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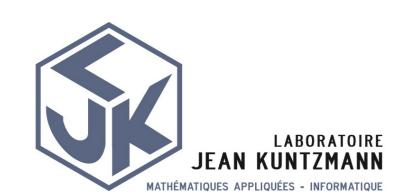
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A COMPARISON OF METHODS FOR ANALYSING LOGISTIC REGRESSION MODELS WITH BOTH CLINICAL AND GENOMIC VARIABLES

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-INTRODUCTION

- An active field in today medical research: prediction from high-dimensional genomic data
- → Number of samples relatively small compared to the number of covariates
- \rightarrow Collinear measurements
- ⇒ Use of reduction dimension methods
 - Traditional approach: Principal Component Regression (PCR) [10]
 - Most useful: Partial Least Square (PLS) [6]
- Most of this studies included clinical data in addition to genomic data
- However most of the proposed prediction methods used only genomic data
- Recent studies consider situations combining both type of covariates improving predictions
- → Development of Clinico-genomic models
- \rightarrow For survival prediction with Cox model's [3], for classification of patients [2]
- ⇒ Few of them used dimension reduction or applied dimension reduction only to the high-dimensional genomic variables
- Recently, prediction method have been proposed to combine both type of covariates [7]
- Developed only in regression Gaussian context
- * Method based on combination of PLS and ordinary least square (OLS)=> LS-PLS
- ⇒ More information from the experiment
- ⇒ Lower variance in the parameter estimates
- Adaptation to logistic regression model
- Not relevant to combine both type of variables without reduction dimension
- -An alternative \rightarrow compress the information from genomic data into new few components before modelling
- * Partial Least Squares (PLS) adapted to logistic regression [11, 9, 4, 1]

OBJECTIVES

- To adapt LS-PLS to combine clinical and genomic variables for logistic regression model
- To perform a comparison by simulation of the performance of these approaches

LS-PLS FOR LOGISTIC REGRESSION

• Linear Logistic Discrimination

- -Y: binary response variable $\{0,1\}^n$
- -D: matrix of clinical variables of size $n \times q$
- -X: design matrix for expression levels of the p genes for the n microarray samples
- $*X = (x_{ij}), 1 \le i \le n, 1 \le j \le p$
- General statistical model
- * The conditional expectation of y_i given D_i , given by $\pi_i = P(y_i = 1 | D_i)$
- * Related to linear predictor $\eta_i = [1; d_i] \gamma$
- with $\gamma \in \mathbb{R}^{q+1}$ and the non-linear relation $\pi_i = h(\eta_i)$
- where $h(\eta_i) = 1/(1 + \exp(-\eta_i))$
- Estimation of γ by maximum likelihood (ML) estimation method
- Use of Iteratively Reweighted Least Squares (IRLS) algorithm [5]

$$z^{(t)} = \tilde{D}\gamma^{(t)} + \left[W(\gamma^{(t)})^{(t)}\right]^{-1} \left(y - \pi^{(t)}\right),$$

$$\gamma^{(t+1)} \Leftarrow weighted \ regression \ by \ W(\gamma^{(t)})^{(t)} \ of \ z^{(t)} \ on \ \tilde{D}$$

$$(2)$$

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(2)

where $\tilde{D} = [1_n \ D], \ 1_n = (1, \cdots, 1)^T$

 $W(\gamma^{(t)})$ the diagonal $n \times n$ matrix with entries $W_{i,i}(\gamma) = \pi_k(1 - \pi_k)$.

• LS-PLS in Gaussian context [7]

- Iterative procedure
- 1. Perform ordinary least squares regression of Y on (D) and estimate the regression coefficients β and calculate residuals.
- 2. Perform PLS regression of the residuals on centred X and combine the design (D)
- 3. Perform OLS regression on the combined matrix design (D) and the score T to predict Y.
- 4. Calculate the predicted \hat{y} based on (D) and calculate new residuals.
- 5. Repeat steps 2 to 4 until convergence.
- \Rightarrow Method denoted LS-PLS (y, D, X, κ) where κ the PLS component number

• Some extensions for logistic regression

- NGUYEN and ROCKE's APPROACH [11]
- * Extension of PLS to logistic regression substituting X by a $n \times \kappa$ matrix T
 - · Columns of which are the first κ PLS-scores given by PLS regression of y on X• Estimation of the parameter with ML with IRLS(y, T).
- ⇒ Replace PLS by LS-PLS
- $\Rightarrow \kappa$ obtained by cross-validation
- \Rightarrow Method denoted LS-PLS.
- MARX's APPROACH [9]
- * Estimation of the parameter γ with ML using IRLS(y,T) algorithm
- * Where T defined by IRPLS, an algorithm that extends PLS to generalized linear models
- * Matrix T collects the first κ components "at convergence" of IRPLS
- ⇒ Replace PLS by LS-PLS to adopt this approach for LS-PLS
- $\Rightarrow \kappa$ obtained by cross-validation
- \Rightarrow Method denoted LS-PLS-irls.
- RIDGE PARTIAL LEAST SQUARES APPROACH [4]
- * Replace binary by a pseudo-response variable $z^{\inf} \leftarrow$ linear relationship with the covariates · At convergence of IRLS algorithm : $z^{\inf} = X\hat{\gamma}^R + \varepsilon$
- $\hat{\gamma}^R$: the true value of the parameter
- $\cdot \varepsilon$ a centered vector of covariance matrix $(W^{\inf})^{-1}$.
- * When $n \ll p \to \text{Regularisation}$ methods as Ridge Penalty with λ the shrinkage parameter [8] * Extension with LS-PLS

⇒ Method called R-LS-PLS

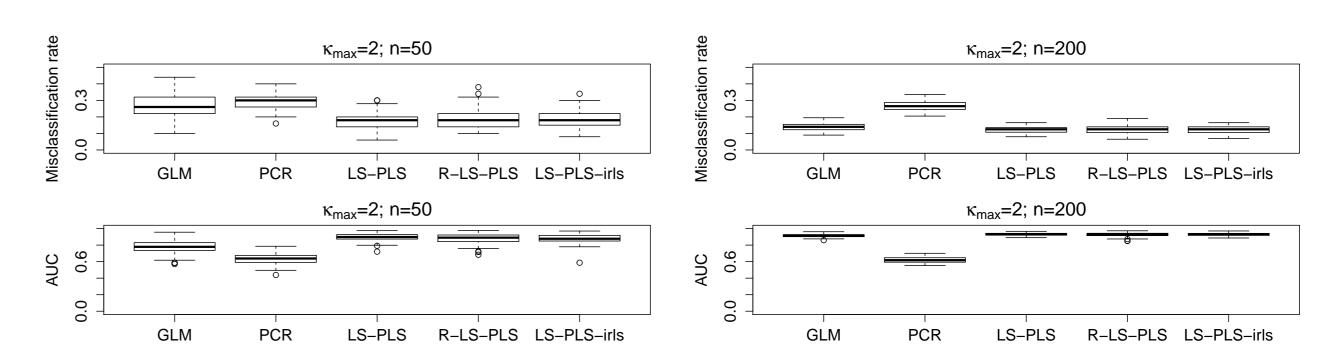
- \Rightarrow R-LS-PLS depends on two parameters : λ and κ obtained by cross-validation.
- BASTIEN's APPROACH [1]
- * Not developed at the moment

SIMULATION STUDY - A "STANDARD" EXAMPLE

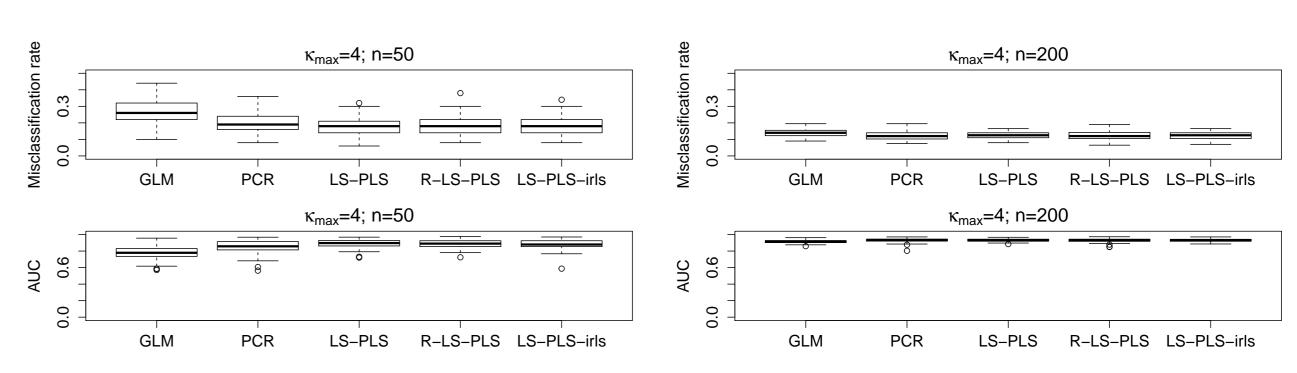
Methods

- -Simulation framework (R software)
- * Simulation of 100 data sets of size n (learning set=100 and test set = 100)
- * Statistical model
- · For an individual i $(i = 1, ..., n), y_i \sim \mathcal{B}(\pi_i)$
- $\beta_X = \{\{0\}^8, \{2\}^8\} \text{ and } \beta_D = \{0.5\}^4 \ (p = 16 \text{ and } q = 4)$
- · X such as $X=(X^1,X^2,X^3,X^4)$ where $X^k\sim N(0_4,\Sigma_X^k)$ with $\Sigma_{i,j}^k=c^k\rho^{|i-j|}$ with $k=1,...4,\ i=1,...,4,\ j=1,...,4$ where $c^1=8,\ c^2=4,\ c^3=2,\ c^4=1$ and $\rho=0.9999$
- $D \sim N(0_q, \Sigma_D)$ with $\Sigma_D = \rho^{\{|i-j|\}}$ with i = 1, ..., q and j = 1, ..., q and $\rho = 0.5$
- -Comparison of the different prediction methods to analyse both X and D matrices:
- * 1) GLM 2) PCR on X then GLM on $[DX_{PCR}]$ 3) LS-PLS 4) LS-PLS-irls 5) R-LS-PLS * Choice for hyperparameters:
- $\cdot \kappa$ (for all approaches) obtained by cross-validation over a grid 1 to κ_{max} (for $\kappa_{max} = 2.4, 8$)
- $\cdot \lambda$ (for R-LS-PLS) obtained by cross-validation
- *n = 50,200
- * Criterion of comparison
- · Computation of AUC and Missclassification rate errror for each method

• Results



- No optimal conditions for PCR \rightarrow Poor performance especially when n increase
- -Similar comportment for GLM only when n=50
- ⇒ Relevance of method using reduction
- -Closed distribution of Missclassification rate and AUC for new approaches and GLM when n=200



- -Slightly poor performance of GLM when n = 50
- $-\Rightarrow$ Correct and closed distribution of missclassification rate and AUC when n and κ increase
- \Rightarrow Relevance of all the approaches as well as PCR

 \Rightarrow Need further exploration

Comput., 17(2):581–607, 1988.

CONCLUSION

- Comparison by simulation of prediction methods developed for logistic regression model to analyse both clinical and genomic data based on LS-PLS approach
- Poor performance of GLM compared to other approaches especially n small
- -Similar relevance for proposed extensions of LS-PLS and PCR with ideal number of components ⇒ Interest of reduction even if reasonable case of "high dimensional" case
- ⇒ Need of extensive simulations to explore high-dimensional situations
- Some applications of these approaches to real data without relevant results
- Extension of LS-PLS approach to survival prediction model Cox'models

REFERENCES

- [1] P. Bastien, V. E. Vinzi, and M. Tenenhaus. PLS generalised linear regression. Computational Statistics & Data Analysis, 48(1):17–46, January 2005.
- [2] A.-L. Boulesteix and W. Sauerbrei. Added predictive value of high-throughput molecular data to clinical data and its validation. Briefings in Bioinformatics, 12(3):215–229, 2011.
- [3] N. S. Bovelstad H.M and B. O. Survival prediction from clinico-genomic models—a comparative study. BMC Bioinformatics, 10(413), 2009.
- [4] G. Fort and S. Lambert-Lacroix. Classification using partial least squares with penalized logistic regression. *Bioinformatics*, 21(7):1104–1111, 2005.
- and resistant alternatives. Journal of the Royal Statistical Society, B, 46(2):149–192, 1984. [6] I. Helland. On the structure of Partial Least Squares Regression. Commun. Stat., Simulation

[5] P. J. Green. Iteratively reweighted least squares for maximum likelihood estimation and some robust

- [7] K. T. K. Jorgensen, V. Segtnan and T. Naes. A comparison of methods for analysing regression models with both spectral and designed variables. Journal of Chemometrics, 18:451–464, 2004.
- [8] S. Le Cessie and J. Van Houwelingen. Ridge estimators in logistic regression. J. R. Stat. Soc., Ser. C, 41(1):191–201, 1992.

[9] B. D. Marx. Iteratively Reweighted Partial Least Squares estimation for Generalized Linear Regres-

- sion. Technometrics, 38(4):374–381, 1996. [10] W. F. Massy. Principal components regression in exploratory statistical research. J. Amer. Stat.
- Assoc., 60:234–246, 1965. [11] D. Nguyen and D. Rocke. Tumor classification by Partial Least Squares using microarray gene expression data. Bioinformatics, 18(1):39–50, 2002.