

# Probability mapping of soil thickness by random survival forest at a national scale

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- 1 **Title:** Probability mapping of soil thickness by random survival forest at a national
- 2 scale
- 3

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#### 27 **Abstract:**

Soil thickness (ST) is a crucial factor in earth surface modelling and soil storage 28 capacity calculations (e.g., available water capacity and carbon stocks). However, the 29 observed depths recorded in soil information systems for some profiles are often less 30 than the actual ST (i.e., right censored data). The use of such data will negatively 31 affect model and map accuracy, yet few studies have been done to resolve this issue 32 or propose methods to correct for right censored data. Therefore, this work 33 demonstrates how right censored data can be accounted for in the ST modelling of 34 mainland France. We propose the use of Random Survival Forest (RSF) for ST 35 36 probability mapping within a Digital Soil Mapping framework. Among 2109 sites of the French Soil Monitoring Network, 1089 observed STs were defined as being right 37 censored. Using RSF, the probability of exceeding a given depth was modelled using 38 freely available spatial data representing the main soil-forming factors. Subsequently, 39 the models were extrapolated to the full spatial extent of mainland France. As 40 examples, we produced maps showing the probability of exceeding the thickness of 41 each GlobalSoilMap standard depth: 5, 15, 30, 60, 100, and 200 cm. In addition, a 42 bootstrapping approach was used to assess the 90% confidence intervals. Our 43 results showed that RSF was able to correct for right censored data entries occurring 44 within a given dataset. RSF was more reliable for thin (0.3 m) and thick soils (1 to 2 45 m), as they performed better (overall accuracy from 0.793 to 0.989) than soils with a 46 thickness between 0.3 and 1 m. This study provides a new approach for modelling 47 right censored soil information. Moreover, RSF can produce probability maps at any 48 depth less than the maximum depth of the calibration data, which is of great value for 49 designing additional sampling campaigns and decision making in geotechnical 50 engineering. 51

- 52 **Keywords:** Soil thickness modelling; Right censored data; Random Survival Forest;
- 53 GlobalSoilMap; Probability mapping.

#### 54 **1. Introduction**

Soils are of great importance in supporting, provisioning, and regulating 55 ecosystem services, such as food production and climate change mitigation (Clothier 56 et al., 2011; Keesstra et al., 2016; Millennium Ecosystems Assessment, 2005). As 57 stated by recent studies (e.g., Bouma, 2018; Groshans et al., 2018; Marx et al., 2019), 58 there is a rising demand for up-to-date and ecosystem service relevant soil 59 information. Therefore, substantial effort is needed to communicate soil information 60 among diverse audiences and produce fine resolution soil maps to support practical 61 land management. In this study, we use the *GlobalSoilMap* project specifications. 62 These specifications focus on delivering consistently produced high-resolution soil 63 property information throughout the world by predicting mean values and their 64 prediction intervals (PIs) (Arrouays et al., 2014a; Arrouays et al., 2014b; Sanchez et 65 al., 2009). Among the twelve soil properties to be predicted following the 66 recommendations of GlobalSoilMap, soil thickness (ST) is a key property. In this 67 study, in line with *GlobalSoilMap*, ST is defined as 'the depth (cm) from the soil 68 surface to the lithic or a paralithic contact' (Soil Survey Division Staff, 1993). The ST 69 is highly relevant for soil hydro-mechanical modelling (Tesfa et al., 2009; Wang et al., 70 2006), soil erosion impact, landscape evolution, vegetation growth (Heimsath et al., 71 2001: Meyer et al., 2007), and for calculating soil functions (e.g., available water 72 capacity (Leenaars et al., 2018; Román Dobarco et al., 2019), soil structure (Rabot et 73 al., 2018; Vogel et al., 2018), and soil organic carbon stocks (Baties, 1996; Chen et 74 al., 2019)). Despite the great importance of accurate ST information, the large spatial 75 variability and high cost of ST measurements make ST determination difficult 76 (Lacoste et al., 2016). Discordance in the definition of ST also hampers ST modelling, 77 especially when data are collected from various projects (Lacoste et al., 2016). The 78

observed ST recorded in soil information systems for some profiles are often less
than the actual ST (i.e., right censored data).

ST results from the mass balance between soil formation from the bedrock 81 and soil transport by erosion and sedimentation (Heimsath et al., 1997; Heimsath et 82 al., 1999); thus, it varies as a function of physical, chemical, and biological processes 83 (Román et al., 2018). ST can be related to these processes by modeling the 84 relationship between the main soil-forming factors, i.e., Jenny's Soil-Landscape 85 paradigm (Jenny, 1941): parent material, climatic conditions, organisms, terrain relief, 86 and time (Dietrich et al., 1995; Minasny and McBratney, 1999). More recently, 87 88 McBratney et al. (2003) formulated the concept of the SCORPAN model, which also includes also soil information and spatial location. 89

Various approaches for ST modelling and mapping have relied on modelling 90 the relationship between the main soil forming factors. The majority of these 91 approaches can be broadly classified into two groups: 1) physically based and 92 mechanistic models, which predict ST using soil process models based on the rates 93 of weathering, denudation, and accumulation (Bonfatti et al., 2018; Dietrich et al., 94 1995; Minasny and McBratney, 1999; Pelletier and Rasmussen, 2009); and 2) 95 empirical models, including statistical and geostatistical methods (Kuriakose et al., 96 2009). These models rely on the empirical relationships between ST and explanatory 97 covariates of inferential attributes (e.g., plant species, precipitation, and parent 98 material). 99

For the latter, a wide range of statistical methods have been previously applied
in ST modelling, including canonical correspondence analysis and principal
component analysis (Odeh et al., 1991), multiple linear regression (Moore et al.,
1993), expert knowledge and fuzzy logic (Zhu et al., 2001), Generalized Additive

Models and Random Forest (Tesfa et al., 2009), and Cubist and Gradient Boosting
Modelling (Lacoste et al., 2016; Mulder et al., 2016a).

Within the field of geostatistics, various kriging techniques have often been
used to predict and spatially interpolate ST from point samples. Ordinary Kriging was
most commonly used among these kriging techniques (Penížek and Borůvka, 2006;
Vanwalleghem et al., 2010). The prediction variance was typically reduced when
including additional prediction variables using regression kriging (Kuriakose et al.,
2009; Odeh et al., 1995) or Kriging with External Drift (Bourennane et al., 1996;
Kempen et al., 2015).

None of the studies referred to above addressed the issue of having right 113 censored data entries in their soil databases. However, it is often the case that the 114 actual ST is thicker than the observed ST, which can mainly be attributed to practical 115 constraints, such as the standard auger length (120 cm), and time constraints. In fact, 116 in soil sciences very few studies consider the effect of right censored data; the issue 117 is often ignored or processed by adding a fixed value (e.g., 30 cm) in ST modelling 118 (Knotters et al., 1995; Vaysse and Lagacherie, 2015; Lacoste et al., 2016; 119 Shangguan et al., 2017). Some previous works dealt with left censored data, 120 especially regarding data below detection limits (e.g., de Oliveira, 2005; Fridley and 121 Dixon, 2007; Orton et al., 2009; Orton et al., 2012; Villaneau et al., 2011). Ignoring 122 the presence of right censored data entries within a database and relying on the 123 observed ST for those entries will result in an underestimation of modelled ST 124 (Vaysse and Lagacherie, 2015; Shangguan et al., 2017). 125

However, right censored data are commonly used in statistics and medical research, especially in survival analysis. Several models have been used to deal with right censored data in survival analysis, including the Kaplan Meier method (Kaplan and Meier, 1958), Cox regression (Andersen and Gill, 1982), and Random Survival
Forest (RSF, Ishwaran et al., 2008). The Kaplan Meier method and Cox regression
mainly deal with linear effects, but RSF is capable of handling complex non-linear
effects that may exist between predictor variables (Mogensen et al., 2012). Therefore,
as previously suggested by Styc and Lagacherie (2016), RSF may have the best
potential for identifying and correcting right censored data used for Digital Soil
Mapping (DSM).

In this study, the potential of RSF was evaluated for ST mapping in mainlandFrance. The main objectives of this study are noted below:

Apply RSF for mapping the probability of exceeding a certain ST using both
 actual and right censored ST data from the French Soil Monitoring Network
 (RMQS) and

141 2) Derive the 90% confidence intervals of the specific ST using bootstrapping.

142

#### 143 **2. Material and methods**

144 2.1. Soil dataset

We used ST data from the RMQS soil database that were gathered between 145 2001 and 2009 (Jolivet et al., 2006), covering different soil, climate, relief, and land 146 cover conditions (Fig. 1). The RMQS dataset is based on a 16 km × 16 km square 147 grid where all sites are selected at the centre of each grid cell. When sampling the 148 exact location was not possible, a site was selected as close as possible to the grid 149 centre. A soil pit was dug, and the surrounding information (land use and 150 geomorphology) and a detailed description of the soil profile were recorded for each 151 site, including soil horizon depth and ST. Auger boring was recommended (but not 152 mandatory) to complete the soil profile when the soil pit was not thick enough to 153

determine the ST. For more detailed information about the soil sampling design and
laboratory analysis, see Chen et al. (2018). Among 2109 RMQS sites, ST was
explicitly recorded for 1020 sites (down to a lithic or paralithic contact), while the
remaining 1089 sites were right censored data. The ST for nine RMQS sites was set
to 0, as these sites were identified as mountainous sites with bare rock.

159

160 2.2. Exhaustive covariates

We used a DSM framework (McBratney et al., 2003) to model the relationships between ST and ancillary covariates (Table 1). These covariates cover a series of soil formation related environmental factors, including soil, climate, organisms, relief and parent material. Before modelling, these covariates were re-projected to Lambert 93 (official projection for mainland France) and resampled to a 90 m resolution (in raster format) using a bilinear interpolation (numeric covariates) or nearest neighbour (categorical covariates).

168

169 2.3. Random survival forest for probability modelling of soil thickness

170 2.3.1. General introduction

RSF is an ensemble tree method for modelling right censored survival data 171 (Ishwaran et al., 2008). RSF is an extension of Breiman's (2001) random forest (RF), 172 known as an ensemble learning approach that is improved by injecting randomization 173 into the base-learning process. For example, using a human analogy, a specific 174 status introduced in RSF aims to distinguish whether it is a death case (status = 1) or 175 a survival case (status = 0) at a given observed time. The RSF does this by 176 estimating the presence-absence probability. Applying this censoring concept to ST, 177 at a given site there are two possibilities for a thickness to be recorded: i) the actual 178

ST has been observed down to lithic or paralithic contact as defined before (status = 179 1) or ii) the lithic or paralithic contact has not been reached and the actual ST 180 remains unknown (status = 0). For the latter, it is only known that the actual ST is 181 greater than the observed ST. RSF uses a new type of predicted outcome that 182 contains a cumulative hazard function (CHF, see Section 2.3.2). 183 184 2.3.2. Random survival forest model fitting 185 RSF model fitting involves the following steps (Ishwaran et al., 2008), as 186 shown in Fig. 2. 187 1) Select *ntree* bootstrapped samples from the calibration data. Approximately 37% 188 (e<sup>-1</sup>) of the calibration data are excluded in each bootstrapped sample, which are 189 so-called out-of-bag (OOB) data. 190 2) Grow a survival tree for each bootstrapped sample. At each node of the survival 191 tree, randomly select *mtry* covariates for splitting the data. Survival splitting 192 criteria are then used, and each node is split on that covariate, which maximizes 193 survival differences across sub-nodes. 194 3) Grow the survival tree to full size under the constraint that a terminal node should 195 have no less than *nodesize* unique actual ST samples. 196 4) Calculate a CHF for each survival tree and obtain the ensemble CHF by 197 averaging all the survival trees for each sample. 198 5) Calculate the prediction error of the ensemble CHF based on OOB data. 199 200 Ensemble cumulative hazard function and ensemble survival function 201 Constructing the ensemble CHF is crucial for RSF. Hereafter, we provide 202 details about the procedure for a better understanding. 203

For a survival tree, let  $(ST_{1,h}, \delta_{1,h}), \ldots, (ST_{n(h),h}, \delta_{n(h),h})$  be the observed ST and the 0–1 censoring status ( $\delta$ ) for *n* samples in a terminal node *h*. Here, let  $ST_{1,h} < ST_{2,h} < \cdots < ST_{n(h),h}$  be the different observed ST in the terminal node. The CHF estimate for *h* is then defined by the Nelson–Aalen estimator  $\hat{H}_h$ :

208 
$$\widehat{H}_h(st) = \sum_{st_{l,h} \le st} \frac{a_{l,h}}{Y_{l,h}}, \qquad (1)$$

where  $a_{l,h}$  and  $Y_{l,h}$  are the number of actual ST samples and all samples at observed ST  $st_{l,h}$ , respectively. All the samples within the terminal node h have the same CHF. Each sample i has a *mtry*-dimensional covariate  $\mathbf{x}_i$  that will belong to a unique terminal node h. Therefore, the CHF for i is the Nelson–Aalen estimator for  $\mathbf{x}_i'$ terminal node:

214

$$H(st|\mathbf{x}_i) = \widehat{H}_h(st). \tag{2}$$

Equation 2 describes the CHF from an individual tree. The ensemble CHF is computed by averaging over *ntree* trees. The bootstrap ensemble CHF for sample *i* is defined below (the definition of OOB ensemble CHF please refer to Ishwaran et al., 2008):

219 
$$H_e(st|\mathbf{x}_i) = \frac{1}{ntree} \sum_{n=1}^{ntree} H_n(st|\mathbf{x}_i),$$
(3)

where  $H_n(st|\mathbf{x})$  is the CHF for a tree grown from the *n*<sup>th</sup> bootstrap sample.

The survival function is a probability density function that describes the survival probability at a given ST. In RSF, the ensemble survival function ( $S_e$ ) could be derived from ensemble CHF (Mogensen et al., 2012):

224 
$$S_e(st|\mathbf{x}_i) = \exp\left\{-\frac{1}{ntree}\sum_{n=1}^{ntree}H_n(st|\mathbf{x}_i)\right\}.$$
 (4)

Here, the survival probability at a given ST is equal to the probability of exceeding a given ST or censored probability at a given ST. The probability of exceeding a given ST ranges from 0 to 1, and when it is close to 1, the location has a
high probability of being censored. Therefore, in this latter case, the actual ST has a
high probability of being thicker than the censored ST.

230

231 Node splitting rule

The node splitting rule is another important parameter in RSF. There are 232 several choices for splitting rules, including the log-rank splitting rule, conservation 233 splitting rule, log-rank score rule, and fast approximation to the log-rank splitting. 234 Here, the log-rank splitting rule is used as the default splitting rule, as suggested by 235 236 Ishwaran et al. (2008). We define  $st_1 < st_2 < \cdots < st_i$  as the ST intervals and  $x_{i,i}$  and 237 *a*<sub>*i*,*i*</sub> as the number of samples and number of actual ST samples at ST *s*<sub>*i*</sub> in the subnodes *j* (1 or 2), respectively. Here,  $x_i = x_{i,1} + x_{i,2}$  and  $a_i = a_{i,1} + a_{i,2}$ . The log-rank test 238 for a split at the value *n* of the covariate *c* is defined as 239

240 
$$L(c,n) = \frac{\sum_{i=1}^{l} (a_{i,1} - x_{i,1} \frac{a_i}{x_i})}{\sqrt{\sum_{i=1}^{l} \frac{x_{i,1}}{x_i} (1 - \frac{x_{i,1}}{x_i}) (\frac{x_i - a_i}{x_i - 1}) a_i}},$$
(5)

where the value |L(c, n)| is the measure of node split, and  $x_{i,1}$  and  $a_{i,1}$  are the number of samples and number of actual ST samples, respectively, at ST  $st_i$  when c is less than n. The larger the |L(c, n)| value, the larger the difference between two subnodes and a better split. The best split at each note is determined by searching the optimized covariate  $c^*$  and split value  $n^*$  to maximize the |L(c, n)| value.

246

247 *Prediction error* 

In survival analysis, Harrell's concordance index (Harrell Jr et al., 1982) is
commonly used for estimating prediction error as it does not depend on choosing a
fixed time for model evaluation and specifically accounts for censoring (May et al.,

2004). The concordance index (*C* index) is calculated by the following steps in ST
modelling.

1) Generate all possible pairs of samples over the data.

254 2) Remove pairs whose lower ST is censored. Remove pairs *i* and *j* if  $st_i = st_j$  unless 255 at least one is an actual ST sample. The total number of permissible pairs is 256 recorded as *Per*.

3) For each permissible pair where  $st_i \neq st_j$ : if the thinner ST has worse predicted

outcome (higher cumulative hazard value), count 1; ii) otherwise, count 0.5. For

each permissible pair where  $st_i = st_j$  and both are actual ST samples: i) if

predicted outcomes are equal, count 1; ii) otherwise, count 0.5. For each

permissible pair where  $st_i = st_j$  and not both, are actual ST samples: i) if the

actual ST sample has a worse predicted outcome, count 1; ii) otherwise, count

263 0.5. The sum of all permissible pairs is recorded as *Con*.

4) The *C* index is defined by the ratio of *Con* to *Per*.

In RSF, the *C* index is computed via OOB data using the steps mentioned above, and it ranges between 0 and 1. The prediction error is calculated by the1-*C* index, so it is also between 0 and 1. A lower prediction error represents better model performance for the calibration model.

269

270 2.3.3. Assessing the main controlling factors for ST modelling

To assess the main controlling factors for ST in France, the variable importance of the ST predictors (i.e., covariates used) in the RSF model were evaluated. In RSF, the variable importance of a covariate c is calculated by dropping OOB samples down their in-bag survival tree. A sub-node is randomly assigned when encountering a split for c, and then an average of the CHF obtained from these trees is calculated. The variable importance for *c* is calculated as the difference of
prediction error between the new ensemble obtained using randomized *c*assignments and the original ensemble. A larger variable importance value indicates
a higher contribution to the model for a covariate.

280

281 2.4. Soil thickness probability mapping and bootstrapping for determining prediction282 uncertainty

As introduced in Section 2.3.2, the RSF model outcome entails a function 283 between the survival (censored) probability and ST for each prediction. In other 284 285 words, the censored probability can be calculated over the full soil profile (0 to the maximum depth of actual ST samples) for any position in mainland France from RSF. 286 As an example, the censored probabilities for the six *GlobalSoilMap* standard depths 287 were extracted from the survival probability function (Fig. 3); those depths are 5, 15, 288 30, 60, 100, and 200 cm, which we refer to hereafter as ST5, ST15, ST30, ST60, 289 ST100 and ST200, respectively. From this, we derived a probability map for each 290 291 *GlobalSoilMap* standard depth in mainland France.

Bootstrapping was applied to determine the average and 90% Confidence 292 293 Intervals (CIs) of the RSF model. Hence, we did not determine the 90% PIs as is recommended by the *GlobalSoilMap* specifications; instead we estimated the 90% 294 Cls. This was deemed suitable, as we were not able to identify the random error in 295 the RSF model. Consequently, the estimated 90% CIs would be narrower than 90% 296 Pls. The bootstrap samples were drawn 50 times by repeated random sampling with 297 298 replacement of the RMQS sites; the RMQS sites not used in each bootstrap sample were used to evaluate the model performance of each bootstrap RSF model (details 299 in Section 2.5). Note that the bootstrap sample used here corresponds to the initial 300

data used in the RSF framework (Fig. 2), not the bootstrap sample used to generate 301 trees. Finally, using these bootstrap samples, 50 bootstrap RSF models were 302 generated, from which 50 probability functions between the censored probability and 303 ST could be exhaustively predicted for mainland France. After several iterative model 304 calibrations leading to the final prediction model, we choose 50 bootstrap models 305 because it is time-consuming to make predictions at a 90 m resolution for mainland 306 France (RSF produces a probability function rather than a value for each pixel, so it 307 takes 2 weeks for 50 bootstrap RSF models under parallel computing that make full 308 use of a computer with 8 cores and 32 GB of RAM). A robust estimate of the 309 probability of exceeding each standard *GlobalSoilMap* soil depth was determined by 310 averaging the bootstrap predictions. Their lower and upper 90% CIs were calculated 311 by the averaged bootstrap predictions minus and plus 1.645 times (Z score for 90%) 312 Cls) the standard deviation of bootstrap predictions, respectively. Surface area 313 percentages of five probability intervals (0-0.2, 0.2-0.4, 0.4-0.6, 0.6-0.8, and 0.8-1) 314 were calculated from the averaged bootstrap predictions of probability maps at six 315 316 GlobalSoilMap standard depths. The mean probability was computed by averaging all pixels of the probability map for each *GlobalSoilMap* standard depth. 317

318

319 2.5. Model performance

In addition to the CIs, the model performance of each *GlobalSoilMap* standard depth was evaluated using the RMQS sites that were not used in the bootstrap samples, which referred to an evaluation dataset from each bootstrap RSF model. For a given *GlobalSoilMap* standard depth ( $st_s$ ), the prediction performance was evaluated based on the confusion matrix in which the misclassification rate was calculated based on whether the data was censored or not. Hence, given a sample

326	with observed ST ( <i>st<sub>o</sub></i> ): 1) when $st_s \leq st_o$ , if the probability exceeds 0.5, the sample is
327	correctly predicted, otherwise, it is incorrectly predicted; and 2) when $st_s > st_o$ , if the
328	probability is less than 0.5, the sample is correctly predicted, otherwise, it is
329	incorrectly predicted.

Subsequently, the confusion matrix was calculated as the mean counts of
 OOB samples with actual ST and censored ST separately from 50 bootstrap
 predictions.

All of the statistics and modelling were performed in R (R Core Team, 2016). R package *randomForestSRC* was used for RSF modelling (Ishwaran and Kogalur, 2017).

336

#### 337 3. Results

338 3.1. Summary statistics of the ST dataset

Among 2108 RMQS sites, more than half were right censored for ST (Fig. 4). The actual ST ranged from 0 to 300 cm, with a mean value of 64 cm. The first quantile, median and third quantile were 39, 59, and 80 cm, respectively, indicating a large percentage of soils thinner than 60 cm. The censored ST ranged from 50 to 270 cm, with the mean ST (104 cm) being higher than the actual observed RMQS sites. For the censored RMQS sites, the first quantile, median, and third quantile were 75, 95, and 120 cm, respectively.

346

347 3.2. Model performance

The prediction error of the calibrated RSF models decreased from 0.27 to 0.15 as the number of trees increased up to 50 (Fig. 5). After 50 trees, the prediction error decreased slightly and became more stable as the number of trees increased (max. 351 300 trees). This indicated that 50 trees were sufficient for this study to produce a
stable model while accelerating the prediction efficiency for big data.

The prediction performance differed when evaluated at the six *GlobalSoilMap* standard depths (Table 2). For the actual RMQS sites, the overall accuracy decreased from 0.989 to 0.546, when depth increased from ST5 to ST60. The overall accuracy then gradually increased up to 0.793 for ST200. The overall accuracy for censored RMQS sites were 1, 0.998, and 0.995, respectively, for SD5, SD15, and SD30, the accuracy then decreased to 0.825 for SD60 and subsequently dropped to 0.534 for ST100 and 0.563 for ST200.

360

#### 361 3.3. Controlling factors of ST modelling

Parent material (PM) and climatic zones (TYPO) were the two most important 362 variables affecting the ST probabilities in RSF models, based on the average 363 bootstrap RSF (Fig. 6). The difference in prediction error between the new and the 364 original ensembles was most affected by these two variables, despite the large 90% 365 Cls. Roughness, precipitation, elevation, slope, gravimetry and Net Primary 366 Production (NPP) also had large contributions in ST modelling. The remaining 367 covariates contributed less to the RSF model and had smaller CIs. 368 369 3.4. ST probability maps and associated confidence intervals 370 Fig. 7 presents the ST probability maps of exceeding the six *GlobalSoilMap* 

Fig. 7 presents the ST probability maps of exceeding the six *GlobalSoilMap* standard depths and their 90% CIs for mainland France. Overall, the average probability of exceeding the *GlobalSoilMap* standard depths of 5, 15, 30, 60,100, and 200 cm were 0.99, 0.97, 0.88, 0.68, 0.51, and 0.42, respectively. The probability of exceeding ST5 was close to 1 across the whole country, except for eastern (the Alps) and southwestern France (the Pyrenees). The 90% CI was very narrow ( $0.02 \pm 0.06$ ), indicating low model uncertainty and thus robust estimates for the ST5 map.

A similar spatial distribution was observed when ST increased to ST15. The low probability in southern France (the Massif Central) showed that this region had a high probability of having STs less than 15 cm. The difference between the lower and upper limits of the 90% CI was still low ( $0.05 \pm 0.08$ ), indicating a robust estimate. Moreover, the surface area percentages for the five probability intervals were also quite close to those of ST5 (Fig. 8).

When the ST depth criteria was further increased to ST30, in addition to 385 previously mentioned locations, low probabilities were found in eastern France (the 386 Jura Mountains, Fig. 7). Moreover, the CIs substantially increased (give numbers) 387 compared to ST5 and ST15. This indicates a larger prediction uncertainty and a 388 lower model robustness. In comparison with ST15, a slight increase (2%) was 389 observed for the surface area with probabilities between 0.4 and 0.6. The surface 390 area having a probability between 0.6 and 0.8 increased from 1 to 14%, while the 391 area with a probability between 0.8 and 1 decreased from 98 to 83% (Fig. 8). 392

Moving from the ST30 up to the ST200 thickness criteria, substantial changes in spatial patterns and the probability of surpassing the ST criteria became apparent. Most notable is how the surface area with probabilities between 0.8 and 1.0 continuously decreased, from 83% (ST30) to 2% (ST200). ST60 corresponded with a probability of 27% and ST100 with a probability of 7% (Fig. 8).

For ST200, more than 50% of the territory of mainland France had a low probability (<0.4) of exceeding ST by 2 m, while less than 17% of the areas had a high probability (>0.6) of exceeding the ST by 2 m (Fig. 7). The areas with a high
probability were mainly located in southwestern France (the Landes of Gascony),
central France (Sologne), and northern France (thick loess deposits).

403

#### 404 **4. Discussion**

Several ways to perform probability mapping have been proposed in the 405 literature since the 1990s. For instance, Bell et al. (1994) applied discriminant 406 analysis with a maximum-likelihood classification function to map the soil drainage 407 probability in south-central Pennsylvania, USA. von Steiger et al. (1996) mapped the 408 probability of exceeding the maximum tolerable heavy metal concentrations by 409 Disjunctive Kriging in northeast Switzerland. Richer-de-Forges et al. (2017) used 410 Logistic Regression Kriging in probability mapping of iron pan presence in sandy 411 412 podzols in southwest France. The largest differences between the methods used in previous studies and RSF can be summarized in two aspects: 1) RSF is able to deal 413 with right censored data while others are not, and 2) RSF can potentially produce 414 probability estimates of any ST value, whereas other methods deal with 415 presence/absence at a given threshold for the soil attributes of interest. Moreover, 416 others used multiple sequential indicator simulations to model this type of distribution 417 (e.g., Cattle et al., 2002). The survival analysis we used is a similar approach, except 418 that it models the survival function rather than the empirical distribution function. 419

In the RMQS dataset, right censored ST observations entail more than half of
the observations. Using them for ST modelling with traditional DSM approaches
would result in highly underestimated ST estimates. Lacoste et al. (2016) proposed
adding a fixed value of 30 cm to censored samples before modelling, which may help
lower the underestimation but does not really solve the problem. Moreover, as actual

425 ST values of these censored sites remain unknown, adding a fixed value may even 426 add more noise to the data, and thus enlarging the prediction uncertainty. As shown 427 in Fig. 9, the probability of exceeding the observed ST for each censored RMQS site 428 was mainly between 0.5 and 1, with a median value of 0.78. Thereafter, as outlined 429 in the methodology Section 2.3.2, RSF makes use of the probability function derived 430 from right censored information, thereby avoiding underestimating ST at these 431 censored positions.

The mean probability of exceeding an ST of 100 cm across mainland France was 0.51 (Fig. 8), which means that all locations have a 50% possibility of being observed with an ST thicker than 100 cm. This result implies that the median ST in mainland France is approximately 100 cm, which is in line with previous work by Lacoste et al. (2016), showing that 48 and 54% of surface areas were below 100 cm when using Gradient Boosting Modelling and Cubist models, respectively.

The results showed that the prediction performance decreased from 0 to 60 438 cm and subsequently increased up to 200 cm for censored RMQS sites (Table 2), 439 implying that the predicted probability of exceeding a given ST from the RSF model is 440 more reliable for extreme values (i.e., a thin ST or thick ST). Indeed, due to the soil 441 forming conditions in mainland France, except for steep slopes in mountainous areas, 442 very thin soils are quite rare, and thus the probability of exceeding a very thin ST is 443 high. Conversely, very thick soils are concentrated in (former) depositional areas 444 (valleys, aeolian sand, or loess deposits) that can be easily mapped using some of 445 the covariates (e.g., parent material and terrain parameters). For the censored 446 RMQS sites, the overall accuracies for ST100 and ST200 were approximately 0.5, in 447 which a large percentage of thin ST samples were misclassified as being thick. This 448 can be explained by the fact that we used observed ST of censored RMQS sites in 449

calculating the confusion matrix. Consequently, we may overestimate the percentage
of misclassification mentioned before and thus underestimate the overall accuracies
of ST100 and ST200.

Parent material and climatic zones were the most important variables for 453 predicting ST in France using the bootstrapped RSF, but roughness, precipitation, 454 elevation, slope, gravimetry, and NPP also substantially contributed to the ST model. 455 These results are in line with previous findings reported by Lacoste et al. (2016). 456 Lacoste et al. (2016) stated that the most important covariates of ST modelling in 457 mainland France were soil properties, climate covariates and land use. Considering 458 459 the variable importance and the variables acting as controlling factors for ST, parent material, climatic zones, precipitation, and gravimetry are direct drivers for the 460 weathering process. Roughness, elevation, slope, and NPP are more related to 461 462 sediment transport dynamics.

Future research should aim to derive an ST map using RSF, instead of the 463 currently presented ST probability map of exceeding a given depth. There are three 464 ways to determine the actual soil ST from the unique probability function produced by 465 RSF for each location of interest: 1) use the ST extracted from the median probability 466 in the predicted function; 2) use the ST extracted from a fixed probability, allowing the 467 classification of censored and actual ST at high accuracy among RSF calibration 468 datasets; 3) perform a derivative analysis on the probability curve. Moreover, it will be 469 interesting to combine RSF with geostatistical methods. For example, kriging of 470 residuals (Hengl et al., 2004) that are not captured by RSF and/or sampling 471 optimizing for future campaigns to reduce the prediction variance at locations where it 472 is highest. Alternatively, the presented probability maps can be used directly for 473 additional ST sampling campaigns, aimed at ST modelling in mainland France. For 474

example, the regions with a high probability (>0.8) of ST200 have a large chance of 475 being censored. Integrating those high probability regions with parent material and 476 climatic zones would yield an efficient and effective sampling design using 477 conditioned Latin hypercube sampling (cLHS, Minasny and McBratney, 2006) to 478 obtain more representative samples of all physiographic contexts. RSF is able to 479 provide a probability at any depth and thus will be helpful for decision making in 480 geotechnical engineering regarding, for example, laying out drains, pipes, and tubes 481 (Zhang et al., 2005). 482

5. Conclusions 483

484 This study introduced the use of RSF in ST probability modelling to deal with right censored data for Digital Soil Mapping. RSF produced a probability function of 485 ST for each soil sample included in the database. This function allowed the 486 estimation of a probability of exceeding a given ST, indicating each soil location was 487 right censored or not. Robust estimates were made by bootstrapping the RSF model 488 to guantify an averaged bootstrap prediction and 90% CI for each GlobalSoilMap 489 standard depth (5, 15, 30, 60, 100 and 200 cm) using the RSF survival probability 490 functions. The model evaluation indicated an overall good performance (overall 491 accuracy from 0.546 to 0.989) of RSF to predict the probability exceeding the six 492 GlobalSoilMap standard depths. The RSF proved suitable for using right censored 493 soil data for digital soil mapping, and thereby this work introduced a new approach 494 capable of using both right censored and actual data for modelling ST accordingly. 495 496

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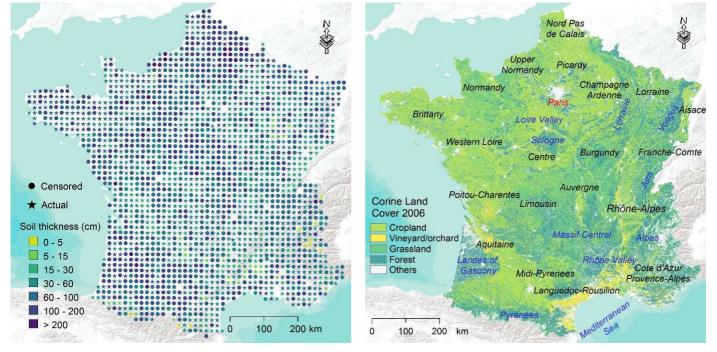
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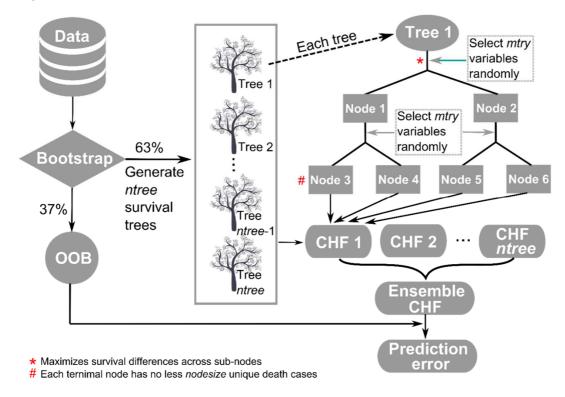
#### 741 Figures

- Fig. 1 Locations of RMQS sites with actual (dotted) and censored (star) ST values.
- For each site, ST is classified based on the *GlobalSoilMap* standard depths. Corine
- Land Cover map of 2006 of mainland France (right) with the administrative regions
- 745 (black italics) and natural geographic regions (blue italics).



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#### 747 Fig. 2 Random survival forest workflow.



- Fig. 3 Survival probability curve (blue solid line) for one location predicted by RSF.
- The orange dashed vertical lines indicate the six *GlobalSoilMap* standard depths,
- and the orange dashed horizontal lines indicate their corresponding censored
- probabilities that are derived from the survival probability curve.

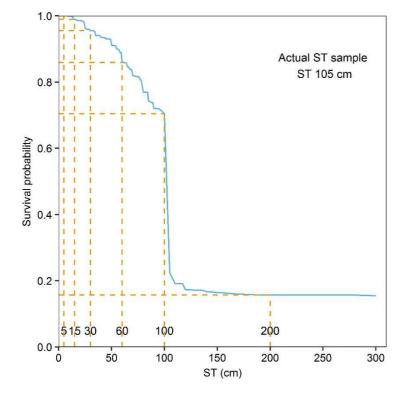
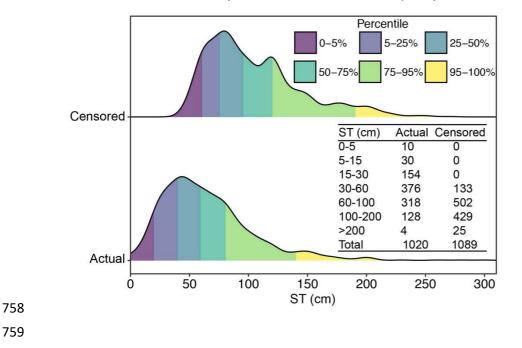


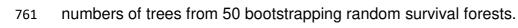


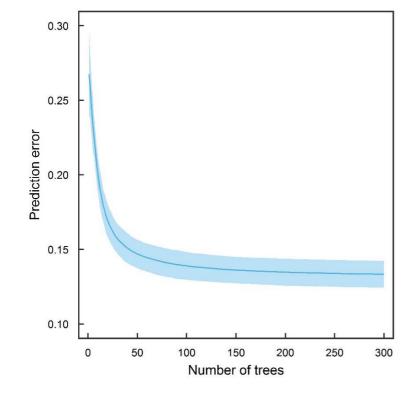
Fig. 4 Density distribution of STs for actual and censored RMQS sites. Counts of



actual and censored samples within *GlobalSoilMap* depth intervals are provided.

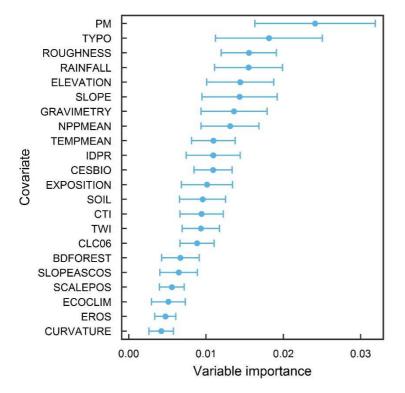
Fig. 5 Mean and 90% confidence intervals of the prediction error, given different





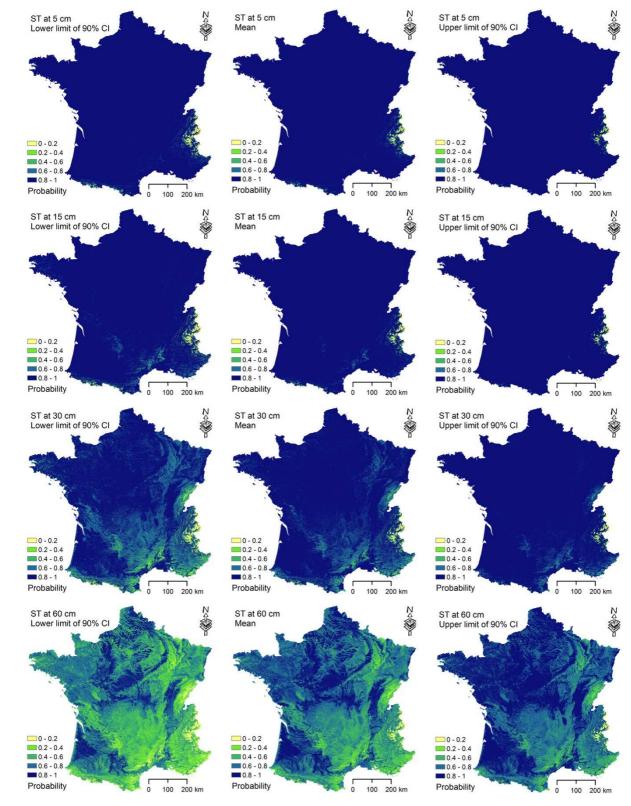


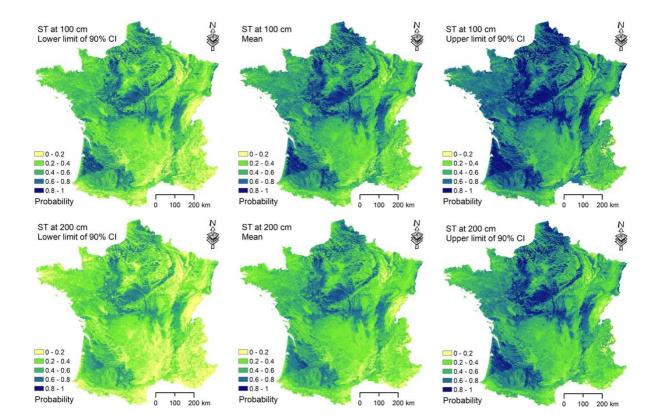
- Fig. 6 Mean and 90% confidence intervals of variable importance from 50
- 764 bootstrapping random survival forests.



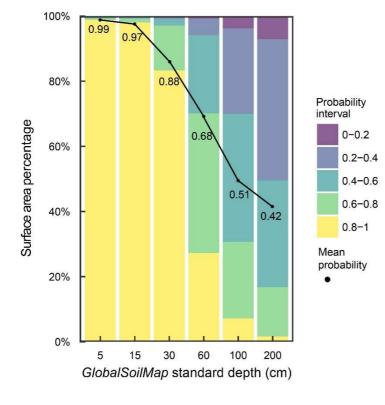
765

- Fig. 7 Probability maps of exceeding the six *GlobalSoilMap* standard depths (middle)
- and their associated 90% confidence intervals (left and right).



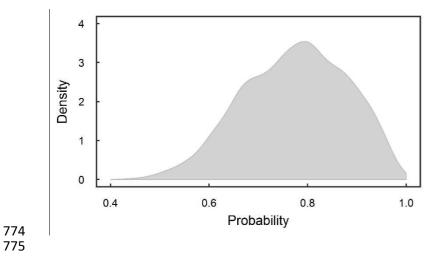


- Fig. 8 Surface area percentage of the probability of exceeding the ST of each
- 769 *GlobalSoilMap* standard depths. The mean probability is calculated by averaging all
- the pixels in the probability map for each *GlobalSoilMap* standard depth.



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Fig. 9 Histogram with the probability of exceeding the observed ST for each censored



773 RMQS site.

## 776 **Tables**

# Table 1 Exhaustive covariates used for ST modelling (after Mulder et al., 2016b)

Variable	Abbreviation	Scale/resolution	Soil forming factor	Reference
Elevation	ELEVATION	90 m	Relief	Jarvis et al. (2008)
Compound topographic	CTI	90 m	Relief	Jarvis et al. (2008)
index				
Curvature	CURVATURE	90 m	Relief	Jarvis et al. (2008)
Exposition	EXPOSITION	90 m	Relief	Jarvis et al. (2008)
Roughness	ROUGHNESS	90 m	Relief	Jarvis et al. (2008)
Slope	SLOPE	90 m	Relief	Jarvis et al. (2008)
Slope cosines	SLOPECOS	90 m	Relief	Jarvis et al. (2008)
Slope position	SLOPEPOS	90 m	Relief	Jarvis et al. (2008)
Topographic wetness index	TWI	90 m	Relief	Jarvis et al. (2008)
Gravimetric data (Bouguer	GREVIMETRY	4 km	Relief	Achache et al. (1997)
anomaly)				
Soil type <sup>a</sup>	SOIL	1:1000000	Soil	IUSS Working Group WRB (2006)
Erosion rates	EROS	1:1000000	Soil	Cerdan et al. (2010)
Rate of river network	IDPR	1:50000	Soil and parent	Info Terre – Site cartographique de
development and			material	référence sur les géosciences
persistence				(2014)
Parent material	PM	1:1000000	Parent material	King et al. (1995)
Mean annual net primary	NPPMEAN	1 km	Organisms	NASA LD (2001)
production				
Forest type	BDFOREST	Min area 2.25	Organisms	Inventaire Forestier National
		ha		(2006)
Land cover from Sentinel-2	LCS	10 m	Organisms	Inglada et al. (2017)
Corine land cover 2006	CLC06	250 m	Organisms	Feranec et al. (2010)
ECOCLIMAP land use	ECOCLIM	1 km	Organisms	Faroux et al. (2013)
Climatic zones	ТҮРО	1 km	Climate	Joly et al. (2010)
Mean annual precipitation	RAINFALL	1 km	Climate	Hijmans et al. (2005)
Mean annual temperature	TEMPMEAN	1 km	Climate	Hijmans et al. (2005)

<sup>a</sup> Soil type defined by World Reference Base (WRB)

Table 2 Model performance of actual and censored RMQS sites per each

780 *GlobalSoilMap* standard depth, based on out of bag samples. The count of correctly

classified sites is marked **bold**, and the overall accuracy is marked *italic underlined*.

ST (cm)		Actual RMQS sites			Censored RMQS sites		
	Rredicted Observed	Thin	Thick	Accuracy	Thin	Thick	Accuracy
5	Thin	2	2	0.500	0	0	1
	Thick	0	367	1	0	400	1
	Reliability	1	0.995	<u>0.989</u>	n.a.	1	<u>1</u>
15	Thin	2	12	0.143	0	0	n.a.
	Thick	0	356	1	1	399	1
	Reliability	1	0.967	<u>0.962</u>	0	1	<u>0.998</u>
30	Thin	5	65	0.063	0	0	n.a.
	Thick	1	300	0.997	2	398	1
	Reliability	0.833	0.843	<u>0.822</u>	0	1	<u>0.995</u>
60	Thin	58	150	0.279	7	43	0.140
	Thick	18	144	0.889	27	323	0.923
	Reliability	0.763	0.490	<u>0.546</u>	0.205	0.883	<u>0.825</u>
100	Thin	203	120	0.628	97	138	0.413
	Thick	19	28	0.596	49	117	0.705
	Reliability	0.914	0.189	<u>0.624</u>	0.664	0.459	<u>0.534</u>
200	Thin	294	76	0.795	219	172	0.560
	Thick	1	1	0.500	3	6	0.667
	Reliability	0.997	0.013	<u>0.793</u>	0.986	0.034	<u>0.563</u>

782 *n.a.* Not available.