

# **On the complementarity between resistivity measurement and ultrasonic measurement for in-situ characterization of phase transitions in Ti-alloys**

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## **To cite this version:**

Jitka Nejezchlebová, Hanuš Seiner, Petr Sedlák, Michal Landa, Jana Šmilauerová, et al.. On the complementarity between resistivity measurement and ultrasonic measurement for in-situ characterization of phase transitions in Ti-alloys. Journal of Alloys and Compounds, 2018, 762, pp.868-872. 10.1016/j.jallcom.2018.05.173 . hal-01985979

# **HAL Id: hal-01985979 <https://hal.science/hal-01985979v1>**

Submitted on 18 Jan 2019

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## **To cite this version:**

Nejezchlebová, Jitka and Seiner, Hanuš and Sedlák, Petr and Landa, Michal and Šmilauerová, Jana and Aeby-Gautier, Elisabeth and Denand, Benoît and Dehmas, Moukran[e](http://www.idref.fr/083540644)<sup>-••</sup> and Appolaire, Benoît *On the complementarity between resistivity measurement and ultrasonic measurement for in-situ characterization of phase transitions in Ti-alloys.* (2018) Journal of Alloys and Compounds, 762. 868-872. ISSN 0925-8388

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## On the complementarity between resistivity measurement and ultrasonic measurement for in-situ characterization of phase transitions in Ti-alloys

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a r t i c l e i n f o

*Keywords:* Metals and alloys Elasticity **Ultrasonics** Phase transitions

We present the results of in-situ characterization of the phase transitions in metastable  $\beta$ -Ti alloy Ti5553 by contactless laser-based resonant ultrasound spectroscopy method and electrical resistance measurement in a four probe configuration. Phase transformations were studied during continuous heating from the room temperature to 700  $\mathrm{C}$  with various heating rates. We showed that both methods provide complementary results and can be successfully used for observation of phase transitions in metastable  $\beta$ -Ti alloys.

#### 1. Introduction

Mechanical properties of metastable  $\beta$ -Ti alloys are strongly dependent on the microstructure which in turn arises from different thermomechanical treatment. High variability of possible microstructure and low density result in a wide applicability of this class of alloys, ranging from orthopedic implants to the structural parts of aircrafts [1]. For this reason, it is crucial to have a reliable technique for the in-situ characterization of phase transitions and their kinetics in the material during thermo-mechanical treatment.

This study is focused on the Ti5553 alloy which belongs to the class of metastable  $\beta$ -Ti alloys and exhibits various solid-solid phase transformations. Nano-sized particles of athermal  $\omega$  phase  $(\omega_{\text{ath}})$ form by diffusionless shuffle transformation during quenching from the temperatures above  $\beta$ -transus temperature. Upon subsequent heating, the particles of isothermal  $(\omega_{iso})$  phase are

\* Corresponding author. *E-mail address:* jitkanej@it.cas.cz (J. Nejezchlebova). ! chemically stabilized by the diffusion of  $\beta$ -stabilizing elements into the surrounding matrix [2]. At higher temperatures,  $\omega_{iso}$  particles serve as nucleation sites for precipitation of finely dispersed particles of  $\alpha$  phase [3–6]. The creation of  $\alpha$  phase can be preceded by formation of orthorhombic  $\alpha''$  phase which existence was also observed in Ti5553 alloy [7,8]. During further heating, the  $\alpha$  phase gradually dissolves and the whole material is transformed into pure  $\beta$  phase at temperatures above  $\beta$ -transus temperature.

Measurement of electrical resistance is one of the most frequently used methods for in-situ observation of phase transformations in metastable  $\beta$ -Ti alloys. This method is well established for the study of kinetics of diffusion-driven formation of  $\omega_{iso}$ particles [9] and it is successfully used for investigation of phase transitions during continuous heating of Ti15Mo [10], TIMETAL LCB [11,12], Ti12Mo [13],  $\beta$ -Cez alloy [14] and Ti6Mo5Ta4Fe [15].

Another techniques used for in-situ study of phase transitions are small angle neutron scattering [16] or high energy synchrotron x-ray diffraction (SXRD)  $[17-19]$ . The advantage of the SXRD method is the possibility of evaluation of volume fractions of individual phases. Bruneseaux et al. [20] and Settefrati et al. [7,21]

proved a good complementarity of electrical resistance and SXRD measurement of transformation kinetics.

Further options of in-situ techniques are dilatometry [13,22] or differential scanning calorimetry [23]. The in-situ techniques can be complemented by post-mortem investigation such as metallography or hardness measurement to obtain a deeper insight into the mechanisms of phase transformations.

The aim of this study is to compare the applicability of electrical resistance measurement with resonant ultrasound spectroscopy (RUS) [24,25] for investigation of phase transformations kinetics in a selected metastable  $\beta$ -Ti alloy. Recently, RUS was utilized for insitu observation of the influence of  $\omega$  phase on the elasticity of TIMETAL LCB alloy [26]. It was shown that the high sensitivity of this method enables examination of formation and growth of  $\omega_{\alpha\beta}$ particles that is quite difficult to observe by previously mentioned conventional techniques. Furthermore, post-mortem study by RUS of TIMETAL LCB and Ti15Mo alloys after plastic deformation by high pressure torsion proved the occurrence of deformation-induced  $\omega$ phase [27].

### 2. Material and methods

The experiments were carried out on the titanium alloy Ti5553 (Ti-5Al-5Mo-5V-3Cr wt. %). The alloy was produced by VSPMO and provided to Institut Jean Lamour within the PROMITI project. The  $\beta$ transus temperature of this alloy was 845 °C [21]. The alloy in the as-received state had a duplex microstructure  $-$  i. e. consisting of equiaxed  $\alpha$ -particles (so-called primary  $\alpha$ ) and a mixture of lamellar  $\alpha$  plates surrounded by some remaining  $\beta$  matrix. Afterwards, two initial states of microstructure were prepared. The specimens were either  $\beta$  solution treated at 890 °C or heat treated at 800 $\degree$ C (below the  $\beta$ -transus temperature). In both cases, the treatment was terminated after 30 min by quenching to room temperature in helium gas. After the solution treatment, the microstructure at room temperature consisted of metastable  $\beta$ matrix with finely dispersed particles of  $\omega_{\text{ath}}$  particles. The heat treatment below the  $\beta$  transus resulted in 15 % of equiaxed  $\alpha$  phase and only 85 % of metastable  $\beta$  phase [7].

Samples for RUS and electrical resistance measurements were prepared from both above described initial states of the material. Samples for RUS measurement, one from each initial condition, had a cylindrical shape with 4 mm diameter and 2.23 mm height. Four samples from the '890  $\degree$ C/30 min' state and one from the '800  $\degree$ C/ 30 min' state were prepared for electrical resistance measurement. They had also cylindrical shapes with 4 mm diameter and 40 mm height. All samples were subsequently studied in-situ by the two aforementioned methods in the temperature range from room temperature to  $700$   $^{\circ}$ C.

The temperature evolution of resonant spectra of samples was recorded by RUS using fully contactless laser-based RUS set-up described in detail in Ref. [28]. The vibrations of the examined sample were generated by focused laser pulses and the modal response was detected by a laser vibrometer. The measured specimen was placed in a temperature chamber filled with lowpressure nitrogen atmosphere that enabled its temperature control. The average heating rate of both samples, '890 $\degree$ C/30 min' and '800 °C/30 min', was 1.9 °C/min.

As discussed in Ref. [29], RUS resonant spectra carry mainly information on shear elastic constants (i.e. shear modulus *G* in case of isotropic material). Therefore, the elastic constants related to longitudinal motion of the material (volumetric changes, unidirectional tension/compression) cannot be determined from resonant spectra with sufficient accuracy. For this reason, only temperature dependences of shear modulus *G* were evaluated from the measured resonant spectra by iterative inverse procedure that

is described in detail in Refs. [24,30].

Electrical resistance of all samples was measured by an in-house built dilatometer using a four-point configuration that allows simultaneous measurement of voltage and electrical current. The temperature was controlled by S-thermocouple spot-welded on the surface of the specimen. For the samples '890 $\degree$ C/30 min', four different heating rates were chosen  $1.4 \degree C/min$ ,  $1.9 \degree C/min$ ,  $3.9 \degree C/m$ min and  $6 °C$ /min. In case of the sample '800  $°C/30$  min', the heating rate of  $1.9 \degree$ C/min was used.

RUS and electrical resistance measurement can be expected to bring slightly different but mutually complementary information on the processes taking place in the material. While electrical resistance measurements are sensitive both to the phase composition of the material and to the number and the structure of interfaces due to scattering of conduction electrons, the RUS data can be assumed as dominantly sensitive only to the volume fractions of individual phases. Hence, RUS results may help to separate the effect of the phase composition and the effect of the interfaces for the electrical resistance measurements.

### 3. Results and discussion

If the thermal expansion of the sample is neglected, the relative electrical resistance  $R/R<sub>0</sub>$  is equal to the relative electrical resistivity  $\rho/\rho_0$  ( $\rho=(RS)/l$ ), where *R* and  $\rho$  are immediate resistance and resistivity,  $R_0$  and  $\rho_0$  are resistance and resistivity measured at initial temperature, *S* is the cross-sectional area of the specimen and *l* is the length of the specimen.

The temperature dependence of relative resistivity of samples '890 °C/30 min' (relative resistivity =  $(\rho - \rho_0)/\rho_0$ , where  $\rho_0$  is the resistivity measured at initial temperature  $66 \degree C$ ) is shown in Fig. 1. It is obvious that the shape of the relative resistivity curves is strongly dependent on the heating rate.

The decrease of relative electrical resistivity that is observed at the beginning of heating for all heating rates is attributed to the combination of anomalous behavior of  $\beta$  phase due to the phonon softening and vanishing of the particles of  $\omega_{\text{ath}}$  phase [10,12,31,32]. Reduction of  $\beta/\omega_{ath}$  interfaces and related stress fields results in a drop of conduction electron scattering and therefore to the decline of relative resistivity.

The change of the slope of the decrease can be seen around 220 $\degree$ C. The small peaks that are visible around this temperature for all heating rates are results of diffusion-driven formation of particles of  $\omega_{i\alpha}$  phase. As temperature increases, the precipitation of  $\alpha$ /  $\alpha^{''}$  phases occurs, while the  $\omega_{\rm iso}$  particles dissolve. The formation of  $\alpha/\alpha^{''}$  phase is visible on the relative resistivity curves as a sharp increase. However, both the position and shape of these peaks depend strongly on the heating rate; for the lowest heating rate  $(1.4 \degree C/min)$ , the peak is sharper and located to lower temperatures ( $\sim$  400 °C), while for the highest studied heating rate (6 °C/min), it is broader and located to higher temperatures ( $\sim$  500 °C). The difference in the position of this peak is clearly caused by the diffusion-driven mechanism of the formation of  $\omega_{\rm iso}$  and of  $\alpha/\alpha''$ phases; i.e. at lower heating rates new phases have longer time for nucleation and growth.

Comparison of the evolution of resistivity and elasticity of sample '890 $\degree$ C/30 min' is plotted in Fig. 2. As it can be seen, variations of shear modulus present two distinctive peaks that are clearly associated with the formation of  $\omega_{\rm iso}$  phase and  $\alpha/\alpha^{''}.$  The shear modulus increase is caused by the higher shear modulus of the  $\omega_{\rm iso}$  phase and  $\alpha/\alpha''$  phase as compared to that of the  $\beta$  matrix, so their formation has well-detectable impact on the elastic properties of the whole material. The peaks of resistivity and shear modulus attributed to diffusional formation of  $\omega_{iso}$  phase are approximately located at the same temperature. Nevertheless, the



Fig. 1. Temperature dependence of relative resistivity of samples '890 °C/30 min' during various heating rates  $-1.4$  °C/min, 1.9 °C/min, 3.9 °C/min and 6 °C/min. The peaks corresponding to formation of  $\omega_{\rm iso}$  and  $\alpha/\alpha^{''}$  phases are marked.

peak corresponding to  $\alpha/\alpha''$  formation is shifted to a higher temperature by approximately  $80^{\circ}$ C in RUS data. It can be observed that the temperature for which there is a peak of relative resistivity coincides with the largest variation of the shear modulus. This agrees well with the assumption that the relative resistivity evolution with temperature is dependent not only on the phase composition (i.e. volume fraction of the  $\alpha/\alpha^{''}$  phase), but also on the number and effective cross-section of the interfaces between the  $\beta$ matrix and the  $\alpha$  particles, as these parameters are probably the highest somewhere in the middle of the transition process.

However, some part of this discrepancy could be also explained by the different way of temperature regulation of the experimental techniques. The temperature during electrical resistance measurement was measured by a thermocouple that was directly spotwelded on the specimen surface. The temperature was controlled by a PID regulator with four halogen lamps that were source of thermal radiation. This way of temperature regulation enabled rapid and precise control of temperature. As the loop time was equal to 10 ms, the time evolution of temperature during resistivity measurement was nearly linear. In contrast, the temperature of the

sample during the RUS measurement was regulated via the nitrogen atmosphere by thermal conduction. This manner of temperature control was slower and the used heating rate of  $1.9 \degree C/min$  was in fact an average rate; during the RUS measurement the dependence of temperature had a 'staircase' shape (heating to desired temperature and stabilization at this temperature). Formation of  $\omega_{iso}$  and  $\alpha/\alpha''$  phases could be very sensitive to this difference because, as was shown in Fig. 1, even a slight change in the heating rate can significantly influence the kinetics of their formation. Such an interpretation is supported by the fact that the location of the shear modulus peak for  $\alpha/\alpha''$  phases from RUS measurements corresponds well to the resistivity peak for  $3.9 \degree C/\text{min}$ , as is also shown in Fig. 2. Nevertheless, in order to reliably separate the effect of the phase composition and the effect of the interfaces, it would be necessary to accompany the RUS and electrical resistance measurement by in-situ observations of the microstructure.

The complementarity of the RUS and electrical resistance measurement was also confirmed in case of sample '800 $\degree$ C/30 min' (see Fig. 3). The  $\beta \rightarrow \omega$  and  $\beta \rightarrow \alpha/\alpha''$  phase transformations were successfully detected by both methods. In the material heat treated



Fig. 2. Comparison of relative resistivity (black curve) and shear modulus *G* of samples '890 °C/30 min' during heating with heating rate 1.9 °C/min. For the purpose of comparison, the relative resistivity (grey curve) of the sample '890  $\degree$ C/30 min' with heating rate 3.9  $\degree$ C/min is also plotted.



Fig. 3. Evolution of relative resistivity and shear modulus *G* of samples '800 °C/30 min' during heating with heating rate 1.9 °C/min.

under the  $\beta$ -transus temperature, the formation of  $\omega_{iso}$  phase and  $\alpha/\alpha''$  phase takes place at higher temperatures in comparison with the '890 °C/30 min' sample that initially contained only  $\beta$  and  $\omega_{\alpha t}$ <sup>h</sup> phases. Similarly to sample '890 $\degree$ C/30 min', peaks of relative resistivity and shear modulus corresponding to  $\alpha/\alpha''$  do not coincide (the difference is roughly 40 $\degree$ C). Moreover, the shear modulus of the sample '800 $\degree$ C/30 min' in the initial state at room temperature is higher in comparison to the sample '890 $\degree$ C/30 min' due to the fraction of  $\alpha$  phase that causes stiffening of the whole material.

### 4. Conclusions

In summary, the results prove the complementarity of two experimental methods  $-$  resonant ultrasound spectroscopy and electrical resistance measurement. These methods were successfully utilized for the in-situ characterization of phase transformations of metastable  $\beta$ -Ti alloy Ti5553 during continuous heating from room temperature to  $700^{\circ}$ C. It was shown that the phase transitions in this alloy are strongly dependent on the heating rate. The temperature of  $\beta \rightarrow \omega$  phase transformation determined by both methods roughly correspond. In case of the temperature of  $\beta \rightarrow \alpha/\alpha$ <sup>"</sup> transformation, the shift of peaks was observed which can be explained by the difference in temperature regulation or by the different sensitivity to the composition and effective cross-section of interfaces.

#### Acknowledgments

The authors wish to dedicate this paper to Michal Landa, our colleague and friend who has passed away recently.

This work has been financially supported by the project of the Czech Science Foundation (17-04871S) and by ERDF, project No. CZ.02.1.01/0.0/0.0/15\_003/0000485. This work also received support from the French State through the program Investment in the future operated by the National Research Agency (ANR) and referenced by ANR-11-LABX-0008-01 (LabEx DAMAS).

#### References

- [1] C. Leyens, M. Peters, Titanium and Titanium Alloys: Fundamentals and Applications, Wiley, 2006, https://doi.org/10.1002/3527602119.
- [2] A. Devaraj, S. Nag, R. Srinivasan, R.E.A. Williams, S. Banerjee, R. Banerjee, H.L. Fraser, Experimental evidence of concurrent compositional and structural instabilities leading to  $\omega$  precipitation in titaniummolybdenum alloys. Acta Mater. 60 (2012) 596-609, https://doi.org/10.1016/j.actamat.2011.10.008.
- [3] F. Prima, P. Vermaut, G. Texier, D. Ansel, T. Gloriant, Evidence of  $\alpha$ -nanophase heterogeneous nucleation from  $\omega$  particles in a  $\beta$ -metastable Ti-based alloy by high-resolution electron microscopy, Scr. Mater. 54 (2006) 645-648, https:// doi.org/10.1016/j.scriptamat.2005.10.024.
- [4] S. Nag, R. Banerjee, R. Srinivasan, J.Y. Hwang, M. Harper, H.L. Fraser, u-Assisted nucleation and growth of  $\alpha$  precipitates in the Ti5Al5Mo5V3Cr0.5Fe titanium alloy, Acta Mater. 57 (2009) 2136-2147, https://doi.org/10.1016/ j.actamat.2009.01.007.
- [5] B. He, X. Cheng, J. Li, G.-C. Li, H.-M. Wang,  $\omega$ -assisted  $\alpha$  phase and hardness of Ti-5Al-5Mo-5V-1Cr-1Fe during low temperature isothermal heat treatment after laser surface remelting, J. Alloys Compd. 708 (2017) 1054-1062, https:// doi.org/10.1016/J.JALLCOM.2017.03.089.
- [6] J. "Smilauerova, M. ! Jane"cek, P. Harcuba, J. Straský, J. Veselý, R. Ku ! "zel, H.J. Rack, Ageing response of sub-transus heat treated Ti6.8Mo4.5Fe1.5Al alloy, J. Alloys Compd. 724 (2017) 373-380, https://doi.org/10.1016/J.JALLCOM.2017.07.036.
- [7] A. Settefrati, E. Aeby-Gautier, M. Dehmas, G. Geandier, B. Appolaire, S. Audion, J. Delfosse, Precipitation in a near beta titanium alloy on ageing: influence of heating rate and chemical composition of the beta-metastable phase, Solid<br>State Phenom. 172–174 (2011) 760–765, https://doi.org/10.4028/ www.scientific.net/SSP.172-174.760.
- [8] E. Aeby-Gautier, A. Settefrati, F. Bruneseaux, B. Appolaire, B. Denand, M. Dehmas, G. Geandier, P. Boulet, Isothermal  $\alpha$ "formation in  $\beta$  metastable titanium alloys, J. Alloys Compd. 577 (2013) S439-S443, https://doi.org/<br>10.1016/j.jallcom.2012.02.046.
- [9] F. Prima, J. Debuigne, M. Boliveau, D. Ansel, Control of omega phase volume fraction precipitated in a beta titanium alloy: development of an experimental method, J. Mater. Sci. Lett. 19 (2000) 2219-2221, https://doi.org/10.1023/A: 1006708420478.
- [10] P. Zháňal, P. Harcuba, J. Šmilauerová, J. Strský, M. Janeček, B. Smola, M. Hájek, Phase Transformations in Ti-15Mo investigated by in situ electrical resistance, Acta Phys. Pol. A 128 (2015) 779-782, https://doi.org/10.12693/ APhysPolA.128.779.
- [11] J. Debuigne, F. Prima, Growth kinetic model for isothermal omega phase particles in low-cost beta titanium Ti6.8Mo4.5Fe1.5Al alloy, Mater. Trans. 46 .<br>(2005) 1433–1435, https://doi.org/10.2320/matertrans.46.1433.
- [12] F. Prima, P. Vermaut, D. Ansel, J. Debuigne,  $\omega$  precipitation in a beta metastable titanium alloy, resistometric study, Mater. Trans., JIM 41 (2000) 1092–1097,<br>https://doi.org/10.2320/matertrans1989.41.1092.
- [13] F. Sun, F. Prima, T. Gloriant, High-strength nanostructured Ti12Mo alloy from ductile metastable beta state precursor, Mater. Sci. Eng. A 527 (2010) 4262-4269, https://doi.org/10.1016/j.msea.2010.03.044
- [14] R. Sanguinetti, M. Zandona, A. Pianelli, E. Aeby-Gautier, Decomposition of  $\beta$ metastable phase in  $\beta$ -Cez alloy during continuous heating, J. Phys. IV 3 (1993) 527e531, https://doi.org/10.1051/jp4:1993785.
- [15] T. Gloriant, G. Texier, F. Sun, I. Thibon, F. Prima, J.L. Soubeyroux, Characterization of nanophase precipitation in a metastable  $\beta$  titanium-based alloy by electrical resistivity, dilatometry and neutron diffraction, Scr. Mater. 58 (2008) 271e274, https://doi.org/10.1016/j.scriptamat.2007.10.007. [16] J. Coakley, V.A. Vorontsov, K.C. Littrell, R.K. Heenan, M. Ohnuma, N.G. Jones,
- D. Dye, Nanoprecipitation in a beta-titanium alloy, J. Alloys Compd. 623<br>(2015) 146–156, https://doi.org/10.1016/J.JALLCOM.2014.10.038.
- [17] E. Aeby-Gautier, F. Bruneseaux, J. Da Costa Teixeira, B. Appolaire, G. Geandier, S. Denis, Microstructural formation in Ti Alloys: in-situ characterization of phase transformation kinetics, Jom J. Min. Met. Mat. S. 59 (2007) 54-58, https://doi.org/10.1007/s11837-007-0011-x.
- [18] P. Barriobero-Vila, G. Requena, S. Schwarz, F. Warchomicka, T. Buslaps, Influence of phase transformation kinetics on the formation of  $\alpha$  in a  $\beta$ -

quenched Ti5Al5Mo5V3Cr1Zr alloy, Acta Mater. 95 (2015) 90-101, https:// doi.org/10.1016/j.actamat.2015.05.008.

- [19] F. Bruneseaux, Apport de la diffraction des rayons X haute nergie sur les transformations de phases, application aux alliages de titane, PhD. Thesis, 2008, http://docnum.univ-lorraine.fr/public/INPL/2008\_BRUNESEAUX\_F.pdf.
- [20] F. Bruneseaux, E. Aeby-Gautier, G. Geandier, J. Da Costa Teixeira, B. Appolaire, P. Weisbecker, A. Mauro, In situ characterizations of phase transformations kinetics in the Ti17 titanium alloy by electrical resistivity and high temperature synchrotron X-ray diffraction, Mater. Sci. Eng. A 476 (2008) 60-68, https://doi.org/10.1016/j.msea.2007.04.072.
- [21] A. Settefrati, Etude exprimentale et modlisation par champ de phase de la formation de  $\alpha$  dans les alliages de titane -mtastable, PhD, thesis, 2012, http:// www.theses.fr/2012LORR0092/document.
- [22] F. Chen, G. Xu, X. Zhang, K. Zhou, Exploring the phase transformation in  $\beta$ quenched Ti-55531 alloy during continuous heating via dilatometric measurement, microstructure characterization, and diffusion analysis, Metall. Mater. Trans. A 47 (2016) 5383-5394, https://doi.org/10.1007/s11661-016-3714-1.
- [23] Q. Contrepois, M. Carton, J. Lecomte-Beckers, Characterization of the  $\beta$  phase decomposition in Ti-5Al-5Mo-5V-3Cr at slow heating rates, Open J. Met. 1 (2011) 1-11, https://doi.org/10.4236/ojmetal.2011.11001.
- [24] A. Migliori, J.L. Sarrao, W.M. Visscher, T.M. Bell, M. Lei, Z. Fisk, R.G. Leisure, Resonant ultrasound spectroscopic techniques for measurement of the elastic moduli of solids, Phys. B Condens. Matter 183 (1993) 1-24, https://doi.org/ 10.1016/0921-4526(93)90048-B.
- [25] A. Migliori, T.W. Darling, Resonant ultrasound spectroscopy for materials studies and non-destructive testing, Ultrasonics  $34$  (1996)  $473-476$ , https:// doi.org/10.1016/0041-624X(95)00120-R.
- [26] J. Nejezchlebová, M. Janovská, H. Seiner, P. Sedlák, M. Landa, J. Šmilauerová, J. Stráský, P. Harcuba, M. Janeček, The effect of athermal and isothermal  $\omega$ phase particles on elasticity of  $\beta$ -Ti single crystals, Acta Mater. 110 (2016) 185e191, https://doi.org/10.1016/j.actamat.2016.03.033.
- [27] K. Václavová, J. Stráský, V. Polyakova, J. Stráská, J. Nejezchlebová, H. Seiner, I. Semenova, M. Janeček, Microhardness and microstructure evolution of ultra-fine grained Ti-15Mo and TIMETAL LCB alloys prepared by high pressure torsion, Mater. Sci. Eng. A 682 (2017) 220-228, https://doi.org/10.1016/ j.msea.2016.11.038.
- [28] P. Sedlák, H. Seiner, J. Zdek, M. Janovská, M. Landa, Determination of all 21 independent elastic coefficients of generally anisotropic solids by resonant ultrasound spectroscopy: benchmark examples, Exp. Mech. 54 (2014) 1073e1085, https://doi.org/10.1007/s11340-014-9862-6.
- [29] H. Seiner, L. Bodnárová, P. Sedlák, M. Janeček, O. Srba, R. Král, M. Landa, Application of ultrasonic methods to determine elastic anisotropy of polycrystalline copper processed by equal-channel angular pressing, Acta Mater. 58 (2010) 235-247, https://doi.org/10.1016/J.ACTAMAT.2009.08.071.
- [30] R.G. Leisure, F.A. Willis, Resonant ultrasound spectroscopy, J. Phys. Condens. Matter 9 (1997) 6001-6029, https://doi.org/10.1088/0953-8984/9/28/002.
- [31] M. Ikeda, Negative temperature dependence of electrical resistivity in Ti-Mo binary alloys, in: de Physique, P. Lacombe, R. Tricot et, G. Beranger (Eds.), Proceedings of the Sixth World Conference on Titanium, vol. I, 1988, pp.  $313 - 318$ .
- [32] T. Fukuda, T. Kakeshita, T. Saburi, K. Kindo, T. Takeuchi, M. Honda, Y. Miyako, Negative temperature dependence of electrical resistivity in TiNi alloys, Phys. B Condens. Matter 237238 (1997) 609–611, https://doi.org/10.1016/S0921-4526(97)00279-2.