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Guided photoluminescence from integrated carbon nanotubes-based optical waveguides

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## **Abstract**

We report the fabrication of planar and ridge waveguides made of semiconducting single-wall carbon nanotubes dispersed in fluorene-based polymers. Optical properties (refractive index, absorption and photoluminescence) of carbon nanotubes-incorporated polymer thin films are presented. Technological processing steps to obtain ridge waveguides are described and optical propagation at 1550 nm in these structures is confirmed by optical near field imaging of guided modes. Photoluminescence experiments on films and ridges waveguides are compared to demonstrate the guided photoluminescence of carbon nanotubes in the near infrared (1500-1600 nm).

Carbon nanotubes (CNT) and graphene exhibit outstanding mechanical, thermal, electronic and optical properties<sup>1,2,3</sup>. Graphene is attracting a growing interest of the scientific community and has been implemented as sensors<sup>4</sup>, photodetectors<sup>5,6</sup> or transparent electrode in high efficiency solar cells<sup>7</sup> and light emitting diodes<sup>8</sup>. Since graphene has no bandgap, this material is not expected luminesce from charge carriers relaxation, however graphene luminescence can be obtained by inducing a bandgap notably after oxygen plasma treatment<sup>9</sup>. The versatile CNT physical properties have also been widely investigated and numerous promising applications have emerged such as FET<sup>10</sup>, biomedical and gas sensors<sup>11,12</sup>.

Recently, a particular attention has been drawn to the implementation of CNT-based photonic devices. Nonlinear optical properties of CNT (notably the large and fast response of the real and imaginary parts of the third-order susceptibility) have found applications<sup>13</sup> as saturable absorber for

mode-locked lasers<sup>14,15</sup> and as nonlinear functional components (optical switch, signal converters or signal regenerator) for telecommunication systems<sup>16</sup>. Light-emitting devices based on electro- and photo-luminescence properties of semiconducting single-wall carbon nanotubes (s-SWCNT) have been developed<sup>17,18</sup> and optical gain has been measured<sup>19</sup>. To overcome the relatively low quantum efficiency of SWCNT<sup>20</sup>, several studies have also been undertaken to couple SWCNT to optical cavities (Fabry-Perot planar cavity based on metallic or Bragg mirrors<sup>21,22</sup>, microring or microdisk resonators<sup>23,24</sup> and photonic crystals<sup>25</sup>). The resulting luminescence enhancement factor can reach more than an order of magnitude.

SWCNT are usually synthesized as a blend that contain both metallic and semiconducting CNT species. As most optoelectronic applications require the solely use of s-SWCNT, the removal of metallic SWCNT and/or catalyst residues is therefore mandatory. To this end, several separation methods including density gradient ultracentrifugation<sup>26</sup> (DGU), dielectrophoresis<sup>27</sup> or extraction using aromatic polymers<sup>28</sup> have been developed. To further increase their performance, some devices must also incorporate s-SWCNT with specific diameter and chirality. S-SWCNT that display spectral signature in the wavelength window around 1.55  $\mu$ m would be for example highly desirable for devices dedicated to optical communications. The selective extraction of corresponding large-diameter ( $\phi$ ~1.3nm) s-SWCNT produced by laser vaporization (LV) has been demonstrated<sup>29,30</sup> using polyfluorene-based polymers.

Recent studies have shown the possible integration of light emitting SWCNT onto waveguiding structures<sup>23,31,32</sup>. In that case, luminescence has to couple into the bus waveguide in order to be collected and this coupling efficiency has been estimated at 10 % and 50% in ref. 31 and 32 respectively. Despite appealing, the electrically-stimulated SWCNT light detected in ref. 32 is said also to originate predominantly from black-body radiation of metallic SWCNT rather than from excitonic transitions of s-SWCNT. To increase the efficiency of such devices, the incorporation of light-emitting s-SWCNT inside the waveguide could be an alternative approach. In this paper, we report the fabrication of planar and ridge waveguides of polymers containing selected chiralities of s-SWCNT in the guiding layer. The fabrication steps of these structures are compatible with CMOS processes and could therefore be integrated in silicon photonics technology. Optical characterizations are presented and guided photoluminescence in such structures is demonstrated.

## **SWCNT** produced

by laser vaporization (LV) at 1125°C were dispersed with poly[(9,9-dihexyl fluorenyl-2,7-diyl)-co-(9,10-anthracene)] (PFH-A) in toluene at the concentration of XXX (to be confirmed by NREL). PFH-A has been shown to selectively wrapped large-diameter SWCNT<sup>29</sup> and the resulting solution is

composed of narrow CNT chirality distributions consisting primarily of near-armchair semiconducting species. The growth temperature of the LV synthesis (1125°C) was chosen as it favors an enrichment in large-diameter s-SWCNT and particularly the (10,8) chirality whose  $S_{11}$  transition lies in the broadly used telecommunication wavelength window around 1.55  $\mu$ m.

PFH-A/CNT films were deposited on different  $1\times1$  cm<sup>2</sup>-substrates (Si, 5  $\mu$ m-thick benzocyclobutene (BCB) on Si and 5  $\mu$ m-thick thermally grown SiO<sub>2</sub> on Si). For all these samples, the PFH-A/CNT solution (60 $\mu$ L) was spin-coated at low spin speed followed by hard baking under ambient atmosphere at 200°C for 5 minutes.

For ridge waveguide fabrication, the following additional processing steps were required. A thin  $SiO_2$  layer was first sputtered on the PFH-A/CNT film by plasma-enhanced chemical vapor deposition (Plassys MP550S) before Shipley S1805 photoresist spin-coating. The  $SiO_2$  layer acts as a protection layer and prevent any possible damage on the PFH-A/CNT film by the photoresist solvent. After soft-baking, a classical photolithographic process was then used for waveguide definition on a Süss Microtec MJB4 mask aligner. PFH-A/CNT ridge waveguides were patterned using the reactive ion etching (RIE) technique by exposing the layer to two successive  $SF_6$  and  $O_2$  plasmas at low pressure (Corial 300R reactive ion etching equipment). In situ monitoring of the dry etching was achieved by reflectometry. Figure 1 shows that vertical sidewalls are achieved with this procedure. Under the optimized etching conditions (125W, 10 mTorr, 25 sccm  $O_2$ ), no lateral undercuts are observed and the etch rate of the PFH-A/CNT film was typically around 100 nm/minute. A 100nm-thick  $SiO_2$  capping layer was finally sputtered to protect the PFH-A/CNT waveguides. The RMS roughness was measured at each stage of the technological process to reach  $^\sim$ 15 nm after the second  $SiO_2$  protection layer sputtering.

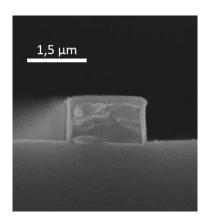


Figure 1 : Scanning electron microscope image of a PFH-A/CNT ridge waveguide cross section after the SiO<sub>2</sub> protection layer deposition on the CNT-based core layer.

Photoluminescence (PL) measurements were performed on PFH-A/CNT films at room temperature using a continuous wave Ti:Sapphire laser (Coherent 890) as the excitation source and an optical spectrum analyzer (OSA - Ando AQ-6315E) for signal detection. The two-dimensional photoluminescence excitation (PLE) contour plot displayed in Figure 2 was generated by recording the PL spectra of the PFH-A/CNT film on Si as a function of the excitation wavelength. The excitation wavelength was tuned around the absorption energy of the S<sub>22</sub> transition whereas luminescence was detected at wavelengths corresponding to the E<sub>11</sub> transition. The PL spectra were recorded every 3 nm in the 845-935 nm wavelength range. This PLE map exhibit clear spectral signatures of near-armchair s-SWCNT species (10,8) and (10,9) and confirms that s-SWCNT with large diameters are extracted using PFH-A. Due to the sensitivity of SWCNT optical transition energies on their surrounding dielectric environment<sup>33</sup>, SWCNT excitation (S<sub>22</sub>) and emission (S<sub>11</sub>) energies in the film are slightly red shifted compared to those observed in toluene<sup>29</sup> or assigned by Weisman *et al.*<sup>34</sup>.

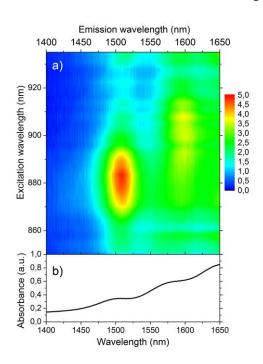


Figure 2: a) PLE map of a PFH-A/CNT film on Si, b) absorption of PFH-A/CNT film deposited on glass

Absorption spectrum of a PFH-A/CNT film on glass substrate in the near infrared region is displayed in Figure 2b. An extended absorption curve of PFH-A/CNT dissolved in toluene can be found in ref. 29. The three peaks observed in this spectrum around 1500, 1575 and 1650 nm correspond respectively to the  $S_{11}$  absorption energy of a few specific chiralities of s-SWCNT selected by PFH-A namely (10,8), (10,9) and (11,9) species. The luminescence of the latter s-SWCNT of (11,9) chirality cannot be seen on the PLE map displayed in Figure 2a. The (11,9) chirality s-SWCNT PL should have been observed around 1650 nm for an excitation wavelength of  $\sim$ 960 nm<sup>29</sup> but was not be recorded

due to the detector bandwidth limitations and because the excitation wavelength was not tuned down to its  $E_{22}$  energy.

Refractive indexes of the PFH-A/CNT films were measured at different wavelengths (632, 980, 1320 and 1550nm) using the prism coupling technique on a Metricon 2010/M system. Using a two-parameter fitting procedure, this technique allows to simultaneously determine the refractive index and thickness of a film provided multimodal optical propagation in the film at the wavelength injected through the prism. As thick films were difficult to achieve due to the low viscosity of the PFH-A/CNT solution, multimodal behavior of the waveguide could only be achieved at 632 nm. Thicknesses obtained from the fitting procedure in the red part of the electromagnetic spectrum were therefore used as a fixed parameter to adjust the curves recorded in the infrared. These thicknesses were later confirmed by profilometry (Veeco Dektak 150 surface profiler) after the technological processing of ridge structures. M-lines measurements were performed on multiple locations on films deposited onto different substrates. The results are summarized in Table I. Refractive index uncertainties are below  $5 \times 10^{-3}$  at each wavelength and may be slightly higher than expected values for the M-lines technique due to the thinness of the film and film thickness and/or CNT loading non-uniformities.

Wavelength	632 nm	980 nm	1320 nm	1550 nm
$n_0$	1,683	1.645	1.633	1.630

Table I: Linear refractive index (n<sub>0</sub>) of PFH-A/CNT films at different wavelengths

From these refractive index values, optical field distributions of the propagating modes and their corresponding effective indices were computed at 1550 nm for TE and TM polarizations as a function of the waveguide width using the film mode matching (FMM) method of a commercially available software (FIMMWAVE from Photon Design). These calculations were performed by considering a  $SiO_2$  lower cladding and a waveguide height of 1  $\mu$ m corresponding to the spin-coated PFH-A/CNT film thickness surrounded by a 100 nm-thick  $SiO_2$  layer ( $n_{SiO_2}$ =1.446). From the simulated dispersion curves plotted in Figure 3a, it can be seen that the waveguide supports multimodal propagation for width larger than 2.3  $\mu$ m for both TE and TM polarizations.

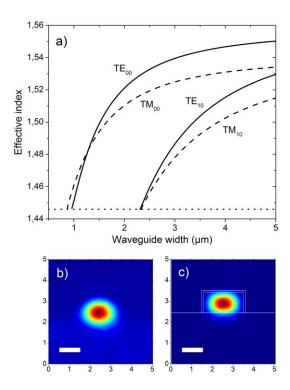


Figure 3 : a) Simulated effective indexes for the fundamental and first excited TE and TM modes as a function of waveguide width at  $\lambda$ =1.55 $\mu$ m. The solid and dashed lines correspond to TE and TM polarizations, respectively, the dotted line represents the SiO<sub>2</sub> refractive index. b) Measured near-field intensity mode profile of a 2  $\mu$ m-wide ridge waveguide (the scale bar is 1 $\mu$ m) and c) Simulated intensity distribution of the TE<sub>00</sub> mode for the same waveguide at a wavelength of 1550 nm.

Infrared light propagation was first demonstrated by in-coupling a 1.55  $\mu$ m-broadband source using a microlensed fiber to ridge waveguides of different widths and imaging their output facet on an infrared camera (Hamamatsu C10633) through a high magnification and high numerical aperture microscope objective. The polarization was not controlled. Figure 3b shows the recorded near field pattern of the output light from a 2  $\mu$ m-wide PFH-A/CNT ridge waveguide with a SiO<sub>2</sub> lower cladding. It confirms the monomodal nature of propagation in the ridge structure for width smaller than 2 $\mu$ m. The mode diameters were measured to 2 × 1.5  $\mu$ m<sup>2</sup> (1/e<sup>2</sup> intensity in horizontal and vertical directions respectively) in good agreement with the calculated value of 1.98  $\mu$ m × 1.31  $\mu$ m (Figure 3c) To record guided luminescence from PFH-A/CNT ridge structure on SiO<sub>2</sub> substrate, the camera was then replaced by a large core diameter multimode fiber connected to an OSA. To limit the region from which the PL could be collected and to prevent the detection of light scattered from the surface, a diaphragm and a long-pass filter were placed between the objective and the fiber.

Alignment between waveguide output, objective and collecting fiber was then optimized. The guided

PL measurements on ridge waveguides were performed at room temperature using a tunable

Ti:Sapphire laser operating between 850 and 935 nm. This laser beam was focused under normal incidence on the ridge top surface to obtain a spot size diameter of  $^{\sim}50\mu m$  at a distance of several hundreds of micrometers from the output facet.

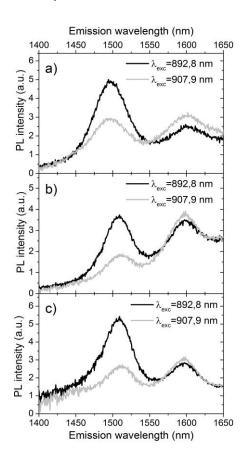


Figure 4 : a) guided PL spectra of 25  $\mu$ m-wide PFH-A/CNT ridge waveguide excited at 892.8 and 907.9 nm, b) PL spectra of PFH-A/CNT films excited at the same wavelengths, c) Calculated guided PL spectra from the PL spectra and absorption curve of PFH-A/CNT films

Figure 4a displays typical guided PL spectra from s-SWCNT with (10,8) and (10,9) chiralities in a 25 x 1  $\mu$ m<sup>2</sup> PFH-A/CNT ridge waveguide recorded for two different excitation wavelengths equal to 892.8 and 907.9 nm respectively. The spectra are corrected form the system response. However, significant differences in the relative intensities of the (10,8) and (10,9) s-SWCNT emission are clearly observed between the guided PL spectra and those obtained from the original films (Figure 4b). The ratio of peak PL intensities corresponding to the S<sub>11</sub> transition of the (10,9) species (~1600nm) and the (10,8) chirality (~1500 nm) changes drastically between these two experiments. The reduction of the PL at longer wavelengths around 1600 nm is more pronounced comparatively to that of at shorter wavelengths. Waveguide losses arising from the technological processing cannot explain such differences between 1.5 and 1.6  $\mu$ m. These changes of spectra shape can however be understood by taking into account the absorption spectra shown in Figure 2b. Indeed, as light emitted by the s-

SWCNT propagates towards the waveguide end, it is partly absorbed. As PFH-A/CNT absorption is higher at longer wavelengths, those will be more affected by the absorption through the propagation. To confirm this assumption, the PL spectra from PFHA-CNT films excited at 892.8 and 907.9 nm were divided by the absorption curve of PFH-A/CNT films (Figure 4c). The very similar shape of the resulting spectra with those recorded during guided PL experiments (Figure 4a) is a clear indication that s-SWCNT luminescence has effectively been guided in the ridge structure.

Fabrication process of planar and ridge waveguides made of s-SWCNT dispersed in fluorene-based polymers on different substrates have been described. Absorption and PL measurements on thin films incorporating selected s-SWCNT were measured. Guiding properties of PFH-A/CNT ridge waveguides at 1550 nm were simulated and compared with a good agreement to experimental near-field imaging of optical modes propagating in the structure. Guided PL at telecommunication wavelengths from specific chiralities s-SWCNT is demonstrated and shows the potential applications of this material for future integrated active photonic circuits based on carbon nanotubes.

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