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Resonance fluorescence revival in a voltage-controlled semiconductor quantum dot

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We demonstrate systematic resonance fluorescence recovery with near-unity emission efficiency in single quantum dots embedded in a charge-tunable device in a wave-guiding geometry. The quantum dot charge state is controlled by a gate voltage, through carrier tunneling from a close-lying Fermi sea, stabilizing the resonantly photocreated electron-hole pair. The electric field cancels out the charging/discharging mechanisms from nearby traps toward the quantum dots, responsible for the usually observed inhibition of the resonant fluorescence. Fourier transform spectroscopy as a function of the applied voltage shows a strong increase of the coherence time though not reaching the radiative limit. These charge controlled quantum dots can act as quasi-perfect deterministic single-photon emitters, with one laser pulse converted into one emitted single photon.

Semiconductor quantum dots (QDs) are commonly considered as artificial atoms due to their discrete electronic structure and are very efficient sources of single and indistinguishable photons [1–3]. Their potential for applications is high as they can be easily integrated into nanophotonic devices [4, 5], defining building blocks for quantum information processing in the solid-state [6, 7]. During the past decade, a lot of effort has been devoted to minimize dephasing processes due to the coupling of QDs to their surrounding solid-state matrix. Indeed, coupling to phonons [8–10] as well as time jitter [11] reduces the degree of indistinguishability and charge or spin noise [12–14] lead to inhomogeneous broadening of the emission line. Therefore, strictly resonant excitation of the QD s-shell has appeared as an essential ingredient [15, 16] to preserve the coherence properties of the emitted photons.

Charge noise is detrimental as it strongly limits or even suppresses the QD resonance fluorescence (RF) [17–19]. The RF quench has been attributed to the structure residual doping and defects which create a fluctuating electrostatic environment. This can lead to a Coulomb blockade effect preventing the photocreation of an electron-hole pair in the QD [18, 20]. To circumvent this difficulty and recover the RF, an additional very low power non-resonant laser can be used. Although this technique has been successful [21–23], the exact physical process of this non-resonant pump has not been sufficiently addressed [23]. Moreover, the lack of control of this non-resonant pump prevents the realization of a fully on-demand single-photon source with a high degree of coherence for any probed QD.

Here, we show how a revival of the RF can be achieved by using a suitably designed voltage-controlled device that stabilizes the resonantly photocreated electron-hole pair in the dot. The resonant excitation is realized in an in-plane waveguide geometry [8], while the single photons are collected from the top. This geometry yields an almost complete suppression of the laser scattered light on the RF detection side. By controlling the QD

electric field environment by a gate voltage, the charging/discharging mechanisms from the nearby trap states to the QD are disabled. The resonantly photocreated electron-hole pairs give rise to a very intense RF line and an increase of the coherence time. However the radiative limit is not reached suggesting that charge and/or spin noise are still present in the structure leading to residual inhomogeneous broadening. Still, the gate control allows to convert one laser pulse into one emitted photon and optimization of the collection efficiency remains the last step to achieve for using such a device in quantum technologies applications.

A low density InAs/GaAs self-assembled QD layer, grown by molecular beam epitaxy, was embedded at the center of a *p-i-n* doped GaAs/AlAs microcavity on a n-doped GaAs (001) substrate. The Bragg mirrors consist, for the n-doped bottom side, of 24 pairs silicon-doped at 2.10^{18}cm^{-3} and 1.10^{18}cm^{-3} closer to the cavity, while the p-doped Bragg mirror was carbon-doped at 2.10^{18}cm^{-3} , except for the last two pairs at 2.10^{19}cm^{-3} to improve the contact ohmicity. The cavity and the $\lambda/4$ layers were designed to obtain a cavity mode centered at 920 nm. The quality factor is only a few hundreds and does not induce any significant Purcell effect. Deep (approximately $1.5\ \mu\text{m}$) ridges were etched by inductively coupled plasma etching realizing one-dimensional waveguides with 0.8 to $1.2\ \mu\text{m}$ width. Standard ohmic contacts were deposited and annealed on the back side. Top contacts were realized by resist planarization and deposition of Ti/Au stripes perpendicular to ridges. The resist was then etched away between the stripes. A schematic view of the experimental geometry, a characteristic I-V curve and the simplified band structure are depicted in Fig. 1 (a), (b) and (c) respectively. In the following, U will denote the external applied bias and V_{BI} the built-in voltage. Then, the QD potential is $(V_{\text{BI}} - U)$ for reverse bias.

To investigate the resonant and non-resonant fluorescence, the sample and the microscope objectives are mounted inside a He closed cycle temperature-variable

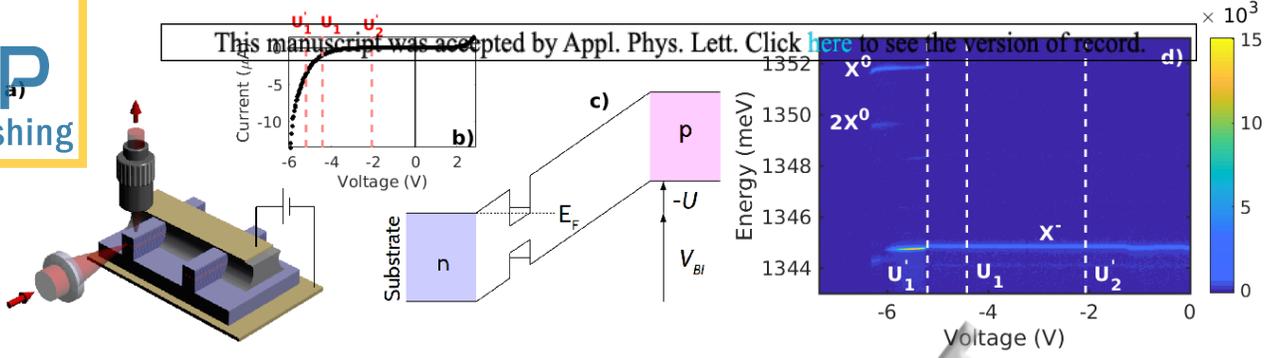


FIG. 1. (a) Schematic structure of the sample: etched ridges (in blue) containing the QDs and microscope objectives for excitation and detection. The electrical contacts are represented in yellow. (b) Typical I-V curve at 4 K indicating the different threshold voltages. (c) Band structure of the sample. The Bragg mirrors are not represented for simplicity. (d) Typical micro-photoluminescence map of a QD as a function of the applied gate voltage for non-resonant excitation. U_1' is the threshold for the emergence of the X^0 transition. U_1 and U_2' indicate the region where the X^- RF exists (see text). The color plot is in units of counts/sec.

cryostat. For the excitation, a tunable picosecond Ti-Sapphire laser beam is focused on a ridge cleaved edge. The 5 ps-wide pulses propagate along the one-dimensional waveguide and pump one or several QDs. The luminescence of a single of these dots is collected from the ridge top surface using confocal microscopy. The signal is coupled to a monomode optical fiber and sent to the detection setup composed by a spectrometer and a CCD camera with spectral resolution of $60 \mu\text{eV}$. It can also be sent either to a Michelson interferometer for Fourier transform spectroscopy, or to a photon correlation setup [8].

Ten different QDs were studied from different ridges and the same behavior was observed for all of them. In the following we show results obtained from the same QD. We present in Fig. 1(d) a typical micro-photoluminescence ($\mu\text{-PL}$) map under non-resonant excitation (at the wetting layer energy), as a function of the applied bias voltage. Polarization and power-dependent measurements have been performed to identify unambiguously the QD neutral electron-hole pair X^0 and charged X^- states as well as the double electron-hole pair state $2X^0$ (Fig. 1(d)). The X^0 emission threshold is around $U_1' = -5.2 \text{ V}$. From the energy positions of the X^0 and X^- lines in the μPL map, we find a binding energy for the X^- charged complex of about 7 meV in agreement with several reported experimental observations [24–26]. Note that due to the long distance between the contacts, the applied electric field on the QDs is low, leading to small Stark shift of the order of tens of μeV .

RF experiments have been performed on the X^- line for all the studied QDs. Fig. 2(a) shows the $\mu\text{-PL}$ map under resonant π -pulsed excitation. We clearly observe two thresholds: at $U_2' = -2.1 \text{ V}$ corresponding to the appearance of the X^- RF and at $U_1 = -4.4 \text{ V}$ where the RF vanishes [27]. We represent schematically in Fig. 2(d)

the different electronic states for an empty QD (upper panel) and a QD containing a photo-created electron-hole pair (lower panel) as a function of the applied gate voltage. The threshold U_1 (U_2) corresponds to the bias voltage where it is energetically favorable for one (two) electron(s) to tunnel from the Fermi sea into the QD in the absence of electron-hole pair [28]. When an electron-hole pair is photocreated in the dot filled with one electron, the threshold U_1 is shifted towards a lower gate voltage U_1' . Indeed, it is straightforward to show that $(U_1 - U_1')$ has the same sign as the energy difference between X^0 and X^- which is positive. This is due to the stronger hole localization in usual InAs QDs [29–31] which bounds the X^- complex. In the same way, $(U_2 - U_2')$ has the same sign as the energy difference between X^- and X^{2-} . This quantity has been measured to be positive [24, 25, 32, 33], thus the threshold U_2 is also shifted toward a lower gate voltage U_2' .

Therefore, the QDs states with and without one photo-created electron-hole pair, can be deterministically controlled at low temperature through the gate voltage, and RF recovery is expected for any desired transition. To show the high efficiency of the gate control, we estimated first the total collection efficiency of our optical setup. The extraction efficiency from the sample structure is about 0.14, and the setup efficiency (from the first collection objective to the detector) is estimated to be $2 \cdot 10^{-3}$. Although the total collection efficiency is not optimized, the corrected number of photons per second is close to the laser pulse repetition rate (82 MHz), indicating an almost one-to-one conversion of one laser pulse into one single photon (Fig. 3(a)).

The RF revival is assisted by an increase of the coherence time T_2 as measured by Fourier transform spectroscopy (FTS) versus the applied bias (Fig. 2(b)). In the radiative limit where a QD is only coupled to the electro-

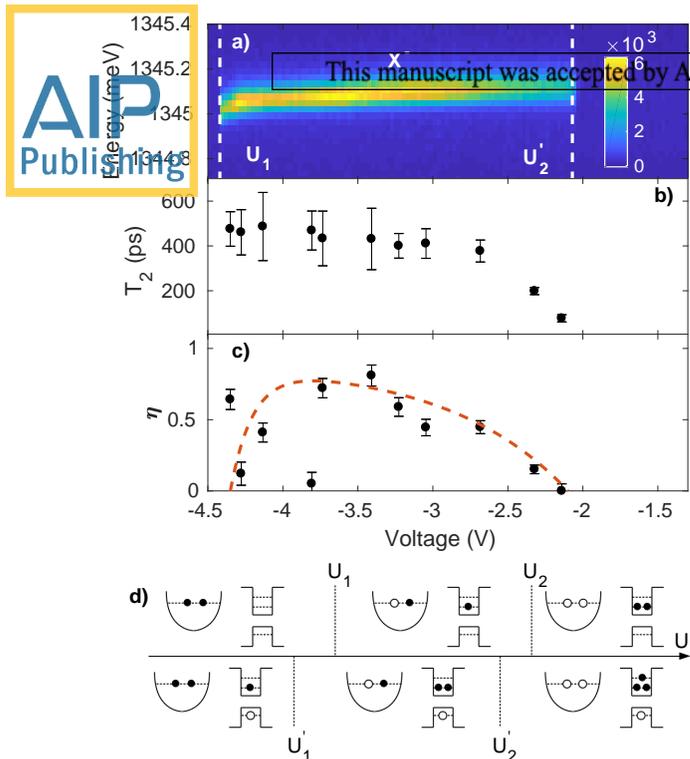


FIG. 2. RF experiments on the X^- line as a function of the gate voltage: (a) μ -PL map under π -pulsed excitation. The color plot is in units of counts/sec. (b) Coherence time T_2 measured by Fourier transform spectroscopy. (c) Inhomogeneous contribution of the pseudo-Voigt profile (see text). The red dotted curve is a guide to the eye. (d) Diagram of the different QD electronic states with applied bias where one or two electrons can tunnel from the Fermi sea to the dot. The upper (lower) panel shows the configurations without (with one) electron-hole pair photocreated in the QD. The black and open dots correspond to electrons and holes respectively.

magnetic field, the RF line is *homogeneously* broadened and $T_2 = 2T_1$. However, a QD is an open quantum system strongly coupled to its environment. For this reason, the RF line is also *inhomogeneously* broadened by the interaction with the phonon bath [34], the fluctuating charges in the vicinity of the QD [12, 13] and the nuclear spins [14]. An additional dephasing process occurs in the presence of a close-lying charge reservoir due to the interaction between the QD discrete excited state and the Fermi sea continuum. Indeed, this coupling leads to an exponentially decaying probability to find the system in the QD discrete state with a characteristic time constant related to the coupling rate. Thus, the QD RF line shape is a lorentzian, i.e. an *homogeneously* broadened line by the interaction with the Fermi sea continuum [35]. Therefore, the value of T_2 and the shape of the RF will depend on the competition between these different dephasing processes. The FTS interference contrast is adjusted by the Fourier transform of a pseudo-Voigt profile [36] as detailed in [8]. Fig. 2(b) shows a rapid increase of the coherence time close to the threshold $U \approx U'_2$ fol-

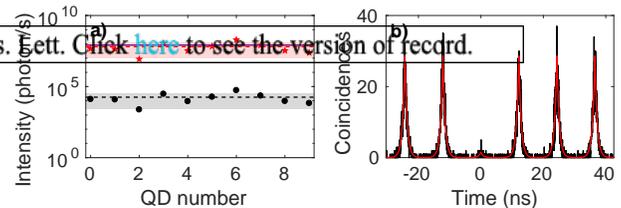


FIG. 3. (a) RF intensity (number of photons per second in log scale) for all the studied QDs: raw data are in black dots and the corrected data by the collection rate of the experimental setup are shown in red stars. The shaded areas represent the data standard deviation and the dotted line corresponds to the mean value. The solid line is the number of laser pulses per second. (b) Coincidences histogram obtained in an HBT setup, measuring a very low multi-photon emission probability $g_{\text{HBT}}^{(2)} = 0.05 \pm 0.02$.

lowed by a plateau where $T_2/2T_1 \lesssim 0.5$, which sets the lower bound for the photons indistinguishability [8, 37]. $T_1 = 580 \pm 5$ ps is the resonant radiative lifetime measured by time-resolved photoluminescence and is independent on the bias voltage. The pseudo-Voigt profile is composed partly by the inhomogeneous contribution discussed above, hereafter called η and shown in Fig. 2(c). η reaches a maximum value of 0.8 around -3.5 V and decreases to zero when the bias voltage gets close to the thresholds U_1 and U'_2 . $\eta = 0$ corresponds to an homogeneously broadened RF line, while $\eta = 1$ indicates that inhomogeneous broadening is dominant.

We now discuss the behavior of T_2 and η as a function of the gate voltage. For $U \approx U'_2$ where an electron from the Fermi sea can easily tunnel into and outside the dot, the coupling between the reservoir and the QD is strong. Therefore, the homogeneous contribution is dominant, η is almost zero and the value of T_2 goes to zero. Between U_1 and U'_2 , the coupling with the Fermi sea is weak, the electron being stabilized in the dot, and the coherence time increases. However, at the same time, the interaction with the solid matrix is still present explaining the high value of η . At 4 K, the loss of coherence due to the interaction with the phonon bath can be estimated [38, 39] and the maximum expected value of T_2 would be about 1 ns. However, the experimental value is lower, suggesting that charge and spin noise are still present and responsible for the residual loss of coherence [40]. For $U \approx U_1$, where the decoherence processes are again dominated by the interaction with the Fermi sea, we observe a decrease of the inhomogeneous contribution but no variation of the coherence time. Indeed, the thresholds for X^0/X^- (U_1) and X^-/X^{2-} (U'_2) do not obey to the same dynamics with applied bias, as also discussed in Ref. [41]. The X^{2-} state has an electron in the p-level with a more delocalized wave function compared to the X^- state where the electrons lie on the s-level. In the former case, the interaction with the Fermi reservoir is stronger and occurs on a larger voltage range, as ob-

served in the variation of the RF intensity (Fig. 2(a)).

On the contrary, close to U_c the RF intensity drops fast with the gate voltage so that expected decrease of T_2 cannot be observed.

Therefore, we performed second order correlation measurements to characterize the single-photon emission purity. Fig. 3(b) presents the coincidences histogram obtained under π -pulsed resonant excitation. We used a Hanbury-Brown-Twiss (HBT) setup with an integration time of 200s. All the photons from the luminescence spectrum are coupled to the fibered HBT without any spectral filtering. We clearly observe an antibunching at zero delay, corresponding to a very low multiphoton emission probability. A multi-exponential decay fit (red solid line) was used to extract the value of $g_{\text{HBT}}^{(2)} = 0.05 \pm 0.02$. We attribute the correlations at zero delay to the scattered laser which nonetheless remains very low, only a few percent compared to the QD RF.

In summary, we present an optimized voltage-controlled device allowing the deterministic control of the QD charge state and the consistent revival of the RF with near unity efficiency. Additionally, strictly resonant coherence time measurements evidence the strong interaction between the QDs and the Fermi sea close to the thresholds with one, or two electrons in the dot. To go further in the understanding and modeling of the coherence time behavior, it would be interesting to treat the coupling between the Fermi sea and the QD with an Anderson-like model [31, 42]. Using this model, interesting experimental features have been addressed like the observation of Mahan excitons [32], the hybridization of the QD states with a filled continuum [43], or the emergence of Kondo correlations [44]. Within the voltage range where the RF is stabilized, minimizing charge and spin noise is still an issue. Additional experiments, for instance, under external applied magnetic field [45] or coherent population trapping [46] would allow polarizing the nuclear spin bath thus reducing the fluctuating spin environment. The contribution of each dephasing mechanism could then be unambiguously assigned. Finally, second order correlation measurements show very low multiphoton emission probability making this kind of device suitable for quantum information applications.

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