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Comment on Article by Wade and Ghahramani

Julyan Arbel*, Riccardo Corradin[†] and Michał Lewandowski*

Abstract. We propose a simulation study to emphasise the difference between Variation of Information and Binder’s loss functions in terms of number of clusters estimated by means of (1) the use of the MCMC output only and (2) a “greedy” method.

Wade and Ghahramani’s paper is a very neat contribution to Bayesian cluster analysis in at least two respects: (i) by formalizing cluster credible coverage via Hasse diagrams, and (ii) by recasting the problem in a decision theory framework, with tangible improvements brought by the Variation of Information (VI) loss function (Meilă, 2007) over Binder’s (Binder, 1978; Dahl, 2006).

We propose a simulation study implementing two algorithms provided by Wade and Ghahramani’s package `mcclust.ext` for finding the argument minimizing the posterior expected loss: (1) the *draw algorithm*, which restricts the minimization problem to the MCMC output, and (2) the *greedy algorithm*, which is more reliable as it also scans the neighbouring clusters of the MCMC output, but with a larger computational cost. While increasing the sample size, we point out the radically different behavior of the number of clusters estimated under VI and Binder, especially with the greedy algorithm.

Our simulation study is based on the same data generation as in the first example of Section 6.1 in Wade and Ghahramani (2017): a mixture of four Gaussian distributions equally weighted with means $(\pm 2, \pm 2)$ and identity covariance matrix. We estimated the model using a marginal approach provided by `BNPmix`¹ R package. We synthesised the output with `mcclust.ext` package.² The Dirichlet process mixture model was estimated with mass parameter fixed to 1, and by specifying an independent base measure on locations and scales, with a 0-vector prior mean for the location component and an identity matrix prior mean for the scale component (25 000 iterations with 5 000 burn-in period). We considered four different sample sizes $n = \{20, 40, 100, 300\}$.

The results are shown in Figure 1. With the draw algorithm, the cluster estimates under both losses are quite close in terms of number of clusters. In contrast, the greedy algorithm leads to cluster estimates obtained via Binder’s loss function with excessive size, while that obtained via VI remains coherent with the number of components of the model (four).

Similarly to the authors’ finding, ours’ indicates that Binder’s loss function exhibits an undesirable property of overestimating the number of clusters (Miller and Harrison, 2013, 2014). Variation of Information tends to lessen this problem. As alluded to by the

* Univ. Grenoble Alpes, Inria, CNRS, LJK, 38000 Grenoble, France.

julyan.arbel@inria.fr; michal.lewandowski@inria.fr

[†] DISMEQ, University of Milano Bicocca, 20126 Milano MI, Italy. riccardo.corradin@unimib.it

¹Package available at <https://github.com/rcorradin/BNPmix>, can be installed via `devtools`.

²Code of the simulation study available at <https://github.com/rcorradin/WGdiscussion>.

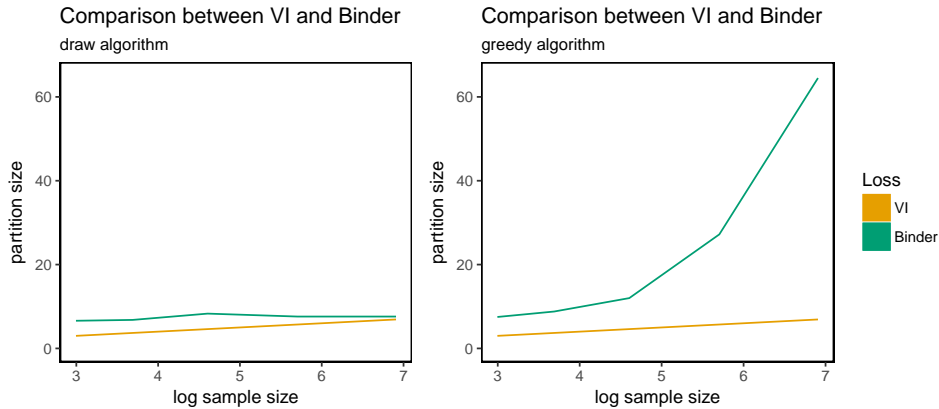


Figure 1: Size of the cluster estimate under VI (yellow line) and Binder (green light). Left: *draw algorithm*. Right: *greedy algorithm*.

authors, a theoretical study of the asymptotic behavior of the VI estimator would be very timely. Especially in light of the recent contribution by [Rajkowski \(2016\)](#) about the asymptotic behavior of the cluster estimator under the 0 – 1 loss (MAP estimator).

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