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The COSMOS-UltraVISTA stellar-to-halo mass relationship: new insights on galaxy formation efficiency out to $z \sim 5$

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ABSTRACT

Using precise galaxy stellar mass function measurements in the COSMOS field we determine the stellar-to-halo mass relationship (SHMR) using a parametric abundance matching technique. The unique combination of size and highly complete stellar mass estimates in COSMOS allows us to determine the SHMR over a wide range of halo masses from $z \sim 0.2$ to 5. At $z \sim$ 0.2, the ratio of stellar-to-halo mass content peaks at a characteristic halo mass $M_h = 10^{12} M_{\odot}$ and declines at higher and lower halo masses. This characteristic halo mass increases with redshift reaching $M_h = 10^{12.5} M_{\odot}$ at $z \sim 2.3$ and remaining flat up to z = 4. We considered the principal sources of uncertainty in our stellar mass measurements and also the variation in halo mass estimates in the literature. We show that our results are robust to these sources of uncertainty and explore likely explanation for differences between our results and those published in the literature. The steady increase in characteristic halo mass with redshift points to a scenario where cold gas inflows become progressively more important in driving star formation at high redshifts, but larger samples of massive galaxies are needed to rigorously test this hypothesis.

Key words: methods: statistical-galaxies: evolution-galaxies: haloes.

1 INTRODUCTION

Galaxy formation is a remarkably inefficient process (e.g. Silk 1977; Persic & Salucci 1992; Dayal & Ferrara 2018). This can be seen quantitatively if one compares the dark matter halo mass function (HMF) and the galaxy stellar mass function (SMF): both in low- and high-mass regimes they differ by several orders of magnitude (see e.g. Cole et al. 2001; Yang, Mo & van den Bosch 2003; Eke et al. 2006; Behroozi, Conroy & Wechsler 2010; Moster et al. 2010).

Understanding how the stellar mass content (M_*) of a galaxy relates to the mass of its dark matter halo (M_h) is, in fact, an alternative way of considering the problem of galaxy formation. In the local Universe, there is a 'characteristic halo mass' (M_h^{peak}) at which the M_*/M_h ratio is maximized. A natural interpretation is that M_h^{peak} corresponds to the halo mass at which star formation, integrated over the entire assembly history of the galaxy, has been the most efficient (Silk, Di Cintio & Dvorkin 2013). We

consider 'galaxy formation efficiency' as the global process of forming stars in dark matter haloes, from the accretion of gas to the actual transformation of baryons into stars. At lower and higher halo masses, the M_*/M_h ratio decreases rapidly, presumably as a consequence of physical processes that suppress star formation in these haloes. Various mechanisms have been proposed in order to explain this inefficiency: for example, supernovae and stellar winds in low-mass haloes and active galactic nuclei (AGNs) feedback processes in more massive objects (see Silk & Mamon 2012 for a detailed review).

Although such comparisons between mass functions are phenomenological in nature (Mutch, Croton & Poole 2013) they provide useful constraints to theoretical models of galaxy formation in particular when the comparison spans a large redshift range. The advent of highly complete, mass-selected galaxy surveys (see e.g. Ilbert et al. 2013) and accurate predictions for the HMF (Tinker et al. 2008; Watson et al. 2013; Despali et al. 2016) allows us to measure the stellar-to-halo mass relationship (SHMR) of galaxies at different epochs. There are many techniques to accomplish this: e.g. in the 'subhalo abundance matching' (SHAM), the number density of galaxies (from observations) and dark matter subhaloes (from simulations) are matched to derive the SHMR at a given redshift (see e.g. Marinoni & Hudson 2002; Behroozi et al. 2010; Behroozi, Wechsler & Conroy 2013b; Behroozi et al. 2018; Moster et al. 2010; Moster, Naab & White 2013, 2018; Reddick et al. 2013). This technique can also be implemented by assuming a non-parametric monotonic relation between the luminosity or stellar mass of the observed galaxies and subhalo masses at the time of their infall on to central haloes (Conroy, Wechsler & Kravtsov 2006).

Other studies use a 'halo occupation distribution' modelling (HOD, see e.g. Vale & Ostriker 2004; Zheng, Coil & Zehavi 2007; Leauthaud et al. 2011; Coupon et al. 2015) where a prescription for how galaxies populate dark matter haloes can be used to simultaneously predict the number density of galaxies and their spatial distribution. In this case, lensing combined with clustering measurements can provide additional constraints on the SHMR.

However, until now, investigations of the SHMR over a large redshift range have mostly relied on heterogeneous data sets each with their own selection functions. Interpreting these results can be challenging since different biases from each survey may introduce artificial trends. In this work, we measure the SHMR and M_h^{peak} in 10 bins of redshifts between z = 0.2 and 5.5 in a homogeneous and consistent way using the SHAM technique applied to a single data set: the COSMOS2015 galaxy catalogue (Laigle et al. 2016).

COSMOS (Scoville et al. 2007) is a 2 deg² field with deep ultraviolet-to-infrared (UV-to-IR) coverage (see Laigle et al. 2016, and references therein). The wealth of spectroscopic observations (Lilly et al. 2007: Le Fèvre et al. 2005, 2015: Hasinger et al. 2018) means photometric redshifts can be validated even in the traditionally poorly sampled 1 < z < 2 redshift range (see fig. 11 of Laigle et al. and fig. 4 of Davidzon et al.). The large area of COSMOS makes it ideal to collect robust statistics of distant, massive galaxies. Moreover, exquisite IR photometry means precise stellar mass estimates can be made over a large redshift range (see e.g. Steinhardt et al. 2014; Davidzon et al. 2017). Extensive tests have been made to validate the mass completeness and the photometric redshift accuracy in COSMOS (Laigle et al. 2016; Davidzon et al. 2017). Far-IR, radio, and X-ray observations are also available to assess the crucial role of AGN (Delvecchio et al. 2017), and the quenching of distant and massive galaxies (Gozaliasl et al. 2018).

Previously in COSMOS Leauthaud et al. (2012) used a combination of parametric abundance matching, galaxy clustering, and galaxy–galaxy lensing to derive the SHMR to $z \sim 1$; galaxy–galaxy lensing measurements with COSMOS ACS data are not feasible above $z \sim 1$. More recently, Cowley et al. (2018) made a halo modelling analysis to derive the SHMR in the UltraVISTA 'deep stripes' region.

The organization of the paper is as follows. In Section 2, we introduce the observed SMF of COSMOS galaxies and discuss the principal uncertainties; we then present the Despali et al. (2016) dark matter HMF we use and our fit using a dark matter simulation to derive the HMF for the maximum mass in the history of the haloes. We also present comparisons with other mass functions for consistency checks. In Section 3, we describe our abundance matching technique, its assumptions and principal sources of uncertainties, along with our Monte Carlo Markov Chain (MCMC) fitting procedure. In Section 4, we present our results, i.e. the SHMR and its redshift evolution up to $z \sim 5$. We discuss the physical mechanisms that may explain our observations in Section 5.

Throughout this paper, we use the *Planck* 2015 cosmology (Planck Collaboration et al. 2016) with $\Omega_{m,0} = 0.307$, $\Omega_{\Lambda,0} = 0.691$, $\Omega_{b,0} = 0.0486$, $N_{eff} = 3.05$, $n_s = 0.9667$, $h = H_0/(100 \text{ km s}^{-1} \text{ Mpc}^{-1}) = 0.6774$, except if noted otherwise. Stellar mass scales as $1/h^2$ whereas halo mass scales as 1/h. The notation ϕ will denote a mass function. The notation ln () refers to the natural logarithm and log () refers to the base 10 logarithm.

2 MASS FUNCTIONS AND THEIR UNCERTAINTIES

2.1 Stellar mass functions

The galaxy SMF corresponds to the number density per unit comoving volume of galaxies in bins of M_* . It is one of the key demographics to understand quantitatively the galaxy formation process as it describes how stellar mass is distributed in galaxies. Traditionally, the SMF has been modelled by a Schechter (1976) function, although for certain galaxy populations a combination of more than one such function may provide a better fit to observations (Binggeli, Sandage & Tammann 1988; Kelvin et al. 2014). Here, we use SMFs derived by Davidzon et al. (2017, hereafter D17) for galaxies in the UltraVISTA-Ultra deep region of the COSMOS field (see McCracken et al. 2012). The sample was constructed using the photometric catalogue of Laigle et al. (2016) which contains more than half a million galaxies with photometric redshifts (z_{phot}) between z = 0.2 and 6 (178 567 of them in the Ultra deep region). By restricting the analysis to the high-sensitivity region ($K_s < 24.7 \text{ mag}$ at 3σ , ~0.7 mag deeper than the rest of COSMOS) the effective area turns out to be $\sim 0.5 \text{ deg}^2$. None the less, this represents a three times larger volume than the one probed by other deep extragalactic surveys like the Cosmic Assembly Near-IR Deep Extragalactic Legacy Survey (Grogin et al. 2011; Koekemoer et al. 2011).

Both z_{phot} and M_* are derived by fitting the galaxy spectral energy distribution (SED) with synthetic templates (see D17 for further details). The unique combination of deep optical (*Subaru*), near-IR (VISTA), and mid-IR (*Spitzer*/IRAC) observations results in a galaxy sample that is >90 per cent complete at $M_* > 10^{10} M_{\odot}$ up to z = 4; for galaxies at 4 < z < 6 above that threshold, the catalogue is >70 per cent complete. More generally, D17 defined a minimal mass ($M_{*,\min}$) as the 75 per cent completeness limit, with a redshift evolution described as $M_{*,\min}(z) = 6.3 \times 10^7 (1 + z)^{2.7} M_{\odot}$. This minimal mass is used as the lower boundary for the SMF.

D17 estimated the SMF in 10 redshift bins from z = 0.2 to 5.5 (see Fig. 1) using three independent methods: the $1/V_{\text{max}}$ technique (Schmidt 1968), the stepwise maximum likelihood (Efstathiou, Ellis & Peterson 1988) and the maximum likelihood method of Sandage, Tammann & Yahil (1979). These three estimators provide consistent SMF estimates. However, they are all affected by observational uncertainties (M_* and z_{phot} errors) that scatter galaxies from their original mass bin. This systematic effect, known as Eddington (1913) bias, dominates at high masses ($M_* \gtrsim 10^{11} M_{\odot}$) because here galaxy number density declines exponentially; this produces an asymmetric scatter and consequently modifies the SMF profile. Depending on the 'skewness' and the magnitude dependence of observational errors the Eddington bias may have a strong impact also at lower masses (Grazian et al. 2015).

When fitting a Schechter (1976) function to their $1/V_{max}$ determinations, D17 account for the Eddington bias using the method introduced in Ilbert et al. (2013). Therefore, in our work, we use the Schechter fits of D17 which should be closer to the intrinsic SMF compared to the other estimators. For consistency, we rescale these

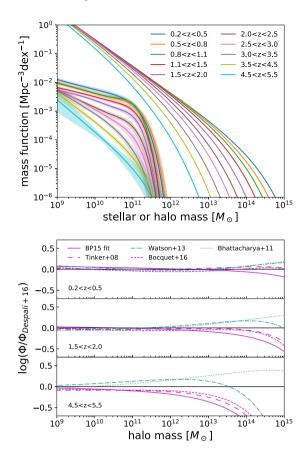


Figure 1. Upper panel: our adopted stellar and HMFs. For the SMF at a given redshift (see the legend), a solid line shows our HMF (Despali et al. 2016, fitted on the Bolshoï–Planck simulation) whilst the solid line and shaded area is the SMF with the associated 1σ uncertainty (corresponding to the best fit to $1/V_{max}$ points corrected for Eddington bias, Davidzon et al. 2017). Lower panel: for three sample redshift bins, the relative difference as a function of halo mass between the original (Despali et al. 2016) using the virial overdensity criterion, our Bolshoï–Planck fit (solid magenta line), and a selection of HMFs from the literature. Magenta lines show numerical simulations in which haloes are defined according to a spherical overdensity threshold (solid line: Bolshoï–Planck, long-dashed line: Tinker et al. 2008, and short-dashed line: Bocquet et al. 2016). Cyan lines show works that use an FoF algorithm (dotted line: Bhattacharya et al. 2011, dotted–dashed: Watson et al. 2013).

estimates to Planck Collaboration et al. (2016, P16) cosmology. The fitting function assumed by D17 is a double Schechter (see equation 4 in D17) at z < 3 and a single Schechter function (their equation 3) above that redshift. At low redshifts, two SMF components are clearly visible (e.g. Ilbert et al. 2010), above z > 3, there is no evidence of this double Schechter profile (Wright, Driver & Robotham 2018).

The SMF error bars include both systematic and random errors including Poisson noise, cosmic variance (computed using an updated version of the software described in Moster et al. 2011) and the scatter due to errors in the SED fitting. The SMF uncertainties due to SED fitting are derived through Monte Carlo re-extraction of z_{phot} and M_* estimates according to the likelihood function of each galaxy. This procedure may be biased if the likelihood were under- or overestimated by the SED fitting code (see Dahlen et al. 2013). However, recent work with simulated photometry suggests that this should not be the case for the code used in D17 (Laigle et al., in preparation).

2.2 Halo mass functions

Our main reference for the dark matter HMF¹ is the work of Despali et al. (2016, see fig. 1). They measure the HMF using six *N*-body cosmological simulations with different volumes and resolutions: all of them have 1024^3 dark matter particles with masses ranging from 1.94×10^7 to $6.35 \times 10^{11} h^{-1} M_{\odot}$ and a corresponding box size from 62.5 to $2000 h^{-1}$ Mpc. Haloes are identified through the 'spherical overdensity' algorithm (Press & Schechter 1974), i.e. each halo is a sphere with a matter density equal to the virial overdensity (see Eke, Cole & Frenk 1996) at the given redshift (which is equal to the median *z* of the observed SMF, see Table B2). The halo mass is defined as the sum of dark matter particles included in such a sphere.

It has been shown (see e.g. Reddick et al. 2013) that for abundance matching applications the stellar mass of galaxies is better correlated to the maximal mass the dark matter haloes have over their history $(M_{\rm h, max})$ rather than the actual mass at a given redshift. This is particularly true for subhaloes which can lose mass due to gravitational stripping by the neighbouring main halo whilst the galaxy inside will keep the same stellar mass. Reddick et al. (2013) have demonstrated that using this $M_{\rm h, max}$ better fits to observations such as galaxy clustering for abundance matching.

Our HMF for the maximal mass $M_{\rm h, max}$ are calculated using the Bolshoï–Planck simulation (Rodríguez-Puebla et al. 2016; Behroozi et al. 2018). This dark-matter-only simulation has a comoving volume of $250h^{-1}$ Mpc on a side with 2048^3 particles with a mass resolution of $1.6 \times 10^8 h^{-1} M_{\odot}$ and uses Planck Collaboration et al. (2016) cosmology. Haloes are identified with the ROCKSTAR halo finder and masses are computed using the virial overdensity criterion of Bryan & Norman (1998). Behroozi et al. (2018) provide halo number densities for several halo mass bins and for 178 snapshots from z = 16 to 0 for this simulation. We fit the HMF of Despali et al. (2016) using a modified version of the COLOSSUS code for these data points in the range 0 < z < 5 and $10^{11}h^{-1}M_{\odot} < M_{h,max} < 10^{15}h^{-1}M_{\odot}$. The parameters of equation 7 of Despali et al. (2016) we find are: A = 0.331, a = 0.831, and p = 0.351. Fig. A1 shows the resulting HMF for several redshifts from 0 to 5.

Besides the variations due to different cosmological parameters (Angulo & White 2010), it is difficult to model the uncertainties affecting the HMF. Despali et al. (2016) thoroughly discuss the implications of different density thresholds in the spherical overdensity algorithm, e.g. replacing the virial overdensity with 200 times critical (ρ_c) or mean background (ρ_b) density. They conclude that the virial definition leads to a 'universal' HMF fit, while in the case of $\rho_{\rm c}$ or $\rho_{\rm b}$ the results are more redshift dependent. A higher density threshold – e.g. $500\rho_c$, as often used in the literature - alters the HMF profile by decreasing the number density of the most massive systems, as some of them are now identified as a complex of smaller, independent haloes. The assumption of sphericity in the finder algorithm is less problematic since its impact on the HMF is mass-independent: accounting for haloes' tri-axiality has only a mild effect on the HMF (Despali, Giocoli & Tormen 2014).

Other studies have investigated the impact of different halo finding algorithms which produce changes in the HMF of the order of ~ 10 per cent (Knebe et al. 2011). Another potential issue is the impact of baryons (not implemented in Despali et al.) on the

¹HMFs were computed using the COLOSSUS python module (Diemer 2018).

growth of dark matter haloes: Bocquet et al. (2016) show that in hydrodynamical simulations the halo number density decreases by ~15 per cent at $z \leq 0.5$ with respect to dark matter only, whereas at higher redshift, the impact of baryons is negligible.

In our analysis, we use Despali et al. mass function fitted on the Bolshoï-Planck simulation where haloes are identified using the virial overdensity criterion and where there mass is the maximal mass in their history $M_{\rm h, max}$. We also use the original version of Despali et al. (2016) HMF with halo mass defined with the virial overdensity criterion. To quantify how such a choice affects our results we consider different HMF estimates. These alternate versions are divided into two categories according to how haloes are identified. HMF estimates in the first category (Tinker et al. 2008; Bocquet et al. 2016) use the spherical overdensity definition, with halo masses defined with the $>200\rho_{\rm b}$ criterion, while the others (Bhattacharya et al. 2011; Watson et al. 2013) rely on the so-called friends-of-friends (FoF) algorithm (Davis et al. 1985). The Bolshoï-Planck fit of Despali et al. HMF is shown in the upper panel of Fig. 1 while the lower panel shows how this fit and the other HMF differ from Despali et al. in three redshift bins. At low redshifts, we find that differences are negligible, in agreement with the literature. However for $> 10^{13} M_{\odot}$ haloes at z > 2, i.e. in a range barely investigated in previous work, there are 0.2-0.5 dex offsets between Despali et al. (2016) and other HMF estimates. Such a difference may be fully explained by Poisson scatter since such massive haloes are rare in the volume of cosmological simulations. We do not attempt to find the physical reasons of such a discrepancy and here we simply take the 'interpublication' bias as a measure of generic HMF uncertainties (see Section 4.4).

3 THE STELLAR-TO-HALO MASS RELATIONSHIP

3.1 The subhalo abundance matching technique

In the SHAM technique, a 'marker' quantity is assigned to dark matter haloes and galaxies (e.g. halo mass and stellar mass, respectively). Both haloes and galaxies are ranked according to their marker quantity, and then the latter are associated to the former by assuming a monotonic one-to-one relationship (Vale & Ostriker 2004; Conroy et al. 2006; Behroozi et al. 2010; Moster et al. 2010; Reddick et al. 2013). Here, the markers we use are the dark matter halo mass and the galaxy stellar mass.

In the hierarchical clustering scenario, small haloes accrete on to more massive ones and become 'subhaloes'. Galaxies are classified as either 'satellite' (those hosted by subhaloes) or 'central' (those in the main halo). Since in the COSMOS2015 catalogue, there is no distinction between satellite and central galaxies to correctly perform the abundance matching we must consider all the haloes (i.e. main haloes and subhaloes) as a whole sample. For sake of simplicity, we will refer to any (sub-)halo hosting a galaxy as a 'halo'. We do not take into account possible 'orphan' galaxies (i.e. satellites with no subhalo, e.g. Moster et al. 2013).

These orphan galaxies may appear when matching a catalogue of dark matter haloes with galaxies from observations (this is done in e.g. Moster et al. 2018; Behroozi et al. 2018). If the resolution of the simulation (or of the halo finder) is not precise enough, the catalogue may miss the smallest haloes and some galaxies will be unassociated. In our work, we do not use directly halo catalogues from a simulation but instead fits of a functional form of the HMF performed on outputs of simulations. Despali et al. (2016) made sure that the fit is performed on a range of halo masses not affected by the limits of the simulation and the HMF is extrapolated below this limit to smaller masses. Campbell et al. (2018) investigated the importance of the orphan galaxies in the Bolshoï–Planck simulation. They concluded that less than 1 per cent of galaxies with $M_* > 10^{9.5}h^{-2}M_{\odot}$ are orphans. As such we consider that the different HMF we use are not impacted by the resolution limits of the simulations and that the impact of orphan galaxies on the SHMR is negligible in the range of mass we consider.

The SHAM method also does not consider either the gas mass or the intracluster medium. Our sources of uncertainties are discussed in more detail in Section 3.3 (see also Behroozi et al. 2010; Campbell et al. 2018).

We perform a 'parametric' SHAM, assuming a functional form for the relation between M_* and M_h . Following the same formalism as in Behroozi et al. (2010), such a parametric SHMR is described by the following equation:

$$\log(M_{\rm h}) = \log(M_1) + \beta \log \left(M_*/M_{*,0}\right) + \frac{\left(M_*/M_{*,0}\right)^{\delta}}{1 + \left(M_*/M_{*,0}\right)^{-\gamma}} - \frac{1}{2}.$$
 (1)

This model has five free parameters M_1 , $M_{*,0}$, β , δ , and γ , which determine the amplitude, the shape, and the knee of the SHMR (see Behroozi et al. 2010, for a more detailed description of the role of each parameter in shaping the SHMR). Roughly speaking, parameter values in equation (1) are adjusted during an iterative process until the HMF, converted into stellar mass through the SHMR, is in agreement with the observed SMF (see Section 3.2).

More specifically, the galaxy cumulative number density (N_*) and the halo cumulative number density (N_h) above a certain mass are respectively given by $N_*(M_*) = \int_{M_*}^{+\infty} \phi_*(M) dM$ and $N_h(M_h) = \int_{M_h}^{+\infty} \phi_h(M) dM$, with ϕ_* and ϕ_h being the stellar and HMFs. The main assumptions of SHAM is that there is only one galaxy per dark matter halo and that the relation between stellar and halo masses is monotonic. As a consequence, the M_* value associated to a given M_h is the one for which $N_*(M_*) = N_h(M_h)$. The derivative of this equation gives the relationship between SMF, HMF, and SHMR:

$$\phi_{*,\text{conv}}(M_*) = \frac{\mathrm{d}M_{\mathrm{h}}}{\mathrm{d}M_*} \phi_{\mathrm{h}}(M_{\mathrm{h}}),\tag{2}$$

where the differential term on the right-hand side can be derived from equation (1). We use the notation $\phi_{*, \text{ conv}}$ because we convolve this SMF with a lognormal distribution to account for scatter in stellar mass at fixed halo mass. The standard deviation (ξ) of the lognormal distribution is kept as an additional free parameter; we assume that ξ is independent of the halo mass (More et al. 2009; Moster et al. 2010) but can vary with redshift. We note here that new hydrodynamical simulations like Eagle (Schaye et al. 2015) have shown that this scatter decreases from 0.25 dex at $M_h = 10^{11} M_{\odot}$ to 0.12 dex at $M_h = 10^{13} M_{\odot}$ (see Matthee et al. 2017). This evolution of the scatter is in agreement with latest abundance matching models (Coupon et al. 2015; Behroozi et al. 2018). Moster et al. 2018). See also fig. 9 of Gozaliasl et al. (2018). However in our analysis,f we restrict ourselves to a mass-invariant scatter for simplicity.

The model SMF defined in equation (2) is then fitted to the observed one (i.e. $\phi_{*, \text{ obs}}$) through the procedure described in the next section.

3.2 Fitting procedure

To fit the model SMF to real data, a negative log-likelihood is defined as:

$$\chi^{2} = \sum_{i} \left(\frac{\phi_{*,\text{conv}}(M_{*,i}) - \phi_{*,\text{obs}}(M_{*,i})}{\sigma_{\text{obs}}(M_{*,i})} \right)^{2},$$
(3)

where σ_{obs} is the uncertainty of the observed SMF in a given stellar mass bin $M_{*,i}$ (with the first bin starting at $M_{*,min}$).

For each of the 10 redshift bins, we minimize equation (3) using an MCMC algorithm.² This algorithm allow the sampling of the parameter space in order to derive the posterior distribution for the six free parameters. We use flat conservative priors on the parameters together with 250 walkers each with a different starting point randomly selected in a Gaussian distribution around the original starting point. Our convergence criterion is based on the autocorrelation length, which is an estimate of the number of steps between which two positions of the walkers are considered uncorrelated (Goodman & Weare 2010). Our MCMC stops when the autocorrelation length has changed by less than 1 per cent and when the length of the chain is at least 50 times the autocorrelation length. As an example, our chains in the case of the HMF fitted on Bolshoï-Planck have a length between 5000 at low redshift and 25 000 in the highest redshift bin. With our 250 walkers this gives between 1.25×10^6 and 6.25×10^6 samples. The first steps up to two times the autocorrelation length are discarded as a burnin phase. To speed up the computation of the posteriors, we keep only the iterations separated by a thin length which is half of the autocorrelation length.

We show in Table B2 the best fit and the 68 per cent confidence interval for the six free parameters in each of the 10 redshift bins, along with the marginalized posterior distributions in Figs B1–B3. These figures show that the parameters M_1 and $M_{*,0}$ are highly correlated. This is expected because as M_1 increases, $M_{*,0}$ should also increase. M_1 and β are also highly correlated which may be explained by the fact that $\log(M_*/M_{*,0})$ is negative for a large range of stellar masses so an increase of β is compensated by an increase of M_1 . As we can see, the value of δ is not well constrained at high redshift, because this parameters controls the high-mass slope which is not well constrained in our data.

3.3 Principal sources of SHAM uncertainties

There are several sources of uncertainties in the SHAM technique. A subhalo may be stripped after infall, leaving the hosted galaxy embedded in the larger, central halo. This may break the one-to-one correspondence between galaxies and dark matter haloes which is the main assumption of our method. The HOD model is a viable solution to take this into account although it would introduce an additional number of assumptions and free parameters. Moreover, observed galaxy clustering is required to constrain the HOD model parameters (e.g. Coupon et al. 2015) but such measurements are challenging at z > 2 (Durkalec et al. 2015). At lower redshift ($z \leq 1$), Leauthaud et al. (2012, see their fig. 13) have shown that M_h^{peak} measurements are consistent between HOD and SHAM measurements.

Another source of uncertainty comes from random and systematic errors in z_{phot} and M_* estimates, with the former propagating into

the M_* error in a way difficult to model (see discussion in D17). In D17, the logarithmic stellar mass uncertainty is described by a Gaussian with standard deviation $\sigma_{M*} = 0.35$ dex multiplied by a Lorentzian function with a parameter τ increasing with redshift to enhance the tails of the distribution (see equation 1 of D17). These observational uncertainties which cause the Eddington bias have been corrected for in the SMF estimates we adopt (Section 2) but some caveats remain (see D17; Grazian et al. 2015). Moreover, in our fitting procedure, we consider that different stellar mass bins are uncorrelated (equation 3). This assumption is a consequence of the fact that in D17 (as the vast majority of the literature) covariance matrices are not provided for their SMF estimates. Once corrected for M_* observational uncertainties, the main source of correlations between mass bins comes from the intrinsic covariance between them. To avoid oversampling, we adopt a mass bin size of 0.3 dex which is comparable to the scatter in D17. We verified that this choice does not introduce any significant bias: modifying the bin size and centre (by $\pm 0.1 \text{ dex}$) results remain consistent within 1σ .

Besides their impact on M_* estimates, z_{phot} uncertainties affect the observed SMF by scattering galaxies in the wrong redshift bin. Our binning is large enough to mitigate this given that typical z_{phot} dispersion in COSMOS2015 estimated from a large spectroscopic galaxy sample reaches $\sigma_z \simeq 0.03(1 + z)$ at 2.5 < z < 6.

None the less, catastrophic z_{phot} errors in the SED fitting (e.g. due to degenerate low- and high-*z* solution) may still be a concern. The fraction of catastrophic redshift outliers in COSMOS2015 is about 0.5 per cent at *z* < 3 and 12 per cent at higher redshifts, so it should not introduce a significant covariance between *z* bins. This seems to be confirmed by test with hydrodynamical simulations (Laigle et al., in preparation).

Despite this, the impact of SED fitting systematics is still an open question which will only be resolved with next-generation surveys (e.g. large and unbiased spectroscopic samples with the Prime Focus Spectrograph at *Subaru*, or the *James Webb Space Telescope*).

However, in this work, we independently constrain parameters of equation (1) at each redshift bin without assuming a functional form for their redshift evolution (contrary to Behroozi et al. 2010). Such a redshift-independent fit reduces the overall number of assumptions in the SHMR modelling.

A final source of uncertainty comes from the M_* scatter we add to the galaxy-to-halo monotonic relation. This is modelled with a lognormal distribution characterized by the parameter ξ which is free to vary in the MCMC fit. This parameter is usually fixed between 0.15 and 0.20 dex (see e.g. More et al. 2009; Moster et al. 2010; Reddick et al. 2013) but in the large redshift range probed here we expect a non-negligible variation due to the evolution of galaxies' physical properties as well as observational effects. We note however that the resulting values (see Table B2) are compatible with the fixed ones assumed by the studies mentioned previously.

4 RESULTS

4.1 The stellar-to-halo mass relationship

Figs 2 and 3 show our derived SHMR fits (upper panels) and the corresponding ratio between stellar mass and halo mass (lower panels) for samples in 0.2 < z < 2.5 and 2.5 < z < 5.5 redshift intervals respectively. The SHMR and the corresponding 1σ uncertainty are computed respectively as the 50th, the 16th, and the 84th

²We use the EMCEE PYTHON package (Foreman-Mackey et al. 2013).

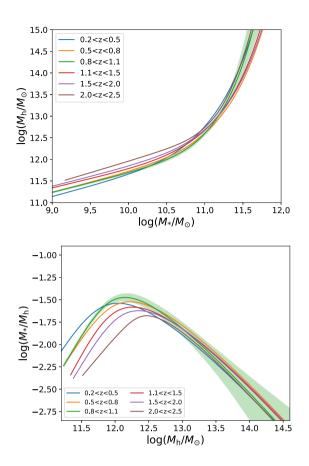


Figure 2. Upper panel: SHMR from z = 0.2 to 2.5. Thick lines show the 50th percentile of the M_h distribution at fixed M_* computed from our MCMC runs. The coloured bands show the 16th and 84th percentile. The band is shown for the 0.8 < z < 1.1 redshift bin only for clarity (for other redshift bins, the uncertainty is of the same order). The limits in stellar mass for each redshift is derived from observations. Lower panel: M_*/M_h ratio derived from this SHMR.

percentile of the distribution of M_h at a given M_* in the remaining MCMC chains (Section 3.2). These uncertainties are shown as the shaded regions. Considering the stellar mass completeness of our data set (Section 2) we limit our samples to $M_* > M_{*,\min}(z)$ and also restrict ourselves at $M_h < 10^{15} M_{\odot}$ since the number density of haloes of such a mass is negligible across the whole redshift range ($<10^{-6}$ Mpc⁻³; see Mo & White 2002).

We note that the stellar mass evolution of haloes between redshift bins might sometime appear at odds with the expected stellar mass assembly. A halo with $M_{\rm h} = 10^{13} M_{\odot}$ has a stellar mass of $10^{11.27} M_{\odot}$ at z = 4. This halo is expected to grow to a mass of $M_{\rm h} = 10^{13.5} M_{\odot}$ at z = 2.5 where our model says the galaxy should have a stellar mass of $10^{11.12} M_{\odot}$. This effect of haloes 'loosing' stellar mass is a consequence of the fact that in our analysis each redshift bin is treated independently and the consistency of the model across different epochs is not guaranteed. The offset of about -0.15 dex in the example above probably arises from systematic uncertainties in the SMF at high redshift, from SED fitting effects (see e.g. discussion in Stefanon et al. 2015) or from cosmic variance issues (see e.g. Davidzon et al. 2017). Besides systematic errors, statistical uncertainties are already able to explain part of the issue: running our MCMC with an SMF shifted by -1σ (statistical error) at z =4, and $+1\sigma$ at z = 2.5, the stellar mass difference in the example above is only -0.06 dex.

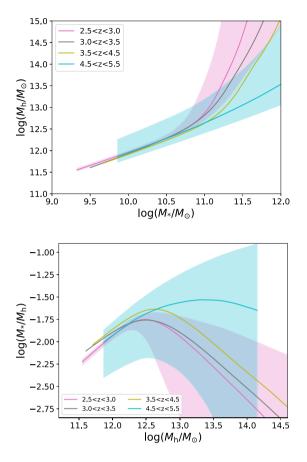


Figure 3. Same as Fig. 2 for redshift bins from z = 2.5 to 5.5. We show only uncertainties for the 2.5 < z < 3.0 and 4.5 < z < 5.5 bins for clarity.

The SHMR in the various redshift bins (upper panels of Figs 2 and 3) monotonically increases as a function of stellar mass with a changing of slope at $\sim M_h^{\text{peak}}$. Below the characteristic halo mass, the SHMR slope is approximately constant with redshift. Conversely, for masses above M_h^{peak} , it becomes flatter as moving towards higher redshifts (Fig. 3, upper panel) modulo the large error bars especially at 4.5 < z < 5.5.

These trends are clearly illustrated also in the lower panels of Figs 2 and 3 which show M_*/M_h versus M_h . In each bin, this ratio peaks at $M_h \simeq M_h^{peak}$ and drops by one order of magnitude at both the extremes of our halo mass range. At z < 0.5, $M_h^{peak} = 10^{12} M_{\odot}$, with $\log(M_*/M_h) = -1.55 \pm 0.5$. At higher redshifts, M_h^{peak} increases steadily up to $10^{12.5} M_{\odot}$ at z = 2, i.e. growing by a factor ~ 3 . It then remains flat up to z = 4. At a fixed halo mass above M_h^{peak} , M_*/M_h does not evolve, while in haloes below M_h^{peak} the ratio decreases from $z \sim 0$ to 2.5.

4.2 Dependence of the peak halo mass on redshift

Fig. 4 shows the redshift evolution of the peak halo mass between z = 0.2 and 4.5 computed from the median $M_{\rm h}^{\rm peak}$ for all the samples retained in the MCMC (see Section 3.2). The results are reported also in Table B2. Fig. 4 also presents a compilation of recent measurements from the literature together with model predictions (lines). At z > 3, it becomes progressively more difficult to measure the position of the peak as the slopes of halo and SMFs become similar (Fig. 1). In addition at higher redshifts, there are correspondingly smaller numbers of massive galaxies in the

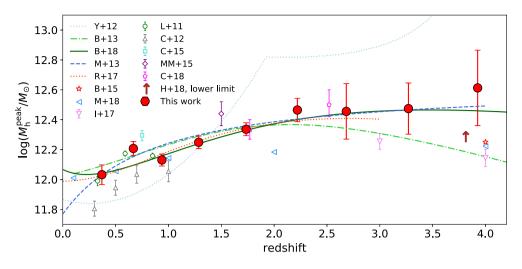


Figure 4. Peak halo mass M_h^{peak} as a function of redshift (red dots). We plot M_h^{peak} at the median redshift of each bin, rescaled to $H_0 = 70 \text{ km s}^{-1}\text{Mpc}^{-1}$. All masses from other studies have been rescaled to match the $H_0 = 70 \text{ km s}^{-1}\text{Mpc}^{-1}$ cosmology. Some points from the literature have been slightly shifted along the redshift axis for clarity. We show results from Leauthaud et al. (2011, L + 11), Yang et al. (2012, Y + 12), Coupon et al. (2012, C + 12), Moster et al. (2013, M + 13), Behroozi et al. (2013b, B + 13), Behroozi & Silk (2015, B + 15), Coupon et al. (2015, C + 15), Martinez-Manso et al. (2015, MM + 15), Rodríguez-Puebla et al. (2017, R + 17), Ishikawa et al. (2017, I + 17), Cowley et al. (2018, C + 18), Harikane et al. (2018, H + 18), Moster et al. (2018, B + 18). The brown arrow is the lower limit for M_h^{peak} from Harikane et al. (2018, H + 18).

COSMOS volume. Nevertheless, our measurements show clearly that the peak halo mass increases steadily from $10^{12}M_{\odot}$ at z = 0.3 to $10^{12.6}M_{\odot}$ at z = 4.

Below $z \sim 2.5$, there is generally a good agreement in the literature with $M_{\rm b}^{\rm peak}$ steadily increasing as a function of redshift. We confirm this trend despite some fluctuation (e.g. at $z \sim 0.7$) due to the overabundance of rich structures in COSMOS (see e.g. McCracken et al. 2015). Leauthaud et al. (2012), using a previous measurement of the COSMOS SMF at z < 1, find the same fluctuations. Leauthaud et al. perform a joint analysis of galaxygalaxy weak lensing and galaxy clustering to fit the SHMR modelled as in Behroozi et al. (2010). Moreover, they use an HOD to describe the number of galaxies per dark matter halo, instead of assuming only a single galaxy inhabits each dark matter halo. In fact, such an assumption has only a small impact on the $M_{\rm b}^{\rm peak}$ position given the fact that at $\sim 10^{12} M_{\odot}$ most of the haloes contain only one galaxy (McCracken et al. 2015). Cowley et al. (2018) used an HOD model to derive $M_{\rm h}^{\rm peak}$ for mass-selected sample of UltraVISTA galaxies in COSMOS at 1.5 < z < 2 and 2 < z < 3; their results are in good agreement with ours. Their error bars account for z_{phot} errors but not the stellar mass uncertainties; in their HMF, they apply Behroozi, Wechsler & Wu (2013a) high-redshift correction and introduce a large-scale halo bias parameter (Tinker et al. 2010).

Above $z \gtrsim 3$, the scatter in $M_{\rm h}^{\rm peak}$ increases. Moster et al. (2013) and Behroozi et al. (2013b)³ find different trends, i.e. an $M_{\rm h}^{\rm peak}$ (z) function that declines (Behroozi et al. 2013b) or flattens (Moster et al. 2013) with increasing redshift. One possible explanation for the discrepancy is that Moster et al. and Behroozi et al. models are based on different observational data sets. To address this issue, Behroozi & Silk (2015) repeated Behroozi et al.'s analysis removing z > 5 constraints (which in their method influence also the fit at lower z). However, this test is inconclusive as their M_h^{peak} estimate (shown as the star symbol in Fig. 4) falls between these curves.⁴

Our higher M_h^{peak} values with respect to Ishikawa et al. (2017) and Harikane et al. (2018) may be a consequence of our near-IR selection (a good proxy for stellar mass, see D17). Ishikawa et al. (2017) and Harikane et al. (2018) samples are selected in rest-frame UV (and a conversion to stellar mass is made through an average $L_{UV}-M_*$ relation). Moreover their redshift classification is derived (instead of z_{phot} estimates) from a Lyman-break colour–colour selection which may result in lower levels of purity and completeness at $z \sim 3$ (Duncan et al. 2014).

Recently, revised versions of Behroozi et al. (2013b) and of Moster et al. (2013) have been presented in Behroozi et al. (2018) and Moster et al. (2018). This new analysis differs from the former ones by following closely the evolution of individual halo-galaxy pairs through time. This results in a better understanding of the scatter of the SHMR, because this scatter results from the evolution of each halo-galaxy pairs, it is not an arbitrary scatter parameter added to the model. In Behroozi et al. (2018), the feedback model regulating star formation has significantly changed since Behroozi et al. (2013b). In the updated model, the $M_{\rm h}$ threshold at which 50 per cent of the hosting galaxies are quiescent grows from $10^{12} M_{\odot}$ at z < 1 up to $\sim 10^{13} M_{\odot}$ at z = 3.5 (see fig. 28 of Behroozi et al. 2018). As a consequence, the $M_{\rm h}^{\rm peak}$ evolution is now in excellent agreement with both Moster et al. (2013) and our estimates. Moster et al. (2018) peak halo mass shown here corresponds to the peak in the ratio between stellar mass and baryonic mass of galaxies (the $[M_*/M_h](M_h)$ relation. We assumed here that the ratio between baryonic mass and halo mass is a constant (equal to the universal baryon fraction), giving the same value for the peak halo mass of

³Values shown here were obtained using *Planck* cosmology instead of the published *WMAP* cosmology (Behroozi private communication). See comparison in fig. 35 of Behroozi et al. (2018).

 $^{{}^{4}}M_{\rm h}^{\rm peak}$ (z) error bars are not explicitly quoted either in Behroozi et al. (2013b) or Moster et al. (2013). However, we can quantify them through the uncertainties of their SHMR models. For example in the model of Moster et al. the 1 σ confidence level of the $M_1(z)$ parameter can be used as a proxy, leading to $M_{\rm h}^{\rm peak}$ error bars of the same order of magnitude of ours.

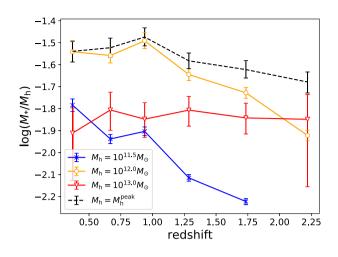


Figure 5. Evolution of M_*/M_h as a function of redshift for fixed halo masses (solid lines) and at $M_h \equiv M_h^{\text{peak}}$ (dashed line). Error bars are derived from Figs 2 and 3.

the $[M_*/M_h](M_h)$ relation. The difference with our results might be explained by a dependence of the baryon fraction of haloes with mass (see Kravtsov, Nagai & Vikhlinin 2005; Davies et al. 2018).

4.3 Dependence of M_*/M_h on redshift at fixed halo mass

Since M_*/M_h depends on host halo mass and redshift, we show in Fig. 5 this trend in more detail by computing the M_*/M_h ratio at different fixed values of halo mass. We restrict our analysis to z < 2.5 because at high-mass bins $(10^{13}M_{\odot})$ uncertainties in the M_*/M_h ratio prohibits a quantitative discussion of its evolution with redshift between z = 2.5 and 5.5.

For massive haloes $(10^{13}M_{\odot})$ the ratio is nearly constant between $z \sim 0.2$ and 2.5, whereas at $M_{\rm h} \simeq 10^{12}M_{\odot}$ it increases as cosmic time goes by reaching the maximum value (about 0.03) at $z \simeq 1$ and then remaining constant until $z \sim 0.2$. The redshift at which $10^{12}M_{\odot}$ haloes reach the maximum $M_*/M_{\rm h}$ ratio corresponds to the epoch when $M_{\rm h}^{\rm peak}$ is equal to their mass. Lower mass haloes, which are $<M_{\rm h}^{\rm peak}$ across the whole redshift range, steadily increase their $M_*/M_{\rm h}$ without any peak or plateau. For instance haloes with $M_{\rm h} \simeq 10^{11.5}M_{\odot}$ increase their $M_*/M_{\rm h}$ ratio by a factor ~ 3.2 from z = 2.5 to 0.2. For comparison, Fig. 5 also shows the increase of the $M_*/M_{\rm h}$ ratio, from z = 2.5 to 0.2, for haloes in a mass bin that evolves with redshift, i.e. $M_{\rm h} = M_{\rm h}^{\rm peak}(z)$. We discuss in Section 5 the interpretation of these evolutionary trends and the implications in terms of galaxy star formation efficiency.

4.4 Impact of halo mass function uncertainties

In order to estimate quantitatively how the choice of the HMF fit impacts our results, we repeat our analysis (Section 3) using different HMFs (Fig. 6). The SMF remains D17 in all the cases. Results at $z \leq 2$ are consistent, whilst at higher redshifts we clearly observe the impact of halo identification techniques. M_h^{peak} values using the HMF of either Tinker et al. (2008), Bocquet et al. (2016), or Despali et al. (2016) are grouped together, as those studies all applied a spherical overdensity criterion to define haloes. Bhattacharya et al. (2011) and Watson et al. (2013) use an FoF algorithm, and the resulting $\log(M_h^{\text{peak}}/M_{\odot})$ is systematically higher by ~0.1 dex at $z \geq 2$. In our study, these differences are smaller than other sources of uncertainty, but it is clear that in future larger surveys these differences may become important.

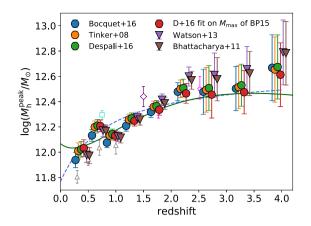


Figure 6. Peak halo mass (M_h^{peak}) computed using different HMFs. M_h^{peak} redshift evolution is independently measured six times, using different HMF fits: our Bolshoï–Planck fit of Despali et al. (2016, our main reference also shown in Fig. 4); the original Despali et al. (2016), Tinker et al. (2008), Bhattacharya et al. (2011), Watson et al. (2013), and Bocquet et al. (2016). Filled circles (triangles) indicate that the halo identification has been done with a spherical overdensity (FoF) algorithm. Each set of $M_h^{peak}(z)$ values derived for a given HMF is shifted by 0.05 in redshift for sake of clarity. SHAM method and observed SMF are the same for all estimates. Literature measurements are shown as in Fig. 4.

5 DISCUSSION

5.1 Evolution of the SHMR observed in COSMOS

To interpret our results, it is worth first recalling how the shape of the SMF changes from z = 5 to 0 (Fig. 1). The number density of intermediate-mass galaxies $(10^{9.5}M_{\odot} < M_* < 10^{11}M_{\odot})$ increases more rapidly compared to lower and higher masses galaxies. This causes the 'knee' of the SMF at $M_* \sim 10^{11}M_{\odot}$ to become progressively more pronounced. In comparison halo number density evolution is nearly independent of mass so the shape of the HMF is similar between z = 2 and 6 (modulo a normalization factor, see Fig. 1). The relative evolution of these two functions causes the changes in the M_*/M_h ratio.

The redshift evolution of the SMF shape is governed by several factors. On one hand, towards higher redshifts the high-mass end becomes increasingly affected by larger observational uncertainties (especially photometric redshift catastrophic failures: Caputi et al. 2015; Grazian et al. 2015). At the same time, specific physical processes control star formation around the knee of the SMF which are different from those affecting galaxies at lower masses (Peng et al. 2010). Here, we assume that most of the observational errors have been accounted for (Section 2) and consequently the redshift evolution of M_h^{peak} we measure in COSMOS is primarily driven by physical mechanisms.

The M_*/M_h ratio is usually interpreted as the comparison between the amount of star formation and dark matter accretion integrated over a halo's lifetime. Thus, a high M_*/M_h ratio in a given M_h bin implies that those haloes have been (on average) particularly efficient in forming stars. 'Star formation efficiency' is used hereafter to indicate 'galaxy formation efficiency', i.e. the whole process of stellar mass assembly from baryon accretion to the collapse of molecular clouds inside the galaxy. In addition to the *in situ* star formation, further stellar mass can be accreted via galaxy merging. In such a framework, the dependence of the M_*/M_h ratio on halo mass and redshift can be explained by a combination of physical phenomena. Our observational constraint on M_h^{peak} can help to understand which mechanisms, amongst those proposed in the literature, are most responsible for regulating galaxy stellar mass assembly.

 $M_{\rm h}^{\rm peak}$ can be considered as the threshold above which haloes maintain a nearly constant $M_*/M_{\rm h}$ ratio across time (Fig. 5). At a fixed halo mass below $M_{\rm h}^{\rm peak}$, the $M_*/M_{\rm h}$ ratio increases as comic time goes by, indicating that stellar mass has 'kept up' with dark matter accretion. For a fixed halo mass above $M_{\rm h} \simeq M_{\rm h}^{\rm peak}$, host galaxies are more likely to enter in a quiescent phase ('quenching' the star formation) and thereafter passively evolve. Fig. 5 clearly shows this evolution with redshift for fixed halo masses. For objects with $M_{\rm h} = 10^{12} M_{\odot}$, their $M_*/M_{\rm h}$ increases until $z \sim 1$ (i.e. when $M_{\rm h}^{\rm peak} = 1.3 - 1.6 \times 10^{12} M_{\odot}$) after which the ratio remains constant until z = 0.2. Note that we do not track the evolution of individual haloes but instead the evolution of the $M_*/M_{\rm h}$ ratio for a given halo mass. This makes the interpretation of the evolution of individual haloes with time more difficult (haloes at high redshift are not necessarily the same as haloes of the same mass at low redshift).

5.2 What physical mechanisms regulate star formation in our sample?

In this work, we consider primarily the redshift evolution of M_h^{peak} . Our deep near-IR observations allow us to leverage the COSMOS2015 galaxy sample to constrain that threshold up to z = 4 (Fig. 4). We find that the $M_h^{\text{peak}}(z)$ function changes slope at $z \sim 2$, showing a plateau at higher redshift. This implies that the threshold for massive galaxies to enter the quenching phase depends on redshift: in the early Universe quenching mechanisms are less effective for galaxies in haloes between 10^{12} and $10^{12.5} M_{\odot}$. This scenario should also take into account the contribution of major and minor mergers but in the redshift and halo mass ranges of our analysis they can be considered sub-dominant (see Davidzon et al. 2018 and references therein). Therefore, in the following we will focus on quenching models affecting the *in situ* star formation.

In their cosmological hydrodynamical simulations, Gabor & Davé (2015) implement a heuristic prescription to halt star formation in systems with a large fraction of hot gas.⁵ The condition to trigger the quenching phase, which Gabor & Davé call 'hot halo' mode, happens exclusively at $M_h > 10^{12} M_{\odot}$ in their simulation. This halo mass threshold is in agreement with M_h^{peak} . However, Gabor & Davé (2015) carry out their analysis at z < 2.5. At higher redshift, this prescription would be in disagreement with our results. Also Behroozi et al. (2018), considering the evolution of the quiescent galaxy fraction, emphasize that a quenching recipe with a constant temperature threshold could not explain the observational trend. As the difference between a constant and a time-evolving threshold becomes more relevant in the first ~2 Gyr after the big bang (see fig. 28 in Behroozi et al. 2018), our results are extremely useful to discriminate between these different scenarios.

The hot halo model is agnostic regarding the sub-grid physics of the simulation: gas heating can be caused by either stable virial shocks (Birnboim & Dekel 2003) or AGN feedback (see a review in Heckman & Best 2014). With respect to the former mechanism, simulations in Dekel & Birnboim (2006) show that shock heating in massive haloes becomes inefficient at high redshift because cold streams are still able to penetrate into the system and fuel star formation (see also Dekel et al. 2009). However, despite that this trend is in general agreement with our results there are quantitative differences in the evolutionary trend. With the fiducial parameters assumed in Dekel & Birnboim (2006) the 'critical redshift' at which $\sim 10^{12} M_{\odot}$ haloes start to form stars more efficiently is $z_{\rm crit} \simeq 1.5$. Moreover, according to their model $M_{\rm h}^{\rm peak}$ should keep increasing at $z > z_{\rm crit}$ instead of plateauing.

Quenching models more compatible with our observational results have been presented e.g. in Feldmann & Mayer (2015). Under the assumption that gas inflow (thus star formation) is strongly correlated to dark matter accretion, the authors note that at z > 2massive haloes are still collapsing fast and dark matter filaments efficiently funnel cool gas into the galaxy. At $z \leq 2$, those haloes should enter in a phase of slower accretion that eventually impedes star formation by gas starvation. However, we caution that they study single galaxies in cosmological zoom-in simulations: a larger sample may show considerable variance in the redshift marking the transition between the two dark matter accretion phases. In addition, we emphasize that not only the accretion rate but also the cooling timescale is a strong function of redshift. Gas density follows the overall matter density of the Universe, evolving as $\propto (1+z)^3$. Since the post-shock cooling time is proportional to gas density, it would be significantly shorter at higher redshift. On the other hand, this argument in absence of more complex factors should lead to a steeper, monotonic increase of $M_{\rm h}^{\rm peak}$ that we do not observe.

As mentioned above, AGN feedback at high redshifts can also regulate galaxy star formation and explain our observed M_h^{peak} trend. AGN activity at high redshift is expected to be almost exclusively in quasar mode (e.g. Silk & Rees 1998) with powerful outflows that can heat or even expel gas. However such radiative feedback has shown to be inefficient in hydrodynamical 'zoom-in' simulations at $z \sim 6$ (e.g. Costa et al. 2014). Observations also indicate that high-*z* quasars do not prevent significant reservoirs of cold gas from fuelling star formation (e.g. Maiolino et al. 2012; Cicone et al. 2014). Therefore, star formation in massive haloes can proceed for 2–3 Gyr after the big bang without being significantly affected by AGN activity, in agreement with our observations. At later times, perturbations to cold filamentary accretion can starve galaxies of their gas supplies (Dubois et al. 2013).

A deeper understanding of the role played by AGN comes from studying their co-evolution with supermassive black hole (BH). Beckmann et al. (2017) show that once renormalized for the ratio between the BH mass ($M_{\rm BH}$) and the virial mass of the halo, the impact of AGN feedback is the same from z = 0 to 5. According to their hydrodynamical simulations (from the HORIZON-AGN suite, Dubois et al. 2014) this process is able to suppress galaxy stellar mass assembly when $M_{\rm BH}/M_{\rm h} > 4 \times 10^{-5}$. In first approximation, this critical threshold is in good agreement with the one that can be derived from COSMOS if the critical BH mass ($M_{\rm BH, crit}$) is correlated with $M_{\rm h}^{\rm peak}$. Assuming a BH-to-stellar mass ratio of 2×10^{-3} (Marconi & Hunt 2003) we can write

$$\frac{M_{\rm BH,crit}}{M_{\rm h}^{\rm peak}} = \frac{M_{\rm BH}}{M_{*}} \times \left(\frac{M_{*}}{M_{\rm h}}\right)^{\rm peak} = 2 \times 10^{-3} \times 10^{-1.7 \pm 0.1},\tag{4}$$

which gives $3-5 \times 10^{-5}$ including the variation in the M_*/M_h ratio calculated at $M_h \equiv M_h^{\text{peak}}$ (see Figs 2, 3, and 5). At least at z < 2, the antihierarchical growth of the BH mass function (Marconi et al. 2004; Shankar, Weinberg & Miralda-Escudé 2009, 2013) implies that more massive BHs form earlier, so M_h^{peak} must also increase (as we find in COSMOS) in order to keep the ratio constant. In other words, if we assume that the quenching threshold $M_{\text{BH,crit}}/M_h^{\text{peak}}$ is universal, BH formation models can use the COSMOS SHMR as an

⁵Namely, their code prevents gas cooling in FoF structures by setting the circumgalactic gas equal to the virial temperature. This condition is triggered when a structure has 60 per cent of gas particles with a temperature > $10^{5.4}$ K (Kereš et al. 2005).

indirect constraint. Part of the redshift evolution may also be due to the ratio between $M_{\rm BH}$ and M_* . In equation (4), we used a constant value but other studies indicate that such a relationship varies depending on the galaxy bulge component (Reines & Volonteri 2015). However, in the HORIZON-AGN simulation this quantity has been shown to remain constant ($\sim 2 \times 10^{-3}$) up to z = 3 (Volonteri et al. 2016).

Recently, Glazebrook et al. (2017) reported a massive $(M_* = 1.7 \times 10^{11} M_{\odot})$ and quiescent galaxy at a spectroscopic redshift of z = 3.717. This observation suggests a scenario where in the early Universe dark matter haloes are hosting massive star-forming galaxies and that the quenching of star formation appears as early as $z \sim 4$. According to our SHMR relation, this stellar mass corresponds to a halo mass of $M_{\rm h} = \sim 10^{12.5} M_{\odot}$ so around our value of $M_{\rm h}^{\rm peak}$ for z = 4. This observation is in agreement with our argument that $M_{\rm h}^{\rm peak}$ is the characteristic mass for haloes currently undergoing quenching.

Depending on their location within the cosmic web (filaments, nodes, voids) haloes with similar masses may experience different accretion histories (De Lucia et al. 2012). One key idea in this context is 'cosmic web detachment' (Aragon-Calvo, Neyrinck & Silk 2016): galaxies tied to nodes or filaments are removed from their original location by interaction with another galaxy. After the detachment gas supply - and then star formation becomes less efficient. Aragon-Calvo et al. (2016) suggest that massive haloes are the first to detach, whereas less massive haloes $0.1-3 \times 10^{10} h^{-1} M_{\odot}$ are still part of the cosmic web today. It is difficult to test this scenario beyond the local Universe because precise measurements of the SMF are required in addition to higher order statistics (e.g. three-point correlation functions). We emphasize that COSMOS is the ideal laboratory to test the impact of large-scale environment in the models mentioned above, because the cosmic structure of this field has been reconstructed at least up to $z \sim 1$ (Darvish et al. 2014; Laigle et al. 2018). We aim to perform such an analysis in a future work.

In summary, we have described different physical processes which could explain our observed trends of M_h^{peak} and the SHMR with redshift. Of course, in the real Universe the truth is likely to be some combination of these mechanisms. But based on this discussion, the physical processes at work in results seem to be best understood as a combination of cold-flow accretion and AGN feedback combined with antihierarchical growth of the BH mass function, with the precise role of evolutionary and environmental effects yet to be determined.

6 CONCLUSIONS

We have used an SHAM technique combined with precise SMF measurements in COSMOS to make a new measurement of the SHMR from $z \sim 0$ to 5. We accounted for the principal sources of uncertainties in our stellar mass measurements and photometric redshifts. We also tested the impact of HMF uncertainties on the resulting SHMR. At $z \sim 0.2$, we found that the ratio of mass in stars to dark matter halo mass (M_*/M_h) peaks at a halo mass of $10^{12.05 \pm 0.07} M_{\odot}$. This peak mass increases steadily to $10^{12.48 \pm 0.08} M_{\odot}$ at $z \sim 2.3$, and remains almost constant up to z = 4.

By comparing our results to studies that rely on models accounting for both central and satellite galaxies, we have shown that at least at z < 2, the distinction between central and satellite galaxies has only a limited impact on the peak halo mass $M_{\rm h}^{\rm peak}$. A complete modelling including satellite galaxies is left to a future work. We found that the M_*/M_h ratio has little dependence on redshift for haloes more massive than M_h^{peak} , but strongly depends on redshift for less-massive haloes, consistent with the picture that the star formation has been quenched in massive haloes and continues in less massive haloes. We showed that the evolution of the shape of the SMF has a strong impact on the SHMR: the change in the position of the knee of the SMF is responsible for the shift in the value of M_h^{peak} . Accurate SMF estimations at high redshift for massive galaxies are needed to constrain the SHMR. We also show how mass function uncertainties can influence our measurements of M_h^{peak} .

We discussed qualitatively which physical processes control the SHMR and $M_{\rm h}^{\rm peak}$, which we interpret as the characteristic mass of quenched haloes. We speculate that this evolutions can either be related to AGN feedback or to environmental effects such as cold gas inflows at high redshift and cosmic web detachment.

Our study is based on a phenomenological model and as such can provide no direct information concerning the physical processes acting inside haloes. Next-generation hydrodynamical simulations will allow us to better understand the small-scale physical processes acting inside dark matter haloes and determine what physical effects control star formation. In the next few years, the combined 20 deg² Spitzer–Euclid legacy and Hawaii-2-0 surveys on the Euclid deep fields will provide much better constraints on the massive end of the SMF at high redshifts. Precise photometric redshifts will allow us to investigate in detail the role of environment and in particular the 'cosmic web' role in shaping galaxy and dark matter evolution.

For future surveys like Euclid, errors on the cosmological figure of merit will be dominated by systematic errors. For this reason, it is essential to understand the interplay between baryons and dark matter on small scales and the uncertainties present in estimates of the HMF.

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APPENDIX A: FITTING THE BOLSHOÏ-PLANCK HMF FOR M_{MAX}

Fig. A1 shows the fit of the Despali et al. (2016) HMF on the halo number densities of the Bolshoï–Planck simulation, using the maximal mass in the history of the haloes. See Section 2.2.

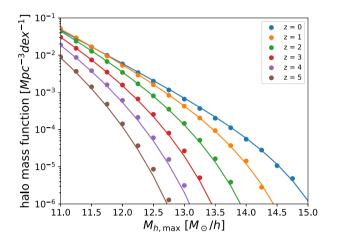


Figure A1. Points show halo densities obtained from the Bolshoï–Planck simulation for different redshift snapshots. The fit of the Despali et al. (2016) HMF on this data points is shown as the plain lines.

APPENDIX B: MCMC BEST FIT PARAMETERS

In this Appendix, we provide further details about the COS-MOS2015 galaxy SMF (median z and limiting stellar mass of each bin, see Table B1) and the best-fitting parameters of equation (1) resulting from our MCMC method (see Table B2). In addition, Figs B1–B3 show the MCMC posterior distributions in the 10 redshift bins independently considered in this analysis.

 Table B1.
 Median redshift of each redshift bin and limiting stellar mass of COSMOS survey as defined in D17.

Redshift bin	Median z	$\frac{\log{(M_{*,\rm lim}/M_{\odot})}}{8.17}$		
(0.2, 0.5]	0.370			
(0.5, 0.8]	0.668	8.40		
(0.8, 1.1]	0.938	8.58		
(1.1, 1.5]	1.29	8.77		
(1.5, 2.0]	1.74	8.98		
(2.0, 2.5]	2.22	9.17		
(2.5, 3.0]	2.68	9.32		
(3.0, 3.5]	3.27	9.50		
(3.5, 4.5]	3.93	9.67		
(4.5, 5.5]	4.80	9.86		

Table B2. Best-fitting parameters for the 10 redshift bins with their 68 per cent confidence intervals, and $M_{\rm h}^{\rm peak}$ recovered from the best-fitting SHMR with its 68 per cent confidence interval.

Redshift bin	$\log{(M_1/M_\odot)}$	$\log{(M_{*,0}/M_{\odot})}$	β	δ	γ	ξ	$\log(M_{\rm h}^{\rm peak}/M_{\odot})$
[0.2, 0.5]	$12.49_{-0.094}^{+0.13}$	$10.84_{-0.077}^{+0.11}$	$0.463^{+0.040}_{-0.030}$	$0.77^{+0.16}_{-0.29}$	< 0.802	$0.138^{+0.034}_{-0.066}$	12.05 ± 0.07
[0.5, 0.8]	$12.668^{+0.089}_{-0.074}$	$11.039_{-0.060}^{+0.074}$	$0.458^{+0.026}_{-0.023}$	$0.81_{-0.24}^{+0.17}$	< 0.723	$0.099^{+0.022}_{-0.027}$	12.22 ± 0.05
[0.8, 1.1]	$12.614_{-0.060}^{+0.073}$	$11.006^{+0.056}_{-0.042}$	$0.437^{+0.025}_{-0.022}$	$0.93\substack{+0.19\\-0.28}$	< 0.955	0.088 ± 0.015	12.14 ± 0.04
[1.1, 1.5]	$12.642_{-0.069}^{+0.086}$	$10.978^{+0.072}_{-0.054}$	$0.407^{+0.029}_{-0.023}$	$0.80\substack{+0.16\\-0.23}$	< 0.629	$0.092^{+0.023}_{-0.025}$	12.26 ± 0.04
[1.5, 2.0]	$12.78_{-0.072}^{+0.10}$	$11.053\substack{+0.080\\-0.055}$	$0.438^{+0.035}_{-0.026}$	$0.82^{+0.17}_{-0.25}$	< 0.724	0.075 ± 0.017	12.35 ± 0.04
[2.0, 2.5]	$13.062\substack{+0.078\\-0.087}$	$11.15_{-0.095}^{+0.11}$	$0.525^{+0.033}_{-0.027}$	$1.09_{-0.68}^{+0.36}$	<2.08	$0.128\substack{+0.045\\-0.050}$	12.48 ± 0.08
[2.5, 3.0]	13.11 ± 0.18	11.09 ± 0.25	$0.598^{+0.045}_{-0.036}$	$1.01^{+0.55}_{-0.72}$	-	$0.216_{-0.14}^{+0.061}$	12.47 ± 0.19
[3.0, 3.5]	$13.14_{-0.20}^{+0.22}$	11.14 ± 0.27	$0.631\substack{+0.071\\-0.038}$	$0.73_{-0.54}^{+0.35}$	<2.47	$0.176_{-0.085}^{+0.074}$	12.49 ± 0.17
[3.5, 4.5]	$13.30_{-0.27}^{+0.20}$	$11.41_{-0.46}^{+0.28}$	$0.625_{-0.039}^{+0.056}$	_	<2.93	0.231 ± 0.099	12.63 ± 0.25
[4.5, 5.5]	$14.35_{-1.0}^{+0.89}$	<13.5	$0.642_{-0.11}^{+0.094}$	_	_	$0.45_{-0.34}^{+0.22}$	13.35 ± 0.54

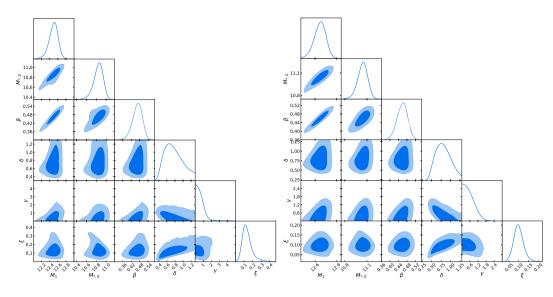


Figure B1. 1D and 2D marginalized distributions for the six free parameters. Solid contours give the 68 and 95 per cent confidence intervals. Left-hand panel is for redshift bin [0.2, 0.5], and right-hand panel is for redshift bin [0.5, 0.8].

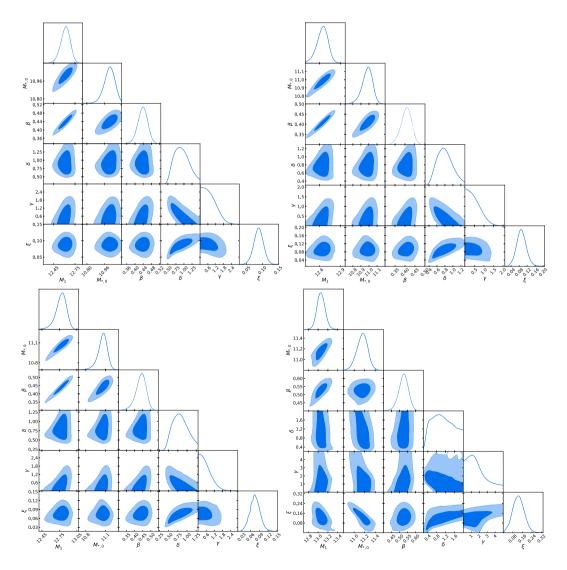
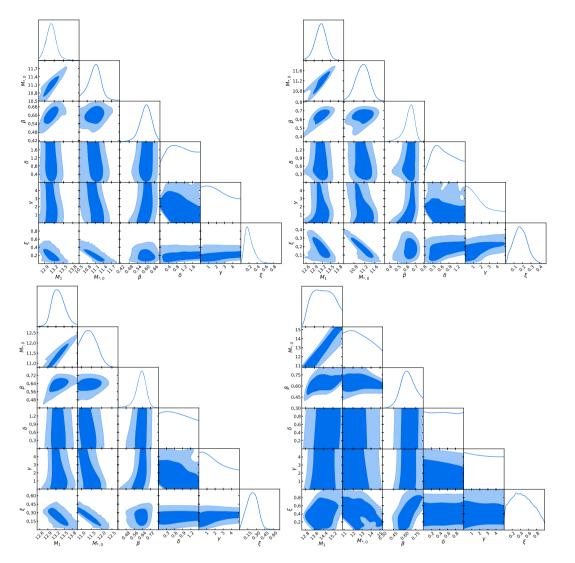


Figure B2. Same as B1 for (from left to right and top to bottom) [0.8, 1.1], [1.1, 1.5], [1.5, 2], and [2, 2.5] redshift bins.



 $Figure \ B3. \ Same \ as \ B1 \ for \ (from \ left \ to \ right \ and \ top \ to \ bottom) \ [2.5, 3], \ [3, 3.5], \ [3.5, 4.5], \ and \ [4.5, 5.5] \ redshift \ bins.$

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