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Effect of water on elastic and creep properties of self-standing clay films

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Abstract

We characterized experimentally the elastic and creep properties of thin self-standing clay films, and how their mechanical properties evolved with relative humidity and water content. The films were films of clay montmorillonite SWy-2, obtained by evaporation of a clay suspension. Three types of films were manufactured, which differed by their interlayer cation: sodium, calcium, or a mixture of sodium with calcium. The orientational order of the films was characterized by X-ray diffractometry. The films were mechanically solicited in tension, the resulting strains being measured by Digital

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Image Correlation. We measured the Young's modulus and the creep over a variety 9 of relative humidities, on a full cycle of adsorption-desorption for what concerns the 10 Young's modulus. Increasing relative humidity made the films less stiff and made them 11 creep more. Both the elastic and creep properties depended significantly on the inter-12 layer cation. For the Young's modulus, this dependence must originate from a scale 13 greater than the scale of the clay layer. Also, hysteresis disappeared when plotting 14 the Young's modulus vs. water content instead of relative humidity. Independent of 15 interlayer cation and of relative humidity greater than 60%, after a transient period, 16 the creep of the films was always a logarithmic function of time. The experimental 17 data gathered on these mesoscale systems can be of value for modelers that aim at 18 predicting the mechanical behavior of clay-based materials (e.g., shales) at the engi-19 neering macroscopic scale from the one at the atomistic scale, for them to validate the 20 first steps of their upscaling scheme. They provide also valuable reference data for 21 bioinspired clay-based hybrid materials. 22

²³ Introduction

Understanding the short and long-term mechanical behavior of clay-based materials and the 24 sensitivity of this behavior to water is relevant for a variety of applications. For instance, a 25 deep disposal facility for high-level and intermediate-level long-lived nuclear waste is being 26 developed in France, in a clayey sedimentary rock called argillite:¹ after a few hundred years, 27 confinement of the radionuclides must be ensured by the geological barrier for more than 28 100,000 years, during which the mechanical integrity of the barrier needs to be guaranteed, in 29 spite of the expected variations of thermal and hygric conditions. Also, the stability of slopes 30 —and therefore the risk of landslides— is governed not only by the short-term mechanical 31 behavior of soils, but by their long-term behavior as well.² Finally, a better understanding 32 of the mechanical behavior of shales —a heterogeneous rock that often contains clay— is of 33 value not only to optimize the process of hydraulic fracturing used in the shale gas industry, 34

³⁵ but also to ensure the stability of boreholes in conventional oil and gas reservoirs, for which
³⁶ the sealing formation is often made of shales.³

Macroscopically, some clays expand significantly with water,⁴ partly as a consequence of 37 the swelling of the slit-shaped or lens-shaped void space between the individual clay layers 38 or between stacks of clay layers.⁵ Also, the macroscopic mechanical properties of clay-based 39 materials are known to be sensitive to relative humidity. For instance, uniaxial compression 40 experiments on $\operatorname{argillite}^{6-8}$ show that their Young's modulus and strength depend signifi-41 cantly on the water content. Equivalent trends are observed when the elastic properties are 42 measured by nanoindentation.⁹ The creep properties of clay materials are also sensitive to 43 water: the coefficient of secondary consolidation (which characterizes the long-term creep of 44 soils in general) depends on the water content.¹⁰ 45

The sensitivity to water of macroscopic clay materials stems from the sensitivity to water 46 of the individual clay layer itself. Several recent studies aim at better characterizing and 47 modeling the response of clay-based materials under hydromechanical loading through so-48 called bottom-up (or upscaling) approaches, in which the goal is to predict the macroscopic 49 behavior by starting from the microscopic level of the clay layer^{7,11}. However, the hydrome-50 chanical behavior at the scale of the clay layer and the relationship between the behavior 51 of the layer and that of the upper scales need to be better characterized. Moreover, the 52 gap between the scale of the clay layer and the macroscopic scale is huge, which makes the 53 elaboration and the validation of upscaling schemes more difficult. 54

Here, we propose and manufacture clay materials at a scale that is intermediate between the scale of the clay layer and the scale of macroscopic natural clay-based materials. The materials we design are self-standing films of pure clay with a thickness of a few dozen micrometers, which are much larger than individual clay layers (whose thickness is on the order of the nanometer) and can be probed mechanically, but remain much smaller and much simpler than macroscopic natural clay-based materials. For instance, we showed in a previous work that the swelling of those films with variations of relative humidity can be easily

inferred from the swelling of the slit-shaped void space between the individual clay layers 62 (i.e., the so-called interlayer space).¹² Here, we characterize the orientational order and the 63 mechanical properties of those films, which can be of value for instance for modelers aiming at 64 validating the first steps of their upscaling scheme. The idea of manufacturing such films and 65 characterizing their mechanical properties is readily inspired from the work of Zabat et al. 66 which, to our best knowledge, is the first textural and mechanical study of self-standing clay 67 films.^{13,14} Actually, self-standing clay films with good transparency have been manufactured 68 and used for several decades for spectroscopic (UV-Visible, IR, fluorescence) and structural 69 (X-ray) studies of clay-organic intercalates, including their sensitivity to water.^{15–17} Clay-70 based films have also been investigated as mimics of nacre $^{18-20}$. 71

In the present work, we prepared thin films of montmorillonite, on which we performed 72 tensile tests in order to characterize an elastic property (i.e., the Young's modulus) and a 73 viscous property (i.e., creep). In order to assess the effect of water, the tensile tests were 74 performed over a wide range of relative humidities. Since the mechanical behavior of clays 75 and their sensitivity to water depend on the interlayer cation, we manufactured films from 76 montmorillonites with various interlayer cations: sodium, calcium, and a mixture of sodium 77 with calcium. First, we present the materials and methods. Then, we introduce the results 78 and discuss them. 79

Materials and methods

81 Materials

We prepared materials from a natural montmorillonite SWy-2 purchased from the Source Clay Repository of the Clay Mineral Society. SWy-2 is a low-charge Wyoming montmorillonite, whose structural formula is $(Al_{3.23}Mg_{0.56}Fe_{0.42})(Si_{7.89}Al_{0.11})O_{20}(OH)_4(Ca_{0.16}Na_{0.36}-K_{0.03})^{21}$: naturally, the clay SWy-2 contains both sodium and calcium interlayer cations, in a ratio of about 2 to 1. Only the clay fraction with particles smaller than 2 μ m was conserved,

following the process described by Arroyo et al.²² The material was then homoionized with 87 either sodium cations or calcium cations. Thus, we obtained three types of montmorillonite 88 which differed by their interlayer cation, from which we prepared three types of clay films: 89 films from the natural SWy-2 clay (which contained both sodium and calcium interlayer 90 cations, and were coined 'raw-SWy-2'), films from the SWy-2 clay homoionized with sodium 91 (which were coined 'Na⁺-SWy-2'), and films from the SWy-2 clay homoionized with calcium 92 (which were coined 'Ca²⁺-SWy-2'). The films were manufactured by evaporation of a clay 93 suspension. The thickness of the prepared films was a few dozens of microns. The meth-94 ods to homoionize the raw material and to prepare the clay films are described in detail 95 elsewhere.¹² SEM pictures of the films are given in Fig. 1. 96

We measured the elastic stiffness of the three types of clay films. We measured the 97 creep properties of the films Na^+ -SWy-2 and Ca^{2+} -SWy-2 only. In order to perform those 98 various measurements, upon application of a mechanical load to the sample, we needed to 99 measure the strain of the sample: those measurements were performed by Digital Image 100 Correlation (DIC), which is introduced later. Note that we also measured elsewhere the 101 adsorption isotherms of the films,¹² and how the films swelled when relative humidity was 102 varied.¹² In parallel of the mechanical characterization here performed, we also conducted 103 a characterization of the orientational order of the obtained films, which is the focus of the 104 next section. 105

¹⁰⁶ Characterization of orientational order of clay films

¹⁰⁷ We considered the films to be transverse isotropic, with the plane of transverse isotropy being ¹⁰⁸ that of the films.²³ We characterized the orientational order of particles in the obtained films ¹⁰⁹ by analyzing experimental rocking curves. The basic principle of this technique is to operate ¹¹⁰ at a fixed 2θ value, corresponding here to the 001 Bragg reflection of the clay material ¹¹¹ under investigation, and to rotate the entire system of an angle α with respect to the film ¹¹² orientation. Accordingly, analysis of experimental intensity provides direct information on



Figure 1: SEM pictures of the edge of the manufactured clay films, at a relative humidity of 75.5 %: a) raw-SWy-2, b) Ca²⁺-SWy-2, and c) Na⁺-SWy-2. The pictures were acquired by L. Wang at the LMS laboratory at Ecole Polytechnique (Palaiseau, France).

the proportion of particles forming an angle α with the film geometry. The experimental 113 curves were acquired at ambient temperature (~ 25°C) and relative humidity (~ 40%) in 114 transmission conditions on an Empyrean Panalytical X-ray diffractometer equipped with an 115 X'Celerator detector operating in receiving slit mode. The step size was 0.15 and $0.5^{\circ}\alpha$ in 116 the 0-7 and 7-90° α angular ranges, respectively, with a time per step of 10 s. The angular 117 α range probed in this study for each sample depended on both the position of the 001 118 reflection of the sample and the relative position of the sample holder with respect to the 119 sample in the fixed 2θ geometry, the sample holder inducing a shadow for both incident and 120 transmitted X-ray beam. 121

The experimental rocking curves, and how they were analyzed, 2^{2-25} are provided in Sup-122 porting Information. More information on the overall degree of particle orientation in 123 the different films can be obtained through the calculation of the scalar order parameter 124 $S = \langle (3\cos^2 \alpha) - 1 \rangle /2$, where $\langle X \rangle$ holds for the ensemble average of the volumetric 125 quantity X^{26} This order parameter S can range from S = 0 for an isotropic medium to 126 S = 1 for a perfectly anisotropic medium (i.e., with all particles oriented perfectly parallel 127 in the film). The order parameter S of the films raw-SWy-2, Ca^{2+} -SWy-2, and Na⁺-SWy-2 128 was 0.69, 0.79, and 0.66, respectively. From those relatively high values, we infer that the 129 clay particles exhibited a preferential orientation in the clay film, as supported by direct ob-130 servation (see Fig. 1). Also, as suggested by this same direct observation, values of the order 131 parameter S confirm that the Na⁺-SWy-2 film and the raw-SWy-2 film were less ordered 132 than the Ca^{2+} -SWy-2 film. 133

¹³⁴ Measurement of strain by DIC

We measured the elastic stiffness of the three types of clay films, but the creep properties of the films Na⁺-SWy-2 and Ca²⁺-SWy-2 only. In order to perform those various measurements, upon application of a mechanical load to the sample, the strains were characterized by using digital image correlation (DIC), which is a contact-free technique.²⁷ DIC consists in

acquiring images of the surface of the sample with a digital camera at various times during 139 the experiment. Then, each image is compared with an image of the surface of the sample 140 in its state of reference (i.e., here, before any load was applied to the sample). Points chosen 141 in the reference image are identified in the image of the deformed sample by matching the 142 gray levels: thus, at a given time, the displacement of various points at the surface of the 143 sample is measured. The two-dimensional strain of the observed surface is obtained by 144 spatial differentiation of the displacements, and average strains over regions of interest are 145 obtained from contour integrals.⁶ 146

To take images of the samples during the tests, a Pike camera from Allied Vision Tech-147 nology was used. The CCD sensor was 2048×2048 -pixels-wide with pixels with a width of 148 7.4 μ m and the gray levels were encoded on 8 bits. To improve the contrast of the images, 149 carbon powder was scattered all over the surface of the films. The camera was equipped with 150 optics from Schneider Kreuznach (Apo-Componen 90 mm lens) with appropriate extension 151 tubes (makro system), so that a pixel in the images represented approximately 25 μ m (i.e., 152 optical magnification was about 0.3). During experiments at ambient relative humidity, we 153 used another Pike camera (Allied Vision Technology) with a lower resolution: the 2/3-inch 154 CCD sensor was 1388×1038 -pixels-wide with pixels with a width of 5.5 μ m. The images 155 were acquired continuously during the tests at a minimum interval of 250 ms. All images 156 were then analyzed by DIC with the in-house software CMV.⁶ We used 30-pixels-wide cor-157 relation windows. First-order affine shape functions were combined with a zero-centered 158 normalized cross-correlation criterion, and subpixel accuracy was obtained by means of a 159 biquintic interpolation of the gray levels.²⁷ The physical size of a correlation window was 160 730 μm with the higher resolution camera. With the lower resolution camera, the physical 161 size of the correlation window was 1 mm (pixel size in the images of about 30 μ m, optical 162 magnification of about 0.18). 163

We estimated from the analysis of controlled rigid body motions²⁸ that the error on the average strain measured by DIC was 6×10^{-5} , which is small with respect to the magnitude ¹⁶⁶ of the strains in this study, which were on the order of 10^{-3} . For a detailed description of ¹⁶⁷ how we estimated this error, see the Ph.D. thesis of Carrier.²⁹

¹⁶⁸ Method for measurement of Young's modulus

We aimed at measuring the Young's modulus in the direction parallel to the film. In order to measure this modulus, we performed tensile experiments on the clay films, at various controlled relative humidities. The clay films were stressed in tension in a direction parallel to the films.

First, in each prepared film, samples which were 9.3-mm-wide and 80-mm-long were cut with sharp blades. The ends of each sample were reinforced with sandpaper before being placed in the grips of the tensile test machine. The free length of the sample was equal to 50 mm. Figure 2 displays the experimental setup.

The tensile tests were carried out under controlled relative humidities in an environmental 177 chamber made of PMMA and built around the testing machine. The relative humidity was 178 controlled with saturated salt solutions. Compressed air was blown into a salt solution 179 so that it reached the desired relative humidity. The humidified air was then injected in 180 the environmental chamber. Thus, the pressure in the chamber was slightly higher than 181 in the room and the relative humidity in the chamber was less sensitive to leaks than if 182 no overpressure had been applied. Equilibration of the chamber required only about 30 183 minutes. The relative humidity and temperature were recorded continuously with a thermo-184 hygrometric sensor. Equilibration of the films with the relative humidity in the environmental 185 chamber required about one hour. 186

During the tensile tests, we controlled the displacement of the upper grip to perform one or two loading-unloading cycles. A force sensor recorded continuously the force with an accuracy of 1 mN. To compute the Young's modulus of the clay films, we used the slope of the unloading portion of the force-strain curve, together with the section of the sample at any relative humidity. To estimate this section, first, we measured the thickness of the samples at



Figure 2: Experimental setup for the measurement of elastic stiffness: a) schematics and b) pictures.

¹⁹² a reference relative humidity of 35 % with an Environmental Scanning Electron Microscope ¹⁹³ FEI Quanta 600 available at LMS at École Polytechnique. We estimated the thickness at ¹⁹⁴ other relative humidities as follows. First, adsorption isotherms measured elsewhere¹² made ¹⁹⁵ it possible to estimate the water content at a given relative humidity. Second, we estimated ¹⁹⁶ the thickness at this water content by considering a linear relationship between thickness ¹⁹⁷ and water content, the validity of such linear relation being supported by data gathered by ¹⁹⁸ Carrier et al.;¹² the slope of this linear relation was fitted on this set of data.

A typical stress-strain curve, acquired at ambient conditions (i.e., temperature of about 199 25°C and relative humidity of about 25 %) is provided as Supporting Information. From 200 this data, we infer that, in all tensile tests performed in this study, for which strains were 201 always smaller than 0.3%, strains were sufficiently small to remain in the linear elastic 202 regime. Also, by loading and unloading 20 times a Ca^{2+} -SWy-2 film at various displacement 203 rates, ranging from 0.3 μ m/s to 32 μ m/s (see Supporting Information), we could observe 204 no damage during the successive loading-unloading cycles and we could conclude that the 205 Young's modulus did not depend on the displacement rate. Finally, by performing tensile 206 experiments under ambient conditions on various films made with all materials (see again 207 Supporting Information), we concluded that relative uncertainties on the measured Young's 208 moduli were all smaller than 19 %, thus proving that both manufacturing and measurement 209 were repeatable. 210

²¹¹ Method for measurement of creep property

We aimed at measuring a creep property of the clay films, i.e., how the clay films deform over time under a constant load. Creep experiments were performed on the films Ca²⁺-SWy-2 and Na⁺-SWy-2, whose geometry was the same as for the samples dedicated to the elastic characterization. The free length of the samples was equal to 50 mm.

Figure 3 displays the experimental setup we used to perform creep tests. One end of the sample was placed in a fixed grip and the other end was fixed to a mobile ball slide which

could move linearly on a rail. The sample was loaded by a weight attached to a string, itself 218 attached to the mobile ball slide. A pulley transformed the vertical gravitational force into a 219 horizontal force on the ball slide. In order to minimize friction, the mobile part had a linear-220 motion bearing at the contact with a lubricated rail. Before performing any experiment, we 221 calibrated the device: to measure the friction, we loaded the device with various weights. For 222 each weight, we measured the force transmitted by the ball slide with a force sensor having 223 an accuracy of 1 mN. We fitted the data with a linear function. The slope of this function 224 was equal to 1 and the extrapolation to a measured force equal to zero gave a friction of 225 0.11 ± 0.1 N. In all results presented in this study of the creep properties, every applied 226 force was corrected by taking into account this friction. To be consistent from one sample 227 to another, the load will be expressed in force per clay layer, i.e., the force transmitted to 228 the sample divided by the number of clay layers in the thickness of the sample, which was 229 estimated by dividing the surface density of the dry film by the surface density of a clay 230 layer. 231

To perform creep tests at various relative humidities, the creep test device was placed in an 232 environmental chamber. The relative humidity was controlled with saturated salt solutions 233 and measured with a hygrometric sensor. Figure 3 shows the experimental setup. Again, 234 the strains of the samples were measured by taking images of the samples and analyzing 235 them with DIC, with the same camera and correlation procedure as the ones presented in 236 Sec. 2.3. Before each creep test, the sample was placed in a chamber in equilibrium with 237 pure water to equilibrate it at a relative humidity close to 100 %. Water was then replaced 238 with a saturated salt solution to bring the chamber to the desired relative humidity. The 239 hydric starting points of all creep tests were therefore located on the desorption branch of 240 the adsorption isotherms. 241



Figure 3: Pictures of the experimental setup to measure tensile creep under controlled relative humidity.

242 Results and discussion

243 Effect of water content on Young's modulus

Figure 4 displays the Young's modulus of the raw-SWy-2, Ca²⁺-SWy-2, and Na⁺-SWy-2 244 films versus relative humidity and water content. Several samples of each material were 245 tested: we observed a good reproducibility of the tests. The Ca²⁺-SWy-2 film was the 246 stiffest one, with Young's moduli ranging from 2.4 GPa at high water content to 6.2 GPa at 247 low water content, while the Young's moduli of the Na⁺-SWy-2 film ranged from 1.0 GPa to 248 5.6 GPa. The raw-SWy-2 film exhibited an intermediate behavior: at low water content, its 249 Young's modulus was smaller than the one of the Ca²⁺-SWy-2 film (5.6 GPa versus 6.2 GPa, 250 respectively); however, at a water content of 0.2 g/g of dry clay, its Young's modulus was 251 higher than the one of the Ca^{2+} -SWy-2 film (3.3 GPa versus 2.8 GPa). 252

The nature of the cation had a clear impact on the elastic properties of clay films at a given water content. The film made with Ca-exchanged montmorillonite (i.e., the Ca²⁺-SWy-2 film) was always stiffer than the film made with Na-exchanged montmorillonite (i.e., the Na⁺-SWy-2 film). But we also observed an effect of the nature of the cation on the softening



Figure 4: Young's modulus of clay films as a function of relative humidity and water content: (a) and (d) raw-SWy-2-raw, (b) and (e) Ca²⁺-SWy-2, (c) and (f) Na⁺-SWy-2. For each material, several samples were tested at various relative humidities.

of the films with the increase of water content. Between the smallest and the largest water contents (i.e., about 0.02 g/g and 0.24 g/g, respectively), the ratio of the Young's moduli was equal to approximately 6 for the Ca²⁺-SWy-2 films while it was equal to approximately 3 in the case of the Na⁺-SWy-2 films. The Young's modulus of the Ca²⁺-SWy-2 films was therefore much more sensitive to water than that of the Na⁺-SWy-2 films. Again, the films

made with the natural clay raw-SWy-2 exhibited an intermediate behavior. The difference in sensitivity to the water content, in particular between the Ca²⁺-SWy-2 films and the Na⁺-SWy-2 films, is quite surprising as, over a full adsorption/desorption cycle, the water contents of the films varied over an identical range.

Part of the decrease of stiffness upon an increase of water content is a geometrical effect 266 consecutive to an increase of basal spacing.³⁰ In order to obtain results insensitive to this 267 geometrical effect, we now choose to focus no more on the Young's modulus of the clay films, 268 but on a normalized stiffness. This normalized stiffness was computed as the slope of the 269 force-strain curve divided by an estimate of the number of clay layers in the film, the basal 270 spacing of a dry clay layer (i.e., 9.55 Å, which corresponds to about 1050 layers through the 271 thickness of a 1- μ m-thick film), and the width of the sample. Note that, with this definition, 272 the normalized stiffness can also be said to be equal to the slope of a stress-strain curve, 273 where the stress is calculated by dividing the applied force by the cross-sectional area of 274 the dry film, whatever the hydric conditions of the experiment are. The number of clay 275 layers in the thickness of a film was estimated (see Sec. 2.5) to be approximately equal 276 to 25000, 16000, and 40000 for Ca^{2+} -SWy-2, Na⁺-SWy-2, and raw-SWy-2, respectively. 277 Figure 5 displays this normalized stiffness upon a full adsorption/desorption cycle for the 278 three types of films tested. As expected, all samples exhibited a softening upon hydration 279 and a stiffening upon dehydration with a hysteresis between the two branches. Moreover, 280 the Ca²⁺-SWy-2 and raw-SWy-2 films were stiffer than the Na⁺-SWy-2 film, all the more so 281 as the relative humidity was low. 282

As can be observed in Figs. 4 and 5, the dependence of the Young's modulus on the relative humidity exhibited a significant hysteresis for the raw-SWy-2 samples, but no hysteresis for the Ca²⁺-SWy-2 films. Interestingly, the same figures show that, when plotting the Young's modulus versus the water content, this hysteresis almost fully disappeared for all samples. Therefore, upon a cycle of adsorption/desorption, the hysteresis observed on the Young's modulus is mostly due to the fact that water is adsorbed in a hysteretic man-



Figure 5: Normalized stiffness of films Ca²⁺-SWy-2, Na⁺-SWy-2, and raw-SWy-2, as a function of (a) relative humidity and (b) water content. Hollow and filled symbols correspond to the adsorption and desorption branches, respectively.

ner: in particular, the film on which no hysteresis was observed for the elastic properties (i.e., the Ca²⁺-SWy-2 film) is indeed the film on which no hysteresis is observed for the adsorption isotherm.¹² When focusing on the swelling of clay films induced by variations of relative humidity, one also observes that plotting swelling versus relative humidity exhibits ²⁹³ a hysteresis, but that plotting swelling versus water content exhibits no hysteresis.¹² Those ²⁹⁴ observations on hysteresis strongly suggest that the natural state variable on which swelling ²⁹⁵ or elastic properties depend is the water content.

²⁹⁶ Discussion on effect of interlayer cation

Figure 5 shows that, at a given relative humidity, the normalized stiffness was larger for the Ca²⁺-SWy-2 film than for the Na⁺-SWy-2 film. Such result can seem somewhat counterintuitive since, at low relative humidities, adsorption isotherms¹² and X-ray diffraction results^{31,32} show that the water content and the basal spacing are larger for montmorillonite homoionized with calcium than with sodium. Also, the raw-SWy-2 film —although it contains more sodium cations than calcium cations— exhibited a normalized stiffness close to the one of the Ca²⁺-SWy-2 film.

The experimental results show that, even at a given water content, the mechanical prop-304 erties of the clay films depended on the nature of the interlayer cation: at a given water 305 content, the Ca²⁺-SWy-2 film was always stiffer than the Na⁺-SWy-2 film, while the film 306 made with natural montmorillonite (i.e., the raw-SWy-2 film, which contained both Na⁺ 307 and Ca^{2+} cations) exhibited an intermediate behavior. This result is not consistent with 308 the mechanical behavior of the clay layer as evaluated from numerical simulations. Indeed, 300 molecular dynamics computations showed a limited impact of the nature of the interlayer 310 cation on the elastic properties of the layer, except in the driest states:³⁰ as soon as the first 311 water layer is formed, no dependence of the coefficients of the stiffness tensors on the in-312 terlayer cation is observed. However, the dependence of the elastic properties of clay-based 313 materials on the interlayer cation was also observed by Wang et al.,³³ who measured the 314 elastic properties of epoxy-clay composites, from which they inferred the elastic properties 315 of the clay minerals only, after subtracting the mechanical contribution of the epoxy by us-316 ing micromechanical relations: their results show that Ca-rich montmorillonites are stiffer 317 than Na-rich montmorillonites. Note however that the water content of their samples was 318

not controlled and therefore was very uncertain. To our knowledge, there is no other work
available in the literature in which the mechanical properties of a same clay with various
interlayer cations are compared.

If the reason for the dependence of the elastic properties of clay-based materials on the 322 nature of the interlayer cations cannot be found at the scale of the clay layer, it must be 323 found at a scale above. Indeed, the nature of the cation has also an effect on the size and the 324 arrangement of the clay particles and on the mesostructure of the material^{34,35}. Experiments 325 show that exfoliating smectite layers with calcium counterions is very difficult ^{36–38} and that 326 Ca-exchanged smectite layers form thicker tactoids in solution than Na-exchanged smectite 327 lavers³⁵. A microscopic reason for those observations can be that cohesive forces between 328 neighboring layers depends on the counterion.²⁹ Indeed, the cohesion of clay systems is 329 mainly governed by electrostatic interactions (rather than by Van der Waals ones), so that it 330 is in particular sensitive to the valence of the counterion. Note that cohesion can vary even 331 if stiffness does not, so that the fact that Ca-rich clays are more cohesive than Na-rich clays 332 is not inconsistent with the molecular simulations of Carrier et al.,³⁰ which show that, at a 333 given water content, the counterion has no effect on the stiffness of the stack of clay layers. 334 In addition, our X-ray diffraction measurements show that the order parameter S is larger 335 in the Ca-exchanged than in the Na-exchanged sample, showing that the orientational order is 336 better in the former case. One can expect that the elastic properties of the film depend on this 337 orientational order since the stiffness coefficients of clay particle that are solicited by tensile 338 loading of the film depend on the orientation of the particle with respect to the film. Another 339 microstructural feature that could play a role in the mechanical properties of the film is how 340 the contacts between neighboring clay particles are spatially organized, as these contacts 341 govern how stresses are being transmitted throughout the film. Intuitively, one could expect 342 that a larger average area of contact would translate into a greater stiffness. It may be that, 343 in our self-standing films, the average area of contact between clay particles in Ca-exchanged 344 montmorillonite differs from that in Na-exchanged montmorillonite: as a result, for the same 345

uniaxial force applied to the film, the stresses (and in particular the shear stresses) acting 346 at the scale of the clay particle would depend on the interlayer cation. Such mesostructural 347 difference could explain our experimental observation that Ca-exchanged films were stiffer 348 than Na-exchanged films. In short, the macroscopic hydromechanical behavior of clays 349 depends strongly on the structure at scales larger than the scale of the clay layer and on the 350 orientational order. This mesostructure should be taken into account in a realistic model 351 to obtain a good estimate of the Young's modulus of an ensemble of particles, may it be 352 ordered or not. 353

³⁵⁴ Effect of water on creep property

The results presented in this section were obtained with the experimental setup displayed 355 in Fig. 3 according to the protocol described in Sec. 2.5. Figure 6(a) displays the typical 356 deformations of a clay film with time. At t = 0 s, a load equal to 26.1 μ N per clay layer 357 was applied and was kept constant during the test. The samples exhibited an instantaneous 358 elastic deformation. The creep strain was then calculated as the difference between the total 359 strain and this instantaneous elastic deformation: thus, the creep strain was the delayed 360 part of the deformation. In Fig. 6(a), the creep strain of two Ca^{2+} -SWv-2 films is displayed 361 in function of time, on a logarithmic scale. After 500 to 600 s, the deformation was a 362 logarithmic function of time. Actually, such feature of a creep strain that evolves linearly 363 with the logarithm of time after a transient period was observed for all films. By analogy 364 with what is done in soil mechanics,³⁹ we introduce a creep coefficient α defined as the slope 365 of the creep strain versus logarithm of time curve: 366

$$\alpha = \frac{d\epsilon}{d(\ln t)}.\tag{1}$$

For each tensile creep experiment, this creep coefficient was back-calculated from the data acquired once the non-logarithmic transient period is exhausted.

In Fig. 6(a), tests performed on two Ca²⁺-SWy-2 films are displayed: the first one was 369 performed at a relative humidity of 92.0 \pm 2.9 % and the second one at a relative humidity 370 of 77.7 ± 2.0 %. The test at 92.0 % was stopped when the sample failed, while we stopped 371 the test at 77.7 % before failure. Relative humidity had a very clear impact on the creep 372 rate. The creep strain was a linear function of the logarithm of time for both tests and the 373 slope α of this function (which we named creep coefficient) was larger at a higher relative 374 humidity: the creep coefficient α was equal to 0.22 % at a relative humidity of 92 % but to 375 0.05~% at a relative humidity of 78 %. 376

The observed logarithmic feature of creep is reminiscent of the creep of macroscopic clay-377 based materials or of soils, which is also known to evolve logarithmically with time after a 378 transient period.³⁹ However, macroscopically, soils are usually tested in compression or in 379 shear, not in tension. The fact that, here, a logarithmic creep was also observed in tension 380 makes it possible to discard one possible explanation for the origin of such logarithmic creep, 381 which is the free volume dynamics theory. Free volume dynamics can explain why the density 382 of vibrated columns of granular materials evolve logarithmically with time^{40,41}, by stipulating 383 that, when the density of the column increases, the free volume between grains decreases, 384 and hence their ability to move and the creep rate. Such theory has also been proposed to 385 explain why the creep of cementitious materials is a logarithmic function of time in the long 386 term.⁴² But, for what concerns our experiments on clay films, since the applied stresses are 387 tensile, the free volume must increase with time, thus making it impossible to explain why 388 the creep rate would decrease over time. Other potential theories to explain this logarithmic 389 creep, sometimes proposed for other materials that exhibit this same feature (e.g., cement 390 or sand), are, among others: relaxation of internal prestresses,⁴³ presence of energy barriers 391 that two solids (e.g., two clay layers) need to overcome in order to slide over each other,⁴⁴ 392 or breakage of bonds or particles.⁴⁵ 393

Figure 6(b) displays the creep strain of two Na⁺-SWy-2 films in function of time, on a logarithmic scale. The two tests were performed at the same relative humidity, but at



Figure 6: (a) Creep strain of films of Ca²⁺-SWy-2 as a function of time (logarithmic scale) at various relative humidities. The force transmitted to the samples was identical for both tests (i.e., 26.1 μ N per clay layer). (b) Creep strain of Na⁺-SWy-2 films as a function of time at various applied forces. The relative humidity was identical for both tests (~ 92 %).

various loads (8.1 and 20.2 μ N per clay layer, respectively). The test with a load equal to 20.2 μ N per layer was stopped when the sample failed, while we stopped the test with a load of 8.1 μ N per layer before failure. For both films, after a transient period, the creep strain was a logarithmic function of time. The amplitude of the creep increased with load: for a load equal to 8.1 μ N per clay layer, the creep coefficient α was equal to 0.12 %, while this creep coefficient was equal to 0.91 % for a load equal to 20.2 μ N per layer. Therefore, the amplitude of creep increased faster than the load: when the load was multiplied by 2.5, the creep coefficient α increased by a factor 4.3. A more thorough study of the effect of the load on the creep coefficient is presented next.

Figure 7 displays the creep coefficient α in function of load for Ca²⁺-SWy-2 films and Na⁺-405 SWy-2 films at a given relative humidity. Four sets of data are displayed, which correspond 406 to 2 experiments: a first experiment on two samples cut out from the same Ca²⁺-SWy-2 film 407 and on two samples cut out from the same Na⁺-SWy-2 film, and a second experiment on a 408 sample cut out from another Ca²⁺-SWy-2 film and on a sample cut out from another Na⁺-409 SWy-2 film. In each experiment, all samples were tested at the same time while located in the 410 same environmental chamber. The 2 experiments were performed at different times but with 411 the same environmental chamber. When the films were loaded during the same experiment, 412 for both materials, the creep coefficient was an increasing function of load in a roughly linear 413 manner. However, experiments performed at different times were not consistent with each 414 other. Although the relative humidities measured in the two experiments were close to each 415 other (e.g., 77.5 \pm 2.8 $\,$ % and 77.7 \pm 2.5 % for the two sets of data on the Ca^{2+}-SWy-2 416 films), because of the experimental difficulty in controlling temperature and relative humidity 417 precisely, the uncertainty on the actual local relative humidity with which the films were in 418 equilibrium may be up to 5 %. Moreover, at relative humidities around 80 %, the creep 419 coefficient α was very sensitive to relative humidity, as is shown next. Such uncertainty 420 could explain the discrepancy between the sets of experiments 1 and 2 displayed in Fig. 7. 421 In any case, experiments under the very same environmental conditions suggested that the 422 creep coefficient depends on the load and that this dependence is quite linear. Therefore, we 423 introduce the creep compliance κ (expressed in Pa⁻¹), defined by: 424

$$\kappa = \alpha \frac{bd}{F},\tag{2}$$

where F is the force applied by clay layer, b is the width of the sample (b = 9.3 mm for all creep tests), and d is the basal spacing of a dry clayer (i.e., 9.55 Å). The results of all creep tests, at all relative humidities and for both types of films, are given as Supporting Information.



Figure 7: Creep coefficient α as a function of load at a given relative humidity. For each film, exp 1 and exp 2 correspond to two different experiments. During experiment 1, two identical films were loaded at the same time in the same environmental chamber. The relative humidity was equal to 77.5 \pm 2.8 % and 81.3 \pm 1.5 % for Ca²⁺-SWy-2 and Na⁺-SWy-2, respectively. Experiment 2 was performed on different films, at a different time. The relative humidity was equal to 77.7 \pm 2.5 % and 80.3 \pm 2.3 % for Ca²⁺-SWy-2 and Na⁺-SWy-2, respectively.

Figure 8 displays the creep compliance κ in function of relative humidity for both the Ca²⁺-SWy-2 and Na⁺-SWy-2 films. The error bars on the creep compliance are only visible for the data with the lowest creep compliance, which correspond to films that creep the least, and on which the noise on the creep measurement was thus the largest. At a given relative humidity, the creep compliance was much higher for the Na⁺-SWy-2 films than for the Ca²⁺-SWy-2 films, by about one order of magnitude. Also, for both types of films, we observed a tremendous effect of relative humidity on the creep compliance: when increasing
the humidity from about 60 % to about 95 %, their creep compliance increased by about
two orders of magnitude.



Figure 8: Creep compliance κ in function of relative humidity for (a) sample Ca²⁺-SWy-2 and (b) Na⁺-SWy-2. Dotted lines are visual guides.

We performed creep tests for relative humidities below 50 %, but we could observe no creep: the very low creep compliance at low relative humidities indeed required very long tests. Controlling the relative humidity with a high accuracy during such periods of several days was impossible: the relative humidity and water content fluctuated slightly over time.
The creep was therefore indistinguishable from the slight swelling and shrinkage of the film
or the small variations of the elastic properties shown in Fig. 4.

Figure 9 displays the creep compliance as a function of water content. We performed a linear regression of the logarithm of the compliance versus water content (dashed lines in Figure 9) and obtained a correlation coefficient equal to 0.83 for the Ca²⁺-SWy-2 films and to 0.78 for the Na⁺-SWy-2 films. The compliance can therefore be well approximated by an exponential function of water content: creep is very much sensitive to the water content. The physical mechanism behind this strong dependency remains unclear.



Figure 9: Creep compliance κ in function of water content for samples Ca²⁺-SWy-2 and Na⁺-SWy-2.

450 Conclusions

⁴⁵¹ The conclusions of this work are:

Whatever the interlayer cations are (here, sodium, calcium, or a mixture of sodium
 with calcium), the elastic and creep properties of clay films depended on relative hu midity/water content. Increasing the water content made the clay films less stiff and

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made them creep more.

• The nature of the interlayer cation had a significant effect on the elastic and creep 456 properties of the clay films and on the dependence of these properties on relative 457 humidity. Since the stiffness tensor of a clay layer at a given water content, as evaluated 458 by molecular simulations, does not depend on the nature of the interlayer cation,³⁰ the 459 reason why the elastic properties of the films depended on the interlayer cation must 460 originate from a scale greater than the scale of the clay layer: the structure of the 461 films at a mesoscale (e.g., the size and shape of the clay tactoids) must significantly 462 impact the elastic behavior of the film. It is likely that such structure at a mesoscale 463 also impacts the creep behavior of the films and at least partly explains why creep 464 depended on the nature of the interlayer cation. 465

• The Young's modulus exhibited a clear hysteresis when plotted versus relative humid-466 ity, but no hysteresis when plotted versus water content. Therefore, the hysteresis 467 observed when plotting Young's modulus versus relative humidity mostly originates 468 from the hysteresis of the water adsorption isotherm. Such vanishing of hysteresis has 469 also been observed when focusing on the swelling properties of the same clay films.¹² 470 Therefore, the natural parameter on which elastic and swelling properties of the films 471 depend is the water content, not the relative humidity. Such observation is likely to 472 hold for other mechanical properties and should be recognized by any model of the 473 hydro-mechanical behavior of clay-based materials, at least at the scale of the clay 474 layers or of the clay particles. 475

After a transient period, the creep of all tested films was a logarithmic function of time. Since the films were loaded in tension, this logarithmic feature of creep cannot be explained by free volume dynamics. The creep compliance could be well approximated by an exponential function of water content.

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In addition to these conclusions, the work here performed provides a complete set of data

on how the elastic and creep properties of films of montmorillonite with various interlayer 481 cations depend on water content and relative humidity. Moreover, the orientational order 482 of the films was characterized, as well as, elsewhere, their adsorption isotherms and swelling 483 properties.¹² Such set of data can serve as reference data for scientists working on bioinspired 484 clay-based hybrid materials. It can also be of value for modelers who aim at predicting the 485 mechanical behavior of clay-based materials (e.g., shales) at the macroscopic scale of the 486 engineer, from the behavior at the atomistic scale. Indeed, the results here presented make 487 it possible for them to confront the first steps of their upscaling scheme with experimental 488 data: such confrontation is necessary since, as we observed, the elastic properties of our films 489 depend significantly on the structure at a mesoscale (i.e., at a scale greater than the scale 490 of the clay layer). In particular, the dependence of the Young's modulus on the interlayer 491 cation must originate from this mesoscale. One can reasonably extrapolate that the mesoscale 492 structure is likely to play a significant role not only on the elastic properties of the pure clay 493 films here tested, but on the mechanical properties of all clay-based materials in general. 494

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