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Effect of inclination on heat transfer coefficient during flow boiling in a mini-channel

Thibaut Layssac¹, Stéphane Lips^{1*}, and Rémi Revellin¹

¹ Univ Lyon, CNRS, INSA-Lyon, CETHIL UMR5008, F-69621, Villeurbanne, France * mailto:stephane.lips@insa-lyon.fr

Abstract

An experimental study of heat transfer during R245fa flow boiling is carried out in a 1.6 mm inner diameter circular channel (198 original data points). The test section is composed of a sapphire tube coated with ITO, which enables a total transparency of the evaporator in the visible spectrum. The acquisition of the outer wall temperature field is ensured by means of an infrared camera and the heat transfer coefficient is calculated by means of a local thermal model. The effect of the inclination on the heat transfer is presented and discussed for various vapour qualities and mass velocities and a saturation temperature of 81° C, corresponding to a Bond number of 4.1. For each experimental condition, the mean heat transfer coefficient is calculated for various inclinations from the vertical downward flow (-90°) to the vertical upward flow (+90°). The variation of the heat transfer coefficient are first presented and analyzed in the horizontal case. The heat transfer coefficient variations with the flow parameters are interpreted in terms of nucleate and convective boiling and these observations are confirmed by the visualisation of the nucleation phenomenon in the evaporator. The inclination has almost no effect on the heat transfer and this lack of effect is finally interpreted in terms of shift between the annular to intermittent flow pattern transition coupled with the nucleate to convective boiling transition.

Keywords: flow boiling, mini-channel, inclination angle, heat transfer coefficient, thermography

Nome	nclature				
Roman	a Letters	Subscripts			
Bd	Bond number	amb	ambient		
d	diameter (m)	bb	black body		
E	enhancement factor (-)	conv	convective		
F	suppression factor (-)	conv,air	natural convection		
<i>Fr</i> _{vap}	vapour Froude number	elec	electric		
G	mass velocity (kg.m ⁻² .s ⁻¹)	i	inner		
М	molar mass (g.mol ⁻¹)	iw	inner wall		
Р	pressure (Pa)	l	linear		
Pr	Prandtl number	meas	measured		
R_l	linear thermal resistance (K.m.W ⁻¹)	пис	nucleate		
Re	Reynolds number	0	outer		
Т	temperature (K)	OW	outer wall		
X	vapour quality (-)	pred	predicted		
z	abscissa (m)	r	reduced		
Greek	Letters	rad	radiative		
α	heat transfer coefficient (W.m ⁻² .K ⁻¹)	sat	saturation		
β	inclination angle (rad)	tp	two-phase		
ε	emissivity (-)	trans	transmitted		
λ	thermal conductivity (W.m ⁻¹ .K ⁻¹)				
ρ	density (kg.m ⁻³)				
σ_{sb}	Stefan-Boltzmann constant (W.m ⁻² .K ⁻⁴)				

 φ heat flux (W.m⁻²)

 $[\]Phi_l$ linear heat transfer rate (W.m⁻¹)

1 Introduction

Two-phase flows with phase change are encountered in many industrial applications, especially considering those using thermodynamic cycles. These cycles can be composed of condensers and evaporators whose efficiency depends on the conditions of the two-phase flow occurring inside. Consequently, the geometrical configuration of these applications affects their performance. In inclined configuration, V-shaped condensers are used for refrigerating applications. The miniaturization of the thermodynamic systems may also require inclined geometrical configurations, in the case of embedded Organic Rankine Cycles for example.

Many studies available in the literature deal with the effect of the experimental conditions on the heat transfer in the cases of heated air-water flow, convective condensation or flow boiling. However, as mentioned in the review of Lips and Meyer [1], the large majority of these studies were carried out for horizontal or vertical flows. Moreover, the few studies dealing with the effect of the inclination on the heat transfer which are cited by Lips and Meyer [1] are focusing on a small range of angles, generally near the horizontal orientation.

The studies of Ghajar and Kim [2], Ghajar and Tang [3] but also the one from Vaze and Banerjee [4] were performed with air-water flows in horizontal and upward flows with inclination angles of 2° , 5° and 7° in a 27.9 mm inner diameter channel. All these studies show a very strong dependency of the heat transfer coefficient with the inclination angle. In these works, two-phase flows were visualised, which enabled an analysis of the effect of the inclination with the various observed flow patterns. It was shown that the heat transfer coefficient was more sensitive to the inclination in the case of a slug flow pattern, with a relative variation of 50% depending on the orientation. Empirical correlations were developed to predict the heat transfer coefficient, taking into consideration the effect of the inclination.

These works were recently completed by the studies of Bhagwat and Ghajar [5,6] for the whole range of inclination. They were conducted with air-water flows in a 12.7 mm inner diameter channel, confirming the strong influence of inclination on heat transfer for low-inertia flows. However, it is shown that the heat transfer is strongly influenced by the inclination not only in the case of an intermittent flow but also with the stratified flows for downward inclinations. In this case, the relative variation of the heat transfer coefficient with the inclination angle may even reach 200% for a gas superficial Reynolds number of 280.

Since the review of Lips and Meyer [1], an intensification of the studies in both flow condensing and flow boiling under inclined configurations was noticed. The main quantitative results of these studies are summarized in Table 1. For each study, the configuration is specified in terms of fluid, inner diameter, geometry and range of tested inclinations. Three main geometrical configurations may be distinguished: the smooth, the corrugated and the multiple channels evaporator. The results of the studies are presented in terms of maximal relative range of variation of the heat transfer coefficient with the

angle of inclination. The configuration which enabled this enhanced effect of the inclination is mentioned in terms of optimal angle of inclination $\beta(\alpha_{max})$, corresponding to the maximal heat transfer coefficient in this configuration. The Bond number and the vapour Froude number (definition of Cioncolini and Thome [7]) corresponding to this configuration are calculated, the lowest values of these two dimensionless numbers being presented in red while the highest ones being presented in green:

$$Bd = \frac{g(\rho_{liq} - \rho_{vap})d_i^2}{\sigma}$$
(1)

$$Fr_{vap} = \frac{\frac{\chi G}{\sqrt{\rho_{vap}}}}{\sqrt{g(\rho_{liq} - \rho_{vap})d_i}}$$
(2)

The Bond number is often used in the literature to make the distinction between mini and macro-channel behaviours. Even if the definition of this kind of criteria is still an open question in the literature, the value of the transition Bond number usually varies from 1 to 4 [8]. The range of variation of the calculated Bond numbers show that the large majority of studies were carried out under macro-channels. As it was observed for heated air-water flows, all the studies about the effect of inclination on the heat transfer coefficient during flow boiling showed a higher dependency of the heat transfer for low-inertia flows, corresponding to low vapour Froude numbers. However, it is observed a relatively high dispersion of the inclination angles that enables to maximize the heat transfer coefficient compared to the little number of studies which were noticed. The effect of inclination on heat transfer, although more recently studied, is not well known and strongly depends on the experimental parameters.

The interpretation and comparison of the results of the three configurations (condensation, gas-liquid flow and flow boiling) must rely on a physical analysis as the heat transfer phenomena can be different for each case. While mostly convective film heat transfer occurs in the case of heated air-water and condensation, nucleate boiling heat transfer is also present during flow boiling. For this reason, due to the coupling between the two heat transfer modes, effect of gravity on flow boiling may be quite different. The comparison between the various configurations may be possible in the case of high vapour quality flows, when convective heat transfer is largely dominant. In addition, a comparison with condensing and heated air-water flows for low vapour qualities may bring a highlight about the effect of convective boiling when nucleate boiling is dominant.

The present paper aims at bringing new insights on the impact of inertial, capillary and gravitational forces on the heat transfer through an experimental study of the effect of inclination angle on heat transfer during flow boiling in a mini-channel. The dependency, or independency, of the heat transfer on the inclination angle is used as a tool to identify the main heat transfer phenomena involved during flow boiling depending on the experimental conditions. The study is based on a test campaign carried out on the effect of the inclination on R245fa flow boiling in a transparent evaporator. The experimental setup and the experimental database are presented in the first section. The effects of the two-phase flow

parameters on the heat transfer coefficient are presented in the second section. Finally, the comparison of the experimental results with asymptotic models available in the literature enables to identify the importance of each heat transfer phenomenon and thus to better understand and explain the experimental results.

2 Test bench description and heat transfer coefficient measurement method

2.1 Description of the test section

The current test section has to ensure the R245fa flow boiling in various conditions, in terms of mass velocity, vapour quality and inclination while the saturation temperature is controlled. The control of the saturation temperature and the mass velocity are ensured by the test bench previously designed by Layssac et al. [23] and presented in Figure 1. The study of the effect of the inclination on the R245fa flow boiling heat transfer is carried out by the mean of an inclinable test section whose schematic is presented in Figure 2. This test section is made of an inclinable aluminium frame, which enables the study of flow boiling for the whole range of inclination. The frame supports the hydraulic loop, which is composed of a preheater and a transparent evaporator. The 2000 mm stainless steel preheater is heated by Joule effect, which enables the control of the vapour quality at the inlet of the evaporator. Due to the low mass velocities and the low heat rates (< 15 W) which were considered in the present study, the calculation of the vapour quality required to take into consideration the preheater and evaporator heat losses. The global heat losses for both these components were obtained by calculating the thermal resistance associated to the transmission of the heat flux to the fluid and the one associated to the heat losses to the surroundings. The final error on the energy balance was less than 5%. Layssac [24] provides more details about the methodology to calculate the heat losses.



Figure 1: Schematic of the test bench

Table 1: Optimal configurations and ranges of variation of the heat transfer coefficient for the studies from the literature

							•	U	
Configuration	Author	Fluid	<i>d</i> _{<i>i</i>} [mm]	Geometry	$[\beta_{min} \beta_{max}]$	$Max(\Delta \alpha / \alpha_{min})$	$\beta(\alpha_{max})$	Bd	Fr _{vap}
Condensation	Lips and Meyer [9]	R134a	8.38	Smooth	[-90° 90°]	50%	-15°	123.0	0.30
	Marchuk et al. [10]	Ethanol	4.8	Smooth	[-90° 0°]	50%	-15°	9.0	0.05
	Mohseni et al. [11]	R134a	8.38	Smooth	[-90° 90°]	80%	30°	115.0	0.08
	Meyer et al. [12]	R134a	8.38	Smooth	[-90° 90°]	100%	-30°	123.0	1.00
	Xing et al. [13]	R245fa	14.81	Smooth	[-90° 90°]	30%	30°	268.0	1.50
	Adelaja et al. [14]	R134a	8.38	Smooth	[-90° 90°]	50%	-30°	145.0	1.30
Gas-liquid	Ghajar and Kim [2]	Air-water	27.9	Smooth	[0° 7°]	90%	5°	106.0	0.05
	Ghajar and Tang [3]	Air-water	27.9	Smooth	[0° 7°]	90%	5°	106.0	0.05
	Vaze and Banerjee [4]	Air-water	27.9	Smooth	[0° 7°]	90%	5°	106.0	0.05
	Bhagwat and Ghajar [5]	Air- water	12.5	Smooth	[0° 90°]	100%	75°	21.0	0.70
	Bhagwat and Ghajar [6]	Air- water	12.5	Smooth	[-90° 0°]	300%	-90°	21.0	0.12
Gas-liquid Flow boiling	Akhavan-Behabadi et al. [15]	R134a	8.92	Corrugated	[-90° 90°]	70%	90°	77.0	0.40
	Wang et al. [16]	HFE7100	0.825	Multiple	[-90° 90°]	50%	45°	0.9	5.80
	Akhavan-Behabadi and Esmailpour [17]	R134a	8.3	Corrugated	[-90° 90°]	60%	90°	67.0	0.40
	Kundu et al. [18]	R134a	7	Smooth	[0° 90°]	15%	90°	58.0	1.00
	Kundu et al. [18]	R407C	7	Smooth	[0° 90°]	15%	90°	60.0	0.30
	Mohseni and Akhavan-Behabadi [19]	R134a	8.9	Smooth	[-90° 90°]	70%	90°	77.0	0.50
	Hsu et al. [20]	HFE7100	0.44	Multiple	[-90° 90°]	50%	45°	0.3	2.60
	Bamorovat Abadi et al. [21]	R245fa	3	Smooth	[0° 90°]	10%	90°	9.0	1.30
	Cheng et al. [22]	R134a	10	Ω grooved	[-90° 90°]	300%	-90°	135.0	0.05

Optimal configuration



Figure 2: Schematic of the inclinable test section (top view)

The study of the effect of the inclination on the R245fa flow boiling heat transfer is carried out with the transparent evaporator and the IR camera (Figure 3). The evaporator is composed of a 200 mm \pm 1.0 mm long sapphire tube which is externally coated with a transparent layer of indium-tin-oxide (ITO). The hydraulic diameter of the evaporator is equal to 1.6 mm \pm 0.15 mm. In the present study, the resistivity of the ITO coating is equal to 450 $\Omega \pm 10 \Omega$ corresponding to a thickness equal to about 1 μ m. The choice of the ITO coating thickness was motivated by a trade-off between its opacity and its resistivity. Moreover, due to the variability of the ITO resistivity with the temperature and aging, both supplied tension and intensity have to be measured during the test campaign. This setup enables the heating of a transparent evaporator by Joule effect.

A global thermal model is necessary to calculate the vapour quality at the middle of the evaporator because the evaporator is not thermally insulated. The choice of avoiding thermal insulation of the evaporator is mainly motivated by the infrared acquisition which would require a harder radiative model with insulation [25]. As for the preheater, the error on the energy balance in the evaporator is less than 10%. The two energy balances result in a mean vapour quality uncertainty of \pm 0.05 in the worst case. The control of the saturation conditions is ensured at the inlet of the evaporator with an absolute pressure transducer whose uncertainty is 0.07 bar and a K type thermocouple whose uncertainty is \pm 0.25 K. The latter is the combination between the uncertainty of calibration (0.1 K) and the estimation of the bias measurement due to the location of the thermocouples on the test set-up. This bias is due to the difficulty to measure the temperature as close as possible to the inlet and outlet of the test section, but avoiding the peek junctions in which heat losses are observed (Figure 3b). The mass flow rate in the test section is measured by means of a Micro Motion Coriolis type mass flowmeter with an accuracy of 0.1 %.



a) Photo



b) Schematic

Figure 3: Photo (a) and schematic (b) of the evaporator

2.2 Infrared measurement

For each condition of mass velocity, vapour quality and inclination angle, the mean heat transfer coefficient at the centre of the evaporator is obtained by means of an IR camera FLIR SC 7000 and a Matlab post-processing. The IR camera is located above the sapphire tube in the case of a horizontal orientation, at a distance of 300 mm from the tube (Figure 4). With this distance and considering a resolution of 512x640 pixels, the maximal zoom enables a precision characterized by a conversion factor of 10 pixels/mm. The electric signal is then coded in 14 bits, which enables to obtain a frame with grayscale values between 0 and 16383. These values are converted into black body temperatures with the software Altair as shown in Figure 5. The rough variations of the black body temperature in the orthogonal direction to the flow are mainly due to the directional emissivity of the ITO, being higher near an angle of emission of 90°.



Figure 4: Top and side views of the IR test section



Figure 5: Black body temperature field

Consequently, longitudinal profiles of black body temperature are obtained by considering the average of the black body temperature field for orthoradial angles of the sapphire tube between 60° and 120° , which corresponds to the region between the two blue lines on Figure 5. Calculating a mean value is necessary to limit the effects of the noises of measurement and the variations of ITO coating thickness.

Considering the direct emission of the ITO coating and the reflexion of the environment of the tube, the digital level *DL* of each pixel of the camera is a function of the sensitivity of the IR camera sensors *F*, the outer wall and ambient temperatures T_{ow} and T_{amb} respectively and the emissivity of the ITO coating:

$$DL = K\sigma_{sb}[\epsilon F(T_{ow})T_{ow}^4 + (1-\epsilon)F(T_{amb})T_{amb}^4]$$
(3)
with *K* a multiplying factor and σ_{sb} the Stefan-Botzmann constant.

The digital level may also be expressed by considering the black body temperature T_{bb} given by the infrared camera, corresponding to a case where there is no reflexion of the ITO coating:

$$DL = K\sigma_{sb}F(T_{bb})T_{bb}^4 \tag{4}$$

The equalisation of equations (3 and (4 enables the following expression of the outer wall temperature:

$$T_{ow} = \left[\frac{1}{F(T_{ow})} \left[F(T_{amb})T_{amb}^{4} + \frac{1}{\epsilon} \left[F(T_{bb})T_{bb}^{4} - F(T_{amb})T_{amb}^{4}\right]\right]^{\frac{1}{4}}$$
(5)

The ambient temperature T_{amb} is given by the three thermocouples set up on the polycarbonate plates located on each side of the test section. The sensitivity of the IR camera sensors F(T) is given by the manufacturer FLIR and was tested in laboratory. The emissivity of the ITO coating is not known a priori and a calibration is then needed. The calibration enables getting the variations of the ITO emissivity with the outer wall temperature and the abscissa of the tube due to the coating heterogeneity. To obtain this emissivity, an outer wall temperature is imposed by heating the tube with a high velocity liquid single-phase flow and is calculated by a local thermal model. For each condition of known outer wall temperature T_{ow} , the emissivity ϵ may be calculated by measuring the corresponding ambient temperature T_{amb} and black body temperature T_{bb} :

$$\epsilon (T_{pe}) = \frac{F(T_{bb})T_{bb}^4 - F(T_{amb})T_{amb}^4}{F(T_{aw})T_{aw}^4 - F(T_{amb})T_{amb}^4}$$
(6)

Profiles of ITO coating emissivity are given for outer wall temperatures of 70°C, 80°C and 90°C in Figure 6. The variations of the emissivity with the abscissa are due to the heterogeneity of the ITO coating. Because of this heterogeneity, the outer wall temperature has to be calculated for each abscissa of the IR visualisation section to be able to obtain the mean heat transfer coefficient for each experimental condition. The outer wall temperature uncertainty is 0.4°C for an ITO coating temperature of 81°C and an ambient temperature of 25°C. This value strongly increases for lower temperatures due to the higher relative part of the radiation flux coming from the environment and the relatively low emissivity of the ITO coating. Consequently, the experiments were carried out with a unique saturation temperature of 81°C.



Figure 6: Variations of the ITO deposit emissivity with abscissa for sapphire outer wall temperature of 70° C, 80° C and 90° C

The heterogeneity of the ITO coating may affect the homogeneity of the imposed heat flux. However, when a heat flux of 13.5 kW.m^{-2} was imposed on the test section, it has been observed a relatively low heterogeneity of the ITO coating temperature as it is shown in the example of Figure 7. The mean standard deviation of the observed distributions for the whole experimental temperature data is 0.25 K and is thus negligible compared to the uncertainty of the wall temperature measurement obtained by the IR camera (0.4 K). The heat flux can thus be considered as homogeneous along the test section. It may be reported that a heat flux of 13.5 kW/m^2 also leads to a maximal variation of the vapour quality of 0.08 on the infrared section, which also ensures the homogeneity of the heat transfer coefficient inside the tube.



Figure 7: Example of variations of the ITO coating temperature $(G = 150 \text{ kg.m}^{-2}.\text{s}^{-1}, x = 0.3, \varphi_{trans} = 13.5 \text{ kW.m}^{-2})$

2.3 Heat transfer data reduction

Outer wall temperature being calculated along the IR visualisation section, it is possible to determine the heat transfer coefficient for each abscissa along this section by a local thermal model. The calculation of the local heat transfer α requires the knowledge of three local quantities: the inner wall temperature T_{iw} , the saturation temperature T_{sat} and the heat flux transfered to the saturated fluid φ_{trans} . Considering a homogenous heat flux, the expression of the heat transfer coefficient at the abscissa z is:

$$\alpha = \frac{\varphi_{trans}}{T_{iw}(z) - T_{sat}(z)} \tag{7}$$

As previously mentioned, the saturation temperature is known at the inlet of the evaporator. Additionally, the pressure drop is measured in the evaporator, which enables the calculation of the saturation temperature at the abscissa *z*, considering a linear evolution of the saturation pressure in the evaporator. This assumption is valid because of the low vapour quality variation inside the test section combined to the fact that the data were obtained in conditions for which the evolution of the pressure gradient is monotonic (far from the its maximum).

In the present test section, the heat flux transfered to the fluid and the inner wall temperature are not measured directly. As a result, a local thermal model is required to calculate them, considering the heat losses of the evaporator (Figure 8). The linear thermal resistances and linear energy flux taken into account in the thermal model are represented in Figure 9.



Figure 8: Thermal model at abscissa z



Figure 9: Electrical equivalent circuit of the local thermal model

This model takes into consideration the sapphire conduction and the heat losses by radiation and by natural convection, which results into the following expressions of the inner wall temperature and the linear heat rate transferred to the flow:

$$\Phi_{l,trans} = \Phi_{l,elec} - \left(\frac{1}{R_{l,rad}} + \frac{1}{R_{l,conv,air}}\right) (T_{ow} - T_{amb})$$
(8)

with $T_{ow} = T_{iw} - R_{l,cond} \Phi_{l,trans}$

where $R_{l,cond}$, $R_{l,rad}$ and $R_{l,conv,air}$ are the linear thermal resistances of conduction in the sapphire, radiation and natural convection respectively. $\Phi_{l,elec}$ is the linear heat flux coming from Joule effect in the ITO coating.

The linear thermal resistance of conduction is calculated by considering a radial conduction in the sapphire:

$$R_{l,cond} = \frac{ln\left(\frac{d_o}{d_i}\right)}{2\pi\lambda_{samphire}} \tag{9}$$

where d_o and d_i are respectively the outer and the inner diameters of the sapphire tube and $\lambda_{sapphire}$ is its thermal conductivity. The value of the thermal conductivity of the sapphire is taken at the saturation temperature.

The linear resistance of radiation is calculated with the emissivity of the ITO coating:

$$R_{l,rad} = \left[\epsilon \sigma_{sb} \pi d_o \left(T_{ow}^2 + T_{amb}^2\right) (T_{ow} + T_{amb})\right]^{-1}$$
(10)
the constant of Stefan-Boltzmann.

The linear resistance of natural convection due to the air circulation around the tube is obtained by calculating the corresponding heat transfer coefficient coming from the correlation of Churchill and Chu [26]:

$$R_{l,conv,air} = \frac{1}{\alpha_{Churchill}\pi d_o} \tag{11}$$

The relative uncertainties of the linear thermal resistances of conduction, radiation and natural convection are respectively 15%, 10% and 25% while less than 10% of the heat flux is lost by radiation and natural convection. Consequently, considering the uncertainties from the local thermal model and the uncertainty of the outer wall temperature, the mean relative error of the heat transfer coefficient is 30% for the whole range of experimental conditions. The test rig performance was validated for single-phase flow configurations (both friction and heat transfer). The results are not presented in the present paper for a sake of clarity, but are available in [24].

2.4 New experimental data points

A test campaign was carried out with a saturation temperature of 81° C with a heat flux of 13.5 kW.m⁻². The choice of these parameters was motivated by considerations about the heat transfer coefficient uncertainty. For each set of mass velocity and vapour quality, the mean heat transfer coefficient along the infrared visualisation section was calculated for inclination angles of -90°, 60°, -45°, -30°, -15°, 0°,

where σ_{sh} is

 15° , 30° , 45° , 60° and 90° . The ranges and the fluctuations of the experimental parameters for each angle of inclination are summarised in Table 2. The fluctuations are calculated as the mean standard deviation of each series of experiment made with a given mass velocity and vapour quality.

Table 2: Ranges of	of experimental	parameters
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	Range	Fluctuations		
Number of data points	198	-		
Heat flux	$\varphi = 13.5 \text{ kW.m}^{-2}$	0.2 kW.m ⁻²		
Hydraulic diameter d	1.6 mm	-		
Saturation temperature T_{sat}	80.9°C	0.2°C		
Mass velocity G	150 - 300 kg.m ⁻² .s ⁻¹	$3 \text{ kg.m}^{-2}.\text{s}^{-1}$		
Vapour quality x	$0.03 \rightarrow 0.85$	0.01		
Inclination angle β	$-90^{\circ} \longrightarrow 90^{\circ}$	$< 0.5^{\circ}$		

The heat flux was chosen sufficiently low to avoid a too large variation of vapour quality in the test section. With a mass velocity of 150 kg.m⁻².s⁻¹, a heat flux of 13.5 kW.m⁻² results in a difference of vapour quality lower than 0.15 between the inlet and the outlet of the evaporator. The vapour quality is then calculated at the middle of the evaporator.

The current ranges of experimental parameters focus on the low inertia driven two-phase flow. This is motivated by the fact that the inclination affects the two-phase flow when the gravity forces are strong compared to inertia forces, which corresponds to a low vapour Froude number. Additionally, the configuration of the study is also characterized by a low diameter compared to the large majority of the previous studies dealing with the effect of inclination on two-phase flows (Table 1). In the present study, the Bond number is equal to 4.2, which corresponds to the case of a mini-channel. However, the effect of inclination on the heat transfer coefficient in the case of flow boiling was still observed with micro-channels (Bd < 1) [16,20].

3 Results and discussion

3.1 Effect of the flow parameters on the heat transfer coefficient Horizontal case

Figure 10 presents the results of the test campaign in terms of variations of the heat transfer coefficient with the vapour quality in the case of horizontal orientation ($\beta = 0^{\circ}$). Results are presented for mass velocities of 150 kg.m⁻².s⁻¹ (red markers) and 300 kg.m⁻².s⁻¹ (blue markers). Note that the relative uncertainty on the measurements increases when the heat transfer coefficient increases because of the lower temperature difference between the wall and the fluid when the vapour quality increases.

For both mass velocities, the heat transfer coefficient increases with the vapour quality. However, the increase is more pronounced in the case of a mass velocity of 300 kg.m⁻².s⁻¹ than for a mass velocity of 150 kg.m⁻².s⁻¹. Despite the important measurement uncertainties, it can be concluded that mass velocity does not affect the heat transfer coefficient for a vapour quality lower than 0.4. A small effect probably exists for higher vapour qualities. All these observations are consistent with the transition between the nucleate boiling and the convective boiling heat transfer mode. With a mass velocity lower than 0.4, heat transfer is insensitive to both vapour quality and mass velocity because nucleate boiling is dominant. For higher vapour qualities, convective boiling becomes dominant and the heat transfer coefficient is thus increased by the vapour phase inertia.



Figure 10: Variations of the heat transfer coefficient with the vapour quality for a mass velocity of 150 kg.m⁻².s⁻¹ (red) and 300 kg.m⁻².s⁻¹ (blue)

The transitions between the two heat transfer modes are observed in the evaporator as it is presented in Figure 11 in the case of horizontal flows. For both mass velocities, with a vapour quality of 0.06, the flow is intermittent and a large amount of little bubbles coming from the nucleation are observed. When the vapour quality increases (x = 0.4), the flow becomes annular but some bubbles coming from the inner wall are still observed. Some of them are highlighted with circles on the figures. These bubbles are more present in the case of a lower mass velocity of 150 kg.m⁻².s⁻¹. With a vapour quality of 0.7, the liquid film becomes thinner and the wall superheat becomes lower. Nucleation at the wall clearly decreases in terms of intensity for G = 150 kg.m⁻².s⁻¹ and even disappeared for G = 300 kg.m⁻².s⁻¹ since no little bubbles are observed around the annular vapour core in the evaporator. The effect of the inclination angle on the flow pattern with and without heat flux is discussed in details in [27] and it appears that the present observations do not depend on the inclination angle.



Figure 11: Pictures of the flow in the evaporator for various mass velocities and vapour qualities $(\varphi_{trans} = 13.5 \text{ kW.m}^{-2} \text{ and } \beta = 0^{\circ})$. The circles highlight area with bubbles due to the nucleate boiling.

Effect of inclination

As it was shown in the literature [2], the heat transfer coefficient may be strongly sensitive to the inclination angle, mainly due to the effect of the gravity forces on the low-inertia flow patterns, such as stratified or intermittent flows. An example of evolution of the heat transfer coefficient as a function of the inclination angle is presented on Figure 12 for a mass velocity of 150 kg.m⁻².s⁻¹ and a vapour quality of 0.54. The range of variation of the heat transfer coefficient is about 20 % for a mean uncertainty of 15 %. Consequently, the inclination effect is very low.



Figure 12: Inclination effect on the heat transfer coefficient for $G = 150 \text{ kg.m}^{-2} \text{.s}^{-1}$ and x = 0.54

The example of Figure 12 actually corresponds to the maximum variation of heat transfer coefficient for the whole set of experiments. Figure 13 presents the variation of the heat transfer coefficient with the vapour quality for various inclination angles and mass velocities of 150 kg.m⁻².s⁻¹ and 300 kg.m⁻².s⁻¹. Although mass velocity and vapour quality affect the heat transfer coefficient, it does not seem impacted by the inclination, whatever the experimental conditions, considering its relative uncertainty in the present study.



b) $G = 300 \text{ kg.m}^{-2}.\text{s}^{-1}$

Figure 13: Variations of the heat transfer coefficient with the vapour quality for inclination angles of -90°, -45°, 0°, 45° and 90° with mass velocities of 150 kg.m⁻².s⁻¹ (a) and 300 kg.m⁻².s⁻¹ (b)

The lack of inclination effect seems to be consistent with the observations of the literature as it is shown in Figure 14. The results are presented in terms of relative variation of the heat transfer coefficient with the inclination angle as a function of the vapour only Froude number for each operating condition of mass velocity, vapour quality, temperature saturation and heat flux. The relative variation of the heat transfer coefficient is defined as the difference between the maximum and minimum heat transfer coefficient divided by the minimum heat transfer coefficient when only the inclination angle varies. These results come from the studies which were made at least under vertical upward and downward configurations to be able to compare the amplitudes of variations of the heat transfer coefficient. Other indicators could be chosen, but the present one enables to maximise the inclination effect and thus to highlight the importance of the gravitational forces on the heat transfer. The results of the experiments made with macro-channels (Bd > 60) show a strong dependency of the heat transfer coefficient with the inclination for low vapour Froude number, corresponding to low-inertia cases. This dependency decreases with the vapour Froude number. In the case of micro-channels (Bd < 1), the relative variations of the heat transfer coefficient with the inclination do not depend on the vapour Froude number. This difference of behaviour may be due to the different phenomenology between micro and macro-channel two-phase flows. In macro-scale [15,17,19,22], the two-phase flow is mainly annular or stratified while in micro-scale slug flows were observed [16,20]. The effect of inclination may be interpreted in terms of partial dry-out of the upper part of the tube in macro-scale. In micro-scale, the stronger effect of capillarity causes the dry-out of the upper part of the tube to strongly decay. In the present case, the intermediate scale (Bd = 4.1) results in a low effect of the inclination which seems to be a limit case of the two observed behaviours. This lack of inclination effect may be also highlighted by considering the relative importance of nucleate and convective boiling in the heat transfers as it is presented in section 3.3.



Figure 14: Relative variations of the heat transfer coefficient with the inclination observed in the literature as a function of the vapour Froude number

3.2 Comparison with asymptotic models

The asymptotic models of the literature consider the variations of the respective intensities of the nucleate boiling and the convective boiling with the experimental conditions to predict the variation of the heat transfer coefficient. To calculate the nucleate boiling term, these models use correlations coming from the pool boiling literature. The convective term is calculated from usual correlations of prediction of the Nusselt number for single-phase flows. The respective weights of the nucleate boiling and the convective boiling are taken into consideration by using two coefficients, generally noted S for the nucleate boiling and E for the convective boiling. For an asymptotic model of order n, the expression of the flow boiling heat transfer coefficient is as follows:

$$\alpha = \left[(S\alpha_{nuc})^n + (E\alpha_{conv})^n \right]^{\frac{1}{n}}$$
⁽¹²⁾

with α_{nuc} the heat transfer coefficient for the nucleate boiling and α_{conv} the heat transfer coefficient for the convective boiling. *S* is the extinction factor, which stands for the weight of the nucleate boiling while *E* is the enhancement factor, which represents the weight of the convective boiling. Consequently, these models are not only able to predict the variations of the heat transfer coefficient with the experimental conditions but also the weights of the nucleate boiling and the convective boiling.

The accuracy of the predictions of eight asymptotic models of the literature was tested for the present dataset. All the details about the correlations, especially the calculation of the extinction factor *S* and the enhancement factor *E*, are provided in [28]. For each model, the accuracy is analysed in terms of Mean Absolute Percentage Error (MAPE), Mean Percentage Error (MPE), Percentage of Experimental Data Captured within \pm 50% (PEDC50), Percentage of Experimental Data Captured within \pm 30% (PEDC30) and Percentage of Experimental Data Captured within \pm 10% (PEDC10). The MAPE and MPE are calculated as follows:

$$MAPE = \sum \left| \frac{\alpha_{pred} - \alpha_{meas}}{\alpha_{meas}} \right| \tag{13}$$

$$MPE = \sum \frac{\alpha_{pred} - \alpha_{meas}}{\alpha_{meas}} \tag{14}$$

The results in terms of statistical indicators are presented in Table 3.

Table 3: Heat transfer coefficient prediction accuracy of eight asymptotic models of the literature

	MAPE [%]	MPE [%]	PEDC50 [%]	PEDC30 [%]	PEDC10 [%]
Chen [29]	57	57	40	10	0
Gungor and Winterton [30]	79	79	20	15	2
Kandlikar [31]	46	-42	51	38	6
Liu and Winterton [32]	32	21	89	36	9
Kandlikar and Balasubramanian [33]	55	-49	39	16	5
Zhang et al. [34]	52	49	66	34	11
Saitoh et al. [35]	34	32	82	34	13
Bertsch et al. [36]	16	9	100	94	29

The model of Bertsch et al. [36] appears to be the best one to predict the variation of the heat transfer coefficient for the present dataset with all the best statistical indicators. The distribution of the predictions of the model of Bertsch et al. [36] for the present experimental database is presented in Figure 15. The particularly good agreement of this model with the experimental data can be explained by the similar experimental conditions of the underlying database of the model. Indeed, the correlation of Bertsch et al. [36] was developed from tests which were carried out with refrigerant flows in micro and mini-channels, corresponding to Bond numbers ranging from 0.06 to 11. It is an asymptotic model based on equation (12) with :

$$n = 1; S = 1 - x; F = 1 + 80(x^{2} - x^{6})e^{-0.6/\sqrt{Bd}}$$

$$\alpha_{nuc} = 55P_{r}^{0.12}(-log_{10}P_{r})^{-0.55}M^{-0.5}\varphi^{0.67},$$

$$\alpha_{conv} = (1 - x)\alpha_{liq} + x\alpha_{vap}$$
(15)
with $\alpha_{j} = \left[3,66 + \frac{0.0668\frac{d}{a}(Re_{j}Pr_{j}^{2})}{1+0.04\frac{d}{a}(Re_{j}Pr_{j}^{2})}\right]\frac{\lambda_{j}}{d_{i}} for j = vap and liq$

$$MAPE = 16\%$$
MPE = 9%
PEDC50 = 100%
PEDC30 = 94%
PEDC10 = 29%
$$\sqrt{\frac{M}{2}} \frac{6000}{6000} + 30\%$$
PEDC10 = 29%
$$\sqrt{\frac{M}{2}} \frac{6000}{2000} - \frac{30\%}{2000} \frac{3000}{6000} = 8000$$
Experimental α [W.m².K⁻¹]

Figure 15: Predictions of the Bertsch et al. [36] model for the present experimental data

3.3 Discussion about the effect of inclination on heat transfer

The asymptotic models are able to predict not only the heat transfer coefficient behaviour but also the effect of the experimental conditions on the respective weights of the two heat transfer modes. As it is impossible to measure directly the importance of each mode, the asymptotic models can be used as a tool to better understand the experimental results. The model of Bertsch et al. [36] being the best asymptotic model to predict the heat transfer coefficient behaviour, it is likely the best to represent well the physics involved in the considered configuration. Its predictions in terms of nucleate boiling and convective boiling can thus be calculated and analysed for the conditions of the experiments. They are

presented on Figure 16 in the case of the data obtained in horizontal configuration with a mass velocity of 150 kg.m⁻².s⁻¹. The transition observed experimentally between annular and intermittent flow is represented by the vertical dashed red line. Representative frames of the flow are presented for vapour qualities of 0.13, 0.3 and 0.7, which illustrates the transitions in terms of flow patterns and intensity of nucleation.

As it is observed in the transparent evaporator, the model of Bertsch et al. [36] predicts the decrease of the nucleate boiling with the vapour quality. Simultaneously, the convective boiling increases. These variations with the vapour quality result in a transition of dominant heat transfer modes for a vapour quality equal to 0.38. the latter is indicated by means of the vertical dashed green line in Figure 16.

In the present study, the transition between the intermittent and the annular flow patterns was observed for a vapour quality of about 0.2 and slightly varied with the inclination. As a consequence, in the present study, it exists three kinds of couplings between the heat transfer modes and the flow patterns:

- In the case of a vapour quality lower than about 0.2, the two-phase flow is intermittent and the dominant heat transfer mode is the nucleate boiling. Nucleate boiling mainly depends on the heat flux and the roughness of the inner wall. It is very slightly affected by the inclination and the effect of the inclination on the heat transfer coefficient is weak.
- For a vapour quality between about 0.2 and about 0.4, the two-phase flow is annular and the dominant heat transfer is nucleate boiling. For the same reason as exposed previously, the inclination does not affect much the heat transfer.
- With a vapour quality higher than about 0.4, the two-phase flow is annular and the dominant heat transfer mode is the convective boiling. The intensity of the convective boiling is directly conditioned by the variations of the thermal boundary layer with the experimental conditions. It may be impacted by the experimental conditions when the liquid film is sufficiently thin. In the present study, the liquid film may be thin in the case of high vapour qualities but in this case, the flow is annular and weakly depends on the orientation. Consequently, the inclination has a low effect on the heat transfer coefficient.

As a conclusion, it seems that the shift between the heat transfer modes and the flow pattern transitions is responsible of the lack of inclination effect on the heat transfer coefficients. An inversion of this shift would enhance the effect of inclination. Indeed, if the nucleate to convective boiling transition would occur at a lower vapour quality than the intermittent to annular flow pattern transition, the dominant heat transfer mode could be convective boiling while the flow would be intermittent. Consequently, both flow pattern and heat transfer mode would be impacted by the inclination, which would enhance the effect of the inclination on heat transfer. This behaviour may be reached for low reduced pressure conditions.



Figure 16: Prediction of the variations of the nucleate and convective heat transfer mode with vapour quality from Bertsch et al. [36] model for $T_{\text{sat}} = 81^{\circ}\text{C}$ and $G = 150 \text{ kg.m}^{-2}.\text{s}^{-1}$

4 Conclusions

Measurements of heat transfer coefficients were carried out in the case of R245fa flow boiling in an inclined mini-channel. The whole range of inclination was tested. The evaporator, composed of a 1.6 mm inner diameter sapphire tube coated with ITO was transparent. It enabled the visualisation of the flow directly in the evaporator and it was possible to observe the nucleation intensity.

The measurement of the outer wall evaporator temperature was ensured by means of an infrared camera and a post-processing. It enabled the acquisition of the temperature profile along the infrared visualisation section. The local heat transfer coefficient was then calculated for each abscissa with a local thermal model considering the heat losses by natural convection and radiation around the evaporator. The acquisition of the mean heat transfer coefficient along the infrared visualisation section was carried out for various experimental conditions in terms of vapour quality (from 0.03 to 0.85) and mass velocity (150 and 300 kg.m⁻².s⁻¹).

The variations of the heat transfer coefficient with both vapour quality and mass velocity were first analysed in the case of a horizontal flow ($\beta = 0^{\circ}$). It was observed that the nucleate boiling and the convective boiling modes were in competition in the present study. This observation was confirmed with the visualisation of the flow in the evaporator. It was observed that the intensity of the nucleation decreased with the inertia of the vapour phase.

The effect of the inclination on heat transfer was then tested and showed to be almost absent in the present study. This observation was interpreted with the intermittent to annular flow pattern transition and the nucleate to convective boiling heat transfer regime transition. The shift between these two transitions was predicted by the model of Bertsch et al. [36] which brought an interpretation to the low effect of the inclination on the R245fa flow boiling heat transfer in the present mini-channel.

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