



HAL
open science

Behavior of noncircular tunnels excavated in stratified rock masses – Case of underground coal mines

Ngoc Anh Do, Daniel Dias, van Diep Dinh, Tien Tung Tran, van Canh Dao,
Viet Doan Do, Phuc Nhan Nguyen

► **To cite this version:**

Ngoc Anh Do, Daniel Dias, van Diep Dinh, Tien Tung Tran, van Canh Dao, et al.. Behavior of noncircular tunnels excavated in stratified rock masses – Case of underground coal mines. *Journal of Rock Mechanics and Geotechnical Engineering*, 2019, 11 (1), pp.99-110. 10.1016/j.jrmge.2018.05.005 . hal-02019384

HAL Id: hal-02019384

<https://hal.science/hal-02019384>

Submitted on 21 Oct 2021

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.



Distributed under a Creative Commons Attribution - NonCommercial 4.0 International License

Behavior of Noncircular Tunnels Excavated in Stratified Rock Masses – Case of Underground Coal Mines

Ngoc Anh Do¹, Daniel Dias^{2,3}, Van Diep Dinh¹, Tien Tung Tran¹, Van Canh Dao¹, Viet Doan Dao¹, Phuc Nhan Nguyen¹

¹*Hanoi University of Mining and Geology, Faculty of Civil Engineering, Department of Underground and Mining Construction, Hanoi, Vietnam*

²*School of Automotive and Transportation Engineering, Hefei University of Technology, Hefei, 230009, China*

³*Laboratory 3SR, Grenoble Alpes University, Grenoble, France*

ABSTRACT. The amount of tunnels excavated along stratified/sedimentary rock masses in the Quangninh coal area is gradually increasing. Rock mass in Quangninh is characterized by beddings between rock layers. The behavior of stratified rock masses surrounding tunnels depends on both the intact rock and the bedding between rock layers. The main characteristics of stratified rock masses which need to be considered are therefore their heterogeneity and their anisotropy. Depending on the dip angle of rock layers, movements and failure zones developed surrounding tunnels can be asymmetrical over the vertical axis of tunnel. This asymmetry causes adverse behaviors of the tunnel structures.

The objective of this study is to highlight convergence displacements and yielded zones developed in rock masses surrounding noncircular tunnels in Quangninh coal mine area using a finite element method. The presence of bedding joints is explicitly simulated. The numerical results indicated that with the bedding joints dip angle increase, the stress asymmetry over the tunnel vertical axis increases. It gradually leads to an asymmetry of the failure zone surrounding the tunnel. An increase of rock mass quality means a decrease of the rock mass sensitivity to the discontinuities. In addition, a dip angle of the bedding joints of approximately 45 degrees could be considered as the critical angle for which the rock mass mechanism changes between sliding and bending.

Keywords: Tunnel; Bedding; Stratification; Anisotropic; Heterogeneity.

1. Introduction

In the Quangninh province (Vietnam), the number of open pit mines is decreasing and are gradually replaced by underground mines. The amount of tunnels in coal mines is therefore constantly increasing. Generally, rock masses in Quangninh are characterized by joints/beddings between rock layers. Unlike for intact rock, the behavior of stratified rock masses surrounding tunnels depends on both the intact rock and on the joints/beddings between rock layers behaviors. Generally, dip angle of bedding varied from 0° to 90° corresponding to respectively a horizontal and a vertical stratification. The main characteristics of the stratified rock masses in Quangninh coal mines are therefore their heterogeneity and their anisotropy.

In the literature, the effect of beddings on the behavior of rock mass is usually considered using explicit or implicit methods. With explicit methods, bedding joints are explicitly simulated using joint elements (Jia and Tang 2008; Fortsakis et al. 2012; He et al. 2012; Małkowski 2015; Yang et al. 2013; Panthee et al. 2016). In Jia and Tang (2008), a finite element code was used to numerically investigate the influence of the joints dip angles and of the lateral earth pressures factor on the stability of tunnels. The results indicated that both the

51 dip angle and the lateral earth pressure coefficient have a considerable impact on the tunnel
52 behavior. They concluded that in the case of horizontal layered joints, the failure mode is of
53 “rock beam” type; for joints with dip angle between 30 degrees and 45 degrees, the failure
54 mode is sliding of sidewall and detaching, flexing and breaking of the layered rock mass near
55 the tunnel shoulder; for joints with a larger dip angle, the failure mode is sliding of the rock
56 mass along the joints interface. In their study, the gravity of rock mass was however not
57 considered. In addition, it is impossible to make a general recommendation of the effect of
58 joints on the tunnel behavior due to the limited number of performed calculations. He et al.
59 (2012) adopted the distinct element method (UDEEC software) to highlight the behavior of a
60 tunnel under the effect of bedding planes. The authors recommended that an asymmetric
61 support structure should be used to reinforce the geologically inclined bedding asymmetric
62 load. Recently, relatively comprehensive studies of the anisotropic behavior of stratified rock
63 mass in tunnelling conducted by Fortsakis et al. (2012) and Wang et al. (2012) pointed out the
64 importance of the stratification planes and of the rock mass quality affecting the radial
65 displacements around the tunnel. Only circular tunnels were considered in these studies.
66 Małkowski (2015) numerically investigated the effect of the constitutive model and of the
67 rock mass stratification on the rock mass deformation around the tunnels. They demonstrated
68 the inaccuracies of modeling the rock mass by using an elastic constitutive model. In other
69 words, it is necessary to use elasto-plastic models to accurately simulate the rock mass
70 behavior. In this study, a horizontal stratification was only considered.

71 With implicit methods, bedding joints are implicitly considered as transversely isotropic
72 material (Fortsakis et al. 2012; Tran et al. 2015; Rafeh et al., 2015; Wang et al., 2015; Bobet,
73 2016). By comparing the displacement developed in a transversely isotropic rock mass with
74 the one obtained in the corresponding anisotropic rock mass, Fortsakis et al. (2012)
75 emphasized that simulating a rock mass as a transversely isotropic material does not lead to
76 the same displacement field as in anisotropic rock mass. This difference is due to the sliding
77 effect along the bedding joints. It is therefore evident that an explicit simulation of the joints
78 is necessary to introduce for stratified rock masses.

79 Obviously, most of previous researches focused on investigating the behaviour of
80 circular tunnels considering the influence of inclined stratification (Jia and Tang, 2008;
81 Fortsakis et al, 2012; He et al., 2012; Wang et al., 2012, etc.) or the behaviour of noncircular
82 tunnels excavated in horizontal stratification (Małkowski, 2015). So far, the effect of inclined
83 beddings in rock mass has not been often mentioned and has not been clarified in the
84 literature.

85 This paper aims, therefore, to highlight the effect of inclined beddings in rock masses
86 and support structures on the displacement field developed around noncircular tunnels using a
87 finite element method (FEM). The presence of bedding joints is explicitly simulated. The
88 numerical results indicated that with the bedding joints dip angle increase, the stress
89 asymmetry over the tunnel vertical axis increases. It gradually leads to an asymmetry of the
90 failure zone surrounding the tunnel. An increase of rock mass quality means a decrease of the
91 rock mass sensitivity to the discontinuities. In addition, a dip angle of the bedding joints of
92 approximately 45 degrees could be considered as the critical angle for which the rock mass
93 mechanism changes between sliding and bending.

94 95 **2. Evaluation of rock mass properties**

96 In the numerical calculations, a constitutive model using the Hoek-Brown failure
97 criterion (Hoek et al. 2002) was adopted for the rock mass surrounding tunnels (Marinos
98 2014; Małkowski 2015). The joints strength was evaluated through the Barton and Bandis
99 failure criterion (Barton and Bandis 1990). Both above constitutive models are widely applied
100 when tunnels are excavated in rock mass (Fortsakis et al 2012; Małkowski 2015). Typical
101 parameters of the Quangninh coal area (IMSAT 2012) were considered in this study.

102 A range of Geological Strength Index (GSI) values changing from 10 to 80 has been
 103 adopted which covers rock mass conditions varying from very poor to very good. The
 104 uniaxial compressive strength of intact rock (σ_{ci}) was chosen in a range from 10 MPa to 100
 105 MPa, the modulus ratio $MR = 500$ and the geomaterial constant $m_i = 7$. The deformation
 106 modulus of intact rock E_i is determined as follows (Hoek et al. 2002):

$$107 \quad E_i = MR \sigma_{ci} \quad (1)$$

109 Where σ_{ci} is the uniaxial compressive strength of intact rock.

110
 111 The deformation modulus of rock mass ($E_{m,ref}$) (Hoek et al. 2002) was calculated on
 112 the basis of the following relationship:

$$113 \quad E_{m,ref} = E_i \left(0.02 + \frac{1-D/2}{1 + e^{((60+15D-GSI)/11)}} \right) \quad (2)$$

115 Where E_i is the deformation modulus of intact rock, D is disturbance factor.

116
 117 The shear modulus of intact rock (G_i) and rock mass ($G_{m,ref}$) are estimated as follows:
 118

$$119 \quad G_i = \frac{E_i}{2(1+\mu)}$$

$$G_{m,ref} = \frac{E_{m,ref}}{2(1+\mu)} \quad (3)$$

120 Where μ is the Poisson's ratio of rock.

121
 122 Assuming that the rock mass is a combination of intact rock and discontinuities, the
 123 deformability properties of these elements are calculated through the following equations
 124 (Barton 1972; Goodman 1989; Fortsakis et al. 2012):
 125

$$126 \quad \frac{1}{E_{m,ref}} = \frac{1}{E_{m,int}} + \frac{1}{s_p k_n}$$

$$\frac{1}{G_{m,ref}} = \frac{1}{G_{m,int}} + \frac{1}{s_p k_s} \quad (4)$$

127 where $E_{m,ref}$ and $G_{m,ref}$ are respectively the reference rock mass deformation and the
 128 shear modulus, $E_{m,int}$ and $G_{m,int}$ are the deformation and the shear modulus of the internal rock
 129 mass, s_p is the bedding width and k_n and k_s are the normal and the shear stiffness of the
 130 discontinuities.

131
 132 The values of k_n and k_s can be calculated based on results of laboratory tests. In this
 133 study, because such data are not available, these values were calculated based on Equation (4)
 134 as follows (Fortsakis et al. 2012):
 135

$$136 \quad k_n = \frac{E_{m,L} E_i}{(E_i - E_{m,L}) s_p}$$

$$k_s = \frac{G_{m,L} G_i}{(G_i - G_{m,L}) s_p} \quad (5)$$

137
 138 where E_i , G_i are the Young's modulus and the shear modulus of the intact rock and $E_{m,L}$,
 139 $G_{m,L}$ are the Young's modulus and the shear modulus of the rock mass determined with the
 140 GSI_{tab} . GSI_{tab} is the GSI value of the first row of the joint surface conditions illustrated in the

141 GSI chart (Hoek et al. 2002). This case corresponds to intact or massive rock with few widely
142 spaced discontinuities.

143
144 The joint wall compressive strength (JCS) and joint roughness strength (JRC) were
145 determined using the rock joint classification condition suggested by Fortsakis et al. (2012)
146 (see Table 1).

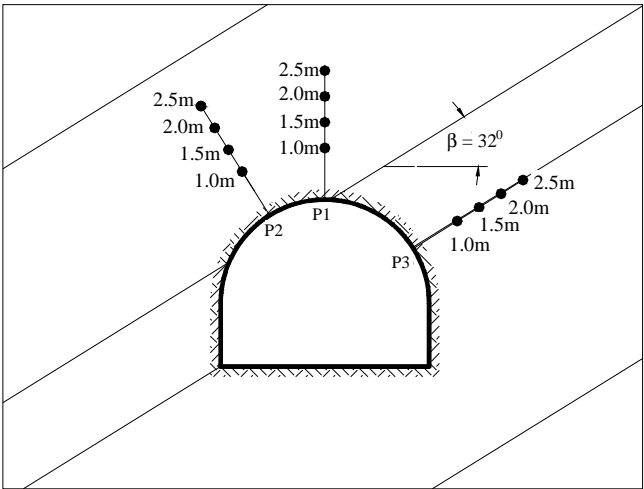
147
148 **Table 1.** Parameters of rock discontinuity

No	Discontinuity surface quality	JRC	JCS
1	Very poor	2	$0,1\sigma_{ci}$
2	Poor	6	$0,3\sigma_{ci}$
3	Fair	10	$0,5\sigma_{ci}$
4	Good	18	$0,6\sigma_{ci}$

149
150 Because the support structure has a great impact on the behavior of the tunnel excavated
151 in stratified rock mass, two cases of tunnels with and without support structure have been
152 investigated in this study.

153
154 **3. Numerical model**

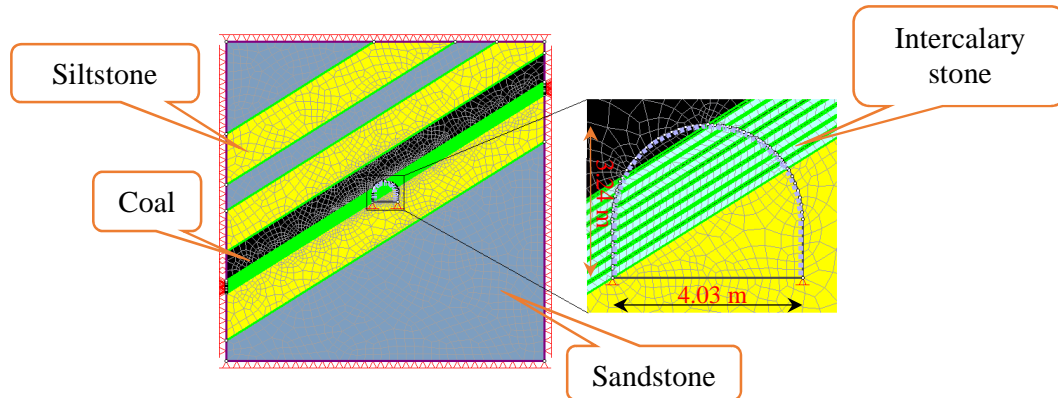
155 FEM was used in this study to model the influence of rock joint on the stability of tunnel
156 and subsequent estimation of parameters which influence on the deformation and
157 development of yielded zone induced in rock mass. FEM has been used previously by many
158 researchers (Fortsakis 2012; Małkowski 2015; Panthee et al. 2016). Firstly, monitoring data
159 (displacements) induced in the surrounding rock mass due to the Tunnel N-6-8 excavation in
160 the Duonghuy coal mine (Quangninh, Vietnam) was used to validate the numerical model.
161 The tunnel shape is presented in Fig. 1. The tunnel dimensions are 4.03 m in width and 3.24
162 m in height. This tunnel was excavated along a coal seam (Fig. 2). This tunnel was used to
163 exploit the coal and transport it to outside. The tunnel is located at the depth of 150 meters
164 from the ground surface. Properties of the rock mass and of the discontinues surrounding the
165 Tunnel N-6-8 are described in Table 2 and Table 3. It should be mentioned that parameters
166 JCS and JRC of joint are determined on the basis of properties of the weaker rock contact.
167 They were determined through both in-site and laboratory tests. This tunnel was supported by
168 steel ribs, their properties are given in Table 4. The steel ribs are installed right after each
169 excavation cycle and at the maximum distance of 0.7m from the tunnel face.
170



171
172

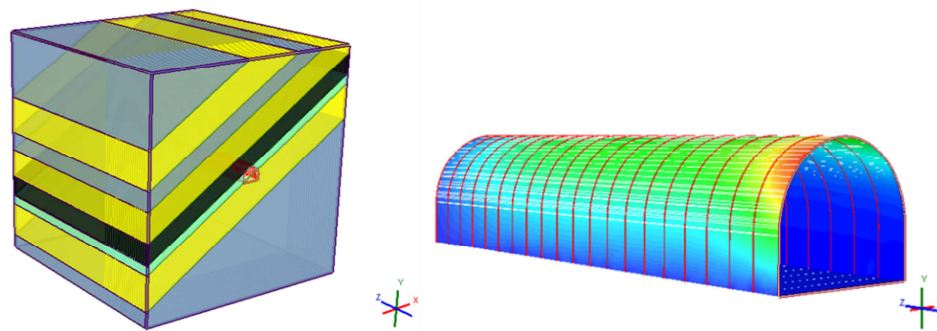
173
174
175

Fig. 1. Location of monitoring extensometers installed in Tunnel N6-8



176
177
178

a) 2D numerical model using the RS2 software



179
180
181
182

b) 3D numerical model using the RS3 software

Fig. 2. Adopted numerical models for the N6-8 Tunnel (Rocscience)

183 Three extensometers have been installed in rock mass from the tunnel wall to monitor the
184 displacements induced in rock mass after the excavation (see **Fig. 1**). Each extensometer has 4
185 rods which have different lengths of 1m, 1.5m, 2m, 2.5m measured from the tunnel wall. The
186 displacements induced in rock mass were frequently monitored during six months until the
187 tunnel boundary reached a stable state.

188 Both 2D and 3D numerical models built using the RS2 and the RS3 softwares
189 (Rocscience 2016), respectively, were used to make a comparison with monitored data
190 obtained from the tunnel site (**Fig. 2**). In the 2D model, a relaxation process using the
191 softening method was applied to take into account of the pre-displacements in rock mass
192 surrounding the tunnel after excavation and before the steel rib installation (Do et al. 2014). A
193 reduced deformation modulus (E_{red}) of 70% of the initial value (E) was adopted on the basis
194 of a back analysis done on the pre-displacement value monitored at the top of the tunnel
195 before the installation of the tunnel support structure.

196
197

Table 2. Parameters of rock layers in Tunnel N6-8

Layers	Density	Uniaxial compressive strength σ_{ci} (MPa)	GSI	Cohesion C (MPa)	Internal friction angle ϕ (degrees)	Young modulus E (MPa)
Sandstone	2.65	86.62	60	1.33	40.59	11,585
Siltstone	2.65	46.48	50	0.69	31.95	4,772
Coal	1.4	20	20	0.19	14.23	556
Intercalary stone	2	25	45	0.392	27.34	2,624

198

199 Measured displacements along three extensometers installed at tunnel site are presented
 200 in **Table 5**. **Fig. 3** shows the yielded zone developed surrounding the tunnel obtained from 2D
 201 numerical model. It can be seen that the ends of extensometers are outside the yielded zone of
 202 the rock mass. The comparison between the numerical and experimental results is presented
 203 in **Table 5**.

204

205 **Table 3.** Stiffness of joints in numerical model for the case of Tunnel N6-8

Rocks in contact	JCS (MPa)	JRC
Sandstone - Siltstone	23.24	10
Siltstone - Intercalary stone	7,5	6
Intercalary stone - Coal	2.0	2
Coal - Siltstone	2.0	2

206

207 **Table 4.** Properties of the steel ribs

Properties	Values
Height of section (m)	0.171
Cross section area (m ²)	0.002173
Inertia moment (m ⁴)	2.43 10 ⁻⁶
Young's modulus (MPa)	210,000
Poisson ratio (ν)	0.25

208

209 **Table 5.** Comparison between monitoring data and numerical models (2D and 3D)

Distance from the tunnel wall (m)	Displacement in rock mass (m)								
	Measured data			2D model			3D model		
	P1	P2	P3	P1	P2	P3	P1	P2	P3
1	0.080	0.095	0.015	0.060	0.088	0.012	0.048	0.094	0.018
1.5	0.045	0.090	0.015	0.047	0.066	0.008	0.038	0.069	0.011
2	-	0.040	0.015	0.033	0.045	0.008	0.030	0.050	0.008
2.5	0.02	0.040	0.015	0.027	0.028	0.008	0.025	0.039	0.004
Maximum displacement (D_{max}) (m)	0.080	0.095	0.015	0.060	0.088	0.012	0.048	0.094	0.018
D_{ratio}	-	-	-	0.75	0.93	0.80	0.60	0.99	1.20

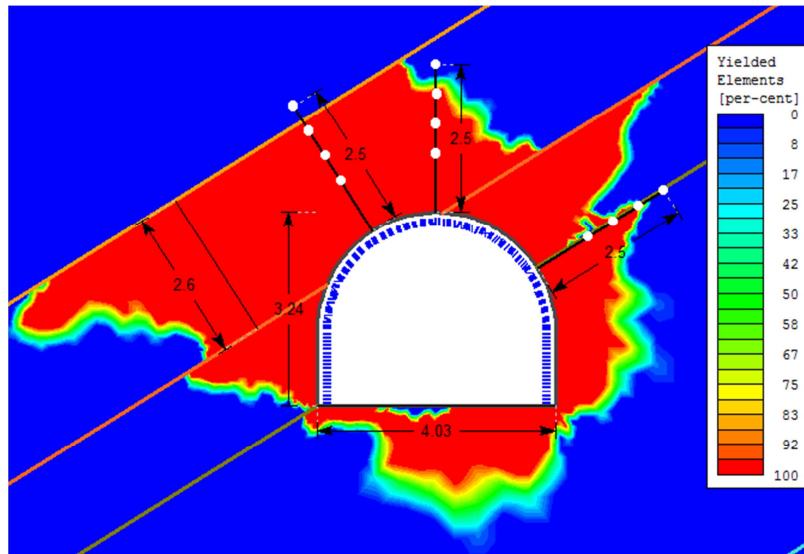
210

211

212

213

Note: D_{ratio} = D_{max-model}/D_{max-measured} (where: D_{max-model} is the maximum displacement obtained in numerical models at each location (P1, P2 or P3); D_{max-measured} is the maximum displacement observed in tunnel site at each location (P1, P2 or P3)).



214
215 **Fig. 3.** Distribution of yielded zone surrounding the tunnel (2D model)
216

217 It can be seen that the 2D numerical model gives displacements which are more or less
218 similar to those obtained in the 3D numerical model and both numerical models are relatively
219 consistent with the monitored data. D_{ratio} values for both numerical models (2D and 3D) are
220 close to unity, especially at point P2. The higher difference between the results of numerical
221 models and monitored data is seen at point 3. This can be related to the fact that this borehole
222 is parallel to the rock mass joint direction (see Figs 1 and 3). The measurements of the
223 extensometer can therefore be disturbed by the joint at this point. Without considering the
224 result at point 3, it is reasonable to conclude that the 2D numerical model using the relaxation
225 process with joint elements between rock layers can be efficiently used. 2D numerical models
226 will be therefore used in the following sections for the parametric analysis.
227

228 4. Tunnels without support

229 In this section, numerical analyses of tunnels without support structure in plane strain
230 conditions have been conducted using the RS2 software (Rocscience). The aim is to highlight
231 the effect of joints parameters on the rock mass behavior surrounding the tunnel in terms of
232 induced displacements and stresses.

233 The section used is not the same as in the first part of the work. A typical section which
234 is usually used in the Quangninh coal mines was adopted here. The tunnel cross section was
235 assumed as an arch-profile crown and vertical sidewalls with dimension of 4.5m wide and 3.5
236 m high. A depth of 300 meters from the ground surface has been chosen because this depth is
237 now widely observed in the Quangninh coal mine area. Typical rock mass parameters
238 including the intact rock and the discontinuities in the Quangninh coal mine area were
239 adopted in this study (see **Table 6**) (IMSAT 2012).
240

241 **Table 6.** Rock mass and joint parameters

Descriptions	Values
<i>Rock mass material</i>	
Modulus ratio MR	500
Unit weight γ (kN/m ³)	24
Poisson's ratio of rock, μ	0.25
Uniaxial compressive strength of intact rock σ_{ci} (MPa)	10; 30; 50; 70; 100

GSI_{tab}	35; 50; 75; 85
GSI (GSI _{tab})	20 (35,50); 40 (50,75); 60 (75,85); 80 (85)
<i>Discontinuities/Joints</i>	
Dip angle of rock layers β (degrees)	0^0 ; 30^0 ; 45^0 ; 60^0 ; 90^0
JCS (GSI_{tab})	$0.1\sigma_{ci}$ (35); $0.3\sigma_{ci}$ (50); $0.5\sigma_{ci}$ (75); $0.6\sigma_{ci}$ (85)
JRC (GSI_{tab})	2 (35); 6 (50); 10 (75); 18 (85)
<i>Other parameters</i>	
Lateral earth pressure coefficient K_0	0.25; 0.5; 1; 1.5; 2
Tunnel depth H (m)	100, 300

242

243

244

245

246

247

248

249

250

251

252

253

254

255

256

257

258

259

The first calculation step of the numerical excavation process consists in setting up the initial stress state taking into consideration the vertical stress under the effect of the gravity field. The ratio between lateral and vertical stresses is assumed to be $K_0=0.5$ for the reference case. For comparison, there are no joints in the first model. In the other models, there are bedding joints at a dip angle of $\beta=0^0, 30^0, 45^0, 60^0, 90^0$ with 0^0 and 90^0 indicating the horizontal and vertical layers, respectively. The joints were modelled as parallel surfaces in the internal rock mass. The distance between joints is equal to 1.0 meter. On the basis of a parametric analysis, numerical models with dimensions of 32m x 32m were adopted to avoid the effect of boundary condition (**Fig. 4**).

260

261

262

263

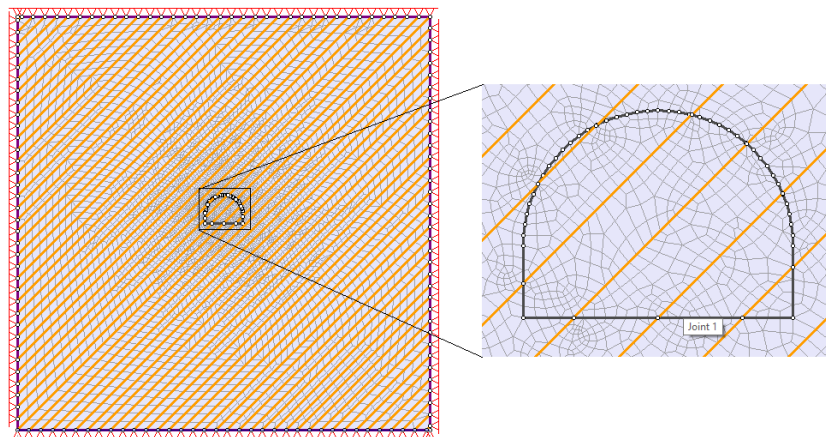
264

265

266

The other discontinuities strength parameters were chosen depending on the rock surface condition. The values of the joint roughness coefficient (JRC) changed from 2 (very poor) to 18 (very good). The joint compressive strength (JCS) varied from $0.1\sigma_{ci}$ (very poor) to $0.6\sigma_{ci}$ (very good) (**Fortsakis et al. 2012**). The GSI value is assumed to change from 10 (very poor) to 80 (very good). All rock masses and discontinuities parameters are presented in **Table 6**. In total, **800** calculations were done, thus covering most of the possible situation that could be encountered in practice of tunnel excavated in stratified rock mass in Quangninh coal mine area.

This section deals with the variations of the convergence displacements of the tunnel wall after excavation considering the influence of the bedding angle, of the joint parameters and of the rock mass quality. These variations were determined at the final state when the unsupported tunnels have reached a steady state. To investigate the effect of joints/beddings on the displacement of the tunnel boundary, 5 observation points were chosen as seen in **Fig. 5**.



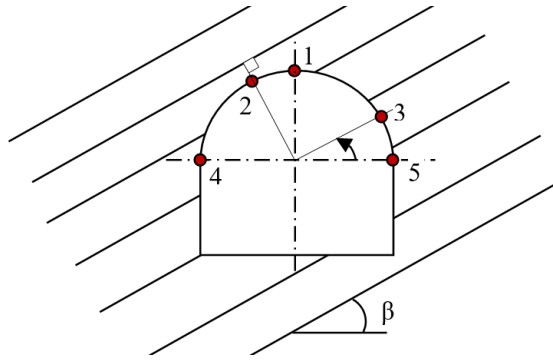
267

268

269

270

Fig. 4. Layout of numerical model

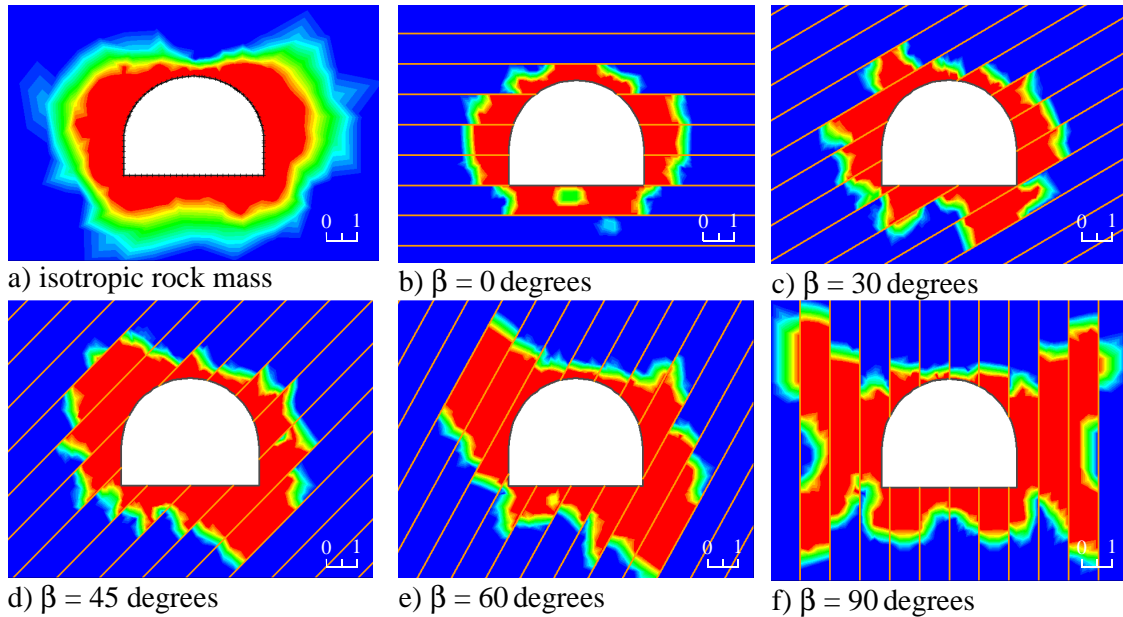


271
272

Fig. 5. Location of observation points on the tunnel boundary

273
274
275
276
277
278
279
280
281
282
283

Fig. 6 presents the yielded zones distribution after excavation in the case of $GSI = 40$, $GSI_{tab} = 50$, $\sigma_{ci} = 30$ MPa, $K_0 = 0.5$. These parameters are the ones of the reference case in this study. For intact rock masses without joints, the yielded zone is smaller than the one observed in the case of stratified rock masses. In addition, the stress distribution around the tunnel excavated in an isotropic rock mass and the case of horizontal and vertical stratification is symmetric. However, for the case of inclined stratified rock mass, with the increase of the dip angle, the asymmetry of the yielded zone developed increases gradually. It is reasonable to conclude that the influence of the stratification on the rock mass behavior surrounding the tunnel after excavation is significant and must be taken into consideration.



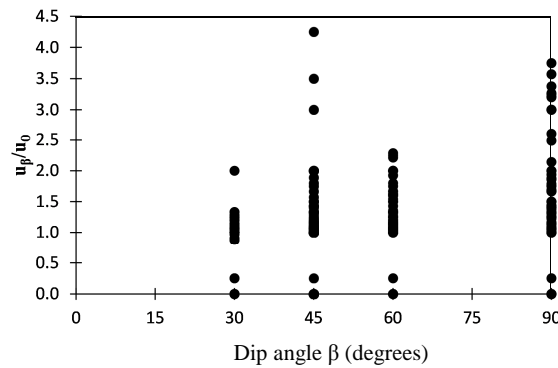
284
285
286

Fig. 6. Yielded zones around tunnels ($GSI = 40$, $GSI_{tab} = 50$ and $\sigma_{ci} = 30$ MPa) for the case of unsupported tunnel

287
288
289
290
291
292
293
294
295

In order to investigate the effect of the dip angle on rock mass behavior, the ratio u_β/u_0 has been adopted. The values of u_β and u_0 are the convergence displacements determined at points 1, 4 and 5 when the dip angles are larger than zero and equal to zero, respectively. The distribution of the ratio u_β/u_0 as a function of the dip angle β for points 1, 4 and 5 is illustrated in **Fig. 7**. It should be noted that the results presented in **Fig. 7** includes all considered GSI values. Generally, the higher the dip angle, the larger the scatter of the ratio u_β/u_0 . In other words, the convergence displacements developed at two sides of tunnel (points 4 and 5) are highly affected by the dip angle of rock layers. It is also interesting to note that the ratio u_β/u_0 is usually larger than the unity which means that the convergence displacements induced in

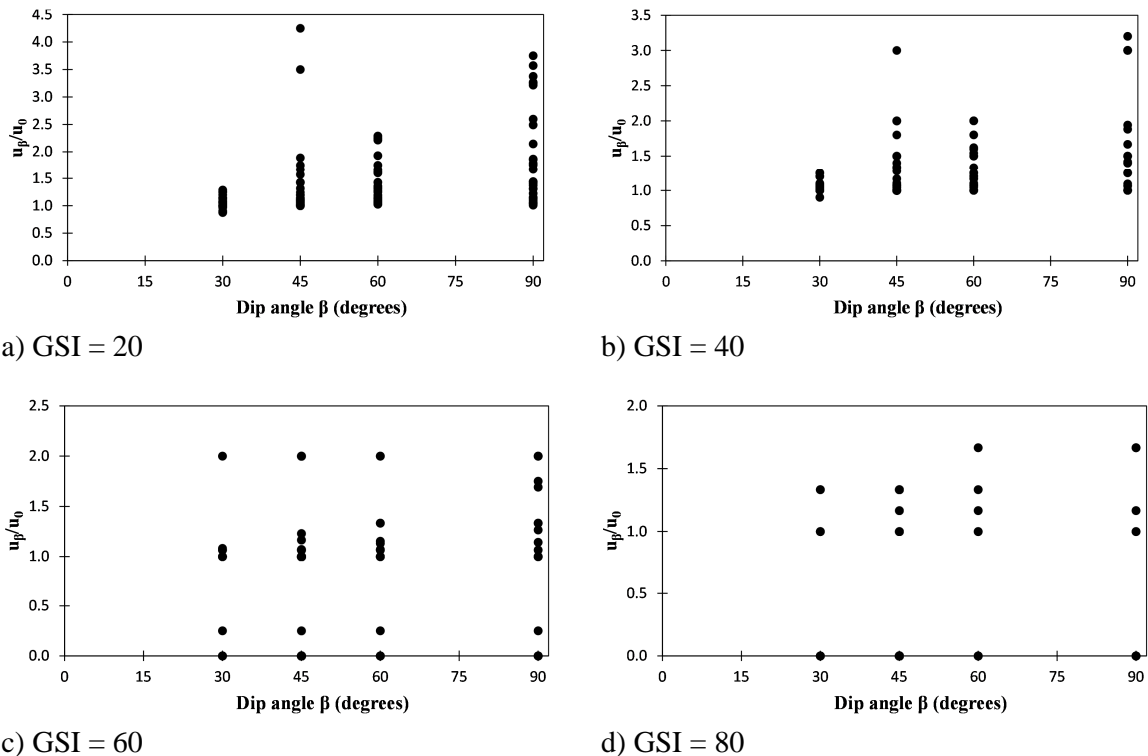
296 the inclined layered rock masses are usually larger than the ones obtained for horizontally
 297 layered rock masses.
 298



299
 300
 301
 302
 303
 304
 305
 306
 307
 308

Fig. 7. Distribution of the ratio u_{β}/u_0 as a function of dip angle (β) for the case of an unsupported tunnel **without differentiation of GSI values**

Using the same data from **Fig. 7**, **Fig. 8** presents the differentiation of the GSI cases influencing on the u_{β}/u_0 ratio at points 1, 4 and 5. It can be seen that the smaller the GSI value, the more dependence of u_{β}/u_0 ratio on the dip angle of rock layers. With GSI values of 60 and 80, the scatter of u_{β}/u_0 ratio depending on the dip angle of rock layer is more or less similar.



309
 310
 311
 312
 313
 314
 315

Fig. 8. Distribution of the ratio u_{β}/u_0 as a function of dip angle (β) for the case of an unsupported tunnel **with differentiation of GSI values**

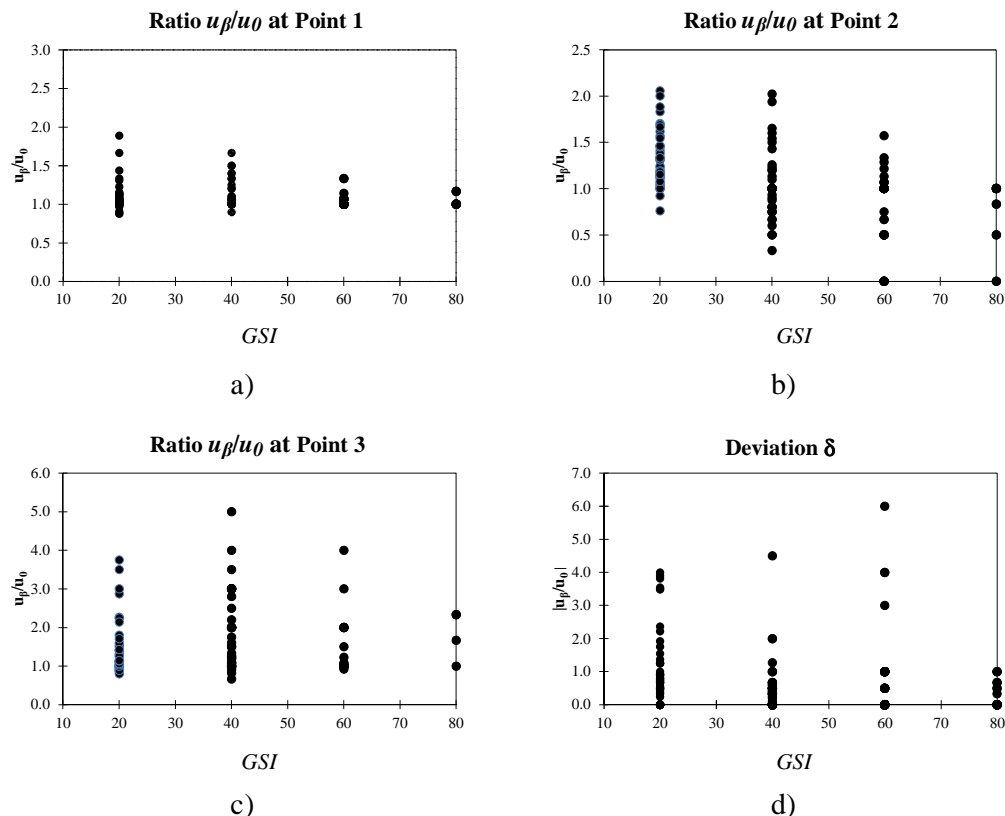
The values of u_{β}/u_0 significantly depend also on the rock mass quality as presented in **Fig. 9**. At tunnel crown (point 1), it can be seen that the scatter of the ratio u_{β}/u_0 tends to decrease as the GSI values increases. Indeed, an increase of the GSI value also means an improvement

316 of the rock mass quality and a decrease of the rock mass sensitivity to the discontinuities. The
 317 same results are also observed for points 4 and 5.

318 As for points 2 and 3, the dependence of the ratio u_β/u_0 on GSI value is not the same as
 319 at point 1. The ratio u_β/u_0 reaches the maximum value and its maximum scatter for a GSI
 320 value of 40 corresponding to a medium rock mass quality. In other cases, for a GSI value of
 321 20 (poor rock mass), or GSI values higher than 60 (good rock masses), a decrease of the
 322 scatter of the ratio u_β/u_0 is observed. It is therefore reasonable to state that the ratio u_β/u_0
 323 strongly depends of the discontinuity in the case of medium rock masses. This dependency
 324 decreases in the case of (1) highly jointed rock masses and/or poor joints condition; (2) rarely
 325 jointed rock mass and/or good joints condition.

326 In order to highlight the asymmetry of convergences, the deviation δ defined as the
 327 difference between the convergences at points 2 and 3 is presented in Fig. 9d. A significant
 328 dependency of the δ value on the GSI can be seen. The higher the GSI value, the smaller the
 329 deviation δ . The deviation of convergences at two sides of the tunnel is larger when the rock
 330 mass quality decreases. Nevertheless, when the GSI values is over 60, the scatter range of δ
 331 value is more or less similar.

332 Fig. 10 presents the convergence displacement of points 1, 2 and 3 considering dip
 333 angle (β) and uniaxial compressive strength (σ_{ci}) variation while other parameters are fixed
 334 ($GSI = 40$, $GSI_{tab} = 50$). The influence of the dip angle (β) on the convergence displacement at
 335 point 2 is significant in the case of weak rock masses ($\sigma_{ci} < 35$ MPa). When the uniaxial
 336 compressive strength (σ_{ci}) increases, its influence decreases. The same results are however not
 337 observed for points 1 and 3. It can also be seen from Fig. 10 a considerable effect of the
 338 compressive strength of the rock mass on the convergence displacements of points 1, 2 and 3
 339 when σ_{ci} value is smaller than 35 MPa. The results obtained for other rock masses qualities in
 340 terms of GSI values are more or less similar to the case mentioned above. For the sake of
 341 simplicity, these results are therefore not presented.
 342



343 Fig. 9. Distribution of the ratio u_β/u_0 as a function of rock mass quality in terms of GSI for the
 344 case of an unsupported tunnel

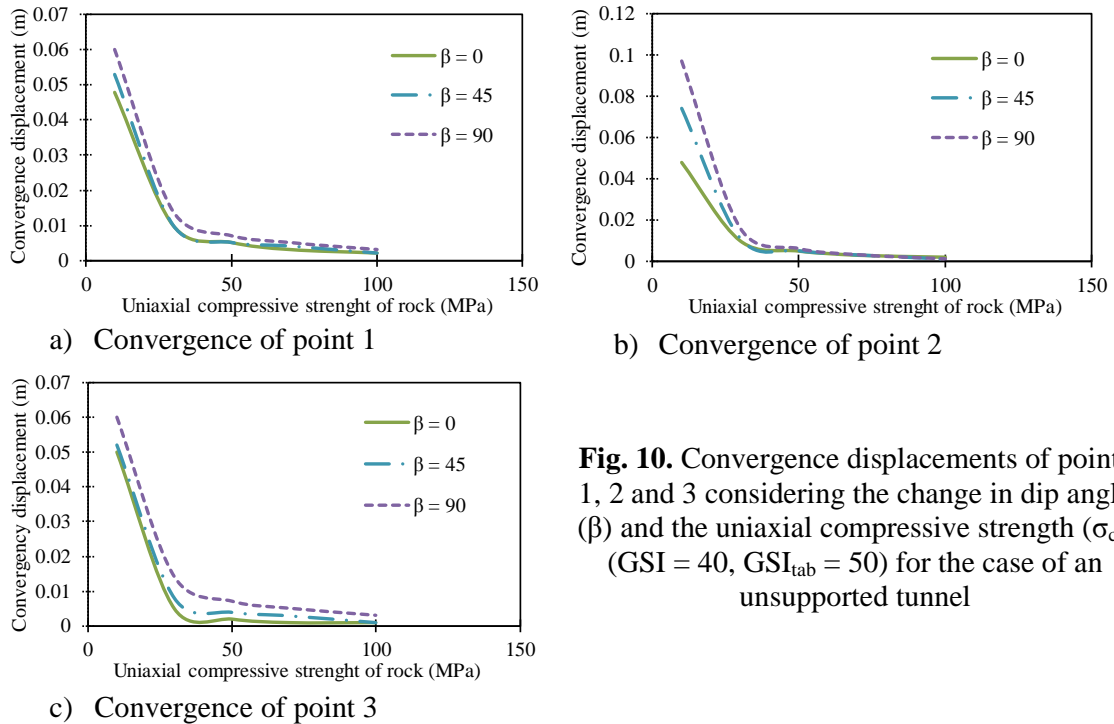


Fig. 10. Convergence displacements of points 1, 2 and 3 considering the change in dip angle (β) and the uniaxial compressive strength (σ_{ci}) ($GSI = 40$, $GSI_{tab} = 50$) for the case of an unsupported tunnel

Fig. 11 presents the effect of the lateral earth pressure coefficient K_0 on the convergence displacement induced on the tunnel wall. Considering the change of joints condition, two values of GSI_{tab} of 50 and 75 have been investigated which corresponds to $k_n = 11,085$ MPa/m, $k_s = 4,435$ MPa/m and $k_n = 111,128$ MPa/m, $k_s = 44,450$ MPa/m. Other parameters are $GSI = 40$, $\sigma_{ci} = 30$ MPa.

In the case of poor joints condition ($GSI_{tab} = 50$), the convergence displacement at point 2 considerably depends on the dip angle of rock layers when K_0 value is larger than unity (**Fig. 11a**). This dependency decreases with good joints condition ($GSI_{tab} = 75$) (**Fig. 11b**). Generally, the higher the lateral earth pressure coefficient K_0 , the larger the convergence displacement at point 2. The same dependency of the convergence displacement of the other points on the tunnel boundary is also observed.

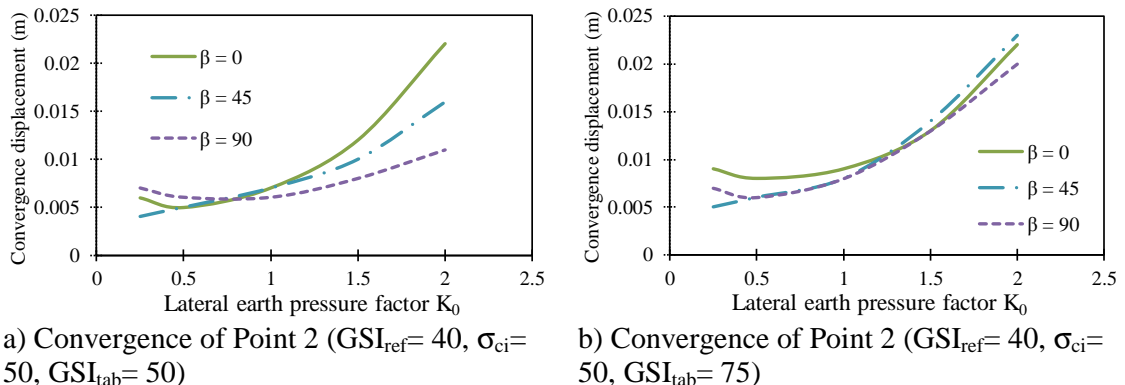
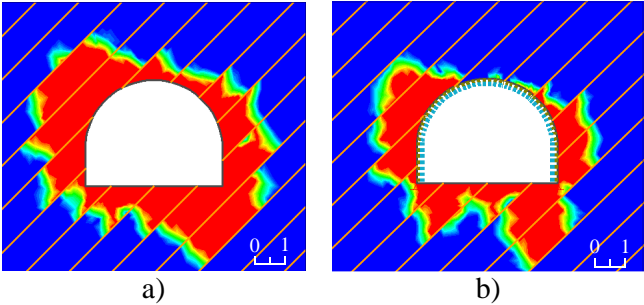


Fig. 11. Convergence displacements at points 2 considering the change in the lateral earth pressure coefficient (K_0) and dip angle (β) ($GSI = 40$, $\sigma_{ci} = 30$ MPa) for the case of unsupported tunnel

5. Tunnels with support

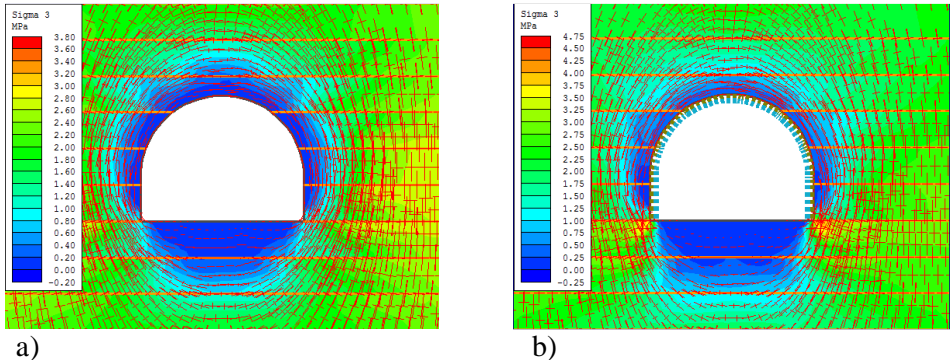
364 Support structure of steel ribs type is widely used to support the tunnel excavated through
 365 inclined stratified rock mass in the Quangninh coal mine area. Parameters of the reference
 366 case has been adopted to analysis the influence of joints on the behavior of supported tunnels.
 367 Tunnels are located at the depth of 300 m from the ground surface. Joint spacing is equal to
 368 1.0 m. The lateral earth pressure coefficient (K_0) is 0.5. Other parameters of rock mass and
 369 discontinuities are presented in **Table 6**. Properties of steel ribs are shown in **Table 4**.

370 **Fig. 12** presents the distribution of yielded zones developed without and with support
 371 structure. It can be seen that the support structure has a great effect on the yielded zone range.
 372 As predicted, a smaller area of yielded zones is observed in the case of support.
 373



374 **Fig. 12.** Yielded zones around tunnels ($GSI = 40$, $GSI_{tab} = 50$, $\sigma_{ci} = 30$ MPa, $\beta = 45^\circ$):
 375 (a) tunnel without support; (b) tunnel with support
 376

377 Obviously, the support structure plays a role in reducing the deformation and/or the
 378 displacements of the rock mass. The development of yielded zones is therefore reduced. In
 379 addition, support structure causes reaction forces which helps to increase the radial stresses in
 380 the rock mass, i.e. the minor stress σ_3 (**Fig. 13**). Consequently, a triaxial stress state
 381 surrounding the tunnel is maintained and helps to mobilize the self-support capacity or the
 382 stability of the rock mass.
 383



384 **Fig. 13.** Minor principal stress (σ_3) in the rock mass: (a) tunnel without support; (b) tunnel
 385 with support ($\beta = 0^\circ$)
 386

387 The influence of the support structure on the tunnel wall radial displacement is presented
 388 in **Fig. 14**. The displacements induced in the case of tunnel with support are smaller than the
 389 ones observed in the case of tunnel without support. However, when the uniaxial compressive
 390 rock mass strength σ_{ci} is greater than 35 MPa, the radial displacements difference in these two
 391 cases is negligible and is generally smaller than 1 cm (see **Fig. 14**). The support structures
 392 play an insignificant role in controlling the displacement of strong rock mass ($\sigma_{ci} \geq 35$ MPa
 393 in this study).
 394

invergence displacement (m)

invergence displacement (m)

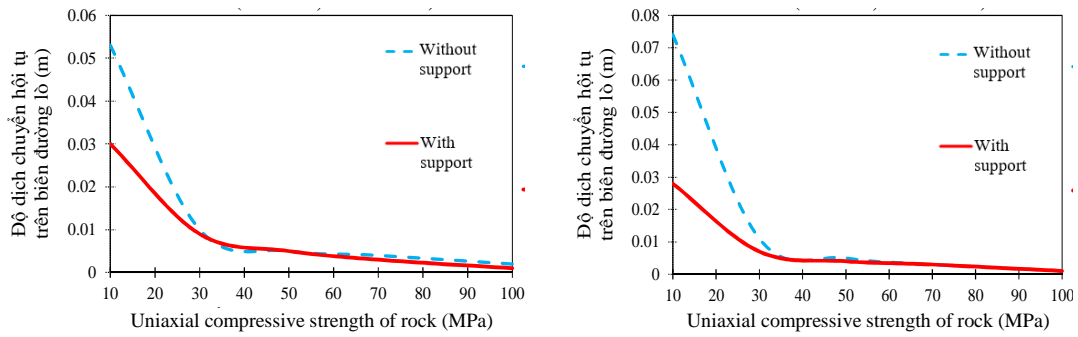


Fig. 14. Convergence displacement of tunnel without support (a) and tunnel with support (b) ($GSI = 40$, $GSI_{tab} = 50$, $\beta = 45^\circ$)

395 **Fig. 15** presents the dependency of the ratio u_β/u_0 with the dip angle of rock layers. It is
 396 necessary to note that the results presented in **Fig. 15** includes all considered GSI values. It is
 397 similar to the investigated results obtained in the case of unsupported tunnels, the scatter of
 398 the ratio u_β/u_0 tends to increase for larger dip angles of rock layers. The larger the dip angle of
 399 rock layers, the greater the influence of joints in rock masses on the radial displacements. It is
 400 evident that the support structure does not significantly change the distribution of the ratio
 401 u_β/u_0 .

402 Using the same numerical data from **Fig. 15**, **Fig. 16** presents the range of u_β/u_0 ratio with
 403 different GSI values. It can be seen from **Fig. 16** that the smaller the GSI value, the more
 404 dependence of u_β/u_0 ratio on the dip angle of rock layers. The same conclusion is obtained by
 405 the case of unsupported tunnel mentioned in section 4.
 406

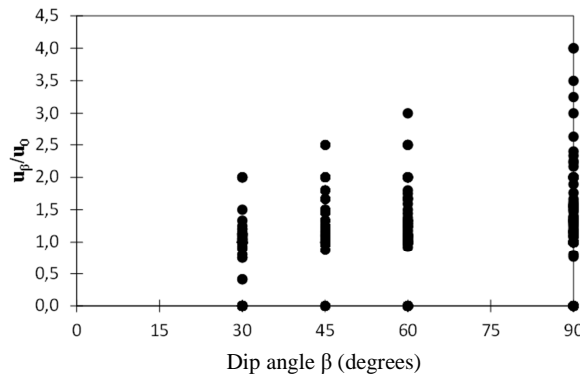
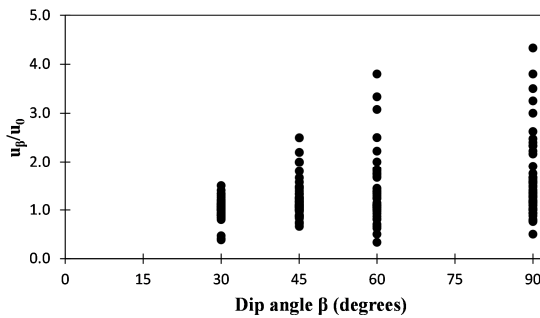
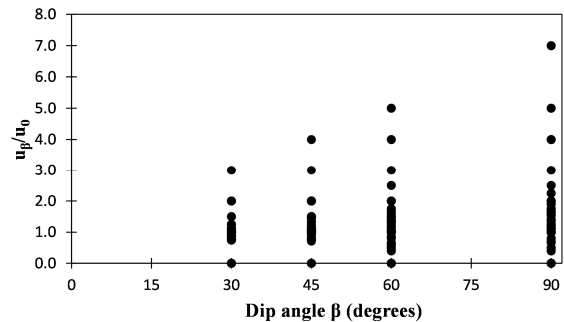


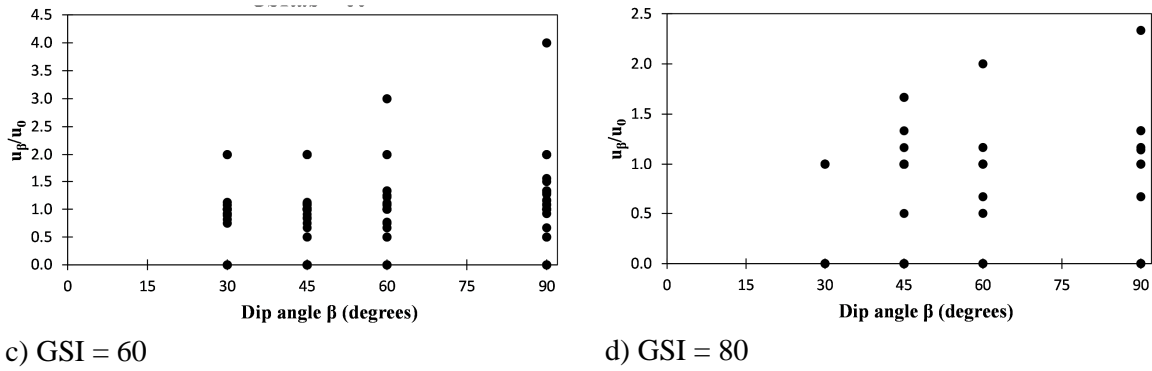
Fig. 15. Distribution of the ratio u_β/u_0 as a function of the dip angle (β) for the case of a supported tunnel without differentiation of GSI values



a) $GSI = 20$



b) $GSI = 40$

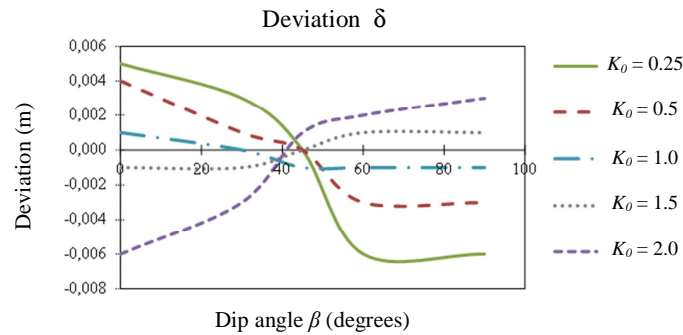


411
412
413
414
415
416
417
418
419
420
421
422
423
424
425
426
427

Fig. 16. Distribution of the ratio u_{β}/u_0 as a function of dip angle (β) for the case of a supported tunnel with differentiation of GSI values

In order to highlight the mechanism of deformation/displacement of the rock layers considering the effect of the lateral earth pressure coefficient (K_0) and of the dip angle of the rock layers (β) (Fig. 5), the deviation δ is presented in Fig. 17. Five different values of K_0 have been considered. Other parameters of the rock masses of the reference case have been adopted.

When the K_0 value is smaller than unity (i.e., $K_0 = 0.25, 0.5$) and the dip angle (β) is approximately smaller than 45 degrees, bending displacements are induced at point 2, which makes a perpendicular direction with the joint surface, is more predominant compared to the sliding displacements induced at point 3. On the other hand, when the dip angle (β) is approximately greater than 45 degrees, the larger displacements are observed at point 3 instead of point 2, which indicates the greater predominance of the sliding mechanism along the joint surface.



428
429
430
431
432
433
434
435
436
437
438
439
440
441
442

Fig. 17. Deviation of the convergence displacements at point 2 and point 3 considering different K_0 values (GSI = 40, $\sigma_{ci} = 30$ MPa, GSI_{tab} = 50) for the case of supported tunnel

For other cases of K_0 which are higher than unity (i.e., $K_0 = 1,5$ and 2), an opposite influence of K_0 on the deformation/displacement behavior of point 2 and point 3, is observed (Fig. 17). However, it should be noted that the predominant bending mechanism at point 2 or sliding mechanism at point 3 change at the critical dip angle of 45 degrees. It is reasonable to conclude that the smaller the angle (α) between the joint surface and the direction of the major principal stress, the more the sliding mechanism is predominant along the joint surface. On the other hand, bending displacements developed perpendicularly with the joint surface observed at point 2 will be greater than the sliding displacements at point 3 when the angle α increases.

Fig. 18 shows the yielded zone distribution for the reference rock with a dip angle of 45 degrees. It can be seen that, the failure area is complex and strongly dependent on the lateral

443 earth pressure coefficient K_0 . In general, the smaller this coefficient is, the greater the yielded
 444 area is. Indeed, when the K_0 values are equal to 0.25 or 2, the yielded area is larger than the
 445 ones observed for K_0 values (i.e., $K_0 = 0.5, 1.0$ and 1.5) (**Fig. 18**). It should also be noted that,
 446 the higher the K_0 value, the greater the yielded area, except for the case of K_0 value of 0.25.
 447 The main yielded area is located on the top left corner of the tunnel, while the small yielded
 448 area is observed on the top right corner.
 449

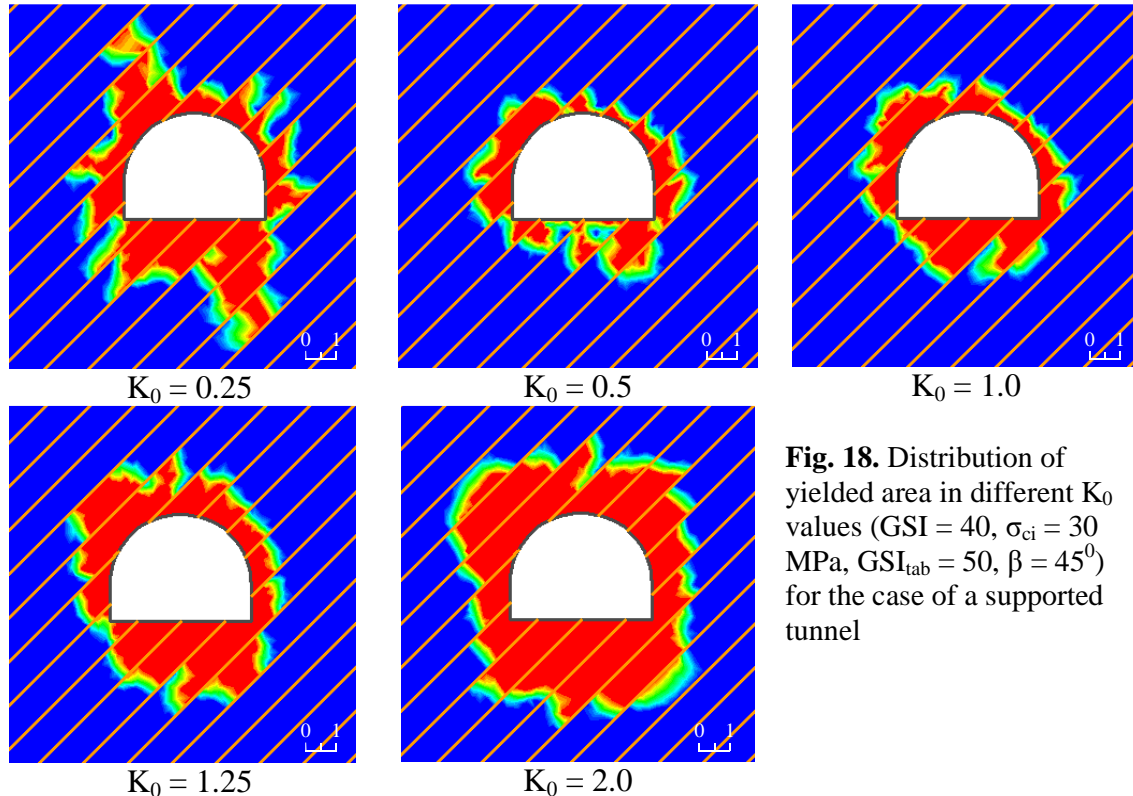


Fig. 18. Distribution of yielded area in different K_0 values (GSI = 40, $\sigma_{ci} = 30$ MPa, $GSI_{tab} = 50$, $\beta = 45^\circ$) for the case of a supported tunnel

450

451 5. Conclusions

452 In this study, numerical calculation has been conducted to investigate the effect of the dip
 453 angle, of the lateral earth pressure coefficient and of the rock mass quality on the convergence
 454 displacements of the surrounding rock mass. Some conclusions can be derived as follows:

455 - For intact rock masses without joints, the yielded zone is smaller than the one observed
 456 in the case of stratified rock masses. In addition, the stress distribution around the tunnel
 457 excavated in an isotropic rock mass and the case of horizontal and vertical stratification is
 458 symmetric. However, for the case of inclined stratified rock mass, the asymmetry of the
 459 yielded zone developed surrounding the tunnel increases gradually when the dip angle is
 460 greater.

461 - The convergence displacements induced in inclined layered rock masses are usually
 462 larger than the ones obtained in horizontally layered rock mass representing by the ratio u_β/u_0
 463 which is usually larger than the unity. In addition, the smaller the GSI value, the more
 464 dependence of u_β/u_0 ratio on the dip angle of rock layers;

465 - An increase of the GSI value means an improvement of the rock mass quality and a
 466 decrease of the dependence of rock mass behavior on the discontinuities. Consequently, the
 467 scatter of the ratio u_β/u_0 tends to decrease as the GSI values increases;

468 - The deviation of convergences at two sides of the tunnel is larger when the stratified
 469 rock mass quality decreases. It means that the higher the GSI value, the smaller the deviation.

470 - For investigated cases in this study, when the uniaxial compressive rock mass strength
 471 σ_{ci} is greater than 35 MPa, the radial displacements difference in the two tunnel cases with

472 and without support structure is negligible. It means the support structures play an
473 insignificant role in controlling the displacement of strong rock mass ($\sigma_{ci} \geq 35$ MPa in this
474 study);

475 - The dip angle of the joint (β) of approximately 45 degrees could be considered as the
476 critical angle at which displacement mechanism of rock mass changes between sliding and
477 bending. When the K_0 value is smaller than unity (i.e., $K_0 = 0.25, 0.5$), bending mechanism is
478 greatly developed at small dip angles (β) while sliding mechanism along the joint surface is
479 more important at large dip angles (β). A sliding mechanism at small dip angle and bending
480 mechanism at large dip angle, is observed for other cases of K_0 which are higher than unity.
481

482 ACKNOWLEDGMENTS: This research is funded by the Vietnamese National Foundation
483 for Science and Technology Development (NAFOSTED) under grant number 105.08-
484 2015.14. The license of Rocscience software at Hanoi University of Mining and Geology is
485 appreciated.

486 REFERENCES

487 Barton N. A model study of rock-joint deformation. International Journal of Rock
488 Mechanics and Mining Sciences 1972; 9: 579-602.

489 Barton N, Bandis S. Review of predictive capabilities of JRC-JCS model in engineering
490 practice. International Symposium on Rock Joints, Loen 1990, 603-610.

491 Bobet A. Deep tunnel in transversely anisotropic rock with groundwater flow. Rock Mech
492 Rock Eng 2016; 49: 4817-4832.

493 Do NA, Dias D, Oreste PP and Djeran-Maigre I. 2D Tunnel Numerical Investigation: The
494 Influence of the Deconfinement method on Tunnel Behavior. Geotechnical and Geological
495 Engineering 2014; 32(1): 43-58.

496 Fortsakis P, Nikas K, Marinos V, Marinos P. Anisotropic behavior of stratified rock masses
497 in tunneling, Engineering Geology 2012; 141-142: 74-83.

498 Goodman RE. "Introduction to rock mechanics", second ed. J. Wiley 1989, Chichester.

499 He B, Zhang Z, Chen Y. Unsymmetrical load effect of geologically inclined bedding strata
500 on tunnels of passenger dedicated lines. Journal of Modern Transportation 2012; 20(1): 24-
501 30.

502 Hoek E, Carranza-Torres C, Corkum B. Hoek-Brown failure criterion-2002 Edition,
503 Proceedings of the 5th North American Rock Mechanics Symposium and the 17th
504 Tunnelling Association of Canada: NARMS-TAC, Toronto, Canada 2002; 1: 267-273.

505 Hoek E, Diederichs MS. Empirical estimation of rock mass modulus. International Journal
506 of Rock Mechanics and Mining Sciences 2006; 43: 203-215.

507 Institute of Mining Science and technology - Vinacomin (IMSAT). "Research on rock mass
508 parameters in Quangninh coal area served to blasting, pressure control during minning".
509 Project report in Vietnamese 2012.

510 Jia P, Tang CA. Numerical study on failure mechanism of tunnel in jointed rock mass.
511 Tunnelling and Underground Space Technology 2008; 23: 500-507.

512 Małkowski P. The impact of the physical model selection and rock mass stratification on the
513 results of numerical calculations of the state of rock mass deformation around the tunnels.
514 Tunnelling and Underground Space Technology 2015; 50: 365-375.

- 515 Marinos V. Tunnel behaviour and support associated with the weak rock masses of flysch.
516 Journal of Rock Mechanics and Geotechnical Engineering 2014; 6: 227-239
- 517 Panthee S, Singh PK, Kainthola A, Singh TN. Control of rock joint parameters on
518 deformation of tunnel opening. Journal of Rock Mechanics and Geotechnical Engineering
519 2016; 8: 489-498
- 520 Rafeh F, Mroueh H and Burlon S. Accounting for joints effect on the failure mechanism of
521 shallow underground chalk quarries. Computers and Geotechnics 2015; 69: 247-261.
- 522 Rocscience. "Software Manual" (<https://www.rocscience.com>) 2016.
- 523 Tran MH, Sulem J, Subrin D. A closed-form solution for tunnels with arbitrary cross section
524 excavated in elastic anisotropic ground. Rock mech. Rock Eng. 2015; 48: 277-288.
- 525 Yang H, Jiang X, Wen C, Yin J. Modeling the deformation of tunnel excavations in layered
526 rock masses. Electronic Journal of Geotechnical Engineering 2013; 18: 723-734.
- 527 Wang M, Gou G, Wang X, Gou Y, Dao VD. Floor heave characteristics and control
528 technology of the roadway driven. International Journal of Mining Science and Technology
529 2015; 25(2): 267-273.
- 530 Wang SY, Sloan SW, Tang CA, Zhu WC. Numerical simulation of the failure mechanism of
531 circular tunnels in transversely isotropic rock masses. Tunnelling and Underground Space
532 Technology 2012; 32: 231-244.

533

534 **Highlights**

- 535 - Effect of the lateral earth pressure coefficient and of the rock mass quality
536 - The stratification influence on the rock mass behavior is significant
537