

# Influence of $\pi$ -conjugated cations and halogen substitution on the optoelectronic and excitonic properties of layered hybrid perovskites

Joshua Leveillee, Claudine Katan, Liujiang Zhou, Aditya D Mohite, Jacky Even, Sergei Tretiak, André Schleife, Amanda J Neukirch

# ▶ To cite this version:

Joshua Leveillee, Claudine Katan, Liujiang Zhou, Aditya D Mohite, Jacky Even, et al.. Influence of  $\pi$ -conjugated cations and halogen substitution on the optoelectronic and excitonic properties of layered hybrid perovskites. Physical Review Materials, 2018, 2 (10), pp.105406. 10.1103/PhysRevMaterials.2.105406. hal-01908196

HAL Id: hal-01908196

https://hal.science/hal-01908196

Submitted on 23 Nov 2018

**HAL** is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

# Influence of $\pi$ -conjugated cations and halogen substitution on the optoelectronic and excitonic properties of layered hybrid perovskites

Joshua Leveillee, 1,2,\* Claudine Katan, Liujiang Zhou, Aditya Mohite, 4 Jacky Even,<sup>5</sup> Sergei Tretiak,<sup>2</sup> André Schleife,<sup>1,6,7</sup> and Amanda J. Neukirch<sup>2,†</sup>

<sup>1</sup>Department of Materials Science and Engineering, University of Illinois at Urbana-Champaign, Urbana, IL 61801, USA <sup>2</sup>Los Alamos National Laboratory, Los Alamos, NM 87545, USA <sup>3</sup>Univ Rennes, ENSCR, INSA Rennes, CNRS, ISCR - UMR 6226, F-35000 Rennes, France <sup>4</sup>Department of Chemical and Bimolecular Engineering, Rice University, Houston, TX 77006, USA <sup>5</sup>Univ Rennes, INSA Rennes, CNRS, Institut FOTON - UMR 6082, F-35000 Rennes, France <sup>6</sup>Frederick Seitz Materials Research Laboratory, University of Illinois at Urbana-Champaign, Urbana, IL 61801, USA  $^{7}$ National Center for Supercomputing Applications, University of Illinois at Urbana-Champaign, Urbana, IL 61801, USA (Dated: November 8, 2018)

Low-cost chemical engineering of two-dimensional layered hybrid halide perovskite structures allows for the design of hybrid semiconductor quantum wells with tailored room temperature excitonic optical absorption, emission, and charge carriers transport properties. Here density functional theory and the Bethe-Salpeter equation are used to predict the electronic structure and optical response of layered perovskites with two representative single-ring conjugated organic spacers, ammonium-propyl-imidazole (API) and 2-phenethylammonium (PEA). The inorganic perovskite quantum well properties are further tuned by analyzing the effect of halogen (X=I, Br, Cl) substitution. We found that visible light absorption occurs primarily within the perovskite layer and that UV light absorption induces partial electron-hole separation between layers. In addition, a strong exciton binding energy and influence on absorption spectrum is found by solving the Bethe-Salpeter equation. Our results suggest that further engineering is necessary beyond the single-ring limit, by introducing more conjugated rings and/or heavier nuclei into the organic spacer. This is a promising future direction to achieve photo-induced charge separation and more generally hybrid heterostructures with attractive optoelectronic properties.

## I. INTRODUCTION

2

11

12

13

Three-dimensional (3D) hybrid organic-inorganic perovskites (HOPs) have rapidly emerged as some of the most promising thin-film photovoltaic materials. 1-3 Their allure comes from a combination of high photo-conversion efficiency (PCE), low device processing cost due to lowtemperature solution processing, and composition from earthabundant and readily available materials. In particular, hybrid lead-halide perovskite (e.g. methylammonium lead iodide, MAPbI<sub>3</sub>, and formamidinium lead iodine, FAPbI<sub>3</sub>) solar cells have undergone a PCE increase from 3.5 % to over 20 % in about 5 years. 4-6 These devices have currently exceeded the certified record efficiency of multicrystalline Si cells.<sup>7</sup> Beyond photovoltaic applications, HOPs show potential in many other fields including hydrogen generation, 8 X-ray and Gamma-ray detection, 9–12 light emitting diodes (LEDs), 13 spintronics, <sup>14,15</sup> and sensors. <sup>16</sup> Setting aside the issue of lead toxicity, <sup>17–22</sup> the main impediment to industry deployment of perovskite devices is their instability to air, moisture, <sup>23</sup> and light exposure.<sup>24,25</sup>

Recently, layered HOPs (LHOPs) have re-emerged as promising alternatives to their 3D counterparts. They LEDs<sup>26</sup> and tunable optical detectors.<sup>27</sup> In these, quantum 41 decent photo-conversion performance: Tsai et al. reported 73 bound electron-hole pairs (excitons) under illumination. 43,44 42 that non-encapsulated single crystals of n-butylammonium- 74 It has further been suggested that inter-chain charge sep-

44 moisture-driven chemical degradation. They also showed that 45 encapsulation of the crystals resulted in no chemical degrada-46 tion under highly illuminated conditions, and built solar cells 47 with a PCE of 12.5 with n=3 and n=4 layers %. 32 The broad applications and variability of LHOPs have opened a field of <sup>49</sup> research that is just beginning to produce deeply insightful and 50 practically applicable results.

The LHOPs studied in this work fall into the Ruddlesden-52 Popper crystal class<sup>35</sup> and their characteristic structure con- $_{53}$  sists of 2D layers of n corner-sharing metal-halide octahedra 54 separated by, and ionically bonded to, large charged poly-55 atomic cations (see Fig. 1). The inorganic perovskite layer  $_{56}$  can be tuned to a specific width of n octahedra or even cleaved 57 along various planes, linking the octahedra in linear or zig-zag <sub>58</sub> corrugated patterns. <sup>36–38</sup> Opportunities to engineer LHOPs 59 not only originate from changing the inorganic perovskite 60 stoichiometry, but also by choosing one or more of many 61 complex large organic cations to separate the layers. <sup>26,36–39</sup> 62 Promising organic cations range from simple carbon chains 63 with ammonium caps to large chromophore complexes. 40-42 64 These degrees of freedom allow for the exploration of a wide 65 variety of electronic properties and to tune optical response.

In this context, optically activated charge separation behave been suggested to be used as highly efficient white 67 tween the organic and inorganic layers of LHOPs has been 68 long sought to reduce the overlap between electron and confinement effects within perovskite layers can be engi- 69 hole wave functions and, thus, allow utilization of separated neered and tailored to specific applications. <sup>28–31</sup> In particu- 70 electron-hole channels for highly efficient charge transport. lar, they are able to overcome some of the above-mentioned  $\tau_1$  The advent of organic solar cells has proven that  $\pi$ -conjugated limitations, 32-34 by offering much improved stability and 72 polymers are fully capable of producing and transporting  $_{43}$  methylammonium lead-iodine with n=3 and 4 layers resists  $_{75}$  aration of bound electron-hole pairs is possible in these

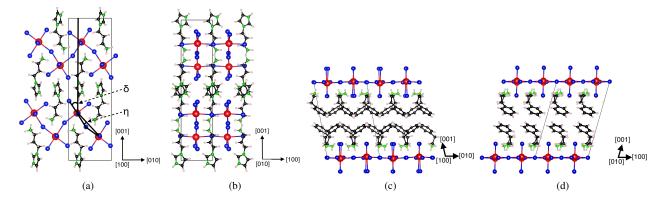


FIG. 1. (Color online.) The atomic structure of ammonium-propyl-imidizole (API)-PbBr<sub>4</sub> projected along the (a) [100] direction and (b) [010] direction and 2-phenethylammonium (PEA<sub>2</sub>)-PbBr<sub>4</sub> projected along the (c) [100] and (d) [010] axis. The stacking direction is [001]. Atomic color coding: Pb (red), Br (blue), C (black), N (green), and H (pink). Tilting angle  $\delta$  and bond angle  $\eta$  are indicated (see text).

<sub>76</sub> systems. Furthermore, charge transfer between semicon- <sub>115</sub> correlation from their analysis of the optical absorption and whether organic layers in LHOPs with  $\pi$ -conjugated organic 119 optical absorption and emission of LHOPs is still open. cations could similarly carry photo-current under illumination if optical absorption excites electrons and holes that are localized in parallel layers of the LHOP system. If so, extensive chemical degrees of freedom in LHOPs could allow for engineering a layered organic-inorganic compound material that are capable of efficiently separating electrons and holes. These layers may provide separate conduction channels for electrons and holes, potentially reducing detrimental recombination. However, it is unknown how active the  $\pi$ -conjugated organic compounds in LHOPs are under UV-VIS absorption, in particular in the stoichiometric limit of n=1 perovskite layers between each organic layer.

magnitude of the Stokes shift, 51,52 Du et al. found no such 148 separate electrons and holes between layers.

ductor CdSe quantum dots and poly[2-methoxy-5-(2-ethyl- 116 emission character of layered Pb(I,Br,Cl)4 perovskites with hexyloxy-p-phenylenevinylene)] bonded functional coatings 117 acene alkylamine organic cation layers. 53 Hence, the debate has been observed. 46 This raises an interesting question 118 to what extent  $\pi$ -conjugated organic layers participate in the

In the present study, we report first-principles calculations, 121 for single  $\pi$ -conjugated LHOPs to determine the organic and 122 inorganic layer contributions to electronic structure and op-123 tical absorption. We also clarify at what energies this be-124 comes a significant contributor to the total optical response. The materials of interest are the  $\langle 110 \rangle$  API-PbX<sub>4</sub> class (X=I, 126 Br, Cl) of layered perovskites, motivated by the work of Li et To address this, Li et al. conclude from a large Stokes  $_{127}$  al.  $^{47}$  and the single  $\pi$ -conjugated organic cation perovskites 2shift in the photoluminescence emission spectrum that charge 128 phenyl-ethylammonium (PEA) PEA<sub>2</sub>-PbX<sub>4</sub> (X=I, Br, Cl) due separation occurs between the organic ammonium-propyl- 129 to their readily available experimental atomic geometries and imidazole (API) layer and inorganic PbBr<sub>4</sub> perovskite layer 130 single π-conjugated (benzene) group per organic ion (see Fig. of [110] oriented API lead-bromide (n=1). <sup>47</sup> They also per- 131 1). We compute the ion-projected electronic structure and formed density functional theory (DFT) calculations and re- 132 single-particle optical response using density functional theport an isolated carbon- $\pi^*$  state in the fundamental band 133 ory (DFT), including spin-orbit coupling (SOC) and band gap gap, to which they attribute the carrier separation and re- 134 corrections determined by HSE06 hybrid-functional calculasulting massive Stokes shift. However, this material has not 135 tions. The PBE+SOC+ $\Delta_{HSE06}$  calculations reported in this been studied by modern first-principles approaches that in- 136 work are an approximation of the full single-particle exciclude the effects of spin-orbit coupling (SOC) and electron- 137 tation energy calculations within the GW+SOC many-body hole interaction on the optical-absorption spectrum. In par- 138 perturbation theory formalism. 54 The two-particle optical reticular, SOC has shown to be very important in determin- 139 sponse, which includes the effect of exciton formation, is ing the correct electronic band structure in Pb-containing hy- 140 calculated from the solution of the Bethe-Salpeter equation brid perovskite materials. 14,15,29,48 Furthermore, several rea- 141 (BSE). Our results clarify energetic alignment of the bands sons for a large Stokes shift are debated and no conclusion 142 associated with organic and perovskite components in both has been reached: It has been suggested recently that it orig- 143 materials and provide detailed analysis of essential electronic inates from strongly bound small-polaron states that form in 144 wavefunctions and individual contributions to optical absorpthe perovskite layer, lowering the emission energy of electron- 145 tion spectra. This allows us to answer the question whether hole pairs. 49,50 While the extent of octahedral tilting in and 146 optical excitations occur within individual layers of single 113 out of the perovskite plane has also been correlated with the 147  $\pi$ -conjugated LHOPs or whether optical excitations partially

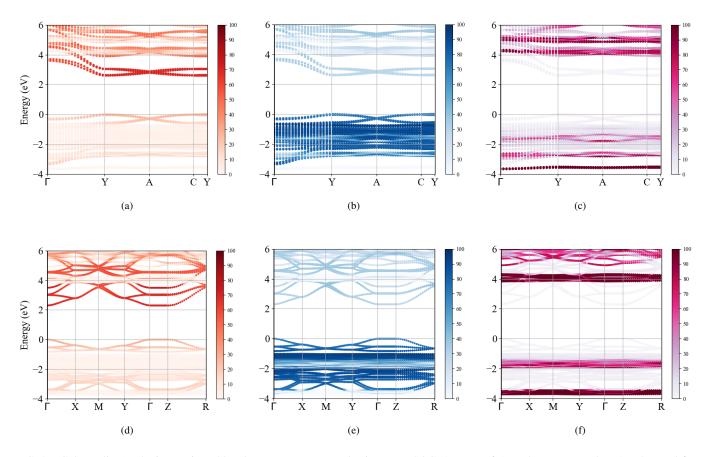


FIG. 2. (Color online.) The ion-projected band structures, computed using PBE+SOC+ $\Delta_{HSE06}$ , of API-PbBr<sub>4</sub> (a-c) and PEA<sub>2</sub>-PbBr<sub>4</sub> (d-f). The color bar indicates the contribution of Pb (red), Br (blue), and API/PEA (magenta) to each state as a percentage.

RESULTS

149

**Atomic Structure:** The structure of single-layer  $\langle 110 \rangle$ API-PbX<sub>4</sub> compounds resembles that of the  $\langle 100 \rangle$  class of layered perovskites: The major difference is the corrugation of the perovskite layer with a zig-zag type octahedral linking in the  $\langle 110 \rangle$  compounds and a linear-type linking in the  $\langle 100 \rangle$ compounds. Figure 1 shows the [100] and [010] projections of both API-PbBr<sub>4</sub> and PEA<sub>2</sub>-PbBr<sub>4</sub>. PEA<sub>2</sub>-PbX<sub>4</sub> experimental structures are used in our study. 53-57 Since experimental data is available only for API-PbBr<sub>4</sub>, 47 we fully relax all API-PbX<sub>4</sub> atomic geometries in the  $P2_1/c$  symmetry space group. The esulting lattice parameters and vector angles, unit-cell volumes, octahedron tilting angles, and Pb-X-Pb bond length ranges are reported in supplemental information (SI) Table S1 for all systems. The relaxed API-PbBr<sub>4</sub> atomic structure in excellent agreement with the experimental structure determined by Li et al., 47 with errors of under 1 % for lattice parameters, 0.2 % for unit-cell volume, 1 % for lattice vector angles, 2.5 % for out-of-plane tilting, and 15 % for in-plane  $_{\text{168}}$  tilting angles. The out-of-plane tilting angles  $\delta_{1}$  and  $\delta_{2}$  in the 169 corrugated (110) API-PbX<sub>4</sub> systems should be 45°, if no tilt-170 ing is present. For the relaxed API-PbX4 structures we find 193

 $_{171}$  two distinct  $\delta_1$  and  $\delta_2$  in the range between 33.7° and 33.8°  $_{172}$  and 51.4° and 53.9°, respectively.

In the linearly-linked PEA<sub>2</sub>-PbX<sub>4</sub> systems,  $\delta$ =0° under no tilting and indeed in the experimental structures, the out-of-plane tilting angles remain small, in the range of 1° to 3°. The in-plane-tilting angles, ranging between  $\eta$ =12.2° and  $\eta$ =14.5°, are larger compared to those found in the API-PbX<sub>4</sub> systems, ranging from  $\eta$ =8.5° to  $\eta$ =10.5°. This in-plane tilting in gis very similar to the octahedron tilting in orthorhombic MAPbX<sub>3</sub> 3D HOPs.<sup>58</sup>

Electronic Structure: The band structures of API-Pb $X_4$  and PEA- $_2$ Pb $X_4$  reveal dispersive band frontiers attributed to states localized on the perovskite as well as flat, non-like dispersive bands, situated more than 1 eV away from the band frontiers, that are attributed to the organic  $\pi$  and  $\pi^*$  states (see Fig. 2). Throughout the remainder of the paper, the label PBE+SOC+ $\Delta_{HSE06}$  refers to the PBE+SOC band structure with conduction bands rigidly shifted to higher energy to fully non-collinear HSE06 hybrid-functional calculations that take SOC into account. Table I reports relevant calculated and experimentally determined energy gaps of these materials.

Ion-projected PBE+SOC+ $\Delta_{HSE06}$  band structures are plot-

TABLE I. Energy gaps (in eV) computed using different levels of theory. PBE+SOC+ $\Delta_{HSE06}$  refers to the PBE+SOC electronic structure with the band gap rigidly shifted to the HSE06+SOC band gap value (see text).

Level of theory	API-PbI <sub>4</sub>	API-PbBr <sub>4</sub>	API-PbC
PBE+SOC	1.44	1.94	2.41 24
HSE06+SOC	2.10	2.74	3.32 24
$\pi - \pi^*$ gap (PBE+SOC+ $\Delta_{HSE06}$ )	5.87	5.88	5.7 24
BSE Optical gap	1.74	2.23	2.68 24
Exp. Optical gap <sup>47</sup>	_	3.18	<b>—</b> 24
	PEA <sub>2</sub> -PbI <sub>4</sub>	PEA <sub>2</sub> -PbBr <sub>4</sub>	PEA <sub>2</sub> -Pb
PBE+SOC	1.33	1.75	2.12 24
HSE06+SOC	1.95	2.45	2.95 24
$\pi - \pi^*$ gap (PBE+SOC+ $\Delta_{HSE06}$ )	5.39	5.82	5.53
Exp. optical gap <sup>53</sup>	2.45	3.0	3.6 24
			24

with spin-orbit coupling underestimates the gap of 3.18 eV measured from the optical onset by Li et al..47 This can be attributed to the fact that HSE06, albeit it improves over the DFT-PBE description, does not fully capture quasiparticle effects for the systems studied here. More sophisticated, but computationally more expensive methods, such as many-body perturbation theory, could mitigate these shortcomings.<sup>59</sup> Additionally, in this comparison the electron-hole interaction was neglected and, thus, the calculated electronic gap differs from the measured optical gap by the exciton binding energy. This will be discussed in the results for optical response. Differences between our relaxed structure and the experimental structure of API-PbBr<sub>4</sub> are expected to result in only small changes of the band gap, within 0.2 eV, based on the effects of in- and out-of-plane angles on gap values explored by Pedesseau et al..<sup>29</sup> Figure 2 clearly shows that the band dispersion of API-PbBr<sub>4</sub> along the  $Y - \Gamma$  direction is free-electron like, with a parabolic curvature near the Y point. Along the Y-A direction, the dispersion has a lower curvature, indicating a higher electron effective mass. Finally, along the Y-Cdirection the bands are effectively flat due to the layered and reduced periodicity of the LHOP crystals along the [001] direction. We observe the same trend for API-PbI<sub>4</sub> and API-225 PbCl<sub>4</sub>. 226

same  $P\bar{1}$  space group as the PEA<sub>2</sub>-PbBr<sub>4</sub> and PEA<sub>2</sub>-PbCl<sub>4</sub> 292 mal, and PBE+SOC+ $\Delta_{\rm HSE06}$  calculations are a good basis for

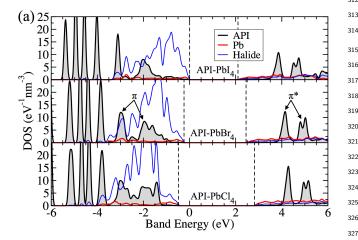
227

235 systems. The band structure of PEA2-PbBr4, illustrated in 236 Fig. 2(d)-(f), exhibits highly dispersive, free-electron like <sub>237</sub> band frontiers along the  $\Gamma - X$  and  $\Gamma - Y$  directions, as well 238 as flat, non-dispersive band frontiers in the  $\Gamma$ -Z direction.  $\frac{1}{2}$  Unlike the API-PbX<sub>4</sub> corrugated perovskites, the PEA<sub>2</sub>-PbX<sub>4</sub> <sup>14</sup>/<sub>40</sub> perovskites explored in this work are not corrugated in either in-plane direction. Thus, they have a higher periodicity in both in-plane lattice directions which manifests itself in highly dispersive band frontiers along two reciprocal-lattice 44 directions. As a consequence, corrugated API-PbX<sub>4</sub> shows  $\square$ 4low effective-mass band frontiers only along  $\Gamma - Y$ , whereas PEA<sub>2</sub>-PbX<sub>4</sub> shows low effective masses along both  $\Gamma$ -X and  $\Gamma - Y$ .

In traditional 3D HOPs such as MAPbX<sub>3</sub>, valence and con-<sup>249</sup> duction band frontiers are comprised of X:p+Pb:6s and Pb:6p 250 states, respectively. 60 While in principle, in the layered sys-251 tems with conjugated organic cations explored in this work, <sub>194</sub> ted for API-PbBr<sub>4</sub> in Fig. 2(a)-(c). Similar data for the other <sub>252</sub> API and PEA  $\pi$  and  $\pi$ \* states could contribute in the near-195 API and PEA LHOPs considered in this work can be found 253 gap region, we find from the ion-projected band structure that in SI Figs. S2 and S3. Due to the  $P2_1/c$  symmetry, the API- 254 the valence and conduction band frontiers are comprised of 197 PbX4 materials exhibit direct gaps of 2.10 eV, 2.74 eV, and 255 X:p+Pb:6s and Pb:6p states, respectively. This is very simi-3.32 eV for API-Pb(I, Br, and Cl), respectively, at the Y point 256 lar to the 3D MAPbX3 HOPs. However, unlike 3D MAPbX3 of the Brillouin zone (BZ). The Y point folds back to the  $\Gamma$  257 HOPs that have organic states far below (about 6 eV) and point when a 2×2 conventional cell is considered as demon- 258 above the band frontiers, 60 API-PbX4 and PEA2-PbX4 have strated by Pedesseau et al.<sup>29</sup> The band gap we computed for 259 flat, non-dispersive bands attributed to API and PEA<sub>2</sub>  $\pi$  and API-PbBr4 using the HSE06 exchange-correlation functional  $_{260}$   $\pi^*$  orbitals within 1.0 to 2.0 eV of the band frontiers, as shown 261 in Fig. 2.

Furthermore, due to the strong contributions of Pb-derived 263 states to the band frontiers in API-PbX<sub>4</sub> and PEA<sub>2</sub>-PbX<sub>4</sub>, the 264 spin-orbit interaction lowers the energy of conduction-band 265 minimum states (see Fig. S5). This energy reduction of 266 Pb:p conduction-band states is well known in Pb- and Sn-267 containing HOP and LHOP systems 14,15,29,48 and attributed 268 to the large mass of Pb atoms. Hence, SOC-related energy 269 contributions are critical for correctly predicting the energetic 270 ordering of states near the band-extrema and, in particular, to 271 qualitatively explain the relative energy position of organic  $_{272}$   $\pi$  and  $\pi^*$  states. In Fig. 2 (as well as Figs. S4 (a) and (b) 273 and S5 (a) in the SI) we clearly show that once SOC is taken 274 into account, the ion-resolved band ordering at the  $\Gamma$ -point 275 conduction band minimum changes: The Pb:p states are low-276 ered in energy relative to the API  $\pi^*$  states which remain 277 unaffected by the spin-orbit interaction. As a result, we ob-278 serve Pb:p character for all k points throughout the BZ. In 279 contrast, without the inclusion of SOC, a band inversion oc- $_{280}$  curs at the  $\Gamma$ -point and the conduction band minimum would <sub>281</sub> be attributed to mostly API  $\pi^*$  states. Hence, if SOC is ne-282 glected, electronic-structure calculations could, depending on 283 transition matrix element amplitude, incorrectly predict that 284 excitations from the Γ-point band frontiers result in charge In contrast, band structures of the PEA<sub>2</sub>-PbX<sub>4</sub> LHOPs, with 285 separation between perovskite and API layers. This behavspace groups  $P2_1/c$ ,  $P\overline{1}$ , and  $P\overline{1}$  for I, Br, and Cl, respectively, 286 ior is different from what has been observed for 3D MAPbX<sub>3</sub> exhibit direct gaps of 1.95 eV, 2.45 eV, and 2.95 eV at the  $\Gamma$ - 287 HOPs, for which ion projection of the band frontiers remain point. The difference between the space groups of PEA<sub>2</sub>-PbI<sub>4</sub> 288 the same, with X+Pb and Pb attributed to the valence and conand PEA<sub>2</sub>-Pb(Br,Cl)<sub>4</sub> is due to the bis-phenylethylammonium 289 duction band frontiers, respectively, 60 whether or not SOC conformation of the chosen PEA<sub>2</sub>-PbI<sub>4</sub> structure.<sup>53</sup> The gen- <sup>290</sup> is included. Finally, we note that the difference between <sub>233</sub> eral PEA<sub>2</sub> conformation explored by Du et al. assumed the <sub>291</sub> HSE06+SOC and the PBE+SOC+ $\Delta_{HSE06}$  approach is mini-

<sub>294</sub> in the SI that for optical excitations energies below 5 eV, only <sub>309</sub> and Cl having ionization energies of 10.45, 11.81, and 12.96 295 small errors of under 0.5 eV are expected for spectral features. 310 eV (from the NIST Atomic Spectra Database Ionization Ener-



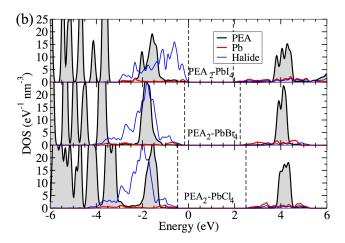


FIG. 3. (Color online.) The PBE+SOC+ $\Delta_{HSE06}$  ion-projected DOS of (a) API-PbI<sub>4</sub>, API-PbBr<sub>4</sub>, API-PbCl<sub>4</sub> and (b) PEA<sub>2</sub>-PbI<sub>4</sub>, PEA<sub>2</sub>-PbBr<sub>4</sub>, and PEA<sub>2</sub>-PbCl<sub>4</sub>. The energies of the Pb 5d states at -15.3eV are used for alignment, and the valence band maxima of API-PbI<sub>4</sub> and PEA<sub>2</sub>-PbI<sub>4</sub> are used as energy zero. Dashed lines mark the band extrema. Color coding: Pb (red), halide (blue), organic layer (shaded brown).

band maximum located at 0.0, -0.17, and -0.47 eV occurs  $_{363}$  to API-derived states are expected between the optical onset <sub>306</sub> for the PEA<sub>2</sub>-PbX<sub>4</sub> systems for X = I, Br, and Cl, respec- <sub>364</sub> and 5.7 eV. This changes in the PEA<sub>2</sub>-PbX<sub>4</sub> systems, where 307 tively. This decrease can be understood by examining stan- 365 the PEA density of states amplitude in the valence and is about

293 optical response calculations. To this end we show in detail 308 dard atomic ionization energies of halide atoms, with I, Br, gies Form).<sup>61</sup> Since the valence-band maximum of each per-312 ovskite material in this work is attributed to halide p-states, our findings are commensurate with trends of these atomic ionization energies.

> At the same time, this figure shows that organic  $\pi$  and  $\pi^*$ states are not affected by the changing halide mass and remain approximately aligned in both systems. The API  $\pi$  states appear as broad peaks at -2.00, -1.78, and -1.40 eV for I, Br, and Cl, respectively. This broadening is due to static molecular disorder and coupling between organic molecular states. The lowest energy  $\pi^*$  states appears as sharp peaks centered around 3.87, 4.10, and 4.30 eV for I, Br, and Cl, respectively. The resulting  $\pi - \pi^*$  gaps, defined as the energy differences of these peaks, are 5.87, 5.88, and 5.70 eV and show a width of about 0.5 eV from the broadening of the  $\pi^*$  state. The PEA<sub>2</sub>-PbX<sub>4</sub> systems display a highest occupied  $\pi$  state peak spanning the range between -1.3 and -2.1 eV. A single lowest unoccupied  $\pi^*$  peak is located between 3.84 and 4.10 eV for all PEA<sub>2</sub>-PbX<sub>4</sub> materials. This leads to  $\pi - \pi^*$  gaps of 5.39, 5.82, and 5.53 eV for I, Br, and Cl, respectively, with a width of about 1.0 eV. The variations in the  $\pi - \pi^*$  gaps in the PEA<sub>2</sub>-PbX<sub>4</sub> systems are attributed to differences in the experimental X-ray atomic structures of the organic layers used in 334 the unit cells of this study. As we chose to relax the API-335 PbX<sub>4</sub> structures (due to the similarities of the relaxed and 336 experimental API-PbBr<sub>4</sub> structures and the lack of available experimental data for API-Pb(I,Cl)<sub>4</sub>) the  $\pi - \pi^*$  gaps are uniform across the choice of halide. We note that quasiparticle corrections computed within HSE06+SOC also produce an energy-dependent band dilation, not reproduced by the scissor approach. This increases the  $\pi - \pi^*$  gaps of the API and PEA systems to about 6.1 – 6.3 eV, suggesting that  $\pi - \pi^*$  optical transitions will occur well in the UV photon energy range. The PBE+SOC+ $\Delta_{HSE06}$  approximation captures the UV response of the intra-organic transitions, albeit at slightly lower energies compared to HSE06+SOC, and therefore provides a reasonable approximation for optical response calculations. It should be mentioned that, in reality, the absorption onset of such molecules is at lower energies due to large exchange en-350 ergy contributions. For example, benzene in an alcohol solu-351 tion has an absorption onset of about 4.8 eV.<sup>62</sup> However, this 352 is still in the UV energy range.

Figure 3 also shows that, due to a lower cation charge of The ion-resolved density of states (DOS) in Fig. 3 illus- 354 +1 on PEA compared to +2 in API, the ratio of organic to trates that in all six perovskite systems, the valence- and 355 inorganic density of states is higher in the PEA<sub>2</sub>-PbX<sub>4</sub> strucconduction-band frontiers are attributed to halide and Pb 356 tures. This implies that, if organic-perovskite optical transistates, respectively. For this analysis, we aligned the Pb:5 $d_{357}$  tions are allowed, the PEA<sub>2</sub>-PbX<sub>4</sub> systems have more possible states at -15.3 eV across the different materials. Importantly, 358 charge-separation pathways under optical excitation. In ex-Fig. 3 shows a reduction of the valence-band maximum in en- 359 amining the ion-resolved density of states of API-PbX<sub>4</sub>, it can ergy with decreasing halide mass: The valence band maxima  $_{360}$  be seen that the optical response below the 5.7 eV  $\pi - \pi^*$  gap of API-PbX<sub>4</sub> shift from 0.0, to -0.24, and -0.48 eV for X <sub>361</sub> contains mostly transitions between perovskite-derived states. = I, Br, and Cl, respectively. The same trend of the valence 362 Only small contributions due to transitions from perovskite<sub>366</sub> equal to or greater than the perovskite density of states at the <sub>424</sub> tions from PbX<sub>4</sub> to PEA states appear at higher energies at states available.

tween layers, however, depends again on the dipole matrix el- 443 separation only occurs in the UV energy range. ements for the corresponding optical transitions between these 444 organic and perovskite states. This will be discussed next.

projections are finite.

separation for visible light energy excitations.

intra-organic optical response within the PEA layers, along with significant inter-layer absorption in the UV energy range. 476

PEA  $\pi$ -state energy. Consequently, the optical response could 425 lower halide masses, corresponding to the increased VBM- $\pi$ \* have a large contribution from perovskite to PEA transitions 426 gap by the decrease in the valence band energy. In PEA<sub>2</sub>at lower energies than the  $\pi - \pi^*$  gap. This implies that if 427 PbI<sub>4</sub>, strong transitions are observed from PbI<sub>4</sub> to PEA states transitions between perovskite and PEA are optically allowed, 428 at lower energies than those between PEA states, leading to the PEA<sub>2</sub>-PbX<sub>4</sub> systems have more possible charge separation 429 the same partial charge separating activity seen in API-PbX<sub>4</sub> 430 above 4 eV. In PEA<sub>4</sub>-PbBr<sub>4</sub>, the contributions due to transi-Finally, in the context of achieving charge separation be- 431 tions from PbBr4 to PEA and PEA to PbBr4 are roughly equal tween organic and perovskite layers upon optical excitation, 432 in the 4 to 5 eV photon range, leading to a cancellation in parwe find that PEA2-PbCl4 is a particularly promising candi- 433 tial charge separation character due to hybridization. PEA2date. The ion-resolved DOS in Fig. 3 shows a pronounced 434 PbCl<sub>4</sub> shows a change in behavior: The optical response bepeak associated with the organic molecule that is centered 435 tween 3.5 and 4 eV largely arises from intra-perovskite trannear 1.5 eV below the valence-band maximum. Not only is 436 sitions and contributions from PEA to PbCl<sub>4</sub> states, partially this peak higher in energy than another peak at -2 eV that is 437 separating holes to the PEA layer and electrons to the PbCl<sub>4</sub> attributed to Cl ions, but it also is of the same magnitude, as  $^{438}$  layer. This behavior is due to the proximity of the PEA  $\pi$ discussed above. This energetic positioning of states suggests 439 states to the PbCl<sub>4</sub> attributed valence band maximum, leading the strong potential for partial charge separation, generating 440 to inter-layer transitions closer to the absorption onset. Howholes in the PEA $_2$   $\pi$  state and electrons in the conduction-band  $_{441}$  ever, overall, in PEA $_2$ -PbX $_4$ , where the organic optical activ-Pb:6p state. The actual probability of charge separation be- 442 ity is more significant compared to API-PbX4, partial charge

In all three LHOP API-PbX4 compounds, excitonic ef-445 fects are expected to be stronger compared to their 3D HOP Optical Response: The ion-projected dielectric function 446 MAPbX<sub>3</sub> counterparts owing to quantum and dielectric con- $\varepsilon_2(\omega)$  is illustrated in Fig. 4 for all considered materials. 447 finement effects. This increased binding energy was first Here we distinguish between transitions among perovskite 448 explained by the works of Rytova and Keldysh, who sepions ('inorganic') and organic cations ('organic') by bundling 449 arately established the theory of quantum confinement of them into the inorganic-inorganic, organic-organic, organic- 450 charge carriers and the Coulomb interaction in low dimeninorganic and inorganic-organic subcategories. The first two 451 sional systems. 63,64 This was further explored in layered semicorrespond to intra-layer transitions and the latter two to inter- 452 conductors by Hanamura and layered perovskites by Ishihara layer transitions. If the two sub-layers were to act as separate 453 and Koutselas. 65-68 In 3D HOPs such as MAPbI<sub>3</sub>, MAPbBr<sub>3</sub>, optically active materials, the amplitude of inter-layer  $\varepsilon_2(\omega)$  454 and MAPbCl<sub>3</sub>, the high-frequency dielectric constants  $\varepsilon_{\infty}$  are is vanishing. In the case of intra-layer optical excitation, these  $_{455}$  about 4-7.48,69-71 MAPbX<sub>4</sub> also has highly dispersive band 456 frontiers, leading to a low reduced electron-hole mass of about By ion-resolving the imaginary dielectric function of API-  $^{457}$  0.1 $m_0$ . Using a simple Wannier-Mott model, the exciton PbX<sub>4</sub>, we show that optical excitations below 4 eV are entirely 458 binding energy is in the range of 25 to 85 meV. As determined dominated by intra-perovskite transitions, whereas inter-layer 459 in experiments and predicted by theory, the low-frequency ditransitions contribute significantly to the optical response 460 electric constants are also large ( $\varepsilon_s > 20$ ), which enhances above 4 eV. As discussed above, this is because states in the 461 the screening of the electron-hole Coulomb potential. 29,72-75 vicinity of the gap are attributed entirely to perovskite states 462 Given the API-PbBr4 electronic structure determined in this (Fig. 3). Absorption between API-derived states, with an on- 463 work, the high-frequency dielectric constant is determined to set around the  $\pi - \pi^*$  gap, contributes weakly to the overall 464 be 3.94 by density-functional perturbation theory (DFPT) and optical response even in the UV energy range due to a low 465 the reduced electron-hole mass at the band frontiers is aprelative API- $\pi$  density of states compared the halide density 466 proximately 0.610 $m_0$ , based on an averaged parabolic fit to of states in the valence band. Figure 4 also shows that transi-  $^{467}$  the dispersive, in-plane,  $Y \to G$  and  $Y \to A$  directions. This tions from PbX<sub>4</sub> to API states are responsible for a significant 468 leads to a Wannier-Mott binding energy of 525 meV, which portion of the optical response in the UV energy range, and 469 is an order of magnitude higher compared to the 3D counterthus partial electron and hole separation occurs between the 470 parts. The lower high-frequency dielectric constants predicted API and PbX<sub>4</sub> layers. However, this partial separation has 471 by DFPT range from 3.47 to 4.76 for the LHOP systems (see little utility for optoelectronic applications requiring charge 472 Tab. S2) and originate from the alternating low and high values of  $\varepsilon_{\infty}$  between layers averaged over the unit cell volume. <sup>76</sup> The PEA2-PbX4 systems demonstrate a much stronger 474 This leads to an average dielectric constant that is lower than those typically measured and calculated for 3D HOPs.<sup>29,30</sup>

The excitation energies of lone API molecules in air are As with API-PbX<sub>4</sub>, the near-gap and visible energy range of 477 calculated in the Gaussian suite<sup>77</sup> to determine if the organic the spectra is governed by intra-perovskite optical response. 478 optical response will comprise a significant portion of the Around the  $\pi - \pi^*$  gap, a large peak appears in the imaginary 479 optical response near the perovskite absorption edge. The dielectric function which is attributed to the intra-PEA optical 480 HSE, B3LYP, and CAM-B3LYP functionals are used to caltransitions and transitions from PbX<sub>4</sub> to PEA states. Transi- 481 culate the homo-lumo gaps of 5.60, 5.84, and 8.05 eV respec-

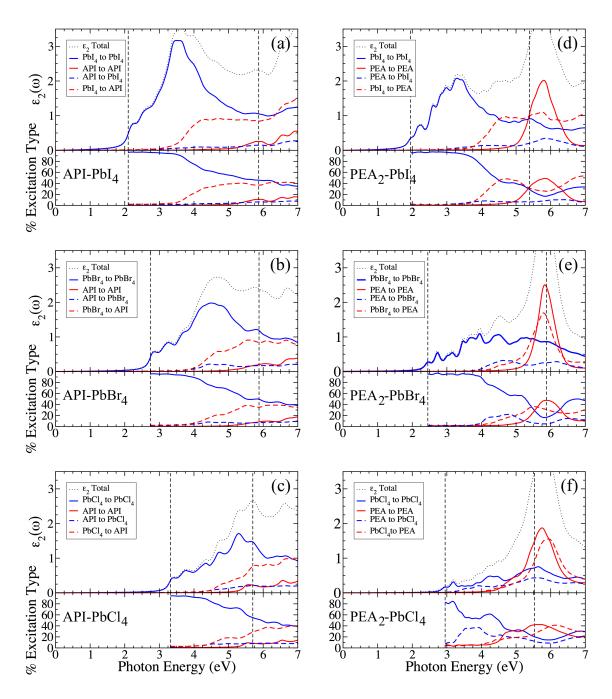


FIG. 4. (Color online.) The ion-resolved imaginary dielectric functions of (a) API-PbI<sub>4</sub>, (b) API-PbBr<sub>4</sub>, (c) API-PbCl<sub>4</sub>, (d) PEA<sub>2</sub>-PbI<sub>4</sub>, (e) PEA<sub>2</sub>-PbBr<sub>4</sub>, and (f) PEA<sub>2</sub>-PbCl<sub>4</sub>. The color coding indicates the resolution of  $\varepsilon_2$  along specific ion-to-ion transitions, which are (in valence ions → conduction ions notation) perovskite →perovskite (blue, solid), organic →organic (red, solid), organic →perovskite (blue, dashed), perovskite-organic (red, dashed), and all (black, dotted). The bottom panels show the percent that each type of transitions contributes to the total  $\varepsilon_2$  as a function of photon energy.

482 tively in the singlet-relaxed geometry. The HSE and B3LYP 489 cur near the perovskite excitonic absorption edge. agree very well with the  $\pi$ - $\pi$ \* gap found in API-PbX<sub>4</sub> at the 490 Strong excitonic effects and, hence, large exciton bind-487 B3LYP functionals, respectively. These results suggest that 494 Fig. 5 that excitonic effects significantly influence the optical-

PBE+SOC+ $\Delta_{HSE06}$  level of theory. Excitation energies are 491 ing energies are predicted for the API-PbX<sub>4</sub> materials from calculated using time-dependent DFT and are found to be 492 first principles, with values comparable to available experi-5.42, 5.23, and 5.75 eV within the HSE, B3LYP, and CAM- 493 mental data for LHOP systems. For API-PbX4, we show in 488 the excitonic absorption onset of the API spacer will not oc- 495 absorption spectra. The gradual absorption onset observed in

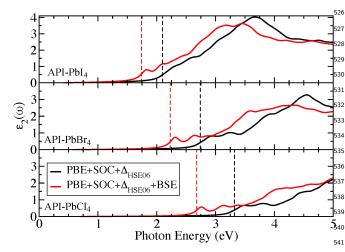


FIG. 5. (Color online.) Imaginary part of the dielectric function of API-PbI<sub>4</sub> (top), API-PbBr<sub>4</sub> (middle), and API-PbCl<sub>4</sub> (bottom) with (red lines) and without (black lines) excitonic effects. The PBE+SOC Kohn-Sham energies and states are used as input to the BSE and the single-particle band gap is shifted to the HSE06+SOC value. That band gap and the lowest excitation from the BSE are marked by vertical black and red dashed lines, respectively.

496 the single-particle dielectric function becomes a pronounced excitonic peak, red-shifted to lower energy, that is associated with the lowest-energy electron-hole bound state. In 553 ≈505 meV. Finally, the strongest excitonic red shift in the op- 571 ization energy of perovskite systems. tical spectrum of  $\approx$ 638 meV is predicted for API-PbCl<sub>4</sub>, with 572 <sub>524</sub> data to compare with for the API-PbX<sub>4</sub> materials, we use the <sub>579</sub> experimentally and between 4.7 and 6.9 eV theoretically by

proximation.

The predicted exciton binding energies and relative positions of spectral peaks are in good agreement with available experimental data of layered perovskite systems. 47 Wang <sub>530</sub> et al. measured exciton binding energies of 218 meV in hexadecammonium-lead bromide (HA)<sub>2</sub>PbBr<sub>4</sub>, <sup>79</sup> Blancon *et* al. measured binding energies of 380, 270, and 220 meV in  $_{533}$   $n = 1, n = 2, \text{ and } n > 2\text{-layered } (BA)_2(MA)_{n_1} Pb_n I_{3n+1},^{39} \text{ and }$ Ishihara et al. calculated a binding energy of 320 meV in n=1 layered PbI<sub>4</sub> octahedra with no organic spacer. 66 As a model 536 function relying on a single, material-averaged, dielectric constant is used to compute the screened Coulomb interaction be-538 tween electrons and holes, we do not account for the local field effects arising from the high spatial variability of the dielectric constant in LHOPs.<sup>29,30</sup> More precise techniques such <sub>541</sub> as including the full inverse dielectric tensor  $\varepsilon_{G,G'}(q)^{-1}$  or 542 semi-classical and semi-empirical methods that describe di-543 electric constant fluctuations can be used for a higher degree of accuracy. <sup>29,80–82</sup> These high binding energies are also potentially detrimental to solar cell applications. which rely on splitting of electron-hole pairs. Investigations by Smith et al. have shown that the introduction of halogens by I<sub>2</sub> inter-548 calation into the organic layer strongly reduces binding energy and the dielectric confinement of the layered perovskite 550 systems, 83 potentially lowering the exciton binding energy of 551 LHOPs which is preferable for photo-voltaic application.

#### CONCLUSIONS AND FUTURE DIRECTION

This computational study predicts that the optical readdition, there is also a significant red shift of broad high- 554 sponse of single-layered lead-halide perovskites with singleenergy peak structures between 3.5 eV and 4.5 eV, resulting in  $_{555}$   $\pi$ -conjugated organic layers API and PEA<sub>2</sub> is dominated by strongly increased absorption at lower energies. In our calcu- 556 intra-perovskite optical excitations in the visible energy range. lations, the energy difference of the onsets of single-particle 557 A partial charge separation between the organic perovskite and BSE spectrum correspond to the binding energy of the 558 states can only be achieved at UV energies. Given these relowest electron-hole pair. The high computational cost of the 559 sults, we conclude that single-layered PbX<sub>4</sub> LHOP systems BSE calculations in this work, due to large unit cells and in- 560 with  $\pi$ -organic cation spacing layers composed of moieties lusion of spin-orbit coupling, does not allow a dense enough 561 with single aromatic rings act as one optically active permultiple k-point sampling<sup>78</sup> to provide fully converged results 562 ovskite material. Transitions involving both layers only ocfor this quantity. Given the choice of k-point mesh, we esti-  $_{563}$  cur at UV photon energies. Importantly, the lack of  $\pi$  and mate that our numbers are within 100 meV of the converged 564  $\pi^*$  states near the band extrema causes transitions in the visresult (see SI figure S6). From our data we extract ≈357 meV 555 ible energy range to be contained within the perovskite layer, (see Fig. 5) for the exciton-binding energy of API-PbI<sub>4</sub>, which 566 meaning all electron-hole generation for optoelectronic appliis the smallest value for the three API-PbX<sub>4</sub> compounds stud- 567 cations in this energy range will be localized to the PbX<sub>4</sub> ocied in this work. API-PbBr<sub>4</sub> shows a stronger exciton binding 558 tahedral layers. At UV energies, significant electronic deloenergy due to the lower dielectric constant compared to API- 569 calization and charge separation is allowed, however the cor-PbI<sub>4</sub>, and consequently a stronger red shift of the onset by 570 responding excitation energies are close to or above the ion-

The natural follow-up question is: How can charge separathe lowest high-frequency dielectric constant. High-frequency 573 tion be further achieved in layered hybrid perovskite systems? dielectric constants are slightly overestimated as they are cal-  $_{574}$  The first item that must be addressed is the  $\pi - \pi *$  gap of the culated at the PBE+SOC level of theory. However, from 575 conjugated groups. As discussed above, the absorption onset test calculations we estimate that increasing the band gap to 576 of single aromatic ring moieties occurs well below the homothe experimental value would decrease the dielectric constant 577 lumo gap due to large exciton binding energies on the order by less than 15%. Since we do not have accurate band gap 578 of electron volts. 84 Benzene, with an optical onset of 4.8 eV PBE+SOC high-frequency dielectric constant as a good ap- 580 PBE0+BSE and GW+BSE calculations, 62,85 has a predicted <sub>581</sub> homo-lumo gap in solution of between 4.5 and 6 eV. <sup>86</sup> Like-<sub>639</sub> the full optical excitation and relaxation process of conjugated wise, imidazole has a range of predicted excitation energies 640 LHOP materials. between 5.61 and 6.96 eV.85 Thus, the interplay between the homo-lumo gap and the optical gap should be carefully considered in further engineering of layered perovskites for interlayer charge separation application. Ideally, the homo-lumo gap can be lowered by adding more conjugated groups such as aromatic rings to the system. For example, layered perovskites with naphthalene groups have been investigated experimentally and have shown signs of exciton energy transfer between perovskite and organic layers. 41,42 Secondly, the orbital overlap between the layers must be improved to increase the amplitude of the inter-layer transition dipole marix elements. Larger overlap could be achieved by including heavier elements, such as chlorine, in the organic layer which has been recently explored experimentally. 36,38,87 Our future studies of such compounds will include organic-PbX<sub>4</sub> ion-projected band structures and densities of states to map the effects of decreased homo-lumo organic gap and organic halogenation. 600

Currently, n = 1 LHOPs with single conjugated rings face challenges as effective solar cell materials but show promise in a wide range of optoelectronic application. Quantum confinement of the perovskite layer increases the gap relative to the 3D HOPs and thus reduces the absorption range of the material in the visible optical spectrum. LHOPs with n > 1 help to decrease the gap,<sup>32</sup> but at the cost of reducing the density of states of, and degree of optical coupling to, the organic lattice. Secondly, minimal  $\pi$ -stacking is observed in these systems, leading to highly localized electron and hole states in the organic layer. This in turn results in a high effective mass, low mobility in the form of incoherent hopping, and large binding energies of electron-hole pairs. Improving  $\pi$ -stacking of the organic conjugated layer in LHOPs is a promising future research direction, to achieve improvements.<sup>88</sup> Recent investigations have also shown that interfacing 2D LHOPs with 3D HOPs can lead to increased photovoltaic efficiency in Snbased systems, opening the intriguing question of whether this can be done with Pb-based systems as well. 89 Besides applications as solar cells, n = 1 layered perovskites have shown promise as light emitters. 90 Resonant coupling between the organic and perovskite layered of n = 1 systems opens the possibility of engineering the emission wavelength and intensity as a function of LHOP stoichiometry. 42,91

It is important to note that everything studied in this manuscript is related purely to absorption in the singlet spin state. Thus, nothing is said about relaxation in the excited state or emission in the explored LHOP systems. Both triplet and singlet energy levels and their post-optical absorption dynamics are fundamental to understanding how organic comounds behave in the excited state. The interplay between perovskite band energies and the organic singlet and triplet states must be understood to determine excited state charge transport, ion dynamics, and recombination in LHOPs with conjugated organic layers. The combination of methods in this work for determining optical absorption properties and methods such as time-dependent density functional theory and 638 molecular dynamics can be used to predict and disentangle

#### ACKNOWLEDGMENTS

The work at Los Alamos National Laboratory (LANL) was supported by the LANL LDRD program (A.J.N., A.D.M, J.L. and S.T.). The work at UIUC work was supported by the National Science Foundation under Grant No. CBET-1437230. A.D.M. acknowledges the DOE-EERE 0001647-1544 grant 647 for this work. This work was done in part at Center for Nonlinear Studies (CNLS) and the Center for Integrated Nanotechnologies CINT), a U.S. Department of Energy and Of-650 fice of Basic Energy Sciences user facility, at LANL. This research used resources provided by the LANL Institutional 652 Computing Program. Calculations were additionally sup-653 ported by the Campus Cluster program at UIUC and this re-654 search is part of the Blue Waters sustained-petascale computing project, which is supported by the National Science Foundation (awards OCI-0725070 and ACI-1238993) and the state of Illinois. Blue Waters is a joint effort of the Univer-658 sity of Illinois at Urbana-Champaign and its National Center 659 for Supercomputing Applications. LANL is operated by Los 660 Alamos National Security, LLC, for the National Nuclear Se-661 curity Administration of the U.S. Department of Energy under 662 contract DE-AC52-06NA25396. J.E. acknowledges financial support from the Institut Universitaire de France.

### COMPUTATIONAL DETAILS

DFT calculations, using the projector-augmented wave method, are 666 performed with the Vienna Ab-Initio Simulation Package (VASP). 92-95 667 The generalized-gradient approximation of Perdew, Burke, and Ernzerhof 668 (PBE)<sup>96</sup> is used to describe exchange and correlation (XC). Kohn-Sham wave 669 functions are expanded into a plane-wave basis with an energy cutoff of 500 670 eV and the Brillouin zone (BZ) is sampled using a Γ-centered  $4 \times 4 \times 2$  k-671 point mesh. With this setup, total energies of the API-PbX4 structures are 672 converged to within 5 meV per formula unit. Equilibrium positions of all atoms, cell volumes, and unit cell parameters are optimized by minimizing the external pressure and Hellman-Feynman forces to below a threshold of  $10^{-2}$ 675 eV/Å using the PBEsol XC functional<sup>97</sup> and an increased plane-wave cutoff 676 of 900 eV. The use of PBEsol is based on previous studies where lattice parameters of hybrid perovskite materials are predicted to high accuracy.<sup>58</sup> The 678 symmetries of the experimentally determined unit cell are preserved in the 679 first-principles atomic position and cell geometry relaxation. Band structures, ion-resolved densities of states (DOS), and ion-resolved optical-absorption spectra are calculated, taking spin-orbit coupling (SOC) into account.<sup>98</sup> The high-frequency dielectric constant  $\varepsilon_{\infty}$  is calculated using density functional perturbation theory on a  $5 \times 5 \times 2$   $\Gamma$ -centered **k**-point mesh for API-PbX<sub>4</sub> (see supplemental material Fig. S1). Band gaps are determined using the 685 Heyd-Scuseria-Ernzerhof (HSE06) hybrid XC functional 99 with a fraction of  $\alpha$ =0.25 exact exchange. Due to the high computational cost of including SOC in hybrid functional calculations, these are performed using a  $2 \times 2 \times 2$  $\Gamma$ -centered **k**-point mesh.

Linear optical response, described by the components of the complex frequency-dependent dielectric tensor  $\varepsilon_2^{\alpha\beta}(\omega)$ , where  $\alpha$  and  $\beta$  are Cartesian coordinates, is computed using the Ehrenreich-Cohen formula: 76,100

$$\varepsilon_{2}^{\alpha\beta}(\omega) = \frac{8\pi^{2}e^{2}}{\Omega} \sum_{cvk} \frac{\langle \phi_{ck} | \hat{p}_{\alpha} | \phi_{vk} \rangle \langle \phi_{vk} | \hat{p}_{\beta} | \phi_{ck} \rangle^{*}}{(\varepsilon_{ck} - \varepsilon_{vk})^{2}} \delta(\varepsilon_{ck} - \varepsilon_{vk} - \hbar\omega) \qquad (1)$$

692 Here,  $\varepsilon_{ck}$  and  $\varepsilon_{vk}$  are the conduction and valence band energies of the single- 724 calculated using the model dielectric function proposed by Cappellini *et al.* 104 particle states at electronic wave vector k, along with their respective Kohn-Sham wave functions  $\phi_{ck}$  and  $\phi_{vk}$ .  $\hat{p}_{B}$  is the Cartesian component of the momentum operator and  $\Omega$  is the volume of the unit cell. We use PBE+SOC Kohn-Sham energies and wave functions and a scissor shift to adjust the en-697 ergies of the conduction bands to the HSE06+SOC band gap (referred to as PBE+SOC+ $\Delta_{HSE06}$ ). The transition-matrix elements in Eq. (1) are computed 698 using the VASP code.76

We also compute the ion- and angular-momentum resolved optical re-700 701 the projection  $p_{lmnk}^N$  of the wave function  $\phi_{nk}$  on a spherical harmonic  $Y_{lm}$  for a given ion N, with m and l being the magnetic and orbital quantum number, respectively. <sup>101</sup> The sum of  $p_{lmnk}^N$  over all N, l, and m equals to one for each wave function  $\phi_{nk}$ . This turns Eq. (1) into:

$$\varepsilon_{2}^{\alpha\beta}(\omega) = \frac{8\pi^{2}e^{2}}{\Omega} \sum_{cvk} \left( \sum_{N,l,m} p_{lmnk}^{N} \right) \frac{\langle \phi_{ck} | \hat{p}_{\alpha} | \phi_{vk} \rangle \langle \phi_{vk} | \hat{p}_{\beta} | \phi_{ck} \rangle^{*}}{(\varepsilon_{ck} - \varepsilon_{vk})^{2}} \delta(\varepsilon_{ck} - \varepsilon_{vk} - \hbar \omega)$$

Restricting the sum in parentheses to certain ions, angular-momentum components, or bands (e.g. n being v or c when resolving valence or conduction states), allows us to compute ion- and angular-momentum resolved optical 708 709 response.

In addition, we study excitonic effects on the dielectric functions of API-710  $PbX_4$  from the solution of the Bethe-Salpeter equation  $(BSE)^{78,102,103}$  for 712 the optical polarization function. The large computational cost of this approach requires us to restrict these calculations to a  $4 \times 4 \times 2$  k-point grid. A small random shift of this grid lifts degeneracies and, on DFT level, allows us 715 to reproduce dielectric functions calculated on a well-converged  $\Gamma$ -centered  $8 \times 8 \times 2$  k-point grid (see supplemental information, Fig. S6). The absorption edges from shifted and well-converged  $\Gamma$ -centered k-point grids disagree 717 by about 100 meV. Converging exciton-binding energies, defined as the dif-719 ference between the lowest optical and the lowest single-particle excitation energies, to high accuracy requires much denser k-point sampling near the 722

725 The dielectric constant used in the model dielectric function is the average of the diagonal components of the high-frequency dielectric tensor  $\varepsilon_{\infty}^{\alpha\beta}$  cal-727 culated by density functional perturbation theory (DFPT) (see supplemental 728 information Tab. S1), representing the average dielectric response of the layered material. It has been extensively shown that the organic and perovskite 130 layers of LHOPs have spatially resolved dielectric constants of  $\approx 2.5$  and 5 731 respectively, <sup>29,30</sup> and thus this work will use the spatially averaged dielec-732 tric constant determined by DFPT as an approximate value. <sup>76</sup> Other methods sponse by weighting the transition-matrix element for a given transition using 733 are available in the literature to handle this spatial variability of the dielec-734 tric constant. <sup>29,80,81</sup> In this work, the BSE is solved as an eigenvalue problem 735 in the Bloch basis 78,103 of the excitonic Hamiltonian, and using the Tamm– 736 Dancoff approximation:

$$H_{cvk}^{c'v'k'} = (\varepsilon_{ck} - \varepsilon_{vk}) \,\delta(cc') \delta(vv') \delta(kk') - W_{cvk}^{c'v'k'} + 2\bar{V}_{cvk}^{c'v'k'}$$
(3)

737 Here, band energies  $\varepsilon_{ck}$  and  $\varepsilon_{vk}$  from the PBE+SOC+ $\Delta_{HSE06}$  level of the-738 ory are used. Non-interacting electron-hole pairs with energies up to 5 eV 739 (applied to the PBE+SOC band structure) are used to compute the excitonic 740 Hamiltonian. These include, in (nv,nc,nk) format: API-PbI4 (112,48,32), <sup>741</sup> API-PbBr4 (110,40,32), and API-PbCl4 (104,32,32). Matrix elements  $W_{cvk}^{c'v}$ 742 of the attractive electron-hole Coulomb potential and  $\bar{V}_{cvk}^{c'v'k'}$  of the local repulsive Coulomb potential are computed using spin-polarized Kohn-Sham wave functions. The eigenvalues  $E^{\lambda}$  of  $H_{cvk}^{c'v'k'}$  describe optical  $\lambda$ th excitation energies, with excitonic states  $A_{cvk}^{\lambda}$  being the eigenvectors, and they can be determined by solving the eigenvalue equation for  $H_{cvk}^{c'v'k'}$ . Dielectric func-747 tions, including excitonic effects, are calculated from the excitonic Hamil-748 tonian in Eq. (3) using a time-propagation technique. <sup>105,106</sup> The rigid band 749 gap shift is added to the diagonal of the excitonic Hamiltonian, increasing 750 the energy window of the excitonic Hamiltonian from 5 eV to  $5+\Delta_{HSE06}$  eV. 751 For the above-mentioned energy window of 5 eV, 5594 time steps of 0.0022 752 per eV are required. The lowest excitation energies are found by applying a band extrema, 78 which is beyond the scope of this study. Hence, estimates 753 conjugate-gradient scheme to iteratively compute the lowest eigenvalues. All for exciton-binding energies reported here have error bars of about 100 meV. 754 these calculations are carried out using the BSE implementation discussed in The screened electron-hole Coulomb interaction W in the BSE kernel is 755 Refs. 78 and 107.

joshua.leveillee@gmail.com

ajneukirch@lanl.gov

756

757

761

762

763

765

766

767

768

769

771

772

777

778

779

789

790

793

794

795

796

798

799

801

802

804

A. Mei, X. Li, L. Liu, Z. Ku, T. Liu, Y. Rong, M. Xu, M. Hu, 758 J. Chen, Y. Yang, M. Grätzel, and H. Han, Science 345, 295 759 (2014).760

M. M. Lee, J. Teuscher, T. Miyasaka, T. N. Murakami, and H. J. 787 Snaith, Science 338, 643 (2012).

R. Sheng, A. Ho-Baillie, S. Huang, S. Chen, X. Wen, X. Hao, and M. A. Green, J Phys Chem C 119, 3545 (2015).

A. Kojima, K. Teshima, Y. Shirai, and T. Miyasaka, Journal of 791 the American Chemical Society 131, 6050 (2009).

J.-H. Im, C.-R. Lee, J.-W. Lee, S.-W. Park, and N.-G. Park, Nanoscale 3, 4088 (2011).

W. S. Yang, J. H. Noh, N. J. Jeon, Y. C. Kim, S. Ryu, J. Seo, and S. I. Seok, Science 348, 1234 (2015). 770

M. A. Green, Y. Hishikawa, E. D. Dunlop, D. H. Levi, 797 J. HohlEbinger, and A. W. HoBaillie, Prog Photovoltaics 26,

<sup>773</sup> J. Luo, J.-H. Im, M. T. Mayer, M. Schreier, M. K. Nazeeruddin, 800 774 N.-G. Park, S. D. Tilley, H. J. Fan, and M. Grätzel, Science 345, 775 776

S. Yakunin, M. Sytnyk, D. Kriegner, S. Shrestha, M. Richter, 803 G. J. Matt, H. Azimi, C. J. Brabec, J. Stangl, M. V. Kovalenko, and W. Heiss, Nat Photonics 9, 444 (2015).

H. Wei, Y. Fang, P. Mulligan, W. Chuirazzi, H.-H. Fang, 806 780 C. Wang, B. R. Ecker, Y. Gao, M. A. Loi, L. Cao, and J. Huang, 807 781

Nat. Photonics 10, 333 EP (2016).

S. Yakunin, L. Protesescu, F. Krieg, M. I. Bodnarchuk. G. Nedelcu, M. Humer, G. De Luca, M. Fiebig, W. Heiss, and M. V. Kovalenko, Nat Commun 6, 8056 EP (2015).

Y. He, L. Matei, H. J. Jung, K. M. McCall, M. Chen, C. C. Stoumpos, Z. Liu, J. A. Peters, D. Y. Chung, B. W. Wessels, M. R. Wasielewski, V. P. Dravid, A. Burger, and M. G. Kanatzidis, Nat Commun, 1609 (2018).

Z.-K. Tan, R. S. Moghaddam, M. L. Lai, P. Docampo, R. Higler, F. Deschler, M. Price, A. Sadhanala, L. M. Pazos, D. Credgington, F. Hanusch, T. Bein, H. J. Snaith, and R. H. Friend, Nat Nanotechnol 9, 687 EP (2014).

J. Even, L. Pedesseau, J.-M. Jancu, and C. Katan, J. Phys. Chem. Lett. 4, 2999 (2013).

<sup>15</sup> M. Kepenekian and J. Even, J. Phys. Chem. Lett. 8, 3362 (2017). X. Hu, X. Zhang, L. Liang, J. Bao, S. Li, W. Yang, and Y. Xie, Advanced Functional Materials 24, 7373 (2014).

M. Espinosa, Nieves, L. Serrano-Lujan, A. Urbina, and F. C. Krebs, Sol Energ Mat Sol C 137, 303 (2015).

B. Hailegnaw, S. Kirmayer, E. Edri, G. Hodes, and D. Cahen, J. Phys Chem Lett 6, 1543 (2015).

J. Gong, S. B. Darling, and F. You, Energy Environ. Sci. 8, 1953

A. Babayigit, A. Ethirajan, M. Muller, and B. Conings, Nat Mater 15, 247 EP (2016).

P.-Y. Chen, J. Qi, M. T. Klug, X. Dang, P. T. Hammond, and

875

881

882

906

910

913

914

922

923

924

925

926

929

931

932

933

934

A. M. Belcher, Energy Environ. Sci. 7, 3659 (2014).

808

811

812

826

827

828

829

830

831

832

833

836

837

841

842

844

- L. Li, G. Qi, C. Yuan, Y. Sun, X. Lei, H. Xu, and Y. Wang, 809 Energy Environ. Sci. 8, 1616 (2015). 810
  - W. Huang, J. S. Manser, P. V. Kamat, and S. Ptasinska, Chemistry of Materials 28, 303 (2016).
- W. Nie, J.-C. Blancon, A. J. Neukirch, K. Appavoo, H. Tsai, 877 813 M. Chhowalla, M. A. Alam, M. Y. Sfeir, C. Katan, J. Even, 878 814 S. Tretiak, J. J. Crochet, G. Gupta, and A. D. Mohite, Nat Com-815 mun 7, 11574 EP (2016). 816
- A. J. Neukirch, W. Nie, J.-C. Blancon, K. Appavoo, H. Tsai, 817 M. Y. Sfeir, C. Katan, L. Pedesseau, J. Even, J. J. Crochet, 818 G. Gupta, A. D. Mohite, and S. Tretiak, Nano Lett 16, 3809 819 820
- E. L. Lucas and E. R. Jarvo, Accounts Chem Res **51**, 567 (2018). 821
- J. Zhou, Y. Chu, and J. Huang, ACS Applied Materials & Inter-822 faces 8, 25660 (2016). 823
- J. Even, L. Pedesseau, and C. Katan, Chem Phys Chem 15, 3733 824 825
  - L. Pedesseau, D. Sapori, B. Traore, R. Robles, H.-H. Fang, M. A. 890 Loi, H. Tsai, W. Nie, J.-C. Blancon, A. Neukirch, S. Tretiak, 891 A. D. Mohite, C. Katan, J. Even, and M. Kepenekian, ACS Nano 10, 9776 (2016).
  - B. Traore, L. Pedesseau, L. Assam, X. Che, J.-C. Blancon, 894 H. Tsai, W. Nie, C. C. Stoumpos, M. G. Kanatzidis, S. Tretiak, 895 A. D. Mohite, J. Even, M. Kepenekian, and C. Katan, ACS Nano **12**, 3321 (2018).
- J. Even, L. Pedesseau, J. Jancu, and C. Katan, Phys Status Solidi 898 834 - R 8, 31 (2014). 835
- H. Tsai, W. Nie, J.-C. Blancon, C. C. Stoumpos, R. Asadpour, 900 B. Harutyunyan, A. J. Neukirch, R. Verduzco, J. J. Crochet, 901 S. Tretiak, L. Pedesseau, J. Even, M. A. Alam, G. Gupta, J. Lou, 902 838 P. M. Ajayan, M. J. Bedzyk, M. G. Kanatzidis, and A. D. Mo-839 hite, Nature **536**, 312 (2016). 840
  - M. D. Smith and H. I. Karunadasa, Accounts of Chemical Research **51**, 619 (2018).
- N. Kawano, M. Koshimizu, Y. Sun, N. Yahaba, Y. Fujimoto, 907 843 T. Yanagida, and K. Asai, J Phys Chem C 118, 9101 (2014).
- S. N. Ruddlesden and P. Popper, Acta. Crystallogr. 11, 54 (1958). 845
- <sup>36</sup> G. Papavassiliou, Prog Solid State Ch **25**, 125 (1997). 846
- 37 D. B. Mitzi, "Synthesis, structure, and properties of organicinor-911 847 ganic perovskites and related materials," in Progress in Inorganic 912 848 Chemistry (Wiley-Blackwell, 2007) pp. 1–121. 849
- N. Mercier, N. Louvain, and W. Bi, Cryst Eng Comm 11, 720 850 (2009).851
- J.-C. Blancon, H. Tsai, W. Nie, C. C. Stoumpos, L. Pedesseau, 916 852 C. Katan, M. Kepenekian, C. M. M. Soe, K. Appavoo, M. Y. 917 853 Sfeir, S. Tretiak, P. M. Ajayan, M. G. Kanatzidis, J. Even, J. J. 918 854 Crochet, and A. D. Mohite, Science 355, 1288 (2017). 855
- M. Braun, W. Tuffentsammer, H. Wachtel, and H. Wolf, Chem 920 856 Phys Lett 307, 373 (1999). 857
- M. Era, K. Maeda, and T. Tsutsui, Chem. Phys. Lett. 296, 417 858 (1998).859
- K. Ema, M. Inomata, Y. Kato, H. Kunugita, and M. Era, Phys. 860 Rev. Lett. 100, 257401 (2008). 861
- B. A. Gregg, J Phys Chem B 107, 4688 (2003). 862
- R. H. Friend, R. W. Gymer, A. B. Holmes, J. H. Burroughes, 927 863 R. N. Marks, C. Taliani, D. D. C. Bradley, D. A. D. Santos, J. L. 928 864 Brédas, M. Lögdlund, and W. R. Salaneck, Nature 397, 121 EP 865 866
- L. Rothberg, M. Yan, F. Papadimitrakopoulos, M. Galvin, 867 E. Kwock, and T. Miller, Synthetic Met 80, 41 (1996). 868
- N. C. Greenham, X. Peng, and A. P. Alivisatos, Phys. Rev. B 54, 869 17628 (1996). 870
  - Y. Y. Li, C. K. Lin, G. L. Zheng, Z. Y. Cheng, H. You, W. D. 935

- Wang, and J. Lin, Chem. Mater. 18, 3463 (2006).
- P. Umari, E. Mosconi, and F. De Angelis, Scientific Reports 4, 4467 (2014).
- J. Yin, H. Li, D. Cortecchia, C. Soci, and J.-L. Brdas, ACS Energy Letters 2, 417 (2017).
- D. Cortecchia, J. Yin, A. Bruno, S.-Z. A. Lo, G. G. Gurzadyan, S. Mhaisalkar, J.-L. Bredas, and C. Soci, J. Mater. Chem. C 5, 2771 (2017).
- M. D. Smith, A. Jaffe, E. R. Dohner, A. M. Lindenberg, and H. I. Karunadasa, Chem. Sci. 8, 4497 (2017).
- L. Mao, Y. Wu, C. C. Stoumpos, B. Traore, C. Katan, J. Even, M. R. Wasielewski, and M. G. Kanatzidis, J Am Chem Soc 139, 11956 (2017).
- K.-z. Du, Q. Tu, X. Zhang, Q. Han, J. Liu, S. Zauscher, and D. B. Mitzi, Inorg Chem 56, 9291 (2017).
- M. S. Hybertsen and S. G. Louie, Phys. Rev. B 34, 5390 (1986).
- D. G. Billing, Acta Crystallogr E 58, m669 (2002).
- K. Shibuya, M. Koshimizu, F. Nishikido, H. Saito, and S. Kishimoto, Acta Crystallogr E 65, m1323 (2009).
- 57 Journal of Solid State Chemistry 145, 694 (1999).
- F. Brivio, J. M. Frost, J. M. Skelton, A. J. Jackson, O. J. Weber, M. T. Weller, A. R. Goñi, A. M. A. Leguy, P. R. F. Barnes, and A. Walsh, Phys. Rev. B 92, 144308 (2015).
- A. Fraccarollo, V. Cantatore, G. Boschetto, L. Marchese, and M. Cossi, J Chem Phys, 164701 (2016).
- B. Joseph, B. Tonio, E. D. A., H. Gary, K. Leeor, L. YuehLin, 897 L. Igor, M. S. R., M. Yitzhak, M. J. S., M. D. B., P. Yaron, R. A. M., R. Ilan, R. Boris, S. Oscar, S. Vladan, T. M. F., Z. David, K. Antoine, G. David, and C. David, Adv Mater 27, 5102 (2015).
  - W. Martin, A. Musgrove, J. Kotochigova, and J. Sansonetti, National Institute of Standards and Technology (2013).
- T. Inagaki, J Chem Phys 57, 2526 (1972). 904
- N. S. Rytova, Moscow University Physics Bulletin 30, 1 (1967). 905
  - L. V. Keldvsh, JEPT Letters 29, 658 (1979).
  - E. Hanamura, Phys. Rev. B 38, 1228 (1988).
- T. Ishihara, J. Takahashi, and T. Goto, Phys. Rev. B 42, 11099 908 (1990).909
  - T. Ishihara, J. Takahashi, and T. Goto, Solid State Communications 69, 933 (1989).
  - I. B. Koutselas, L. Ducasse, and G. C. Papavassiliou, Journal of Physics: Condensed Matter 8, 1217 (1996).
  - M. A. Pérez-Osorio, R. L. Milot, M. R. Filip, J. B. Patel, L. M. Herz, M. B. Johnston, and F. Giustino, J. of Phys. Chem. C 119, 25703 (2015).
  - M. Sendner, P. K. Nayak, D. A. Egger, S. Beck, C. Mller, B. Epding, W. Kowalsky, L. Kronik, H. J. Snaith, A. Pucci, and R. Lovrini, Mater. Horiz. 3, 613 (2016).
  - M. Bokdam, T. Sander, A. Stroppa, S. Picozzi, D. D. Sarma, C. Franchini, and G. Kresse, Sci Rep - UK 6, 28618 EP (2016).
  - K. Galkowski, A. Mitioglu, A. Miyata, P. Plochocka, O. Portugall, G. E. Eperon, J. T.-W. Wang, T. Stergiopoulos, S. D. Stranks, H. J. Snaith, and R. J. Nicholas, Energy Environ. Sci. **9**, 962 (2016).
  - J. Even, L. Pedesseau, and C. Katan, J Phys Chem C 118, 11566 (2014).
  - A. Miyata, A. Mitioglu, P. Plochocka, O. Portugall, J. T.-W. Wang, S. D. Stranks, H. J. Snaith, and R. J. Nicholas, Nat Phys 11, 582 EP (2015).
  - T. Ishihara, J Lumin 61, 269 (1994).
  - M. Gajdoš, K. Hummer, G. Kresse, J. Furthmüller, and F. Bechstedt, Phys. Rev. B 73, 045112 (2006).
  - M. J. Frisch, G. W. Trucks, H. B. Schlegel, G. E. Scuseria, M. A. Robb, J. R. Cheeseman, G. Scalmani, V. Barone, G. A. Peters-

992

993

997

son, H. Nakatsuji, X. Li, M. Caricato, A. V. Marenich, J. Bloino, 975 B. G. Janesko, R. Gomperts, B. Mennucci, H. P. Hratchian, 976 J. V. Ortiz, A. F. Izmaylov, J. L. Sonnenberg, D. Williams- 977 Young, F. Ding, F. Lipparini, F. Egidi, J. Goings, B. Peng, 978 A. Petrone, T. Henderson, D. Ranasinghe, V. G. Zakrzewski, 979 J. Gao, N. Rega, G. Zheng, W. Liang, M. Hada, M. Ehara, 980 K. Toyota, R. Fukuda, J. Hasegawa, M. Ishida, T. Nakajima, 981 942 Y. Honda, O. Kitao, H. Nakai, T. Vreven, K. Throssell, J. A. 982 Montgomery, Jr., J. E. Peralta, F. Ogliaro, M. J. Bearpark, J. J. Heyd, E. N. Brothers, K. N. Kudin, V. N. Staroverov, T. A. 945 Keith, R. Kobayashi, J. Normand, K. Raghavachari, A. P. Rendell, J. C. Burant, S. S. Iyengar, J. Tomasi, M. Cossi, J. M. Millam, M. Klene, C. Adamo, R. Cammi, J. W. Ochterski, R. L. 948 Martin, K. Morokuma, O. Farkas, J. B. Foresman, and D. J. Fox, 949 "Gaussian 16 Revision B.01," (2016), gaussian Inc. Wallingford 950

936

937

938

939

940

941

943

944

946

947

951

952

953

954

955

956

957

958

959

960

961

962

964

973

974

- F. Fuchs, C. Rödl, A. Schleife, and F. Bechstedt, Phys. Rev. B **78**, 085103 (2008).
- Q. Wang, X.-D. Liu, Y.-H. Qiu, K. Chen, L. Zhou, and Q.-Q. Wang, AIP Advances 8, 025108 (2018).
- E. A. Muljarov, S. G. Tikhodeev, N. A. Gippius, and T. Ishihara, Phys. Rev. B 51, 14370 (1995).
- S.-L. Chuang, S. Schmitt-Rink, D. A. B. Miller, and D. S. Chemla, Phys. Rev. B 43, 1500 (1991).
- J. C. Blancon, A. V. Stier, H. Tsai, W. Nie, C. C. Stoumpos, B. Traoré, L. Pedesseau, M. Kepenekian, F. Katsutani, G. T. Noe, 1000 J. Kono, S. Tretiak, S. A. Crooker, C. Katan, M. G. Kanatzidis, 1001 J. J. Crochet, J. Even, and A. D. Mohite, Nature Communica- 1002 tions 9, 2254 (2018).
- M. D. Smith, L. Pedesseau, M. Kepenekian, I. C. Smith, 1004 965 C. Katan, J. Even, and H. I. Karunadasa, Chem. Sci. 8, 1960 1005 966 1006 967
- M. L. Tiago, J. E. Northrup, and S. G. Louie, Phys. Rev. B 67, 1007 968 115212 (2003). 1008 969
- D. Jacquemin, I. Duchemin, and X. Blase, J Chem Theory Comp 1009 970 11, 3290 (2015), pMID: 26207104. 971 1010
- The Journal of Chemical Physics (2013), computational 1011 972 Chemistry Comparison and Benchmark Data Base from Na- 1012 tional Institute of Standards and Technology available at 1013

- https://cccbdb.nist.gov/gap1.asp.
- O. J. Weber, K. L. Marshall, L. M. Dyson, and M. T. Weller, Acta. Crystallogr. B 71, 668 (2015).
- T. S. van der Poll, A. Zhugayevych, E. Chertkov, R. C. Bakus, J. E. Coughlin, S. J. Teat, G. C. Bazan, and S. Tretiak, J Phys Chem Lette 5, 2700 (2014), pMID: 26277966.
- S. Shao, J. Liu, G. Portale, H.-H. Fang, G. R. Blake, G. H. ten Brink, L. J. A. Koster, and M. A. Loi, Advanced Energy Materials 8, 1702019 (2017).
- X. Yang, X. Zhang, J. Deng, Z. Chu, Q. Jiang, J. Meng, P. Wang, L. Zhang, Z. Yin, and J. You, Nat Comm 9, 570 (2018).
- K. Jemli, P. Audebert, L. Galmiche, G. Tripp-Allard, D. Garrot, J.-S. Lauret, and E. Deleporte, ACS Appl. Mater. Interfaces 7, 21763 (2015), pMID: 26340054.
- G. Kresse and J. Hafner, Phys. Rev. B 47, 558 (1993).
- G. Kresse and J. Furthmller, Comp. Mater. Sci. 6, 15 (1996).
- G. Kresse and J. Furthmüller, Phys. Rev. B 54, 11169 (1996).
- G. Kresse and D. Joubert, Phys. Rev. B 59, 1758 (1999).
- J. P. Perdew and Y. Wang, Phys. Rev. B 45, 13244 (1992).
- J. P. Perdew, A. Ruzsinszky, G. I. Csonka, O. A. Vydrov, G. E. Scuseria, L. A. Constantin, X. Zhou, and K. Burke, Phys. Rev. Lett. 100, 136406 (2008).
- 98 J. Even, L. Pedesseau, M.-A. Dupertuis, J.-M. Jancu, and C. Katan, Phys. Rev. B 86, 205301 (2012).
- A. V. Krukau, O. A. Vydrov, A. F. Izmaylov, and G. E. Scuseria, J. Chem. Phys. 125, 224106 (2006).
- 100 H. Ehrenreich and M. H. Cohen, Phys. Rev. 115, 786 (1959).
- G. Kresse, M. Marsman, and Furthmüller, (2016), vASP Manual, available at http://cms.mpi.univie.ac.at/vasp/vasp/vasp.html.
- E. E. Salpeter and H. A. Bethe, Phys. Rev. 84, 1232 (1951).
- M. Rohlfing and S. G. Louie, Phys. Rev. B 62, 4927 (2000).
- G. Cappellini, R. Del Sole, L. Reining, and F. Bechstedt, Phys. Rev. B 47, 9892 (1993).
- P. H. Hahn, W. G. Schmidt, and F. Bechstedt, Phys. Rev. Lett. **88.** 016402 (2001).
- W. G. Schmidt, S. Glutsch, P. H. Hahn, and F. Bechstedt, Phys. Rev. B 67, 085307 (2003).
- C. Rödl, F. Fuchs, J. Furthmüller, and F. Bechstedt, Phys. Rev. B 77, 184408 (2008).