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Mode I fracture of tropical woods using grid method.

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Abstract

The cracking properties in opening mode of three tropical species from the Gabonese forest, namely Iroko (*Milicia Excelsa*), Okume (*Aucoumea klaineana* Pierre), and Padouk (*Pterocarpus soyauxii*), were investigated in this study. Various tests were performed at room temperature and for two different thicknesses. A full-field measurement technique, namely the grid method, was used in order to obtain the displacement and strain maps near the crack during the tests. The mechanical parameters, the specificities of the wood species, the Arcan system and the grid transfer method are first described. For all the specimens, the initial crack length was oriented along the fiber direction (RL). The instantaneous failure tests were performed using two types of specimens: the modified Compact Tension Shear (CTS) and the Mixed Mode Crack Growth (MMCG) specimens. The images of the grid were recorded and analyzed to obtain the displacement maps. The crack opening, the location of the crack tip as well as the strain fields on the surface of the specimens were deduced from these displacement maps. The experimental critical energy release rate G_c was evaluated by the compliance method in imposed displacement. In the case of instantaneous crack with CTS specimens, the comparison of the initial value of G_c for all the samples show that this quantity strongly depends on the thickness and density of the species under study. Crack propagation was observed for a thickness equal to 20 *mm* only. The results of the crack propagation with the MMCG specimens show the same dependence, and confirm the quasi-brittle fracture behavior of Iroko. The experimental results are scattered, but clear trends can be observed concerning the fracture parameters of the in previous studies described in the literature on wood species with wood species under study. The results are finally compared with those given densities similar to those studied here.

Keywords: Tropical woods, fracture analysis, MMCG and CTS specimens, grid method.

1. Introduction

Wood contributes to sustainably limit global warming by fixing greenhouse gases [1]. In Central Africa and more specifically in equatorial regions, the forest plays a key role in this regulation [2, 3]. In the case of Gabon, which shelters various species [4], the forest represents 85% of the territory, among which 13% represents protected national parks. This significantly contributes to the regulation of the climate change [5, 6, 7]. In addition, the recent decision of the Gabonese government to stop the exportation of tropical species has opened the way to their local expansion, and a more systematic use in local individual and industrial buildings [8, 9, 10]. However, the mechanical behavior of these species, and more specifically their failure properties, remains poorly studied in the literature, which hampers the reliable design of such structures. This may lead for instance to the sudden failure of structures during their service life, which is not acceptable. Studying the failure properties of tropical woods is therefore crucial to guide local engineers in their choice of building materials other than concrete and steel.

This paper focuses on the initiation of crack and on crack propagation at room temperature of the following tropical species: Okume (*Aucoumea Klaineana Pierre*), Iroko (*Milicia Excelsa*) and Padouk (*Pterocarpus Soyauzii*). The choice of these species is justified first by the fact that they are widespread in the tropical forest. They are therefore commonly used in carpentry/paper marking, in cooperage, packaging, maritime work, and luxury furniture [11, 12, 6]. A short review of the literature shows that few authors investigated the mechanical behavior of these tropical species [13], which limits their use in structural applications. Such species however feature interesting properties. For example, they are quite homogeneous, and the studies available on their mechanical properties show that they have interesting characteristics in terms of hardness, fracture toughness, shearing and compression properties parallel to the grain. Some authors propose suitable models for the strength of some Cameroonian hardwood species in tension [14], as well as for the strength properties of branchwood and stemwood of some tropical hardwood structure species [15], but these studies do not deal with failure properties. Some other papers concern Okume, see [12, 6], for instance. The radial growth and characterization

of juvenile and adult wood in plantations is investigated more specifically in [6]. Recently, the hydro-mechanical behavior of *Aucoumea Klaineana Pierre* under drying process [16] and under cyclic compressive loading has been studied for different internal moisture contents [17, 10]. However, the fracture mechanics aspects are not discussed for the three species studied here. Note finally that the influence of the physical and mechanical characteristics on the behavior of some tropical woods during machining is studied in [18].

Various geometries have been proposed in the literature in order to determine the fracture parameters of non-tropical species. Among them, following the compact shear specimen developed by Richard [19], Valentin [20] proposed a new Compact Tension Shear (CTS) specimen geometry in order to study the mixed mode fracture properties of orthotropic materials such as wood. However, due to the shape and thickness of such wood specimens, the portion of the loading curve where crack propagation occurs is narrow and unstable. In order to overcome this instability issue, it is proposed in Ref. [21] a specimen featuring a new geometry inspired from that described in Ref. [22]. This new specimen is named Mixed Mode Crack Growth (MMCG) specimen. It is shown in [21] that crack growth in Abied Alba Mills is stable in opening mode with this type of specimen. With this geometry, it is also possible to obtain a stable crack process in mixed mode configuration, and to identify the most influencing parameters of wood failure [23]. The MMCG geometry was used in the present study for these reasons. Some CTS specimens were also employed to investigate the effect of the thickness on the failure properties of the three species under study.

In mechanics, proposing the appropriate model in order to track the crack tip and to measure the crack opening generally relies on specific tests for which suitable models and measuring methods are available. Full-field measurement techniques such as Digital Image Correlation (DIC) have been used for this purpose in several cases [24, 25, 26, 27, 28, 29]. Belrhiti et al. dealt with the refinement of the digital image correlation technique to study the fracture behavior of refractory materials [30]. The grid method features however a better compromise between spatial resolution and displacement resolution than DIC, as recently shown in [31]. This is illustrated in [32] for instance, where crack propagation is studied in notched aluminium specimens. This technique is therefore used here again in the case of wood specimens.

In the present work, the objective is to study the fracture behavior in the crack opening mode of Okume, Iroko and Padouk by using the grid method at room temperature. CTS and modified MMCG specimen geometries are considered in order to obtain the instantaneous crack for these species. In addition, different thicknesses are also tested to see their impact on the energy release rate at the beginning of propagation and at break, especially for MMCG specimens.

2. Materials and method

Wood specimens

Tropical climates are characterized by a high rainfall almost all the year. The dry season is short in time, and this does not allow the soil to absorb large amount of water. This also causes the dryness of the plants not to occur. It means that the trees have a continuous growth in these regions. The distinction between summer wood and winter wood is therefore not perceptible in tropical species, which is not the case in species growing in temperate-climate countries. The samples were cut approximately one meter above the roots of the tree on feet (see the blue square in Figure 1). All samples were oriented along the direction of the grain (see the direction of the red arrow in Figure 1). The three species under study also exhibit various density values, which is important here since this parameter is known to influence the fracture properties of wood. Okume belongs to the category of very light woods (relative density 0.44). Okume has a light red color, which tends towards the white in the dry state. Its grain is fine. It can reach between 60 and 120 *cm* in diameter. Its use class is 2 [33]. Iroko is classified as light and medium heavy (relative density 0.64). Iroko is yellow brown in color with golden reflections. Its grain is coarse and its diameter can reach 80 to 100 *cm*. It is classified in use class 3. Finally, Padouk falls in the categories medium heavy and heavy (relative density 0.79). Padouk is red in color. Its grain is coarse and its diameter lies between 60 and 100 *cm*. Its use class is 4 et 5. Figure 1 shows the aspect of the three species, from the tree to the specimens.

The moisture content (MC) of the specimens are given in Table 1. This quantity is found using the following formula:

$$MC(\%) = \frac{m_S - m_0}{m_0} \times 100\% \quad (1)$$

where m_S is the original weight and m_0 the oven-dried weight. The specimens were therefore first weighted to obtain the wet mass noted m_S . These values were obtained at room temperature, $T=21^\circ\text{C} \pm 2^\circ\text{C}$, and relative humidity (HR) = $42\% \pm 2\%$. The other mechanical properties are collected in Ref. [11]. They were obtained for $T = 22^\circ\text{C}$, $MC = 12\%$ and $HR = 44\%$ (Table 1). The specimens were put in an oven set at a temperature of 110°C to determine the dry mass m_0 . The standardized temperature is 103°C [34], but temperature between 100°C and 130°C are often used in practice and accepted. The temperature that we used here falls within this range. The specimens remained in the oven until the mass had completely stabilized for 4 days. The specimens were weighted three times a day to check if their weight had stabilized. The values were also measured with a hygrometer and the results obtained with this device are similar to those obtained with Equation 1.

Wood	Aucoumea klaineana	Milicia excelsa	Pterocarpus soyauxii
Species	or Okume (SD)	or Iroko (SD)	or Padouk (SD)
Average Relative Density	0.44 (0.06)	0.64 (0.06)	0.79 (0.09)
MOE (MPa)	9690 (1231)	12840 (2496)	15870 (1885)
MC (%)	9.12	7.94	7.29
CSR (MPa)	36 (5)	54 (6)	65 (8)
CRFS (MPa)	62 (11)	87 (15)	116 (24)

Table 1: Mechanical characteristics. MOE: longitudinal modulus of elasticity, MC: moisture content, CSR: compression stress of rupture, CRFS: static bending failure stress, SD: Standard deviation.

In Table 1, it can be observed that the internal humidity of the specimens decreases as the density increases, which seems logical. The pieces of trunks of all the species tested here were cut in Gabon beforehand and kept under equatorial atmosphere for 1 month. They were then shipped to the place where the tests were carried out (Aubiere, France). These pieces were kept at room temperature in the laboratory, under the environment described above. The samples were therefore debited in the environmental conditions of the laboratory. In this case, no drying of the samples was observed during the tests. The internal moisture content of all the specimens given in Table 1 were measured just before

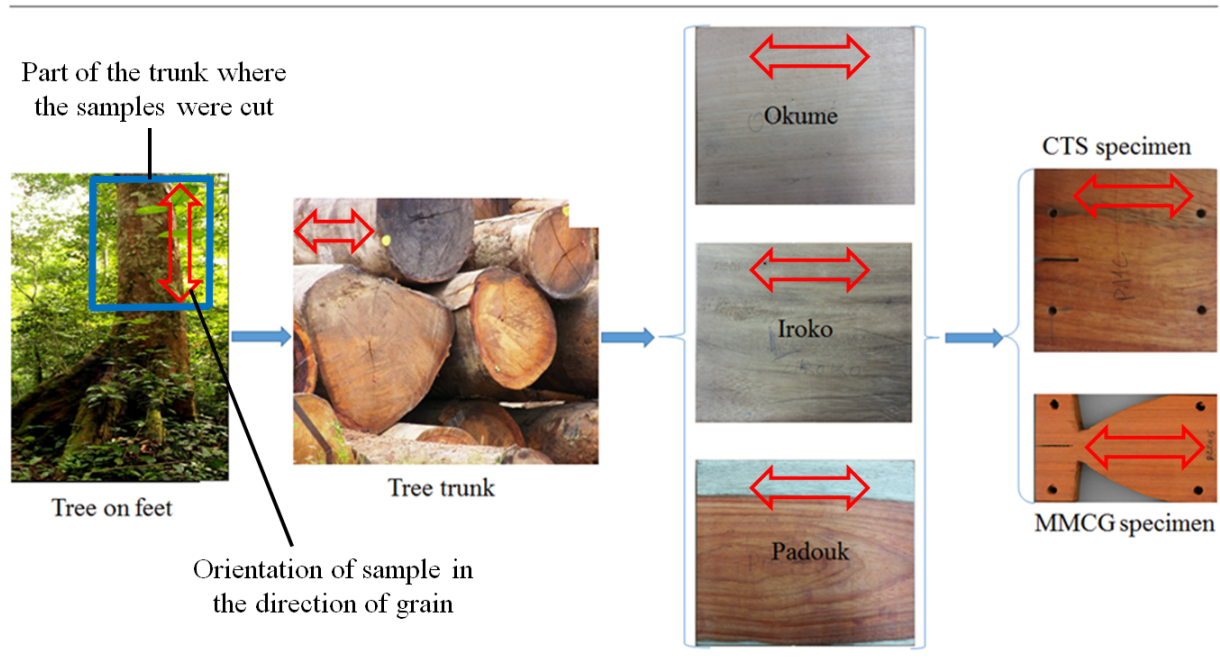


Figure 1: From the tree to the specimens.

testing.

Wood CTS and modified MMCG specimens

The dimensions of the CTS specimens are given in Figure 2. Two values for the thickness were considered, namely 12.5 mm and 20 mm , to see if this parameter influences the results. For all the specimens, a notch (25 mm in length) was machined along the fiber (RL) direction. The notch was then slitted with a cutter over a length of about 3 mm to initiate the crack so the initial length a of the crack is equal to 28 mm . Figure 3 represents an example of CTS specimen for each wood specie.

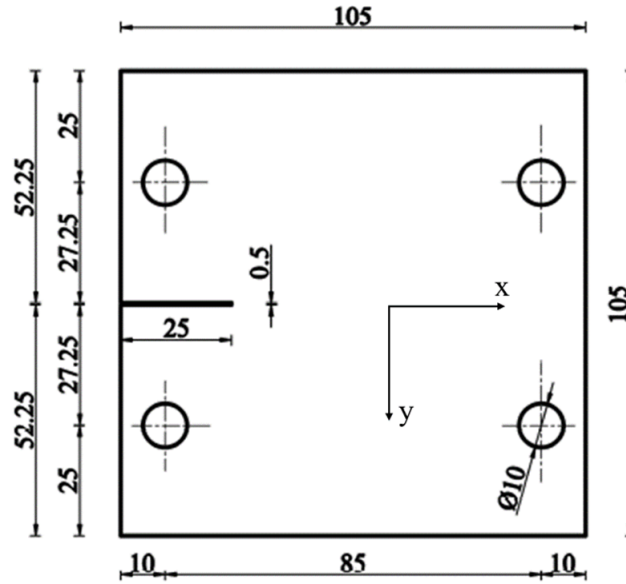


Figure 2: Dimensions of the CTS specimen (in mm).

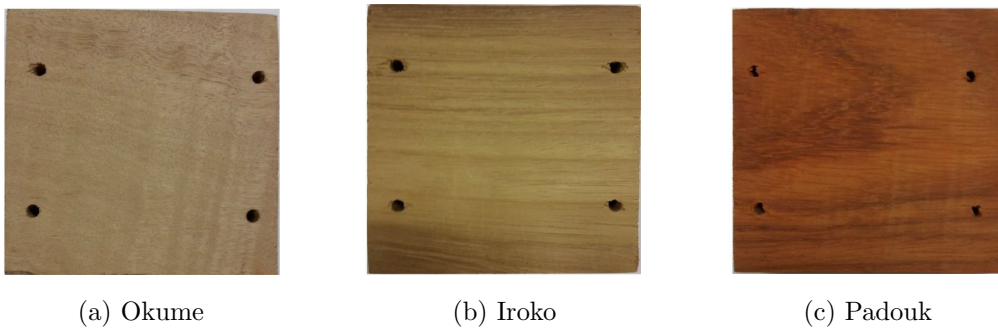


Figure 3: Typical CTS specimens.

Compared to the initial version of the MMCG specimen [21], the size of the specimens tested here is somewhat smaller. The reason is that we used here the same testing device as that used for the CTS specimen, thus limiting the size of the MMCG specimens (see Figure 4). For all the MMCG specimens, the initial length a of the crack was equal to $(20\text{ mm} + 2\text{ mm})$. Figure 5 shows typical MMCG specimens. Two values for the thickness were considered in the study, namely 15 mm and 20 mm .

The advantage of the MMCG specimen is that crack propagates in a stable manner after appearance. On the contrary, CTS specimens are generally characterized by the instantaneous crack propagation after appearance, making the phenomenon unstable. An apparent crack stability is observed if the thickness of the CTS specimen becomes significant. The advantage of the MMCG specimen is also to obtain a decrease of the energy release rate during crack growth. In this case, if the material is viscoelastic, one can easily

separate time-dependent effects and fracture parameters in order to know the real impact of time on the failure of the material.

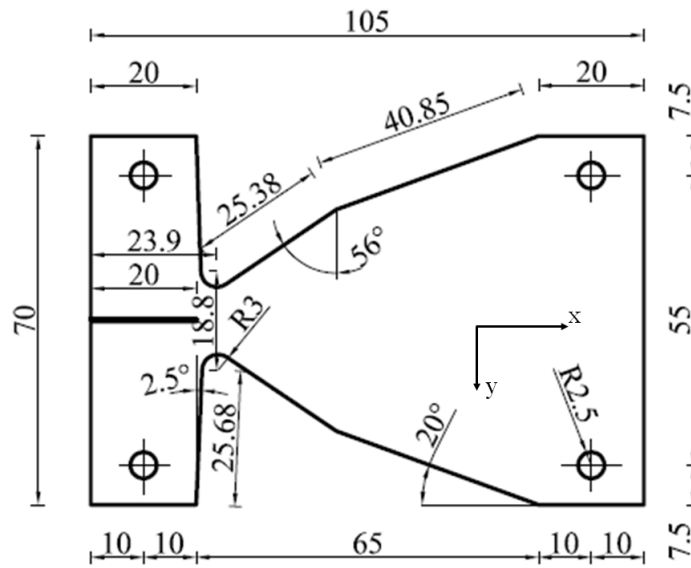


Figure 4: Dimensions of the modified MMCG specimen (in mm).

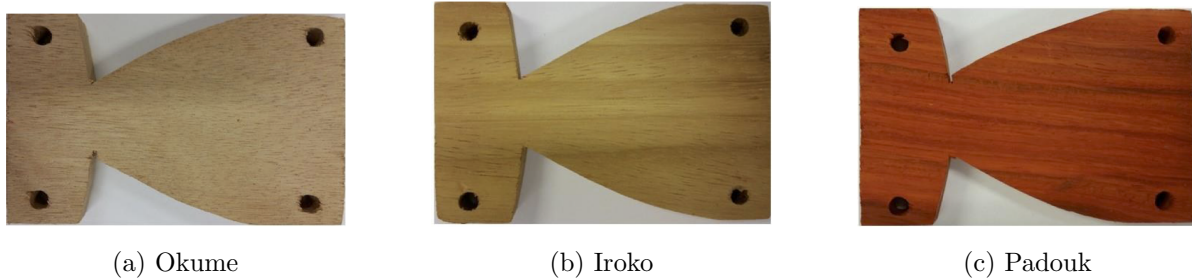


Figure 5: Typical MMCG specimens for three wood species: Okume, Iroko and Padouk.

Wood species	Aucoumea klaineana (Okume)	Milicia excelsa (Iroko)	Pterocarpus soyauxii (Padouk)
Tested CTS specimens	O12.5	I12.5	P12.5
	O20	I20	P20
Tested MMCG specimens	O1M15	I1M15	P1M15
	O2M15	I2M15	P2M15
	O1M20	I3M15	P3M15
	O2M20	I4M15	P1M20
	O3M20	I1M20	P2M20

Table 2: Notations used in this study. where: O = Okume; I = Iroko; P = Padouk; 1,2,3,..= Test number for MMCG specimens; M = MMCG; 12.5, 15 and 20 = Thickness of the specimens.

Table 2 gives the notation and the name of the specimens tested for this paper. Six CTS specimens were tested (three species, two thickness values per specie). For the MMCG specimens, we report here only the tests for which crack propagation could really be observed and quantified, which explains why the percentage of specimens featuring a 15 *mm* and 20 *mm* thickness fluctuates from one specie to each other.

Figure 6 shows two typical examples of tested specimens. Aluminium washers were bonded to reinforce the fastening holes. They limit the risk of early failure of the specimens in the connexion zone. The upper part of the specimens was reinforced with small aluminum plates for the same reason. An epoxy adhesive was used to bond the washers and the small plates. A grid was transferred on the surface of each specimen in order to determine the displacement and strain fields. It is clearly visible in Figure 6. The method used to process the grid images is described in the next section. Depending on the specie and on the specimen, the orientation of the fibers is more or less visible to the naked eye. Some deviation with the theoretical orientation of the fibers can also be observed. This is visible through the slight inclination of the fibers with respect to the orientation of the initial crack.

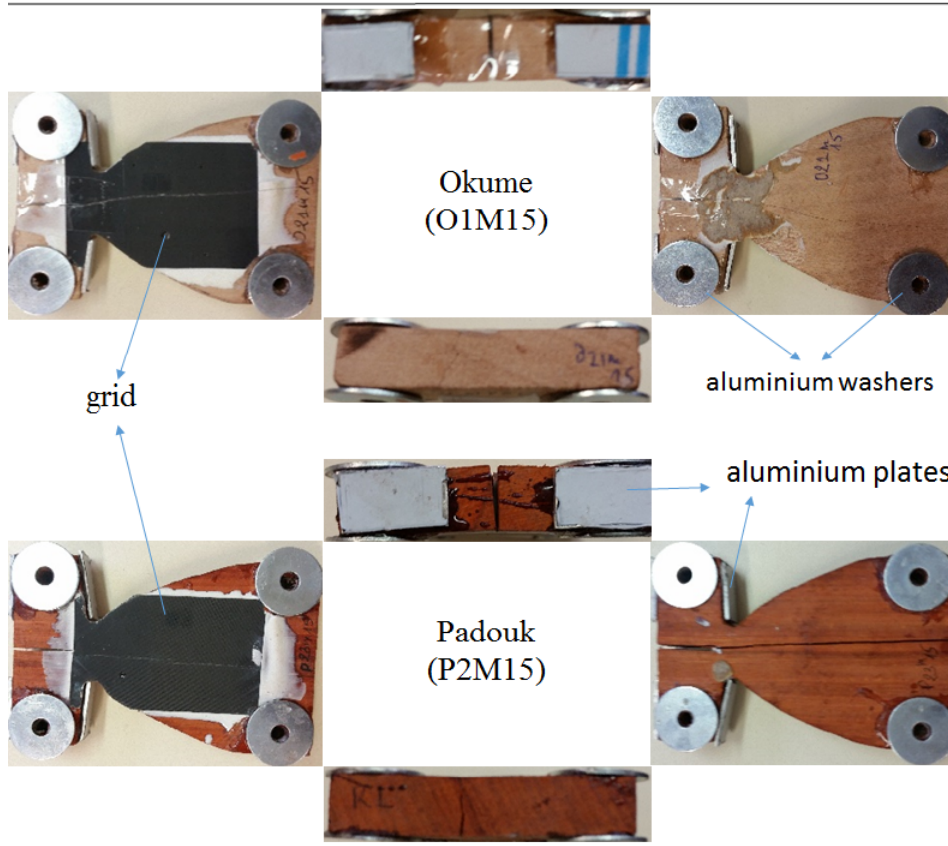


Figure 6: Typical MMCG specimens equipped with grids.

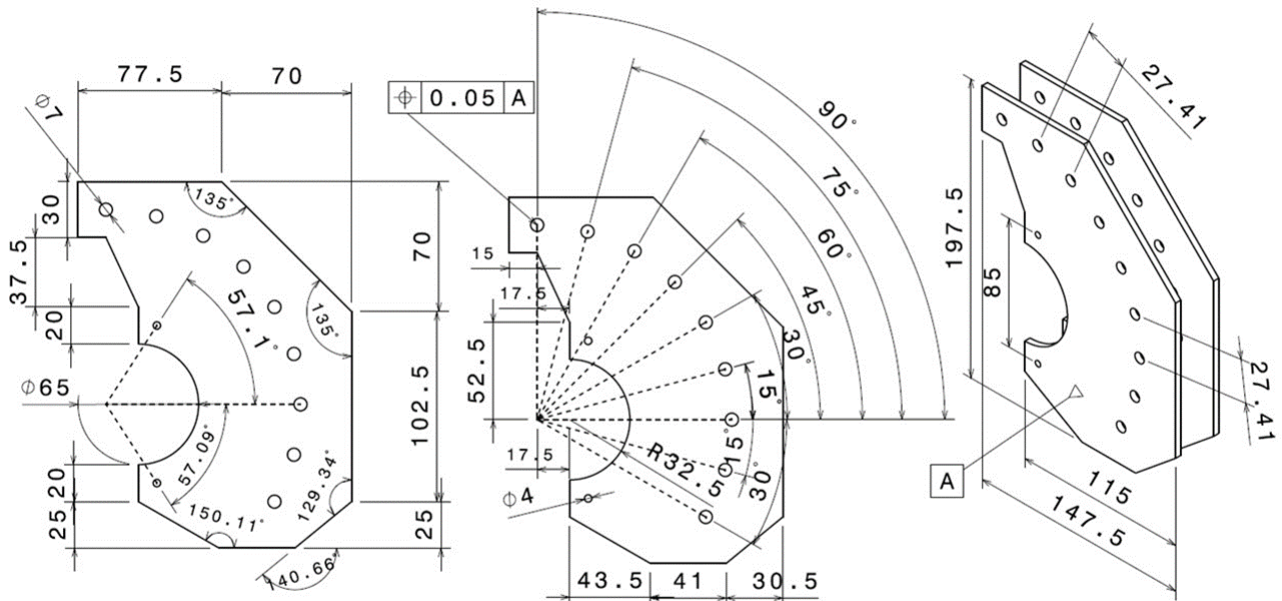


Figure 7: Dimensions of the Arcan fixture (in mm).

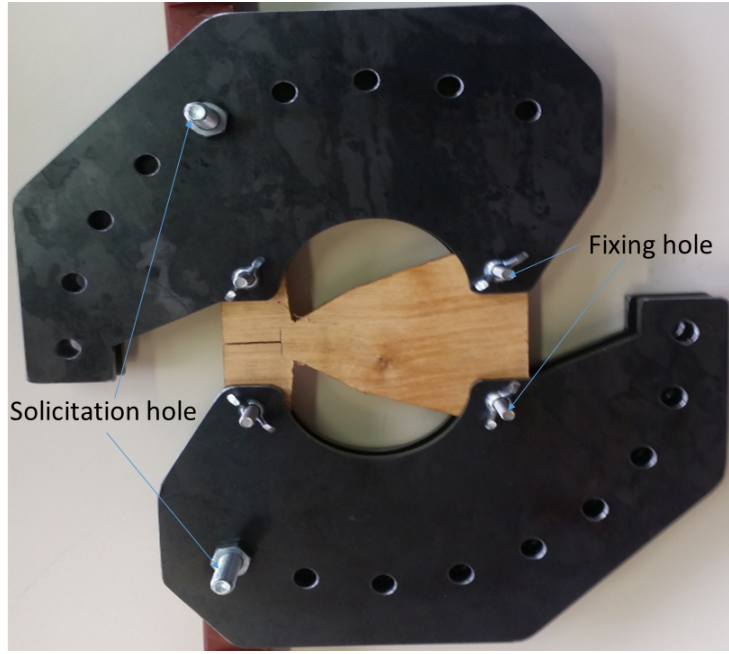


Figure 8: MMCG specimen and Arcan fixture.

Figures 7 and 8 show the Arcan testing device designed and machined specifically for this study. It is made of high tensile strength steel (HLE), whose main characteristics are given in [35]. This Arcan device is suited to both the modified CTS and the modified MMCG specimen geometries. A finite element simulation was performed to check that the limit of elasticity in the Arcan testing device was not attained during the test. The fixing holes for the wood specimens had a diameter $\varphi = 5 \text{ mm}$, and the loading holes (see Figure 8) a diameter $\phi = 7 \text{ mm}$. These fixing holes were drilled in order to be able to load the specimen with different orientations with respect to the vertical direction in order to activate mixed cracking modes. This orientation is described by an angle denoted β . In the present cas, only mode 1 is considered, which corresponds to the specimen and device shown in Figure 8.

Measuring displacement and strain fields using the grid method

The grid method is employed here to measure the in-plane displacement field on the front face of the specimen in order to detect and track the crack tip during the tests. This technique consists in processing images of a grid transferred onto the specimen before testing in order to determine the displacement and strain maps [36]. A bidirectional grid with a pitch value equal to 0.2 mm is first printed with a high-resolution printer (50,800 dots per inch) onto a thin polymeric sheet. This sheet is then bonded on the sample

using a thin white adhesive layer (reference: Epotecny E504). After polymerization of the adhesive layer, the polymeric sheet is peeled off and only the ink remains bonded on the white adhesive layer. The final thickness of this layer is typically equal to some tenths of mm, so it can be reasonably assumed that the grid perfectly reflects the deformation of the surface of the specimen without influencing it. Full details on the grid transfer procedure are given in [37]. Images of transferred grids are then taken with a camera during the test. The PCO Sensicam camera used in this study has a 12-bits/ 1040×1376 -pixels CCD sensor (CCD=charge-coupled device). It is equipped with a 105 mm lens. The magnification (and thus the distance d between camera and specimens) was adjusted in such a way that the grid period was sampled with 5 pixels. This leads to $d = 670 \text{ mm}$. With this setting, the crack and a portion of the specimen, which contains the crack under study, were in all the cases within the field of view of the camera. The camera captured about 1.83 frames/second during the tests. It was checked that with this configuration and with the prescribed displacement rate equal here to 0.005 mm/s , a temporal image averaging over 8 frames could be performed without inducing any blurring of the grid images. This averaging procedure is performed for noise reduction purposes, as studied in [38]. This averaging was made only for the CTS specimens, not with the MMCG specimens tests. The reason is that some dynamic events such as sudden crack propagation appeared during the tests, and the best possible temporal resolution was needed to capture such events between two consecutive images. Finally all these grid images were processed after testing using an in-house programme. The pattern being quasi-periodic, the program relies on Fourier analysis to compute the phase change of the quasi-regular marking of the surface. The reason is that the displacement field is proportional to this phase change [36]. Note that this measurement technique has been used successfully recently to measure the strain fields in wood specimens [39, 40]. Full details on this grid image processing technique are given in a recent review [31]. In this last paper, the authors compared the grid method and DIC, which is the most popular technique used in experimental mechanics. Other recent versions of the corresponding programs are available online [41].

As for DIC, the systematic error is all the higher as the frequency of the actual strain distribution is high. Further information on this phenomenon is available in [36, 42, 43]. The random error is mainly due to sensor noise propagation. The standard deviation for the noise in displacement and strain maps has been estimated in [43] with similar experi-

mental conditions (lighting, type of camera, shutter time, aperture). In [43], the standard deviation for the noise in displacement maps (U_x or U_y) due to sensor noise propagation is less than one micrometer. The same quantity for strain (ε_{xx} or ε_{yy}) typically lies between 3 and 4×10^{-4} , depending on the lighting conditions. It is $\sqrt{2}$ times lower for ε_{xy} . This noise level is lower when grid images are averaged over time.

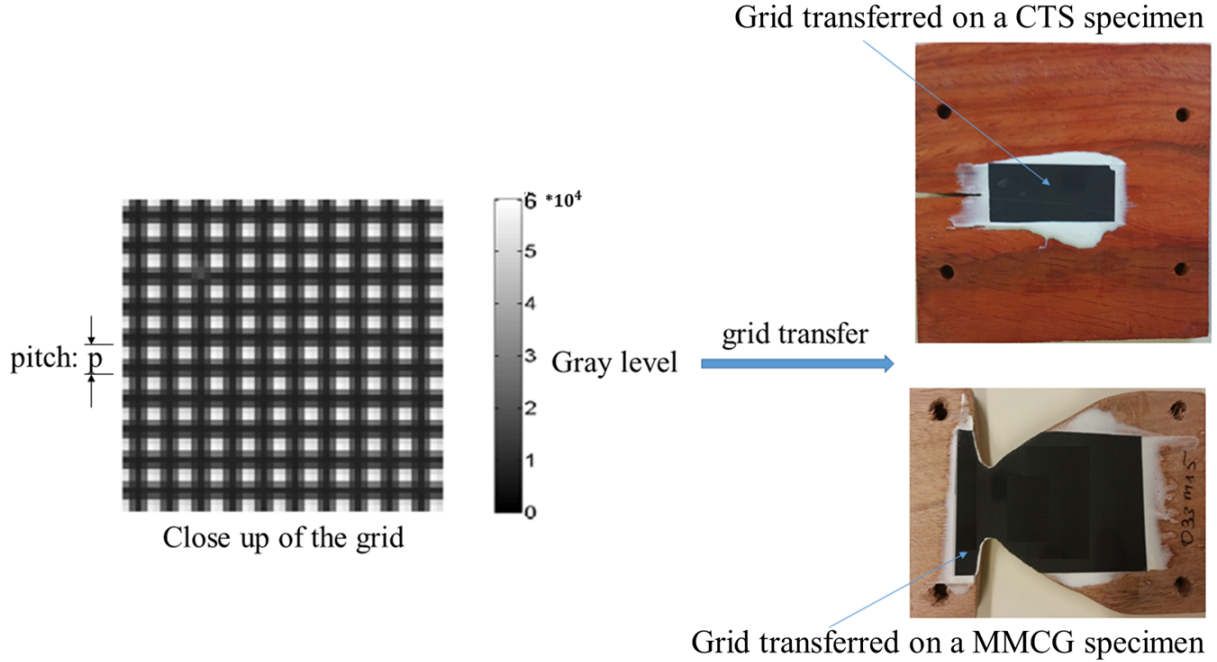


Figure 9: Typical examples of grid transferred on CTS and MMCG specimens.

Compliance Method

In this study, the value of G_c of the three species was calculated using the compliance method. The following equation was used for this calculation:

$$G_C = \frac{F c_i^2}{2b} \times \left(\frac{\Delta C}{\Delta a} \right)_d \quad (2)$$

where $F c_i$ ($i = 1, 2, 3, \dots$) is the so-called critical strength which indices an increase Δa of the crack length a , and b is the thickness of the specimen. As a general remark, the compliance is defined by $\Delta C = U_i / F c_i$, where U_i is the crack opening induced by each critical load $F c_i$. In Equation (2), ΔC is the increase in compliance corresponding to the increase in crack length Δa . Index d in Equation 2 means that the test is carried out

with an imposed displacement. For the MMCG specimens, crack propagating stepwise, we deal with the increments ΔC and Δa between two stable configurations of the crack. Figure 10 shows a typical strength-crack opening curve in which sudden strength drops are clearly visible. Small force changes are however not really observable in practice to the naked eye, so small drops are detected automatically by a in-house program, and the corresponding crack length increase is deduced from the displacement maps.

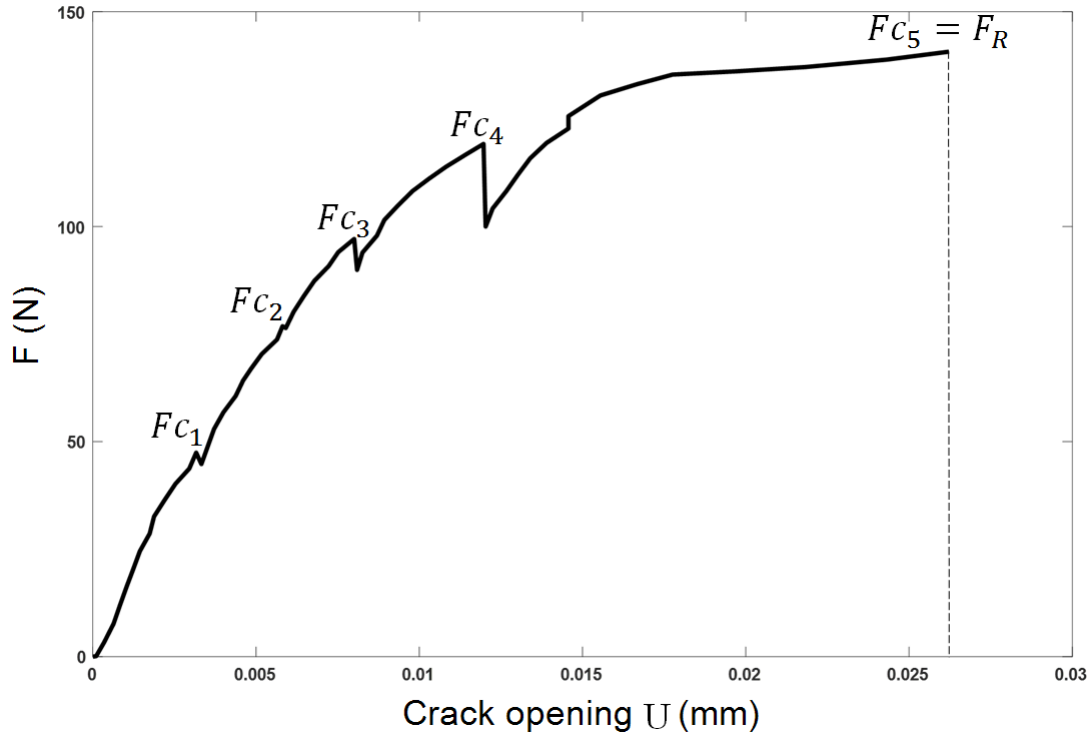


Figure 10: Force versus the crack opening U .

Deducing the crack opening and the location of the crack tip from the displacement field

Crack opening

The crack opening U involved in Equation 2 is deduced from the displacement maps by using the following procedure. Two points A and B are chosen. They are located each on one of the opposite sides of the crack (see Figure 11). These points are sufficiently far away from the crack itself to be sure that the determination of the displacement at those points is not impaired by the presence of the singularity in the displacement field due to the crack. These points must however be sufficiently close to the crack, so that the

difference between the vertical displacement measured at those points can be considered as the crack opening along the vertical line defined by these points. In practice, this distance is slightly greater than one half of the width of the window of the Windowed Fourier Transform (WFT) used in the software which processes the grid images. This window is a Gaussian with a standard deviation equal to 5 pixels. It means that according to the 3-sigma rule, $5 \times 3=15$ pixels is the minimum distance that should be used between each point and the crack. The crack is located between these two points but its location may fluctuate from one specimen to each other. Consequently, the distance between A and B was chosen to be equal to 90 pixels to have a sufficient safety margin. Then, the crack opening is obtained according the difference introduced by the following absolute value $u_y(A) - u_y(B)$.

Location of the crack tip

The location of the crack tip must be precisely estimated, the crack tip propagation being involved in Equation 2 above. It is important to mention that the precise location of the crack tip cannot be directly estimated by investigating the displacement field to the naked eye. The main reason is that the displacement field returned by the program processing the grid images is, at first approximation, the actual one convolved by the window used in the WFT [44]. A spatially correlated noise, whose covariance matrix is estimated in [44], is added to this result. The convolution causes the displacement maps to be slightly blurred, and the crack tip is thus not clearly visible. In this context, the location of the crack tip was determined using the same procedure for all the displacement maps. Its main steps are as follows:

- a rectangular zone supposed to contain the crack tip is first defined ;
- the gradient of the displacement field along the vertical y direction, in other words the apparent value for ε_{yy} , is estimated by numerical differentiation of the displacement field in this zone ;
- the apparent value for ε_{yy} is expected to tend toward infinity for the points of the maps belonging to the crack, but the apparent value returned by the image differentiation of the displacement map is finite, with a value which diminishes when approaching to the crack tip. A threshold value for the apparent value of ε_{yy}

is therefore fixed, and the coordinates of the crack tip are defined by the coordinates of the point located as right as possible (the crack propagates from left to right), and for which this threshold value is attained.

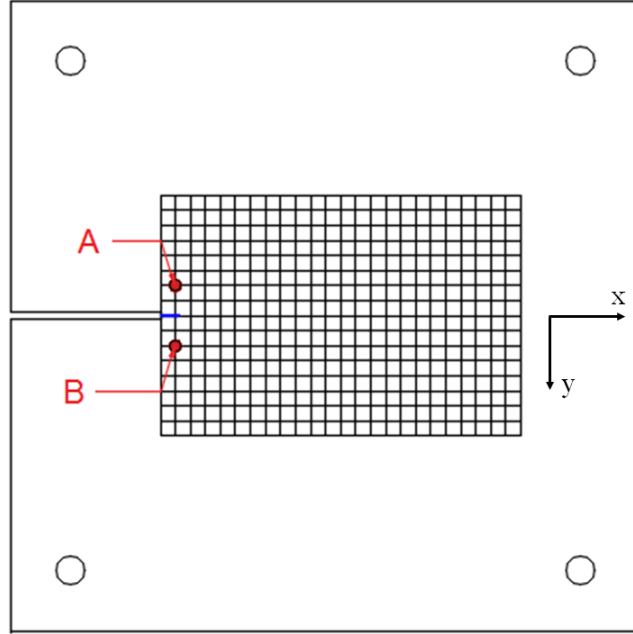


Figure 11: Points A and B used for determination of the crack opening U .

The threshold value for ε_{yy} was chosen to be equal to 0.10. This choice may potentially affect the result, so other values close to 0.10 were also tested to see if the coordinates of the crack tip are really sensitive to this parameter. Figure 12 shows the coordinate of the crack tip obtained for three values of this threshold, namely 0.08, 0.10 and 0.12. A Padouk specimen (P32M20) is used for this purpose. It should be noted that the crack front is not precisely defined in quasi-fragile materials, because of the mechanism of propagation of the crack which creates a failure zone.

It can be concluded that changing this threshold value around 0.10 does not influence the results. Choosing 0.10 can therefore be considered as reliable. Figure 13 shows a typical point cloud showing the location of the crack tip for a set of images captured during a typical test on a Padouk specimen. These coordinates are obtained with the detection method described above.

It is clear in this figure that the crack propagates stepwise, since some “voids” are visible along the x -direction, between the abscissa of two consecutive locations of the crack tip, see for instance between $x = 500$ and $x = 530$ pixels. Δa in Equation 2 is

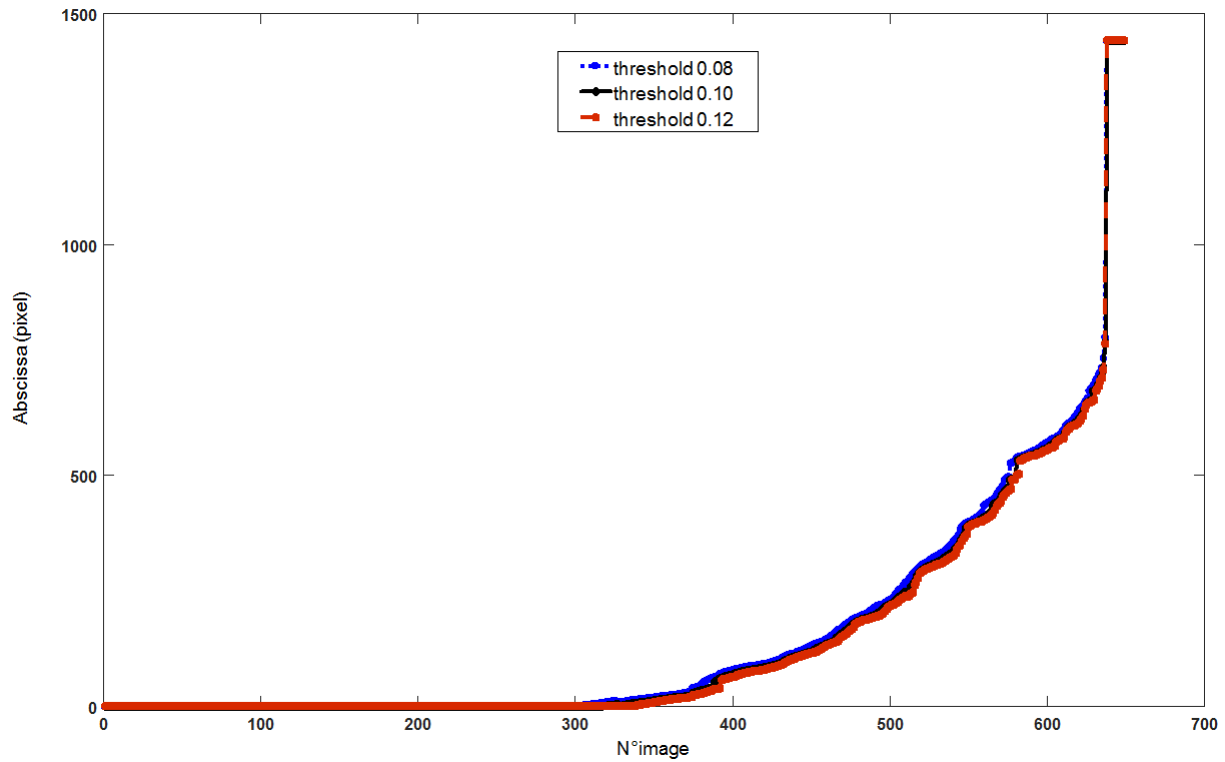


Figure 12: Abscissa of the crack tip obtained for three different threshold values of ε_{yy} .

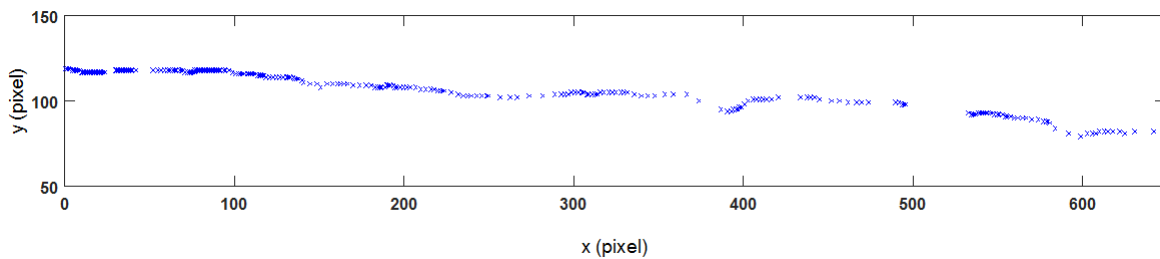


Figure 13: Location of the crack tip.

obtained by subtracting directly the abscissa of two consecutive points in case of force drop, the vertical change in location being negligible.

Experimental setup

A 200 kN Zwick / Roel testing machine shown in Figure 14 was used to perform the tests. The camera and the Arcan fixture described above are clearly visible in this figure. The camera was fixed on a tripod in order to shot stabilized grid images during the tests. The miniature steel Arcan fixture used to load the specimens is also visible. The testing machine, driven with imposed displacements, was equipped with a force transducer. The information combined with the displacement u_y obtained with the grid method gave us the force-displacement curves for each test.

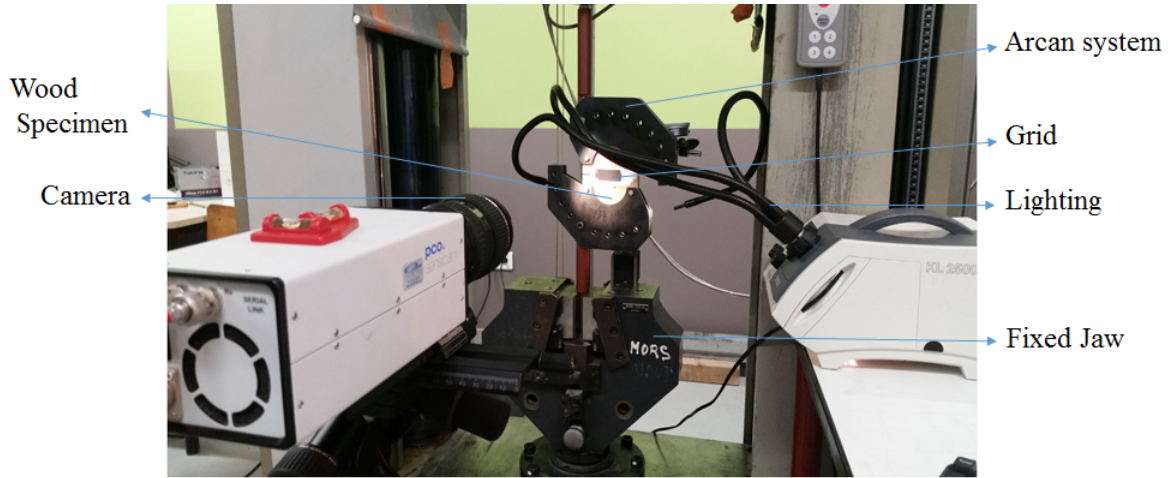


Figure 14: Experimental setup.

3. Results and Discussion

The results of the tests are presented in this section. Various curves are presented and discussed. The energy release rate for both the CTS and MMCG specimens are calculated and analyzed for the three wood species.

Displacement and strain maps.

Typical vertical displacement (u_y) and strain maps (ε_{yy}) obtained with the grid method at the end of the tests are shown in Figures 15 and 16 for the CTS and MMCG specimens, respectively. Displacement maps are used to determine the crack opening during the test and strain maps enable us to localize the location of the crack tip. The methodology was presented in the previous section. For the sake of clarity, only two species (Okume and Padouk) are presented in Figures 15 and 16 for the two thicknesses considered here (12.5 mm and 20 mm for CTS specimens and 15 mm and 20 mm for MMCG specimens).

Cracks are clearly visible in Figures 15 (a) and 16 (a). They correspond to discontinuities in the vertical displacement maps. The value of the displacement is negative because the upper jaw moves in the opposite direction of the y-axis. Consequently, the absolute value of the vertical displacement is the highest at the top zone of the maps. Generally, cracks tend to propagate along the fiber direction. This is clearly visible for the MMCG specimens which were tested in the RL plane. In practice, the crack path is very complex: when specimens are tested in the LR or LT planes, cracks always propagate along a direction, which is parallel to the grain.

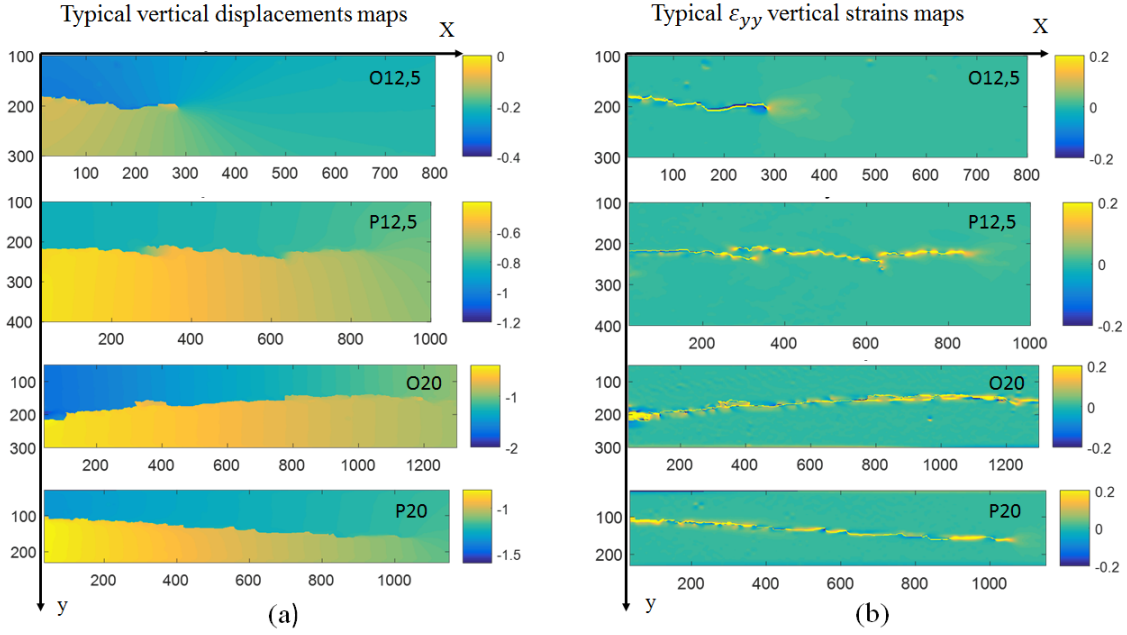


Figure 15: Typical maps for CTS specimens at the end of the tests : a) displacement maps; b) strain maps.

The strain values presented in Figures 15 (b) and 16 (b) are close to zero except in the neighborhood of the cracks. Observing the typical maps shown in Figures 15 (b) and 16 (b) enables us to highlight an interesting feature: for the CTS *O12.5* and MMCG *O1M15* specimens for instance, the crack propagation is driven by the transverse tension at the front of the crack tip, where strain concentration occurs. This result is also visible for CTS *P12.5* and *P20* specimens in the corresponding strain maps showing the crack tip.

Analyzing the strain maps for several loading levels is useful to characterize the two types of cracks: instantaneous or progressive. Results for the three wood species, the two types of tested specimens and the two thicknesses for each type of test are presented in the following sections.

Load - Crack opening curves.

The global load - crack opening curves are presented in Figure 17 for the CTS specimens, and in Figures 18 to 20 for the MMCG specimens. The crack opening values (displacement of the two lips of the crack) are directly obtained from the displacement maps, following the methodology presented in Section “crack opening”. The displace-

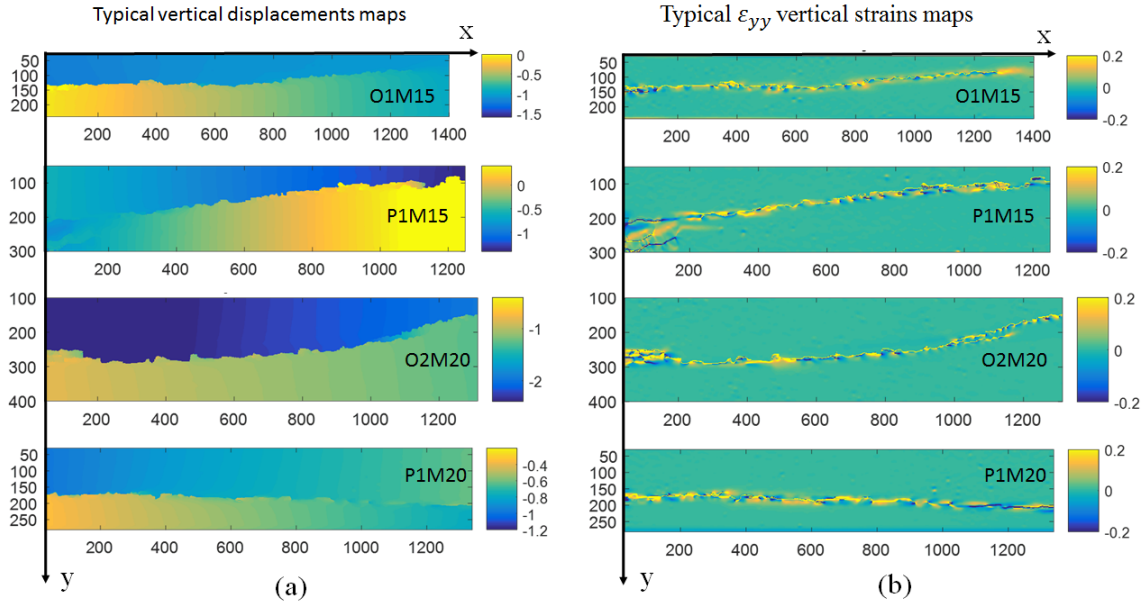


Figure 16: Typical maps for MMCG specimens at the end of the tests : a) displacement maps; b) strain maps.

ment of the moving jaws is not used here because it is higher than that obtained with the displacement maps due to the clearance take-up that occurs during the test.

Two thickness values are studied: 12.5 mm and 20 mm for the CTS specimens. Table 3 presents the loading values at failure and the corresponding maximum crack opening for these two thicknesses and for the three wood species. The influence of the thickness on the loading value at failure is clearly visible. Indeed, the loading value at failure is smaller for the thin specimens than for the thick ones. The maximum crack opening also depends on the thickness of the specimen but its influence is less sensitive than for the loading value at failure. For the $P20$ and $O20$ specimens, the crack opening evolves progressively, and several critical force F_c directly obtained from the load-crack opening curves. The maximums crack opening corresponding to the failure load for thickness values equal to 12.5 and 20 mm have been specified.

Two thicknesses are studied: 15 mm and 20 mm for the MMCG specimens. Due to the high heterogeneity of the specimens and their densities, the load values at failure are not directly related to what was obtained with the the thickness, contrary to what was obtained with the CTS specimens. Similarly, the maximum crack opening value strongly fluctuates from one specimen to another for a given specie and for a given thickness. However, the load at failure of the Padouk specimens are above 1200 N regardless of the thickness of the specimen, with two exceptions. This result underlines the influence of the

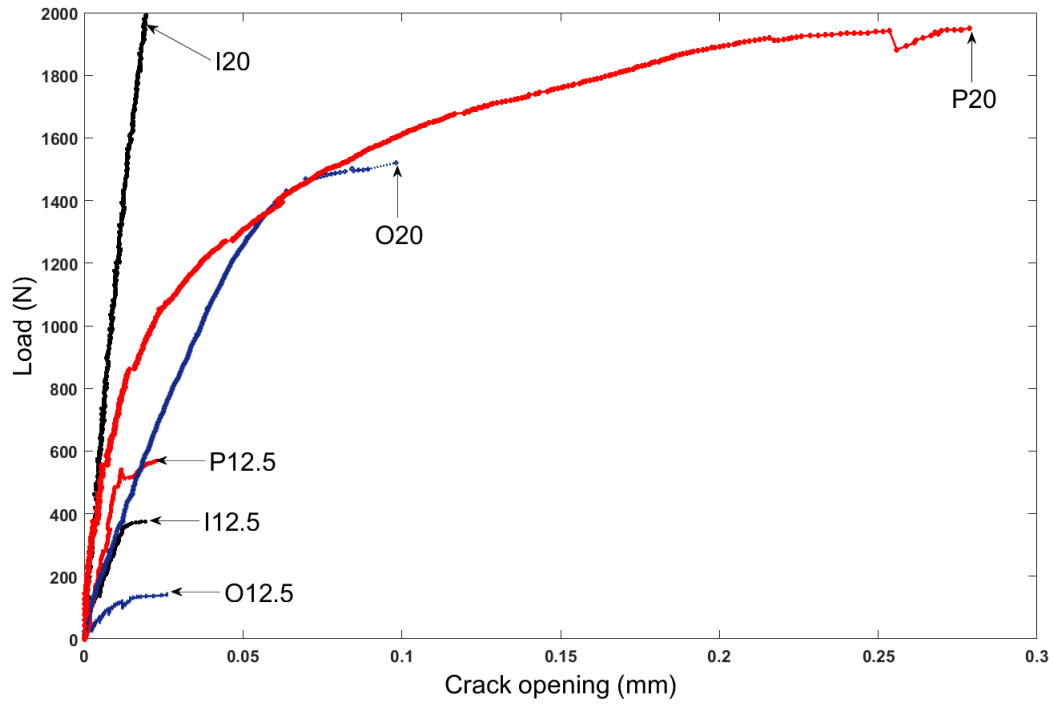


Figure 17: Load - crack opening curves for the CTS specimens.

	Thickness: 12.5 mm		Thickness: 20 mm	
	Load value at failure (N)	Maximum crack opening (mm)	Load value at failure (N)	Maximum crack opening (mm)
Okume	141	0.030	1520	0.090
Iroko	375	0.019	1991	0.019
Padouk	568	0.020	1950	0.280

Table 3: Load value at failure and corresponding crack opening for the CTS specimens.

density of the specimen on the fracture toughness.

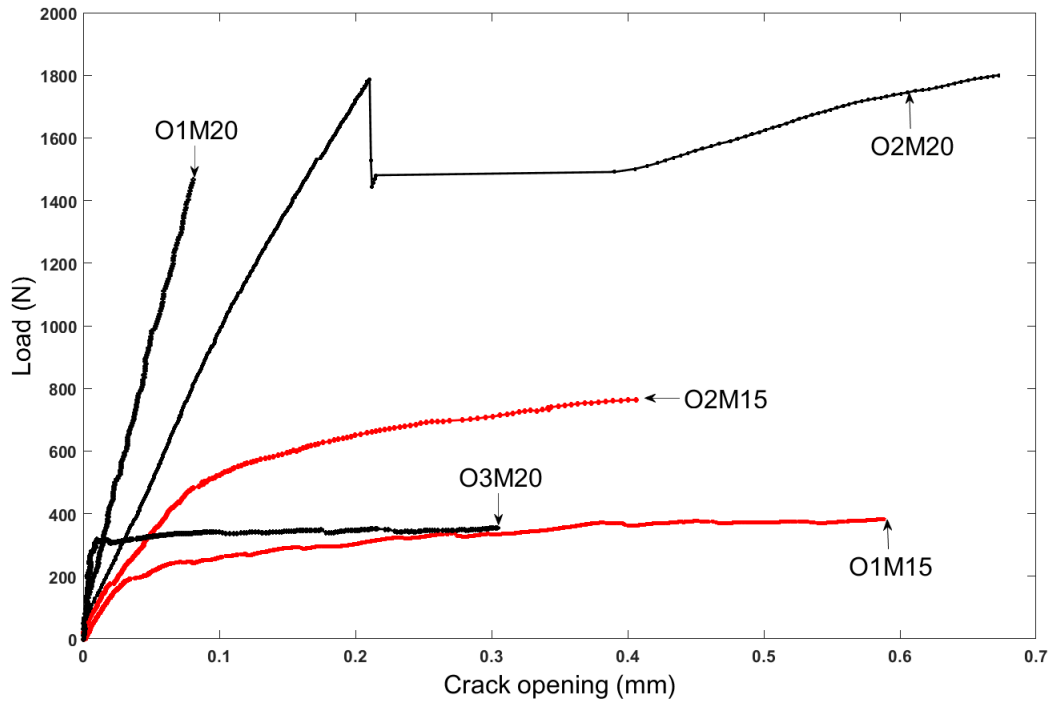


Figure 18: Load - crack opening curves for the MMCG Okume specimens and two thicknesses (15 mm and 20 mm).

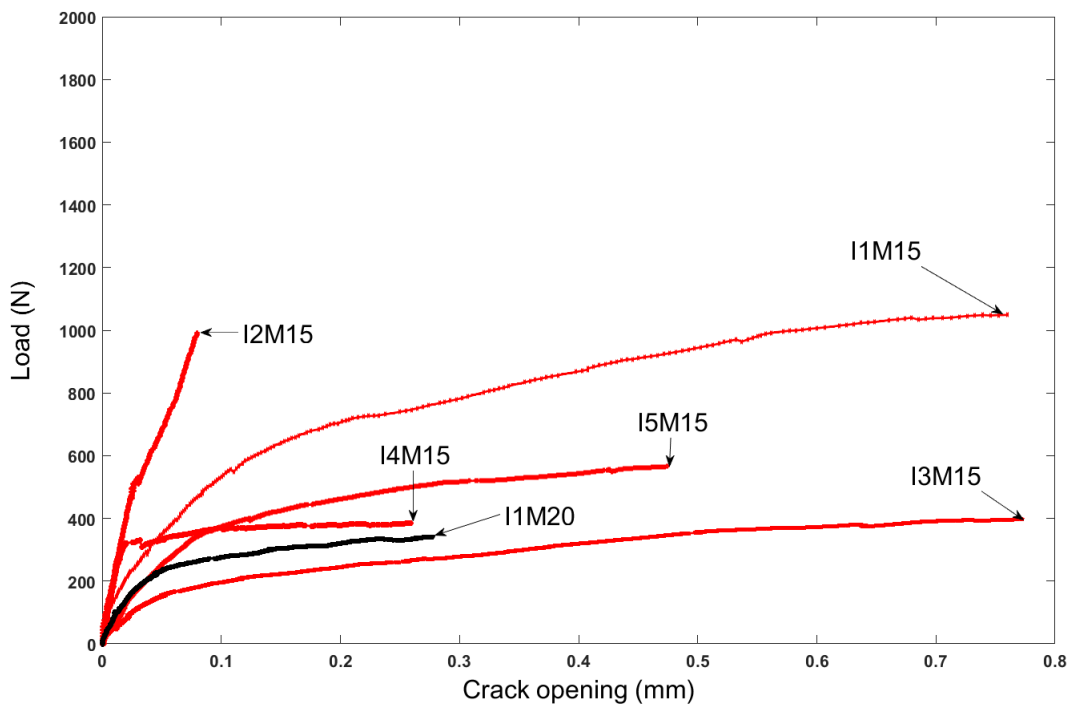


Figure 19: Load - crack opening curves for the MMCG Iroko specimens and two thicknesses (15 mm and 20 mm).

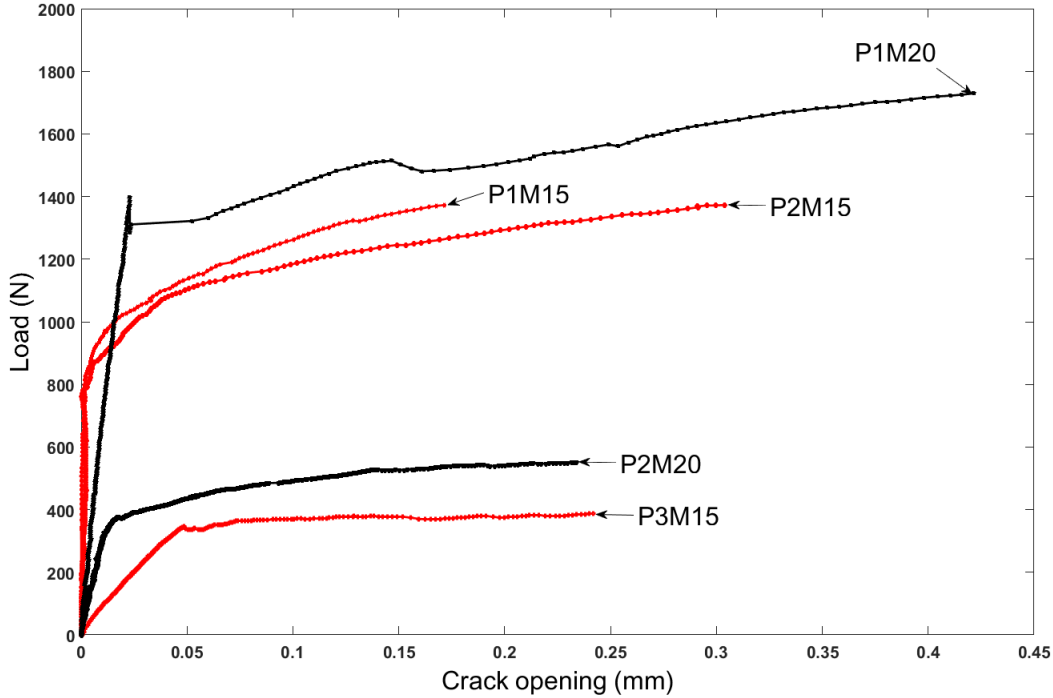


Figure 20: Load - crack opening curves for the MMCG Padouk specimens and two thicknesses (15 mm and 20 mm).

Crack length-load analysis.

For the 12.5 mm-thick specimens, a sudden failure corresponding to a sudden drop of the load is observed. Consequently, the crack length instantaneously increases by 11 mm for the Okume specimen, 16 mm for the Iroko specimen and 32 mm for the Padouk specimen. No crack propagation is observed while the loading level increases. By contrast, the crack length increases while the loading level decreases. This result is due to the bridging of the crack caused by the wood fibers, which cannot be considered for the calculation of G_c .

The crack propagation scheme is different for the 20 mm-thick CTS specimen, more particularly for the Okume and Padouk specimens. Figure 21 presents the evolution of the crack length as a function of the load for these two specimens. The crack length slightly increases up to a load value equal to 1520 N and 1950 N for the Okume and Padouk specimens, respectively. Then the crack length suddenly increases, leading to the failure of the specimen. No crack propagation is observed for the 20 mm-thick CTS concerning the Iroko specimen. The crack developed out of the grid, in the connecting zone and the holes through which the load was applied. This is certainly due to the brittleness of Iroko.

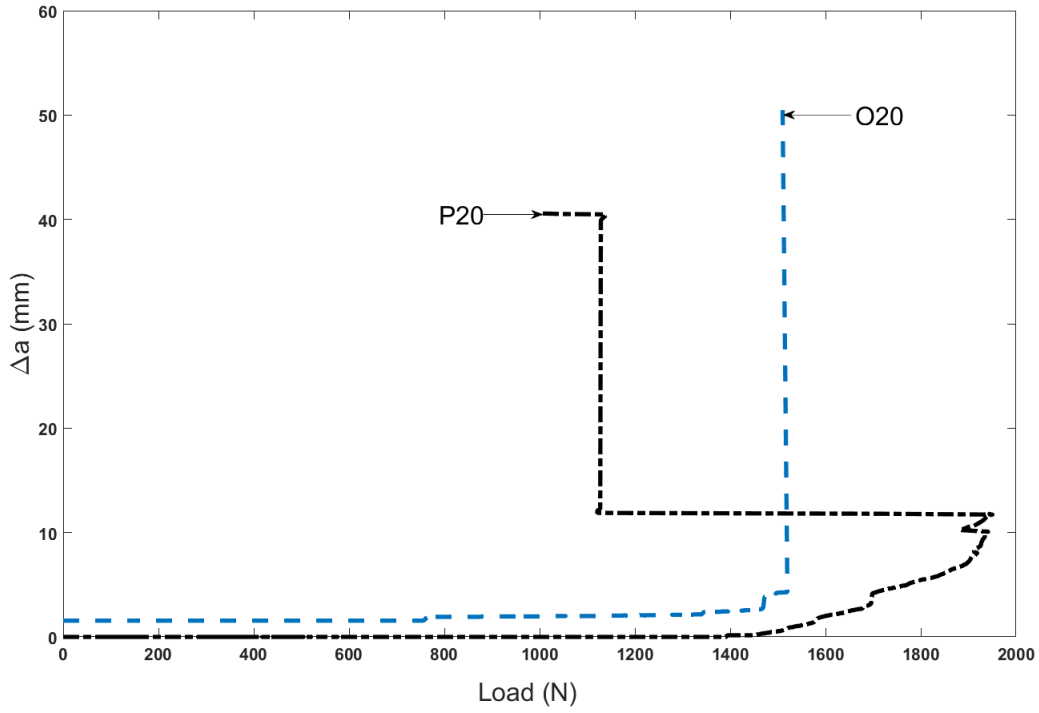


Figure 21: Example of crack length as a function of the load for two CTS specimens (Thickness 20 mm).

Figure 22 shows an example of crack length change as a function of the load for the three species. Δa is the crack length increment. The initial value of the crack length, denoted a_i is $a_i = 28 \text{ mm}$ for the CTS specimens, and $a_i = 22 \text{ mm}$ for the MMCG specimens. The total crack length is equal to $a = a_i + \Delta a$ for the MMCG specimens whatever the thickness. The crack length gradually and continuously increases contrary to what happens with the CTS specimens, for which the crack suddenly propagates up to the failure of the specimen.

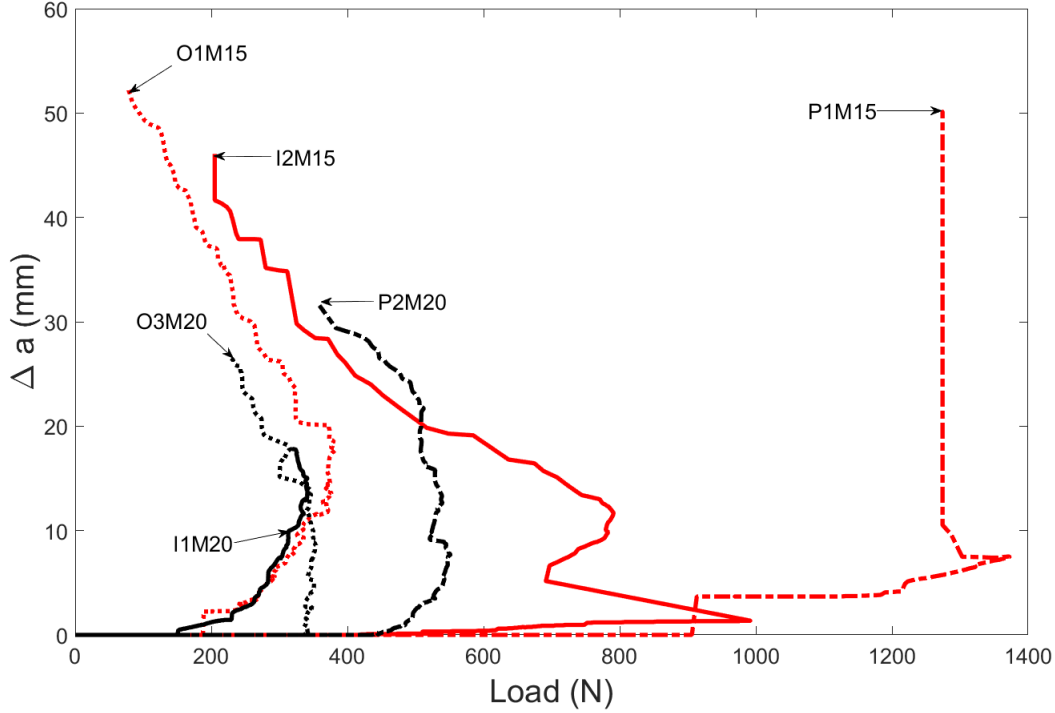


Figure 22: Example of crack length as a function of the load for three MMCG specimens (thickness: 15 mm and 20 mm).

Critical energy release rate

In this section, the value of G_c obtained with both the CTS and MMCG specimens are calculated, and the influence of the thickness of the specimens is highlighted.

Figure 23 presents G_c as a function of the crack length a calculated with the (compliance) method for the CTS specimens, for the three wood species and the two thickness values. For the 12.5 mm-thick specimens, only one value of G_c is calculated because no crack propagation was observed. The obtained values are equal to 5 J/m^2 , 10 J/m^2 and 18 J/m^2 for the Okume, Iroko and Padouk species, respectively. It is worth highlighting that G_c is directly connected to the average density given in Table 1. Indeed G_c increases proportionally to the density of the species. For the 20 mm-thick specimens presenting a crack propagation (O20 and P20 specimens), the initial critical energy release rate G_{ic} inducing the beginning of the crack propagation is equal to 3 J/m^2 for the Okume specimen and to 282 J/m^2 for the Padouk specimen. The initial energy release rate (G_{ic}) is the value obtained from the onset of crack propagation. Globally, G_c is much higher for Padouk than for Okume. It means that the amount of energy necessary to induce the

crack initiation and the crack propagation is higher for Padouk than for Okume as proven before. As for the 12.5 mm-thick specimens, this result is consistent with the density of the tropical species. Finally, the maximal critical energy release rate G_{mc} is also correlated to the crack opening obtained just before the failure of the *O20* and *P20* specimens. The maximum critical energy release rate (G_{mc}) is that obtained at the failure of the specimen. Indeed, the obtained values are equal to 4.3 mm and 12.4 mm, for the Okume and Padouk specimens, respectively (see Figure 21). To conclude with the 20 mm-thick specimens, no crack propagation is observed for the *I20* specimen. Consequently, only one value of G_c is obtained in this case. The obtained value is equal to 35 J/m².

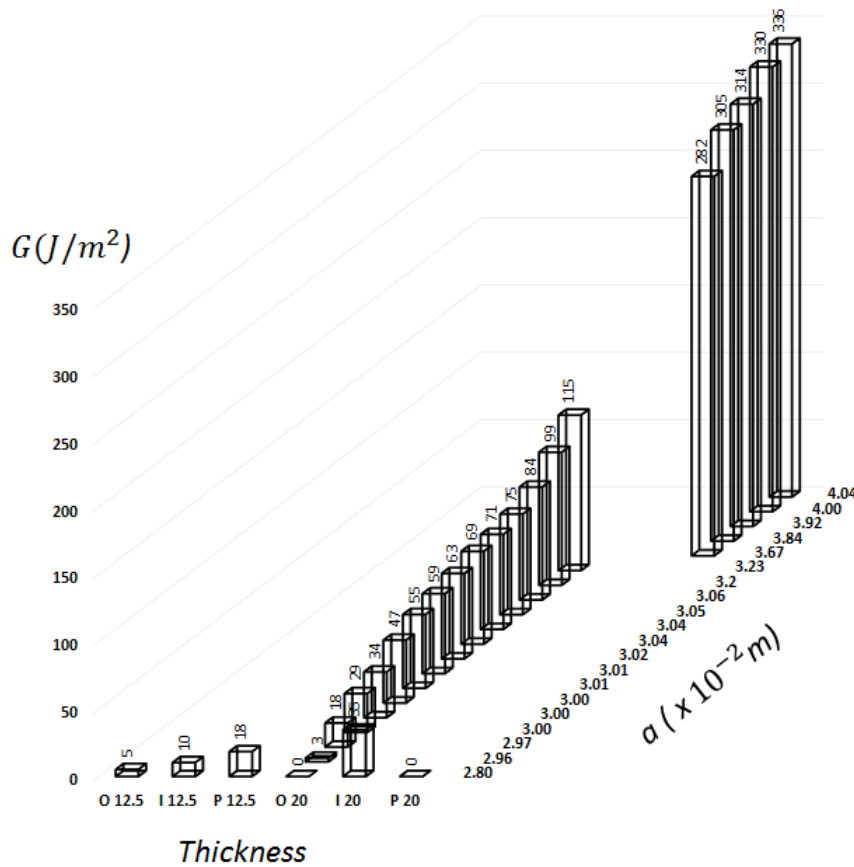


Figure 23: Critical energy release rate of Okume (O), Iroko (I) and Padouk (P) (thickness 12.5 mm and 20 mm).

The results obtained with the MMCG specimens is now presented for the three species and for the two thicknesses. Figure 24 shows the value of G as a function of the crack length for Okume. It is worth remembering that the initial crack length is equal here to 22 mm. The results for the two thicknesses are presented and analyzed. The G_{ic} and G_{mc} values of the specimens are calculated. The results are presented in Table 4.

The average value G_{ic} for the 15 mm and 20 mm-thick specimens is equal to $6.5 J/m^2$ and $46 J/m^2$, respectively. This clearly underlines the influence of the thickness on this value. The average values of G_{mc} inducing the failure of the specimens for the 15 mm and 20 mm-thick specimens are equal to $317 J/m^2$ and $248 J/m^2$, respectively. These last results are difficult to interpret because of the variability and the heterogeneity of the different specimens. On the contrary, the G_{ic} values are relatively close to each other. Consequently, the influence of the thickness of the specimens on this quantity is clearly visible. The greater the thickness, the greater the initial value for G_c .

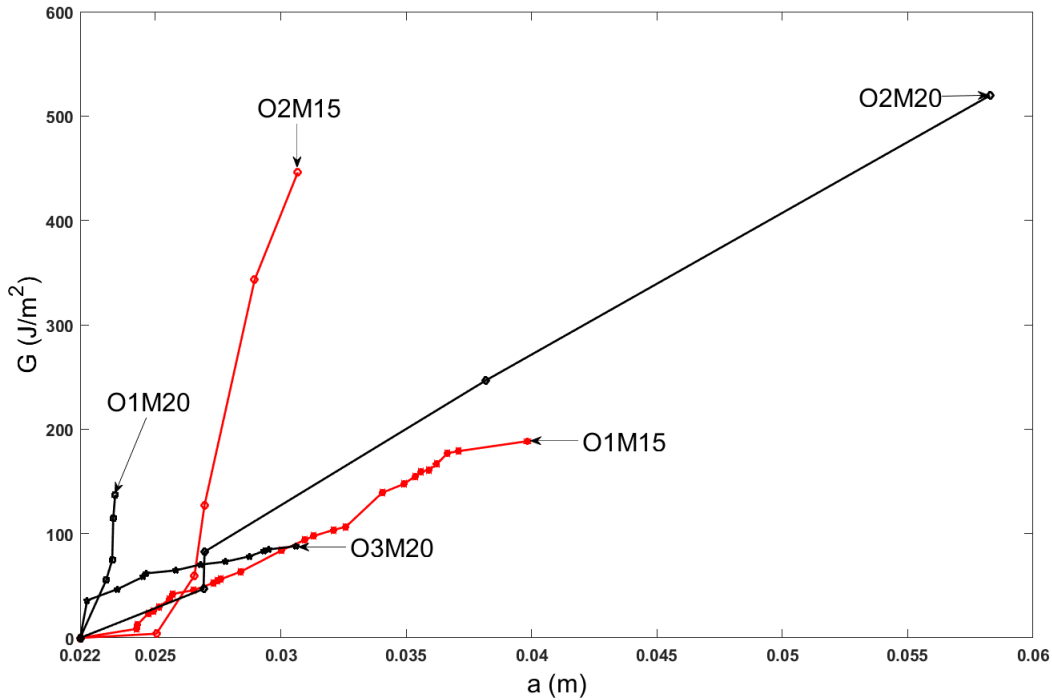


Figure 24: Critical energy release rate G_c as a function of the crack length for Okume (O).

	O1M15	O2M15	O1M20	O2M20	O3M20
G_{ic}	9	4	55	47	36
G_{mc}	188	446	137	520	88

Table 4: Individual values of Okume: G_{ic} is the initial critical energy release rate; G_{mc} is the maximum critical energy release rate.

The same analysis can be performed for both the Iroko and Padouk specimens. Figures 25 and 26 present G as a function of the crack length for the Iroko and Padouk

specimens. G_{ic} is given in Tables 5 and 6 for Iroko and Padouk, respectively. Concerning Iroko, the average values of G_{ic} for the 15 mm and 20 mm-thick specimens are equal to $19 J/m^2$ and $37 J/m^2$, respectively. This shows the influence of the thickness. The same remark as for Okume can be drawn concerning the significant fluctuations of G_{mc} for the 15 mm thick specimens.

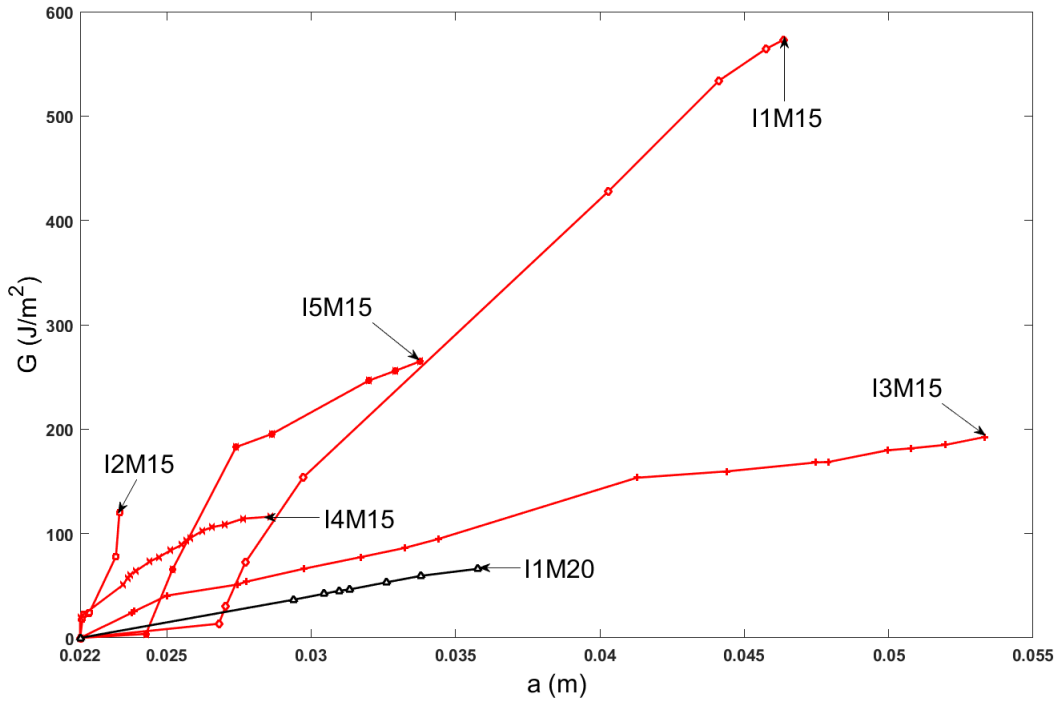


Figure 25: Critical energy release rate G_c as a function of the crack length for Iroko (I).

	I1M15	I2M15	I3M15	I4M15	I1M20
G_{ic}	14	18	24	20	37
G_{mc}	575	120	192	116	66

Table 5: Individual values of Iroko: G_{ic} is the initial critical energy release rate; G_{mc} is the maximum critical energy release rate.

Finally, the Padouk specimens are analyzed in terms of G_c values. In Table 6, the average value of G_{ic} is equal to $12 J/m^2$ and $35 J/m^2$ for the 15 mm and 20 mm thick specimens, respectively. The initial value of G_c for specimen $P2M15$ ($1 J/m^2$) may look strange. A detailed analysis of the orientation of the crack revealed an inclination of the wood rings with respect to the initial crack of about 30 degrees. The same remark as for

Okume can be drawn concerning the significant fluctuations of the maximal value of G for both the 15 mm and 20 mm thick specimens.

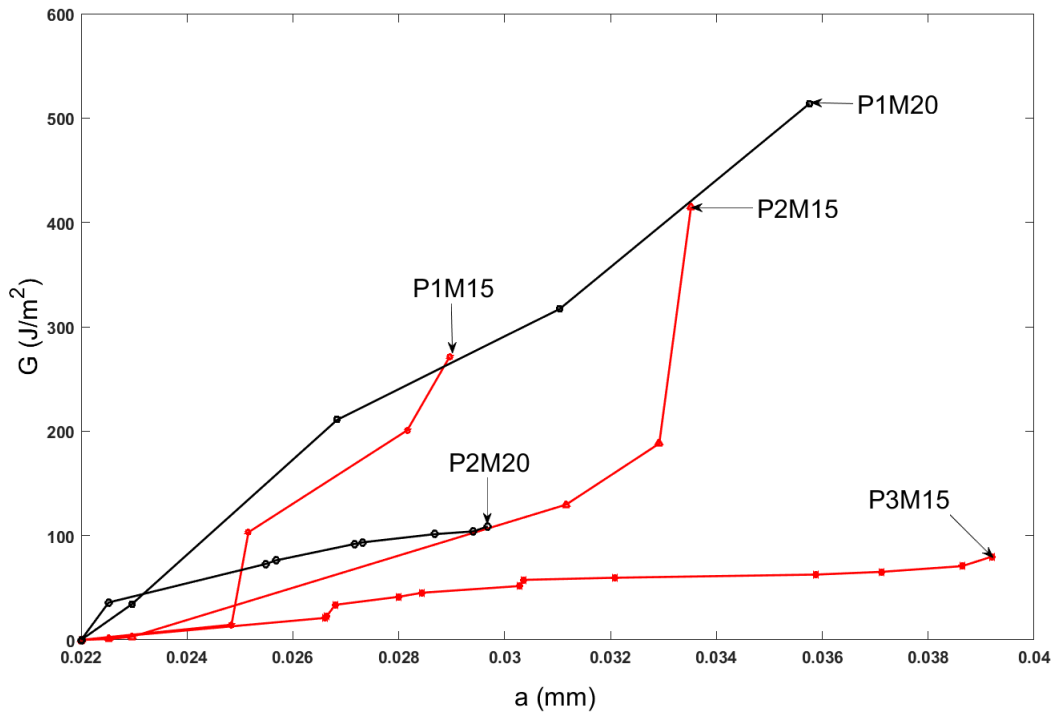


Figure 26: Critical energy release rate G_c as a function of the crack length for Padouk (P).

	P1M15	P2M15	P3M15	P1M20	P2M20
G_{ic}	15	1	21	34	36
G_{mc}	271	415	80	514	109

Table 6: Individual values of Padouk: G_{ic} is the initial critical energy release rate; G_{mc} is the maximum critical energy release rate.

Discussion

Table 7 compares the different values obtained with the values from the bibliography.

Designation	Orientation	Relative density	G_{mc} (J/m^2)	Standard deviation (SD)
Spruce [45, 46]	RL	0.40 - 0.50	159 - 345	60 / 186
Pine [46]	RL	0.40 - 0.50	346	≈ 90
Oak [46]	RL	0.70 - 0.80	234	≈ 110
Okume	RL	0.39 - 0.50	248⁽²⁾ / 317⁽¹⁾	129 / 160
Iroko	RL	0.56 - 0.70	251⁽¹⁾	200
Padouk	RL	0.70 - 0.88	255⁽¹⁾ / 312⁽²⁾	175 / 200

Table 7: Comparison of the means of G_{mc} for MMCG specimen with the literature: thickness 15 mm (1) and 20 mm (2).

The literature is silent about cracking of tropical species. However, cracking studies on temperate species are available especially in opening mode. In order to propose an objective comparison, the discussion focuses here on tempered species featuring the same density as well as a crack orientation along the RL direction [47]. Indeed, Voichita Bucur [45] studied the spruce. He tested the specimens along the RL direction. Reiter et al. [46], also cited by [45], performed tests on cubic specimens along the RL direction. According to the principle of the Wedge Splitting test (WS), these tests were carried out on Spruce, Pine, and Oak specimens. The experimental tests were carried out in the same conditions (air-conditioned room at 20°C and 65% relative humidity). The specific breaking energy or maximal critical energy release rate Gf (average values and standard deviation of six measurements for each softwood and hardwood) is considered. Hence, the mean of G_{mc} for Okume, Iroko and Padouk (given in Tables 4, 5 and 6 respectively) are reported in Table 7 in bold and compared with Spruce, Pine and Oak respectively. The comparison shows that small deviations were obtained between the Okume and Spruce values for the two thicknesses considered here. For the 15 mm-thick Okume specimens, a 8% difference with the values obtained with Spruce is observed. A 8% difference is observed between 15 mm-thick Padouk specimens and the Oak specimens. Only the standard deviation in terms of G_c values at minimum and maximum failure is observed. We have approximately the same conclusion for the Iroko specie. The scatter of the results is

certainly caused by the very nature of the material. Indeed the crack path is more regular with tempered species than with tropical species because of the annual rings, which exist in tempered species. Annual rings behave as channels for crack propagation and thus make crack paths more regular and predictable. The measurement technique used here (the grid method) does not feature a higher measurement error than similar techniques used to measure displacement and strain fields on wood specimens, such as DIC [28, 31].

In numerous studies dealing with fracture mechanics of tempered wood species, the G_c value increases with crack extension up to a plateau value (see [48, 49]). Then, a stability range is observed before a sudden increase and the final collapse of specimen. This observation depends on the shape of the specimen, the length of the stability range, the orientation of the annual rings and the microstructure of the specie. For the MMCG specimens made of the tropical specie studied in this work, the stability range is narrow compared to what is observed with the tempered species investigated in [20, 21, 23, 48, 49] and [50]. Consequently, the collapse occurs suddenly before reaching the plateau value. In addition, the phenomenon of fiber bridging in this type of materials is more pronounced because of the fact that annual growth rings do not exist. This can lead to the increase of the observed R-curves.

4. Conclusion

In this study, fracture tests were performed on three tropical species: Iroko (*Milicia Excelsa*), Okume (*Aucoumea klaineana Pierre*) and Padouk (*Pterocarpus soyauxii*). A grid was transferred on each specimen to follow the crack tip. A new Arcan system was designed to test both the CTS and modified MMCG specimens. The opening and the crack tip location were detected from the displacement maps obtained by the grid technique. The obtained values made it possible to use the empirical compliance method in order to calculate the critical energy release rate of each wood specie for different thicknesses. For both the CTS and MMCG specimens, it is clear that the thickness, and the density have an influence on the toughness. Indeed it is shown that the critical energy release rate increases when the density increases in both the stationary and the crack growth processes. The crack length increment could not be measured for Iroko because of the quasi-brittle behavior of this specie compared to Okume and Padouk. The mean value G_{mc} for the three tested species were compared with those of various tempered species

featuring the same density.

In future studies, it would be necessary to investigate the thickness value of the CTS specimen necessary to observe the crack growth process. Further tests should also be performed in the other preferential directions of the wood for both the CTS and MMCG specimens. At the end, the mixed mode configuration should be applied at room temperature and for different moisture contents in order to know the real fracture toughness of tropical wood under indoor and outdoor conditions of tropical environments.

Acknowledgements

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