

Ultrafine versus coarse grained Al 5083 alloys: From low-cycle to very-high-cycle fatigue



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ABSTRACT

The fatigue performance of coarse and ultrafine-grained (UFG) 5083 Al alloy were compared, from low to very high cycle fatigue. The UFG alloy exhibited cyclic hardening and predominant kinematic hardening. At high plastic strain amplitude (and only in this regime), it showed easier crack initiation and a lower fatigue resistance. Its resistance to HCF was hardly better than that of its coarse grained counterpart until 2.10^6 cycles, but 43% higher in VHCF, until 5.10^8 cycles. Beyond that point, internal crack initiation occurred, and the fatigue resistance of the UFG material decreased, which was explained using Fracture Mechanics.

1. Introduction

Substantial improvements in yield stress and tensile strength of metals and alloys can be obtained through a refinement of their microstructure to obtain nano-crystalline metals (grain size smaller than 100 nm) or ultrafine grained (UFG) metals (with a mean grain size ranging from 100 nm to 1 μ m). The latter can be obtained either by compaction of nano-crystalline powders produced by cryo-milling or by several severe plastic deformation processes, among which Equal Channel Angular Pressing (ECAP) is quite popular.

For many industrial applications though, the fatigue performance is a selection criterion of structural materials and it was thus assessed for many UFG alloys [1,2]. However, fatigue damage is very sensitive to microstructural features like precipitates size and spatial distribution, heterogeneity in grain size and shape, as well as local textures, which all depend on the manufacturing process. As a consequence, conclusions drawn for materials issued from friction-stir processing, high pressure torsion, accumulative roll bonding, or cryo-milled powder consolidation may not be valid for those issued from ECAP [3]. Besides, observations made on ECAPed materials may themselves differ, depending on the ECAP route (i.e. rotation of the billet between consecutive extrusions) [4], or even on the number of ECAP passes [5].

Furthermore, the gain or loss in fatigue resistance due to grain refinement into the UFG regime is likely to be dependent on the intended life and on the loading mode. A higher tensile strength as compared to coarse grained (CG) materials is expected to improve the resistance of

UFG materials to high or very high cycle fatigue (denoted below as HCF and VHCF), which is generally observed [1,2,5–7], while a lower ductility is expected to reduce the performance in low-cycle fatigue (LCF), which is generally observed in strain-controlled tests [1,8–10], but not in stress-controlled tests [11,12]. While the entire S-N curve of a UFG material generally stands above that of its CG counterpart, their strain-life curves often cross [1,4].

Pure UFG metals, even at room temperature (RT), are prone to cyclic softening induced by grain growth. Such grain growth can occur inside localized shear bands, as observed for UFG Al [10,13], or UFG Cu [14], around micro-cracks [15], from unrefined grains, or any pre-existing inhomogeneity [16,17]. However, An et al. [18] and Zhang et al. [15] have shown the beneficial effect of an increased Al or Zn content on the cyclic stability and fatigue performance of UFG copper alloys, while Canadinc et al. [5] have shown that solute Mg, which restricts dislocations mobility and recovery processes, promotes cyclic stability in UFG Al-Mg alloys.

Walley et al. [19] investigated the LCF behavior of a UFG Al 5083 -obtained by compaction of cryo-milled powder- through plastic strain-controlled push-pull tests. In spite of a moderate grain growth observed by TEM after cyclic loading at $\Delta\epsilon_p/2 = 0.2\%$, cyclic hardening was observed. For a given plastic strain range, a similar fatigue life was found for CG and UFG alloys. By contrast, Sedighi et al. [9] who investigated the LCF behavior of a UFG Al 5083 alloy obtained by Equal Channel Angular Rolling, through total strain-controlled tests reported a slight cyclic softening and reduced fatigue lives, as compared to the

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CG material. Patlan et al. [11] investigated the LCF and HCF behavior of a UFG Al 5056 Al-Mg alloy obtained by ECAP. They did not observe any significant cyclic hardening or softening during plastic-strain-controlled LCF tests, but a reduced life compared to the CG material. Under stress-control, the UFG material had a better resistance to LCF, but nearly the same resistance as the CG material in the HCF regime. A study in the HCF regime was run on a UFG Al 5083 obtained by cryo-rolling with or without subsequent warm rolling by Singh et al. [6]. They reported a significant enhancement in fatigue strength of the UFG material, compared to the coarse-grained material in the range $5 \cdot 10^5 - 6 \cdot 10^6$ cycles. The S-N curves did not exhibit any horizontal asymptote. Majchrowicz et al. [7] investigated the HCF behavior of a UFG 5083 alloy obtained by hydro-extrusion through repeated tension tests at -50°C , 25°C and 100°C . At RT, they observed a significant enhancement in fatigue strength of the UFG material, compared to the coarse-grained material in the range $5 \cdot 10^5 - 2 \cdot 10^6$ cycles. Micro-hardness measurements made before and after the fatigue tests at 25°C suggested a slight softening, which was not due to grain growth, but to a reduction in dislocations density by a recovery process, according to TEM observations and X-ray diffraction peak analysis.

From this survey of the literature devoted to Al 5083 or 5056, it appears that for nearly the same composition, depending on the method used to obtain a UFG microstructure, cyclic hardening or softening can occur in LCF, with or without a reduction in fatigue resistance in strain-controlled tests, and that the expected improvement of the resistance to HCF is not always observed. The gain or loss in fatigue performance associated with a UFG microstructure is thus a more complex issue than anticipated, and seems to be influenced by other factors than strength and ductility.

Surprisingly, while the strong texture generally inherited from severe plastic deformation processes, and the presence of intermetallic particles might have a decisive influence on the damage mechanisms, their roles have not been much discussed so far. These two points deserve more attention and are considered in the present study. Furthermore, the idea that UFG materials have a better resistance to crack initiation –inferred from their better resistance to HCF– is generally supposed to hold whatever the loading range. But in most papers, the description of fatigue damage is purely qualitative, and does not allow to check that point. In the present study, an extensive statistical analysis of secondary micro-cracks shows that this may be wrong in LCF. Concerning cyclic plasticity of UFG materials, nearly all previous work focused on the amount and kinetics of hardening or softening, with little attention paid to the isotropic/kinematic character of this hardening, which might however shed light on the underlying deformation mechanisms. Vinogradov et al. [20] as well as Patlan et al. [11] underlined the more pointed shape of the stress-strain loops in UFG copper, suggesting a stronger Bauschinger effect. In the present study, constitutive equations are identified for both CG and UFG 5083 Al alloy, allowing a comparison of their isotropic/kinematic hardening, and the results are discussed, based on TEM observations.

From the elements provided above it is clear that in order to fully determine the potential and limitations of a UFG alloy in fatigue, it is important to investigate its behavior over a wide range of stress/strain amplitudes and fatigue lives. However, the literature on VHCF of UFG materials is very limited, and deals only with copper with various impurity levels [21–23] or commercially pure aluminum [24]. In both metals, cracks kept initiating from PSBs on the surface, like in LCF and HCF regimes, and no internal crack initiation was observed in VHCF, as it is often the case in CG alloys in this regime. Grain coarsening was observed around cracks propagating at rates between 10^{-12} and 10^{-10} m/cycle in pure copper, but not in commercially pure Cu [22,23]. The VHCF behavior of UFG alloys thus remains to be explored. That is why the present study compares the fatigue performance of a 5083 Al-Mg UFG alloy obtained by ECAP to that of the as received, CG material, from about 10^2 to 10^{10} cycles. The results are discussed based on microstructural features, quantitative data about fatigue damage, as well

Table 1
Chemical composition of the material.

Element	Mg	Fe	Mn	Si	Cr	Cu	Al
Weight%	4.6	0.36	0.46	0.22	0.15	0.16	Balance

as on Fracture Mechanics.

2. Experimental procedure

2.1. Investigated materials

An extruded bar of Al-5083 (composition in Table 1) in the H112 condition – that is slightly strain hardened – with a diameter of 20 mm was used to machine specimens of CG material, or rods for ECAP processing.

Fig. 1 shows the initial CG microstructure in longitudinal (Fig. 1a) and transverse sections (Fig. 1b), as revealed by electron backscatter diffraction (EBSD). The grains are nearly equiaxed in the transverse plane, with a diameter ranging from 400 to 900 μm , but are elongated parallel to the bar axis, with a mean aspect ratio of 2.5. A typical bar texture with $\langle 111 \rangle$ and $\langle 100 \rangle$ fibers is observed (Fig. 1d). A post-treatment of EBSD data, based on Nye's tensor computation [25] and available in the ATEX© software allowed the density of geometrically necessary dislocations (GND) to be estimated as $3.6 \cdot 10^{13} \text{ m}^{-2}$. The material contains two types of intermetallic particles (Fig. 1c). EDS chemical analyses show that one type is rich in Mg and Si, and the other in Fe and Mn. These particles form rows parallel to the bar axis, up to $18 \mu\text{m}$ long. In the transverse section, their maximum diameter is $7 \mu\text{m}$.

105 or 80 mm long pieces of the same bar were submitted to 6 ECAP passes at 150°C , with a punch displacement rate of 0.05 mm/s , following route Bc (rotation of 90° around the sample axis between each pass), in a lubricated die with an angle of 90° . The resulting microstructure is presented in Fig. 2, with the grain size distribution. This widespread distribution ranges from 200 nm to $2 \mu\text{m}$, with a mean value around 600 nm . The microstructure is thus not fully ultrafine grained (UFG) but also contains some micron-sized grains.

The pole figures reveal a stronger and different texture than in the CG material, with a high density of $\{110\}$ directions normal to the entrance and exit directions of the die, which is typical after ECAP following route Bc [26]. Fig. 3 compares maps of the maximum Schmid factor in each grain (for a stress applied in the same direction as during the fatigue tests) in CG and UFG alloys, and the corresponding distributions of Schmid factors. The fraction of grains with a Schmid factor above 0.4 on at least one of their slip systems is 48% in the CG material, but only 17% in the UFG material.

More than 80% of the grain boundaries are high angle grain boundaries (HAGBs, with more than 15° misorientation). The GND density after ECAP is increased to $9.0 \cdot 10^{14} \text{ m}^{-2}$.

The grains are elongated at $50 - 60^\circ$ to the extrusion axis, which corresponds to the shearing direction during the last ECAP pass. The intermetallic particles are somewhat fragmented by this severe plastic deformation, but their fragments remain clustered, and the diameter of the largest particles on a transverse section is not significantly lower than in the CG material.

Fig. 4 compares the engineering stress-strain curves of CG and UFG materials in tension at $2 \cdot 10^{-3} \text{ s}^{-1}$. Both materials exhibit serrated flow, due to solute Mg-induced dynamic strain aging, but this aspect is beyond the scope of the present paper. As can be seen in Table 2, the 0.2% yield stress and ultimate tensile stress (UTS) of the UFG material (314 and 391 MPa, respectively) are much higher than those of the CG material (128 and 281 MPa, respectively). However, the ductility of UFG material (15.8%) is somewhat reduced, as compared to its CG counterpart (21.6%).

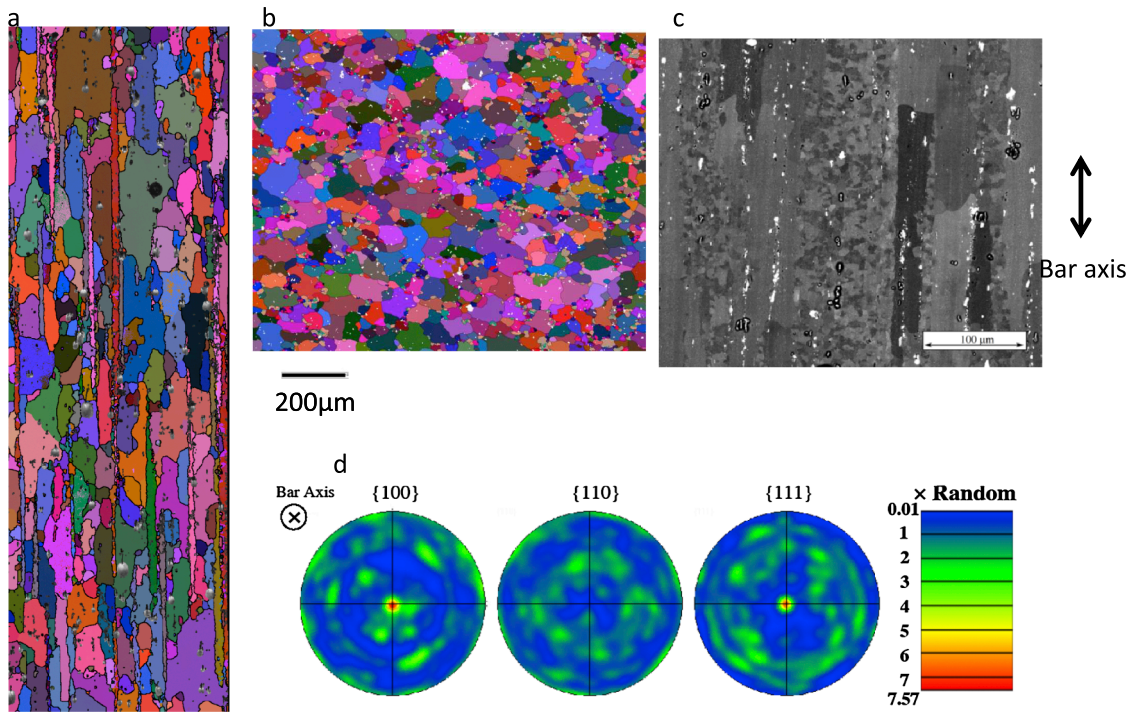


Fig. 1. Microstructure of the coarse grained material. EBSD maps of Euler angles (a) parallel and (b) normal to the bar axis (c) Rows of intermetallic particles along the bar axis and (d) pole figures.

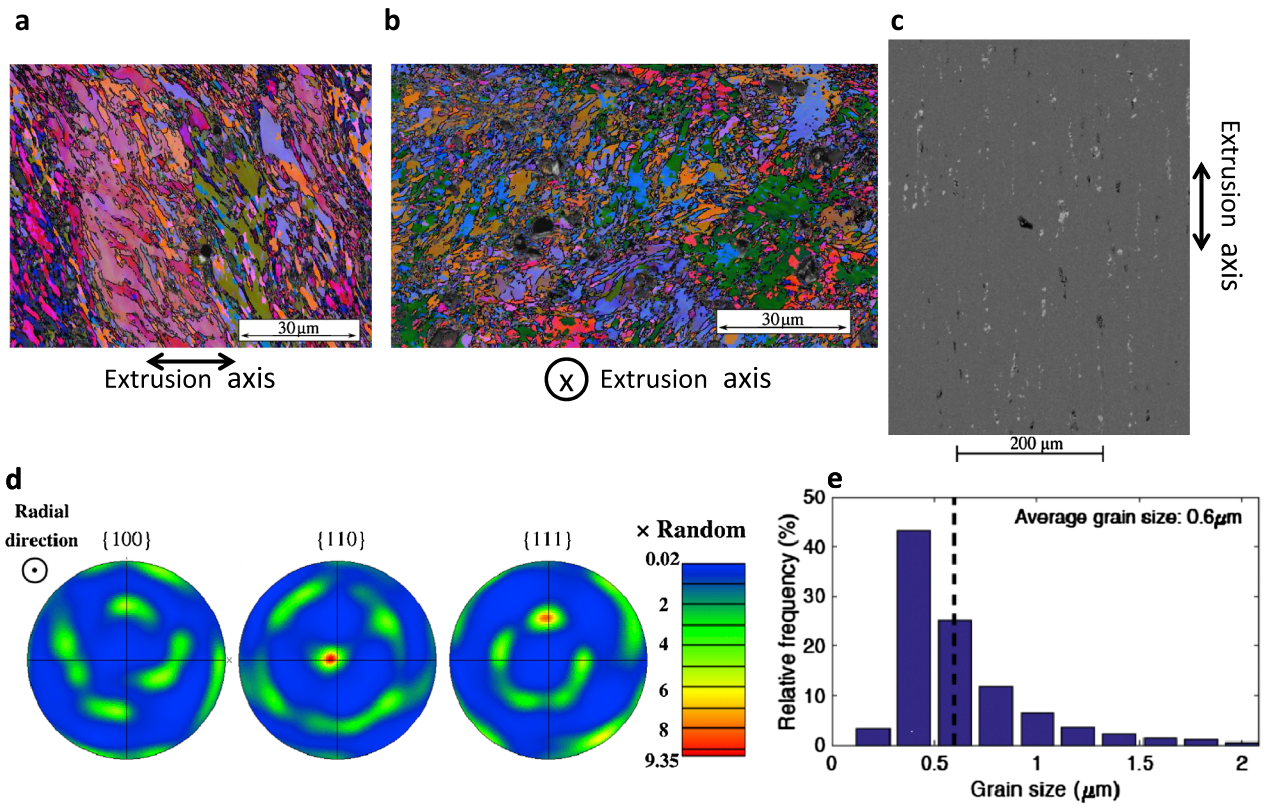


Fig. 2. Microstructure of the ultrafine grained material. EBSD maps of Euler angles (a) parallel and (b) normal to the bar axis, (c) BSE image of the fragmented intermetallic particles, (d) pole figures and (e) the grain size distribution.

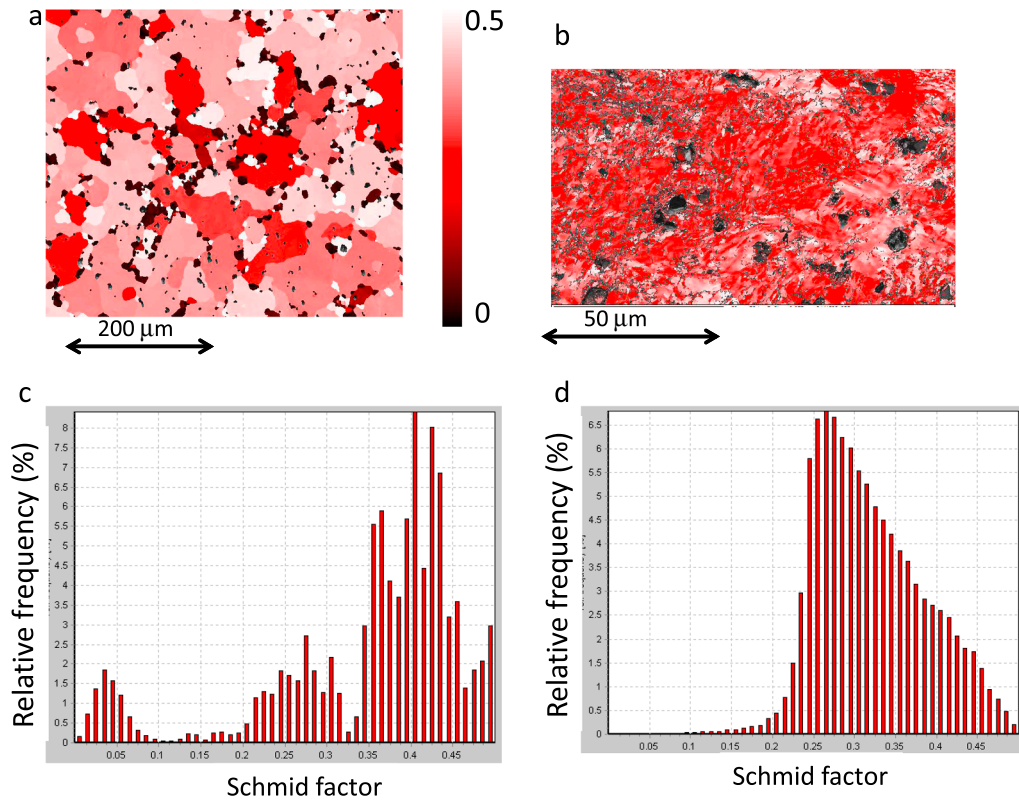


Fig. 3. (a, b) Maps of maximum Schmid factor in each grain and (c, d) corresponding histograms in CG (a, c) and UFG (b, d) materials.

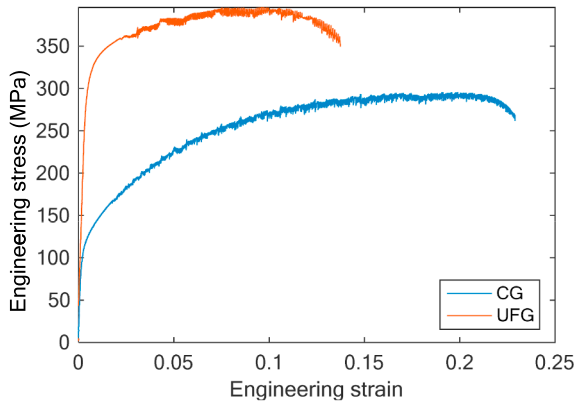


Fig. 4. Engineering stress-strain curves of coarse and ultrafine grained materials.

Table 2
Tensile properties of CG and UFG Al 5083 at 2.10^{-3} s^{-1} .

Material	$\sigma_{0.2\%}$ (MPa)	UTS (MPa)	Fracture strain (%)
CG Al 5083	128 ± 3	281 ± 7	21.6 ± 1.6
UFG Al 5083	314 ± 8	391 ± 10	15.8 ± 1.2

2.2. Procedures for the fatigue tests and subsequent observations

90 mm long cylindrical specimens, 8 mm in diameter and 16 mm in gage length (Fig. 5a), for LCF and HCF push-pull tests, as well as 54 mm long waisted cylindrical specimens for VHCF push-pull tests (Fig. 5b) were machined from the as received bar, or from the extruded rods, with the tensile axis parallel to the die exit direction. Both types of samples were mechanically polished and electro-polished.

A servohydraulic testing machine was used for fully reversed push-

pull tests, which were plastic strain controlled, thanks to an extensometer, in LCF (with a fixed strain rate of 10^{-3} s^{-1}), or stress-controlled in HCF (with a frequency between 5 and 10 Hz). Stress control in the plastic regime would not allow a good control of the strain rate, which might lead to substantial heating of the samples.

An ultrasonic testing device operating at 20 kHz was used for fully reversed push-pull tests in the VHCF regime. The geometry of the specimen, given in Fig. 5b was designed to have its first longitudinal vibration mode at a frequency of 20 kHz. The machine was controlled via the tension applied to a piezoelectric converter, and therefore the vibration amplitude imposed on one edge of the specimen was controlled. Air cooling was applied to the samples, whose temperature never rose by more than 1°C , as checked by infrared thermography. The stress applied to the specimen was calculated with a harmonic model, assuming a purely elastic response of the tested material. The normalized axial stress profile along the gage length, issued from the harmonic calculation is plotted in Fig. 5c. Since the stress peaks at mid-length, fatigue fracture is expected to occur in that plane. However, in a few cases, the fracture plane was slightly shifted along the axis (by a few hundred microns). In that case, the stress amplitude in the fracture plane was reported and used to plot the S-N curve. However, in all cases, the correction remained small.

Optical digital microscopy was used for a statistical analysis of micro-cracks density, lengths and orientations on the outer surface of fatigued samples. Series of pictures with a magnification of 200–300 were captured and stitched to cover the whole gage length of the specimens. To ensure a statistical representativeness, a minimum of three such bands per specimen, at different angular positions along the circumference were used for a manual counting of micro-cracks and a measurement of their lengths, using imaging softwares (Gimp or Fiji). Such counting was done only for the high loading ranges, which produced at least a few tens of micro-cracks in the observed area.

Scanning electron microscopy was used for observations of the fracture surfaces, and in some cases after cross sectioning with a Focused Ion Beam (FIB).

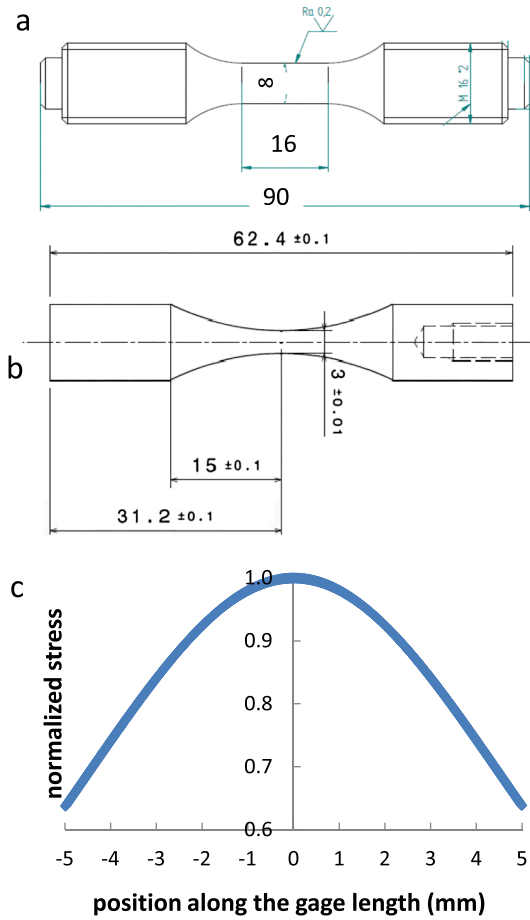


Fig. 5. Specimens geometry for (a) LCF and HCF tests, (b) VHCF tests and (c) the normalized profile along the gage length.

TEM was used to analyze and compare the dislocation structures induced by cyclic plasticity in CG and UFG materials. For that purpose, slices were cut normal to the tensile axis of fatigued samples, as far away from the fracture surface as possible, mechanically ground, and finally electropolished in a double jet Tenupol apparatus, using a solution of 25% nitric acid in 75% methanol kept at -33°C , under 12 V. Observations were carried out under bright-field and/or weak-beam conditions.

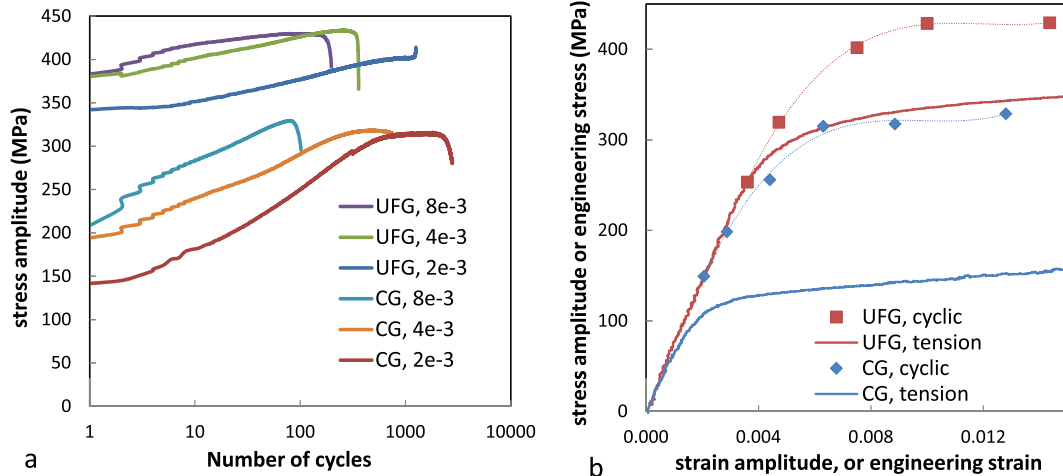


Fig. 6. (a) Evolution of the stress amplitude and (b) monotonic and cyclic stress-stress curves.

3. Experimental results

3.1. Cyclic plasticity

Fig. 6a compares the evolutions of the stress amplitude versus the number of cycles, in CG and UFG materials during plastic-strain controlled tests. Both materials exhibited cyclic hardening. This implies that the cyclic stress-strain curves -plotted using the stress amplitudes at mid-life, since no steady-state value exists- stand above the monotonic stress-strain curves (Fig. 6b). Cyclic hardening was more moderate in the UFG material, which will be discussed later.

The nature of this hardening was also different, as evident from the compared mid-life stress-strain loops CG/UFG at the same amplitude, shown in Fig. 7: the loops are more elongated, with a steeper slope in the plastic regime in the UFG material, which suggests a more pronounced kinematic hardening (in other words: stronger Bauschinger effect).

The recorded stress-strain loops were fed to a Levenberg-Marquardt algorithm in order to fit constitutive equations using isotropic and non-linear kinematic hardening variables, according to Lemaitre and Chaboche's model [27]:

Von Mises yield criterion was used, since the aim is not to describe the plastic anisotropy of the UFG material, but just the nature of its uniaxial cyclic hardening:

$$J_2(\sigma - X) - R = 0 \quad (1)$$

where J_2 denotes the second invariant. R denotes the isotropic hardening variable:

$$R = R_0 + Q(1 - e^{-b.p}). \quad (2)$$

X denotes the kinematic hardening variable:

$$dX = C. d\epsilon_p - D. X. dp \quad (3)$$

where p denotes the cumulated plastic strain, R_0 , Q , b , C and D are material parameters.

The best sets of parameters for CG and UFG materials are reported in Table 3. Fig. 8 compares the measured and simulated stress-strain loops. The importance of kinematic hardening can be estimated by the ratio C/D , which corresponds to the asymptotic value of the kinematic variable at high tensile strain, while the importance of isotropic hardening is indicated by parameter Q . In UFG material, C/D is equal to 121.2 MPa, and is 3.3 times higher than Q , (36.2 MPa), while in CG material, C/D is equal to 94.6 MPa, which is smaller than Q (132 MPa). Kinematic hardening thus largely prevails in the UFG material, while isotropic hardening predominates in the CG alloy.

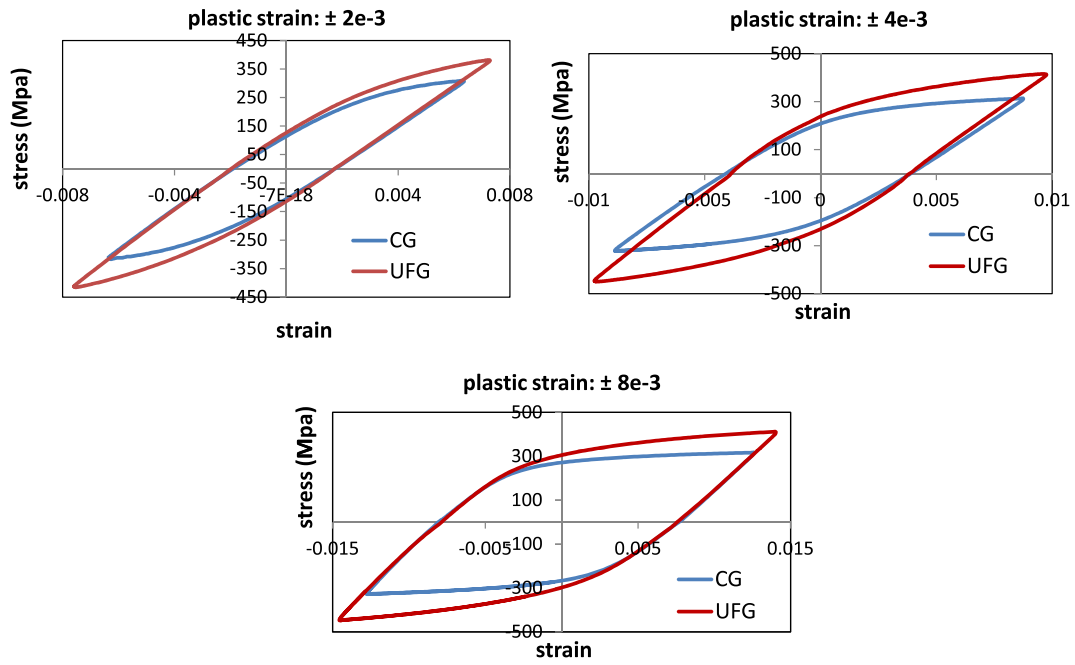


Fig. 7. Compared mid-life stress-strain loops for CG and UFG materials.

Table 3
Best fit parameters for the constitutive equations of CG and UFG materials.

	E (GPa)	ν	R_0 (MPa)	Q (MPa)	b	C (MPa)	D
CG	67	0.3	102.5	132	2.6	54,467	575.7
UFG	66.5	0.3	276	36.2	9.86	29,523	243.5

Figs. 9 and 10 show TEM micrographs of dislocation patterning for the CG and UFG materials, respectively and for plastic strain amplitudes of $\pm 2.10^{-3}$ and $\pm 8.10^{-3}$. In CG material, a dense and uniform distribution of tangled and jogged dislocations was observed, for the lower amplitude (Fig. 9a). Many dislocations loops were also found in the microstructure, probably formed by the dipole bypassing mechanism after jog dragging [28]. The presence of curved dislocations near the

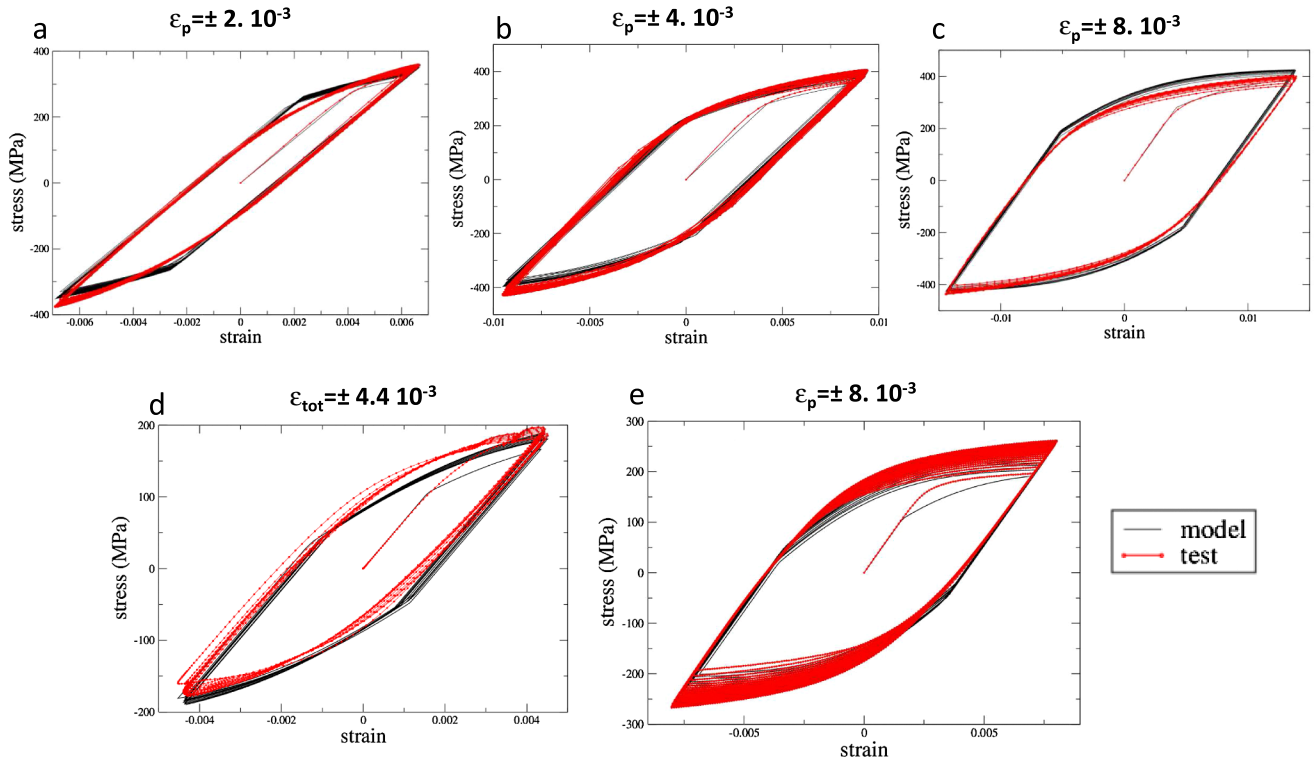


Fig. 8. Comparison of measured and simulated stress-strain loops for UFG (a-c) and CG (d, e) materials.

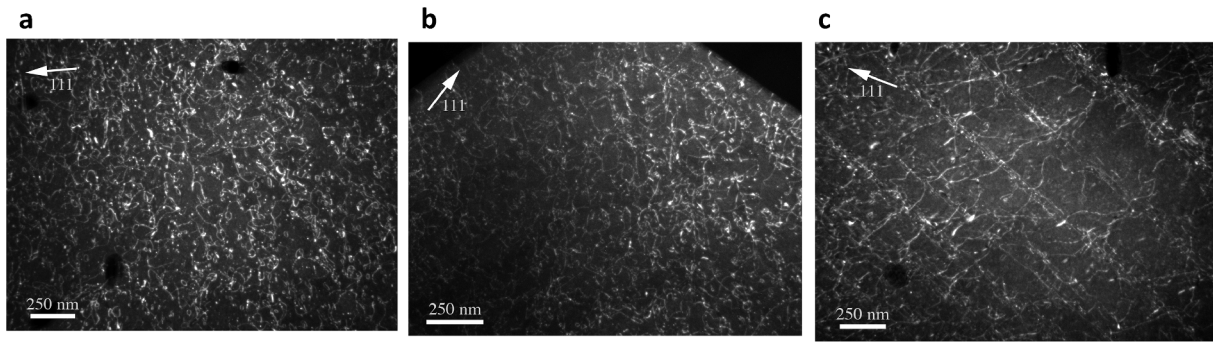


Fig. 9. Weak-beam dark field TEM micrographs of coarse grained LCF samples. (a) $\epsilon_p = \pm 2.10^{-3}$, $N_f = 2784$ cycles (b–c) $\epsilon_p = \pm 8.10^{-3}$, $N_f = 102$ cycles.

incoherent second phase particles suggests the Orowan-type bypassing mechanism. No organized features like veins, cells, labyrinths or ladders were found. In the UFG material, a heterogeneous microstructure was observed from one grain (or sub-grain) to the other after fatigue, contrary to the CG material for the same amplitude. While the smallest grains exhibited low dislocation densities (Fig. 10a), the larger ones contained loops and tangled dislocations (Fig. 10b), not so different from those observed in the CG material. The strong curvature of the dislocations suggests high internal stresses and probable pinning effects. Dislocation loops bowing out of low-angle grain boundaries (LAGBs) could also be observed (Fig. 10b).

For the larger amplitude, a high density of tangled dislocations was observed in most grains of the CG material (Fig. 9b), and occasionally, some long and narrow band-like structures (Fig. 9c). In the UFG material, a very dense and non-structured network of tangled dislocations and loops was observed, without any obvious difference with the microstructure found at the lower amplitude (Fig. 10c). The grain-to-grain heterogeneity in dislocations content previously observed was still present. The post-treatment of EBSD mappings made on the outer surface of fatigued samples did not reveal any evolution in the mean grain size.

3.2. Fatigue lives

Fig. 11 shows the fatigue lives versus plastic strain amplitudes in the LCF regime. Except for the highest amplitude, for a given plastic strain range, the UFG material exhibits a lower fatigue life than its CG counterpart, and the difference tends to rise as the plastic strain range decreases. This unusual trend will be discussed later.

The S-N curves for CG and UFG materials, from LCF to VHCF are compared in Fig. 12. Several domains can be distinguished. In the LCF range ($N < 10^4$ cycles) the S-N curve of the UFG material lies clearly above that for the CG material. For intermediate lives (N ranging from

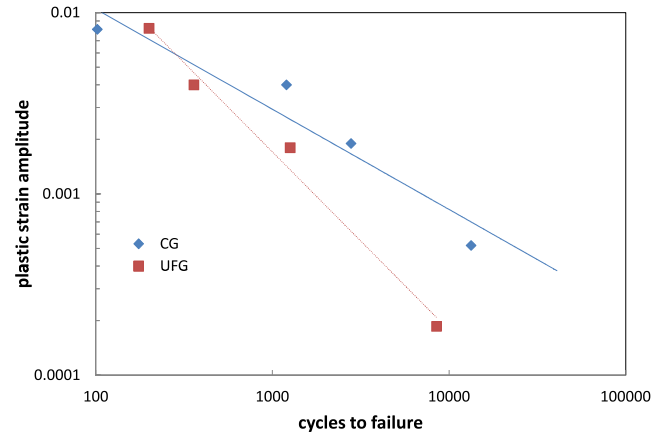


Fig. 11. Compared fatigue lives of CG and UFG materials in the LCF regime.

10^4 to 2.10^6 cycles) the two curves nearly overlap, with a slightly better resistance of the UFG material. Above 2.10^6 cycles, the S-N curve of the CG material exhibits a plateau at 140 MPa, which corresponds to 1.09 times the 0.2% yield stress of the CG material. The S-N curve of the UFG material first exhibits a plateau at 200 MPa, which is 0.64 times its 0.2% yield stress. However, above 5.10^8 cycles, the fatigue resistance of the material slowly decreases, and at 5.10^9 cycles, it has the same level as for the CG material.

3.3. Damage mechanisms

In CG material, crack initiation always occurred at the surface, mostly from persistent slip bands (Fig. 13a), and marginally from broken intermetallic particles (Fig. 13b), even in the VHCF regime. More than one crack initiation site was often observed on the fracture

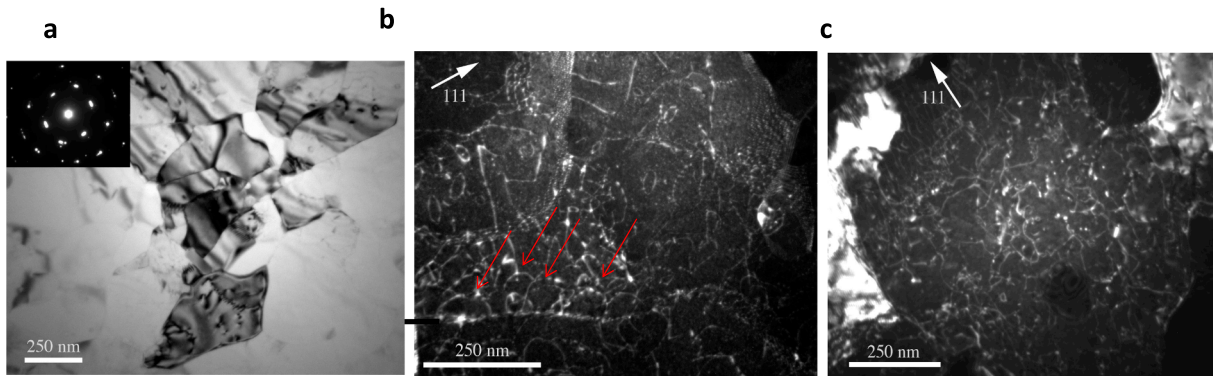


Fig. 10. TEM observations of UFG LCF samples. (a–b) $\epsilon_p = \pm 2.10^{-3}$, $N_f = 1259$ cycles, (c) $\epsilon_p = \pm 8.10^{-3}$, $N_f = 200$ cycles. Micrographs (b) and (c) were taken under weak-beam dark field conditions. Red arrows show dislocations bowing out from a LAGB. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

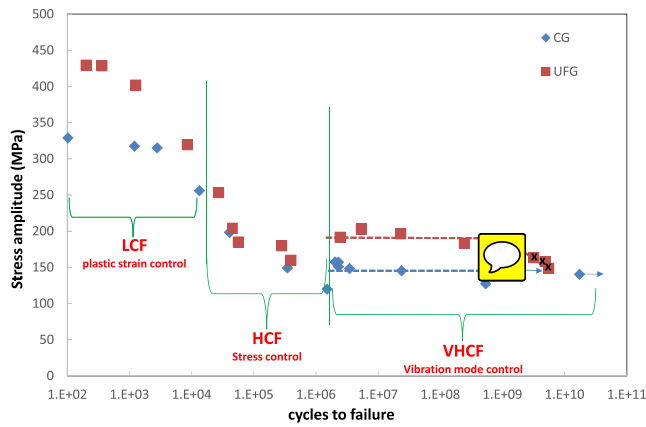


Fig. 12. Compared S-N curves for CG and UFG materials. A superimposed \times denotes internal crack initiation.

surfaces, up to $5.8 \cdot 10^8$ cycles. These surfaces, quite classically, were characterized by a crystallographic faceted area around the crack initiation(s) site(s), corresponding to stage I growth, followed by a striated area (stage II), and finally a more or less slanted area covered with dimples, corresponding to ductile fracture. No significant difference was noticed between the fracture surfaces corresponding to LCF, HCF and VHCF, except the decreasing size of the shear lips when the loading range decreased.

By contrast, in the UFG material, two regimes have to be considered separately in terms of damage mechanisms: below $5 \cdot 10^8$ cycles (end of the plateau on the S-N curve), and above.

In the first domain, a minority of crack initiations associated with extrusions was observed, especially in the largest grains (Fig. 14a and b). More frequently, cracks initiated from broken intermetallic particles (Fig. 14c and d), not always normal to the tensile axis, as might be expected, but most often along a direction inclined by $50 - 60^\circ$. In the LCF regime, micro-cracks often exhibited multiple branches, maybe along grain boundaries (Fig. 14d). Two micro-cracks paths are superimposed on EBSD maps in Fig. 15. It appears that the cracks grew straight across relatively large grains, but exhibited a zigzag path in areas of finer grains. A closer look suggests an alternation of transgranular growth, across large grains, and intergranular growth, in fine grain areas. A post-treatment of these EBSD data to get the local grain size distribution, and a comparison with that of the undeformed UFG

material did not reveal any local grain growth.

Fig. 16 shows a fracture surface typical of the LCF regime (45,000 cycles to fracture). Several semi-circular micro-cracks (no less than 6 in this case), like the one shown in Fig. 16a initiated from the surface, and the fracture surface looked relatively smooth, with radial markings, until these cracks reached approximately $150 \mu\text{m}$ in depth (which for the stress level of 200 MPa corresponds to ΔK_I close to $3 \text{ MPa}\sqrt{\text{m}}$). Then striations appeared (Fig. 16b) as if a transition from stage I to stage II occurred. However, contrary to what usually happens in CG materials during such a transition, the crack roughness increased substantially. In the final slanted area, heavy friction marks and spalling due to the repeated contact between the crack lips were observed (Fig. 16c).

Fig. 17a and b compare the distributions of secondary cracks lengths on the outer surface of CG and UFG samples submitted to the same plastic amplitude: $\epsilon_p = \pm 2.10^{-3}$. In CG material, the steady-state stress amplitude was 315 MPa and the fatigue life 2876 cycles, while in UFG material, the steady-state stress amplitude was 402 MPa and the fatigue life 1259 cycles. In spite of this smaller number of cycles, the density of micro-cracks was much higher (82 per mm^2) in the latter than in the former (8.8 per mm^2). For this plastic strain range, crack initiation was thus easier and faster in the UFG material.

Fig. 17c shows the distributions of secondary cracks lengths on the outer surface of a UFG sample submitted nearly to the same stress amplitude ($\pm 319 \text{ MPa}$) as the sample analyzed in Fig. 17b. In the UFG sample, the mean cracks length was only $57.3 \mu\text{m}$, compared to $112 \mu\text{m}$ in the CG sample, in spite of a much larger number of cycles (8482 cycles, as compared to 2876). This indicates that for this high stress amplitude, micro-cracks growth was slower in the UFG material.

By contrast, at a lower stress amplitude ($\pm 200 \text{ MPa}$, Fig. 17d-e), the density of micro-cracks in the UFG alloy (0.97 per mm^2) became lower than in the CG alloy (1.22 per mm^2), and the mean crack length was 40% larger ($38.8 \mu\text{m}$ instead of $26.8 \mu\text{m}$), even though the number of cycles was only 11% larger. This suggests a faster growth in the UFG alloy, at this stress amplitude.

The mean crack nucleation rates (final crack density divided by the number of cycles to failure) in nine CG and UFG samples are plotted as a function of the strain amplitude in Fig. 18. It is much higher in the UFG alloy at high strain range, but the difference with the CG alloy decreases as the strain rate decreases, and a crossing of the curves might exist. More tests would be necessary to check that point. While the angular distribution of the micro-cracks on the outer surface was relatively wide for the CG material, it was quite narrow and asymmetrical in the UFG material, with a preferential inclination around 60 degrees.

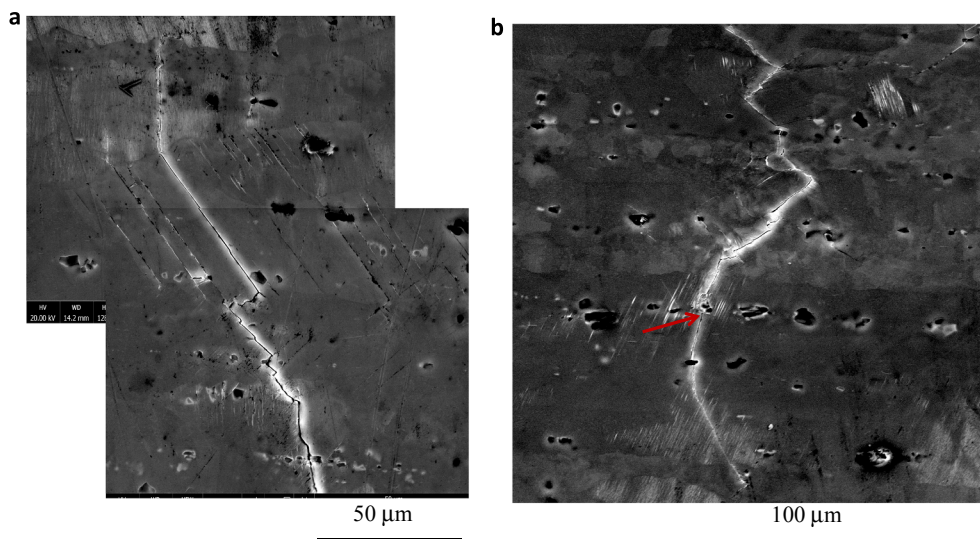


Fig. 13. Damage mechanisms in the CG material. $\epsilon_p = \pm 2.10^{-3}$, $N_f = 2784$ cycles. (a) Crack initiation from localized slip bands, and (b) crack initiation from broken intermetallic particles. The tensile axis is horizontal.

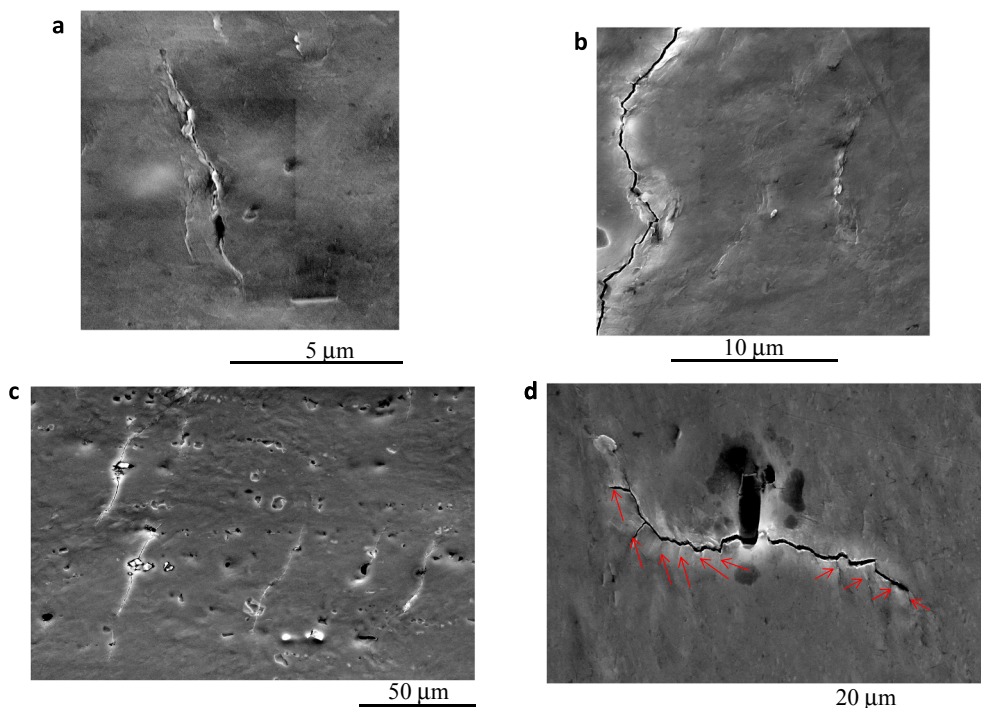


Fig. 14. Damage mechanisms in UFG material. $\epsilon_p = \pm 4.10^{-3}$, $N_f = 359$ cycles. (a–b) Crack initiation from localized slip bands, and (c–d) Crack initiation from broken intermetallic particles. The red arrows point to branches. The tensile axis is horizontal. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

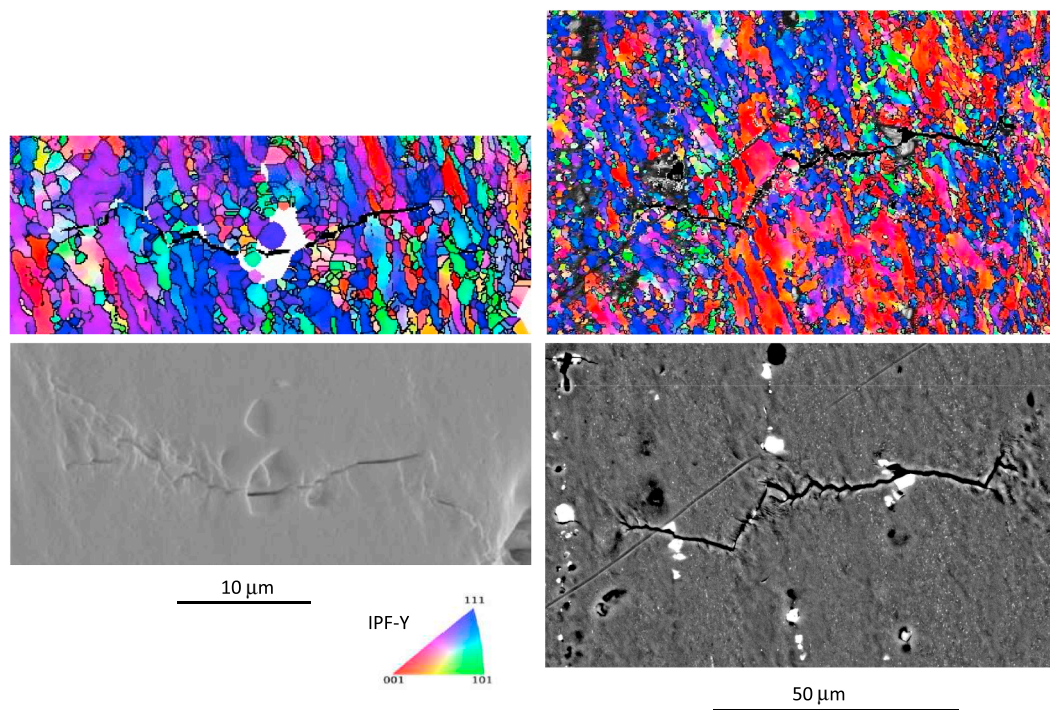


Fig. 15. EBSD analysis of two micro-cracks paths relative to the microstructure of a UFG sample $\epsilon_p = \pm 4.10^{-3}$. The tensile axis is vertical.

Above 5.10^8 cycles, a transition towards internal crack initiation with the so-called “fish-eye patterns” was observed (Fig. 19). In seven cases out of eight, the “defect” at the origin of fracture looked like a cluster of intermetallic particles (Fig. 19b), while for the sample corresponding to the longest life of $5.5 \cdot 10^9$ cycles, no such particles were visible on the fracture surface, which seemed covered with roof tiles-like features all along the same direction (Fig. 19d). No striations were observed for any of these internal cracks, contrary to the cracks grown in air.

To get more information about internal crack initiation

mechanisms, radial cross sections from the center of such “fish-eye patterns” were made, after platinum deposition, using FIB. Fig. 20 shows SEM images of two such sections, for the same UFG samples as those shown in Fig. 19. Fig. 20b confirms the presence of a relatively large broken intermetallic particle along the crack path, near the initiation site for the sample failed after $9.44 \cdot 10^8$ cycles, while Fig. 20c reveals the presence of several more or less aligned, 90–280 nm large cavities below the probable crack initiation site.

In both cases, the crack path was initially quite rough, with 5–15 μm high “cliffs” and became smoother and more normal to the tensile axis

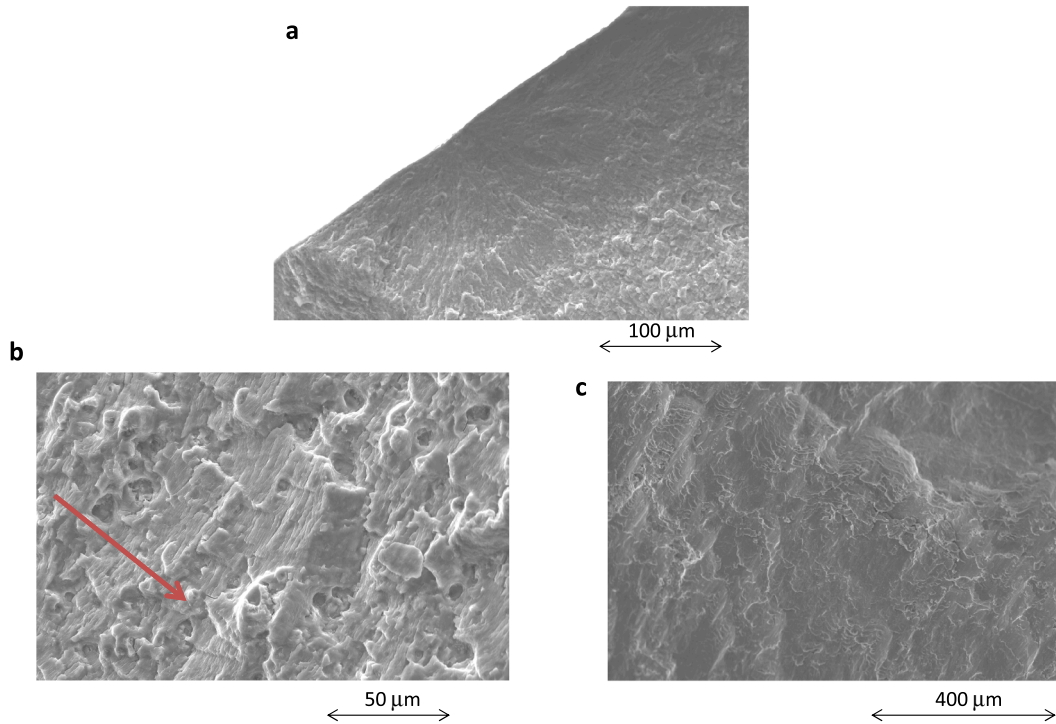


Fig. 16. Fracture surface of a UFG sample submitted to a stress-controlled test at ± 200 MPa ($N_f = 45,438$ cycles). (a) One of the cracks initiated from the surface, (b) striations (the arrow indicates the crack growth direction) and (c) heavily mated slanted zone.

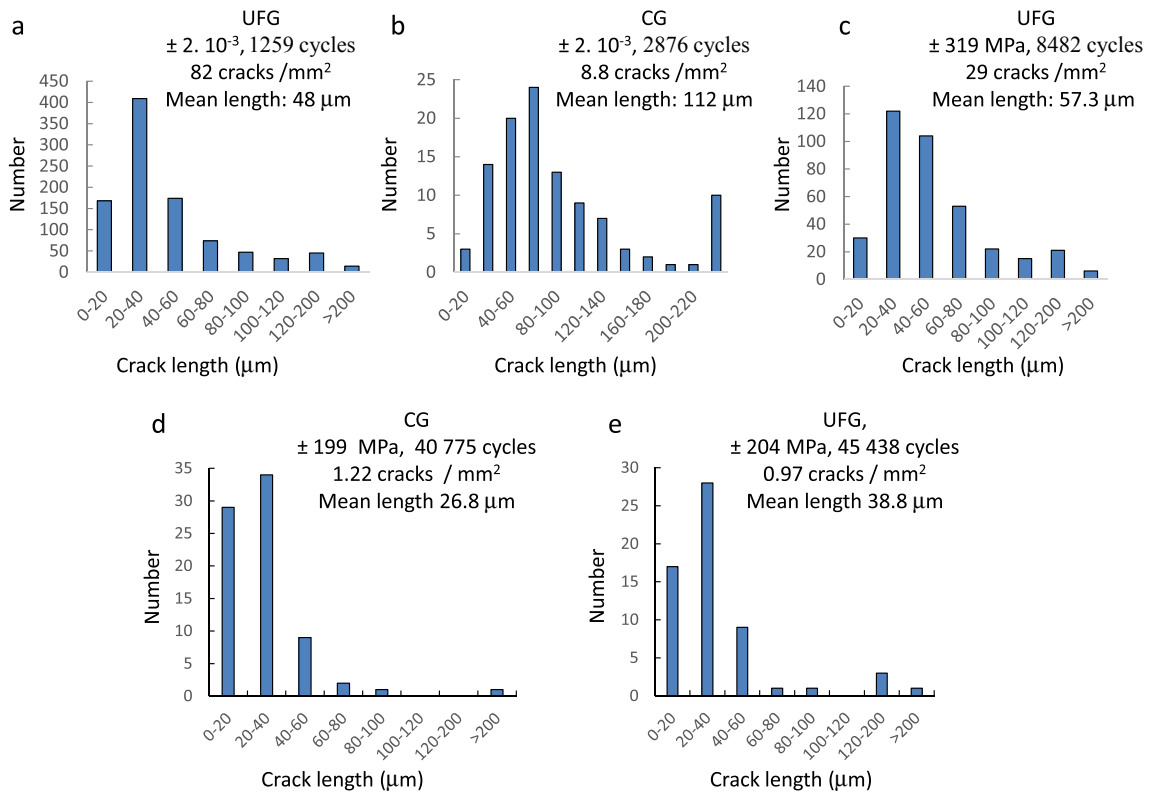


Fig. 17. Distributions of secondary cracks lengths.

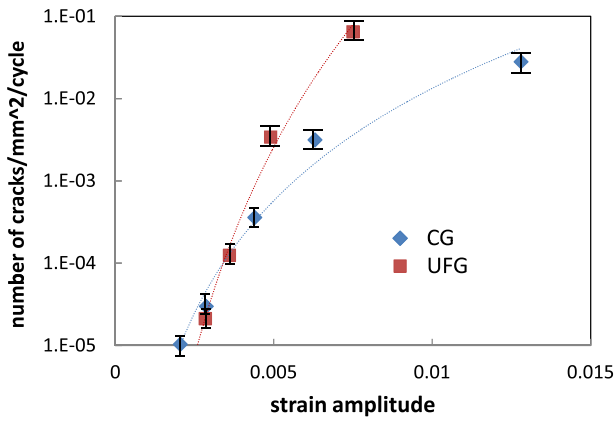


Fig. 18. Crack nucleation rate in CG and UFG alloys.

as the crack grew. No sign of local grain growth was found along this path. In a few places, areas of very fine grains (120–150 nm large) were observed along the crack path. However, it cannot be concluded that a nano-crystalline layer was formed, as it is often the case for “fish-eye patterns” in coarse grained materials in VHCF, because (1) such small grains are only present over limited portions of the crack path and (2) such a grain size is actually present (although not so frequent) in the wide grain size distribution of the UFG material (see Fig. 2e).

4. Discussion

The large isotropic hardening highlighted in CG material is consistent with the large number of dislocation loops and jogged

dislocations revealed by TEM after plastic-strain controlled tests. Loops and jogs constitute strong obstacles on gliding dislocations [28]. The non negligible kinematic hardening can be related to the interaction of dislocations with incoherent intermetallic particles. The dislocation loops left around the particles after Orowan's bypassing process is known to induce a back stress on gliding dislocations, that assists their backward glide upon load reversal and thus a Bauschinger effect.

The absence of cyclic softening of the UFG material is consistent with the results from Canadinc et al. [14] about the stabilizing effect of solute Mg, which restricts dislocations mobility and thus hinders recovery and grain growth in Mg rich Al-Mg alloys. The high fraction of HAGBs in the material (more than 80%) probably contributes to its stability as well. The dislocation density is already very high after ECAP and the capacity for a further increase is limited, which explains the more modest isotropic hardening compared to the CG material.

The heterogeneity in deformation from one grain to the other, especially between the “large” and ultrafine grains in the UFG material contributes to its high kinematic hardening. A higher Bauschinger effect in the UFG microstructure was also reported (based on the pointer shape of the stress-strain loops) for ECAPed copper by Vinogradov et al. [20].

In LCF, the reduction in life of the UFG material compared to its CG counterpart decreases as the plastic strain amplitude increases, up to the point that the two curves seem to cross at the highest amplitude -which should not be considered as a definitive result, owing to the limited number of data-points and the scatter often found, even in this regime [29]. This result is opposite to the trend reported in several papers (for example [4]). However, these papers mostly concern microstructurally unstable, cyclically softening UFG materials in which softening and grain coarsening, associated with strain localization tend to increase with the strain amplitude, leading to a more pronounced

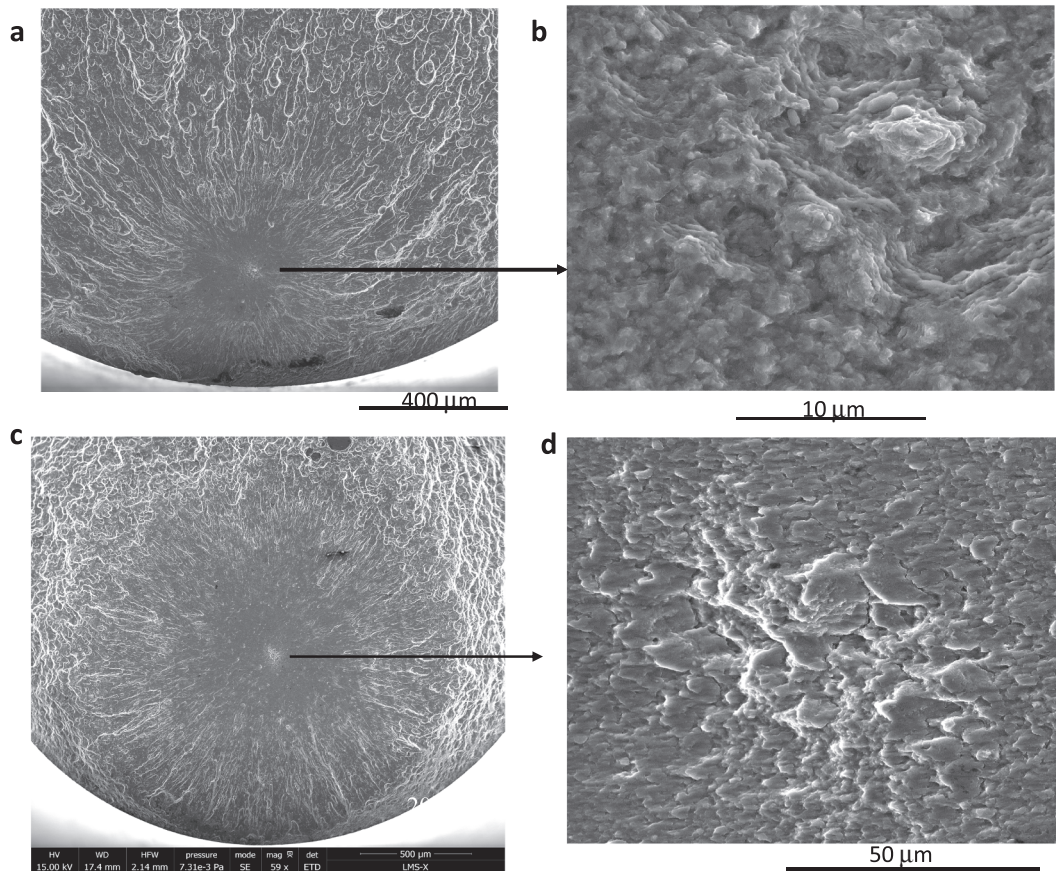


Fig. 19. Internal crack initiation with “fish-eye” patterns in the UFG material (a–b) $\Delta\sigma/2 = 186$ MPa, $9.44 \cdot 10^8$ cycles, and (c–d) $\Delta\sigma/2 = 149$ MPa, $5.5 \cdot 10^9$ cycles.

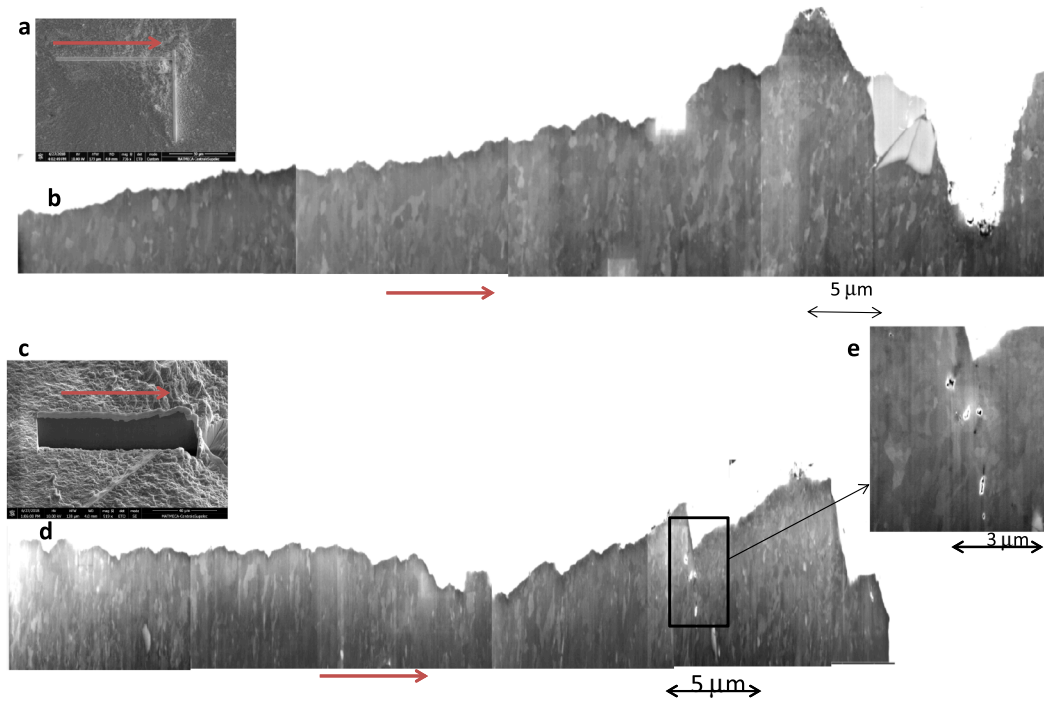


Fig. 20. Radial cross sections of “fish-eye” patterns in the same UFG samples as those shown in Fig. 19. (a–b) $\Delta\sigma/2 = 186$ MPa, $9.44 \cdot 10^8$ cycles, and (c–e) $\Delta\sigma/2 = 149$ MPa, $5.5 \cdot 10^9$ cycles. The arrows point towards the center of the fish eyes.

reduction in life than at lower amplitudes. In the present study, no such cyclic softening is observed, but at the contrary, a significant hardening. Walley et al. [19] who performed plastic-strain controlled LCF tests on cryo-milled 5083 Al alloy (that exhibited cyclic hardening as well, after a slight transient softening attributed to the relaxation of residual stresses) also reported very little difference in life with the CG material at high plastic strain amplitude, or even slightly better life for the UFG alloy, as in the present case.

The easier crack nucleation and the slower growth of micro-cracks observed here in the UFG alloy at high plastic strain amplitude are also in contradiction with what is usually reported, but these two results are consistent with one another and, paradoxically, with the divergence of the Manson-Coffin curves when the plastic strain amplitude decreases. A large micro-cracks density might produce a shielding effect that would slow down micro-cracks growth. Diffuse energy dissipation by (slow) growth of many cracks would occur, instead of a more localized dissipation by (fast) growth of a smaller number of cracks. The presence of many branches along the micro-cracks in LCF might also reduce their growth rate. When the plastic strain amplitude decreases, so does the micro-cracks density, and without a shielding effect, the usual tendency for faster crack growth in UFG materials [30] reappears.

On the other hand, the large density of micro-cracks that form in the UFG alloy in LCF also promotes the coalescence of those initiated in the same cross section, and indeed, up to six different crack initiation sites were sometimes observed on a given fracture surfaces, in this regime. Such a crack coalescence phenomenon might be the main cause for its earlier fracture (with a minor contribution of the reduced crack initiation stage, which does not constitute a large part of life in LCF).

While the micro-cracks exhibit a wide variety in their orientations relative to the tensile axis in the CG material, a preferential orientation around 60° was found in the UFG material. This direction corresponds more or less to the shear-induced elongation direction of the grains during ECAP, and it was shown by Niendorf et al. [31] or Arzaghi et al. [32] that ECAP-processed UFG materials have a preference for fatigue crack growth along the grain elongation direction. In addition, the grains with a high SF in the UFG material were found to have a (001) direction nearly parallel to the tensile axis, so that the {111} plane

with the highest SF on one of its slip systems would have a trace on the surface inclined by $50\text{--}60^\circ$, which corresponds to the preferential micro-cracking direction.

For the smooth cylindrical specimens used in conventional fatigue tests, the uniformly stressed volume and external surface were 804 mm^3 and 402 mm^2 , respectively, while for the waisted specimens used in ultrasonic fatigue tests, due to the non uniform stress profile along the gage length, the volume and external surface submitted to more than 90% of the maximum stress were only 194 mm^3 and 127 mm^2 , respectively. The two types of specimens thus differed nearly by a factor of four for both parameters. This size effect might explain the slight apparent upward shift of the data points from ultrasonic fatigue tests relative to those from conventional tests, although it might as well be due to the scatter of fatigue lives inherent to HCF.

The results of the VHCF tests suggest an endurance limit around 140 MPa for the CG material. This value –which might be somewhat lower in larger specimens– is 1.09 times its yield stress and 0.5 times its UTS. The latter is close to the ratio of 0.4–0.5 reported by Estrin and Vinogradov for slightly strain hardened CG Al-Mg alloys [2]. In this material, no transition towards internal crack initiation was observed when the stress range was further reduced.

The plateau at 200 MPa on the S-N curve of the UFG material corresponds to a limit for surface-initiated fatigue fracture. This stress level – which might be somewhat lower in larger specimens – is 0.64 times

Table 4
Computation of ΔK_I for incipient internal penny-shape crack growth.

Defect radius (μm)	Peak stress (MPa)	ΔK_I (MPa $\sqrt{\text{m}}$)
21	186	0.95
30	186	1.15
32	181	1.15
30	177	1.10
29	169	1.08
30	163	1.01
31	158	1.00
46	149	1.14

the 0.2% yield stress, as compared to a ratio of 1.09 in the CG material. While the yield stress reflects the average behavior of a material, the fatigue resistance reflects the “weakest link” in the microstructure. Since the heterogeneity of the ECAPed material –which contains both UFG and micron-sized grains– is more pronounced than that of its CG counterpart, it seems logical that its fatigue resistance represents a lower fraction of its yield stress.

The value of 200 MPa also corresponds to 0.51 times the UTS, which is substantially higher than the ratio (0.34) reported by Patlan and Vinogradov [11] for UFG 5056 Al-Mg alloy obtained by 4 ECAP passes following route Bc at 110 °C. Although this material was comparable in terms of tensile properties, it was prone to cyclic softening, contrary to the present one, which might explain the difference

Linear Elastic Fracture Mechanics was well suited to explain the subsequent decrease in resistance to fatigue above 5.10^8 cycles, because (1) the peak stress was less than 0.64 the 0.2% yield stress and (2) the internal cracks already constituted “microstructurally long cracks” when their diameter was above 10–15 μm . For a penny-shape crack of radius a , the amplitude of the stress intensity factor, ΔK_I can be computed, taking only the tensile part of the cycle into account as:

$$\Delta K_I = 2\sigma_{max} \sqrt{\frac{a}{\pi}} \quad (4)$$

The radius of the cluster of defects at the center of the “fish-eye patterns”, as well as the peak stress of each test, and the computed ΔK_I for incipient internal crack growth are gathered in Table 4. ΔK_I appears to be nearly the same for all tests, and close to 1 $\text{MPa}\sqrt{\text{m}}$, which corresponds to the threshold ΔK_I for short fatigue cracks growth at $R = -1$ in Al 5083 alloy, according to Costa et al. [33] and is also consistent with the threshold measured on UFG Al-7.5 Mg by Pao et al. [34]. The fatigue resistance of the UFG alloy above 5.10^8 cycles seems thus controlled by the capacity of internally-initiated cracks to propagate. The lower the stress amplitude, the larger the cluster of defect needed to allow crack growth.

In the CG material, in which cracks initiated mostly from slip bands in suitably oriented grains, an external surface of 127 mm^2 was still sufficient at 140 MPa to ensure the presence of at least one such grain with a relatively large size, and neighbors that do not exhibit too much misorientation, so that the micro-crack can cross the first grain boundaries, reach the threshold ΔK_I and grow until failure.

In the UFG material where the grains and most intermetallic particles were smaller, and where the probability for a grain to be surrounded by grains suitably oriented for plasticity was lower (see Fig. 3), an external surface of 127 mm^2 might not be sufficient below 200 MPa to ensure the presence of at least one “defect” large enough for the crack to reach the threshold ΔK_I . The probability to have such a defect in the highly stressed volume of 194 mm^3 was higher, and this might explain the transition towards internal crack initiation.

Fig. 20 a and b suggest that two different mechanisms for internal crack initiation in the UFG material might actually exist: one triggered by the fracture of a few microns-wide intermetallic particles or clusters of particles, and the other, observed only at very long lives ($5.5 \cdot 10^9$ cycles) triggered by the coalescence of one to two hundred nanometer wide cavities. Such cavities might result from the ECAP process, as suggested by the Small angle X-ray scattering measurements of Lapovok et al. [35] who reported the presence of 5–100 nm wide cavities in UFG titanium or by those of Betekhtin et al. [36] in an Al-Mg-Li alloy.

To the author’s best knowledge, the only other report of internal crack initiation in a UFG alloy was made recently by Esmaeili et al. [5], for a 7075 Al UFG alloy obtained by 4 ECAP passes, after several million rotating bending cycles, but no “fish-eye” pattern was mentioned, nor a possible cause for this internal initiation, and it was not clear whether this occurred once, or repeatedly.

5. Conclusions

The UFG Al 5083 produced by 6 passes of ECAP at 150 °C investigated here exhibits a stable microstructure, and cyclic hardening when submitted to plastic-strain-controlled push-pull tests. This hardening is however less pronounced than for its CG counterpart, because its initial dislocation density after ECAP is high, and its capacity to store more dislocations is limited. In the ECAPed alloy, a strong kinematic hardening is observed, which is attributed mainly to a high heterogeneity in plastic deformation from grain-to-grain, especially between “large” and small grains.

A statistical analysis of secondary micro-cracks shows that at high plastic strain amplitude, the crack nucleation rate (mostly from intermetallic particles) is much higher in the UFG alloy, so that crack coalescence phenomena might be responsible for its reduced fatigue life, in spite of a lower crack growth rate attributed to shielding effects, as well as to the presence of many branches. The micro-cracks exhibit transgranular growth across the largest grains, but intergranular growth in the small grained areas.

As the loading range decreases, the difference in crack nucleation rate between CG and UFG alloys however decreases, and at the lowest amplitude for which the statistical analysis of damage is meaningful, this rate becomes lower in the latter. On the other hand, the micro-crack growth rate in the UFG alloy becomes higher than in the CG alloy in the HCF regime, which might explain why between 10^4 and 2.10^6 cycles, its fatigue performance is just slightly better.

The S-N curve of the CG material exhibits a horizontal asymptote around 140 MPa which corresponds to 1.09 times its yield stress or 0.5 times its UTSs.

The S-N curve of the UFG material also exhibits a plateau at 200 MPa between 2.10^6 and 5.10^8 cycles. This stress level, which is 0.64 times its 0.2% yield stress or 0.51 times its UTS corresponds to the endurance limit for surface crack initiation.

However, above 5.10^8 cycles, a transition towards internal crack initiation from intermetallic particles or from cavities clusters occurs, with a very rough initial crack path. The fatigue resistance of the UFG material slowly decreases until at 5.10^9 cycles, it has the same level as for the CG material. This decrease can be explained considering the threshold ΔK_I for the growth of a penny shape crack.

For engineering applications, the UFG alloy only exhibits a clear superiority over its CG counterpart between 2.10^6 and 5.10^8 cycles, where its resistances is 43% higher.

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