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Ioannis Tanis, Konstantinos Karatasos, Thomas Salez. Molecular dynamics simulation of the capillary leveling of a glass-forming liquid. 2019. hal-01909064v3

## HAL Id: hal-01909064 https://hal.science/hal-01909064v3

Preprint submitted on 28 Aug 2019 (v3), last revised 16 Sep 2019 (v4)

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1	Molecular Dynamics Simulation of the Capillary Leveling of
2	a Glass-Forming Liquid
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Abstract. Motivated by recent experimental studies probing i) the existence of a mobile layer at the free surface of glasses, and ii) the capillary leveling of polymer nanofilms, we study the evolution of square-wave patterns at the free surface of a generic glass-forming binary Lennard-Jones mixture over a wide temperature range, by means of molecular dynamics simulations. The pattern's amplitude is monitored and the associated decay rate is extracted. The evolution of the latter as a function of temperature exhibits a crossover between two distinct behaviours, over a temperature range typically bounded by the glass-transition temperature and the mode-coupling critical temperature. Layer-resolved analysis of the film particles' mean-squared displacements further shows that diffusion at the surface is considerably faster than in the bulk, below the glass-transition temperature. The diffusion coefficient of the surface particles is larger than its bulk counterpart by a factor that reaches  $10^5$  at the lowest temperature studied. This factor decreases upon heating, in agreement with recent experimental studies. 

#### 67 **I. Introduction**

Thin films and their free interfaces are used in a variety of applications such as 68 catalysis<sup>1</sup>, fast crystal growth<sup>2, 3</sup> and the formation of low-energy glasses<sup>4, 5</sup>. Apart 69 from their applications in industry and technology, molecular mobility and relaxation 70 71 at surfaces and interfaces have been recently a subject of growing interest for 72 fundamental research. To this end, several experimental approaches have been used to probe the surface evolution and mobility of thin films<sup>6-10</sup>. More specifically, an 73 74 efficient way to gain insight into the surface mass transport and the associated dynamics, is to deposit nanoparticles on the film surface and subsequently to monitor 75 the host material's response<sup>9,11</sup>. Another powerful and versatile technique widely 76 utilized for the determination of the surface-diffusion coefficient  $D_{s}$ , characterizing 77 the in-plane translation of molecules at the film surface, is the capillary-driven 78 leveling of surface-gratings<sup>6, 9, 12-14</sup>. Several studies suggest that the mechanism 79 governing the relaxation of these gratings is temperature and material dependent<sup>12, 15.</sup> 80 81 More specifically, recent works on glass-forming molecular liquids reported a transition from bulk viscous flow at temperatures higher than the glass-transition 82 temperature  $T_{\rm g}$ , to surface diffusion below  $T_{\rm g}^{-13, 16}$ . Analogous studies in polymeric 83 liquids revealed that bulk viscous flow was the only mechanism governing the surface 84 decay, even at the highest viscosities studied <sup>14, 17, 18</sup>. According to Mullin's pioneering 85 work<sup>19</sup>, the different mechanisms that could flatten the surface pattern (surface and 86 bulk diffusions, evaporation-condensation, bulk viscous flow) can be distinguished by 87 determining the decay rate dependence on spatial frequency. This method has been 88 applied in crystalline metals<sup>20</sup>, amorphous silica<sup>21</sup> and molecular glasses<sup>22</sup>. 89

Measurements of diffusion coefficients at the surface report values considerably
higher than the respective bulk coefficients at the glass-transition temperature<sup>12,13</sup>.
Furthermore, large variations in surface diffusion coefficients among different
molecular glass formers bearing a similar bulk mobility were linked to the strength of
the intermolecular forces<sup>23</sup>.

95 Further insight into glass-forming systems has been provided by numerical 96 simulations. Several studies have addressed the factors that govern dynamical 97 heterogeneity and spatial correlations in the bulk<sup>24-30</sup>. Furthermore, other works 98 addressing systems under confinement have managed to elucidate the effects of 99 confinement by rough or smooth walls on the liquid dynamics and to extract 100 associated length-scales<sup>31-35</sup>. Extensive simulation studies have also been conducted

101 on ultrastable vapor-deposited glasses <sup>4, 36, 37</sup>. However, to our knowledge, a small
102 number of simulation studies probing the surface mobility in glass formers have been
103 reported so far.

Surface-diffusion-mediated decay of two-dimensional nanostructures has been 104 recently studied by a combined analytical and kinetic Monte-Carlo approach<sup>38</sup>, 105 whereas Kayhani et al. performed molecular dynamics (MD) simulations to examine 106 the coalescence of platinum nanoclusters<sup>39</sup>. Concerning simulation work on the 107 surface mobility of molecular glass formers, Hoang et al. performed MD studies on 108 freestanding monatomic glass-forming liquids<sup>40</sup>. The study of Akbari *et al.* addressed 109 the effects of the substrate in kinetic and thermodynamic properties of a binary 110 Lennard-Jones (LJ) liquid<sup>41</sup>, whereas Malshe and co-workers extracted surface-111 diffusion coefficients by the aid of the grating-decay approach<sup>42</sup> in free standing films 112 of the aforementioned liquid type. Results were consistent with data obtained from the 113 114 mean-squared displacements of the liquid particles. In a very recent study, Kuan and 115 co-workers examined single-particle dynamics in the surface and in the bulk of supported films prepared by vapour deposition. Both bulk and surface particle 116 displacements showed evidence of heterogeneous dynamics<sup>43</sup>. 117

The aim of the present work is to provide additional insight into the surface mobility 118 119 of a glass-forming liquid by means of molecular dynamics simulations. Similarly to a 120 recent work where we probed the viscoelastic behaviour of nonentangled polymer films above the glass-transition temperature, through the capillary leveling of a 121 square-wave surface pattern<sup>44</sup>, we examine here the evolution of a square-wave 122 surface pattern atop a generic binary LJ mixture supported by an attractive substrate. 123 124 This new study is carried out over a wide temperature range, sampling both the glassy 125 and liquid states of the film. The associated decay rates are extracted whereas surface 126 and bulk mobilities are examined. Further insight into the surface and bulk mobilities 127 is gained by examining the self part of the van Hove function, as well as via the layer-128 resolved analysis of the liquid particles' mean-squared displacements.

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#### 130 II. Computational Details

131 We examine a binary mixture of 80% A and 20% B particles that interact via a LJ 132 potential  $V_{\alpha\beta} = 4\epsilon_{\alpha\beta} \left[ \left( \sigma_{\alpha\beta}/r \right)^{12} - \left( \sigma_{\alpha\beta}/r \right)^6 \right], (\alpha, \beta \in \{A, B\})$ . The Van der Waals 133 parameters were chosen as  $\epsilon_{AA} = 1.0, \sigma_{AA} = 1.0, \epsilon_{AB} = 1.5, \sigma_{AB} = 0.8, \epsilon_{BB} =$ 

0.5,  $\sigma_{BB} = 0.88$ . The potential was truncated at a cut-off radius  $r_c = 2.5\sigma_{AB}$ . The 134 numbers of particles of type A and B are 2938 and 734, respectively. The binary 135 mixture interacting with this parameter set corresponds to the Kob-Andersen liquid 136 model which is not prone to crystallization or to phase separation; it is extensively 137 utilized in studies of glass-forming liquids<sup>45, 46</sup>. The liquid film is supported by a 138 strongly attractive substrate whose atoms (henceforth designated by the type S) are 139 located on the sites of an hexagonal lattice and are kept fixed to their lattice positions. 140 The substrate particles' radius is  $\sigma_s = 2.41$  and they attract A and B atoms with the 141 following energy magnitudes<sup>47</sup>:  $\epsilon_{AS} = 4.425$  and  $\epsilon_{BS} = 3.129$ . The length of the 142 cubic box is  $16.56\sigma_{AA}$  in the lateral directions x and y, and  $441.17\sigma_{AA}$  in the z 143 144 dimension. The value of the latter is chosen large enough to avoid interaction of the particles with periodic images of the substrate, and ensure a system pressure p = 0. All 145 quantities are reported in LJ units, *i.e.* length is measured in units of  $\sigma_{AA}$ , energy in 146 units of  $\epsilon_{AA}$ , time in units of  $\tau = (m\sigma_{AA}^2/(48\epsilon_{AA}))^{1/2}$  and temperature in units of 147  $\epsilon_{AA}/k_B$  where  $k_B$  stands for the Boltzmann constant. For the case of argon, these units 148 correspond to a length of 3.4 Å, an energy of  $120Kk_B$  and a time of  $3 \cdot 10^{-13}$  s. All 149 150 simulations are performed in the canonical (NVT) ensemble using the DL\_POLY code<sup>48</sup>. Temperature is maintained constant through the use of the Nosé-Hoover 151 152 thermostat. Simulations are conducted at the temperature range T = 0.20-0.525, and 153 the length of each run is  $3 \cdot 10^5$ .

The initial configuration of the glassy film was obtained by the aid of the Aten program<sup>49</sup>. To create the 3-dimensional pattern at the free surface of the film, a flat film was initially equilibrated in the canonical ensemble at a temperature of T = 0.3. Afterwards, particles were removed from both edges of the free surface in order to obtain the 3D pattern, henceforth designated as the 'top layer' (see Fig.1). The lateral dimensions of the latter were  $L_x = L_y = 4.41$ , whereas its thickness and initial height (counted from the substrate) were respectively d = 4.36 and  $h_0 = 15.67$ .

To examine the behaviour in the bulk, a configuration comprising 5076 particles was constructed at an elevated temperature, T = 0.80, and at a density of  $\rho = 1.2$ . After removing close contacts, the system was cooled to T = 0.30 by conducting runs in the isothermal-isobaric ensemble (*NPT*) at pressure p = 0. The temperature step between the isothermal runs ranged from dT = 0.1 for the highest temperatures to dT = 0.025and dT = 0.0125 at temperatures around the bulk glass-transition temperature  $T_g$ . The

duration of each isothermal run ranged from  $1.6 \cdot 10^4$  (at T > 0.5) to  $3 \cdot 10^5$  (at  $T \le 0.5$ ). 167 Defining the cooling rate as the difference between the starting temperature and the 168 final temperature divided by the time of the quench, the cooling rate was  $0.75 \cdot 10^{-7}$ . 169 This amounts to half the cooling rate used in the original model of Kob and Andersen 170 and, although it remains quite fast, it is slower than the fastest cooling rate in 171 experiments<sup>45</sup>. The glass-transition temperature of the binary mixture was determined 172 by extrapolating and intersecting the affine dependencies of the low- and high-173 temperature specific-volume-vs-temperature curves. This yielded a value of  $T_g$  = 174 0.392 which is below the reported mode-coupling critical temperature for this system, 175  $T_{\rm c} \approx 0.435^{50}$ . 176

Figure 1 displays the initial configuration of the samples, as well as snapshots from a run at T = 0.3 at times t = 20000 and 233333. All snapshots were generated by the aid of the VMD software<sup>51</sup>. The particles that evaporated at elevated temperatures were disregarded from post-analysis.





Figure 1: Top: Initial configuration of the sample bearing a total number of 3672 particles. Periodic boundary conditions are applied in all directions.  $L_x$  stands for the *x*-dimension of the simulation box and  $h_0$  is the maximum vertical height (colour code : blue = top layer, yellow = bottom layer, purple = substrate). Middle: Snapshot of the film at t = 20000, where  $h_{av}$  is the average height value. Bottom: Snapshot of the film at t = 233333;  $h_{bv}$  the average height of the fully leveled film.

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#### 189 III. Results

To investigate the mobility of the liquid's molecules, we examine the self-part of thevan Hove space-time correlation function defined as :

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$$G_{s}(x,t) = \frac{1}{N} \sum_{i=1}^{N} \left\langle \delta \left( x + x_{i}(0) - x_{i}(t) \right) \right\rangle, \tag{1}$$

with  $x_i$  representing the position of particle *i* along any of the *x*, *y* and *z* directions, *N* 193 194 being the number of particles that constitute the top layer,  $\langle ... \rangle$  being the ensemble 195 average over realizations and time origins and  $\delta$  is the Dirac's distribution. In order to 196 account for the natural anisotropy of the system induced by the interfaces, the van Hove function was evaluated in each direction separately. In Fig.2, the x dependencies 197 198 of  $4\pi x^2 G_s(x,t)$  for the top layer particles and two times t, are displayed. A 199 practically indistinguishable behaviour (not shown for clarity reasons) was observed 200 in the y direction, as well. Also shown in the figure, are the corresponding curves for the bulk sample. The van Hove functions were evaluated at the temperatures T = 0.30201 202 and T = 0.35, which lie below the bulk  $T_g$  as well as at a temperature T = 0.375 near 203 the bulk  $T_{\rm g}$ .



Figure 2: Self part of the van Hove function (eq.1) for the top layer particles, as a function of the molecular displacement in the *x* direction, evaluated at a) T = 0.30, b) T = 0.35 and c) T = 0.375. The different line colours correspond to different times and the references for a bulk sample are provided for comparison.

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A visual inspection of Fig.2 reveals that the top layer particles are significantly more 209 210 mobile than those corresponding to the bulk. Focusing on the top left panel, we 211 observe that in the bulk, and at low temperature, the distribution shows a vanishing probability for x-displacement larger than the near-neighbour distance ( $x \sim 1$ ). As 212 213 expected for a glassy behaviour, this implies that the particles have not managed to escape from the cages in which they were trapped initially. In contrast, the 214 distribution for the top layer particles exhibits non-negligible values up to  $x \sim 4$ , thus 215 216 providing evidence for an enhanced mobility at the free interface of the film. As 217 expected, the difference between surface and bulk mobilities grows with time. Bulk mobility remains practically unchanged at the timescales examined, since the system
at the temperatures shown in Fig.2 resides below the estimated glass-transition
temperature. Focusing on the top layer particles' distribution at early times, one can
discern, apart from the peak at

- 222  $x \sim 0.1$ , the existence of a "shoulder" at distance  $x \sim 1$ . The distribution at later times 223 further confirms the existence of two different populations, as reflected in the peaks at 224  $x \sim 0.2$  and at  $x \sim 1.1$ . The appearance of these two peaks reflects a clear distinction in mobility for the surface and internal particles belonging to the top-layer and lies in 225 accordance with the findings of Malshe et al.<sup>42</sup>. On the other hand, the distribution 226 also shows that the peak belonging to the more mobile particles gains significantly in 227 228 intensity as time lapses. This is consistent with the fact that an increasing fraction of 229 the top-layer particles gets closer to the free surface with time (as demonstrated by the 230 snapshots in Fig.1, blue particles).
- 231 The previous two-peak fine-structure separation of relaxation processes is no longer 232 detected at late times for T > 0.30, thus indicating a more homogenous mobility at 233 higher temperature. Nevertheless, the "shoulder" observed in panels b and c at  $x \sim 1$  at 234 early times, is maintained and gains significantly in intensity at higher temperatures. 235 Assuming that the mechanism of diffusion does not change appreciably at the sub- $T_{\rm g}$  temperatures examined, it is reasonable to surmise that this behavior arises from 236 237 the same origin as in the lowest temperature case, *i.e.* the increase with time of the 238 number of top-layer particles gaining access to the free surface. In sharp contrast, 239 there is no sign of enhanced mobility in the bulk samples as temperature rises. Only at 240 T = 0.375, one can discern a marginal increase in the mobility of the bulk particles at 241 long times, as reflected by the tail of the van Hove distribution. Since the bimodal 242 distribution at low temperatures which is indicative for the dynamic heterogeneity in 243 the motion of the top layer particles, is no longer detected at elevated temperatures, it 244 may be considered as a signature for the transition for these particles to the glassy 245 state.

To examine the global consequences of the enhanced surface mobility on the film leveling, we have monitored the average height  $h_{av}(t)$  of the top layer particles. The initial value of  $h_{av}$  (counted from the substrate) was  $h_{av0} = 13.5$ . An example of the time evolution of the rescaled amplitude,  $\frac{h_{av}(t)-h_{|v|}}{h_{av0}-h_{|v|}}$ , for a temperature T = 0.45, is displayed in Fig.3a, where  $h_{|v|} = 11.31$  is the average height of the top layer particles 251 after the film leveling. It should be noted here that  $h_{|v|}$  is smaller than the value 252 predicted from the volume conservation. This is due to the fact that, in this work, it is 253 the average height of the square pattern that is monitored rather than its maximum 254 height. On these grounds,  $h_{|v|}$  does not correspond the value of  $h_{av}(t)$  at infinite time 255 and, consequently, it is not an equilibrium value. We stress that the total number of evaporated particles did not exceed 0.35% of the total number of particles constituting 256 257 the film, for all simulated systems. As stated earlier, the evaporated particles were 258 excluded from all analysis calculations. As it can be inferred from Fig.3a, the 259 temporal decay is exponential. Figure 3b displays the associated decay constant as a 260 function of temperature. We note that the minimum temperature at which full leveling 261 of the square pattern was observed within the total simulation time, was T = 0.30.



Figure 3: a) Time evolution of the rescaled pattern amplitude at T = 0.45. The red line is an affine fit. b) Decay constant *K* extracted from the affine fits as a function of temperature. Error bars in *K* are on the order of  $10^{-6}$ .

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Examining Fig.3b, it appears that in between  $T_g = 0.392$  and  $T_c = 0.435$ , a crossover 266 267 takes place. At temperatures above  $T_c$ , a weak slope characteristic of a liquid-like behaviour is observed, while below  $T_{\rm g}$  a stronger dependence corresponding to a 268 269 glassy-like behaviour is noticed. This observation is consistent with the fact that the onset of supercooling effects is generally observed near T<sub>c</sub>. Interestingly, recent 270 experimental studies report different rates for the decay of patterned surfaces in 271 supported films above and below the glass-transition temperature<sup>6, 9, 11, 13, 23</sup>. The 272 flattening of profile patterns at the free surface of films below  $T_{g}$  has been ascribed to 273 surface diffusion as suggested by Mullin's theory<sup>19</sup>. It must be noted that, since the 274 mobile layer can still be considered at equilibrium within a certain temperature range 275

below  $T_{\rm g}$ , and thus the Stokes-Einstein relation is valid there, one can also describe 276 the surface mobility as a surface flow which leads to an identical partial differential 277 equation for the profile's evolution<sup>9</sup>. Surface diffusion levels a sinusoidal surface 278 pattern at a decay rate proportional to  $q^4$ , where q is the angular-wavenumber. Other 279 280 mechanisms, such as bulk viscous flow and evaporation-condensation exhibit weaker q dependences (except for the limiting lubrication case<sup>9</sup>, that accidently shows the 281 same  $q^4$  dependence for a bulk viscous flow above  $T_g$ ). We have not investigated the 282 283 angular- wavenumber dependence of the decay rate here but, instead, we have carried out a layer-resolved analysis of the particles' z-dependent mean-squared 284 285 displacements (MSDs) as defined by:

$$\Delta r^{2}(z,t) = \left\langle \frac{1}{n_{t}} \sum_{i} |r_{i}(t) - r_{i}(0)|^{2} \prod_{t'=0}^{t} \delta[z - z_{i}(t')] \right\rangle,$$
(2)

where  $r_i(t)$  is the position of particle *i* at time *t* and  $\langle ... \rangle$  is an ensemble average. This definition takes into account only the  $n_t$  particles which are at all times t' < t within the slab centred at *z* and bearing a width of  $\Delta z = 1.5$ . The results for the runs carried out at T = 0.35 are presented in Fig.4. For comparison purposes, the results for runs carried out above  $T_g$ , at T = 0.46, are also shown. We note here that the simulation runs at T = 0.46 were significantly shorter than the runs below  $T_g$  due to the evaporation of the surface particles.



Figure 4: Layer-resolved mean-squared displacements (see eq.2) as a function of time, for various distances z from the substrate as indicated, and at temperatures a) T = 0.35and b) T = 0.46. Also shown in orange, is the scaling law  $\Delta r^2 \sim t$ .

Focusing on the left panel of Fig.4, it appears that, at T = 0.35, the MSD of the particles located in the outermost film layer near the film surface is about 5 times larger than the one for the particles in the second outermost film layer. There is no

sign of major propagation of the enhanced surface mobility into the bulk. This observation corroborates a scenario in which the relaxation of the square pattern is governed by surface diffusion below the glass transition. A similar behaviour was observed at all sampled temperatures below  $T_g$ . Furthermore, a visual inspection of the MSDs of the innermost particles (black lines in Fig.4), demonstrates enhanced dynamics near the solid substrate at short times. This behaviour lies in accordance with simulation studies of polymers near solid interfaces<sup>52,53,54</sup>.

- 307 Finally, the diffusion coefficients  $D_s$  of the top layer particles were extracted from the
- 308 MSD curves at different temperatures, and compared with the corresponding bulk 309 values,  $D_b$  in Fig.5.



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Figure 5: Diffusion coefficients of the top layer  $(D_s)$  and bulk  $(D_b)$  particles versus inverse temperature. The latter is scaled by the bulk  $T_g$ . The solid line is an affine fit in log-linear representation.

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As can be discerned, the diffusion coefficient of the top layer particles seems to exhibit an Arrhenius-type temperature dependence, which is reminiscent of previous observations for oligomer glasses<sup>6, 9</sup>. Moreover, diffusion at the surface is faster than in the bulk by a factor that ranges from  $10^2$  to  $10^5$  at the lowest temperature studied. This ratio drastically rises with cooling as it has been observed in both experimental and theoretical studies<sup>6, 9, 13, 42</sup>.

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#### 322 IV. Conclusion

323 Molecular dynamics simulations have been conducted in order to examine the decay 324 process of a periodic square-wave pattern at the free surface of a binary Lennard-325 Jones film. Contrary to previous simulation studies of the capillary leveling of thin 326 films, the evolution of the height was examined over a wide temperature range 327 sampling both the liquid and glassy states of the film. Different mechanisms appeared 328 to control the pattern leveling in those two states. By the aid of layer-resolved analysis 329 of the particles' mean-squared displacements, we showed that diffusion is much more 330 efficient in the layer close to the free surface than elsewhere in the bulk. Specifically, at the lowest temperature studied, the diffusion coefficient of the surface particles is 331 found to be  $10^5$  times larger than the bulk counterpart and this difference decreases 332 upon heating. 333

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#### 335 Acknowledgements

The authors gratefully acknowledge financial support from ANR WAFPI and ANR FSCF, as well as the Global Station for Soft Matter, a project of Global Institution for Collaborative Research and Education at Hokkaido University. Hendrik Meyer is kindly thanked for providing the layer-resolved analysis code. The authors also thank Anthony Maggs, Elie Raphaël, Kari Dalnoki-Veress, James Forrest, Joshua McGraw, Oliver Bäumchen and Jörg Baschnagel for stimulating discussions. K.K. would like to thank FO.R.TH.-IESL for the warm hospitality during his stay there.

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