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# Electronic ratchets as necessary stepping stones for new PV concepts

Amaury Delamarre<sup>1,2</sup>, Daniel Suchet<sup>1,4</sup>, Nicolas Cavassilas<sup>1,5</sup>, Zacharie Jehl<sup>1,2</sup>, Yoshitaka Okada<sup>1,2</sup>, Masakazu Sugiyama<sup>1,2</sup> and Jean-François Guillemoles<sup>1,3,\*</sup>

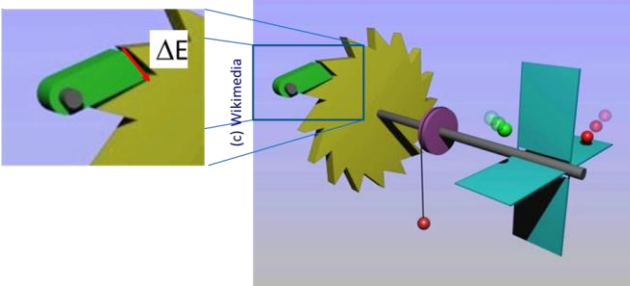
<sup>1</sup>NextPV, LIA, CNRS-RCAST/U. Tokyo-U. Bordeaux, Tokyo, Japan; <sup>2</sup>RCAST, The University of Tokyo, Tokyo, Japan ; <sup>3</sup>CNRS, IPVF, UMR 9006 Palaiseau, France ; <sup>4</sup>Ecole Polytechnique, IPVF, UMR 9006 Palaiseau, France ; <sup>5</sup>Aix Marseille Université, IM2NP UMR 7334, Marseille, France

\* Corresponding author: jf.guillemoles@cnrs.fr

**ABSTRACT** — Although promising, new solar cells concepts such as Intermediate Band Solar Cells have not shown efficiency improvements beyond single junction records so far. A potential path for increasing the performances would be to introduce electronic ratchets, which consists in a slight energy shift within one of the three bands of the system. Considering realistic properties such as sub optimal absorption and non-radiative recombination, we show that intermediate band can result in severe decrease of the performances, while a ratchet state can compensate those non-idealities. This allows us to consider new structures for the practical realization of intermediate band solar cells, such as quantum wells, which have been largely less considered than quantum dots so far.

## I. INTRODUCTION

A ratchet is a concept popularized by Richard Feynman[1], in which a dented wheel is designed in such a way that it can rotate in one direction only. The allowed rotation involves a dissipation of  $\Delta E$  so that the pawl can block the reverse rotation. The wheel can be coupled to blades, which, being sensitive to gas pressure fluctuations, could rotate the wheel so as to lift a weight, thereby producing work from a single heat source (Fig. 1).



**Figure 1:** The principle of a Feynman Ratchet is illustrated. A dented wheel is designed in such a way that it can rotate in one direction only. The allowed rotation involves a dissipation of  $\Delta E$  so that the pawl can block the reverse rotation. The wheel can be coupled to blades, which, being sensitive to gas pressure fluctuations, could rotate the wheel so as to produce work.

This apparent paradox, which opposes the second law of thermodynamics, can be lifted by a closer look into the details of the device. The pawls has to be loose enough to allow the wheel to rotate at all; but then temperature induced fluctuations, can also lift the pawl, and allow the wheel to rotate backwards. At the end of the day, at constant temperature, the device works as an electrical rectifier where the mechanical torque plays the role of the electric field and the angular velocity that of the electrical current.

It is therefore not surprising to see that such a ratchet system can bring significant insights in the context of solar cells, where the same rectifying behavior allows charge separation and thereby energy conversion. And just as in the case of

Feynman's ratchet, a closer look on the details of charge separation in a solar cell has led (and still leads) to lively debates concerning the behavior of the ratchet mechanism – in this case, the built-in potential [2], [3].

In this work, we highlight the role of a ratchet system for advanced concepts in PV. We will mainly focus on Intermediate level Solar Cell (IBSC), an advanced concept [4]–[7], that has been predicted to result in efficiencies of about 46.7% under one sun illumination [6]. We show that adding a ratchet system to such a device appears not as a mere improvement, but as a requirement to overcome the Shockley-Queisser limit [8] with materials currently available. Considering electrical figures of merit, we offer a qualitative and quantitative interpretation of the influence of the ratchet on such systems. This analysis can contribute to a better understanding of the physics at stake behind the ratchet mechanism.

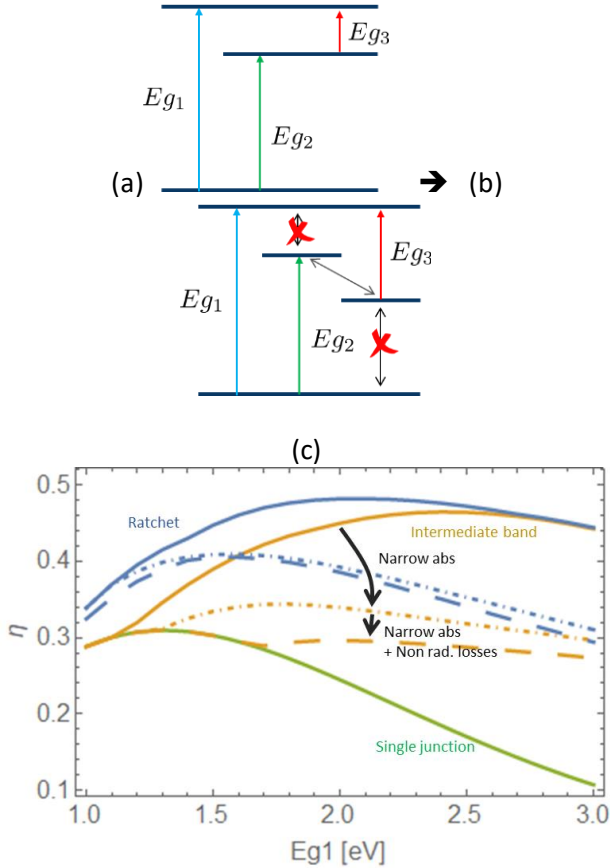
## II. THEORETICAL MODEL

The IBSC is a concept of device where, in parallel to the direct generation of carriers by absorption of photons, these can be generated in two absorption steps via an intermediate level (Figure ). Nevertheless, photogenerated carriers can also recombine back using the intermediate level, that acts as a catalyst for this reaction. The theoretical performance of IBSC is close to that of triple junctions, series connected, but efficient devices have not been demonstrated yet because of current material limitations in absorption efficiency and bandwidth, and because of non-radiative recombination.

In nanostructures (quantum dots (QD) and quantum wells (QW)), which are one of the most considered path to the practical implementation of an intermediate band [9], this can be explained by two intrinsic properties: the reduced absorption energy width between the quantized states and the continuum, as well as increased non-radiative recombinations. As a consequence, a  $V_{oc}$  drop and a limited current increase are commonly observed. We have quantified [10] the impact of those two properties on the expected efficiencies, and highlighted that currently considered

structures are not compatible with efficiencies in excess of the SQ limit.

It has been suggested that a ratchet mechanism can increase the efficiency of an IBSC [10]–[15]. When implemented on the intermediate band (as in Figure (b)), although implementation on the conduction or valance band can be also considered [14]), a ratchet consists in an additional state at a slightly lower energy, from which recombination to the valance band is forbidden. In case of reduced absorption strength, it has been further demonstrated that the efficiency reduction becomes less pronounced [14]. However, the effect on the non-radiative recombination has been given less consideration so far [12], despite a  $V_{oc}$  loss being regularly reported in practical realization of IBSC.



**Figure 2** Band diagram of (a) an IBSC and (b) an RBSC with a ratchet implemented in the IB. (c) Efficiencies of the single junction (full green line), IBSC and RBSC, as a function of the largest gap value ( $E_{g1}$ ), in the radiative limit and for an ideal absorption (respectively full orange and blue lines), with a narrow absorption ( $\delta E = 250$  meV, orange and blue dotted lines), with a narrow absorption and non-radiative recombination ratio of  $10^{-3}$  for the transition  $E_{g3}$  (dashed orange and blue lines).

To account for these effects, the bandgap configuration and the notations of Figure 2 (a) are considered. The limit efficiencies are calculated following a method similar to [13], to which the non-ideal behavior of the nanostructures will be added. For each transition  $i$ , the absorption  $G_i$  is given by the convolution of the absorption  $a_i$  and the sun spectrum, approximated by the black body radiation flux at a temperature  $T_{sun} = 6000$  K. We consider the efficiencies in

non-concentrated light. The radiative emission  $R_i$  for each transition  $i$  is given by the generalized Planck's law, for  $T_{cell} = 300$  K and using the quasi-Fermi level splitting for each bandgap,  $\Delta\mu_i$ .

The transitions associated with the bandgap  $E_{g1}$  and  $E_{g2}$  are considered ideal, that is,  $a_1=1$  strictly above  $E_{g1}$ , and  $a_2=1$  strictly between  $E_{g2}$  and  $E_{g1}$ , whereas their recombination is purely radiative. Non-idealities will be considered for  $E_{g3}$ . This will mimic the nanostructured devices in which the intermediate band is obtained thanks to quantized states in the conduction band, such as the widely studied InAs QDs in GaAs [9]. For this transition, both absorption and recombination are assumed only between  $E_{g3}$  and  $E_{g3}+\delta E$  where  $\delta E$  is the absorption energy width. Moreover the recombination is increased by considering a radiative recombination ratio  $r_{rad}$  such that  $R_3^* = \frac{1}{r_{rad}} R_3$ .

The full model can be found in [10], [13], [16]. It is firstly used to numerically compute I-V curves and efficiencies for given sets of bandgaps, which allows finding the best configurations. Another solution is to solve the system analytically, in the framework of Lagrange multipliers, which provides additional equations by explicitly considering the system constraints (matching of the currents through  $E_{g2}$  and  $E_{g3}$ ,  $\Delta\mu_1 = \Delta\mu_2 + \Delta\mu_3$ ).

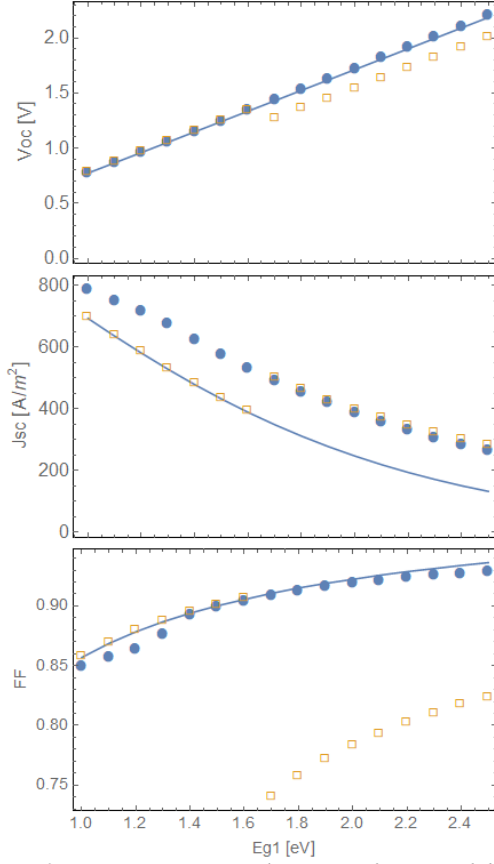
### III. RESULTS

On Figure (c) are represented the efficiency as a function of  $E_{g1}$ , for the single junction, the IBSC and the RBSC. The position of the intermediate level and of the ratchet is optimized for highest efficiency. The full lines represent the efficiencies in the ideal configuration ( $r_{rad}=1$ , unlimited  $\delta E$ ). Already in that configuration, it is observed that the implementation of a ratchet can result in an efficiency improvement. When the absorption width is reduced ( $\delta E = 250$  meV), an efficiency reduction is observed for both the IBSC and the RBSC. When considering in addition a non-radiative recombination ratio of  $r_{rad}=10^{-3}$  for  $E_{g3}$ , we observe that the IBSC gives efficiencies lower than what can be achieved with the best single junction. Oppositely, we find that the introduction of the reduced radiative efficiency has a negligible impact on the RBSC performances.

A more detailed study [10] shows that a ratchet makes the cell tolerant to non-ideal characteristics, to that point that any value of the absorption width and radiative recombination ratio is compatible with efficiencies in excess of the Shockley-Queisser limit. This result gives new opportunities to realize IBSC with quantum structures. So far, QD have been preferred to QW for the practical implementation of IBSC, since the former are expected to exhibit larger radiative recombination ratios. We show here that when a ratchet system can be included, the reduced radiative efficiency of the QW can be acceptable to overcome the SQ limit, thanks to their larger expected absorption.

For a better understanding of the mechanisms at stake, the  $V_{oc}$ ,  $J_{sc}$  and FF values are compared in Figure , instead of the aggregated efficiency value. As could be seen on Fig 2.c, for too small values of  $E_{g1}$ , the optimal situation in the absence of ratchet aborts the intermediate band and behaves as a single junction. Above this threshold, we observe that the

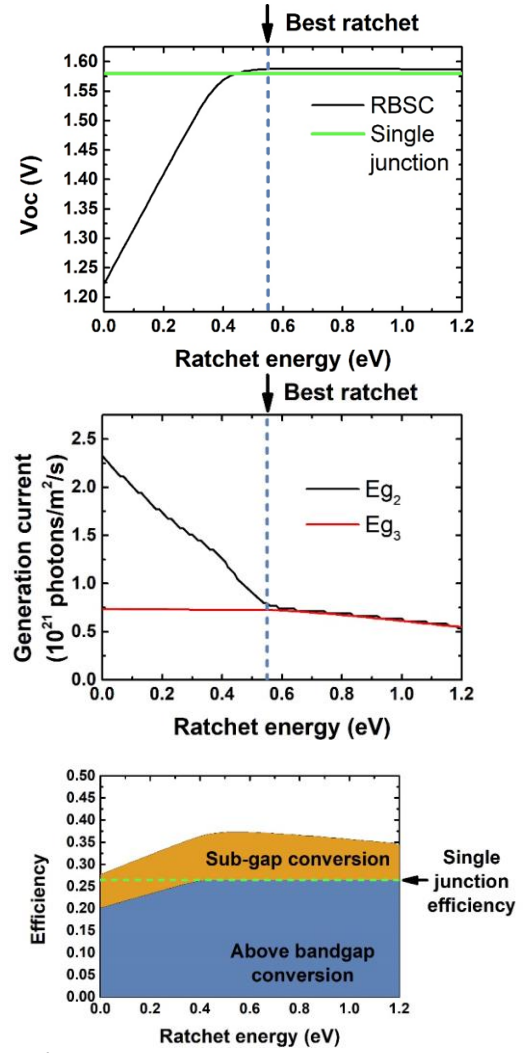
$V_{oc}$  of the cell including a ratchet keeps values close to that of the single junction, whereas the standard IBSC shows values reduced by about 10 %. Conversely, the RBSC gives a  $J_{sc}$  close to that of the IBSC, much above that of SJ, therefore taking advantage of the additional generation from the IB.



**Figure 3** Top: Open-circuit voltage, as a function of the  $E_{g1}$  bandgap, for an IBSC with a ratchet (filled blue symbols) and an IBSC w/o ratchet (open yellow symbols). A narrow absorption ( $\delta E = 250$  meV) and non-radiative recombination ratio of 10-3 are considered for the transition  $E_{g3}$  Middle: same for the short circuit current. Bottom: same for the FF.

These numerical observations have been supported analytically [16]. It has been shown that the introduction of a ratchet, by offering one additional degree of freedom to the system thanks to the  $\Delta E$  adjustable parameter, allows for the simultaneous preservation of the open-circuit voltage and the current matching of the transition associated to  $E_{g2}$  and  $E_{g3}$ . Oppositely, a standard IBSC cannot fulfill those two criteria, resulting in a trade-off providing lower performances. This is illustrated in Figure , where the global open-circuit voltage, the generation through the sub- $E_{g1}$  transitions ( $E_{g2}$  and  $E_{g3}$ ) and the energy conversion are represented as a function of the ratchet energy. For the energy conversion graph, we have differentiated the energy provided by the largest gap ( $E_{g1}$ ) and the energy provided by the two lowest gaps (together  $E_{g2}$  and  $E_{g3}$ ). In those graphs, we fixed  $\delta E = 200$  meV and  $r_{rad}=10^{-3}$ .  $E_{g1}$  is also fixed at 1.86 eV, which is the value that optimizes the IBSC efficiency. We observe that the ratchet is at the same time able to achieve current matching ( $G_2$  equaling  $G_3$ ) and to optimize the

recombination, the  $V_{oc}$  reaching a plateau, equivalent to the single junction at a similar  $E_{g1}$ .



**Figure 4** Evolution of recombination, generation and conversion efficiency as a function of the ratchet value, for  $E_{g1}$  fixed at 1.86 eV, which is the optimal value for an IBSC when the absorption width is 200 meV and the radiative efficiency  $10^{-3}$ .  $E_{g2}$  is optimized for each ratchet value. Top:  $V_{oc}$  as a function of ratchet energy  $\Delta E$ . The green line represents the value of the single junction for the same  $E_{g1}$ . Middle: photogenerated current via transition 2 (middle) and 3 (small gap) as a function of  $\Delta E$ . Bottom: fraction converted by the  $E_{g1}$  transition and fraction converted with the help of the intermediate band (i.e. converted by  $E_{g2}$  and  $E_{g3}$ ). The green dashed line represents the efficiency of the single junction with the same  $E_{g1}$ .

For an implementation of a ratchet in real world, it is needed that some transitions must be forbidden (Figure ), and this calls for specific selection rules. They may be spatial, in momentum space, or spin related [9]. Structure with quantum cascade, exhibiting spatial separation have been demonstrated experimentally recently [17]. Structures using spin selection rules could be realized in principle with dilute magnetic semiconductors [12], albeit in practice it is hard to obtain long minority carrier lifetimes and high Curie temperatures in these materials. Finally, another unexplored possibility is some 2D materials (MoS<sub>2</sub> nanoribbons) that



could exhibit relevant selection properties in reciprocal space [18].

These conclusions were obtained with detailed balance calculations using the generalized Planck law. When more elaborate models are used, such as NEGF are used [19], an additional  $V_{oc}$  loss is found due to broadening of the final states that leads to increased recombination. Moreover,  $J_{sc}$  losses from lower optical absorption were also found.

#### IV. DISCUSSION

Several interpretations are often considered to explain the influence of a ratchet. It is sometimes argued that the ratchet induces an energy dissipation  $\Delta E$  as carriers relax from the top to the bottom of the shifted intermediate band. However, this picture does not hold when considering the full process driving a carrier from the valence to the conduction band. In an IBSC, when absorbing two photons with energies  $E_{\gamma 1}$  and  $E_{\gamma 2}$ , the carrier will dissipate  $(E_{\gamma 1} - E_{g2})$  when relaxing after the first transition from VB to IB and  $(E_{\gamma 2} - E_{g3})$  when relaxing after the second transition from IB to CB. In an RBSC, the carrier would first dissipate  $(E_{\gamma 1} - E_{g2})$ , then  $\Delta E$  through the ratchet, then  $(E_{\gamma 2} - (E_{g3} + \Delta E))$  over the second transition. The total amount of dissipated energy is unchanged; what changes is the band in which this energy is dissipated, and the spectral range of absorbed photons.

It is also worth noting that, in some conditions, the optimal ratchet can be negative (see Figure 5). In this case, carriers brought to the intermediate band have to climb up a potential barrier, gathering energy from the ambient temperature, before they undergo a second transition to the conduction band. This situation occurs when photogeneration  $G_3$  is initially so low that its increase compensates the additional recombination induced by  $\Delta E < 0$ . While this situation is purely conceptual (an appropriate treatment would require considering the influence of populations on the absorptivity), it highlights the limits of an interpretation based on relaxation.

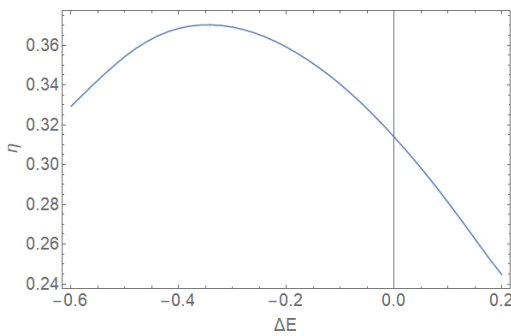


Figure 5 Power conversion efficiency as a function of the ratchet  $\Delta E$  in the ideal case with  $E_{g1} = 2$  eV and  $E_{g2} = 1.1$  eV.

Ratchet have also been suggested to reduce the “Boltzmann” entropy creation [13], which is due to the geometrical mismatch between the absorption and emission optical étendues. As concentration is increased, it appears indeed that the role of the ratchet becomes more and more limited in the ideal case [13], even if a direct link with the absorption and emission étendues mismatch is not obvious. This numerical observation on the impact of concentration

can be expanded with the other non-idealities considered above. We have found that the ratchet remains useful even under full concentration when non-radiative recombination (which produce additional entropy) are included, but not when considering a narrow absorption (which does not produce additional entropy). While there is a clear role of the ratchet energy to improve net current photogeneration through the IB while keeping current matching, the numerical observation above may also support the idea that the ratchet helps mitigating entropy production in the system.

#### V. CONCLUSION

We have discussed the ratchet analogy that has been proposed in the context of intermediate band solar cell. In this course, we have quantified the impact of non-radiative recombination and reduced absorption on the efficiency of nanostructured IBSC. The impact of those two intrinsic deficiencies result in strong performance reductions, unless an electronic ratchet is introduced, in which case efficiencies in excess of the SQ limit can be expected.

We have analyzed in depth the origin of the action of the ratchet on efficiency and concluded after careful examination of the proposed explanations that the main actions are (i) matching of the currents in the 2 step photogeneration process and (ii) reduction of the recombination losses.

These conclusions were obtained with detailed balance calculations using the generalized Planck law. When more elaborate models are used, such as NEGF, other factors affecting recombination and generation were found that also serendipitously pointed out to additional beneficial action of the ratchet.

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