

Hydrodynamics and scale-up of bubble columns in the heterogeneous regime: Comparison of bubble size, gas holdup and liquid velocity measured in 4 bubble columns from 0.15 m to 3 m in diameter

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14				
15	Keywords			
16	Bubble Column, Sauter Diameter, Scale-up, Velocimetry, Heterogeneous Regime, Experimental,			
17	Cross-correlation, Multiphase reactor, Clustering			
18				
19	Highlights			
20	Bubble Sauter diameter, gas holdup and axial liquid velocity measurements are performed			
21	• 0.15m, 0.4m, 1m and 3m diameter bubble columns are investigated			
22	• A wide experimental database is furnished to assist further model developments			
23	• Void fraction and liquid velocities profiles happen to be self-similar in the heterogeneous			
24	regime			
25	• The entrained liquid flow rate, proportional to D ^{3/2} , is only set by the column diameter			
26	• The quantity (gD) ^{1/2} appears as a natural scale for mean and fluctuations velocities.			

27

29 Abstract

The development of CFD models coupled with Population Balance is a very promising topic 30 31 concerning multiphase reactors. In the case of bubbly flows and bubble columns, a serious lack of 32 local hydrodynamic characterizations still harms development and validation of relevant models. To 33 fill partially this gap, a new bubble size measurement technique, previously introduced by Maximiano 34 Raimundo et al. (2016), has been applied on a very wide range of bubble column diameters (from 35 0.15m to 3m) and superficial gas velocities (from 0.06m/s to 0.35m/s). Size measurements have been 36 coupled with others concerning gas holdup and axial liquid velocity, in order to provide an 37 experimental database allowing to clarify the scale-up rules and to assist future modelling works. Average bubble sizes have been measured as globally similar at every scale. Measured holdup and 38 39 average liquid velocity confirm already reported behaviours at lower column diameters. Liquid 40 velocity fluctuations also follow self-similar radial profiles and are proportional to the average liquid 41 velocity at the centre of the column leading to a strong turbulence intensity. The fact that the quantity (gD)^{1/2} appears as a natural velocity scale and the presence of strong gas-holdup gradients 42 43 underline the similarity between bubble columns operated heterogeneous regime and free thermal 44 convection in pipes.

Strong gas holdup gradients are present in the flow due to convective instabilities

45 1. Introduction

46

Although being a major research topic for decades, the design and scale-up of bubble column reactors is still a difficult task for chemical engineers, as associated hydrodynamic and transfer phenomena are very sensitive to physical properties of fluids, operating conditions and geometrical settings. A huge number of correlations have been developed in the past to assist scale-up by means of 0D or 1D approaches (Deckwer, 1992; Kantarci et al., 2005, Besagni et al., 2018). Available correlations are generally valid in rather narrow ranges of design parameters, physical properties and 53 operating conditions. Nowadays it is generally admitted that CFD can be used to secure industrial 54 designs when outside of validation ranges of empirical correlations. But preliminary parameter 55 adjustments are generally necessary to fit initial simulations on a given well investigated scale. The fitting step keeps CFD far from being a full predictive tool. Parameters to be adjusted can concern 56 57 turbulence modelling, including Bubble Induced Turbulence (McClure et al., 2014 ; Joshi, 2001), but 58 above all, interfacial forces (Jakobsen et al., 2005). There is no real consensus concerning the forces to consider to achieve realistic simulations, except for the drag law that all authors point out as 59 60 impacting mostly the calculated gas holdup. The use of lift, added mass, wall lubrication and 61 turbulent dispersion are sometimes suggested to improve the agreement between experimental data and CFD simulations (Krishna et al., 2001; McClure et al., 2015). However, during a previous 62 work (Gemello et al., 2018b), it was found that time-averaged hydrodynamics (i.e. gas holdup and 63 64 liquid velocity profiles) of several bubble columns were satisfactorily predicted using an apparent drag formulation as the only interfacial force. Nevertheless, the mean bubble diameter had to be 65 66 beforehand known to perform such simulations, as it conditions directly the drag force, and thus gas 67 holdup (Guedon et al., 2017). To overcome this limitation in presence of breakage and coalescence 68 phenomena, one powerful possibility consists in associating CFD with a population balance on Bubble 69 Size Distribution (BSD) (Buffo et al., 2013, Lehr et al., 2004, Sanya et al., 2005). If efficient, this would 70 make CFD a much more predictive tool.

71 Whether to develop interfacial force models for CFD or Population Balance kernels, experimental 72 data are essential, including information concerning bubble sizes in flow regimes of industrial 73 interest. Only a few experimental data are usable for this purpose. Major of them are based on 74 multitips optical probes (Chaumat et al., 2005, Xue, 2004, Xue et al., 2008, McClure et al., 2017). 75 Multitips technique ideally allows to measure both bubble chord and velocity distributions. The technique is based on the processing of the phase-signal delay between probes located at different 76 77 heights. As often pointed out by authors, its accuracy is acceptable at the centre of the column, 78 where bubble have mostly vertical trajectories, but it rapidly decreases with the distance from it, as

79 bubble trajectories become more chaotic and include downward motion and the delay between signals is not linkable with the axial bubble velocity anymore. In addition, the performances of 80 81 multitips probes in terms of minimum detectable bubble size are not clearly determined. An alternative approach consists in the use of a measurement technique independent of the bubble 82 83 trajectory. This is the case of the cross correlation (CC) technique developed by Maximiano 84 Raimundo et al. (2016) and validated in the heterogeneous regime by comparison with endoscopic measurements. The CC technique does not measure the global BSD, but only the mean Sauter 85 diameter, i.e. the ratio between 3rd and 2nd moments of the BSD. But the measurements have the 86 same accuracy regardless of the radial position. It has been applied recently to the study of the effect 87 of water quality and the gas sparger design, in a 400mm column diameter (Gemello et al., 2018a). 88

In the present work, the same cross correlation technique has been used to measure bubble sizes in 89 90 four bubbles columns from 0.15m to 3m in internal diameter, with the purpose of investigating the effect of scale-up on bubble sizes, for an identical gas/liquid system. Distilled or demineralized water 91 92 are generally used in academic studies, but as tap water and air were the only fluids usable in the 93 biggest column, a similar system has been used at all scales. The tap water used in the present work 94 can be qualified as partially contaminated, as it exhibits a less coalescent behaviour than 95 demineralized water. One limitation of using tap water is that its quality depends on the location and 96 can lead to difficulties to repeat experiments elsewhere. To overcome this issue, It has been shown 97 in (Gemello et al., 2018a) that the tap water used in the present study behaves as a solution of 98 demineralized water containing 0.01% in weight of ethanol (Gemello et al., 2018a). In addition to the 99 bubble size, the global ($<\alpha_G>$) and local (α_G) gas fractions have been measured via the liquid 100 elevation measurement and the optical probes used for the cross correlation technique, respectively. 101 Axial liquid velocity profiles (average and fluctuation RMS values) have been also measured with a 102 modified Pitot tube, so-called Pavlov tube technique (Forret et al., 2003). This technique is the only 103 one usable at high gas holdup in all column sizes. Measurements have been done at different Vsg 104 from 0.03m/s to 0.35m/s depending on bubble columns. In the following, the four experimental

setups are introduced, as well as the involved measurement techniques. Then results concerning gas fraction, liquid velocity and bubble sizes are summarized and discussed. A discussion concerning the presence of bubble clusters and of voids (regions with few bubbles) and the role of these meso-scale structures on the hydrodynamics of the heterogeneous regime is finally proposed.

109 2. Experimental setups

110 In the present work, four different columns with 0.15 m, 0.4 m and 1 m and 3m inner diameters have 111 been tested. All the experiments were conducted with compressed air, which had been dried and 112 cooled, as the gas phase and with water, with no net liquid flow rate (batch mode), as the liquid 113 phase. In the different columns, a partially contaminated tap water is used. Table 1 reports water 114 analysis.

115 Table 1: tap water analysis @ 20°C

Surface tension (mN/m)	67
Conductivity @ 25°C (µS/cm)	559
Carbonate (mg/L)	≈0
Hydrogenocarbonate (mg/L)	251
рН	7.9

116

In the four columns, the gas was introduced into the column from the base. The volumetric flow rate 117 was determined by a row of several calibrated flow-meters, with an uncertainty given by suppliers 118 119 equal to 1.6%. The gas distributors are perforated plates, the number of holes and their diameters in 120 the different columns are given in the following table. The injectors have been designed to ensure 121 comparable porosities (at a value small enough to uncouple the gas injection and the bubble column 122 dynamics), and also to form gas jets with comparable ejection velocities (as the ejection velocity is 123 equal to the superficial gas velocity divided by the porosity of the injection plates) which are 124 expected to experience similar break-up process and thus to deliver comparable bubble size 125 distributions at injection in all columns. Columns of 0.15 and 0.4m inner diameter exhibit exactly the 126 same conditions of gas sparging with orifices 1mm in diameter and 10mm long. The injector for the 127 1m inner diameter column has the same porosity, i.e. the same gas velocity at the outlet of injections 128 holes (from 13 to 140m/s), but the diameter of holes is doubled. Indeed, the effect of the hole size 129 can be considered as small as hole diameters stand much smaller than bubble sizes in the columns. 130 The biggest column is equipped with a different sparger, with larger and shorter injection holes and 131 with a lower porosity, but leading to comparable ejection gas velocities (from 37 to 100m/s). 132 However, Gemello et al. (2018a) have studied the impact of the sparger on the bubble size in the 133 0.4m inner diameter column used in the present study. It has been found that the sparger design has an important effect at the bottom of the column. This effect is due both to the spatial gas 134 distribution, conditioned by the number of holes, and the bubble sizes generated by different 135 136 spargers, which can be very disparate. But the effect of the sparger becomes negligible above a 137 distance of 0.4m from the bottom of the column because of the dominant breakup phenomena whatever the water quality. This behaviour is in agreement with the usual observation that, in the 138 139 heterogeneous regime, quantities such as local void fraction and velocities are weakly sensitive to 140 injection conditions when $H_0/D > 2$ and when the data are gathered within the (almost) fully 141 developed region (Forret et al., 2006). In addition, it will be shown in section 4 that the mean bubble sizes are similar for all columns and all flow conditions, probably thanks to an efficient break-up 142 143 process of the gas jets formed at injection.

144 Table 2: gas distributors characteristics in the different columns

Column	Number of	Hole diameter	Length/diameter	Porosity (%)	Pitch (mm)
	holes	(mm)	ratio of injectors		
Ø0.15m	55	1	10	0.24	15 (triangular)
Ø0.4m	391	1	10	0.24	15 (triangular)
Ø1m	613	2	10	0.25	37 (triangular)
Ø3m	164	9	0.5	0.15	200 (squared)

145

The columns used in this study present of pairs of diametrically opposed holes at different heights (0.5m, 1m, 1.5m, 2.6m, 3.4m and 4.6m above the gas distributor in the case of the 1 m in diameter column), enabling the position of different technical means (Pavlov tube, optical probe...) or can be used as pressure taps. The scheme of the 1 m in diameter column is given in the Figure 1. The scheme of the other columns is very similar to this one.

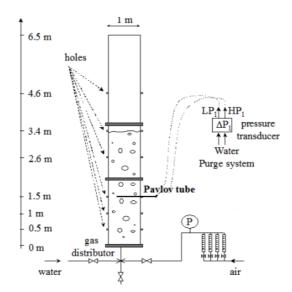


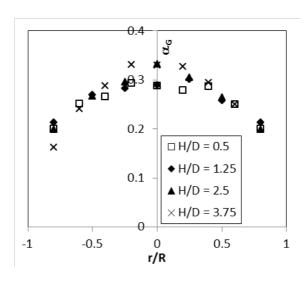


Figure 1: schematic view of the 1 m in diameter column and its perforated plate

154 In addition, the 0.15 m, 0.4 m and 1 m diameter columns were operated with a liquid static height/column diameter "aspect ratio" (H_0/D) of 4. The 3 m diameter column has operated with 2.2 155 156 liquid static height/diameter ratio because the column is only 12 m high. Besagni et al. (2017a) 157 studied the effect of the aspect ratio on the gas holdup and suggested a critical aspect ratio of 5. 158 Nevertheless, exhaustive experimental results reported by these authors show that above 3-4, the 159 effect of the aspect ratio on gas holdup becomes very weak. This is also confirmed by the 160 measurements of Sasaki et al. (2016). Measurements have been performed at an elevation height of 161 2.5 times the column diameter (H/D=2.5), except in the 3m column, inside which measurements are 162 performed at H/D=2. According to Forret et al. (2006), such elevations are indeed within the fully 163 developed flow region. However, the recent work of Guan et al. (2016) may lead to moderate this conclusion. They found that gas holdup and liquid velocity radial profiles were never totally 164 165 independent of the axial position in a column of 0.8m in diameter. Yet, using a uniform gas sparger, 166 the flow happens to be almost fully developed between H/D from 2 to 4. Guan et al. (2016) also 167 suggested that the height of flow development depends on the column diameter. Figure 2 reports gas holdup profiles measured in the Ø0.4m column at Vsg=0.16m/s and at different heights. Profiles 168 169 measured at H/D = 2.5 and 3.75 are similar, while some discrepancies are observed below, especially in the middle of the column. In summary, the aspect ratio of the studied columns is considered to be
sufficient to neglect its effect on hydrodynamics, and the height of measurement is comprised within

172 the range of fully developed flow.

173



174

175Figure 2 : Comparison of gas holdup profiles measured in the Ø0.4m column at different H/D. Vsg=0.15m/s (H₀/D=4)176

177

178 3. Measurement techniques

179 *3.1. Gas holdup*

180 The global gas holdup can be directly calculated by the visual observation of the expansion of liquid

181 height by:

182

$$183 \quad \langle \alpha_G \rangle = 1 - \frac{H_0}{H_D} \tag{1}$$

184

185 Where $\langle \alpha_G \rangle$ represents the global void fraction, H_0 represents the non-aerated liquid height and H_D 186 the aerated liquid height. In the present study, the liquid height is measured by visual observation 187 along a graduated rule, and fluctuations of liquid level induce a relatively high uncertainty of the 188 measurement, estimated at 10%. Sasaki et al. (2016) strongly decreased the uncertainty while using image processing to detect liquid level. The local gas holdup was measured by a light reflective 189 190 optical probe. The beam is generated by a laser and is sent through the optical fiber to the point of 191 the probe. If the probe is in contact with the liquid phase, the light beam is refracted through the 192 liquid media. Otherwise, if the probe tip is in contact with the gas phase, the light beam is reflected 193 by the bubble into the probe tip and then detected by a photodiode where the light beam intensity is 194 converted into voltage. Adding the time that the probe detects the gas phase, the local gas hold up is 195 determined by the following equation.

196

197
$$\alpha_G = \frac{Cumulated gas time}{Experimental time}$$
 (2)

198

The local gas holdup detected with the optical probe was compared with global gas hold-up for heterogeneous conditions in the 0.4m bubble column. The agreement was within ±15% (Maximiano Raimundo et al., 2016), which is satisfactory owing to the uncertainty on the determination of $\langle \alpha_G \rangle$.

202

203 3.2. Cross-Correlation (Bubble size)

In order to characterize bubbles in dense, heterogeneous bubbly flows such as those encountered in industrial bubble columns, a recently developed measuring technique based on the spatial correlation of phase indicator functions is proposed (Maximiano Raimundo et al., 2016). The normalized cross-correlation is a function that quantifies the similarity of two binary signals by analysing both signals simultaneously:

$$209 \qquad CC = \frac{\int_{t=0}^{texp} Signal_A(t) \times Signal_B(t) dt}{\int_{t=0}^{texp} Signal_A(t) dt}$$
(3)

Here Signal A and Signal B represent the raw signals coming from two different probes at the same 211 212 elevation in the column at a radial distance (d) and t_{exp} represents the time of registration. The cross-correlation value is maximal if both probes are at the same point in space (distance between 213 214 probes d of 0 mm), since the signals will be identical. In a single bubble-probe interaction, as the 215 distance between the probes increases, the cross-correlation of the probe signals will decrease. The 216 cross-correlation will be zero when the distance between probes becomes larger than the bubble 217 horizontal diameter due to the fact that the same bubble cannot be detected by both probes at the 218 same time. Nevertheless, in a bubble column, the cross-correlation is never zero even if the distance 219 between probes reaches a value much larger than the largest bubble horizontal diameter. At large 220 distances, the cross-correlation tends to the local gas hold-up α_{G} . It has been shown that some 221 information related to the horizontal bubble size can be extracted from the initial linear slope of the 222 cross-correlation curve as a function of probes distances (Maximiano Raimundo et al., 2016). The relationship between the Sauter mean value of horizontal bubble diameters, noted $d_{32,h}$, the 223 224 correlation coefficient CC and the inter-probes distance d always expresses as follows:

225

226
$$d_{32,h} = a \frac{d}{(CC(d)-1)}$$
 (4)

227

where the prefactor *a* is function of the bubble shape, as detailed in the following table (details inMaximiano Raimundo et al., 2016).

230

231 Table 3: Prefactors *a* for various bubble shapes

	Sphere	Oblate	Prolate with Ecc=0,7
Prefactor a	-1.472	-1.5978	-1.7

232

To validate this method, it has been compared to endoscopic imaging. The Sauter mean horizontal diameters detected with the correlation technique happen to be in good agreement with those provided by endoscopic imaging. This latest method enables also the determination of the average eccentricity (ecc) : the latter has been measured equal to 0.7 for all flow conditions and all column dimensions except for the 3m I.D. column for which the eccentricity was not measured. Therefore, the Sauter mean diameter d_{32} can be linked to the $d_{32,h}$ measured by the cross-correlation as follows.

240
$$d_{32} = d_{32,h} * ecc^{1/3}$$
 (5)

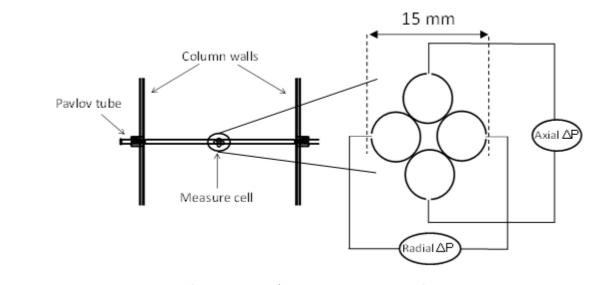
241

with *ecc* = 0.7.

243

244 *3.3. Pavlov tube(axial liquid velocity)*

The Pavlov tube used in this work is composed by four 5 mm diameter tubes, arranged as it is shown in the right-hand side of the Figure 3. The four tubes are placed inside a 30 mm diameter tube, which crosses horizontally the column, in order to obtain rigidity and to allow horizontal displacement. The 5 mm diameter tubes are completely closed, except for a 0.5 mm diameter lateral hole that assures that the pressure inside the tube is equal to the one in the column.



- 250
- 251 252

Figure 3: Schematic representation of the Pavlov tube (Axial measurements are performed along a vertical axis, radial measurements are performed along a horizontal axis)

253

The holes of the tubes on the vertical plan are placed in the same axis but in opposite directions, as depicted in Figure 3. Additionally, each tube on the vertical direction is connected to 256 one of the chambers of a differential pressure sensor. These tubes serve to measure the axial 257 pressure difference, since the holes on the tubes are aligned with the column vertical axis. The 258 Pavlov tube allows also the measurement of the radial liquid velocity, quite low in this study, not 259 discussed in this paper. The measurements of the axial pressure differences (ΔP) can be used to 260 calculate the instantaneous axial liquid velocity recurring to the following equation.

261
$$U_{(x,t)=}\begin{cases} \sqrt{\frac{2\Delta P(x,t)}{\rho_{l}}} & \text{if } \Delta P(x,t) \ge 0\\ -\sqrt{\frac{-2\Delta P(x,t)}{\rho_{l}}} & \text{if } \Delta P(x,t) < 0 \end{cases}$$
(6)

262 The axial ΔP measurement was made with a differential pressure transmitter Rosemount 3051T with 263 a range of ±60 mbar, a frequency of 8 Hz and resolution of 0.01 mbar Let us mention that corrections 264 of eq.(6) accounting for local void fraction have been sometimes proposed. On one hand, the largest 265 of these corrections is the one proposed by Bosio and Malnes as discussed by Riemann et al. (1984). 266 According to that correction, the difference in velocity prediction remains smaller than 3% since 267 the void fraction are always below 35% in all our experiments. On another hand, these corrections 268 consider that the dynamic pressure collected from pitot or pavlov tubes in two-phase flows is 269 associated with the density and the velocity of the mixture. However, in bubbly flows, the orifices of 270 pitot or pavlov tubes are always wetted, meaning that the gas phase is never detected as such. 271 Therefore, the local stopping pressure detected with such sensors provides a measure of the local 272 liquid velocity even when the sensor is in the vicinity of a bubble, and no correction is required. All 273 Pavlov tube measurements presented hereafter are grounded on eq.(6).

The radial profiles are easily obtained by moving the measuring cell along the column radius. The axial velocity fluctuations can be calculated through the instantaneous and the averaged velocity, using Reynolds decomposition, as presented in the following equation.

278
$$U(x,t) = U(x) + u'(x,t)$$
 (7)

```
where U(x) represents the mean liquid velocity, u'(x,t) represents the liquid fluctuation velocity
at the instant t and U(x,t) represents the liquid velocity at the instant t.
```

282

283 4. Results

Thereafter, the discussion focuses on the heterogeneous regime. On all columns, one can observe in Figure 4, that the almost linear behaviour of $\langle \alpha_G \rangle$ with Vsg is observed only below 4-5cm/s, approximately. This value corresponds to the transition to the heterogeneous regime.

287 4.1. Gas holdup

Global gas volume fractions have been measured for all columns and Vsg. Radial gas holdup profiles have been measured with the optical probes at H/D=2.5 (Figure 4). Schweitzer et al. (2001) found similar profiles of $\alpha_G(x)$ when normalized by the average gas holdup in the column $\langle \alpha_G \rangle$. Authors suggest the correlation reported in eq.(8) to represent holdup profiles. The correlation has been initially developed and validated in a 50mm inner diameter column for Vsg between 0.03 to 0.25m/s. Its range of validity has been extended by Forret et al. (2006) to columns up to 1m of inner diameter.

295
$$\alpha_G(x) = \langle \alpha_G \rangle [-1.638(x^6 - 1) + 1.228(x^4 - 1) - 0.939(x^2 - 1)]$$
 (8)

296

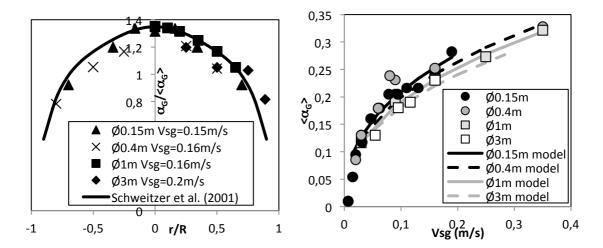
On Figure 4 (left), unsurprisingly it is verified that gas holdup follows the same profile at any scale, with an average error below 5%. Concerning the average gas holdup, keeping in mind that the liquid elevation measurement method eq.(1) is relatively imprecise (+/- 10%), different correlations validated in air/water systems may be found in acceptable agreement with present experimental data. As the gas holdups have been measured with the same technique and using the same water, experimental data have been used to fit a new correlation in the aim to extract the specific effect of scale up in the heterogeneous regime. Remember that existing models have been generally 304 developed based on a single column diameter, generally lower than 0.4m. The following correlation 305 has be found to predict $\langle \alpha_G \rangle$ with an error below 6% when Vsg > 0.1m/s:

306

307
$$\langle \alpha_G \rangle = 0.49. V sg^{0.41}. D^{-0.047}$$
 (9)

308

309 Measured and predicted average gas holdups are compared in Figure 4 (right). Only experiments 310 corresponding to Vsg >0.05 m/s are considered to fit eq.(9), given that gas holdup is proportional to 311 Vsg in the homogeneous regime. It is observed a small, but not negligible effect of the column diameter on the gas holdup, especially in intermediate range of Vsg, between 0.1 and 0.2 m/s. 312 313 Although most of existing correlations do not include the effect of D (Kantarci et al., 2005), the question of the impact of the column diameter on the gas holdup is still not completely settled as 314 315 notably discussed by Rollbush et al. (2015). Additional experiments may although be necessary at higher D to confirm this trend, as at high Vsg measurements in 0.4 and 1m diameters are relatively 316 317 close. Alternatively the eq. (9) can be replaced by an equation involving only Vsg with an exponent of 318 0.41 and a prefactor of 0.5 instead of 0.49, with a mean error of 8%.



319 320

Figure 4: Gas holdup profiles at H/D=2.5, normalized by the average gas holdup (left), and average gas holdup measurements (right). Comparison with correlations (eq. 8&9).

322

323 4.2. Liquid velocity

In a similar manner, Forret et al. (2006) suggested to normalize axial liquid average velocity profiles by the liquid velocity at the center U₀, and found a good agreement with the following polynomial model:

327

328
$$U(x) = \frac{U_0}{a-c} [a.\exp(-b.x^2) - c]$$
(10)

329

With a=2.976, b=0.943, c=1.848. The eq. (10) has been compared to the present experimental measurements of U(x), and a very good agreement has been found, except in the largest column where the magnitude of the liquid velocity close to the walls is slightly underestimated by the model. The comparison between U(x)/U₀ and eq.(10) are reported in Figure 5. The liquid velocity at the center can also be correlated with Vsg and D. The equation (11) presents the result of the regression, which predicts U₀ with an average error below 8%:

336

337
$$U_0 = 1.35. Vsg^{0.16}. D^{0.40}$$
 (11)

338

339 Figure 6 (left) presents the parity diagram between eq.(11) and experimental measurements in 340 different columns. In Figure 6 (right), experimental results are also compared to a short selection of 341 existing correlations of Miyauchi & Shyu (1970), Riquarts (1981), Nottenkämper (1983) and Zehner 342 (1986). In this figure, each experimental centreline velocity, reported in abscissa, is compared to the 343 velocity given by the different listed correlations, including eq.11, at the same operating Vsg and D, 344 which are reported in ordinate. This comparison shows that our experiments are in good agreement 345 with previous works of Miyauchi & Shyu (1970) and Nottenkämper (1983), but not with others, 346 pointing out the disparity of experimental results obtained in different laboratories. This disparity can 347 have different origins, as the different measurement methods, different quality of water, different

gas sparging conditions or different column sizes. The present study allows to eliminate the 3 firstpossibilities.

While the exponent on D in eq. (11) is quite classical – in the range of 0.3-0.7, the exponent on Vsg can be considered lower than generally observed (0.3-0.5). This later result may be a consequence of the quality of water, which partially prevents coalescence when compared with non-contaminated water, resulting in a less pronounced heterogeneity of bubble sizes and possibly a lower liquid recirculation as suggested by Rollbusch et al. (2015). Thus, from the above results, it happens that the flows in bubble column operated in the heterogeneous regime self-organise, leading to selfsimilar radial profiles for the void fraction and for the mean liquid velocities.

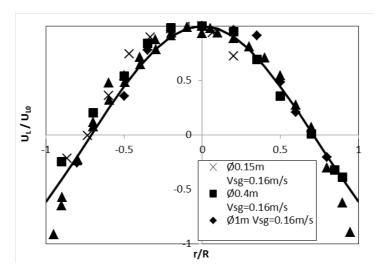


Figure 5: Normalized liquid velocity profiles (left) and comparison between the axial average liquid velocity at the center
 U₀ and eq.(11).

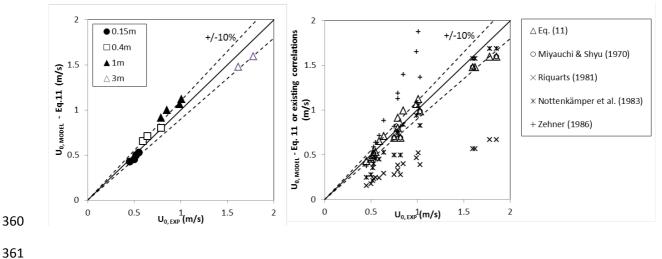




Figure 6: Centre-line velocity parity diagram of eq.11 (left) ; parity diagram of different correlations (right)

364

Besides, a well-known behaviour concerning the liquid velocity profile is observed: the section of the columns can be divided into two surfaces of equal area: the core region when $r < \frac{\sqrt{2}}{4}D$ or x<0.71, where U is positive, and the external region where U is negative. In the core region, the liquid upward flux can be calculated as:

369

370
$$Q_{L,up} = \int_0^{\frac{\sqrt{2}}{4}D} 2\pi . r. (1 - \alpha_G) . U(r) . dr$$
(12)

371

The calculated liquid upward flux for three Vsg and for all the investigated columns are reported in Figure . The liquid upward flux surprisingly happens to be independent of the superficial gas velocity in the heterogeneous regime. Results correlates very well with $\propto D^{2,5}$, implying that the average liquid velocity in the core region follows a trend $\propto \sqrt{D}$. One possible explanation of that could be the predominant role of the natural velocity scale \sqrt{gD} . If we define a Froude number based on the mean liquid velocity in the core region of section S_{core} (= $\pi D^2/8$), a constant value of the Froude number is observed:

379

$$380 \qquad Fr = \frac{Q_{L,up}}{S_{core}\sqrt{gD}} \approx 0.024 \tag{13}$$

381

This result also illustrates the close link between liquid volume fraction and velocity profiles, as both change with the gas flow rate but not their mutual product. The above velocity scaling and the observed flow organisation are reminiscent of free thermal convection in pipes for which the natural scale for velocity has been shown to be the free fall velocity under buoyancy acceleration evaluated for a length scale equal to the pipe diameter (Tisserand et al., 2010, Rusaouen et al., 2014).

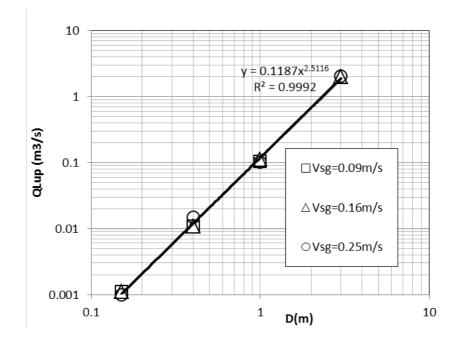


Figure 7: Liquid upward flux in the core region as a function of the bubble column diameter for the heterogeneous
 regime.

388

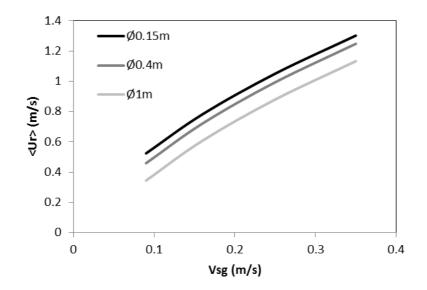
392 Relative velocity

393 In the core region, the mean flow is directed upward and it is thus similar to a co-current upward 394 two-phase flow. According to classical kinematic approaches (e.g. Zuber and Findlay 1965), the 395 difference between the gas flow rate fraction defined as the volumetric gas flow divided by the sum 396 of liquid and gas volumetric flow rates and the void fraction is controlled by the relative velocity 397 between phases. In the same spirit, let us introduce the apparent (in the sense that it is a global 398 quantity at the scale of the core region of the column and not a local one) relative velocity between 399 gas and liquid <Ur> in the core region as the difference of mean velocities between gas and liquid in 400 the core section. Each mean velocity is calculated as the phasic volumetric flow rate divided by the 401 associated cross section, i.e. the core section multiplied by the volume fraction of the concerned 402 phase in this section:

403

$$404 \qquad \langle Ur \rangle = \frac{Q_{G,core}}{\langle \alpha_G \rangle_{core} \cdot S_{core}} - \frac{Q_{L,up}}{(1 - \langle \alpha_G \rangle_{core}) \cdot S_{core}} \tag{14}$$

406 Where $Q_{G,core}$ is the gas flow rate in the core region, $Q_{L,core}$ the liquid flow rate in the core region is 407 given by (eq.(13) and $\langle \alpha_G \rangle_{core}$ is computed from eq. (8) and is found \approx 1.33 $\langle \alpha_G \rangle$. $Q_{G,core}$ can be 408 roughly estimated by the total gas flow rate Q_G . Note that this approximation tends to minimize the estimation of the relative velocity as the recirculation of a part of the bubbles is not taken into 409 account. The estimation of relative velocities are reported in Figure 8 for Vsg > 0.09m/s and for three 410 411 columns. The relative velocity increases with Vsg and achieves values that are much higher than the terminal bubble velocity (≈ 0.22 m/s). Such an increase in the bubble relative velocity in the 412 413 heterogeneous regime has been evoked by Ruzicka (2013). Possible origin of this phenomenon is 414 discussed below.



415

Figure 8: Estimation of the relative velocity in the core region, considering that the gas flow rate in the core region equals the totality (Ur max) or the half (Ur min) of the total gas flow rate.

418

419 Fluctuating velocity

RMS of axial liquid velocity fluctuations (u') have been measured in various operating conditions.
Results presented in Figure 9 (left) point out that u' radial profiles also follow self-similar profiles. The
following polynomial function has been regressed in eq. (15) and is also reported in Figure 9 (left) to
illustrate the self-similarity of profiles.

425
$$u'(x) = u'(0.71) [a + bx^2 + cx^4 + dx^6]$$
 (15)

With a=0.48, b=2.25, c=-2.6, d=0.40. The normalization of the u' profiles can be done whatever the position of reference (x) but it has been found that using the maximal u' value minimizes the error of residues of the regression. The maximal value of u' is always located at the boundary between positive and negative liquid velocities ($x = \sqrt{2}/2 \approx 0.71$). When comparing u'_{max} at different scales, it is found proportional to U₀. As a consequence, the maximal u' value can be written as follows:

432

433
$$u'(x = \sqrt{2}/2) = u'_{max} = 0.695 U_0$$
 (16)

434

435 u'_{max} is reported in Figure 9 (right) for the different columns. The experimental data of Menzel et al.
436 (1990) using a hot wire probe is also reported on the same figure. The consistency between the
437 values measured with different techniques confirms the reliability of Pavlov tube measurements
438 concerning axial liquid velocity fluctuations. Note that in the core region, the liquid fluctuations are
439 about half their maximum, corresponding to a turbulent intensity u'/Uo about 25-30%. Hence, large
440 velocity fluctuations are present over the entire cross-section at all flow conditions: that feature is a
441 clear characteristic of the heterogeneous regime.



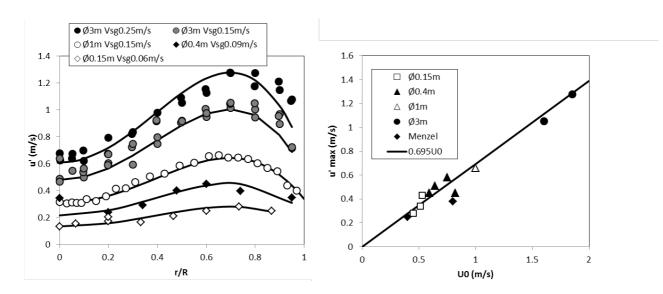


Figure 9: u' radial profiles (left) and correlation between u'(x=0,71) and U₀ (right).

445

446 4.3. Bubble diameters

Sauter mean diameters measured with the cross-correlation technique are reported in Figure 10. On the left, bubble Sauter diameter (d32) profiles are reported at a given Vsg. On the right, volume average Sauter diameters <d32> for the 4 columns are given as a function of Vsg. <d32> is computed as the gas-volume averaged Sauter diameter over column sections. Let us recall that, in the up-flow region, the typical relative uncertainty on the Sauter diameter is less than 10% for the large superficial velocities considered here (Maximiano Raimundo et al., 2016). Important results can be summarized as follows:

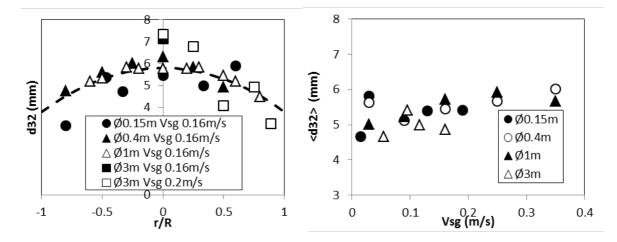
454 • The mean bubble diameter increases slowly from ≈4.5 - 5 mm at low Vsg to 5.5-6mm at high
 455 Vsg

• The mean bubble diameter is almost insensitive to the column diameter,

Bubble size profiles follow roughly a parabolic shape, as suggested by the parabolic function
 (y=5.8-2x²) reported in Figure 10.

Bigger bubbles are measured at the center of the column, and the bubble size decreases with
 x typically by 1 to 2mm indicating that a small amount of spatial segregation between upflow
 and downflow regions occurs in these flows.

In all our experiments, the terminal velocity of the average bubbles varies over a limited range (0.21-0.23m/s in clean water), and the bubbles always pertain to the same regime i.e. ellipsoids at high particulate Reynolds number (the latter ranges between 950 and 1300) experiencing wobbling (Clift et al., 1978). Hence, the present database has been built-up for nearly the same mean bubble size irrespective of the dimension of the bubble column and of the amount of gas injected.



467

468 469

Figure 10: Sauter diameter profiles in the 4 columns (right) and volume average Sauter diameter for the 4 columns versus Vsg. (H/D=2.5 except in the 3m column where H/D=2).

As the mean bubble size does not exhibit strong variations for Vsg in the range of 0.03 to 0.35 m/s, this quantity does not explain by itself the transition between the homogeneous and the heterogeneous regime. Further investigation based on bubble size distributions may be required to identify a presumed link between coalescence phenomena and flow regime transition as suggested and reviewed by Besagni and Inzoli (2017b).

476

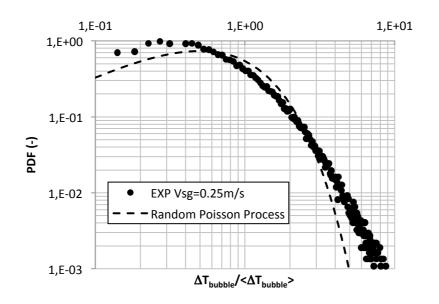
477 4.4. Discussion

478 Bubble size measurements suggest information concerning turbulence. Classical population balance 479 kernels (Buffo et al., 2013) use the dissipation rate (ε) as a major parameter to predict breakage and coalescence. ε can classically be written as ~ u'^3/Λ , Λ being a turbulence macroscale. Besides, the 480 global dissipation rate inside bubble columns can be estimated via different ways, but it is generally 481 considered as not depending on the column diameter (Deckwer, 1992; Roels and Heijnen, 1980). 482 Indeed in bubble columns ε is usually calculated as $g.(\rho_L - \rho_G)/\rho_L.Vsg$. The observed almost 483 constant bubble size with scale-up is consistent with this theory. In the present study u' has been 484 found to follow ~ $D^{0,4}$, this implies that Λ increases during scale up as ~ $D^{1,2}$, let say ~ D, which makes 485 sense from a pure geometrical consideration. Further investigations concerning the size of 486 487 turbulence macroscales in bubble columns may be useful to understand the link between flow

structures and turbulence production, as well as with breakage and coalescence phenomena. 488 489 Concerning velocity scales, the above discussion on the apparent relative velocity indicates that the terminal velocity of bubbles is not the most relevant scale in these buoyancy driven bubbly flows. 490 491 Indeed, a natural velocity scale (gD)^{0.5} arises from the analysis of the entrained liquid flow rate in the 492 central portion of the column. Such a scale is reminiscent of turbulent flows driven by convection. In 493 buoyancy driven flows such as in thermal convection, the equilibrium between flow convection and Archimedian forcing leads to a velocity scaling as $V^2 \approx gL\Delta\rho/\rho$, where the density gradient $\Delta\rho$ is 494 495 evaluated at the length scale L. L is tentatively taken here as the column diameter. That choice is 496 supported here by the fact that we are considering the fully developed region, and, as the flow 497 happens to be self-similar in that zone, the height of the column is no longer a relevant parameter.

In addition to these large-scale gradients, localised variations in the density of the gas-liquid mixture, equivalent then to variations in the local gas concentration, can also arise. Indeed, dispersed twophase flows can be prone to the formation of clusters, and Voronoï tessellations that are an efficient way to detect and characterise such clusters (Monchaux et al., 2012) have been exploited here.

502 In the present experiments, we exploited the signals delivered by optical probes that provide the 503 arrival time of bubbles. From such a time history, it is straightforward to define successive Voronoï 504 time intervals ΔT_{bubble} containing a single bubble centred into it. Figure 11 provides the statistics 505 gathered on the axis of the 1m I.D. column at Vsg =25cm/s: the data correspond to a record of 600 506 seconds during which 85000 bubbles have been detected. The abscissa in Figure 11 is the time 507 interval ΔT_{bubble} normalised by the mean value $\langle \Delta T_{bubble} \rangle$. The quantity $\Delta T_{bubble} / \langle \Delta T_{bubble} \rangle$ represents 508 the inverse of the ratio of the local and instantaneous gas concentration to the average gas hold-up. 509 Clearly, the measured probability density function differs from that of a random Poisson process 510 referred to as RPP in the sequel (Ferenc and Néda, 2007). In particular, the probability to found small 511 time intervals ΔT_{bubble} , below 0.6 < ΔT_{bubble} >, is higher than in RPP indicating that clusters (i.e. regions 512 where bubbles accumulate) are more probable than in a random process. Similarly, the probability to 513 found large time intervals ΔT_{bubble} , above 4 < ΔT_{bubble} , is higher than in RPP indicating that voids (i.e. 514 regions with few bubbles) are also more probable than in RPP. This demonstrates that clusters and 515 voids are indeed present in the heterogeneous regime (this behaviour holds for others columns size 516 and superficial velocities). Moreover, that plot indicates that local, instantaneous concentrations 517 evolve between 0.1 and 10 times the average gas holdup. Local, instantaneous concentrations 518 varying over a so wide range imply quite strong fluctuations in density and thus in buoyancy. 519 Therefore, one expects strong local velocity differences between dense and dilute regions. The latter 520 can contribute to enhance the apparent relative velocity between phases as the bubbles are mostly 521 located in clusters while the liquid in mostly present in voids. This may explain the large apparent 522 relative velocity detected since the bubble terminal velocity in a still fluid is no longer the relevant 523 scale. Such structures are also prone to contribute to turbulence production as they produce strong 524 local and instantaneous shear rates. The velocity fluctuations shown in Figure 9 combined with the 525 correlation (13) support that statement. Finally, if one sticks to the mean values of bubble sizes, the 526 transition between homogeneous and heterogeneous regimes observed in the present experiments 527 is not related with coalescence; instead, convective instabilities that lead to the formation of dense 528 and dilute regions are believed to be responsible for that transition. To pursue along these lines, it 529 would be worthwhile to characterise these clusters and voids in terms of gas holdup and size 530 distributions and to examine how they evolve with flow conditions and column diameter. Another 531 key issue is how to quantitatively relate these clusters and voids with the apparent relative motion 532 between phases and with the turbulence production in the liquid phase. In particular it would be 533 relevant to examine the connections between clusters and void dimensions and the correlation 534 length scale Λ discussed above.



536 Figure 11: Voronoï diagram deduced from an optical probe signal collected in the centre of the 1m diameter column 537 operated at Vsg =25cm/s (dots). The dashed line represents the statistics of a Random Poisson Process.

538

539 5. Conclusions

540 The objective of this work was to study specifically the scale-up of bubble columns in the heterogeneous regime using similar fluids and the same measurement techniques at very different 541 542 scales, which has never been reported before in literature. The wide range of column diameter, from 543 0.15 to 3m and of superficial gas velocities, from 0.05m/s to 0.35m/s, involved in this study makes 544 the reported data an important material for validation of Population Balance and CFD models and for 545 up-scaling issues. Correlations concerning gas holdup, mean liquid velocity and turbulence have been 546 validated over a wide range of geometry and operating conditions. In particular, the self-similarity of 547 the flow structure in terms of void fraction, liquid mean as well as fluctuating velocities have been demonstrated in the heterogeneous regime. This is believed to hold while the aspect ratio of the 548 549 bubble column remains large enough so that end effects no longer affect the flow organisation in the 550 central portion of the column. That self-similarity leads to an entrained liquid flow rate proportional to $D^{2}(gD)^{1/2}$, meaning that the entrainment capability of a bubble column is only set by its size and 551 552 does not depend on the injected gas superficial velocity. This result also demonstrates that the velocity scale $(gD)^{1/2}$ is a key descriptor for bubble column scale-up. Also, both the average and the 553

554 fluctuations of the liquid velocity are very sensitive to the scale-up. Small dependencies to the 555 column diameter have been found on local and global gas holdup. The above results hold for all 556 columns and flow conditions pertaining to the heterogeneous regime, and for almost the same 557 average Sauter bubble diameters. The presence of strong concentration gradients has also been 558 demonstrated, and the impact of these clusters and voids on the flow characteristics and on 559 turbulence production deserves to be analysed further. As the turbulent dissipation rate plays an 560 important role on the BSD, the turbulence induced in the heterogeneous regime needs to be better 561 characterised in particular by determining its integral length scale.

562

563 Abbreviations

564	d	distance between probes (m or mm)
565	d ₃₂	Local mean Sauter diameter (m or mm)
566	<d<sub>32></d<sub>	volume averaged mean Sauter diameter (m or mm)
567	d _{32,h}	Local mean Sauter horizontal diameter (m or mm)
568	СС	cross-correlation
569	D	Column diameter (m)
570	есс	bubble eccentricity
571	Н	height from gas distributor (m)
572	H ₀	static (non aerated) liquid height (m)
573	H_D	aerated liquid height (m)
574	\mathbf{Q}_{G}	gas flow rate (m ³ /s)
575	$\mathbf{Q}_{G,core}$	gas flow rate in the core region(m ³ /s)
576	Q _{L,up}	Upward liquid flow rate in the core region (m ³ /s)
577	r	Radial position (m)
578	R	radius of the column (m)
579	Sc	Section of the core region (m ²)

580	U(x,t) Liquid axial instantaneous velocity (m/s)		
581	U(x,t) Liquid axial average velocity (m/s)		
582	U_0	Liquid axial velocity at the center of the column (m/s)	
583	Ur	Relative velocity between gas and liquid (m/s)	
584	u'	RMS of liquid axial velocity fluctuation (m/s)	
585	Vsg	Superficial gas velocity (m/s)	
586	x	normalized radial position (=2r/D)	
587	Symbo	bls	
588	α_{G}	Local gas holdup	
589	<a_g></a_g>	Average gas holdup	
590	ε	Turbulence dissipation rate (w/kg)	
591	Λ	Turbulence macroscale (m)	
592	ρ	Liquid density (kg/m³)	

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