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Hydration and Ion Pairing in Aqueous Mg^{2+} and Zn^{2+} Solutions: Force Field Description Aided by Neutron Scattering Experiments and *Ab Initio* Molecular Dynamics Simulations

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Abstract

Magnesium and zinc dications possess the same charge and have an almost identical size. Yet, they behave very differently in aqueous solutions and play distinct biological roles. It is thus crucial to identify the origins of such different behaviors and to assess to what extent they can be captured by force field molecular dynamics simulations. In this work, we combine neutron scattering experiments in a specific mixture of H₂O and D₂O (the so-called null water) with *ab initio* molecular dynamics simulations in order to probe the difference in the hydration structure and ion pairing properties of chloride solutions of the two cations. The obtained data are used as a benchmark to develop a scaled charge force field for Mg²⁺ that includes electronic polarization in a mean field way. We show that using this electronic continuum correction we can describe aqueous magnesium chloride solutions well. However, in aqueous zinc chloride specific interaction terms between the ions need to be introduced to capture ion pairing quantitatively.

Introduction

Magnesium(II) and zinc(II) are both closed shell divalent cations with almost the same ionic radii (0.72 vs 0.74 Å),¹ with the hydration free energy of Zn²⁺ being slightly more negative than that of Mg²⁺.^{2,3} Structural experimental and computational studies suggest an octahedral hydration for Mg²⁺ with six water molecules in the solvent shell, while the hydration number is found experimentally to be slightly smaller (5.3) in non-ion-pairing zinc triflate solutions.⁴ Computational studies have reported a roughly octahedral hydration for Zn²⁺ in solution,^{5,6} but its hydration shell has been suggested to be more flexible than that of Mg²⁺.⁷

In molecular simulations using empirical force fields, where an ion is described by its charge and radius (typically via the Lennard-Jones potential) the two ions thus behave almost identically. Yet, in reality they never act interchangeably, even if they may in some biological

situations bind to common structural motifs, most notably porphyrines⁸—chlorophyll for magnesium and hemes for zinc. Typically, each of the two cations performs several unique and critical biological roles. For instance, Mg^{2+} plays a crucial role in the synthesis and biological function of ATP,^{9–11} while Zn^{2+} has a structural role in zinc fingers and is involved in insulin storage in pancreatic vesicles.^{12–14} It is, therefore, critical to establish the origins of such different behaviors and to determine whether these can be successfully captured by force field molecular dynamics (MD) simulations.

Divalent cations are known to represent a challenge for empirical force field calculations because of strong polarization and charge transfer effects.^{15–17} Previous works have shown that standard force fields using full integer charges on the divalent ions capture poorly ion pairing in ionic solutions.^{16,18} Effort has been made to refine divalent ion full charge force fields to describe both single ion and ion pair properties in halide salt solutions,¹⁹ but it was found necessary to use specific interaction parameters for the Mg^{2+} -anion interaction instead of the usual combination rule. A promising way to improvement is the use of the Electronic Continuum Correction (ECC), which consists in taking into account the fast electronic polarization in a mean field approach.^{16,20} This is numerically implemented by scaling the charges of the ions.²⁰ This approach has been shown in previous works to considerably improve the description of ion pairing in calcium chloride¹⁶ and calcium acetate¹⁸ ionic solutions; therefore, we seek here to develop a similar ECC description for magnesium and zinc.

The strategy adopted in the present work is to characterize first the structure of concentrated MgCl_2 and ZnCl_2 solutions with neutron scattering in order to assess the difference in the behavior of the two ions. Electrolyte solutions have been studied by x-ray and neutron diffraction for decades (see *e.g.* refs^{21–24}), realizing that the sheer number of correlations in the obtained total scattering patterns (10 for a simple salt solution) makes the data difficult to interpret. This led to the development of the technique of neutron diffraction with isotopic substitution (NDIS),²² in which the total neutron scattering patterns are obtained for

two chemically identical solutions differing only in isotopic compositions. The subtraction of these two scattering patterns yields data originating only from the hydration of the substituted nuclei. This approach has become one of the most powerful methods to gain structural insights into the behavior of ions in aqueous solution.^{4,23,25,26} While zinc has suitable (albeit expensive) isotopes for the NDIS technique, magnesium does not, which precludes the direct use of NDIS to compare the hydration of the magnesium and zinc ions. For this reason, we employ here a technique,²⁷ developed by one of us, which can provide insight into the hydration of small ions using solutions prepared with null water (*i.e.*, a mixture of D₂O and H₂O in proportions that cancel the scattering from hydrogens), without the need for multiple isotopes. This approach thus allows us here to directly compare structural properties of aqueous MgCl₂ and ZnCl₂.

The purpose of this work is to assess the quality of commonly used force fields against the newly obtained neutron scattering data and to use the latter as a benchmark for the development of ECC force fields for magnesium and zinc cations, following an analogous strategy as previously adopted for calcium.^{16,18} In addition, we characterize here at the molecular level the difference between the Mg²⁺ and Zn²⁺ interaction with chloride using *ab initio* MD simulations.

Methods

Experimental details

3 m solutions of magnesium and zinc chloride were prepared by direct dissolution of MgCl₂ (Sigma-Aldrich 99.9 % anhydrous) and ZnCl₂ (Sigma-Aldrich 99.999 % anhydrous) in null water, *i.e.*, a mixture of H₂O and D₂O in a molar ratio 1.78:1. This specific ratio of light and heavy water ensures that the average coherent neutron scattering length of hydrogen (which is negative for ¹H and positive for ²H) is zero, which in practice removes any contribution of the hydrogens from the neutron signal. Null water was prepared by the direct mixing

of H₂O (18 MΩ) and D₂O (Aldrich, 99.9 atom %). The samples were loaded into a null scattering titanium/ zirconium alloy cell. Total neutron scattering patterns were obtained at a wavelength of 0.5 Å on the D4C diffractometer²⁸ at the ILL in Grenoble (France). Each sample (null water, 3 m MgCl₂, and 3 m ZnCl₂) was measured for 6 hours. The data²⁹ were corrected for multiple scattering and absorption,³⁰ and normalized versus a vanadium standard. Three total structure factors were thus obtained, $S^W(Q)$, $S^{MgCl_2}(Q)$ and $S^{ZnCl_2}(Q)$ (for the null water, 3 m MgCl₂, and 3 m ZnCl₂ solutions, respectively). These can be expressed as a sum of pair-wise structure factors as follows (the experimental offset being subtracted so that the defined structure factors terminate at zero at long Q):

$$S^W(Q) = 0.0374S_{OO}(Q) - 0.0374, \quad (1)$$

$$\begin{aligned} S^{MgCl_2}(Q) = & 0.0337S_{OO}(Q) + 0.0120S_{OCl}(Q) + 0.0034S_{OMg}(Q) + 0.0011S_{ClCl}(Q) \\ & + 0.0006S_{ClMg}(Q) + 0.00008S_{MgMg}(Q) - 0.0508, \quad (2) \end{aligned}$$

$$\begin{aligned} S^{ZnCl_2}(Q) = & 0.0337S_{OO}(Q) + 0.0120S_{OCl}(Q) + 0.0036S_{OZn}(Q) + 0.0011S_{ClCl}(Q) \\ & + 0.0006S_{ClZn}(Q) + 0.0001S_{ZnZn}(Q) - 0.0511. \quad (3) \end{aligned}$$

Here, the prefactors (in barns) are obtained from the concentration and coherent scattering length of each nucleus.²⁴ Substraction of the null water reference provides the difference structure factors $\Delta S^{Mg-W}(Q)$ and $\Delta S^{Zn-W}(Q)$. The difference is taken such that the S_{OO} term would perfectly cancel if the water structure was identical in the pure water and in the salt solution:

$$\Delta S^{Mg-W}(Q) = S^{MgCl_2}(Q) - \frac{0.0337}{0.0374}S^W(Q), \quad (4)$$

$$\Delta S^{Zn-W}(Q) = S^{ZnCl_2}(Q) - \frac{0.0337}{0.0374} S^W(Q). \quad (5)$$

The residual Placzek effect³¹ was removed through Fourier filtering (see Supporting Information) to enable direct comparison with simulation results. A most straightforward comparison between the structure of MgCl₂ and ZnCl₂ solutions is obtained by taking the direct difference:

$$\Delta S^{Mg-Zn}(Q) = S^{MgCl_2}(Q) - S^{ZnCl_2}(Q). \quad (6)$$

The Q-space signals are Fourier transformed to obtain the corresponding signals in the r-space— $\Delta G^{Mg-W}(r)$, $\Delta G^{Zn-W}(r)$, and $\Delta G^{Mg-Zn}(r)$. Windows functions were applied to the Q-space data and two spurious peaks (at 8 and 11 Å⁻¹) due to noisy detectors were deleted before the Fourier transform to limit ringing artifacts. We checked that this did not affect the peak positions (see Supporting Information). Such pre-treatment of the data was not needed for $\Delta S^{Mg-Zn}(Q)$, since most of the experimental noise already canceled in the difference.

Computational details

We performed force field simulations of concentrated aqueous 3 m MgCl₂ and ZnCl₂ solutions in order to model the neutron scattering signals, $\Delta S^{Mg-W}(Q)$ and $\Delta S^{Zn-W}(Q)$. These were computed with different force fields and compared to the experimental data. The simulation box contained 5670 water molecules, 612 chloride anions, and 306 cations (Mg²⁺ or Zn²⁺). A reference simulation of pure water was also performed (with a unit cell containing 2165 water molecules). All the simulations were performed with the Gromacs5.1.1 software³² in the constant temperature/constant pressure (NpT) ensemble using the Parinello-Rahman barostat³³ with a 1 ps coupling constant and the velocity rescaling thermostat with a 0.5 ps coupling time. Periodic boundary conditions were used employing a Particle Mesh Ewald³⁴ treatment of long range electrostatic interactions with a 12 Å cutoff. Hydrogen containing bonds were constrained using the LINCS algorithm.³⁵ The simulation box was first equili-

brated for at least 100 ns before a 20 ns production run.

Water molecules were described using the SPC/E force field,³⁶ while a series of different force fields was used for the ions, in order to assess their performance in reproducing the neutron data. First, we used standard non-polarizable (full charges) force fields both for the chloride³⁷ and the cations, Mg^{2+} ³⁸ and Zn^{2+} .³⁹ It has been shown previously^{16,18,40,41} that, especially for divalent cations, the description of the solution structure improves significantly upon employing the so called Electronic Continuum Correction (ECC).^{16,20,40} This approach takes into account the fast electronic polarization in a mean field way by scaling the charges of all the ions by the inverse of the square root of the electronic part of water dielectric constant $1/\sqrt{\epsilon_{el}}$. The radius of each ion needs to be further slightly reduced compared to the original full charges model in order to recover the proper ion-water distances. We used in this work the previously developed ECC force field for the chloride anion,⁴¹ which was fitted against neutron scattering data of LiCl solutions. Two ECC force fields were developed for Mg^{2+} here; the first was adjusted to reproduce the Mg^{2+} -O distance previously reported in the literature (around 2.10-2.12 Å⁴²⁻⁴⁴) and used for force field parametrization,³⁸ while the second was fitted to the measured neutron scattering signal, which required the use of a smaller Mg^{2+} radius. A new ECC force field was also developed for Zn^{2+} . Since it did not capture the ion pairing in the ZnCl_2 solution, we additionally defined a specific Zn^{2+} - Cl^- Van der Waals interaction with $\sigma_{\text{ZnCl}} = 2.6$ Å, fitted to reproduce the *ab initio* Zn^{2+} - Cl^- free-energy profile. The parameters of all the employed ionic force fields are summarized in Table 1. The Lorentz-Berthelot mixing rule was used to derive the mixed Lennard-Jones parameters from self-parameters.

We obtained further insight into the ion pairing properties of MgCl_2 and ZnCl_2 solutions by computing the free energy profiles along the cation-chloride distance using Born-Oppenheimer *ab initio* molecular dynamics (AIMD) simulations. These simulations were performed using the Quickstep module of the CP2K3.0 package⁴⁵ with the hybrid Gaussian and plane waves (GPWs) method. Due to the high computational cost of such calculations,

Table 1: Force field parameters for the different employed ion models.

| Ion | Force field | q (e) | σ (\AA) | ϵ (kJ/mol) |
|------------------|--------------------|-----------|---------------------------|---------------------|
| Cl ⁻ | Full ³⁷ | -1 | 4.417 | 0.4928 |
| | ECC ⁴¹ | -0.75 | 4.100 | 0.4928 |
| Mg ²⁺ | Full ³⁸ | +2 | 1.89 | 3.6610 |
| | ECC big | +1.5 | 1.55 | 3.6610 |
| | ECC small | +1.5 | 1.36 | 3.6610 |
| Zn ²⁺ | Full ³⁹ | +2 | 1.95 | 1.046 |
| | ECC | +1.5 | 1.75 | 1.046 |

the simulation box had to be rather small, containing one cation (Mg²⁺ or Zn²⁺) and one chloride together with 64 water molecules. The box sizes were determined from NpT simulations using the ECC classical force fields. All the AIMD simulations were performed in the NVT ensemble using a velocity rescaling thermostat (CSVR)⁴⁶ with a 50 fs time constant. We used the BLYP density functional^{47,48} with the D3M dispersion correction^{49,50} with a Becke-Johnson damping scheme,⁵¹ D3M(BJ). The same calculations were repeated with the older D2 dispersion correction,⁵² with the results being qualitatively consistent. (see Supporting Information). We used the DZVP-MOLOPT-SR-GTH double- ζ basis set,⁵³ optimized for the condensed phase, with GTH pseudopotentials⁵⁴ for the core electrons and a 400 Ry cutoff for the auxiliary plane wave basis.

The free energy profile along the cation-chloride distance was obtained using 23 (for Mg²⁺) and 27 (for Zn²⁺) umbrella sampling windows, the cation-chloride distance being restrained in each window by a harmonic potential around a fixed value moving from 2.3 \AA to 6.0 \AA . The initial configuration in each window was taken from the same umbrella sampling window equilibrated using a scaled charge force field. Each window was equilibrated for 5 ps before a 40 ps production run. A single free energy profile thus accumulates about 1 ns of sampling. Within such a timescale, given the very slow water exchange in the ion hydration shell,⁵⁵ the system does not have time to explore all the possible hydration geometries. In the barrier region between the contact and solvent-shared ion pair, where the number of water molecules in the cation hydration shell is expected to go from 5 to 6, we thus used several starting

points with different typical hydration geometries. The free energy profile was reconstructed from the biased umbrella sampling windows using the WHAM algorithm.⁵⁶ Error bars on the obtained profile were estimated by dividing each window in 8 blocks, independently evaluating the free energy profile on each block, and finally using as the estimate error the standard deviation (aligning the profiles at the top of the barrier) for the 8 blocks.

Results and Discussion

Neutron scattering from concentrated MgCl_2 and ZnCl_2 solutions

We obtained neutron scattering signals for 3 m MgCl_2 and ZnCl_2 solutions in null water as well as for a pure null water sample (Fig. 1). The total structure factors $S^{\text{MgCl}_2}(Q)$ and $S^{\text{ZnCl}_2}(Q)$ are dominated by water oxygen-oxygen correlations, with only a minor fraction of the signal corresponding to correlations involving the divalent cation (Eqs. 2 and 3). Subtraction of the null water reference (Eqs. 4-5) allows us to remove most of the water O-O correlation from the experimental signal. The only remaining water O-O contributions originate from the difference in water structure between pure water and the salt solutions, and thus characterize the influence of the salt on the surrounding water. The obtained difference structure factors, $\Delta S^{\text{Mg}-W}(Q)$ and $\Delta S^{\text{Zn}-W}(Q)$ (Fig. 2a), offer a very straightforward characterization of the hydration structure of Mg^{2+} and Zn^{2+} . Differences between the hydration structures of Mg^{2+} and Zn^{2+} are readily apparent in Q-space in the shape and frequency of the low-Q signal. These differences translate in r-space into markedly different peak positions and shape. The r-space signal for the MgCl_2 solution is mainly composed of two sharp peaks, located at 2.05 Å and 3.11 Å, and of a smaller well-defined peak at 4.15 Å. In contrast, the first peak for the ZnCl_2 solution is broader and shifted to 2.15 Å, while the second peak is very broad, extending between 2.9 and 3.9 Å. These features are likely due to significant ion pairing in the zinc chloride solution, as previously suggested.^{4,57,58}

In contrast, experimental studies^{38,44} show no sign of contact ion pairs between magne-

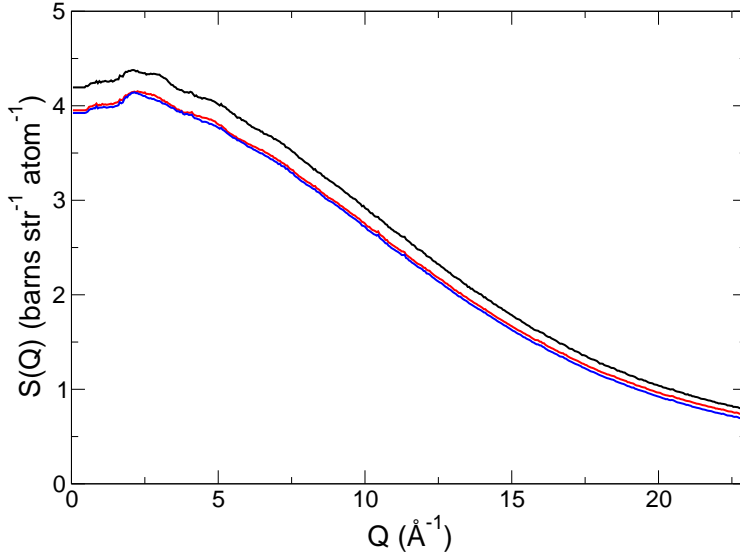


Figure 1: Raw total structure factor for null water $S^W(Q)$ (black), 3 m MgCl_2 in null water $S^{\text{MgCl}_2}(Q)$ (red) and 3 m ZnCl_2 in null water $S^{\text{ZnCl}_2}(Q)$ (blue).

sium and chloride ions in MgCl_2 solutions; the first peak of the neutron signal $\Delta G^{\text{Mg}-W}(r)$ can thus be readily assigned to the Mg-O distance. The presently obtained value of 2.05 Å falls within the range of experimental values, 2.0-2.12 Å, previously reported in the literature,^{42-44,59,60} but is shorter than the most recent neutron scattering estimate⁴⁴ of 2.10 Å. The position of the first peak is found here to be rather insensitive to the employed signal treatment. Namely, the use of different smoothing and window functions before the Fourier transform leads in r-space to peak positions in a narrow range of 2.03-2.05 Å. We note that while Ref⁴⁴ fits the total neutron scattering pattern, which is dominated by water-water contributions and where only a small fraction of the signal pertains to Mg-O correlations, our present experiment offers a more direct estimate of the Mg^{2+} -O distance.

Direct comparison between the MgCl_2 and ZnCl_2 solution structures is made possible by taking the difference between the two raw signals. This procedure allows us to cancel most of the experimental noise so that the obtained $\Delta S^{\text{Mg}-\text{Zn}}(Q)$ (Eq. 6 and Fig 2c) is a very direct characterization of the difference between the Mg^{2+} and Zn^{2+} hydration. The data is

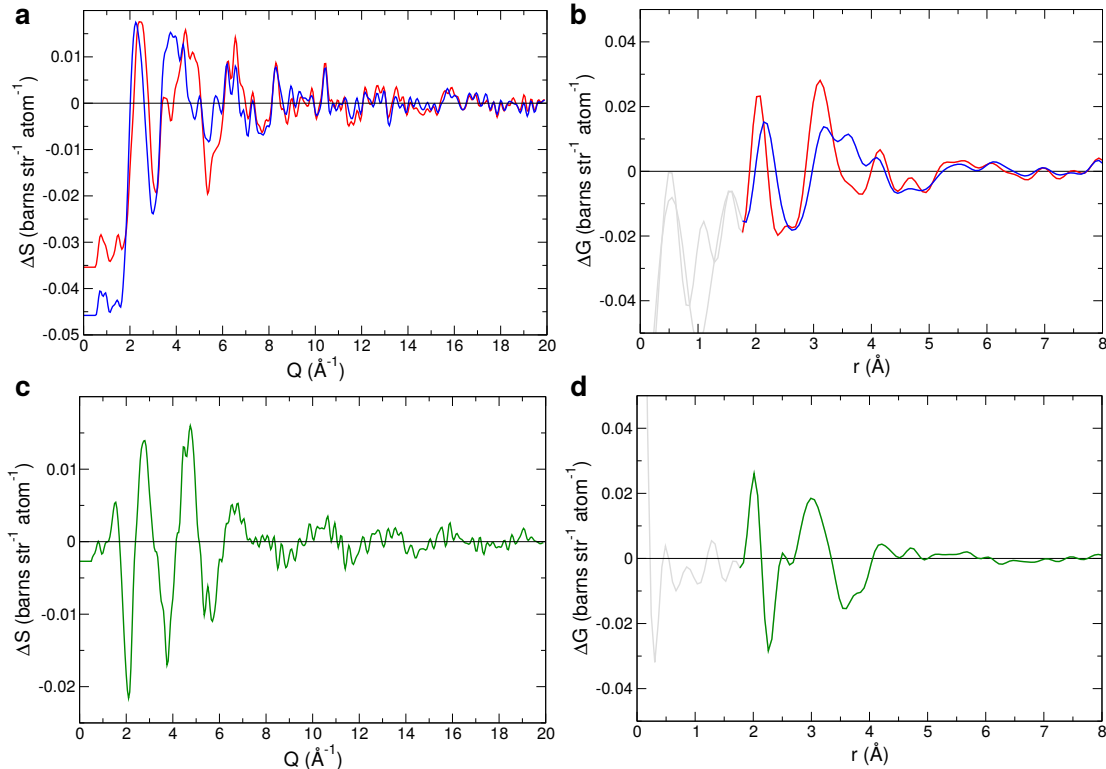


Figure 2: a) Difference structure factor $\Delta S^{Mg-W}(Q)$ (red) and $\Delta S^{Zn-W}(Q)$ (blue), together with b) the corresponding Fourier-transformed r-space signals $\Delta G^{Mg-W}(r)$ (red) and $\Delta G^{Zn-W}(r)$ (blue). c) Direct difference structure factor $\Delta S^{Mg-Zn}(Q)$ and d) the corresponding r-space signal $\Delta G^{Mg-Zn}(r)$.

so smooth that no signal treatment is needed to perform the Fourier-transform and obtain the r-space signal (Fig 2d). The resulting signal clearly shows a sharp positive peak around 2.05 Å and a sharp negative peak around 2.25 Å.

Refining Mg^{2+} and Zn^{2+} ECC force fields

Comparison of the experimental neutron scattering patterns to those computed from molecular simulations forms a stringent test of the quality of the force fields used in molecular simulations. In particular, since most of the water-water correlations are canceled out in the first order difference, it represents a very sensitive probe of the ions' hydration. We now use this data as a benchmark for the development of scaled-charges ECC descriptions of

Mg^{2+} and Zn^{2+} . Note that such approach has been previously shown¹⁸ to better describe the interaction of aqueous calcium with biologically relevant anions.

In figure 3 we compare the experimental neutron scattering signal $\Delta S^{\text{Mg-W}}(Q)$ with that computed from MD simulations of the same concentrated system using different force fields (the experimental resolution is applied to the computed signal for a fair comparison). We first use a standard force field (Fig. 3a), where ions bear the usual integer charges (*i.e.*, +2 for Mg^{2+} and -1 for Cl^-). The shape of the simulated signal is qualitatively similar to the experimental one. It exhibits two sharp peaks—the first one corresponding to the Mg-O correlation, the second one to the remaining O-O correlations and the O-Cl correlations— and a third smaller peak at larger distance, which can be very clearly assigned to the correlation between two water oxygen atom in *trans* position around a Mg^{2+} cation. However, the computed Q-space signal exhibits a too high frequency compared to the experimental signal; this manifests as a phase shift. This corresponds in r-space to a significant shift to larger distances of all the peaks. We thus need to refine the original full charges force field by scaling the ionic charge and readjusting the ionic radius to obtain a scaled charge ECC force field with the proper Mg-O distance. In a first ECC model, we tune σ to obtain a 2.10-2.12 Å Mg-O distance, following the estimates obtained in previous works,⁴²⁻⁴⁴ labeling this model as "ECC big". Fig. 3b shows that this model improves the agreement with neutron scattering compared to a full charge force field. However, the Q-space signal is still slightly out of phase and the r-space peaks are found at too large distances. Reducing the Mg^{2+} van der Waals radius σ by about 12 % ("ECC small") allows us to obtain an extremely good agreement with the experimental signal both in Q- and r-space (Fig. 3c).

We follow the same parametrization strategy for the Zn^{2+} ion, which is at first sight structurally very similar to Mg^{2+} (*i.e.*, they possess the same charge and practically the same ionic radius). Fig. 4a demonstrates that the standard full charges description does not capture any of the specificities of the experimental ZnCl_2 neutron scattering pattern. Rather, the computed r-space signal is composed of two sharp peaks and a third smaller

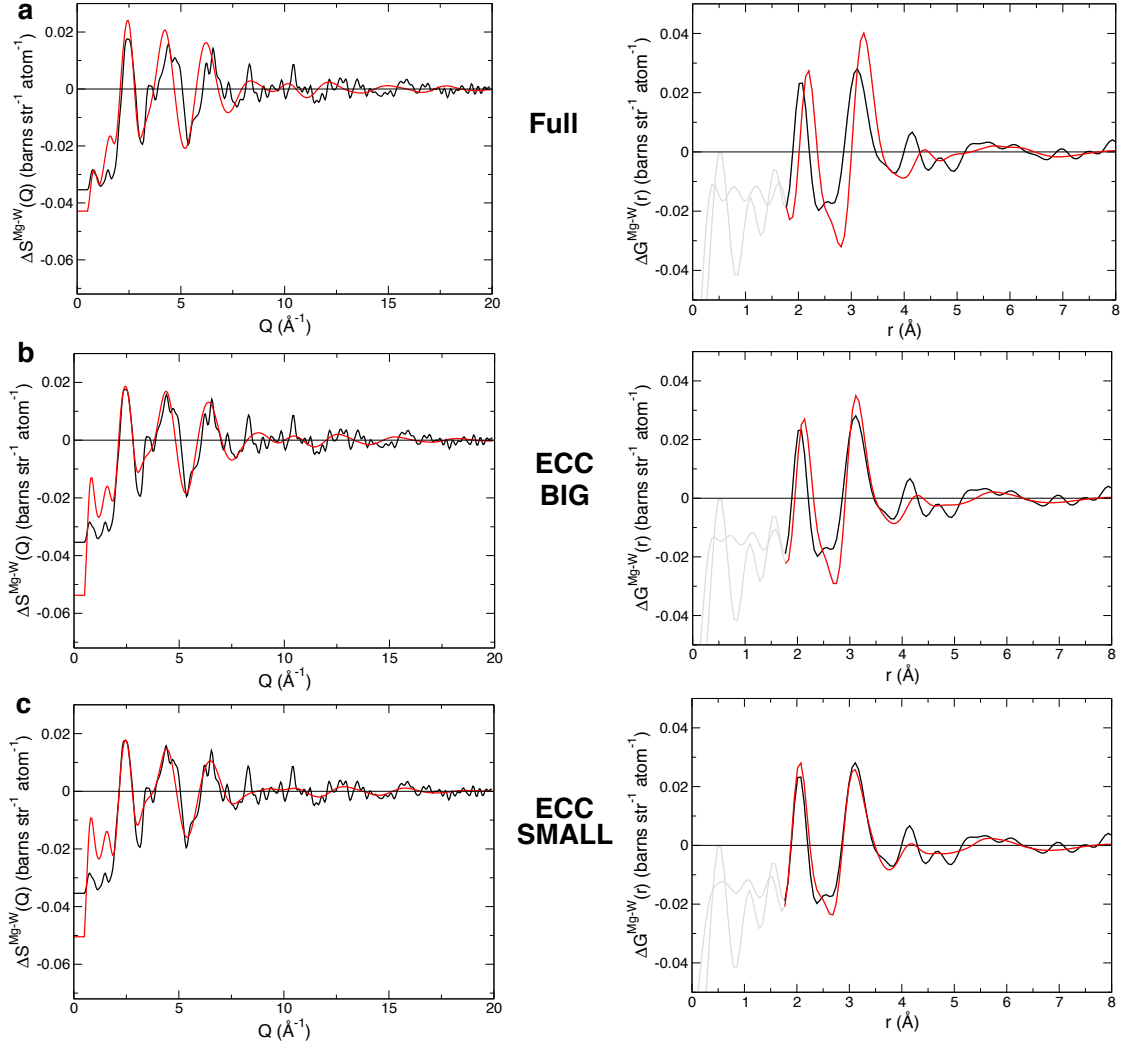


Figure 3: Comparison between the experimental (black) direct difference structure factor $\Delta S^{Mg-W}(Q)$ in Q -space (left hand side) and $\Delta G^{Mg-W}(r)$ in r -space (right hand side) with that obtained with a) the full charges, b) the "ECC big" and c) the "ECC small" force field for Mg^{2+} .

well-defined peak, very similar to what we obtained for MgCl_2 . The model does not capture the characteristic broadening of the peaks observed for the ZnCl_2 solution, which means that classical Zn^{2+} force fields do not provide a good description of the zinc ion. We now use the neutron scattering data as a reference to try to develop a scaled charge ECC description of the zinc cation, reducing the ionic size to recover a Zn-O distance of 2.10 \AA , which is in the range of experimental values found in the literature.^{4,61,62} In this case, the use of a scaled

charges ECC description has almost no influence on the structure of the solution as captured by the neutron scattering signal.

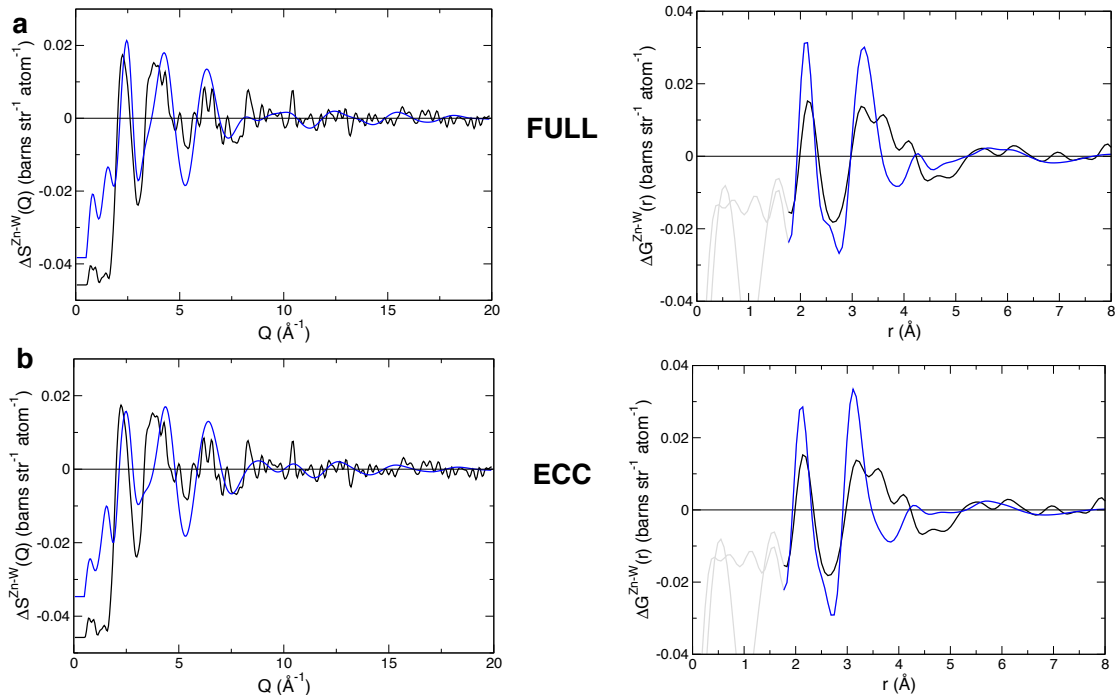


Figure 4: Comparison between the experimental (black) direct difference structure factor $\Delta S^{Zn-W}(Q)$ in Q-space (left hand side) and $\Delta G^{Zn-W}(r)$ in r-space (right hand side) with that obtained with a) the full charges and b) the "ECC" force field for Zn^{2+} .

Several previous experimental results indicated the presence of strong ion pairing in $ZnCl_2$ solutions.^{4,57,58} In contrast, none of our simulations (neither full charges nor ECC) show formation of $Zn^{2+}Cl^-$ ion pairs. We further investigate this ion pairing by computing the free energy profile along the $Zn^{2+}-Cl^-$ distance using *ab initio* MD simulations and compare it with that obtained with the above force fields (Fig. 5). We also contrast these results with those obtained for the $Mg^{2+}Cl^-$ ion pair in order to identify the key differences between the aqueous behavior of the zinc and magnesium cations to be captured in the force field simulations.

Comparison of the *ab initio* free energy profiles for the magnesium and zinc chloride ion pairs immediately reveals significant differences between $MgCl_2$ and $ZnCl_2$ solutions, despite

the relatively large error bars due to short simulation times and issues with sampling different hydration geometries at the barrier region. While the $\text{Mg}^{2+}\text{Cl}^-$ contact ion pair (CIP), at a interionic distance of 2.55 Å, is about 9 kJ/mol higher in free energy than the solvent shared ion pair (SShIP), the $\text{Zn}^{2+}\text{Cl}^-$ CIP is found at a much smaller distance of 2.25 Å and is about 4 kJ/mol more stable than the SShIP. This means that we do not expect significant contact ion pairing in MgCl_2 solutions, while the formation of $\text{Zn}^{2+}\text{Cl}^-$ ion pairs is strongly implied. Moreover, higher coordination zinc chloride complexes, *i.e.*, ZnCl_2 , ZnCl_2^- , ZnCl_3^{2-} , and ZnCl_4^{3-} are likely to exist too, as suggested in the literature.^{4,57,58}

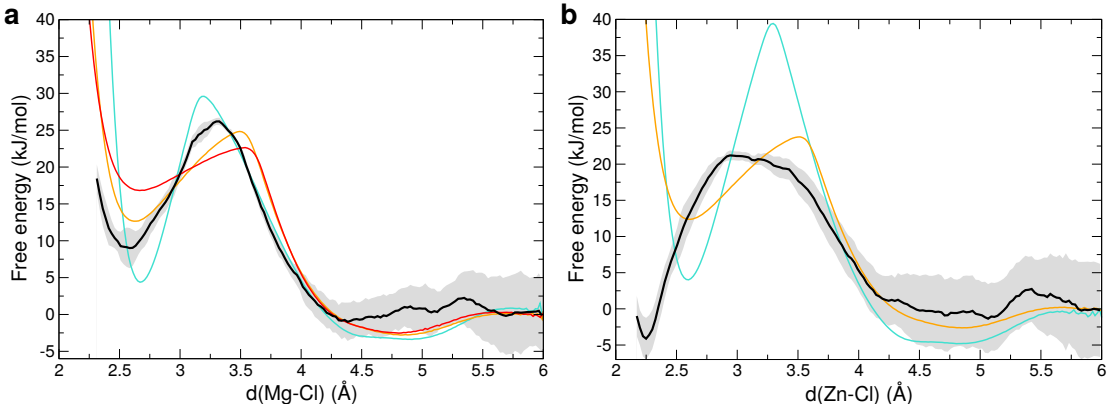


Figure 5: a) Free energy profile along the $\text{Mg}^{2+}\text{-Cl}^-$ distance using *ab initio* MD (black), and the full charges (cyan), the "ECC big" (orange) and the "ECC small" (red) force fields. b) Free energy profile along the $\text{Zn}^{2+}\text{-Cl}^-$ distance using *ab initio* MD (black), and the full charges (cyan) or the ECC (red) force field

All the studied Mg^{2+} force fields are in qualitative agreement with the AIMD reference, with all of them finding the CIP much higher in free energy than the SShIP, which thus leads to negligible contact ion pairing in concentrated solutions. Even after a long equilibration of our concentrated solutions, we do not observe a single $\text{Mg}^{2+}\text{Cl}^-$ contact ion pair. The present "ECC big" Mg^{2+} force field provides the best agreement with the AIMD profile in terms of the barrier height and relative free energy of the CIP and SShIP. It, however, does not provide the best fit with the neutron scattering experiment, which implies the use of a smaller Mg^{2+} . At this point it is interesting to note that the *ab initio* MD simulation yields

an optimal Mg-O distance of 2.10 Å (corresponding to the first peak in the magnesium-water radial distribution function), which is consistent with previous works⁶³⁻⁶⁶ but larger than the 2.05 Å value determined from the neutron experiment. We thus tested the influence of the employed level of electronic structure theory on the geometry of a $\text{Mg}(\text{H}_2\text{O})_6^{2+}$ cluster (see Supporting Information, Table S1). We found variations of up to 0.04 Å of the Mg-O distance with the level of theory and size of the basis set. These tests suggested that the BLYP-D3M(BJ) level of theory used in our AIMD simulations may slightly overestimate the Mg-O distance; however, the use of more advanced methods is at present computationally too expensive to be employed in condensed phase simulations.

While all the employed magnesium force fields provide at least a qualitative agreement with the reference AIMD profile, none of the zinc force field correctly captures the remarkable stability of the contact ion pair. Hence, we find no contact ion pairs in our force field simulations of concentrated ZnCl_2 solutions, while AIMD and experiments clearly indicating their presence. Another problem is that both force fields find an interionic distance for the (energetically unfavorable) contact ion pair around 2.6 Å, similar to what was obtained for magnesium but much higher than the reference AIMD distance of 2.25 Å. Additionally, the full charge force field overestimates the barrier between the SShIP and the CIP by about 20 kJ/mol, while this barrier is reproduced within a couple of kJ/mol with the ECC description. Comparison with the free energy profile obtained using the fully polarizable force field AMOEBA⁶⁷⁻⁶⁹ (see Supporting Information) shows that the results obtained with the ECC and AMOEBA force fields are very similar to each other and that the specific character of the Zn-Cl ion pairing is not captured even with an explicit description of the electronic polarization. This, together with the very short Zn-Cl distance in the CIP, suggests that the observed effects are due to specific electronic interactions between the ions.

We further investigate the interaction of Zn^{2+} with the chloride anion by analyzing the distribution of the distances between the chloride anion and the localized Wannier orbital center (WOC)⁷⁰ corresponding to the chloride-cation bond (Fig. 6a). The WOC is clearly

located further away from the chloride (hence closer to the cation) in the zinc ion pair than in that with magnesium, which is indicative of a more covalent interaction in the former case. In addition, we note that the zinc hydration at the SShIP and further is found to be more flexible than that of magnesium, with an average zinc coordination number slightly below six (Fig. 6b). At short distances, the chloride anion replaces exactly one water molecule from the Mg^{2+} solvation shell, so that it remains perfectly octahedral (Fig. 6c). In contrast, the hydration number of zinc in the CIP falls down to three, with the solvation shell adopting a tetrahedral geometry (Fig. 6d). Such changes in the zinc hydration shell are not captured by any of the tested force field, which all exhibit a behavior more similar to Mg^{2+} than to Zn^{2+} .

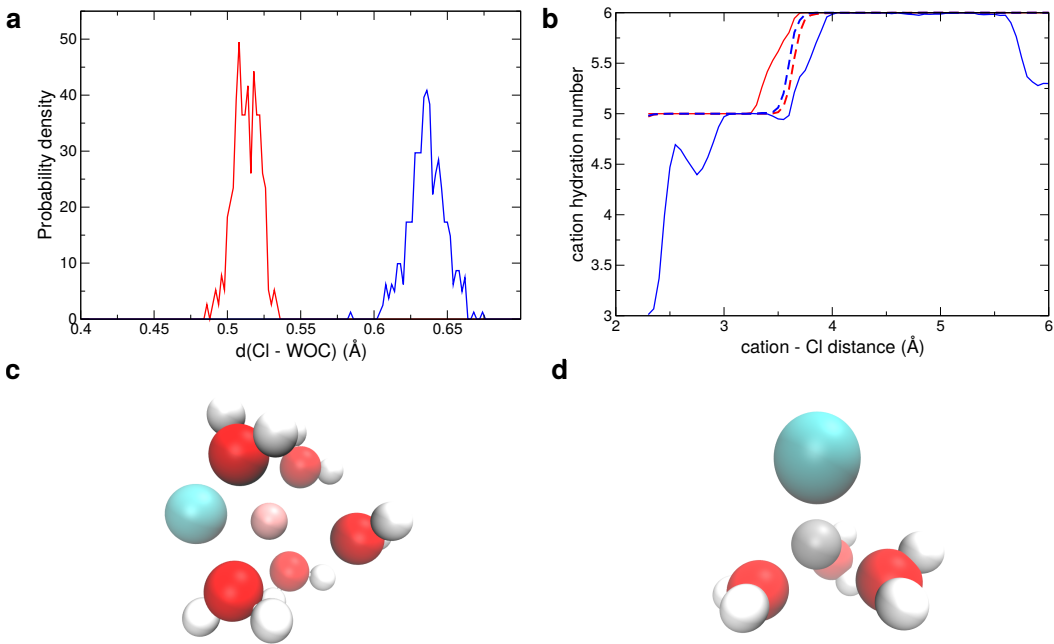


Figure 6: a) Distribution of distances between the chloride anion and the WOC describing the cation-chloride interaction. b) Hydration number (defined as the number of water molecules within 3.0 Å of the cation) of Mg^{2+} (red) and Zn^{2+} (blue) as a function of the cation-chloride distance, obtained from AIMD (solid lines) and ECC force field simulations (dashes). Representative snapshot of c) the magnesium chloride and d) the zinc chloride ion pairs.

In order to describe better the hydration structure and the ion pairing for zinc in the

force field simulations, we introduce a specific Lennard-Jones interaction between zinc and chloride ($\sigma_{ZnCl} = 2.6 \text{ \AA}$), which is adjusted to reproduce the AIMD free energy profile along the Zn-Cl distance (Fig. 7a). While no ion pairs are found with the original ECC force field in a concentrated 3 m $ZnCl_2$ solution, the addition of the specific Zn-Cl interaction leads to the formation of numerous zinc chloride complexes, with 15 % of the zinc ions being involved in a $ZnCl_4^{2-}$ complex, 9 % in a $ZnCl^+$ complex, 7.5 % in a $ZnCl_3^-$ complex, and less than 1 % in a $ZnCl_2$ complex (Fig. 7b). The computed neutron scattering signal $\Delta S^{Zn-W}(Q)$ (Fig. 8) is in much better agreement with the experiment than the original ECC force field, with a sizable broadening in the r-space of the second peak, corresponding to Cl-Cl correlations around a zinc ion. However, the first peak remains too sharp and the second peak is still not broad enough compared to the experiment.

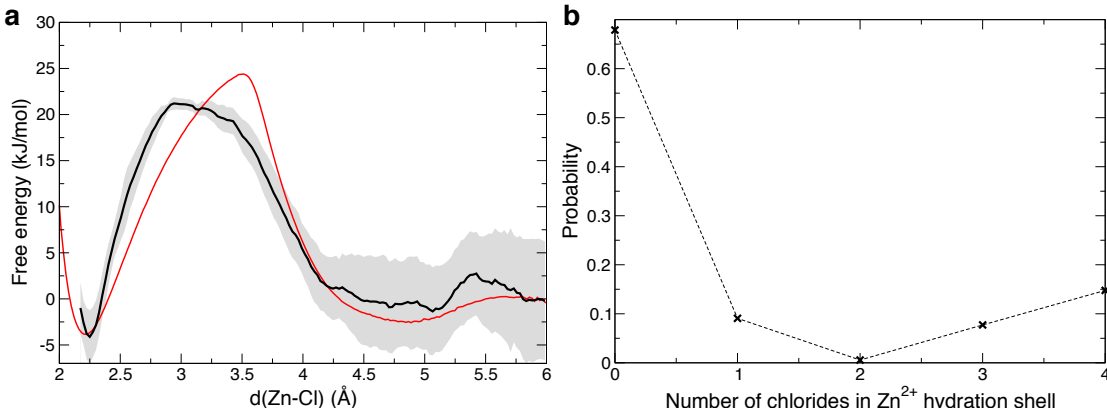


Figure 7: a) Free energy profile along the zinc chloride distance from *ab initio* MD simulations (black) and force field simulations using the ECC description of Zn^{2+} with an additional specific Zn^{2+} - Cl^- interaction. b) Probability distribution of different zinc chloride complexes as obtained from force field simulations with the ECC description of Zn^{2+} with an additional specific Zn^{2+} - Cl^- interaction.

As a next step, we took 10 different snapshots from a simulation using the above force field (employing a small box of 92 water molecules, 5 Zn^{2+} and 10 Cl^-) where we observe a range of different zinc chloride complexes, and ran from each of these starting points a 20 ps AIMD simulation. This allowed for the relaxation of the different bond distances and of the hydration geometries of the ions. The neutron scattering signal computed from these

10 AIMD simulations now compares extremely well with the experiment, with the proper shape and size of the first peak in r-space (Zn-O correlation) and a very broad second peak (Fig. 8b). The improvement in the neutron signal is primarily due to the relaxation of the Zn-Cl distance, which is found to be shorter with our force field than in the AIMD simulation of the concentrated ZnCl_2 solution (2.15 Å vs 2.25-2.30 Å). Since the amount of ion pairing and nature of the observed complexes does not change within the timescale of the AIMD simulation, the extremely good agreement with the experiment shows that our ECC Zn^{2+} force field with a specific Zn-Cl interaction correctly captures the amount of ion pairing in the solution.

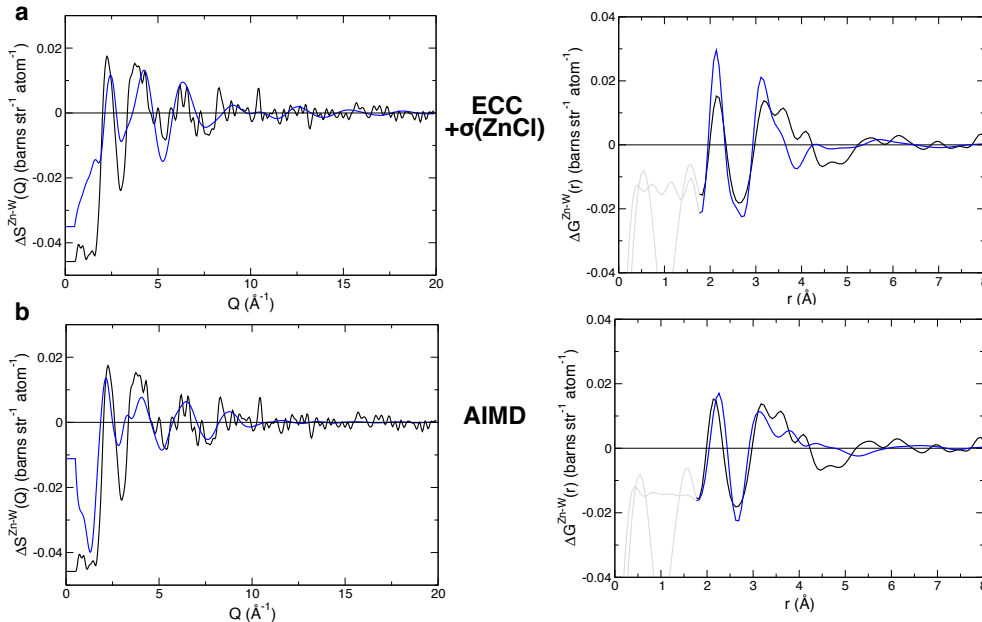


Figure 8: Comparison between the experimental (black) direct difference structure factor $\Delta S^{Zn-W}(Q)$ in Q-space (left hand side) and $\Delta G^{Zn-W}(r)$ in r-space (right hand side) with that obtained with a) the ECC force field with a specific σ_{ZnCl} and b) after short *ab initio* MD equilibration of the geometries.

Finally, we compute the neutron scattering signal $\Delta S^{Mg-Zn}(Q)$ using our best ECC force fields for Mg^{2+} and Zn^{2+} and compare it with the experimental data and with the signal computed with the original full charge force field (Fig. 9). As we already noted, the $\Delta S^{Mg-Zn}(Q)$ and $\Delta G^{Mg-Zn}(r)$ experimental signals are obtained with only minimal data

treatment, and are thus a direct measure of the difference in solvation properties of zinc and magnesium ions. The standard force field performs extremely poorly, with a totally out of phase Q-space signal and an opposite behavior of the difference in r-space. In contrast, our best ECC force fields (*i.e.*, "ECC small" for Mg^{2+} and the ECC with specific σ_{ZnCl} for Zn^{2+}) provide a good agreement with the experimental data, with proper Q-space phasing and correct peak positions in r-space.

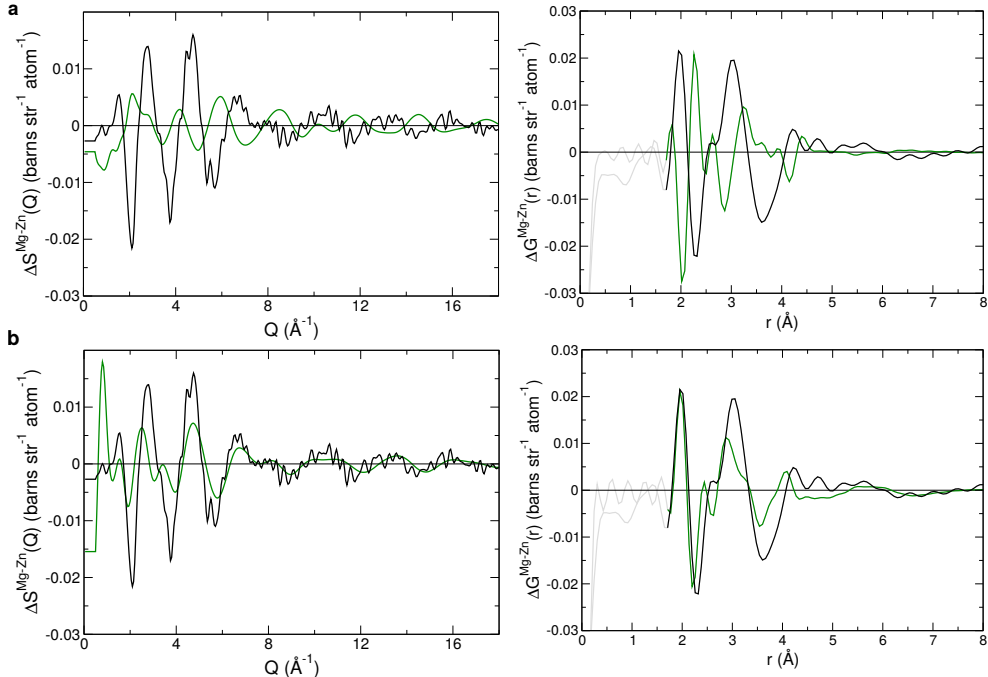


Figure 9: Comparison between the experimental (black) direct difference structure factor $\Delta S^{\text{Mg-Zn}}(Q)$ in Q-space (left hand side) and $\Delta G^{\text{Mg-Zn}}(r)$ in r-space (right hand side) with that obtained with a) the full charges or b) our best ECC force field ("ECC small" for Mg^{2+} and "ECC+ σ_{ZnCl} " for Zn^{2+}).

Conclusions

In the present work we have investigated the difference in hydration and ion pairing behaviors between Mg^{2+} and Zn^{2+} cations by combining neutron scattering experiments with *ab initio* and force field molecular dynamics simulations. The chosen experimental strategy, with

the use of null water solutions, allowed us to directly compare MgCl_2 and ZnCl_2 solution structures using exactly the same experimental setup for both cations, without the need for isotopic substitution on the cations. We took advantage of this newly obtained neutron scattering data—which notably provide a slightly smaller estimate of the Mg-O distance than previously determined—to assess the performance of standard force field in capturing the difference in behavior between Mg^{2+} and Zn^{2+} in aqueous solutions and to develop improved ECC (scaled charges) force fields for both ions. While we found that we could very well reproduce the Mg^{2+} experimental data with such a force field, no force field, neither standard nor ECC, could capture the specific behavior of the Zn^{2+} ion. We further analyzed the aqueous zinc chloride interaction with *ab initio* MD simulations, showing that Zn^{2+} forms very stable contact ion pairs with the chloride ion with a partly covalent character. The AIMD simulations also evidenced a change in the zinc hydration geometry from octahedral to tetrahedral upon ion pairing with the chloride anion. These differences are beyond polarization effects, and therefore, cannot be captured even by fully polarizable force fields. An improved description of the ZnCl_2 solution is obtained upon adding a specific interaction term between zinc and chloride ions, which allows us to recover the strong ion pairing and formation of various zinc chloride complexes.

Further testing of the newly developed ECC Mg^{2+} force field will be performed in future studies, in particular to assess the accuracy of the Mg^{2+} interaction with biomolecules. Future work will also consist in systematically assessing the ion pairing properties of Zn^{2+} with important biological motifs (*e.g.*, carboxylate groups or imidazole moieties). In particular, we will try to determine when the addition of a specific interaction term to the ECC force field (which was successfully tested here for the aqueous ZnCl_2 solutions) is required and whether it suffices to obtain a correct description of the ion-ion and ion-water interactions.

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Supporting Information Available

Additional information about the neutron scattering experiments, influence of dispersion correction on AIMD simulations, and comparison with the fully polarizable AMOEBA force field. This material is available free of charge via the Internet at <http://pubs.acs.org/>.

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