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Probabilistic and sensitivity analysis of analytical models of corrosion onset for reinforced concrete structures

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ABSTRACT

Chloride ingress and carbonation are the main factors leading to corrosion initiation of reinforced concrete (RC) structures. Lifetime assessment and maintenance optimization of these deteriorating structures has been based for several practical applications on analytical predictive models. The literature review shows that there are numerous analytical models of chloride ingress and carbonation. It was also found that comprehensive lifetime assessment requires that the selected models be able to propagate uncertainties in a correct manner. Thus, this paper proposes a methodology for probabilistic sensitivity analysis of analytical models for chloride ingress and carbonation. Given that different parameter notations were found for each model, a homogenization of notations and generic forms are first proposed. The sensitivity analysis is based on the following indicators: elasticity coefficient, Pearson coefficient, bias of the mean and standard deviation of the response of the model. The results highlighted which parameters are influential for each model by considering three concrete types. Overall results indicated a higher effect of the non-linearity of the models on the sensitivity indicators. It was found that the level of influence of each parameter depends also on the concrete type and the duration of the exposure to chlorides or carbon dioxide.

KEYWORDS

uncertainty, analytical models, sensitivity, carbonation, chloride ingress, reinforced concrete.

1. Introduction

Corrosion of steel reinforcement is a critical issue for many reinforced concrete (RC) structures; in particular, when they are located in chloride-contaminated environments and/or exposed to carbon dioxide (Tefamariam et al., 2018). Given the high alkalinity of concrete after construction, a thin passive layer of corrosion products protects steel

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bars against corrosion, and therefore, the structure is initially protected from corrosion attack. Corrosion of rebars generally starts due to: (i) the breakdown of this protective oxide layer wrapping the rebar (chloride ingress), or (ii) the decrease of pH of the pore solution (carbonation).

The study of corrosion onset mechanisms in RC contributes to: (i) the better understanding of the causes leading to corrosion, and (ii) the prevention or at least reduction of corrosion-induced damage (Winston Revie and Herbert H, 2008; Zhou et al., 2015). Both items are important for an optimal maintenance strategy based on inspection (condition assessment) and repair (damage mitigation). Nevertheless, in order to optimize the resources allocated to the maintenance strategy and reduce environmental impact and failure risks, the prevention of corrosion-induced damage seems preferable (Bastidas-Arteaga and Schoefs, 2012, 2015; Li, 2003). Thus, an efficient detection and/or a realistic prediction of the corrosion initiation time can contribute to the reduction of maintenance costs and failure risks.

The present study is carried out within the framework of the ANR-EVADEOS project¹. The main purpose of this project was to develop an engineering-oriented approach for preventive maintenance optimization of RC structures exposed to corrosion. It combines: non-destructive condition assessment, deterioration modeling, and inspection and maintenance optimization considering global uncertainties and allocated funds. Such an approach requires selecting degradation models with the following requirements:

- (1) they should be able to account and propagate correctly the uncertainties involved in the problem (material properties, exposure, etc) (Rakotovo Ravahatra et al., 2017; Yajun and Xianming, 2012), and
- (2) they should account for the availability of information and resources for parameters estimation.

The selection of models that account for these requirements is still a challenge. We focus in this study on analytical models because they are used in engineering and some research applications. This paper will therefore provides to users useful informations when using these models with respect to the following considerations. First, it is difficult to compare model outputs because models could use parameters obtained by different experimental tests whose accuracy are various (e.g., chloride diffusion coefficient estimated from migration test or chloride profiles). Second, although analytical models have a similar form, there is no a unified formulation of these models. Third, there is no comparison of the capacity of each model for propagating uncertainties for various materials and exposures. And fourth, the performance of each model when input information is more or less available is still unknown.

In this context, this paper aims at (i) providing unified formulations for chloride ingress and concrete carbonation models and (ii) perform a probabilistic sensitivity analysis to identify the more influencing parameters for each model.

The paper is organized as follows: section 2 provides an overview of models for corrosion onset assessment. Section 3 describes the summary and generalization of notations for several chloride ingress and carbonation models. Section 4 presents the studied material properties that were used in sections 5 and 6 for a sensitivity analysis based on four indicators: elasticity, Pearson coefficient, bias on the response mean, and standard-deviation of the response (Schoefs, 2008).

¹Non-destructive evaluation of the structures for damage prediction and optimization of the follow-up. Website: <http://www-lmdc.insa-toulouse.fr/evadeos/accueilevadeos.htm>

2. Overview of corrosion onset models

The assessment of the corrosion initiation time of RC structures is based on chloride ingress or carbonation predictive models. Literature review shows two major groups of predictive models: analytical (or semi-analytical) and numerical. The first group of models is expressed by analytical or empirical equations. For chloride ingress, they are frequently expressed as a function of an error function (Colleparidi et al., 1970; Euro-LightCon, 1999; JSCE, 2007; Petre-Lazar, 2001; DuraCrete, 2000; Tang and Gulikers, 2007). For carbonation, they are generally expressed in terms of a square root of time (CEB, 1997; Miragliotta, 2000; Papadakis et al., 1991; Petre-Lazar, 2001; DuraCrete, 2000; Ying-Yu and Qui-Dong, 1987). These analytical models were mainly developed for engineering purposes but they are still used for some research applications and require a reduced number of input parameters. However, the oversimplification of various physical phenomena (e.g., some of them neglect the time-dependency of model parameters or correlation between parameters) could affect the accuracy of their predictions.

In contrast, numerical models account for various physical phenomena – e.g. the consideration of the effects of heat and humidity transfers on chloride ingress or carbonation processes. Therefore, they provide more informations on their outputs. They are generally expressed by partial differential equations and require numerical methods (finite elements, finite differences, etc.) to be solved. Numerical models could lead to more accurate assessments of the corrosion initiation time; however, they require a larger number of model parameters (and experimental tests to characterize it) and vast end-user experience.

For Chloride ingress, we can find two major groups of numerical models: (i) those which are based on Fick’s law, that means without considering the interactions between chlorides and other ionic species (ii) those which depends on the law of Nernst-Planck, taking into account these interactions. We present in Table 1 and 2 the phenomena taken into account in some numerical models based on Fick’s and Nerns-Planck laws, respectively. For concrete carbonation, we present in Table 3 the phenomena taken into account in some numerical models.

Finally, the numerical model of Mai-Nhu (2013) takes into account simultaneously chloride ingress and concrete carbonation.

3. Summary of analytical models

3.1. Chloride ingress models

3.1.1. Unified formulation

Analytical models consider that chloride penetration through the porous network is mainly produced by the difference in chloride content between the surface and the core of concrete. The phenomenon is described as a pure diffusion process on a saturated concrete. These models also neglect the interaction between chlorides and other species in the pore solution. This simplifies the problem from ionic to molecular diffusion. Analytical models of chloride ingress are then simplified solutions of Fick’s second law and could be expressed as a function of the complementary error function erfc or the Mejlbro-Poulsen function Mejlbro (1996). This work only considers unidimensional solutions based on the complementary error function because they are more used in

practice. The general form of these models takes the following generic expression:

$$C(x, t) = C_s \operatorname{erfc} \left(\frac{x}{2\sqrt{\xi(\mathbf{X}, t)}} \right) + C_{ini} \quad (1)$$

where $C(x, t)$ is the chloride content [% wt. of concrete or % wt. of binder] at distance x from the concrete surface [m] and at time t [s], C_s is the chloride content at the concrete surface that could be constant or time-dependent [% wt. of concrete or % wt. of binder], $\xi(\mathbf{X}, t)$ is a general function of concrete diffusivity which depends on a vector \mathbf{X} of input parameters that are specific to each model and the time t [s]; depending on the models, concrete diffusivity could be constant or time-dependent, C_{ini} is the initial chloride content of the concrete [% wt. of concrete or % wt. of binder]. \mathbf{X} and $\xi(\mathbf{X}, t)$ are detailed in Table 4 for seven studied analytical models.

3.1.2. Model description and parameters

Figure 1 and Table 5 summarize the type of data required for each model. These input parameters can be classified into two levels. The parameters of level 1 can be provided directly by destructive or non-destructive testing or supplied in project archives (so-called “observables”). Any computation is necessary. The parameters of level 2 are deduced from level 1. The parameters of the second level are mostly used for chloride ingress modelling. This level includes material parameters (water content, apparent diffusion coefficients, etc.) or factors derived to account for the kind of exposure, aging, etc. The evolution of chloride profiles (output) is obtained by evaluating the parameters of this level that correspond to the components of the vector \mathbf{X} (eq. (1) and Table 4). Except one model that considers the effect of temperature (Petre-Lazar, 2001), the parameters of the second level will be mostly considered in the sensitivity analysis.

Analytical chloride ingress models can be classified into two classes according to its capability to account for time-dependency of input parameters:

- Class 1: models without time-dependent input parameters (Colleparidi et al., 1970; JSCE, 2007; Petre-Lazar, 2001).
- Class 2: models with time-dependent input parameters (EuroLightCon, 1999; DuraCrete, 2000; Tang and Gulikers, 2007).

3.1.3. Models without time-dependent input parameters

This category of models considers that all their input parameters are constant over time. Some of them account for uncertainties and the accuracy for determining their parameters, in a simplified way, through safety factors JSCE (2007). Other use empirical equations to account for interactions between ions or between chlorides and the concrete matrix Petre-Lazar (2001). Even if they are simpler, they are consistent with onsite discrete measurements in time, from which it is tricky to obtain time variant properties.

3.1.4. Models with time-dependent parameters

Various studies have shown that D_a is time-dependent (Maage et al., 1995; Mangat and Molloy, 1994; Sandberg, 1995; Takewaka and Mastumoto, 1998). Physically, concrete aging is due on the one hand to the micro-structure evolution caused by the continued

hydration of the cement and by carbonation. This causes a porosity reduction that slows down chlorides and CO₂ penetration. On the other hand, during the diffusion process, the difference between surface and bulk chloride contents is reduced along time till equilibrium. This implies that the gradient of chloride content decreases and thus also the kinetics of the diffusion process. Other studies revealed or accounted for the time dependency of C_s (Bastidas-Arteaga et al., 2011; Crank, 1975; Swamy et al., 1995; Uji et al., 1990). The consideration of these time-dependencies could improve corrosion initiation assessment.

Concerning the time-dependency of the chloride diffusion coefficient, three diffusivity definitions are found in the literature: instantaneous, average and achieved diffusivity.

Instantaneous diffusivity: is the value of the diffusion coefficient at each time step. An expression deduced by rapid diffusivity test is proposed in Tang and Nilsson (1992) as follows:

$$D(t) = D_{ar} \left(\frac{t_r}{t} \right)^n \quad (2)$$

where D_{ar} [m²/s] is the diffusivity value determined at a reference time t_r [s]. The dimensionless parameter n is an age exponent. Eq. 2 should be integrated over time. However, some studies neglect this integration step for the assessment of diffusion coefficient (Maage and Molloy, 1995; Nilsson and Carcasses, 2004; Stanish and Thomas, 2003).

Average diffusivity: is defined over the time interval $[t_{ex}, t]$ (Frederiksen et al., 2008):

$$D_{av}(t) = \frac{1}{t - t_{ex}} \int_{t_{ex}}^t D(t) dt \quad (3)$$

where t_{ex} is the age of the concrete at the beginning of the exposure to chloride environment.

It can be expressed as follows:

$$D_{av}(t) = D_{ar} \left(\frac{t_r}{t} \right)^\sigma \quad (4)$$

where D_{ar} (m²/s) is the average diffusivity at t_r (s). The age exponent σ is not the same as in eq. (2).

Tang and Gulikers (2007) gives the following expression, with the same age factor n as in equation (2).

$$D_{av}(t) = \frac{D_{ar}}{1 - n} \left[\left(1 + \frac{t_{ex}}{t - t_{ex}} \right)^{1-n} - \left(\frac{t_{ex}}{t - t_{ex}} \right)^{1-n} \right] \left(\frac{t_r}{t} \right)^n \quad (5)$$

The DuraCrete model DuraCrete (2000) is supposed to use this diffusivity definition with:

$$D_{av}(t) = k_t k_c k_e D_{rcm} \left(\frac{t_r}{t} \right)^n \quad (6)$$

where k_t , k_c , k_e , are respectively the test, cure condition and environmental parameters, D_{rcm} is the migration coefficient obtained with rapid test according to NT-Build492 (1999). Contradiction arose in the literature with respect to this statement about DuraCrete model. In Tang and Gulikers (2007) it is claimed that $D_{av}(t)$ in eq (6) is instantaneous diffusion coefficient, since it is not underlined in the DuraCrete report DuraCrete (2000) that the compensation $\frac{1}{1-n}$ is introduced in k_e or k_c . Thus an integration should be made over an interval in order to obtain the average diffusivity. In contrast, in Frederiksen et al. (2008), it is defined that $D_{av}(t)$ in eq (6) is the average diffusivity. However, since the environmental parameter k_e is obtained without considering the time dependency of the surface chloride content (C_s), it is still explained in Frederiksen et al. (2008) that this parameter is quantified erroneously.

Given that the migration test duration t (s) is involved in the D_{rcm} determination, it is assumed in the present work that D_{rcm} and therefore $D_{av}(t)$ in eq (6) could be considered as average diffusivities.

Achieved diffusivity: is the regression parameter D_{ach} obtained by curve-fitting of the following equation to a measured chloride profile (Nilsson, 1993):

$$C(x, t) = C_s \operatorname{erfc} \left(\frac{x}{\sqrt{D_{ach}(t - t_{ex})}} \right) + C_{ini} \quad (7)$$

D_{ach} could be seen as the average diffusivity in the time interval $[t_{ex}, t]$ where t is the age of the structure when the chloride profile is measured. Hence, a time dependent $D_{ach}(t)$ could be established using measurements at different time-steps.

The model proposed in the EuroLigthCon project (EuroLightCon, 1999) uses this diffusivity definition. However, this model defines two age exponents: α which corresponds to achieved diffusion coefficient, and β to the potential diffusion coefficient obtained from a short time laboratory testing according to NTBuild492 (1999). The concrete composition and environmental conditions are taken into account by α , whereas only concrete type is considered by β . Therefore, the sensitivity analysis for this model will be only based on the parameter α . The reference EuroLightCon (1999) provides these parameters for some concrete types.

Concerning the time-dependency of surface chloride content, the false-erfc model (Nilsson, 2001), takes into account this effect as:

$$C_s(t) = A \ln(t - t_{ex}) + B \quad (8)$$

where A and B are fitting parameters.

Table 6 presents the input parameters for each studied chloride ingress model that are classified into environmental and material parameters.

3.2. Carbonation models

3.2.1. Unified formulation

Analytical carbonation models assume that carbon dioxide pressure varies linearly from the exposed surface, where it is equal to outer partial pressure, to the carbonation depth, where it is equal to zero due to the instantaneous CO_2 consumption by reaction

with dissolved hydrates. These models can be written in a generalized expression:

$$x(t) = \sqrt{k_{exp}k_{exe}k_P D_{CO_2} \sqrt{t}} \quad (9)$$

where $x(t)$ [m] is the carbonation depth at time t [s], k_{exp} is a factor which introduces environmental conditions, k_{exe} is a factor accounting for execution conditions, k_P is a factor accounting for the interaction between the diffusion coefficient of the carbon dioxide D_{CO_2} [m²/s] and the concrete porosity ϕ . In some models (Hyvert, 2009; Petre-Lazar, 2001; Ying-Yu and Qui-Dong, 1987), k_P is expressed as:

$$k_P = k_{P,M}k_{P,E} \quad (10)$$

where $k_{P,M}$ is related to material properties and $k_{P,E}$ to exposure conditions. Expressions of $k_{P,M}$, $k_{P,E}$, k_{exp} and k_{exe} are given in Table 7 for each considered model. α_1 and n_1 are fitting parameters, f_p is the volumetric fraction of the cement paste, R is the gas constant (8.31 USI), a is the binding capacity for CO_2 , a' is the required quantity of CO_2 for a complete carbonation of the concrete studied, RH is relative humidity, T is temperature, P_{CO_2} is carbon dioxide pressure, R_c is concrete compressive strength, ϕ is porosity, S_r is saturation degree, ρ is concrete density, [Component] is the ‘‘component’’ content, C_{abs} is the absorbed carbone dioxide, C_0 is the CO_2 content at the exposed surface, k_e is a parameter which assesses environmental conditions, k_c is a parameter which considers cure conditions.

The analytical models of carbonation can be divided into three classes:

- Class 1: models that mainly account for exposure conditions (Petre-Lazar, 2001; Ying-Yu and Qui-Dong, 1987).
- Class 2: models that mainly account for the potentially carbonated material content, estimated as a whole (CEB, 1997; DuraCrete, 2000) or as function of hydrates content (Miragliotta, 2000; Papadakis et al., 1991).
- Class 3: models that account for all previously mentioned factors (Hyvert, 2009).

This study considers seven carbonations models (Table 7): two in class 1 (Petre-Lazar, 2001; Ying-Yu and Qui-Dong, 1987), four in class 2 (CEB, 1997; Miragliotta, 2000; Papadakis et al., 1991; DuraCrete, 2000), and one in class 3 (Hyvert, 2009). The following section presents the proposed classification of the parameters considered for all models.

3.2.2. Model description and parameters

In order to generalize the presentation of analytical models, the input parameters have been gathered into three levels (Figure 1 and Table 5). As well as for chloride ingress models, the parameters of level 1 are ‘‘observables’’. Three kind of parameters could be found in the level 1:

- level 1a: environmental parameters – e.g. RH (relative humidity), T temperature;
- level 1b: parameters which represent physical properties of concrete – e.g. R_c (compressive strength), ϕ (porosity), S_r (saturation degree); and
- level 1c: other parameters – e.g. cement composition, concrete mixture, etc.

The parameters of level 2 are deduced from level 1. The parameters of level 3 are derived from level 2 and they are the direct inputs of the models. The sensitivity analysis (section 4) will be carried out with respect to the parameters of levels 1

and 2 that are input parameters of models. The variability, according to hydrates or unhydrates contents, is quite difficult to supply and has been therefore introduced throughout the hydration degree α_{hyd} and cement content c .

As well as for chloride ingress models, Table 8 presents the input parameters for each studied carbonation model that are classified into environmental and material parameters.

3.3. Discussion

It can be seen from Tables 6 and 8 that the number of input parameters varies from a model to another, from 3 to 10. It could be erroneously deduced that models requiring a larger number of parameters are the most accurate. Supplying models parameters is a more or less difficult task (in particular for the amount of hydrates in cement paste), and thus, may be a source of uncertainty and indirectly inaccuracy for lifetime assessment. Estimating the influence of uncertainties of parameters on the output of models is therefore an essential issue for probabilistic modeling. From building and infrastructure managers point of view, the choice of a model depends on both its accuracy and its cost in terms of informations to be supplied. When comparing the models according to their number of input parameters, it can only be stated that some of them are more elaborated than others. Sections 5 and 6 will study and compare the sensibility of these models to propagate uncertainties for the materials described in section 4.

4. Description of the studied materials

In order to represent various existing concrete structures, three typical concrete mixes have been accounted for: they are referred as C25, C35 and C45. These concretes were designed for specific earlier research works, except C35 concrete which was designed for the EVADEOS project. The compositions of CEM I cement and mixes of these concretes are reported in Table 9 and Table 10, respectively. Useful contents of hydrates in cement paste and concrete properties are reported in Table 11, where it can be noted that average resistances comply with European standard EN 206 (European Standard, 2004). Cement compositions are similar for all concretes and the variation of material parameters is mainly caused by the mix proportions (Table 9). For instance, incorporating three classes of aggregate size with an efficient balance between the respective amounts, led to a good compactness of the C45 concrete, with a favorable effect on strength. But simultaneously the low water to cement ratio, w/c , prevented the content of hydrates to be high and the porosity remained rather elevated for the C45, despite the use of a superplasticizer. An almost opposite situation prevails for the C35 concrete, where both porosity and strength are rather low. Finally the C25 concrete is an ordinary quality concrete.

Outer surfaces of concrete structures considered in this study are supposed sheltered and exposed to commonly encountered yearly average environmental conditions. Average relative humidity and temperature were thus 72% and 11°C, respectively.

5. Methodology and indicators for the sensitivity analysis

5.1. Notation and methodology

For the sensitivity analysis, analytical models of carbonation and chloride ingress are expressed as follows:

$$y = f(t, \mathbf{Z}) \quad (11)$$

where y is the model output, and $\mathbf{Z} = \{z_1, \dots, z_n\}$ is the vector of input parameters of the model.

This study uses several sensitivity indicators: the elasticity coefficient, the Pearson's coefficient, the bias on the mean, and the standard deviation of the response. The methodology follows the approach suggested in Schoefs (2008) for physical response surfaces. The values of input parameters are summarized in Tables 12 and 13 for chloride ingress models and carbonation models, respectively. The range of variability of each parameter corresponds to the possible realistic variability for the three studied concretes. The values of parameters that are considered as deterministic are presented in Table 14. Moreover, k_e is determined from DuraCrete (2000) as:

$$k_e = \left(\frac{1 - \left(\frac{\text{RH}}{100}\right)^{2.5}}{1 - \left(\frac{\text{RH}_{ref}}{100}\right)^{2.5}} \right)^5 \quad (12)$$

where RH_{ref} corresponds to a reference relative humidity ($\simeq 65\%$).

As previously mentioned, despite the fact that cement paste hydrates and unhydrates contents are input parameters for some models, it was decided to consider their variability through hydration degree α_{hyd} and cement content c , using the empirical expressions, found in Hyvert (2009).

5.2. Elasticity coefficient

Elasticity measures the effect on the output (here chloride content or carbonation depth) following a variation of one input parameter. The elasticity coefficient is computed deterministically as follows (Lemaire, 2009):

$$e_{i,k}(t) = \frac{\Delta y_k(\mathbf{Z}, t)(\%)}{\Delta z_i(\%)} \quad \text{at depth } x_k \text{ for chloride ingress models} \quad (13)$$

$$e_i(t) = \frac{\Delta y(\mathbf{Z}, t)(\%)}{\Delta z_i(\%)} \quad \text{for carbonation models} \quad (14)$$

where Δz_i and $\Delta y(\mathbf{Z}, t)$ (or $\Delta y_k(\mathbf{Z}, t)$) are the variations of the input z_i and the model output, respectively. We considered an increase of 10% from the mean value for each input parameter. This value could be considered excessive or insignificant for some parameters; nevertheless, it is relevant to keep the same perturbation for all parameters. A larger absolute value of $e_i(t)$ means that the model is very sensitive with respect to the variation of the considered parameter, while a value close to zero indicates a low sensitivity. A value of 1 means that a change of z_i causes the same variation on y_j (case of a linear model).

5.3. Monte Carlo simulations for other sensitivity indicators

In order to analyse how the response of a system is influenced by the variation of its inputs, a common approach is to randomly vary these inputs into a given interval. Monte Carlo simulations are a relevant tool in such a purpose.

A variation interval $[a_i; b_i]$ is defined for each input parameter (Tables 12 and 13), whose bounds have been proposed from literature review (Buenfeld and Wong, 2009; GrandDubé, 2007; DuraCrete, 2000) or experimental data. Uniform distributions are used for generating random values.

5.3.1. Pearson's correlation coefficient

Pearson's coefficient ρ_{cor} estimates the linear correlation between two random variables (Bowley, 1901). In a sensitivity analysis of model parameters, the effect of the i^{th} component z_i of the input vector \mathbf{Z} on y at the time t is assessed as follows:

$$\rho_{cor,x_k}(t) = \frac{\text{cov}(y_k(t), z_i)}{\sigma_{y_k(t)} \times \sigma_{z_i}} \text{ at depth } x_k \text{ for chloride ingress} \quad (15)$$

$$\rho_{cor}(t) = \frac{\text{cov}(y(t), z_i)}{\sigma_{y(t)} \times \sigma_{z_i}} \text{ for carbonation} \quad (16)$$

where $\text{cov}(y_k(t), z_i)$ (or $\text{cov}(y(t), z_i)$) is the covariance between z_i and y (or y_k), and σ_{z_i} and σ_{y_k} (or σ_y) are their respective standard deviations. The value of ρ_{cor} varies from -1 to 1. An absolute value close to 1 indicates a strong correlation while it indicates a low linear correlation when ρ_{cor} is approaching zero. A positive sign means a similar trend of variation for both variables while a negative one indicates an opposite one. This indicator is able to highlight the physical meaning of the model and can also be used to rank input parameters according to their influences. However, Pearson's coefficient is meaningful only if a linear or quasi-linear relationship between inputs and output is expected to exist.

5.3.2. Bias on the output mean value

This method is classified as a local method and relies on the OFAT (one-factor-at a time) method (Daniel, 1973). The previous sensitivity indicators aimed to evaluate the effect of the variability of input parameters upon the model output in terms of proportionality (elasticity coefficient) and statistical dependency (correlation coefficient). The global weight of a parameter can also be rendered by the bias imposed on the output mean value when it remains constant as the other parameters are randomly varying. This is assessed by the bias factor that is estimated using the following procedure (see Schoefs (2008)):

- (1) compute, the global expected value $E[f(t, \mathbf{Z})]$ of the output.
- (2) fix the parameter z_i at its mean value \bar{z}_i ; then, the i^{th} component of the input vector \mathbf{Z} , now noted Z_{i0} , is no longer random.
- (3) estimate the bias factor regarding z_i as:

$$b_{k,z_i} = E[y_k(t, \mathbf{Z})] - E[y_k(t, Z_{i0})] \text{ at depth } x_k \text{ for chloride ingress} \quad (17)$$

$$b_{z_i} = E[y(t, \mathbf{Z})] - E[y(t, Z_{i0})] \text{ for carbonation} \quad (18)$$

5.3.3. Standard deviation of the output

This method is also one of the OFAT methods. The standard deviations of the carbonation depth and chloride content at given depths are essential informations for estimating corrosion initiation risks. It is therefore of utter importance to examine how the standard deviation of the model output depends on the variability of input parameters. The procedure to estimate this indicator is summarized in the following steps (Schoefs, 2008):

- (1) consider as random variable the parameter z_i
- (2) fix the other parameters at their mean values
- (3) estimate The so-called reduced standard deviation of the output as:

$$\sigma_{z_i/y_k}(t) = \sqrt{\text{E} \left[(y_k(t, \mathbf{Z}_i) - \text{E} [y_k(t, \mathbf{Z}_i)])^2 \right]} \text{ at depth } x_k \text{ for chloride} \quad (19)$$

$$\sigma_{z_i/y}(t) = \sqrt{\text{E} \left[(y(t, \mathbf{Z}_i) - \text{E} [y(t, \mathbf{Z}_i)])^2 \right]} \text{ for carbonation} \quad (20)$$

6. Results and discussions

6.1. Chloride ingress models

6.1.1. Elasticity results

Tables 15 and 16 summarize the results obtained at 2.5 cm depth and 3 dates (10, 25 and 50 years) for first and second group of models, respectively.

Due to the linearity of all analytical chloride models with respect to C_s , the value of elasticity is equal to 1 for all the models except for LEO model (Petre-Lazar, 2001). For this last one, the influence of the non-linearity decreases over time and the value of the elasticity tends to 1. The same trend is observed with respect to γ_{cl} for the JSCE model. On the other hand, when parameters are multiplying others in the model, the values of their elasticity are the same -e.g. k_e , k_c , k_t and D_{rcm} for the Duracrete model (DuraCrete, 2000). Consequently, it is difficult to study the sensitivity of these parameters using this indicator.

Figure 2 illustrates the variation in time of the elasticity indicator for the Leo model, C25 concrete and $x = 2.5$ cm. As previously explained, analytical chloride ingress models describe an increase of the chloride content into the concrete bulk over time leading to a constant value which correspond to the chloride content on the concrete surface C_s . Consequently, at the beginning of the exposure to chloride environment, the diffusion process is significant and the diffusion parameters such as D_a , have higher influence on the output of the model. For the same reason, similar results are found for diffusion related parameters (e.g. D_{rcm} and w/c) in Tables 15 and 16. When the chloride content into the concrete bulk is near to C_s , the diffusion kinetic slows down. At this stage, the only way that could boost up the process is a modification of the value of C_s . Any disturbance of the value of this parameter has significant impact on the output of the model. The influence of diffusion parameters is hence significant at the beginning of the exposure and decreases over time, while the influence of C_s

increases over time.

Concerning the aging parameter n (or α), one observe the same tendency as for diffusion parameters: increasing influence at the beginning of the exposure and decrease over time. Indeed, the kinetic of the aging of concrete (here, we are referring to continued hydration process, reduction of porosity caused by carbonation) slows down after long term exposure. The decrease starts earlier for material with lower resistance (C25 end C35).

The effects of the type of concrete depend on the values and the variation range of the input parameters. When the concrete has higher resistance to chloride ingress (C45), material parameters have larger influence because any disturbance of the property of the involved concrete could affect the kinetics of the chloride diffusion.

6.1.2. Pearson's coefficient results

Tables 17 and 18 provide the Pearson's coefficient results for the first and second group of models, respectively. Any conclusion could be made when the absolute value of this indicator is less than 0.5. Indeed, it may indicate either independence and/or non-linearity of the dependence. It is observed for all models a higher influence of diffusion coefficients (D_a , D_{ar}) and k_c . The temperature T has also large influence for the model of Leo (Petre-Lazar, 2001). Finally, with respect to the models of the second group, the aging parameters n and α have a significant impact. These results underline that aging of the concrete plays a significant role in the models of the second group.

Concerning the effect of the concrete type, it was observed the same trend as for the elasticity coefficient.

6.1.3. Bias of the output

Tables 19 and 20 show the results for the first and second group of models, respectively. The non-linearity of the model with respect to the involved parameter increases the bias. Therefore, diffusion and aging parameters (D_a , D_{ar} , k_c , n and α) are the most influential with respect to this indicator. However, lower values of bias are noted for W_{gel} , w , k_e , k_t , and D_{rcm} because their variation ranges are smaller (Table 12).

Given that the output of analytical chloride ingress model has always positive value (chloride content), and that at the beginning of the exposure the values of the output are close to zero, the distribution of the output values is not symmetric. The values of the bias are hence positive during the first years of exposure for some model parameters, and then the sign changes. Figure 3 presents an illustration with the model of Leo and for concrete C25. For long-term prediction, the absolute values of bias decrease over time. Indeed, according to analytical chloride ingress model, the chloride content in the concrete bulk tends to C_s without exceeding this value. This means that the mean model output tends to C_s , and thus the bias decreases.

Concerning the effect of the type of material, when the concrete has higher resistance against chloride ingress, the kinetics of the phenomenon is lower. Consequently, the distribution of the output of the model remain asymmetric during a long period for this type of concrete (C45).

6.1.4. Standard deviation of the output

Tables 21 and 22 show the results with respect to output's standard deviation for the first and second group of models, respectively.

The non-linearity of the model and the variation interval width of the input parameters have significant impact on the standard deviation of the model output. This indicator provides better assessment of the ability of the models for uncertainty propagation. Indeed, it shows the variability on the model output when the parameter studied varies within its variation range. The parameters with respect to which the non-linearity of the model has significant impact for this indicator are D_a , w , T , n and α . k_c , k_t and D_{rcm} are multiplying factors in the model of Duracrete, their impact on the model output depends on their variation ranges.

As well as for the bias, the standard deviation of the output of the model increases over time and decreases after a maximum, this with respect to diffusion parameters such as D_a , k_c , k_t and D_{rcm} . The decrease begins when the diffusion slows down which is due to reduction of the gradient of chloride content. The decrease starts earlier for concretes with lower resistance against chloride ingress.

In the computation of this indicator, all the parameters are fixed to a predetermined value except the parameter of interest for the sensitivity analysis. The previous results were obtained considering the mean as the predetermined value, but they could differ for another selected value. It should be relevant to underline how the choice of another predetermined value of the fixed parameters would have an effect on the results. Figure 4 presents an example with respect to the model of Collepardi and concrete C45. The input parameters of this model are C_s and D_a . It is shown firstly in this figure, the evolution of the output's standard deviation when C_s varies and D_a is fixed on its minimum ($C_{s_{min}D_a}$), mean ($C_{s_{mean}D_a}$) and maximum ($C_{s_{max}D_a}$) values. And secondly, the evolution of the output's standard deviation when D_a varies and C_s is fixed at its minimum (D_{minC_s}), mean (D_{meanC_s}) and maximum (D_{maxC_s}) values. No significant differences could be observed concerning the ordering of parameters. It can be concluded from this figure that the order of importance is not affected by the considered combinations.

6.2. Carbonation models

Table 23 summarizes the results of the sensitivity analysis for all carbonation models. For each model, the maximum and minimum value of each indicator are highlighted with bold text. The impact on the mean and standard deviation of the output varies over time, but the results of elasticity and the linear Pearson's correlation coefficient remain fairly constant. Figures 5 and 6 present illustrations of the effects of time with respect to elasticity and standard deviation respectively, for the model of Hyvert and for concrete C45. Since the order of importance of the parameters does not change over time, results are reported only for $t=50$ years which is the usual lifetime of RC structures.

6.2.1. Elasticity results

The non linearity of the models with respect to the parameter studied has significant impact on the value of its corresponding elasticity coefficient. For instance, elasticity coefficient are higher for the parameter n for the models CEB (CEB, 1997) and Duracrete (DuraCrete, 2000), R_c for the Oxand model (Petre-Lazar, 2001), RH for the models of Hyvert (Hyvert, 2009), Papadakis (Papadakis et al., 1991) and Miragliotta (Miragliotta, 2000). On the other hand, when parameters are multiplying other parameters in the models, the values of their elasticity coefficient are similar e.g k_e and k_c for the Duracrete model (DuraCrete, 2000).

It was also found that time (t) has no effect on the elasticity coefficient excepting models including the parameter n which is linked to t through the expression $\left(\frac{t_0}{t}\right)^n$. However it has no effect on the ranking of parameters.

Concerning the type of concrete, the material parameters (R_{carb} , ϕ , c , ρ , and α_{hyd}) have higher values of elasticity coefficient when the concrete has higher resistance against concrete carbonation. Indeed, from physical point of view, carbonation has lower kinetics in such concretes.

6.2.2. Pearson's coefficient results

As well as for chloride ingress models, when the absolute value of this indicator is less than 0.5, any conclusion could be drawn. Results highlight the significant influence of the following parameters: RH, n , R_c , S_r , k_c . No conclusion could be drawn with respect to other parameters. As well as for the elasticity coefficient, time has no effect on the Pearson's coefficient. The effects of the type of concrete are the same as for elasticity coefficient, -i.e., the coefficient of Pearson is higher for concretes with higher resistance against concrete carbonation.

6.2.3. Bias of the carbonation depth results

The values of the bias changed over time because carbonation models are increasing functions of time; however, the ranking of parameters for all models remained similar. The non-linearity of the model has significant impact on the bias. For instance, n is by far the parameter that introduces the higher value of bias for the models Duracrete (DuraCrete, 2000) and CEB (CEB, 1997). When the model has the same level of non-linearity with respect to two parameters, the one which has the larger width of variation interval has higher value of bias. For instance, parameter k_c generates a higher bias than k_e and k_t because it has a larger variation interval (Table 13).

In contrast to the previous indicators, the bias is small when the concrete has higher resistance against carbonation. Indeed, the kinetic of carbonation is reduced for the more resistant concretes, and therefore, the values of carbonation depth and its bias are smaller.

6.2.4. Standard deviation of the carbonation depth results

As well as for the bias, the standard deviation of the output of the model is very sensitive to non-linearity of the involved parameters. For example, large values were observed for parameter n with respect to which the models Duracrete (DuraCrete, 2000) and CEB (CEB, 1997) are significantly non-linear. It is possible to observe the same trend with respect to RH for the models of Oxand (Petre-Lazar, 2001), Miragliotta (Miragliotta, 2000), Papadakis (Papadakis et al., 1991), Ying-yu (Ying-Yu and Qui-Dong, 1987) and Hyvert (Hyvert, 2009). Similarly with respect to S_r for the models of Miragliotta (Miragliotta, 2000) and Ying-Yu (Ying-Yu and Qui-Dong, 1987), and R_c for the model of Oxand (Petre-Lazar, 2001). The width of the variation interval of the parameter has also significant impact. For instance, the parameters k_c for the model Duracrete (DuraCrete, 2000), CEB (CEB, 1997) and the model of Hyvert (Hyvert, 2009) have large variation interval width (Table 13).

Concerning the effect of time, the standard deviation of the model output increases over time for any input variation. Figure 6 presents an example with the model of Hyvert and for the concrete C45. This means that a long-term prevision is affected by more significant uncertainties.

Since the variation range of each parameter is not the same for each type of concrete (Table 13), the standard deviations of the model output are also different. Higher dispersion corresponds to concretes with lower resistance against carbonation (C35 and C25). On the other hand, for the Oxand model (Petre-Lazar, 2001), the order of parameters is not the same for two different materials because the gaps between the values of R_c are quite significant (Table 13).

As well as for chloride ingress models, it should be relevant to underline how the choice of another predetermined value of the fixed parameters would have an effect on the results, especially for selected values leading to minimize or maximize the carbonation depth. For instance, regarding Oxand model (Petre-Lazar, 2001), minimum values of R_c and RH make easier the access of carbon dioxide into the concrete bulk. Figure 7 depicts the curves obtained for the combinations expected to modify the order of parameters with respect to the standard deviation for the Oxand model (Petre-Lazar, 2001). However, it can be observed in this figure that the order of importance is not affected by the considered combinations.

7. Conclusions

Steel corrosion is one of the phenomenon that reduces significantly life-cycle of RC structures. This paper focused on analytical models of concrete carbonation and chloride ingress that could be used to assess corrosion onset. An homogenization of these models leads to unified formulations. Two groups of models have been identified for chloride ingress models. The first one gathers models with constant parameters while the second one encompasses those with time-dependent parameters. For concrete carbonation, three groups of models are highlighted. A classification of the input parameters of these models has been proposed in which inputs are decomposed into three levels of parameters. This paper provided helpful tools for understanding and using these analytical models.

The relative importance of each parameter was assessed through the following indicators: elasticity coefficient, Pearson's coefficient, bias, and standard-deviation of the output. In order to compute the three last indicators, the variation range of each input parameter for three concrete types are presented. It was found that the non-linearity of the models has significant impact in the values of each indicator as well as the variation range of the studied parameter.

The most influential parameters are C_s , D_a and the aging parameters n or α for chloride ingress models. However, at earlier age, the diffusion parameters have higher influence while at long-term, C_s becomes the most important parameter.

Concerning carbonation assessment the parameters which describe the porous media appear to be the most influential ones -i.e., RH which is linked to saturation degree, k_c which gives an assessment of the quality of the firsts centimeters from the exposed surface, and the porosity ϕ . Considering the variability of these parameters, it seems to be necessary to include it for a probabilistic assessment of carbonation. The second group of important parameters are those which introduced the amount of material that can be carbonated: the hydration degree α_{hyd} and the cement content c .

These findings could help the end-user of a given model to optimally allocate the resources for obtaining each parameter. A parameter could be obtained either with expert advice or through destructive or non destructive tests. The amount of resources required to obtain a given parameter and then the required investment to use the corresponding model depend on the methods used to obtain the parameters. Nevertheless,

the strategy of maintenance as well as the resources allocated are different for each structure. Within this framework, the results of this study could be used to develop a methodology for the choice of the appropriate model for a given structure, taking into account the chosen strategy of maintenance and the availability of the resources allocated to the maintenance. Rakotovao Ravahatra et al. (2019) present a framework to help decision-makers towards this aim.

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Table 1. Physical phenomena that are taken into account in some numerical chloride ingress models based on Fick’s law

Model	Diffusion of chloride	Humidity transfer	Heat transfer
LERM (2000)	×		
Bentz and Thomas (2008)	×		×
Deby (2008)	×		
Clincon Nilsson et al. (1997)	×		×
Bastidas-Arteaga (2010, 2018)	×	×	×
Nguyen et al. (2017)	×	×	×

Table 2. Physical phenomena that are taken into account in some numerical chloride ingress models based on the law of Nernst-Planck

Model	Diffusion ionic species i	Humidity transfer	Air transfer
Clincon Nilsson et al. (1997)	×		×
Li and Page (2000)	×		
Marchand (2001)	×		
Sleiman et al. (2009)	×	×	×
Baroghel-Bouny et al. (2011)	×	×	×
Friedmann et al. (2012)	×	×	×

Table 3. Physical phenomena that are taken into account in some numerical carbonation models

Model	Diffusion of CO_2	Dissolution of hydrates	Humidity transfer	Diffusion of Ca	Heat transfer
Saetta et al. (1995)	×	×			×
Steffens et al. (2002)	×	×	×		×
Isgor and Razaqpur (2004)	×				×
Thiery (2005)	×	×	×	×	
Bary and Sellier (2004)	×	×	×	×	
Talukdar et al. (2012)	×	×		×	
de Larrard et al. (2013)	×	×	×	×	
de Larrard et al. (2014)	×	×	×	×	×

Table 4. Expressions of \mathbf{X} and $\xi(\mathbf{X}, t)$ for the chloride ingress models

Model	\mathbf{X}	$\xi(\mathbf{X}, t)$
Colleparidi et al. (1970)	$\begin{pmatrix} D_a \\ t_{ex} \end{pmatrix}$	$D_a(t - t_{ex})$
JSCE (2007)	$\begin{pmatrix} w/c \\ t_{ex} \end{pmatrix}$	$D_{a,JSCE}(t - t_{ex})^*$
Petre-Lazar (2001)	$\begin{pmatrix} D_{ar} \\ W_{gel} \\ w \\ C_{s1} \\ T \end{pmatrix}$	$(1 + \frac{1}{4C_{s1}}) \left(\frac{1}{1+0.5\frac{W_{gel}}{w}} \right) D_a(T)t^{**}$
Nilsson (2001)	$\begin{pmatrix} D_{ar} \\ n \\ t_r \\ t_{ex} \end{pmatrix}$	$\frac{D_{ar}}{1-n} \left(\frac{t_r}{t} \right)^n (t - t_{ex})$
EuroLightCon (1999)	$\begin{pmatrix} D_{ar} \\ \alpha \\ t_r \\ t_{ex} \end{pmatrix}$	$\frac{D_{ar}}{1-\alpha} \left(\frac{t_r}{t} \right)^\alpha (t - t_{ex})$
DuraCrete (2000)	$\begin{pmatrix} D_{rcm} \\ n \\ t_r \\ k_e \\ k_c \\ k_t \end{pmatrix}$	$k_e k_c k_t D_{rcm} \left(\frac{t_r}{t} \right)^n$
Tang and Gulikers (2007)	$\begin{pmatrix} D_{ar} \\ n \\ t_r \\ t_{ex} \end{pmatrix}$	$\frac{D_{ar}}{1-n} \left[\left(1 + \frac{t_{ex}}{t-t_{ex}} \right)^{1-n} - \left(\frac{t_{ex}}{t-t_{ex}} \right)^{1-n} \right] \left(\frac{t_r}{t} \right)^n$

* $D_{a,JSCE}$ is an empirical formula to determine D_a in the model of JSCE for OPC: $\log_{10} D_a = -3.9(w/c)^2 + 7.2(w/c) - 2.5$

** $D_a(T) = D_{ar} \exp\left(\frac{E}{R}\left(\frac{1}{T} - \frac{1}{293}\right)\right)$ where E is the activation energy and R is the gaz constant

Table 5. Classification and data required for determining model input parameters

Level	Chloride ingress	Carbonation
1a*	RH (Relative humidity), T (Temperature)	RH (Relative humidity), T (Temperature), P_{CO_2} (CO_2 pressure), P_{atm} (atmospheric pressure)
1b**	ϕ (porosity), S_r (Saturation degree), ρ (concrete density), migration coefficient, chloride profiles	R_c (28 days compressive concrete strength), ϕ (porosity), S_r (Saturation degree), ρ (concrete density)
1c***	Concrete mix, cement composition, execution conditions	Concrete mix, cement composition, execution conditions
2	Diffusion coefficient, w (water content), n (aging parameter), k_e (environmental parameter), k_c (execution parameters), k_t (test method parameter), C_s (surface chloride content)	a (binding capacity for CO_2), a' (required quantity of CO_2 for a complete carbonation), n (aging parameter), C_0 (carbone dioxide content), f_p (volumetric ratio of cement paste), hydrates content, unhydrates content, C_{abs} (required carbone dioxide content for a complete hydration of the concrete), α_{hyd} (hydration degree), α_1 et n_1 (fitting parameters of the model of Hyvert), k_e (environmental parameter), k_c (execution parameters), k_t (test method parameter)
3		k_{exp} (exposure model factor), k_{exe} (execution model factor), k_P (factor accounting for the interaction between the diffusion coefficient and the carbon dioxide), D_{CO_2} (diffusion coefficient)

*Meteorological data

**Tests or project archives

***Project archives

Table 6. Input parameters of analytical chloride ingress models

Description	Parameters		Models					
	Symbol	Collepardi et al. (1970)	JSCÉ (2007)	Petre-Lazar (2001)	Nilsson (2001)	EuroLightCon (1999)	DuraCrete (2000)	Tang and Gulikers (2007)
Env.	Chloride content on concrete surface	C_s	×	×	$C_s(t)^*$	×	×	×
	Safety factor for C_s	γ_{cl}	×					
	Temperature	T		×				
	Environmental factor	k_e					×	
	Water content	ω		×				
	Gel content	W_{gel}		×		×		
	Aging factor	α						
		n				×		×
	Age at exposure time	t_{ex}				×		×
	Reference time	t_r	×			×		×
Material	Cure condition	k_c					×	
	Factor of test method	k_t					×	
	Rapid chloride migration coefficient	D_{rcm}					×	
	Apparent chloride diffusion coefficient	D_a	×	$D_{a,JSCÉ}^{**}$				
	Known D_a at reference time t_r	D_{ar}		×	×	×		×

* $C_s(t) = A \ln(t - t_{ex})t + B$, A and B are fitting parameters

** Empirical formula to determine D_a in the model of JSCÉ for OPC: $\log_{10} D_a = -3.9(w/c)^2 + 7.2(w/c) - 2.5$

Table 7. Expressions of $k_{P,E}$, $k_{P,M}$, k_{exp} and k_{exe}

Model	$k_{P,E}$	$k_{P,M}$	D_{CO_2}	k_{exp}	k_{exe}
Ying-Yu and Qui-Dong (1987)	$2PCO_2/(C_{abs}\rho)$	1	$D_{Y_u} = \exp(105.66\phi - 0.877)$	1	1
Papadakis et al. (1991)	C_0	$2/([CH] + 3[CSH] + 3[C_3S] + 2[C_2S])$	$D_{P_a} = 1.64 \times 10^{-6} f_p^{1.8} (1 - RH)^{2.2}$	1	1
CEB (1997)	C_0	$2/a'$	$D_{Du}(\frac{a}{l})^{n^*}$	k_e	k_c
DuraCrete (2000)	C_0	$2/a$	$k_t D_{Du}(\frac{a}{l})^n$	k_e	k_c
Miragliotta (2000)	C_0	$2(1 - S_r)(1 - \phi)^{-1}([CH] + 3[CSH] + 3[C_3S] + 2[C_2S] + 4[C_4AF] + 3[C_3A])^{-1}$	D^{**}	1	1
Petre-Lazar (2001)	$[-3.8533(RH)^2 + 3.4833(RH) + 0.2]^2$	$(365 \times (\frac{1}{2.1\sqrt{R_c}}) - 0.06)^2$	1	γ^2	1
Hyvert (2009)	$\frac{2PCO_2}{RT}$	$f_p^{-1} \left([CH] + 4[AFt] + 3[AFm] + \frac{1.65[CSH]}{n_1+1} \left(\frac{PCO_2}{P_{atm}} \right)^{n_1} \right)^{-1} \times \left(1 + \alpha_1 1.65 [CSH] \left(\frac{PCO_2}{P_{atm}} \right)^{n_1} \right)^{-1}$	D	k_e	k_c

* $D_{Du} = \frac{a}{R_{carb}}$

** D could be measured through destructive testing or calculated using previous empirical expressions, in this work D_{P_a} is used

Table 8. Input parameters of analytical models of carbonation

Parameter		Model							
Description	Symbol	Ying-Yu and Qui-Dong (1987)	Papadakis et al. (1991)	CEB (1997)	DuraCrete (2000)	Miragliotta (2000)	Petre-Lazar (2001)	Hyvert (2009)	
Env.	CO_2 pressure	P_{CO_2}	×					×	
	Temperature	T						×	
	Relative humidity	RH	×			×	×		
	CO_2 content	C_0	×	×	×	×			
	Porosity	ϕ				×			
	Saturation degree	S_r				×			
	Compressive strength	R_c					×		
	Absorbed CO_2	C_{abs}	×						
	Concrete density	ρ	×						
	Binding capacity for CO_2	a				×			
Material	Required quantity of CO_2 for a complete carbonation	a'		×					
	CSH content	$[CSH]$		×		×		×	
	CH content	$[CH]$		×		×		×	
	AFt content	$[AFt]$				×		×	
	AFm content	$[AFm]$				×		×	
	C_3S content	$[C_3S]$		×		×			
	C_2S content	$[C_2S]$		×		×			
	C_3A content	$[C_3A]$					×		
	C_4AF content	$[C_4AF]$		×			×		
	Reference period	t_0			×				
Fitting parameters	α_1 and n_1				×			×	

Table 9. Cement composition (%)

Concrete	SiO ₂	Al ₂ O ₃	Fe ₂ O ₃	CaO	MgO	SO ₃	K ₂ O
C45	20.1	5	3	64.1	1	3.2	0.72
C35	20.43	4.9	1.83	65.4	1.06	3.5	0.25
C25	20.29	5.56	2.32	64.22	2	3.17	0.57

Table 10. Concrete mixes

Concrete	Cement (kg/m ³)	Fly ash (kg/m ³)	Sand 0/4 (kg/m ³)	Aggregates 4/12 (kg/m ³)	Aggregates 12/20 (kg/m ³)	Water (L/m ³)	Superpla- sticizer (kg/m ³)	<i>w/c</i>
C45	350	80	900	320	630	177	3	0.51
C35	350	0	815	998	0	195	1.4	0.56
C25	295	0	989	792	0	200	0	0.68

Table 11. Physico-chemical properties

Concrete	[AFm] (mol/L)	[AFt] (mol/L)	[CSH] (mol/L)	[CH] (mol/L)	SiO ₂ (mol/L)	Porosity (%)	R _c (MPa)
C45	0.41	0.25	3.16	3.11	0	11.8	58
C35	0.41	0.15	3.185	3.585	0	12.7	46.2
C25	0.34	0.25	2.879	2.90	0	14	40.2

Table 12. Values of input parameters for chloride ingress models

Parameters	Units	Mean	Coef of variation	Min (a_i)	Max (b_i)
C_s - C45	% mass of binder	6.24	-	5.29	7.19
C_s - C35		8.76	-	8.37	9.17
C_s - C25		10.01	-	9.52	10.49
T	Kelvin	284.04	0.067	282.55	285.53
D_a - C45	$10^{-12}\text{m}^2/\text{s}$	2.99	0.136	1.95	2,57
D_a - C35		3.45	0.136	2.99	3.92
D_a - C25		7.09	0.133	6.15	8,04
W_{gel} - C45	kg/m^3	205.19	-	198.62	211.76
W_{gel} - C35		208.56	-	201.88	215.23
W_{gel} - C25		174.58	-	168.99	180.17
w - C45	kg/m^3	118	0.05	112.1	123.9
w - C35		127	0.012	125.47	128.52
w - C25		140	0.06	131.6	148.4
k_c		0.656	0.26	0.48	0.82
k_t		0.832	0.029	0.80	0.85
k_e - C45, C35		1.325	0.17	1.09	1.55
k_e - C25		0.676	0.18	0.55	0.79
n - C45		0.69	0,07	0.6417	0.7383
n - C35, C25		0.3	0.17	0.249	0.351
α - C45, C35		0.60	0,07	0.558	0.642
α - C25		0.40	0.17	0.332	0.468
D_{rcm} - C45	$10^{-12}\text{m}^2/\text{s}$	4.14	0.136	3.57	4,70
D_{rcm} - C35		6.33	0.136	5.47	7,19
D_{rcm} - C25		13	0.133	11.27	14.73
γ_{cl}		-	-	1.00	1.30
w/c - C45		0.51	0.027	0.50	0.52
w/c - C35		0.56	0.027	0.54	0.57
w/c - C25		0.68	0.027	0.66	0.70

NB : – Means no data

Table 13. Values of input parameters for carbonation models

Parameter	Unit	Mean	Coef of Var (%)	Min (a_i)	Max (b_i)
RH	%	72.91	3	70.68	75.14
R_c C45	MPa	58	6	54.52	61.48
R_c - C35		46.2	4	44.35	48.04
R_c C25		40.2	3	38.99	41.40
k_c	-	0.63	26	0.46	0.79
k_t	-	0.98	2.3	0.96	1.005
n	-	0.4	20	0.32	0.48
R_{carb} - C45	10^{10}kgCO_2 /m ³ /(m ² /s)	2	7.5	1.9	2.1
R_{carb} - C35		0.4	8.9	0.36	0.43
R_{carb} - C25		0.28	5	0.271	0.3
T	K	284.04	6.7	282.55	285.53
ϕ - C45	-	0.118	5	0.112	0.124
ϕ - C35		0.127	1.6	0.124	0.129
ϕ - C25		0.14	8	0.129	0.151
c - C45	kg/m ³	350	14	345	355
c - C35		350	13.6	345	355
c - C25		295	16	290	300
α_{hyd} - C45	-	0.81	3.9	0.778	0.842
α_{hyd} - C35		0.84	3.8	0.808	0.872
α_{hyd} - C25		0.89	3.6	0.858	0.922
S_r	-	0.65	10	0.59	0.72

Table 14. Deterministic parameters

Parameter	Unit	Value
P_{atm}	Pa	101325
P_{CO_2}	Pa	40.53
C_0	kg/m ³	6.5×10^{-4}
γ	-	1
α_1	L/mol	23.5
n_1	-	0.67

Table 15. Elasticity coefficient for the models of the first group of chloride ingress models (non time-dependent parameters) at 2.5 cm

Concrete			C45			C35			C25		
Age (years)			10	25	50	10	25	50	10	25	50
Colleparidi	Env	C_s	1	1	1	1	1	1	1	1	1
	Mat	D_a	3.1	1.31	0.74	0.52	0.27	0.17	0.31	0.17	0.11
JSCE	Env	C_s	1	0.99	0.99	1	1	1	1	0.99	1
		γ_{cl}	1	1	1	1	1	1	1	0.99	1
	Mat	w/c	1.1	0.64	0.43	1.12	0.66	0.45	0.72	0.44	0.3
LEO	Env	C_s	0.68	0.86	0.92	0.97	0.98	0.99	0.98	0.99	0.99
		T	646.32	51.5	17.27	6.1	2.8	1.69	4.45	2.15	1.33
	Mat	W_{gel}	-3.16	-1.5	-0.84	-0.38	-0.19	-0.12	-0.25	-0.13	-0.08
		w	4.14	1.6	0.84	0.36	0.18	0.11	0.23	0.12	0.07
		D_a	11.11	3.77	1.9	0.84	0.42	0.26	0.64	0.32	0.2

Table 16. Elasticity coefficient for the models of the second group of chloride ingress models (with some time-dependent parameters) 2.5 cm

Concrete			C45			C35			C25		
Age (years)			10	25	50	10	25	50	10	25	50
Eur.	Env	C_s	1	1	1	1	1	1	1	1	1
	Mat	D_{ar}	1.36	0.99	0.79	0.95	0.7	0.57	0.35	0.24	0.18
		α	-1.73	-1.86	-1.86	-1.26	-1.37	-1.38	-0.49	-0.44	-0.4
DuraCrete	Env	C_s	1	1	1	1	1	1	1	1	1
	Material	D_{rcm}	6.06	4.4	3.5	0.68	0.42	0.3	0.34	0.22	0.16
		k_e	6.06	4.41	3.51	0.69	0.43	0.30	0.34	0.22	0.16
		k_c	60.06	4.41	3.51	0.69	0.43	0.30	0.34	0.22	0.16
		k_t	6.06	4.41	3.51	0.69	0.43	0.30	0.34	0.22	0.16
n	-8.71	-8.54	-8.37	-1.05	-0.8	-0.65	-0.54	-0.42	-0.35		
Luping	Env	C_s	1	1	1	1	1	1	1	1	1
	Mat	D_{ar}	1.6	1.24	1.04	0.47	0.3	0.21	0.28	0.18	0.13
		n	-1.32	-1.82	-2.04	-0.51	-0.42	-0.36	-0.31	-0.26	-0.23

Table 17. Pearson's coefficient for the models of the first group of chloride ingress models (non time-dependent parameters) at 2.5 cm

Concrete			C45			C35			C25		
Age (years)			10	25	50	10	25	50	10	25	50
Colleparidi	Env	C_s	0.35	0.63	0.81	0.98	0.99	0.99	0.71	0.87	0.94
	Mat	D_a	0.93	0.78	0.59	0.16	0.08	0.05	0.69	0.46	0.32
JSCE	Env	C_s	0.84	0.85	0.85	0.42	0.43	0.43	0.47	0.47	0.47
		γ_{cl}	0.5	0.51	0.51	0.85	0.87	0.88	0.86	0.87	0.87
	Mat	w/c	0.104	0.08	0.05	0.26	0.15	0.1	0.17	0.11	0.08
LEO	Env	C_s	0.09	0.23	0.41	0.29	0.51	0.69	0.38	0.62	0.78
		T	0.51	0.52	0.48	0.5	0.45	0.37	0.12	0.1	0.08
	Mat	W_{gel}	-0.09	-0.09	-0.08	-0.07	-0.06	-0.05	-0.05	-0.04	-0.03
		w	0.14	0.14	0.13	0.02	0.02	0.02	0.12	0.1	0.08
		D_a	0.86	0.8	0.76	0.8	0.71	0.6	0.77	0.64	0.51

Table 18. Pearson's coefficient for the models of the second group of chloride ingress models (with some time-dependent parameters) at 2.5 cm

Concrete			C45			C35			C25		
Age (years)			10	25	50	10	25	50	10	25	50
Eur.	Env	C_s	0.54	0.6	0.64	0.25	0.28	0.31	0.46	0.52	0.57
	Mat	D_{ar}	0.67	0.55	0.47	0.77	0.66	0.59	0.46	0.36	0.3
		α	-0.49	-0.57	-0.59	-0.56	-0.67	-0.72	-0.76	-0.78	-0.77
DuraCrete	Env	C_s	0.09	0.11	0.12	0.12	0.19	0.26	0.31	0.42	0.51
	Material	D_{rcm}	0.28	0.27	0.27	0.33	0.31	0.28	0.32	0.28	0.25
		k_e	0.36	0.35	0.34	0.39	0.36	0.33	0.41	0.36	0.32
		k_c	0.52	0.52	0.51	0.61	0.56	0.52	0.48	0.43	0.38
		k_t	0.06	0.06	0.05	0.06	0.05	0.05	0.07	0.06	0.05
		n	-0.49	-0.57	-0.62	-0.57	-0.63	-0.66	-0.59	-0.62	-0.62
Luping	Env	C_s	0.5	0.53	0.55	0.38	0.47	0.55	0.58	0.67	0.74
	Mat	D_{ar}	0.74	0.62	0.54	0.58	0.47	0.4	0.49	0.38	0.3
		n	-0.41	-0.55	-0.61	-0.72	-0.74	-0.73	-0.62	-0.61	-0.58

Table 19. Bias on the output's mean for models of the first group of chloride ingress models (non time-dependent parameters) at 2.5 cm (10^{-04} % mass of binder)

Concrete			C45			C35			C25		
Age (years)			10	25	50	10	25	50	10	25	50
Col.	Env	C_s	0.43	1.48	2.06	-0.31	-0.32	-0.34	0.22	0.48	0.63
	Mat	D_a	15.59	-18.17	-47.09	-0.94	-0.94	-0.94	-84.68	-63.28	-47.25
JSCE	Env	C_s	-1.08	-0.82	-0.67	-1.9	-1.9	-1.91	1.63	1.55	1.5
		γ_{cl}	1.12	1.14	1.15	-4.52	-4.58	-4.63	-4.1	-4.62	-4.88
	Mat	w/c	-9.69	-7.24	-5.39	-17.94	-17.43	-16.95	-26.4	-17.05	-12.14
LEO	Env	C_s	0	0.37	1.33	0.05	0.05	0.06	-0.39	-0.42	-0.42
		T	0.95	15.49	20.9	-59.81	-64.09	-67.45	-93.81	-94.32	-77.27
	Mat	W_{gel}	0.01	0.44	0.8	0.85	0.84	0.82	0.42	0.24	0.15
		w	0.02	-0.07	-1.68	-0.39	-0.4	-0.4	-9.23	-8.03	-6.31
		D_a	0.92	15.08	27.1	-60.43	-64.69	-68.02	-84.98	-86.43	-70.95

Table 20. Bias on the output's mean for models of the second group of chloride ingress models (with some time-dependent parameters) at 2.5 cm (10^{-05} % mass of binder)

Concrete			C45			C35			C25		
Age (years)			10	25	50	10	25	50	10	25	50
Eur.	Env	C_s	-0.35	-0.22	-0.08	-0.89	-0.92	-0.95	3.5	3.94	4.12
	Mat	D_{ar}	-16.98	-34.34	-44.2	-51.67	-53.69	-55.46	-79.89	-69.88	-60.56
		α	34.55	37.34	31.67	43.97	43.88	43.69	-44.3	-47.96	-76.23
DuraCrete	Env	C_s	0.26	0.69	1.2	-3	-3.03	-3.06	-1.17	-1.12	-1.03
	Material	D_{rcm}	6.02	9.64	10.83	-68.78	-70.89	-72.56	-79.79	-67.14	-56.08
		k_e	10.14	16.75	19.41	-101.51	-104.4	-106.67	-126.33	-106.85	-89.46
		k_c	21.74	35.71	40.42	-243.38	-250.29	-255.74	-176.31	-148.99	-124.72
		k_t	0.29	0.46	0.51	-3.24	-3.31	-3.37	-4.13	-3.55	-3.01
		n	24.96	67.06	114.75	-5.93	-13	-19.47	-64.83	-92.54	-103.39
Luping	Env	C_s	45.95	45.91	40.6	-4.41	-7.53	-10.39	-96.74	-100.66	-99.12
	Mat	D_{ar}	54.18	69.64	75.25	-82.08	-85.2	-87.9	-15.11	-34.59	-44.97
		n	-7.6	-22.41	-32.6	-4.23	-7.32	-10.15	-81.25	-65.77	-54.07

Table 21. Output's standard deviation for the models of the first group of chloride ingress models (non time-dependent parameters) at 2.5 cm (% mass of concrete)

Concrete			C45			C35			C25		
Age (years)			10	25	50	10	25	50	10	25	50
Colleparidi	Env	C_s	0.01	0.08	0.17	0.09	0.14	0.16	0.16	0.2	0.22
	Mat	D_a	0.03	0.1	0.12	0.01	0.01	0	0.15	0.1	0.07
JSCE	Env	C_s	0.43	0.49	0.52	0.19	0.21	0.22	0.27	0.28	0.29
		γ_{cl}	0.25	0.29	0.31	0.38	0.42	0.44	0.5	0.53	0.54
	Mat	w/c	0.07	0.05	0.03	0.11	0.07	0.05	0.09	0.05	0.04
	Env	C_s	0.00003	0.006	0.03	0.06	0.11	0.14	0.09	0.15	0.18
		T	0.0002	0.01	0.04	0.1	0.09	0.07	0.12	0.1	0.07
LEO	Mat	W_{gel}	0.00004	0.002	0	0.01	0.01	0.01	0.01	0.01	0.01
		w	0.00006	0.004	0.01	0	0	0	0.03	0.02	0.02
		D_a	0.0004	0.02	0.07	0.17	0.15	0.12	0.19	0.16	0.12

Table 22. Output's standard deviation for the models of the second group of chloride ingress models (with some time-dependent parameters) at 2.5 cm (% mass of concrete)

Concrete			C45			C35			C25		
Age (years)			10	25	50	10	25	50	10	25	50
Eur.	Env	C_s	0.07	0.12	0.15	0.05	0.07	0.09	0.14	0.17	0.19
	Mat	D_{ar}	0.09	0.11	0.11	0.16	0.16	0.16	0.15	0.13	0.1
		α	0.07	0.11	0.14	0.11	0.16	0.19	0.25	0.27	0.26
DuraCrete	Env	C_s	0.001	0.004	0.009	0.07	0.11	0.13	0.15	0.18	0.2
	Material	D_{rem}	0.005	0.01	0.02	0.17	0.15	0.13	0.15	0.12	0.1
		k_e	0.006	0.01	0.03	0.2	0.18	0.16	0.19	0.15	0.12
		k_c	0.01	0.02	0.04	0.32	0.29	0.25	0.23	0.18	0.15
		k_t	0.001	0.003	0.005	0.03	0.03	0.02	0.03	0.02	0.02
		n	0.009	0.03	0.05	0.3	0.32	0.31	0.28	0.26	0.24
Luping	Env	C_s	0.05	0.08	0.11	0.1	0.13	0.15	0.16	0.19	0.21
	Mat	D_{ar}	0.08	0.1	0.11	0.16	0.13	0.11	0.14	0.11	0.09
		n	0.05	0.09	0.12	0.2	0.21	0.2	0.18	0.18	0.17

Table 23. Summary of the results of sensitivity analysis for all concrete carbonation models at 50 years

Concrete			C45				C35				C25			
Models	Param	E	P	M	Std	E	P	M	Std	E	P	M	Std	
Duracrete	R_{carb}	-0.46	-0.1	1229.2	3.28	-0.46	-0.08	8541.26	3.04	-0.46	-0.04	1170.37	2.3	
	RH	-1.93	-0.13	1229.99	4.33	-1.93	0.03	8525.41	1.04	-1.93	-0.1	1172.11	4.6	
	k_c	0.48	0.37	1250	11.42	0.48	0.24	8644.25	8.92	0.48	0.23	1184.31	12.2	
	k_t	0.48	0.05	1227.9	1	0.48	0.02	8523.79	0.78	0.48	0.01	1169.65	1.05	
	n	-1.44	-0.89	1404.14	27.66	-1.48	-0.95	11376.55	36.61	-1.48	-0.95	1557.57	50.4	
CEB	R_{carb}	-0.46	-0.04	0.47	2.08	-0.46	-0.67	216.64	5.79	-0.46	-0.04	0.49	0.23	
	RH	-1.93	-0.08	-1.58	4.14	-1.93	-0.06	-1.25	0.35	-1.93	-0.09	-1.57	0.46	
	k_c	0.48	0.24	-4.01	10.9	0.48	0.14	-4.51	0.92	0.48	0.24	-5.07	1.23	
	n	-2.28	-0.95	65.32	44.81	-2.28	-0.55	61.84	3.78	-2.28	-0.95	73.51	5.07	
	RH	-1.3	0.06	-5.34	7.56	-1.76	-0.92	10204.19	21.03	-1.76	-0.96	-618.89	31.6	
Oxand	R_c	-13.38	-0.99	41.08	123.47	-3.24	-0.36	9779.7	8.2	-2.31	-0.2	9.41	6.59	
	RH	-2.92	-0.68	0.08	0.35	-2.92	-0.64	9	0.35	-2.92	-0.69	0.11	0.48	
Ying-Yu	α_{hyd}	-0.53	-0.15	-0.01	0.08	-0.53	-0.13	-2	0.08	-0.23	-0.09	0.01	0.5	
	S_r	1.09	0.71	0.29	0.36	1.09	0.66	0.03	0.37	1.09	0.71	0.04	0.5	
	ϕ	0.89	-0.16	-0.96	0.18	0.89	-0.38	-0.003	0.06	0.6	-0.17	-1.58	0.26	
	c	-0.77	-0.09	0.01	0.05	-0.75	-0.08	0.02	0.05	-0.41	-0.06	0.0002	0.05	
	ρ	-0.91	-0.16	0.36	0.27	-0.91	-0.38	0.85	0.28	-0.91	-0.17	0.45	0.37	
	RH	-2.91	-0.53	0.03	3.58	-2.91	-0.66	0.07	3.7	-2.91	-0.47	0.16	6.8	
	α_{hyd}	-0.11	0.001	0.0003	0.17	-0.13	-0.04	0.004	0.2	0.24	0.05	0.12	0.6	
Miragliotta	S_r	-0.97	-0.57	-0.98	5.4	-0.97	-0.68	-1.02	4.01	-0.97	-0.49	-1.83	12.5	
	ϕ	2.05	0.59	0.3	3.94	2.05	0.24	0.04	1.3	1.75	0.71	1.39	10.3	
	c	-1.19	-0.11	0.05	0.72	-1.17	-0.14	0.04	0.7	-0.85	-0.08	0.1	1.3	
	RH	-2.91	-0.78	0.41	16.68	-2.91	-0.95	0.21	16.5	-2.91	-0.67	0.43	24.8	
Papadakis	α_{hyd}	-0.11	-0.04	-0.01	0.87	-0.14	-0.07	0.01	0.9	0.21	0.04	0.37	1.9	
	c	-1.16	-0.13	0.16	3.3	-1.17	-0.18	0.2	3.2	-0.94	-0.1	0.23	4.7	
	ϕ	1.38	0.6	-0.31	12.88	1.41	0.23	-0.05	4.1	1.19	0.71	-1.21	26.3	
	RH	-4.29	-0.69	2.44	31.59	-4.29	-0.72	0.06	0.07	-4.29	-0.63	3.8	4.69	
Hyvert	T	-0.46	-0.1	0.01	0.59	-0.46	-0.04	0.0003	0.001	-0.46	-0.003	0.0028	0.012	
	k_c	0.48	0.65	-11.15	29.52	0.48	0.67	-0.27	0.07	0.48	0.65	15.01	4.18	
	ϕ	0.67	0.16	-1.26	8.03	0.002	-0.01	-10 ⁻⁵	6 \times 10 ⁻⁵	0.49	0.22	-3.5	1.5	
	c	-1.29	-0.1	0.32	4.59	-0.65	-0.04	0.003	0.005	-1.13	-0.13	-0.7	0.71	
	α_{hyd}	-1.19	-0.21	1.63	9.48	-0.55	0.004	-7\times10⁻⁷	2\times10⁻⁵	-1.05	-0.15	-2.5	1.25	

Param = parameter, E = Elasticity coefficient, P = Pearson's coefficient, M = Bias on the output's mean [$\times 10^{-6}$ m], Std = Output's standard deviation [$\times 10^{-4}$ m]

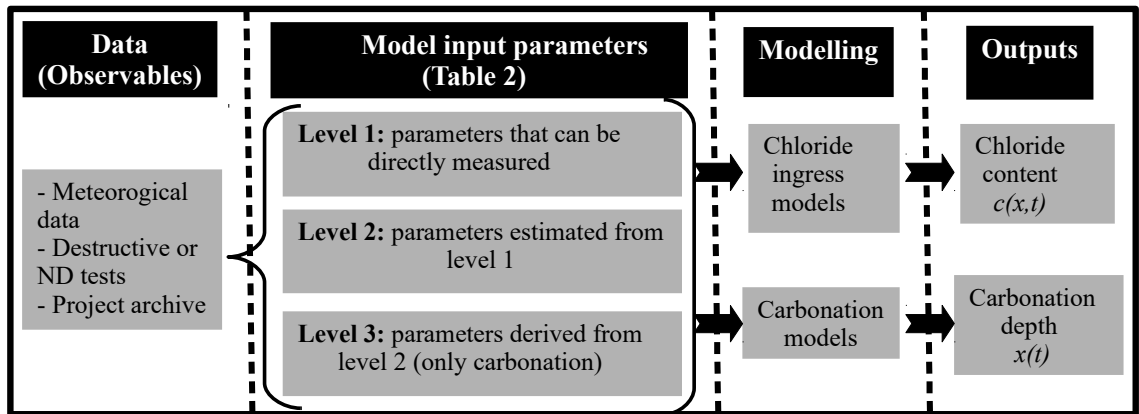


Figure 1. General representation of input parameters for analytical carbonation and chloride ingress models

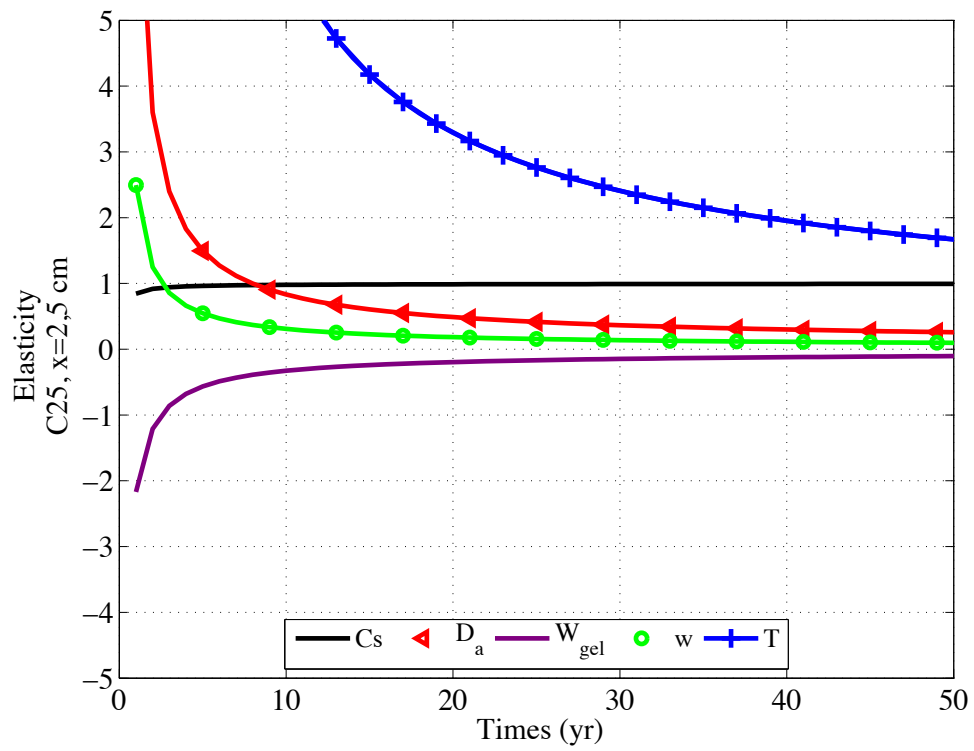


Figure 2. Elasticity of input parameters of the model of Leo for concrete C25 and at depth $x=2.5$ cm

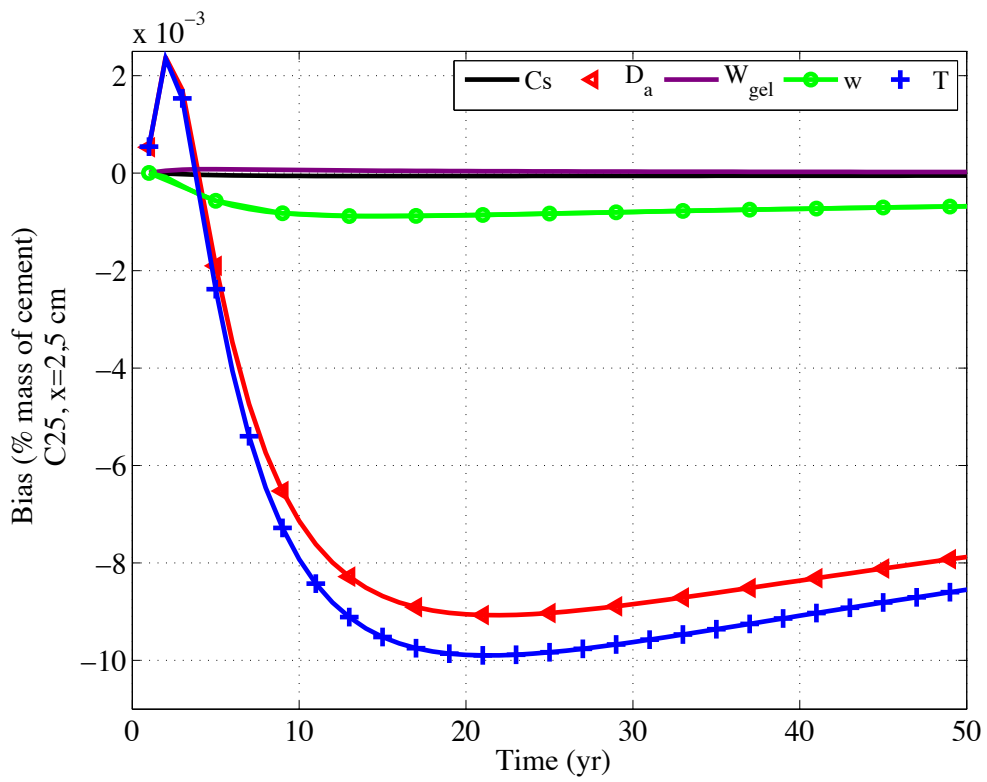
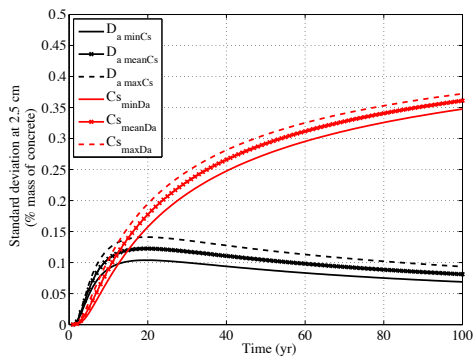
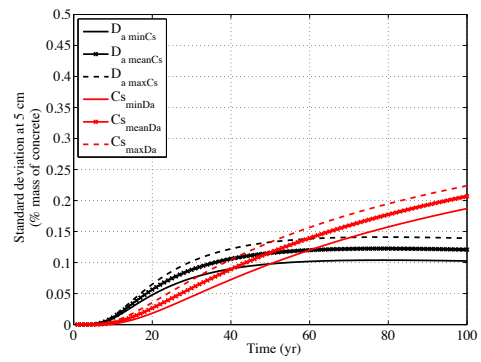


Figure 3. Bias of input parameters of the model of Leo for concrete C25 and at depth $x=2.5$ cm



(a)



(b)

Figure 4. Evolution of output's standard deviation of the Collepardi model applied to the concrete C45, when the parameter C_s (respectively D_a) varies and D_a (respectively C_s) is stated at his minimum, mean and maximum value at 2.5 cm (a) and 5 cm (b)

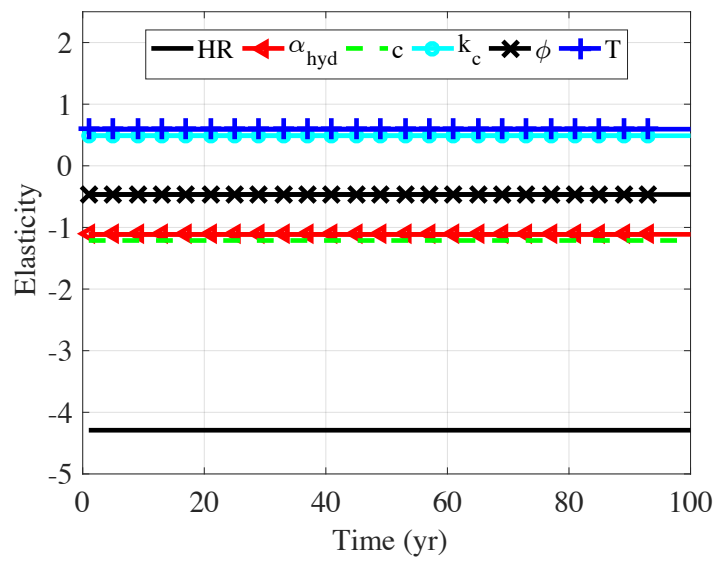


Figure 5. Elasticity of input parameters of the model of Hyvert for concrete C45

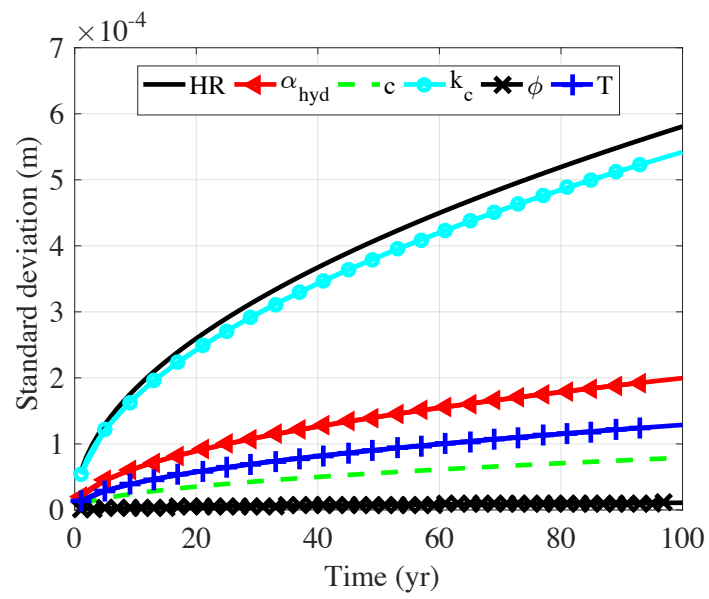


Figure 6. Standard deviation for the model of Hyvert for concrete C45

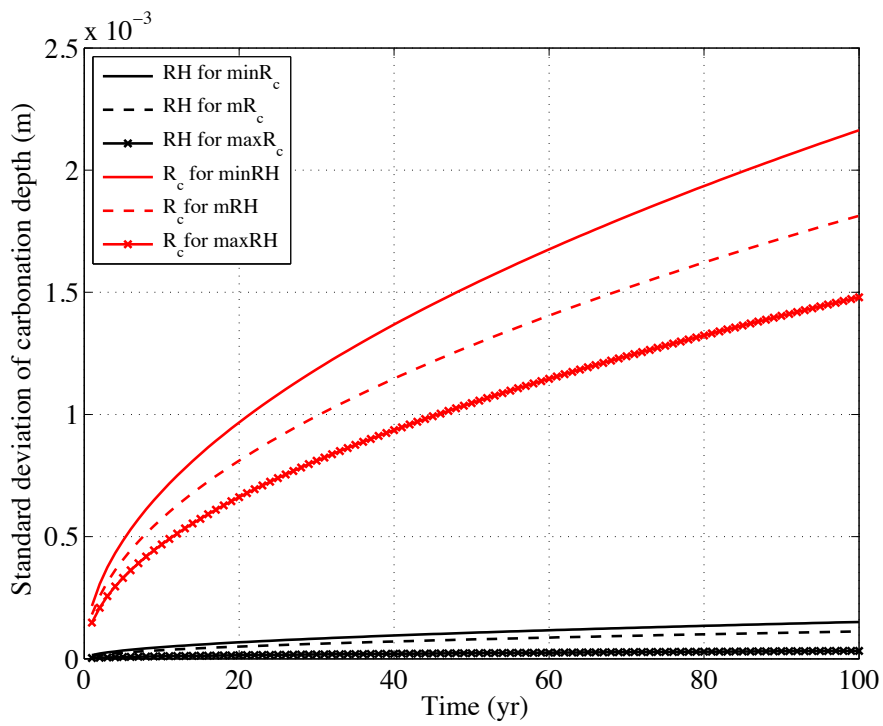


Figure 7. Standard deviation of output for several combinations of the constant and variable parameters, for the model of Oxand Petre-Lazar (2001). $\min x_i = x_i$ is stated on its minimum value; $\max x_i = x_i$ is stated on its maximum value; $m x_i = x_i$ is stated on its mean value; $x_i = x_i$ varies on its range of values.

Nomenclature

[Component]	The “component” content
[<i>AFm</i>]	AFm content
[<i>AFt</i>]	AFt content
[<i>C₂S</i>]	C ₂ S content
[<i>C₃A</i>]	C ₃ A content
[<i>C₃S</i>]	C ₃ S content
[<i>C₄AF</i>]	C ₄ AF content
[<i>CH</i>]	Portlandite content
[<i>CSH</i>]	CSH content
α	Age exponent of the Eurolighcon model which corresponds to achieved diffusion coefficient
α_1 and n_1	Adjusting parameters of Hyvert model
α_{hyd}	Hydration degree
β	Age exponent of the Eurolighcon model which corresponds to the potential diffusion coefficient obtained from a short time laboratory testing according to NT Build 443 NTBuild443 (1995)
$\Delta y(\mathbf{Z}, t)$	Proportional variation of model output
$\Delta y_k(\mathbf{Z}, t)$	Proportional variation of model output at depth x_k
Δz_i	Variation of the input z_i
ϕ	Porosity
ρ	Concrete density
ρ_{cor}	Pearson’s correlation coefficient
σ	Age exponent after integration
σ_{y_k}	Standard deviation of y_k
σ_y	Standard deviation of y
$\sigma_{z_i/y_k}(t)$	Standard deviation of the output at depth x_k when z_i is random
$\sigma_{z_i/y}(t)$	Standard deviation of the output when z_i is random
σ_{z_i}	Standard deviation of z_i
\mathbf{X}	Vector of input parameters that are specific to each model
\mathbf{Z}	Vector in which each component z_i is an input parameter of the model
$cov(y(t), z_i)$	Covariance of z_i and y
$cov(y_k(t), z_i)$	Covariance of z_i and y_k
ξ	Concrete diffusivity
a	Binding capacity for CO_2
a'	Required quantity of carbon dioxide for a complete carbonation
a_i	Lower bound of the variation interval
b_i	Upper bound of the variation interval
b_{k,z_i}	Bias coefficient when the parameter z_i is stated to its mean value at depth x_k
b_{z_i}	Bias coefficient when the parameter z_i is stated to its mean value
$C(x, t)$	Chloride content at distance x from the concrete surface and at time t
C_0	CO_2 content at the exposed surface
C_{abs}	Absorbed carbone dioxide
C_{ini}	Initial chloride content of the concrete
D	Measured diffusion coefficient or calculated using empirical formulation
$D(t)$	Instantaneous diffusivity
$D_{a,JSCE}$	Empirical formula to determine diffusion coefficient in the model of JSCE for OPC

D_{ach}	Achieved diffusivity
D_{ar}	Diffusivity value determined at a reference time t_r
D_{av}	Average diffusivity
D_{CO_2}	Diffusion coefficient of de carbone dioxide
D_{Du}	Diffusion coefficient according to DuraCrete (2000)
D_{Pa}	Diffusion coefficient according to Papadakis et al. (1991)
D_{rcm}	Migration coefficient obtained with rapid test according to NT Build 492 NTBuild492 (1999)
D_{Yu}	Diffusion coefficient according to Ying-Yu and Qui-Dong (1987)
$e_{i,k}(t)$	Elasticity at depth x_k over time
$e_i(t)$	Elasticity over time
f_p	Volumetric fraction of cement paste
$k(\xi(\mathbf{X}, t), x)$	Chloride ingress model factor
k_c	Parameter which assesses the cure condition effects
k_{exe}	Factor which introduces execution conditions
k_{exp}	Factor which introduces exposure conditions
k_e	Parameter which assesses environmental conditions
$k_{P,E}$	Part of k_P associated to environmental proprieties
$k_{P,M}$	Part of k_P associated to material proprieties
k_P	Factor which introduces phenomenons that could influence the diffusion coefficient of the carbon dioxide into concrete porosity
n	Age exponent before intergration
P_{atm}	Atmospheric pressure
P_{CO_2}	Pressure of CO_2
R	Gas constant
R_{carb}	Ability of the considered concrete, in resisting carbonation
R_c	Compressive strength
S_r	Saturation degree
t_0	Reference period for carbonation model
t_c	Cure duration
t_{ex}	Age of the concrete at the beginning of the exposure to chloride environment
t_r	Reference time for chloride ingress model
x	Distance from the concrete surface
y	Model output
Z_{i0}	\mathbf{Z} when a parameter z_i is stated at its mean value \bar{z}_i
z_i	Input variable
RH	Relative humidity
RH_{ref}	Reference relative humidity
T	Temperature