorithm 1 to derive a method to compute the minimal number of perturbations and the corresponding inevitable temporary reprogramming paths in Algorithm 2. As mentioned in Sect. 4.1, we encode BNs with perturbations in BDDs, hence most operations of the algorithm are performed with BDDs. This algorithm takes a BN with perturbations \mathcal{G} , the maximal number of perturbations allowed k , a source attractor A^s and a target attractor A^t as inputs. Note that A^t is an attractor of the original $STG(f)$ and does not contain the value of the perturbation counter. If there exist temporary reprogramming paths within k perturbations, the minimal number of perturbations p_{min} and all inevitable temporary reprogramming paths ρ will be returned as outputs.

We first compute the corresponding set of states of the target attractor A^t in the perturbed transition graph at each layer i , $i \in [0, k]$ as line 3. We cycle through lines 4–15 to compute the minimal number of perturbations p_{min} and the corresponding reprogramming paths ρ . Let m denote the number of perturbations. Starting from $m = 0$, we gradually increase m by 1 until we find a solution or m is greater than k . For each m , we compute two sets \mathcal{W} and \mathcal{P} according to lines 6–9. W_m is the basin of the projection of the target attractor at layer m (line 6). $P_i, i \in [0, m-1]$ stores the direct predecessors of W_{i+1} at layer i and $W_i, i \in [0, m-1]$ is the basin of P_i at layer i . The basin is computed using the fixed point computation of strong basins in [16]. In this way, any state $s, s \in P_i$ can reach a state $s', s' \in W_{i+1}$ with one perturbation and any state $s, s \in (W_i \setminus P_i)$ can reach a state $s', s' \in P_i$ spontaneously.

Algorithm 2 Temporary sequential reprogramming of BNs

```

1: procedure COMPUTATION_OF_SEQUENTIAL_REPROGRAMMING_PATHS( $\mathcal{G}, A^s, A^t, k$ )
2:   Initialize the minimal number of perturbation  $p_{min} = 0, flag = False$ ;
3:   Compute the corresponding set of states of  $A$  at each layer  $i, i \in [0, k]$ , denoted as  $\{A_0^t, A_1^t, \dots, A_k^t\}$ .
4:   for  $m = 0; m \leq k; m++$  do
5:     Initialize  $\mathcal{W} = \{W_0, W_1, \dots, W_m\}, \mathcal{P} = \{P_0, P_1, \dots, P_{m-1}\}$ ;
6:      $W_m = bas_m(A_m^t)$ 
7:     for  $z = m - 1; z \geq 0; z--$  do
8:        $P_z = pre(W_{z+1}) \cap \mathcal{N}_z$ 
9:        $W_z = bas_z(P_z) \cap \mathcal{N}_z$  // local basin of  $P_z$  at layer  $z$ 
10:    if  $A^s \subseteq W_0$  then
11:       $p_{min} = m, flag = True$ 
12:      Initialize a vector  $\rho$  to store the paths.
13:       $\rho = COMPUTE\_PATHS(1, A^s, \rho, \mathcal{W}, \mathcal{P})$ ; // Algorithm 3
14:       $TS_\rho = EXTRACT\_PATHS(\rho, TS)$ .
15:      break;
16:    if  $flag == False$  then
17:      There is no temporary sequential reprogramming paths within  $k$  perturbations.

```

Algorithm 3 Helper functions

```

1: procedure COMPUTE_PATHS( $z, T_{z-1}, \rho, \mathcal{W}, \mathcal{P}$ )
2:    $S_z = post^*(T_{z-1}) \cap P_{z-1}$ ;
3:    $T_z = post(I_z) \cap W_z$ ;
4:   Insert  $(S_z, T_z)$  to  $\rho$ .
5:   if  $z < \mathcal{W}.size()$  then
6:      $\rho = COMPUTE\_PATHS(z + 1, T_z, \rho, \mathcal{W}, \mathcal{P})$ 
7:   return  $\rho$ 
8: procedure EXTRACT_PATHS( $\rho, TS$ )
9:   Initialize a BDD  $TS_\rho$ 
10:  for  $(S_z, T_z) \in \rho, z \in [1, m]$  do
11:    Add the transition relation from any state  $s$  in  $S_z$ 
    to any state  $t$  in  $T_z$  to  $TS_\rho$ .
     $TS_\rho = TS_\rho \wedge TS$ 
12:  return  $TS_\rho$ 

```

For the two loops, an invariant is that m is the maximum number of perturbations for a minimal solution. The first loop stops when such a m is found, and the fact that W is the set of states that have an inevitable reprogramming solution to A , as in Algorithm 1.

There exist reprogramming paths with m perturbations if and only if $A^s \subseteq W_0$. If so, the minimum number of perturbations required is m and the reprogramming paths ρ can be computed with Procedure “COMPUTE_PATHS” in Algorithm 3. We start with A^s and by iteratively performing lines 2-4 of Algorithm 3, we can identify all the paths ρ from s to A with m perturbations. ρ stores a list of tuples $\{(S_1, T_1), (S_2, T_2), \dots, (S_m, T_m)\}$. S_1 is a set of states at layer 0, that can be reached by the source state s_0 spontaneously. With one perturbation, any state $s_1, s_1 \in S_1$ can reach a state $t_1, t_1 \in T_1$, and t_1 can always reach a state $s_2, s_2 \in S_2$. With the co-action of the spontaneous evolutions of BNs and m perturbations, the network will eventually reach A^t .

However, S_z and $T_z, z \in [1, m]$ are two sets of states, for any state $s_z \in S_z$, its successors $post(s_z)$ are a subset of T_z and this information is missing in ρ . In order to identify the

reprogramming determinants, we extracted the transition relations of the reprogramming paths TS_ρ from the transition system TS using Procedure “EXTRACT_PATHS”.

Due to the utilization of the spontaneous evolutions of BNs, this method requires a full observation of the transition system to identify which path the system follows.

Existential Reprogramming

As for Algorithm 1, Existential Reprogramming can be achieved easily by replacing $bas_z(X)$ by $pre_z^*(X)$ in Algorithm 2.

4.3 Example

For the example in Sect. 2, we compute all the minimal inevitable sequential reprogramming paths from 0000 to 1101 with Algorithm 2. We cycle through lines 4-15 and increase the number of perturbations m from 0 to k until we find a solution. Fig. 9 shows the computation process when $m = 2$. For every state, the number after the comma is the perturbation count. We first compute \mathcal{W} and \mathcal{P} according to lines 6-9. At layer 2, W_2 (green and red states) is the basin of the projection of the target at that layer, 1101.2. At layer 1, P_1 (green states) represents the predecessors of W_2 , from which, by applying one perturbation, we can reach each one of the states in W_2 . And W_1 (green and blue states) is the basin of P_1 at layer 1. Similarly, P_0 represents the predecessors of W_1 and W_0 is the basin of P_0 at layer 0. For this example, P_0 and W_0 are the same, and they include green and red states at layer 0. Since the source state 0000,0 is in W_0 , the minimal number of perturbation required is 2.

We compute the reprogramming paths by iteratively applying the procedure COMPUTE_PATHS. The intersection $S_1 = \{0000,0\}$ of P_0 with the successors of the source state 0000,0 at layer 0, is the set of states from which we can apply one perturbation to reach a subset $T_1 = \{1000,1\}$ of W_1 . The intersection $S_2 = \{1011,1\}$ of P_1 with the successors of T_1 at layer 1, is the set of states from which we apply the second perturbation to reach a subset $T_2 = \{1111,2\}$ of W_2 . Thus, the reprogramming paths are $\rho =$

$\{(S_1:\{0000,1\}, T_1:\{1000,1\}), (S_2:\{1011,1\}, T_2:\{1111,2\})\}$.
 For this example, there is only one path and the reprogramming determinants are x_1 and x_2 . The whole control process will be $s_0 \rightarrow S_1 \xrightarrow{x_1=1} T_1 \rightarrow S_2 \xrightarrow{x_2=1} T_2 \rightarrow A_2$.

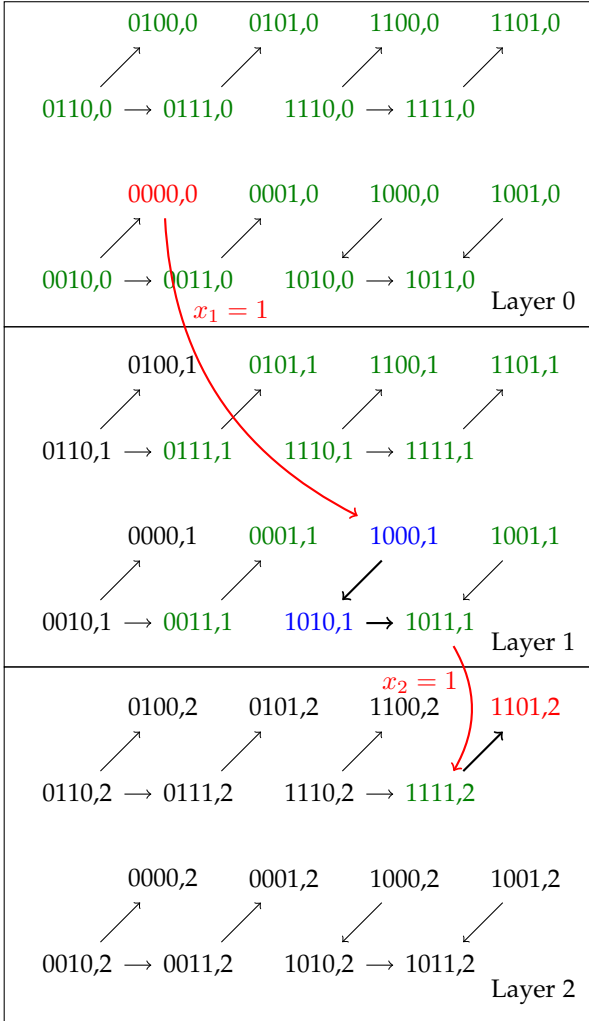


Fig. 9: Computation of reprogramming paths of the example of Sect. 2 with Algorithm 2.

5 CASE STUDIES

To demonstrate the efficiency and effectiveness of the temporary sequential control method, we apply it to three real-life biological networks. The method is implemented in ASSA-PBN[13], based on the model checker MCMAS [11] to encode BNs into BDDs. All the experiments are performed on a computer (MacBook Pro), which has a CPU of Intel Core i7 @3.1 GHz and 8 GB of DDR3 RAM. Program executables and model files are provided as supplementary material. We first describe the three biological networks.

The cardiac gene regulatory network is constructed for the early cardiac gene regulatory network of the mouse, including the core genes required for the cardiac development and the FHF/SHF determination [9]. This network has 15 variables and 6 single-state attractors.

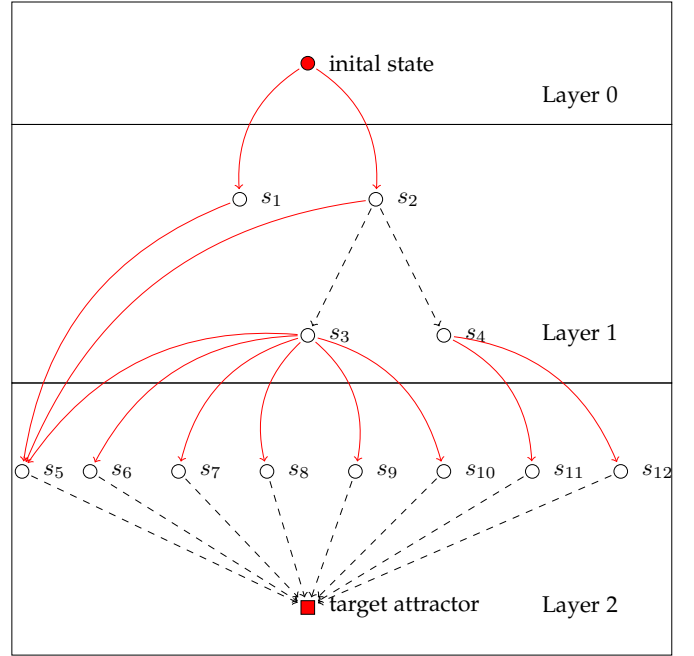


Fig. 10: Reprogramming paths from attractor A_2 to attractor A_5 for the cardiac network.

The PC12 cell differentiation network is a comprehensive model used to clarify the cellular decisions towards proliferation or differentiation [15]. It shows the interactions between protein signalling, transcription factor activity and gene regulatory feedback in the regulation of PC12 cell differentiation after the stimulation of NGF. This network consists of 32 variables and has 7 single-state attractors.

The bladder network is designed for studying patterns and conceiving counter-intuitive observations, which allow us to formulate predictions about conditions where combining genetic alterations benefits tumorigenesis [17]. This network consists of 35 variables. It has 5 single-state attractors and 3 cyclic attractors.

We choose two different attractors as the source and target attractors. For each pair of the source and target attractors, we compute the minimal number of perturbations and all inevitable reprogramming paths for the sequential control.

Table 1, 2 and 3 give the minimal number of perturbations for the initial reprogramming [16] and the sequential control on three networks for all combinations of the source and the target attractors. It is obvious that the sequential control always outperforms the initial reprogramming in terms of the number of perturbations. This is due to the fact that the initial reprogramming performs all the perturbations at once [16], while our sequential control takes advantage of the spontaneous evolutions of the networks, which helps to drive the network towards the desired target.

We compute all possible inevitable paths for every pair of the source and the target attractors. Figure 10 describes the reprogramming paths from attractor A_2 to attractor A_5 for the cardiac network. It is also a partial transition system of the cardiac network with perturbations. The red arrows represent perturbations and the dashed arrows represent

| \mathcal{A} | A_1 | | A_2 | | A_3 | | A_4 | | A_5 | | A_6 | |
|---------------|-------|-----|-------|-----|-------|-----|-------|-----|-------|-----|-------|-----|
| | sim | seq | sim | seq | sim | seq | sim | seq | sim | seq | sim | seq |
| A_1 | 0 | 0 | 7 | 3 | 4 | 2 | 1 | 1 | 8 | 4 | 6 | 3 |
| A_2 | 2 | 2 | 0 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 4 | 3 |
| A_3 | 1 | 1 | 1 | 1 | 0 | 0 | 2 | 2 | 4 | 3 | 3 | 3 |
| A_4 | 1 | 1 | 6 | 2 | 6 | 3 | 0 | 0 | 8 | 3 | 9 | 4 |
| A_5 | 2 | 2 | 1 | 1 | 2 | 2 | 1 | 1 | 0 | 0 | 1 | 1 |
| A_6 | 1 | 1 | 2 | 2 | 1 | 1 | 2 | 2 | 1 | 1 | 0 | 0 |

TABLE 1: The minimal number of perturbations for the initial reprogramming and the sequential control on the cardiac network.

| \mathcal{A} | A_1 | | A_2 | | A_3 | | A_4 | | A_5 | | A_6 | | A_7 | |
|---------------|-------|-----|-------|-----|-------|-----|-------|-----|-------|-----|-------|-----|-------|-----|
| | sim | seq | sim | seq | sim | seq | sim | seq | sim | seq | sim | seq | sim | seq |
| A_1 | 0 | 0 | 1 | 1 | 10 | 2 | 1 | 1 | 11 | 3 | 2 | 2 | 1 | 1 |
| A_2 | 9 | 8 | 0 | 0 | 1 | 1 | 10 | 9 | 3 | 2 | 11 | 10 | 10 | 9 |
| A_3 | 7 | 7 | 1 | 1 | 0 | 0 | 8 | 8 | 1 | 1 | 9 | 9 | 8 | 8 |
| A_4 | 1 | 1 | 1 | 1 | 10 | 2 | 0 | 0 | 11 | 3 | 1 | 1 | 2 | 2 |
| A_5 | 8 | 8 | 1 | 1 | 1 | 1 | 9 | 9 | 0 | 0 | 8 | 8 | 7 | 7 |
| A_6 | 2 | 2 | 1 | 1 | 11 | 2 | 1 | 1 | 10 | 3 | 0 | 0 | 1 | 1 |
| A_7 | 1 | 1 | 1 | 1 | 11 | 2 | 2 | 2 | 10 | 3 | 1 | 1 | 0 | 0 |

TABLE 2: The minimal number of perturbations for the initial reprogramming and the sequential control on the PC12 cell network.

| \mathcal{A} | A_1 | | A_2 | | A_3 | | A_4 | | A_5 | | A_6 | | A_7 | | A_8 | |
|---------------|-------|-----|-------|-----|-------|-----|-------|-----|-------|-----|-------|-----|-------|-----|-------|-----|
| | sim | seq | sim | seq | sim | seq | sim | seq | sim | seq | sim | seq | sim | seq | sim | seq |
| A_1 | 0 | 0 | 1 | 1 | 1 | 1 | 3 | 3 | 2 | 2 | 2 | 2 | 7 | 4 | 13 | 4 |
| A_2 | 1 | 1 | 0 | 0 | 2 | 2 | 8 | 4 | 1 | 1 | 9 | 3 | 10 | 3 | 8 | 3 |
| A_3 | 1 | 1 | 2 | 2 | 0 | 0 | 2 | 2 | 1 | 1 | 3 | 3 | 3 | 3 | 7 | 3 |
| A_4 | 3 | 3 | 2 | 2 | 2 | 2 | 0 | 0 | 3 | 3 | 1 | 1 | 1 | 1 | 9 | 3 |
| A_5 | 2 | 2 | 1 | 1 | 1 | 1 | 3 | 3 | 0 | 0 | 8 | 4 | 2 | 2 | 4 | 2 |
| A_6 | 2 | 2 | 1 | 1 | 3 | 3 | 1 | 1 | 4 | 2 | 0 | 0 | 6 | 2 | 14 | 4 |
| A_7 | 4 | 2 | 1 | 1 | 3 | 3 | 1 | 1 | 2 | 2 | 6 | 2 | 0 | 0 | 6 | 2 |
| A_8 | 2 | 2 | 1 | 1 | 1 | 1 | 6 | 3 | 2 | 2 | 12 | 4 | 5 | 4 | 0 | 0 |

TABLE 3: The minimal number of perturbations for the initial reprogramming and the sequential control on the bladder network.

| $T(s)$ | A_1 | A_2 | A_3 | A_4 | A_5 | A_6 |
|--------|-------|-------|-------|-------|-------|-------|
| A_1 | 0 | 0.115 | 0.082 | 0.007 | 0.186 | 0.171 |
| A_2 | 0.013 | 0 | 0.045 | 0.006 | 0.1 | 0.166 |
| A_3 | 0.005 | 0.045 | 0 | 0.012 | 0.133 | 0.196 |
| A_4 | 0.007 | 0.069 | 0.099 | 0 | 0.134 | 0.228 |
| A_5 | 0.011 | 0.044 | 0.072 | 0.006 | 0 | 0.043 |
| A_6 | 0.007 | 0.069 | 0.067 | 0.012 | 0.063 | 0 |

TABLE 4: The time costs of the sequential control on the cardiac network.

| $T(s)$ | A_1 | A_2 | A_3 | A_4 | A_5 | A_6 | A_7 |
|--------|-------|-------|-------|-------|-------|-------|-------|
| A_1 | 0 | 0.188 | 0.463 | 0.479 | 0.458 | 0.473 | 0.486 |
| A_2 | 3.509 | 0 | 0.446 | 3.803 | 0.254 | 2.676 | 4.358 |
| A_3 | 2.906 | 0.185 | 0 | 3.843 | 0.21 | 2.86 | 3.597 |
| A_4 | 0.833 | 0.188 | 0.467 | 0 | 0.457 | 0.399 | 0.519 |
| A_5 | 3.589 | 0.183 | 0.4 | 5.792 | 0 | 3.473 | 3.229 |
| A_6 | 0.946 | 0.188 | 0.453 | 0.485 | 0.542 | 0 | 0.43 |
| A_7 | 1.183 | 0.189 | 0.453 | 0.601 | 0.545 | 0.388 | 0 |

TABLE 5: The time costs of the sequential control on the PC12 cell network.

| $T(s)$ | A_1 | A_2 | A_3 | A_4 | A_5 | A_6 | A_7 | A_8 |
|--------|-------|-------|-------|--------|--------|--------|-------|-------|
| A_1 | 0 | 1.037 | 3.909 | 2.984 | 15.547 | 3.519 | 7.318 | 5.991 |
| A_2 | 3.37 | 0 | 6.11 | 12.349 | 6.64 | 10.705 | 5.286 | 4.651 |
| A_3 | 3.538 | 1.073 | 0 | 2.402 | 6.559 | 3.249 | 5.467 | 4.581 |
| A_4 | 5.426 | 1.073 | 6.085 | 0 | 18.906 | 1.737 | 0.951 | 4.564 |
| A_5 | 3.987 | 0.995 | 3.908 | 3.277 | 0 | 43.301 | 4.238 | 3.344 |
| A_6 | 4.037 | 0.982 | 9.357 | 2.325 | 16.124 | 0 | 4.273 | 9.803 |
| A_7 | 4.144 | 0.991 | 6.882 | 1.974 | 16.021 | 4.974 | 0 | 3.340 |
| A_8 | 4.13 | 0.973 | 4.659 | 3.107 | 16.106 | 11.763 | 8.111 | 0 |

TABLE 6: The time costs of the sequential control on the bladder network.

paths in the transition system. The initial state is A_2 at layer 0 and the target attractor is the extension of A_5 at layer 2. By perturbing variables “Tbx5” or “Nkx25”, we can reach s_1 or s_2 at layer 1. At this step, on one hand, we can perturb “Nkx25” at s_1 or “Tbx5” at s_2 to reach s_5 at layer 2. On the other hand, we can let the network evolve and when the network is at states s_3 or s_4 , by performing different perturbations, we can reach one of the states (s_5 - s_{12}) at layer 2, which is in the basin of the target attractor A_5 at layer 2. In this way, the network will eventually reach the target attractor spontaneously.

Table 4, 5 and 6 show the time costs of the sequential control on three networks. The time costs include the computation of the minimal number of perturbations as well as the computation of all inevitable reprogramming paths. The ranges of the time costs for the cardiac network, the PC12 network and the bladder network are 0.005-0.228, 0.183-5.792, 0.951-43.301 seconds, indicating the efficiency and scalability of our sequential control method. There are mainly two factors that influence the efficiency of the sequential control: the minimal number of perturbations and the number of reprogramming paths. If the required minimal number of perturbations is big, many iterations will be performed since we start from $m = 0$. Meanwhile, it also takes time to compute all the solutions using the procedure “COMPUTE_PATHS” if there exist many reprogramming paths.

6 DISCUSSION

Sequential reprogramming consists in applying perturbations in a specific order and in specific states of the system to trigger and control an attractor change. It relies on the transient dynamics of the system. Sequential reprogramming is interesting for biologists wanting to reprogram cells: it can return new targets, and can lower costs by requiring lighter interventions.

As discussed in Sect. 2, initial reprogramming is only allowing perturbations from the initial state, thus there is no order needed. This case is discussed in multiple other works, and has been the main computation technique for perturbations. Once all the perturbations have been done, the system stabilizes itself in the targeted attractor. By ordering and “waiting” between the perturbations, other dynamics of the system can be used, thus possibly reducing the number of variables to be perturbed, and returning new solutions.

Other works [4], [8], [3], [19] can use probabilistic methods to determine perturbations to do in the initial state. These reprogramming techniques compute initial existential reprogramming. Technically, no proof is given that the network will reach the wanted target, however there is a high probability that it will. Some of these works [4], [3] choose an initial state randomly for each test.

Some works [5], [20] focus on making the target always reached, but still only use initial perturbations, making them initial inevitable reprogramming techniques.

In other works [1], [18], the model allows for sequential reprogramming, making them sequential existential reprogramming. In [1], the existence of solutions is checked through a model checker, and specific perturbation paths can be tested. In [18], the model is probabilistic and use time-series data, thus allowing to make perturbations at different times in the series.

Lastly, some works [23], [12] allow for sequential inevitable reprogramming.

Most of mentioned methods provide incomplete or non-guaranteed results. Our aim is to provide a formal framework for the complete and exact characterization of the initial state and sequential reprogramming of Boolean networks.

This paper establishes a set characterization of sequential reprogramming for Boolean networks with either permanent (mutations) or temporary (e.g, through signalling) perturbations. Perturbations can be applied at the initial state, and during the transient dynamics of the system. This later feature allows identifying new strategies to reprogram regulatory networks, by providing solutions with different targets and possibly requiring fewer perturbations than when applied only in the initial state.

The algorithm we designed relies on modelling the combination of Boolean network asynchronous transitions with perturbation transitions by using binary decision diagrams. The identification of sequential reprogramming solutions then relies on an explicit exploration of the resulting transition system. Our method has no restriction on the nature of the target state, which could be either a transient state, fixed point attractor, or within a cyclic attractor. Our framework can handle temporary perturbations for the inevitable

reprogramming to the targeted state, and the use of BDDs allows for some scalability as supported by performed case studies.

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