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Limin Huang, Gérard Meunier, Olivier Chadebec, Jean-Michel Guichon, Nicolas Galopin, et al.. A Highly Efficient Post-Processing Method for Computing Magnetic Flux in Coils Considering Magnetic and Conductive Regions. IEEE Transactions on Magnetics, 2018, 58 (3), 10.1109/TMAG.2017.2759255. hal-02063223

HAL Id: hal-02063223 https://hal.science/hal-02063223v1

Submitted on 11 Mar 2019

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A High Efficient Post-Processing Method for Computing Magnetic Flux in Coils Considering Magnetic and Conductive Regions

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A high-efficiency post-processing method for computing the magnetic flux in coils is discussed and applied to magnetodynamic problem analysis. The method separates the contribution of magnetic flux in a coil into three parts, respectively generated by source coils, the magnetization of magnetic region and eddy currents in conductive region. The computation of the three components of magnetic flux in coil can be transformed to coil-region-independent integrals, which can help to reduce the mesh size used around the coil, thus increasing the computational efficiency. The method is well adapted to any numerical techniques, such as the finite element and volume integral methods. A typical electromagnetic shielding problem is used to validate the performance of the post-processing magnetic flux computational method at low frequency application.

Index Terms—Coil, electromagnetic shielding, magnetic flux, magnetodynamic, volume integral method (VIM).

I. INTRODUCTION

MAGNETIC flux in coils is an important quantity in the analysis, design and optimization of electromagnetic devices. The magnetic flux in a coil is generally calculated in a post-processing step of a computational electromagnetic problem, where the field distribution is firstly obtained by a given numerical method, such as the finite element method (FEM) or the volume integral method (VIM).

With integral formulation method, it is unnecessary to discretize the inactive region. This approach is therefore more suitable for the study of electromagnetic devices with a predominant air region. Thanks to the matrix compression algorithm development, solving electromagnetic problems by integral equations is becoming more and more efficient, from magnetostatic applications [1], [2] to magnetodynamic applications [3], [4] with both magnetic and conductive volume regions, and also a coupling with external circuits.

After solving the problem and getting all the field quantities on the mesh, it is necessary to put forward a high efficient computational method for evaluating magnetic flux in coils in the analysis of electromagnetic devices. In an electromagnetic problem, as illustrated in Fig. 1, the magnetic flux flowing in a coil can be divided into a summation of three terms: 1) one is generated by the magnetic field of source coils; 2) one by the magnetization field of magnetic region and 3) one by the eddy current field of conductive region.

Based on the physical signification of the magnetic flux in coils, these three terms are traditionally calculated by integrating respectively the field quantities on the considered coil region. However, due to the irregular distribution of the fields around the considered coil, the coil mesh should be very fine discretized to have a precise result of the flux



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Fig. 1. Illustration of a magnetodynamic problem regions.

computation. The increased element number will also increase the computational complexity of the problem.

To avoid using too complex coil mesh, a coil-regionindependent method has been presented in [5]. This computational method allows obtaining the flux component through a coil by integrating directly on the magnetic region rather than the coil region. It has shown a good efficiency in the study of inductive power transmission system for the mutualinductance calculation. However, this method can only deal with the magnetostatic problems and has not been extended yet to conductive region in magnetodynamic context.

Following the previous research, in this paper we propose a new general approach to compute the magnetic flux in coils under magnetodynamic context. The approach begins by solving a magnetodynamic problem by an integral formulation, then dividing the magnetic flux flowing in a coil into the summation of three flux components, which can be calculated by simplified integrals. Finally, the proposed coil-regionindependent computational method is applied and verified in an electromagnetic shielding application example.

II. INTEGRAL FORMULATION METHOD

A magnetodynamic problem can be described as a problem with three typical regions: 1) the source coil region (noted by Ω_0), 2) the magnetic region (noted by Ω_m) and 3) the conductive electrical region (noted by Ω_c). Starting from Maxwell equations, the electric field **E** and the magnetic field **H** can be expressed by the potential formulation, as

$$\begin{cases} \mathbf{E} = -\frac{\mathrm{d}\mathbf{A}}{\mathrm{d}t} - \mathrm{grad}V \\ \mathbf{H} = \mathbf{T} - \mathrm{grad}\phi \end{cases}$$
(1)

where \mathbf{T} and \mathbf{A} are the electric and magnetic vector potentials, V and ϕ are the electric and magnetic scalar potentials.

A. Magnetodynamic Integral Equation

Displacement currents can be neglected when considering the low frequency magnetodynamic problem and application. According to the adequate gauges, all the four potentials can be expressed from the integral formulation that are limited to the regions Ω_0 , Ω_m and Ω_c , as

$$\begin{cases} \mathbf{A}_{p} = \frac{\mu_{0}}{4\pi} \left(\int_{\Omega_{0}} \frac{\mathbf{J}_{0q}}{r} \mathrm{d}\Omega + \int_{\Omega_{m}} \frac{\mathbf{M}_{q} \times \mathbf{r}}{r^{3}} \mathrm{d}\Omega + \int_{\Omega_{c}} \frac{\mathbf{J}_{q}}{r} \mathrm{d}\Omega \right) \\ \frac{\mathrm{d}V_{p}}{\mathrm{d}t} = \frac{1}{4\pi\varepsilon_{0}} \int_{\Omega_{c}} \frac{\mathbf{J}_{q} \cdot \mathbf{r}}{r^{3}} \mathrm{d}\Omega \\ \mathbf{T}_{p} = \frac{1}{4\pi} \left(\int_{\Omega_{0}} \frac{\mathbf{J}_{0q} \times \mathbf{r}}{r^{3}} \mathrm{d}\Omega + \int_{\Omega_{c}} \frac{\mathbf{J}_{q} \times \mathbf{r}}{r^{3}} \mathrm{d}\Omega \right) \\ \Phi_{p} = \frac{1}{4\pi} \int_{\Omega_{m}} \frac{\mathbf{M}_{q} \cdot \mathbf{r}}{r^{3}} \mathrm{d}\Omega \end{cases}$$
(2)

The formulation allows computing exact solution of fields **E** and **H** at any point p from the knowledge of a point q (current densities \mathbf{J}_0 in the coil region, the magnetization field **M** in magnetic region and **J** in conductive region). Because **M** and **J** are also variables to be solved, constitutive laws of materials should be added to obtain a complete solution. In the magnetodynamic context, two constitutive laws which link, respectively, the current density **J** to the electric field **E** (in Ω_c) and the magnetization **M** to the magnetic field **H** (in Ω_m) should be essentially considered as

$$\begin{cases} \mathbf{J} = \sigma \mathbf{E} \\ \mathbf{M} = \chi \mathbf{H} = (v_0 - v) \mathbf{B} \end{cases}$$
(3)

B. Facet Interpolation

The magnetic region and the conductive region can be discretized with Whitney first-order facet finite element functions. In this case, the interpolation of current and flux density are

$$\begin{cases} \mathbf{J} = \sum_{j} \mathbf{w}_{j} I_{j} \\ \mathbf{B} = \sum_{g} \mathbf{w}_{g} \psi_{g} \end{cases}$$
(4)

where \mathbf{w}_j and \mathbf{w}_g are facet shape functions; I_j and ψ_g are the current or flux across the facets. Facet interpolation is well adapted to unknowns **J** and **B** since it imposes the continuity of the flux into the finite element mesh [4].

Then, two Galerkin procedures can be then associated respectively in the magnetic region Ω_m and the conductive region Ω_c :

$$\begin{cases} \int_{\Omega_c} \mathbf{w}_i \left(\frac{\mathbf{J}}{\sigma} - \mathbf{E} \right) d\Omega = 0 \\ \int_{\Omega_m} \mathbf{w}_f \left(\frac{\mathbf{M}}{\chi} - \mathbf{H} \right) d\Omega = 0 \end{cases}$$
(5)

where the field distribution E and H are obtained thanks to (1) and (2). By using facet interpolations, facet shape functions are chosen for the Galerkin projection of J and B. Furthermore, such a method can also lead to an equivalent circuit representation which avoids the convexity problem and strongly imposes the solenoidality of J and B [3].

C. Matrix System Computation

From relations (2) and the constitutive laws, the relation between **J**, **A**, **B** and **T** can be expressed in terms of currents I_j through the facets of the conductive region and magnetic flux Ψ_j across the facets of magnetic region. After the Galerkin procedures in the magnetic region Ω_m and the conductive region Ω_c , a matrix system of equations, which links the difference of averaged potentials between two adjacent elements (V and Φ) with the flux through facets (I_j and Ψ_j) is obtained as

$$\begin{bmatrix} [\mathbf{R}] + \frac{\mathrm{d}}{\mathrm{d}t} [\mathbf{L}] & \frac{\mathrm{d}}{\mathrm{d}t} [\mathbf{C}] \\ [\mathbf{D}] & [\mathbf{E}] \end{bmatrix} \left\{ \begin{array}{c} I \\ \Psi \end{array} \right\} = \left\{ \begin{array}{c} \Delta V \\ \Delta \Phi \end{array} \right\} + \left\{ \begin{array}{c} U \\ Q \end{array} \right\}$$
(6)

where the coefficients of the matrix is defined as

$$\begin{aligned} \mathbf{R}_{ij} &= \int_{\Omega_c} \mathbf{w}_i \cdot \frac{\mathbf{w}_j}{\sigma} \mathrm{d}\Omega \quad \mathbf{L}_{ij} = \frac{\mu_0}{4\pi} \int_{\Omega_c} \mathbf{w}_i \cdot \int_{\Omega_c} \frac{\mathbf{w}_j}{r} \mathrm{d}\Omega \mathrm{d}\Omega \\ \mathbf{C}_{ig} &= \frac{\mu_0}{4\pi} \int_{\Omega_c} \mathbf{w}_i \cdot \int_{\Omega_m} (\nu_0 - \nu) \frac{\mathbf{w}_g \times \mathbf{r}}{r^3} \mathrm{d}\Omega \mathrm{d}\Omega \\ \mathbf{D}_{fi} &= -\frac{1}{4\pi} \int_{\Omega_c} \mathbf{w}_f \cdot \int_{\Omega_m} \frac{\mathbf{w}_j \times \mathbf{r}}{r^3} \mathrm{d}\Omega \mathrm{d}\Omega \\ \mathbf{E}_{fg} &= \int_{\Omega_m} \nu \mathbf{w}_f \cdot \mathbf{w}_g \, \mathrm{d}\Omega \\ \mathbf{F}_{fg} &= \frac{1}{4\pi} \int_{\Gamma_f} \frac{1}{S_f} \cdot \int_{\Omega_m} (\nu - \nu_0) \frac{\mathbf{w}_g \cdot \mathbf{r}}{r^3} \mathrm{d}\Omega \mathrm{d}\Omega \end{aligned}$$
(7)

and the terms U and Q in the second hand are the source terms produced by all the active coils in the problem. Such a matrix system can be easily calculated by magnetic vector potential formulation that combines equivalent network based on Whitney facet interpolation and Green's function volume integral method proposed in [4].

III. MAGNETIC FLUX COMPUTATION

Formulated by the magnetic vector potential **A**, the magnetic flux Φ through a considered coil k, with a region denoted by Ω_{0_k} , can be expressed by an integral on the coil region:

$$\Phi_k = \int_{\Omega_{0_k}} \mathbf{j}_{0_k} \cdot \mathbf{A} \,\mathrm{d}\Omega \tag{8}$$

where \mathbf{j}_{0_k} is a vector function describing the normalized current density of the considered coil region Ω_{0_k} . For a magnetodynamic problem containing three typical domains: 1) source coil region Ω_{0_k} ; 2) non-conducting magnetic region Ω_m and 3) electrical conductive regions Ω_c , as illustrated in Fig. 1, the magnetic vector potential \mathbf{A} can be separated in three components, i.e. $\mathbf{A} = \mathbf{A}_0 + \mathbf{A}_m + \mathbf{A}_c$, where \mathbf{A}_0 , \mathbf{A}_m and \mathbf{A}_c are generated respectively by the three aforementioned regions. Therefore, the contribution of total magnetic flux Φ_k through a coil k can be expressed by

$$\Phi_k = \Phi_{0_k} + \Phi_{\mathbf{m}_k} + \Phi_{\mathbf{c}_k} \tag{9}$$

where Φ_{0_k} is the contribution of all source coils in vacuum, Φ_{m_k} is the contribution of the magnetization of magnetic region and Φ_{c_k} is the contribution of eddy currents in conductive region.

A. Φ_{0_k} Computation

In a magnetodynamic problem with multiple coils, the magnetic vector potential \mathbf{A}_{0_k} through the coil k can be computed by considering all the coils in vacuum, as

$$\mathbf{A}_{0_k} = \frac{\mu_0}{4\pi} \sum_l \left(\int_{\Omega_{0_l}} \frac{\mathbf{j}_{0_l}}{r} \,\mathrm{d}\Omega \right) I_l \tag{10}$$

where each coil l is defined with a region Ω_{0_l} and carrying a current I_l . Thus, the first part of flux Φ_{0_k} , generated by all coils is the problem, can be calculated by a double integral:

$$\Phi_{0_k} = \frac{\mu_0}{4\pi} \int_{\Omega_{0_k}} \mathbf{j}_{0_k} \cdot \left(\sum_l I_l \int_{\Omega_{0_l}} \frac{\mathbf{j}_{0_l}}{r} \,\mathrm{d}\Omega \right) \mathrm{d}\Omega \tag{11}$$

The double integration (11) can be computed by a semianalytical integration method. An analytical expression proposed in [6] can be used to evaluate the first integral on the source coil region Ω_{0_l} , and the quadratic Gauss points integration can be used to compute the first integral on the objective coil region Ω_{0_k} .

B. Φ_{m_k} Computation

Considering the magnetization effect in the magnetic region $\Omega_{\rm m}$, the magnetic vector potential $\mathbf{A}_{\rm m}$ can be computed as an integral on $\Omega_{\rm m}$. Similarly, the flux component $\Phi_{\rm m_k}$ through the coil k can be computed by a double integral:

$$\begin{cases} \mathbf{A}_{\mathrm{m}} = \frac{\mu_{0}}{4\pi} \int_{\Omega_{\mathrm{m}}} \mathbf{M} \times \nabla\left(\frac{1}{r}\right) \mathrm{d}\Omega_{\mathrm{m}} \\ \Phi_{\mathrm{m}_{k}} = \frac{\mu_{0}}{4\pi} \int_{\Omega_{0_{k}}} \mathbf{j}_{0_{k}} \left[\int_{\Omega_{\mathrm{m}}} \mathbf{M} \times \nabla\left(\frac{1}{r}\right) \mathrm{d}\Omega_{\mathrm{m}} \right] \mathrm{d}\Omega \end{cases}$$
(12)

Because the computation of the magnetic flux component Φ_{m_k} is related to the considered coil region Ω_{0_k} , it should thus be sufficiently meshed to have a precise result. A great number of elements will increase dramatically the computation time, it is relatively inefficient to solve directly the double integral, especially dealing with the complex geometries.

A method which allows to obtain Φ_{m_k} by integrating directly in the magnetic region Ω_m has been presented in [5]. This method begins with the usage of the partial integral theorem to the equation (8), as

$$\Phi_{\mathbf{m}_{k}} = \int_{\Omega_{0_{k}}} \mathbf{j}_{0_{k}} \cdot \mathbf{A}_{\mathbf{m}} \, \mathrm{d}\Omega = \int_{\Omega} \left(\nabla \times \mathbf{h}_{0_{k}} \right) \cdot \mathbf{A}_{\mathbf{m}} \, \mathrm{d}\Omega$$

$$= \int_{\Omega} \mathbf{h}_{0_{k}} \cdot \left(\nabla \times \mathbf{A}_{\mathbf{m}} \right) \mathrm{d}\Omega$$
(13)

where \mathbf{h}_{0_k} represents the normalized magnetic field generated by the coil k with 1 A. Considering the relation $\nabla \times \mathbf{A}_{m} = \mu_0 (-\nabla \varphi_r + \mathbf{M})$, the equation (13) becomes

$$\Phi_{\mathbf{m}_{k}} = \mu_{0} \int_{\Omega} \mathbf{h}_{0_{k}} \left(-\nabla \varphi_{\mathbf{r}} + \mathbf{M} \right) \mathrm{d}\Omega \tag{14}$$

where the integral $\int_{\Omega} \mathbf{h}_{0_k} (\nabla \varphi_r) d\Omega$ can be proved to be 0 by applying another time the partial integration theorem and considering the boundary condition of infinity. Finally, the magnetic flux component Φ_{m_k} generated by the magnetization effect can be computed as

$$\Phi_{\mathbf{m}_{k}} = \mu_{0} \int_{\Omega_{\mathbf{m}}} \mathbf{h}_{0_{k}} \cdot \mathbf{M} \,\mathrm{d}\Omega \tag{15}$$

C. Φ_{c_k} Computation

Similarly, by considering the eddy currents effect in the conductive region Ω_c , the magnetic vector potential \mathbf{A}_c can be computed as an integral on Ω_c and the flux component Φ_{ck} through the coil k can be computed as a double integral:

$$\begin{cases} \mathbf{A}_{c} = \frac{\mu_{0}}{4\pi} \int_{\Omega_{c}} \frac{\mathbf{J}}{r} d\Omega_{c} \\ \Phi_{c_{k}} = \frac{\mu_{0}}{4\pi} \int_{\Omega_{0_{k}}} \mathbf{j}_{0_{k}} \left[\int_{\Omega_{c}} \frac{\mathbf{J}}{r} d\Omega_{c} \right] d\Omega \end{cases}$$
(16)

In order to increase the computational efficiency by solving directly the double integral in (16) for the flux component Φ_{c_k} , here we propose a coil-region-independent method which allows to simplify the double integral to a single integration in the conductive region Ω_c . The method begins by applying the partial integral theorem:

$$\Phi_{\mathbf{c}_{k}} = \int_{\Omega_{0_{k}}} \mathbf{j}_{0_{k}} \cdot \mathbf{A}_{\mathbf{c}} \, \mathrm{d}\Omega = \int_{\Omega} \left(\nabla \times \mathbf{h}_{0_{k}} \right) \cdot \mathbf{A}_{\mathbf{c}} \, \mathrm{d}\Omega$$
$$= \int_{\Omega} \nabla \cdot \left(\mathbf{h}_{0_{k}} \times \mathbf{A}_{\mathbf{c}} \right) \mathrm{d}\Omega - \int_{\Omega} \mathbf{h}_{0_{k}} \cdot \left(\nabla \times \mathbf{A}_{\mathbf{c}} \right) \mathrm{d}\Omega$$
(17)

where the term $\nabla \cdot (\mathbf{h}_{0_k} \times \mathbf{A}_c) = 0$. The magnetic flux Φ_{c_k} generated by eddy currents can be then computed by

$$\Phi_{\mathbf{c}_{k}} = \int_{\Omega} \mathbf{h}_{0_{k}} \cdot (\nabla \times \mathbf{A}_{\mathbf{c}}) \,\mathrm{d}\Omega \tag{18}$$

In the integral (18), the terms \mathbf{h}_{0_k} and $\nabla \times \mathbf{A}_c$ can be substituted by:

$$\begin{cases} \mathbf{h}_{0_{k}} = \frac{1}{\mu_{0}} \left(\nabla \times \mathbf{a}_{0_{k}} \right) \\ \nabla \times \mathbf{A}_{c} = \mu_{0} \mathbf{H}_{c} \end{cases}$$
(19)

where \mathbf{H}_{c} is the field produce by the eddy current. Then (18) becomes

$$\Phi_{\mathbf{c}_{k}} = \int_{\Omega} \frac{1}{\mu_{0}} \left(\nabla \times \mathbf{a}_{0_{k}} \right) \cdot \left(\mu_{0} \mathbf{H}_{\mathbf{c}} \right) \mathrm{d}\Omega$$
(20)

By applying another time the partial integration theorem, the equation (20) becomes

$$\Phi_{c_k} = \int_{\Omega} \mathbf{a}_{0_k} \cdot (\nabla \times \mathbf{H}_c) \, \mathrm{d}\Omega + \int_{\Omega} \nabla \cdot (\mathbf{a}_{0_k} \times \mathbf{H}_c) \, \mathrm{d}\Omega \quad (21)$$

According to the divergence theorem, the second term $\int_{\Omega} \nabla \cdot (\mathbf{a}_{0_k} \times \mathbf{H}_c) d\Omega$ becomes $\int_{\Gamma} \mathbf{a}_{0_k} \times \mathbf{H}_c d\Gamma$. Because of the continuity, this term can be expended to the infinity boundary Γ_{∞} , where the field is null, and so the integral $\int_{\Omega} \nabla \cdot (\mathbf{a}_{0_k} \times \mathbf{H}_c) d\Omega = 0$, thus

$$\Phi_{\mathbf{c}_{k}} = \int_{\Omega} \mathbf{a}_{0_{k}} \cdot (\nabla \times \mathbf{H}_{\mathbf{c}}) \,\mathrm{d}\Omega \tag{22}$$



Fig. 2. 3-D axisymmetric electromagnetic shielding application example. (a) Geometry and (b) eddy currents density on the conductive region.

In the conductive region Ω_c , the relation between \mathbf{H}_c and \mathbf{J}_c can be written as

$$\nabla \times \mathbf{H}_{c} = \mathbf{J}_{c} \tag{23}$$

By substituting the relation (23) into (22), the integral of computing the flux component Φ_{c_k} becomes finally an integral on the conductive region Ω_c :

$$\Phi_{\mathbf{c}_{k}} = \int_{\Omega} \mathbf{a}_{0_{k}} \cdot (\nabla \times \mathbf{H}_{\mathbf{c}}) \,\mathrm{d}\Omega = \int_{\Omega_{\mathbf{c}}} \mathbf{a}_{0_{k}} \cdot \mathbf{J}_{\mathbf{c}} \,\mathrm{d}\Omega \qquad (24)$$

where \mathbf{a}_{0_k} represents the normalized magnetic vector potential generated by the coil k with 1 A, and \mathbf{J}_c means the eddy current density. The computation of the magnetic flux Φ_{c_k} , which is generated by eddy current is finally changed into an integral which is related only to the domain of electrical conductive region Ω_c .

IV. APPLICATION EXAMPLE

The proposed coil-region-independent computational method for magnetic flux is tested by a strong magneticelectric coupling problem, as illustrated in Fig. 2. The test 3-D problem is composed of:

1) solenoid coil (radius 6 mm, thickness 0.1 mm, height 10 mm, effective value of current: 1 Ampere, number of turns: 100);

2) linear magnetic core (average radius 4 mm, thickness
 2 mm, height 10 mm, relative permeability 100);

3) thin surface copper layer (radius 5.5 mm, thickness 0.1 mm, height 10 mm, conductivity 55×10^6 S/m).

After modeling the probem in 3-D context, the problem is solved by the volume integral method (VIM) to obtain the fields distribution. The flux is computed by summing the three components at the post-processing step.

Thanks to the advantage of VIM and the proposed magnetic flux computation method, only the active regions (magnetic core structures and the surface copper layer) should be fine considered and discretized. Only one tenth of the element number in the active region can thus realize a precision of 0.5% in comparison with the FEM which should take account of the predominant air region and the traditional magnetic flux computational method where the coils should be fine meshed.

Figure 3 shows the variation of the flux in the coil versus the frequency, with an axisymmetric finite element analysis to the same problem in the software Flux as reference. The comparison to the results with a finite element method shows a difference less than 0.4% at any frequency.



Fig. 3. Comparison between the proposed post-processing method results and FEM simulation results of magnetic flux in the coil.

In this configuration, the thin surface copper layer is placed between the coil and the magnetic core, to realize an electromagnetic shield. The computational results of the flux in the coil versus the frequency shows that when the system operation frequency increases, the eddy currents on the thin surface copper begin to act as a shield and the magnetic flux in coil decreases.

V. CONCLUSION

A coil-region-independent post-processing computational method for the magnetic flux in coils under magnetodynamic context is presented and applied to solve electromagnetic shielding problem. The computational method begins by solving the magnetodynamic problem with integral formulation method, which is unnecessary to consider the massive inactive region and it can thus ignore the predominant air region. Then, a high efficient computational method for magnetic flux has been presented by using coil-region-independent integrals. The decomposition of the magnetic flux in coils considering both magnetic and conductive regions is well adapted to the magnetodynamic problem. The method to compute the magnetic flux in coil at post-processing step by three simple integrals is general and it can be applied to any numerical methods, such as FEM and VIM.

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