

Logarithmic mathematical morphology: a new framework adaptive to illumination changes

Guillaume Noyel

To cite this version:

Guillaume Noyel. Logarithmic mathematical morphology: a new framework adaptive to illumination changes. CIARP2018 - 23rd Iberoamerican Congress on Pattern Recognition, Nov 2018, Madrid, Spain. , 2018. hal-01957566

HAL Id: hal-01957566 <https://hal.science/hal-01957566>

Submitted on 17 Dec 2018

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

Logarithmic Mathematical Morphology: a new framework adaptive to illumination changes

Guillaume Noyel International Prevention Research Institute - iPRI, Lyon, France | Strathclyde Institute of Global Public Health, University of Strathclyde, Glasgow, UK Correspondence: guillaume.noyel@i-pri.org

Abstract

- LIP is a model based on the Transmittance Law which is adapted to process images
- LIP is consistent with the Human Visual System

Let f, g be two images defined on $D \subset \mathbb{R}^N$ with values in $[0, M[, M \in \mathbb{R}$

• the transmittance is related to the grey level by

The negative values $\triangle f$, with $f > 0$, are light intensifiers that can be used to compensate the light attenuation due a variation of exposure-time (or light intensity).

$$
T_f(x) = 1 - \frac{f(x)}{M}
$$
 (1)

• the transmittance law is

 $T_{f \triangle q} = T_f \times T_g$ (2)

• Equation (2) and (1) gives the sum law

$$
f \triangle g = f + g - \frac{f \cdot g}{M}
$$

(3)

 $\delta_b^{\mathbb{A}}(f)(x) = \mathsf{V} \{f(x-h) \mathbb{A} b(h), h \in D_b\}$ $\varepsilon_b^{\mathbb{A}}(f)(x) = \Lambda \{ f(x-h) \triangle b(h), h \in D_b \}$ form an adjunction $(\varepsilon_{b}^{\hat{\mathbb{A}}},\delta_{b}^{\hat{\mathbb{A}}})$, with $\varepsilon_{b}^{\hat{\mathbb{A}}}$ an erosion and $\delta_{b}^{\hat{\mathbb{A}}}$ a dilation. $\varepsilon_b^{\mathbb{A}}$ is called a logarithmic-erosion and $\delta_b^{\mathbb{A}}$ a logarithmic-dilation.

As $(\varepsilon_b^{\mathbb{A}})$, $\delta^{\mathbb{A}}_b$) is an adjunction,

- $\gamma_b^{\mathbb{A}} = \delta_b^{\mathbb{A}} \varepsilon_b^{\mathbb{A}}$ is an opening called logarithmic-opening
- $\varphi_b^{\mathbb{A}} = \varepsilon_b^{\mathbb{A}} \delta_b^{\mathbb{A}}$ is a closing called logarithmic-closing

Relation with classical Mathematical Morphology

The logarithmic-dilation $\delta^\mathbb{A}_b$ and the logarithmic-erosion $\varepsilon^\mathbb{A}_b$ are related to the dilation $\delta^{\mathbb{A}}_b$ and erosion $\varepsilon^{\mathbb{A}}_b$ by: $\delta^{\mathbb{A}}_b(f)(x) = M(1 - \exp(-\delta_{\acute{b}}\acute{f}))$ and $\varepsilon^{\mathbb{A}}_b(f)(x) = M(1 - \exp(-\varepsilon_{\acute{b}}\acute{f}))$ $\bigg)\bigg)$ where $\hat{f} = -\ln(1 - f/M)$, $\hat{f} \in \overline{\mathbb{R}}$.

Results

Adaptivity to illumination changes

• From equation (3), a LIP-negative function is deduced

$$
\Delta f = \frac{-f}{1 - f/M} \tag{4}
$$

• From equations (4) and (3), the difference law is deduced

$$
f \triangle g = \frac{f - g}{1 - g/M} \tag{5}
$$

A strong physical property

A new set of mathematical morphology (MM) operators adaptive to illumination changes caused by variation of exposure time or light intensity is defined thanks to the Logarithmic Image Processing (LIP) model. This model based on the physics of acquisition is consistent with human vision. The fundamental operators, the logarithmic-dilation and the logarithmic-erosion, are defined with the LIP-addition of a structuring function. The combination of these two adjunct operators gives morphological filters, namely the logarithmic-opening and closing, useful for pattern recognition. The mathematical relation existing between "classical" dilation and erosion and their logarithmic-versions is established facilitating their implementation. Results in simulated and real images show that logarithmic-MM is more efficient on low-contrasted information than "classical" MM.

Logarithmic-Mathematical Morphology

Let $\bar{\mathcal{F}} = [-\infty, M]^D$ be the lattice of functions with values in $[-\infty, M]$ Let $f \in \overline{\mathcal{F}}$ be a function and $b \in]-\infty$, M $[{\rm D}_{\rm b}$ a structuring function , the mappings defined in $\mathcal F$ by

Logarithmic Image Processing (LIP)

- Complementation of the images
- Morphological gradient
- $f^c = (M 1) f$ ^c) = $\delta_b(f^c) - \varepsilon_b(f^c)$ • Logarithmic-morphological gradient $\varrho_b^{\mathbb{A}}(f^c)$ $\frac{A}{b}(f^c)\bigtriangleup \varepsilon_b^A(f^c)$

Visit us at www.i-pri.org

The logarithmic MM operators are adaptive to illumination changes caused by a variation of the camera-exposure time or the source intensity.

O iPRI - International Prevention Research Institute, 95 Cours Lafayette, 69006 Lyon, France - Tel: +33472171199 | Web: www.i-pri.org | Email: info@i-pri.org - Poster ref: v080 2018/11/15

"Drevention is better than healing because it saves the labour of being sick." Chemas Adams, 1680

Mathematical Morphology (MM)

Let $f: D \to [0; M]$ be a grey level image and $b: D_h \to [0, M]$ a structuring function (invariant under translation (in D)), the dilation δ and erosion ε , are usually defined in the lattice $(\overline{\mathbb{R}}^D,\leq)$ by : $\delta_h(f)(x) = \vee \{ f(x - h) + b(h) , h \in D_h \}$ $\varepsilon_h(f)(x) = \Lambda \{f(x-h) - b(h), h \in D_h\}$

Adjunction

 $(\varepsilon_h, \delta_h)$ is an adjunction because it satisfies

 $\forall f, g \in \overline{\mathbb{R}}^D$, $\delta_b(f) \leq g \Leftrightarrow f \leq \varepsilon_b(g)$

As $(\varepsilon_b, \delta_b)$ forms an adjunction:

- $\gamma_b = \delta_b \varepsilon_b$ is an opening (increasing, anti-extensive and idempotent)
- $\varphi_b = \varepsilon_b \delta_b$ is a closing (increasing, extensive and idempotent)

Conclusion

Fig. Comparison between the classical MM and the Logarithmic-MM

Robustness to illumination changes caused by variation of the camera exposure-time