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REVISITED MODEL FOR INWARD AND OUTWARD GROWTH OF GAS HYDRATE PARTICLES IN WATER-IN-OIL EMULSIONS

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Abstract. The correct prediction of the gas hydrate formation rate is important to estimate pipeline blockage (plugging) in oil and gas production operations. This study presents a revisited model for growth of gas hydrates in water-in-oil emulsions. Literature points out that hydrates form as shells around the water droplets. The water core shrinkage rate (inward growth) is related to gas diffusion through the hydrate shell, while water permeation through the hydrate shell is the limiting phenomenon for outward growth. The models of literature are herein corrected (consideration of gas solubility in the hydrate shell, consideration of gas concentration along the shell coupled with gas consumption in the outer surface, correct coupling between gas absorption by the bulk and gas consumption due to hydrate formation, considering the crystal integration process in the outer particle surface and the mass transfer between the particle and the bulk. The model is compared to experimental data and the trend of the gas consumption due to hydrate formation is validated, though model closure is still an open question.

Keywords: flow assurance, gas hydrates, particle growth, mass transfer

1. Introduction

Gas clathrate hydrates are crystals formed by the imprisonment of gas molecules inside cages of water-bonded molecules [1]. Hydrate formation is usually related to high pressure and low temperature conditions, which is often the case of offshore oil and gas production operations. The presence of natural gas and seawater in the pipelines may cause nucleation of those crystals, which may grow and agglomerate causing partial or complete pipeline obstruction, also known as *pipe plugging*. Plugging due to hydrate formation is considered one of the most challenging flow assurance issues in the oil and gas industry in the last decade [2].

The correct prediction of the hydrate formation rate – with related gas and water consumption rates – is important to assure flow along the pipeline without any partial or complete blockages. Several growth kinetic models have been proposed in literature to estimate the gas hydrate formation rate [see Ribeiro Jr and Lage [3] and Yin et al. [4] for a compilation of kinetic models] whereas fewer of them are predictive models and capable of estimate the particle size evolution in time [5–11]. For gas-oil-water systems, the models are scarce and reduced to growth phenomenon only [7,8]. The kinetic models are said to be apparatus-dependent due to the lack of closure parameters, which are usually micro or meso scale variables of difficult measurement, and therefore all models have a consequent necessity of some sort of curve fitting.

In the present study, the models of Turner et al. [7] and Shi et al. [8] are revisited and extended: (i) the gas solubility in the hydrate shell is considered [12,13]; (ii) the gas concentration distribution along the shell is coupled with the gas consumption in the outer surface, (iii) gas absorption by the bulk is coupled with gas consumption due to hydrate formation [5,6]; (iv) the entire particle population is considered for the hydrate formation rate; (v) and some minor corrections of the literature models are made (use of hydrate properties for growth rates instead of water properties in Gong et al. [9] and Shi et al. [8] and correction of mixed molar and mass basis in Turner et al. [7]).

2. Mathematical model

Water is considered flowing as an emulsion, i.e., small and spherical droplets homogeneously distributed in oil continuous phase [14]. In this kind of system and whenever pressure and temperature conditions are favorable, gas hydrates form as a shell around the water droplets [15], as depicted in Fig. 1(a). The main phenomena associated to growth kinetics of this kind of particle is presented in Fig. 1(b-g). Inner growth is related to gas diffusion through the hydrate shell, which also competes with mass transfer between the particle and the bulk and crystal integration process in the inner surface. The core shrinkage makes water from the core to be expulsed through the hydrate porous shell, thus turning possible crystal integration in the outer surface to happen, with consequent outer growth.

The major assumptions of the model are: (i) the inner and outer surfaces are considered to be at the same temperature as the bulk, although hydrate formation is an exothermic mass change process; (ii) hydrate formation takes place only at the inner and outer surface of the particle, not in the capillaries of the hydrate porous shell; (iii) the hydrate shell is non-deformable; (iv) the particle is spherical; (v) the water expulsion from the water core is due only to core shrinkage, and no capillary-induced flow or head loss in the capillaries are taken into account.

Hydrate is consider to form at a rate proportional to a fugacity (*f*) driving force relatively to the equilibrium condition (*eq.*). The local fugacity is transformed to the local concentration by the use of Henry's constant of the gas in water, defined as H = C/f [mol/(m³Pa)], where C is the concentration in [mol/m³]. Therefore, the gas consumption rate due to hydrate formation in [mol/s] comes:

$$-\frac{dn_g}{dt}\Big|_{hyd} = k_i A_i \left(f - f_{eq}\right) = k_i A_i \left(\frac{C}{H_w} - f_{eq}\right)$$
(1)

where H_w is related to Henry's constant of the gas inside water, A_i is the interfacial surface of the growing surface and k_i is the constant of proportionality of the crystal integration process (related to the time it takes for the gas and water to form the hydrogen bonds of the hydrate crystalline structure; or yet the time a growth unit takes to be integrated to the already existent crystal structure; Mersmann, 2001). The local concentration *C* comes from mass transfer modeling.

Gas diffusion along the hydrate shell is modeled by Fick's Law in spherical coordinates, Eq. (2). The boundary conditions are shown in Eq. (3) and are interpreted as following: (i) the gas diffused through the hydrate shell is consumed by the crystal integration process in the inner surface; and (ii) the gas transferred between the outer surface of the particle and the bulk will be consumed by both inner and outer growth.

$$\frac{d}{dr}\left(r^2\frac{dC_h}{dr}\right) = 0\tag{2}$$

$$-\underbrace{D_{h}A_{in,i}\frac{dC_{h}}{dr}\Big|_{r=r_{in}}}_{\text{molar diffusion rate through the hydrate shell}} = -\underbrace{k_{i}A_{in,i}\left(\frac{C_{h}\Big|_{r=r_{in}}}{H_{w}} - f_{eq}\right)}_{\text{gas consumption due to crystal integration in the inner surface}}; -\underbrace{D_{h}A_{out,i}\frac{dC_{h}}{dr}\Big|_{r=r_{out}}}_{\text{molar diffusion rate through the hydrate shell}} = \underbrace{h_{m}A_{out,i}\left(\frac{C_{h}\Big|_{r=r_{out}}}{S_{h}} - C_{b}\right)}_{\text{gas mass transfer between bulk and particle}} - \underbrace{\frac{dn_{g,i}}{dt}\Big|_{out}}_{\text{gas consumption due to outer growth}}$$
(3)

where D_h is the gas diffusivity in the hydrate shell, C_b is the gas concentration in the bulk phase, S_h is the gas solubility inside hydrate in [mol of gas/mol of hydrate for a given pressure], indexes *in* and *out* refer to inner and outer surface of the particle and index *i* refers to one particle only. The gas concentration distribution along the hydrate shell then comes:

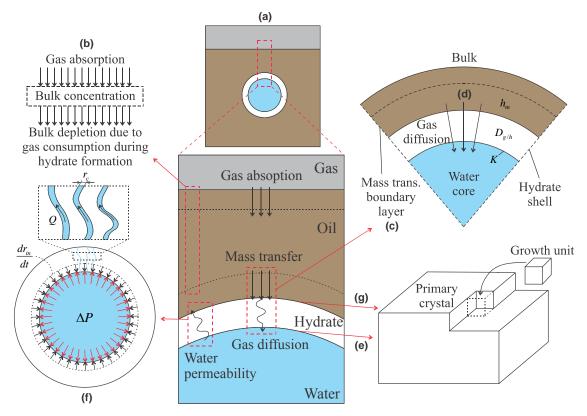


Figure 1. (a) Gas hydrate shell formed around a water droplet in oil continuous phase, which is in contact with the gas free phase. (b) Gas absorption by the bulk competes with gas consumption due to hydrate formation. (c) Gas consumption due to hydrate formation creates a concentration boundary layer around the particle. (d) Gas diffuses through the hydrate shell. (e) Once the gas reaches the inner surface, crystal integration process takes place, causing inner growth. (f) Core-shrinkage makes water to be expulsed through the porous hydrate shell. (g) Once water reaches the outer surface, crystal integration process happens with consequent outer growth.

$$C_{h} = C_{eq} + \frac{\left[\frac{1}{r_{in}} - \frac{1}{r} + \frac{1}{r_{in}^{2}} \frac{H_{w}D_{h}}{k_{i}}\right]}{\left[\frac{1}{r_{in}} - \frac{1}{r_{out}} + \frac{1}{r_{out}^{2}} \frac{S_{h}D_{h}}{h_{m}} + \frac{1}{r_{in}^{2}} \frac{H_{w}D_{h}}{k_{i}}\right]} \left[\left(S_{h}C_{b} - H_{w}f_{eq}\right) - \frac{S_{h}}{h_{m}} \frac{1}{4\pi r_{out}^{2}} \left(-\frac{dn_{g,i}}{dt}\right) \right]$$
(4)

The gas molar flux through the hydrate shell equals the amount of gas consumed to form hydrates in the inner growth and comes from derivation the concentration distribution, as showed in Eq. (5) (left). Yet knowing that hydrate formation follows the (pseudo)-stoichiometry of $1G + \eta H_2 O \rightarrow (1+\eta)Hyd$, where η is the hydration number and is related mainly to the hydrate crystalline structure, then the hydrate formation rate can be related to the gas consumption rate, Eq. (5) (right). The word pseudo-stoichiometry is used because η may vary during hydrate growth depending on the occupancy factor of the gas molecules in the water cages, but for simplification purposes η is considered constant in this study. Furthermore, the linear growth rate of the inner surface of the particle $-dr_{in}/dt$ is related to the molar hydrate formation rate, Eq. (6).

$$\frac{dn_{g,i}}{dt}\Big|_{in} = 4\pi r_{in}^2 D_h \frac{dC_h}{dr}\Big|_{r=r_{in}} \quad ; \quad \frac{dn_h}{dt}\Big|_{in} = (\eta+1)\left(-\frac{dn_g}{dt}\Big|_{in}\right) \tag{5}$$

$$\frac{dn_{h,i}}{dt}\Big|_{in} = -\frac{\rho_h}{M_h} \frac{d}{dt} \left(\frac{4}{3} \pi r_{in}^3\right)_{\text{core volume}} \rightarrow -\frac{dr_{in}}{dt} = \frac{1}{4\pi r_{in}^2} \frac{M_h}{\rho_h} \frac{dn_{h,i}}{dt}\Big|_{in}$$
(6)

where ρ is the density, *M* is the molar mass and index *h* refers to the hydrate phase. It is important to notice that Eq. (6) is corrected from Gong et al. [9] by using the hydrate properties and not the water properties (water properties are mistakenly used when considering that the water core shrinks; while actually it is the hydrate shell that grows inwardly). From Eqs. (5) in (6), the inner growth rate comes:

$$-\frac{dr_{in}}{dt} = (\eta + 1)\frac{M_{h}}{\rho_{h}}\frac{\left(S_{h}C_{b} - H_{w}f_{eq}\right) - \frac{S_{h}}{h_{m}}\frac{1}{4\pi r_{out}^{2}}\left(-\frac{dn_{g,i}}{dt}\right)_{out}}{\left[\frac{r_{in}^{2}}{D_{h}}\left(\frac{1}{r_{in}} - \frac{1}{r_{out}}\right) + \frac{H_{w}}{k_{i}} + \frac{S_{h}}{h_{m}}\frac{r_{in}^{2}}{r_{out}^{2}}\right]}$$
(7)

This expression is the corrected and extended form of Eq. (3) of Shi et al. [8] considering hydrate properties instead of water, the outer consumption of gas, the mass transfer between the particle and the bulk and the gas solubility inside the hydrate shell. When considering that gas diffusion through the hydrate shell is the limiting factor, that no outer growth happens, that the equilibrium concentration is near zero, Eq. (7) converges to Eq. (12) of Turner et al. [7], where the hydrate molar mass M_h should be used for not mixing molar and mass basis.

Outward growth is limited to water availability in the outer surface, which is in contact with the oil. Shi et al. [8] considered a capillary-induced flow through the hydrate porous shell that drains out water from the core (hydrophilic nature of gas hydrate). However, the consideration of a rigid shell as did by them would imply in not respecting the water mass balance of the water inside the particle core, since the capillary-induced flow is independent on the inward growth. Considering no head loss in the capillaries, the water volumetric flowrate through the hydrate shell is the difference between the core volume shrinkage and the amount of water consumed to form hydrates, which are related to the inner growth rate as:

$$Q = \left(-\frac{d\forall_{core}}{dt}\right) - \left(-\frac{d\forall_{w}}{dt}\Big|_{in}\right) \Rightarrow Q = 4\pi r_{in}^{2} \left[1 - \frac{\eta}{(\eta+1)} \frac{M_{w}}{M_{h}} \frac{\rho_{h}}{\rho_{w}}\right] \left(-\frac{dr_{in}}{dt}\right)$$
(8)

This expression is only valid if a rigid shell is considered, where capillary-induced flow would quickly stops due to a depressurization of the core and consequent counter-acting force from outside to inside of the core. However, capillary-induced flow may deform the shell and, if a fully deformable shell is considered, then the capillary-induced flow relates to the core volume deformation so as to maintain pressure of inner and outer surfaces. The capillaryinduced flow is however dependent on capillary parameters such as radius, tortuosity and density of capillaries, which evolve in time (porous will fill-up with time). Probably the hydrate shell is not fully deformable neither fully rigid and both mechanisms will happen together. To avoid any capillary parameters, the assumption of rigid shell is herein considered.

Once the permeation rate of water through the hydrate shell is known, the gas consumption due to outer growth comes:

$$-\frac{dn_{g,i}}{dt}\Big|_{out} = \min\left[\frac{\rho_w}{\eta M_w}Q; 4\pi r_{out}^2 k_i \left(\frac{C_{out,o}}{H_o} - f_{eq}\right)\right]$$
(9)

where at the maximum, all the permeated water will be converted into hydrates instantly (assumption of Shi et al., 2010); but if enough water arrives at the particle outer surface, then crystal integration process may limit outer growth. The gas concentration in the outer surface in the oil phase is $C_{out,o} = C_h |_{r=r_{out}} / S_h$, and by evaluating Eq. (4) at $r = r_{out}$:

$$-\frac{dn_{g,i}}{dt}\Big|_{out} = \min\left[\frac{\rho_w}{\eta M_w}Q; 4\pi r_{out}^2 \frac{k_i}{H_o} \frac{1}{S_h} \left(k_{out} \left(C_b - H_w f_{eq}\right) + \left(1 + \frac{k_i}{H_o} k_{out}\right) \left(H_w - S_h H_o\right) f_{eq}\right)\right]$$
(10)

$$k_{out} = \left[1 + \frac{1}{h_m} \frac{k_i}{H_w} + \frac{\frac{S_h}{h_m} \frac{r_{in}^2}{r_{out}^2}}{\frac{r_{in}^2}{D_h} \left(\frac{1}{r_{in}} - \frac{1}{r_{out}}\right) + \frac{H_w}{k_i}} \right]^{-1}$$
(11)

and by considering Eqs. (5) and (6) for the outer radius, the outer growth rate comes:

$$\frac{dr_{out}}{dt} = \frac{(\eta+1)}{4\pi r_{out}^2} \frac{M_h}{\rho_h} \min\left[\frac{\rho_w}{\eta M_w} Q ; 4\pi r_{out}^2 \frac{k_i}{H_o} \left(k_{out} \left(C_b - H_w f_{eq}\right) + \left(1 + \frac{k_i}{H_o} k_{out}\right) \left(H_w - H_o\right) f_{eq}\right)\right]$$
(12)

Knowing the inner and outer growth rate, Eqs. (7) and (12) (valid for one single particle), the hydrate formation rate of the entire particle population is estimated by Eq. (13). The related gas and water consumption rates comes from the (pseudo)-stoichiometry of hydrate formation and are calculated as shown in Eq. (14).

$$\frac{dn_h}{dt} = \sum_i \left(\frac{dn_{h,i}}{dt} \bigg|_{in} + \frac{dn_{h,i}}{dt} \bigg|_{out} \right) = 4\pi \frac{\rho_h}{M_h} \sum_i \left(r_{out,i}^2 \frac{dr_{out,i}}{dt} - r_{in,i}^2 \frac{dr_{in,i}}{dt} \right)$$
(13)

$$\frac{dn_g}{dt}\Big|_{hyd} = \frac{1}{(\eta+1)}\frac{dn_h}{dt} \quad ; \quad \frac{dn_w}{dt}\Big|_{hyd} = \frac{\eta}{(\eta+1)}\frac{dn_h}{dt}$$
(14)

Finally, the gas concentration in the bulk comes from a mass balance between the gas absorbed by the bulk and the gas consumed due to hydrate formation [5,6]:

$$\frac{dC_b}{dt} = \underbrace{\frac{k_{g/o}A_{g/o}}{\forall_o} \left(C_{g/o} - C_b\right)}_{\text{gas absorption by the bulk}} - \underbrace{\frac{1}{\forall_o} \frac{4\pi}{(\eta+1)} \frac{\rho_h}{M_h} \sum_i \left(r_{out,i}^2 \frac{dr_{out,i}}{dt} - r_{in,i}^2 \frac{dr_{in,i}}{dt}\right)}_{\text{gas consumption due to hydrate formation}}$$
(15)

where $k_{g/o}$ is the absorption coefficient of gas by the oil bulk, $A_{g/o}$ is the gas-oil interfacial surface, \forall_o is the volume of the oil bulk, $C_{g/o} = H_o f_g$ is the gas concentration in the gas-oil interface, H_o is Henry's constant of the gas inside the oil and f_g is the gas fugacity in the gas free phase.

3. Solution method

The model is composed of three ODEs for the inner growth rate (Eq. (7)), the outer growth rate (Eq. (12)) and the bulk concentration (Eq. (15)). This system of ODEs is solved using Runge-Kutta method of 4th order. As initial conditions, the bulk is considered saturated and the inner and outer radius are considered equal to the droplet radius:

$$C_{b}|_{t=t_{0}} = C_{sat,o} = H_{o}f_{g} \quad ; \quad r_{in}|_{t=t_{0}} = r_{in}|_{t=t_{0}} = r_{droplet}$$
(16)

where $t = t_0$ is the time step where hydrates nucleated and a hydrate shell of infinitesimal width already contours the water droplet. The water permeation rate, Eq. (8), is evaluated explicitly and is considered zero for the initial value, $Q|_{t=t_0} = 0$. All the particles are considered to be equal and not to agglomerate. Therefore, the sum term of Eq. (15) becomes a multiplication by the number of particles *i* in the system.

The main difficulty of the presented model is to estimate the closure parameters, which often come from meso or micro scale properties. The interfacial surface between oil and gas $A_{g/o}$ can be estimated through gas-liquid flow models (e.g., Taitel and Barnea, 1990). The droplet radius $r_{droplet}$ can be estimated through liquid-liquid models [14,18].

The equilibrium fugacity of hydrate formation equals the gas fugacity in the equilibrium pressure for the given system temperature, $f_{eq} = f_g \Big|_{T, P_{eq}}$. The gas fugacity is estimated through an EoS (e.g., Peng-Robinson). The equilibrium pressure for the given pressure is estimated through hydrate equilibrium models [1].

Hydrate properties of common former gases (e.g., methane, ethane) may be found in literature [15,19], but sometimes only an order of magnitude of the parameter exists. Also, hydrate properties may evolve with time due to cage occupancy and hydrate porosity evolution. Gas and water properties are well known in literature. Oil properties may be experimentally measured or estimated through compositional models (e.g., MultiflashTM).

The blocking point are the kinetic parameters. The absorption coefficient of gas by the oil $k_{g/o}$ is dependent on the oil composition and the shear rate of the flow, and usually comes from experimentation [5,6,20]. The constant of proportionality of the crystal integration process k_i is a micro scale parameter and usually curve fitted from experiments [5,8]. The mass transfer coefficient between the particle and the bulk may be estimated through proper correlations [12],

which are valid when the concentration layers around the particles do not interact among themselves, i.e., the bulk exists – a continuous phase with spatially homogeneous concentration. This is probably the case of dilute flow, and for higher particle fraction in the flow the mass transfer coefficient is expected to decrease.

4. Results and discussions

The model is compared with experimental results from Melchuna et al. [20,21]. They measured the amount of gas consumption due to hydrate formation in a flowloop of 40 m length and 10.2 mm ID. The fluids used were methane, deionized water and Kerdane (a light oil with C11 to C14 composition). The case of 40% water cut and 1.36 m/s of mixture superficial velocity was chosen. The main characteristics of the experiment are shown in Table 1. The values of the closure parameters used for the model evaluation (with the range of magnitude suggested in literature) are presented in Table 2.

Table 1. Characteristics of the experiments of Melchuna et al. [20].
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Fluids	Methane, deionized water, Kerdane	
Water cut	40%	
Pressure	80 bar	
Temperature	275.5 K	
Mixture superficial velocity	1.36 m/s	
Total liquid volume in the flowloop	10 L	

The number of particles *i* in the system is estimated by the use of the droplet radius and the total volume of water in the system as:

$$i = \frac{\forall_{w}}{\forall_{droplet}} \alpha = \frac{3}{4} \frac{WC \times \forall_{total}}{\pi r_{droplet}^{3}} \alpha$$
(17)

where *WC* is the water cut (ratio between volume of water \forall_w and total volume of the system \forall_{total}). Factor α is introduced in to represent an efficiency of particles that are actually consuming gas. This efficiency may be related:

- i. To the amount of droplets that are actually converted to particles.
- ii. To the assumption of an average droplet radius (monodisperse) instead of a distribution of droplets with different sizes and therefore different mass transfer resistances (polydisperse).
- iii. To the amount of particles that are actually in contact to the bulk, that is, an efficiency due to the impossibility of mass transfer between the particles and the bulk for a dense dispersion and for long distances from the oil-gas surface to the particle.

The presented model converges with the experimental result of Melchuna et al. [20] for an efficiency value of $\alpha \approx 2.4\%$. This low value is probably related to effect iii, since in the experiments of Melchuna et al. [20] the contact surface between oil and gas is restricted to a small region in the top of the riser section (called 'separator'), whereas the flowloop presents a semi-industrial scale of 40-m length, with a capacity of 10 liters of liquid. This means that probably only the particles inside the liquid volume near the 'separator' interacts with the gas-oil interface and grow. Following this idea, only the particles inside the 240 ml of the flowloop near the 'separator' are growing, while the rest of the experiment is mostly propagating the slurry flow to capture agglomeration, deposition and plugging tendencies of the oil-water-hydrate flow.

Figure 2 presents the comparison of the proposed model against the experimental data of Melchuna et al. [20] for the evolution in time of the gas consumption due to hydrate formation. The model is capable of representing the experimental results with the order of magnitude of the closure parameters presented in literature (Table 2) and for a curve fitting of $\alpha \approx 2.4\%$. Although the model cannot be considered as fully validated (since the curve fitting may mask the omission of important phenomena for hydrate growth or even mistakes during the modeling), the trend of the amount of gas consumption is considered as validated. The trend is composed of an initial faster hydrate formation rate, followed by a decrease in the gas consumption rate and an asymptote trend. This asymptote trend is related to the growth of the hydrate shell and related increase of the diffusion resistance.

Parameter	Order of magnitude from literature	Used value
G 1100 1 1	$D_h \approx (3.4 - 7.6) \times 10^{-13} \text{ m}^2/\text{s}$	
Gas diffusivity in hydrate	Validity: $3 \le P \le 15$ MPa and $263 \le T \le 268$ K	$D_h = 3.4 \times 10^{-13} \text{ m}^2/\text{s}$
in nyulute	Davies et al. (2008, apud Jung et al., 2010)	
Solubility of gas in solids	$\frac{S_h}{P} \approx 10^{-3} - 10^{-5} \frac{\text{molgas/molsolid}}{\text{atm}} [13]$	$S_h = 10^{-1} \frac{\text{molgas}}{\text{molgalid}}$
	Valid for different gas species in different solids, but no experiments of methane in methane sI hydrates.	(at 80 bar)
Mass transfer coefficient around a spherical particle	$h_m = \frac{D_{g/o}}{2r_{out}} \left(2 + 0.52 \mathrm{Re}^{0.52} \mathrm{Sc}^{1/3} \right)$	
	With: $\operatorname{Sc} = \frac{V_o}{D_{g/o}}$, $\operatorname{Re} = \frac{D^{4/3} \varepsilon^{1/3}}{V_o} \approx \frac{2\rho_o J r_{out}}{\mu_o}$	$h_m = (0.15 - 1.31) \times 10^{-3} \frac{m}{s}$
	J = mixture superficial velocity	(for the range of r_{out} calculated by the model)
	Validity: $r_{out} < 15 \mu\text{m}$, Re > 10 ⁻² , Sh > 3.5 Armenante and Kirwan (1989, apud Herri et al., 1999)	
of crystal integration	$k_i \approx 5.5 - 6.5 \times 10^{-12} \text{ mol/(m}^2 \text{sPa})$ [5] (data regression without considering mass transfer resistances around the	
	particle, therefore k_i is expected to be higher) $k_i \approx 6 \times 10^{-10} \text{ mol}/(\text{m}^2\text{sPa})$ [8]	$k_i \approx 6 \times 10^{-10} \frac{\text{mol}}{\text{m}^2 \text{sPa}}$
	(data regressed for a gas composition with ~85% of methane considering mass transfer resistances)	
Henry's constant of methane in water		$H_{w} = 8.9 \times 10^{-6} \frac{mol}{m^{3}Pa}$
	With: $T^{\circ} = 298.15K$. Validity: $(T^{\circ} - T \le 20K)$ [22]	m ³ Pa
Henry's constant of methane in		
Kerdane	Calculate from solubility measurements of Melchuna	[20]
Absorption	$\frac{k_{g/o}A_{g/o}}{\forall} \approx 8.1 \times 10^{-3} s^{-1}$	
coefficient	Experimental measurements of Melchuna [20] for the analyzed	case of Table 1
Properties of methane sI	$\rho_h \approx 917 kg/m^3$; $M_h \approx 17.7 g/mol$ [19] $\eta \ge 5.75$ [1]	$\eta = 6$ since hydrate kinetic may cause less cage
hydrates		occupancy
Kerdane properties	$\rho_o \approx 815 kg / m^3$; $\mu_o \approx 3 \times 10^{-3} Pa.s$ [23] $D_{g/o} \approx 10 \times D_{g/w}$ (assumption that diffusivity of methane in Kerdane is one	$D_{g/o} = 1.5 \times 10^{-9} \frac{m^2}{s}$
P P	order of magnitude higher than methane in water)	5
Equilibrium pressure for the given temperature	$P_{eq} = 32.5 \times 10^5 Pa$ (CSMGem, Ballard and Sloan, 20	004)
Equilibrium fugacity	$f_{eq} = P_{eq}$ (ideal gas)	
Gas fugacity at gas free phase	$f_g = P = 80 \times 10^5 Pa$ (ideal gas)	
Droplet size	$r_{droplet} = (13 - 23) \mu m$ FBRM measurements of Melchuna [20] for the analyzed case of Table 1	$r_{droplet} = 23 \mu m$

Table 2. Closure parameters used for model evaluation and suggested range of order of magnitude in literature.

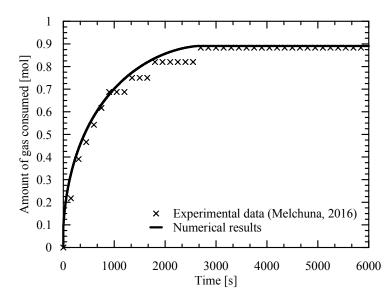


Figure 2. Comparison of model results against experimental data of Melchuna et al. [20] for the amount of gas consumed over time due to hydrate formation.

5. Further improvements

The inward and outward growth model of hydrate particles based on gas diffusion through solid is capable of predicting the time scale of hydrate formation only if a high solubility of gas in the hydrate structure is adopted. The value adopted in Table 2 is however optimist, coming from compatible gases inside metal alloys or ceramics at high temperature (e.g., helium in Pyrex at 200°C). This is however not probably the case of methane (a much larger molecule than helium) inside the hydrate crystalline structure at a temperature where hydrates would form (~ 4°C). Furthermore, the use of $S_h = 10^{-1}$ implies in a negative sign for the second term inside the minimum function of Eq. (12), which is not Physically acceptable. This is an indication that the closure parameters are ill-posed. The results of the last section were generated considering the water permeation rate as the limiting step and neglecting the outer crystal integration due to this ill-posed closure.

Literature often mention an effective diffusion of the gas through the solid hydrate structure and through the liquid trapped in the capillaries. However, if ever water is continuously being expulsed through the particle, then the capillaries are filled-up with water. In this case, gas consumption would happen in the capillary walls and inner growth would probably not happen unless: (i) diffusion through the capillaries is much faster than crystallization; or (ii) the shell width is very small, which happens at the beginning of the hydrate formation. If the capillaries are filled-up with oil, then inner growth may happen, but outer growth will not happen.

6. Conclusions

The present article revisited and extended the predictive models for hydrate growth in gas-oil-water systems in literature. The model was compared with experimental data and the trend of gas consumption over time was validated, though closure parameters are still scarce in literature for model implementation in other scenarios then the herein chosen. The model captures the fast initial growth rate of the hydrates, with an asymptotic trend as the hydrate shell imposes higher mass transfer resistances. The mass transfer resistances are associated with gas diffusion and water permeation trough the hydrate shell, which are related to the shell width and therefore increase in time as the shell becomes thicker.

The analysis did in this work further highlights the omission in the use of the gas solubility inside the hydrate solid structure, which may imply in much smaller time scales of hydrate formation than the ones experimentally observed. Furthermore, diffusion through the liquid trapped in the capillaries would imply in either a non-existing shrinking core (if the liquid trapped is water, with consequent crystallization in the capillary walls) or a non-existing outer growth (if the liquid trapped is oil, and therefore water never reaches the outer surface). Although the inward and outward growth model explains the asymptotic trend of hydrate formation due to mass transfer limitation, future work shall analyze the mass transfer and crystallization inside of the capillaries of the hydrate porous structure.

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