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Analysis of vibrations on an aerial cable car system with moving mass

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The transport of people and goods over aerial cableways has been in use over the last hundred years for many different applications but published works are still only a few years old. Either by transporting uphill, between a long valley or canyon. Since it is a complex mechanical system with many bodies and subject to environment perturbation, nonlinearity features may appear such as excitation of sub and super harmonics of the cable and cause vibration to the traction mechanism, which can damage the machinery and endanger the operation.

For this work, we analyze the effect of those vibrations according to the speed of operation. The coupling of two ropes and a mass-spring system creates a complex dynamic that cause a nonlinear movement, and can even show some chaotic behavior. For such we had to study many articles that not only show horizontal cable cars, but also vertical systems such as elevators.

The study of cable car systems is an interesting subject in modern literature, with many different aspects of the system approached. Brownjohn (1998) analyses the vertical plane motion of the cable car that connects Singapore main island and the island of Sentosa. Mathematical simulations are presented for the normal operation of the system, free vibration and when the system is halted. Measurements with accelerometers were performed in the real system to obtain vibrations for each condition of operation. A finite element model of the system is then proposed and the results analyzed.

Terumichi et. al. (1997) studies the nonstationary lateral vibration of a string with time-varying length and a rail guided mass-spring system attached at the lower end, a system representative of an elevator. The string is sinusoidal excited by a horizontal displacement at its upper end. The influence of the axial velocity of the string on the vibrations are analyzed and a simplified experimental setup is presented. Experimental and simulation results are then compared showing good results.

Bao et. al. (2015) also analyzes lateral vibrations in a string in a vertical motion system analog to an elevator, but in this case, the source of excitation is the lateral motion of the mass coming from an imperfect rail guide. The Hamilton principle is used to obtain the equations of motion of the string, and experimental tests are performed and its results compared to the numerical simulations.

Kaczmarczyk and Iwankiewicz (2006) propose a stochastic approach to the source of excitation of an elevator model. The stochastic parameter is the guide rail imperfections that excite the car laterally. These imperfections are written as a zero-mean stationary Gaussian process.

The complete mechanical system is exemplified in Figure 1, where the overhung cable is shown as a cable under a constant tension T supported on both ends with density ρ , circular cross section A , and constant length L . Its model is simplified as a spring k that connects to the concentrated mass M representing the car. This car is pulled by the traction cable with density ρ' , cross section A' , and tension T' . However, this length of the traction cable varies in time with constant velocity v .

In order to find the equivalent stiffness of the rail cable a simple case study is presented. If one only considers the rail cable and the car passing through the extent of the rail cable is simplified as a concentrated load travelling with constant velocity. The solution of this problem is analytically solved and demonstrated in Hagendorn (2007). The deflection of the cable is

$$w(x,t) = -\frac{2FLv}{\rho A c \pi^2 (c^2 - v^2)} \sum_j \frac{(-1)^j}{j^2} \left[\left(\cos \frac{j\pi c}{v} - (-1)^j \right) \sin \omega_j t - \sin \frac{j\pi c}{v} \cos \omega_j t \right] \sin \frac{j\pi x}{l}. \quad (1)$$

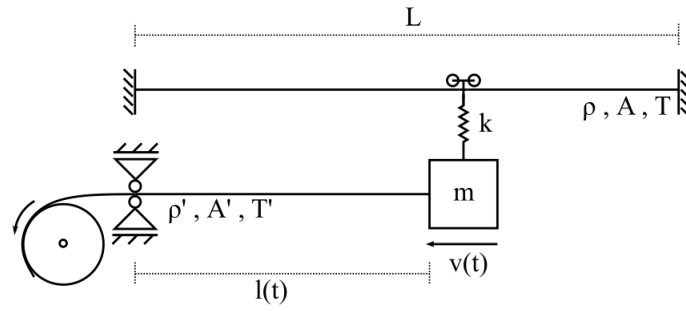


Figure 1 – The complete mechanical system

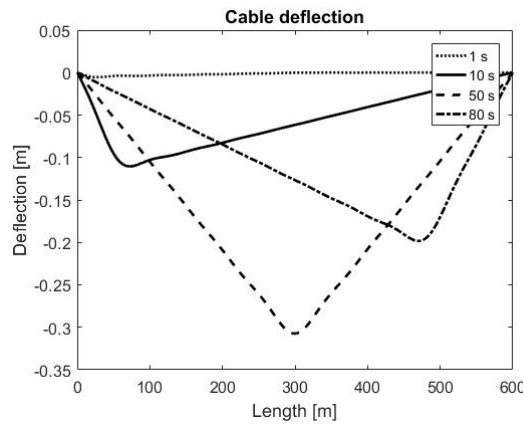


Figure 2 – Deflection of the cable with a moving load

In Figure 2 it is shown the deflection of the cable at different instants while the load moves with velocity v . The parameters used to generate these results are shown in Table 1. The deflection of the rope reaches its maximum value when the load is close to the half of the length. Therefore, the value of the equivalent stiffness of the rail cable is approximately obtained as

$$k = \frac{F}{w\left(500, \frac{L}{2}\right)} = 16.27 \frac{\text{KN}}{\text{m}}. \quad (2)$$

Then the analysis of the mechanical system of a mass being pulled by a cable can be performed. We begin by stating the kinetic and the potential energy of the rope and the mass. The total kinetic energy is

$$E_k = \frac{1}{2} \int_0^{l(t)} \rho' A' \left[\dot{y}^2 + (\dot{y} + v y')^2 \right] dx + \frac{1}{2} M \left[\dot{y}^2 + (\dot{y} + v y')^2 \right]_{l(t)}, \quad (3)$$

and the total potential energy is

$$E_p = \frac{1}{2} \int_0^{l(t)} T' (y')^2 dx + \frac{1}{2} K y^2 \Big|_{l(t)} + M g y|_{l(t)}. \quad (4)$$

Table 1 – Parameters used to model the rail cable

Parameter		[]
Linear density	ρA	39.21 kg/m
Length	L	600 m
Load	F	25 KN
Velocity	v	6 m/s
Mean Tension	T	23.87 MPa

Using the Hamilton principle with the adequate definition of the boundaries conditions and considering the variation of the length, the equations of motions of the cable and for the mass can be obtained, respectively, as

$$\rho \left(\ddot{y} + 2v\dot{y} + v^2 y'' \right) - T y'' = 0, \quad 0 \leq x < l(t), \quad (5)$$

$$M \left(\ddot{y} + 2v\dot{y} + v^2 y'' \right) \Big|_{x=l(t)} + T y' \Big|_{x=l(t)} + M g + K y \Big|_{x=l(t)} = 0, \quad (6)$$

where the \dot{y} is the time-derivative and y' is the spatial derivative. Now, it is introduced a slow time variation $\tau = \varepsilon t$, in which $\varepsilon = v/\omega_0 L_0$ and where ω_0 is the natural frequency of the cable without mass and spring and L_0 is the maximum extent of the cable. Knowing that $l(t) = L_0 + vt$, so

$$\dot{t} = v = \frac{\partial \tau}{\partial t} \frac{\partial l}{\partial \tau} = \varepsilon l'. \quad (7)$$

Therefore, we will seek solutions of the following form

$$y(x, t) = \sum_{n=1}^N \Psi_n(x, \tau) q_n(t), \quad (8)$$

where $\Psi(x, \tau) = \sin(\beta_n(\tau)x)$. The term $\beta_n(\tau)$ is a slow variation in time of the natural frequency of the cable.

Since the dynamical equations involved in the present problem are highly nonlinear, the exact solution is sought through approximate methods such as perturbation methods or by numerical methods. A Finite Element Method (FEM) is employed to solve the equations in time. Different parameters and speeds are carried out in the simulation code in order to find a mechanical configuration, which will show an excitation of a natural frequency during the simulated time.

In the present work the main contribution is the construction of a dynamical model of a car being pulled by a traction cable and simultaneously suspended by another cable working as rails. The equations that govern the elements and the adequate hypotheses are derived. This model can be further improved by considering the stiffness of the rail cable as equally varying in time and even as a continuum body with a fixed length. The results of the FEM simulations will be given in time as well as in the frequency domain, where the variation of the vibration modes and natural frequencies will be evident.

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