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Experimental investigation of water distribution in a two-phase zone during gravity-dominated evaporation

Cesare M. Cejas,^{1,*} Jean-Christophe Castaing,² Larry Hough,¹ Christian Frétigny,³ and Rémi Dreyfus¹

¹*Complex Assemblies of Soft Matter, CNRS-Solvay-UPenn UMI 3254, Bristol, Pennsylvania 19007-3624, USA*

²*Solvay Research and Innovation Centre, Aubervilliers, France 93300*

³*Sciences et Ingénierie de la Matière Molle CNRS SIMM UMR 7615 ESPCI, Paris, France 75005*

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We characterize the water repartition within the partially saturated (two-phase) zone (PSZ) during evaporation from mixed wettable porous media by controlling the wettability of glass beads, their sizes, and as well the surrounding relative humidity. Here, capillary numbers are low and under these conditions, the percolating front is stabilized by gravity. Using experimental and numerical analyses, we find that the PSZ saturation decreases with the Bond number, where packing of smaller particles have higher saturation values than packing made of larger particles. Results also reveal that the extent (height) of the PSZ, as well as water saturation in the PSZ, both increase with wettability. We also numerically calculate the saturation exclusively contained in connected liquid films and results show that values are less than the expected PSZ saturation. These results strongly reflect that the two-phase zone is not solely made up of connected capillary networks but also made of disconnected water clusters or pockets. Moreover, we also find that global saturation (PSZ + full wet zone) decreases with wettability, confirming that greater quantity of water is lost via evaporation with increasing hydrophilicity. These results show that connected liquid films are favored in more-hydrophilic systems while disconnected water pockets are favored in less-hydrophilic systems.

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I. INTRODUCTION

Evaporation from porous media such as soil involves complex mechanisms that enable water flow across liquid-air interfaces in the pores. These liquid networks control the rigidity of porous materials [1], as well as the total amount of water that plants can extract from the soil [2,3]. Evaporation affects energy balance and involves phase changes and fluid displacement [4] at pore scales, thereby providing different levels of challenges when predicting evaporation using theoretical models [5]. The challenges are due to the different mechanisms involved at the pore scale level, such as pore impregnation and drying [6], liquid flows due to pore size distributions [5,7], and flows due to local gradients of temperature [8]. Because of this inherent complexity, several models and experimental approaches have been established to analyze evaporation, such as pore-network models [9,10] and silica spheres sandwiched between glass slides [4].

Experimental studies on evaporation have been commonly performed in two dimensions (2D) for simplicity and reproducibility [11,12]. The morphology of the front and the dynamics of the liquid films during evaporation are affected by a competition among viscous, capillary, and gravity forces [11–13]. Some studies have probed the effect of reduced gravity conditions on front dynamics and the fluid displacement patterns by using parabolic flight experiments [14] or tilting the sample cell at an angle relative to the direction of gravity [12]. Notable studies have also focused on the drying front [13] and the fractal formation that accompanies it [11,15,16]. Most

evaporation experiments have been devoted to measuring and predicting the extent or depth of the capillary film network in the two-phase zone [12,13], which links the fully wet region and the evaporating surface [11], arguing that comprehension of the capillary film network would be useful for numerous applications. For instance, recent results used evaporation principles on the prediction of total mass loss from combined evapotranspiration fluxes for root growth applications [3]. Some drying studies have also coupled experiments with numerical simulations [17].

Prediction of the extent of the liquid film region has already been largely studied using various models. However, what still remains an area of interest is the water repartition within the partially saturated (two-phase) zone (PSZ), also referred to as unsaturated zone [13] or vadose zone [18] in the literature. The PSZ is a dynamic air-water mixture formed by saturated pores, liquid bridges, and films that coalesce to form networks, which establish hydraulic connections inside the porous medium [19]. The negative curvature of the water-air menisci in these films [20] mean that they are subject to intense pressure that play a crucial role in fluid transport mechanisms, including having an impact on infiltration [21] and groundwater recharge [18]. Experimental evidence has revealed that some liquid films are indeed disconnected from the principal network and thus form isolated water clusters or pockets [11,13]. Although these isolated clusters have been qualitatively observed in experiments [5,11,13], our understanding of the evaporation process would benefit from the analysis of the water content repartition within the two-phase zone, i.e., the quantity of water contained in continuous liquid films and those contained in disconnected isolated pockets. Such information will not just contribute to our comprehension of evaporation dynamics but it will help improve applications in soil additive design [22,23].

In this paper, we present an experimental investigation of evaporation from a 2D porous medium that consists of a

*Present address: Microfluidics, MEMS, Nanostructures Laboratory, CNRS Gulliver UMR 7083, Institut Pierre Gilles de Gennes (IPGG), ESPCI Paris, PSL Research University, 6 rue Jean Calvin 75005 Paris, France.

monolayer stack of monodisperse beads inside a Hele-Shaw cell. We study evaporation using well-controlled experimental conditions including different relative humidities, sizes of glass beads, and mixtures of particles with varying wettability. The primary objective is to estimate the general repartition and saturation of water within the PSZ subject to gravity. We find evidence of a complex coexistence of connected capillary networks and disconnected water clusters or pockets, where the quantity of the latter dominates during later evaporation times and in less-hydrophilic media. We find that the saturation of the PSZ is a function of the Bond number, where packing of smaller particles (lower Bond number) have higher saturation values. From these scalings, we extract information on total saturation in the two-phase zone. By comparing total PSZ saturation values to the saturation exclusively contained in continuous films, we obtain the amount of water contained in isolated pockets. We find that for different wetting conditions, the increase in hydrophobicity in the porous medium is generally accompanied by an increase in the amount of water in isolated pockets.

II. MATERIALS AND METHODS

A. Cell preparation

We perform experiments in Hele-Shaw cells constructed by putting together two glass sheets (Peerless Store and Glass, PA) of 15 cm in length and 10 cm in width. The thickness of the cell is the diameter of the beads, $e = d = 2R$. Because of the silicon needed to glue the sheets together, the effective size of the medium becomes 13.5 cm in length and 7.5 cm width. The glass sheets are coated with hydrophobic silane solution (OMS Chemicals, Canada) to reduce wetting effects. When oriented vertically, only the top of the cell is left unsealed. Once dry, the cells are filled with glass beads forming a monolayer. We study two different glass bead diameters: $d_1 = 0.5 \pm 0.1$ mm (soda lime, MO-SCI) and $d_2 = 1.0 \pm 0.1$ mm (borosilicate, Sigma-Aldrich). For each experiment, we measure the cross section of the cell, S . The thickness of the Hele-Shaw cell is $e_1 = 0.53 \pm 0.05$ mm and $e_2 = 1.1 \pm 0.1$ mm. As a result, our system is quasi-2D.

We use deionized water, whose properties are shown in Table I. The porosity of the medium, ϕ , is experimentally measured for the entire cell using standard imbibition method. This method involves measuring the following mass quantities: empty cell (m_{empty}), cell with beads (m_{beads}), cell with water (m_{water}), and cell with both beads and water (m_{all}). The porosities, ϕ , are deduced from: $\phi = (m_{\text{all}} - m_{\text{beads}})/(m_{\text{water}} - m_{\text{empty}})$. The average porosities for d_1 and d_2 are $\phi_1 = 0.63 \pm 0.02$ and $\phi_2 = 0.53 \pm 0.02$, respectively.

TABLE I. Properties of water at $T = 25^\circ\text{C}$

Quantity	Symbol	Unit	Value
Diffusion of water in air	D_M	m^2/s	2.5×10^{-5}
Diffusion of water in porous medium	D_{eff}	m^2/s	$D_M \phi^{1.5}$
Liquid density	ρ	kg/m^3	1000
Surface tension	σ	mN/m	73

TABLE II. Equivalent contact angle of porous media mixture, α , of $\theta_1 = 16 \pm 5^\circ$ and $\theta_2 = 82 \pm 4^\circ$.

α	0	0.25	0.50	0.75	1
θ_{equ} (deg)	82	68.6	56.2	41.6	16

B. Surface treatment

We use a heterogeneous mixture, α , of glass beads of two different wettabilities, characterized by contact angles: (1) more hydrophilic, $\theta_1 = 16 \pm 5^\circ$, for glass beads washed with 0.01 M HCl for a few hours at 70°C and neutralized by washing with deionized water and left to dry in the oven at 70°C for 24 h and (2) less hydrophilic, $\theta_2 = 82 \pm 4^\circ$, for glass beads washed with the same hydrophobic silane solution. We use the Cassie equation [Eq. (1)] to estimate the equivalent contact angle, θ_{equ} , of our mixture,

$$\cos(\theta_{\text{equ}}) = \alpha(\cos\theta_1) + (1 - \alpha)(\cos\theta_2), \quad (1)$$

where Eq. (1) is based on the principle that a mixture of particles having two different contact angles will have a macroscopic effective contact angle that is proportional to their respective fractional components, α [13]. This is a reasonable assumption in the framework of the experimental conditions since the beads are essentially hydrophilic, only one type is less hydrophilic than the other. The values are presented in Table II.

C. Experimental conditions

We fill the cells with water by fully submerging them in a closed water tank attached to a vacuum pump, which draws air out of the medium as the surrounding water slowly percolates through the pores. The pump also reduces the presence of bubbles that could otherwise affect evaporation measurements. Bubbles in pore spaces can block flow in the pore and can therefore disrupt film continuity and reduce hydraulic conductivity [24–27]. As a result, the disruption of fluid flow can influence the final value of the film region extent. Once filled with water, the cell is oriented vertically such that water evaporates from the top. Evaporation experiments are performed inside a glove box with humidification systems, which permit precise control of the humidity. The relative humidity, H_R , is regulated and set at $20.0 \pm 2.0\%$ and $40.0 \pm 2.0\%$ by servocontrol device (model 5100, Electro-Tech Systems) and recorded. The temperature inside the glove box remains constant at $T = 32 \pm 2^\circ\text{C}$. We measure the mass loss of water using a digital balance (P4002 model, Denver Instruments) at specific time intervals controlled by a Matlab program.

D. Image treatment

We obtain images of the water repartition by taking pictures every 30 min using a Canon 500D camera with an 18- to 55-mm lens with a spatial resolution of about $35 \mu\text{m}$ per pixel. The cells are back-illuminated, allowing for the observations of the three zones, as shown in Fig. 1(a): the dry zone, the PSZ, and the fully saturated zone. Images are treated using Matlab.

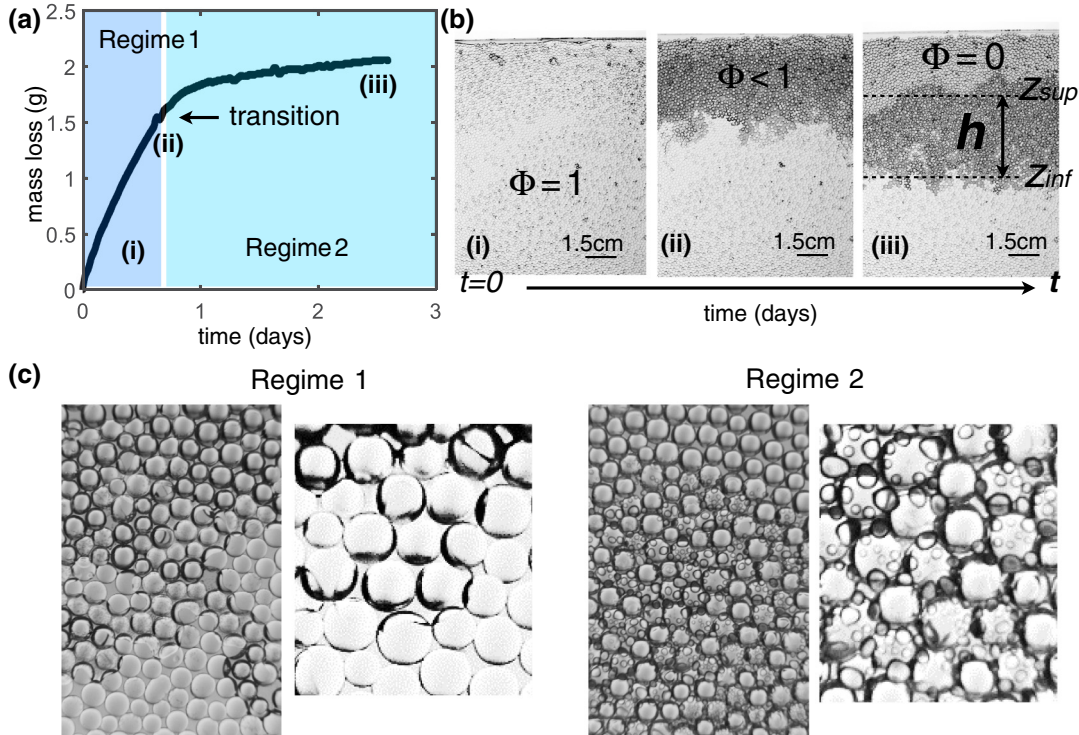


FIG. 1. (a) Typical evaporation curve showing mass loss, $m = \tilde{m}(t)$, described by two regimes separated by a transition point. (b) Experimental images of the time evolution of the water distribution with three distinct zones: dry zone ($\Phi = 0$), partially saturated zone (PSZ) ($\Phi < 1$), and a fully saturated or wet zone ($\Phi = 1$). The PSZ is bound by an evaporating front, z_{sup} (in the upper or superior portion), and a percolating front, z_{inf} (in the lower or inferior portion). Scale bar refers to ≈ 1.5 cm. (c) Experimental image during regime 1 showing liquid films in the form of pendular bridges between adjacent beads. The image on its right is a zoom of one of the areas, where blackened portions are air-water interfaces. The next set of images is typical of regime 2, showing the appearance of disconnected droplets, which can coalesce to form water pockets. The image on its right is a zoom of one of its areas. The bead size on these images is $d_2 = 1$ mm.

III. DEFINITIONS AND EXPERIMENTAL DATA

A. Observations and flux definition

We perform evaporation experiments using a wide variety of physical parameters (particle size, wettability fraction, and humidity) and each experiment exhibits similar features. A typical mass loss curve, $m = \tilde{m}(t)$, due to evaporation is shown in Fig. 1(a). The corresponding images are shown in Fig. 1(b). Let Φ be the saturation level of the medium. The system starts out fully saturated, $\Phi = 1$ [Fig. 1(b)]. Evaporation proceeds via two regimes. During the first regime, air enters the medium and displaces water, resulting in the appearance of a two-phase air-liquid mixture called the PSZ, where $0 < \Phi < 1$. The PSZ consists of an intricate hydraulic network connecting z_{inf} and z_{sup} . The first regime is controlled by mass transfer across an external mass transfer length scale, δ , above the cell surface, where drying rates [7,12,13,28] are approximately constant and mass loss due to evaporation is linear with time [29,30]. During regime 1, the rate of mass loss remains high due to hydraulic connections that ensure rapid transport of water from the bulk (interior of the porous medium) to the surface. As a result, water is continuously supplied at the surface to sustain the rate of evaporation [28], an action that is macroscopically described as a wicking effect [12]. In

literature, regime 1 is also referred to as the constant rate period (CRP) [11–13,31,32].

At a certain characteristic depth of z_{inf} , the liquid films can no longer sustain capillary flow and they detach from the evaporating surface. The disruption of the hydraulically connected films marks the transition [Fig. 1(a)] from the first to the second regime characterized by much lower evaporation rates [33]. At this point, a dry region, $\Phi = 0$ now separates the front and the evaporating surface [Fig. 1(b)]. Due to loss of hydraulic connections at the surface, evaporation during regime 2 now shifts to vapor diffusion [5] across air-filled pores in the dry region and drying rates continue to slow down. In the literature, regime 2 is also referred to as the falling rate period (FRP) [11–13,31,32].

The presence of the two regimes signifies that the overall evaporation flux can be separated into J_1 (flux regime 1) and J_2 (flux regime 2). Analytical expressions of both fluxes can be found extensively in the literature [3,11–13,19,29,32], showing that the mass loss in regime 1 is linear with time while the mass loss in regime 2 scales as \sqrt{t} . Such descriptions are in accordance with our own experimental observations.

In our experiments, we control the wettability by varying the ratio, α . We show in Fig. 2(a), $m = \tilde{m}(t, \alpha)$, for particle size d_1 . Results for d_2 are shown in Appendix A. From these results,

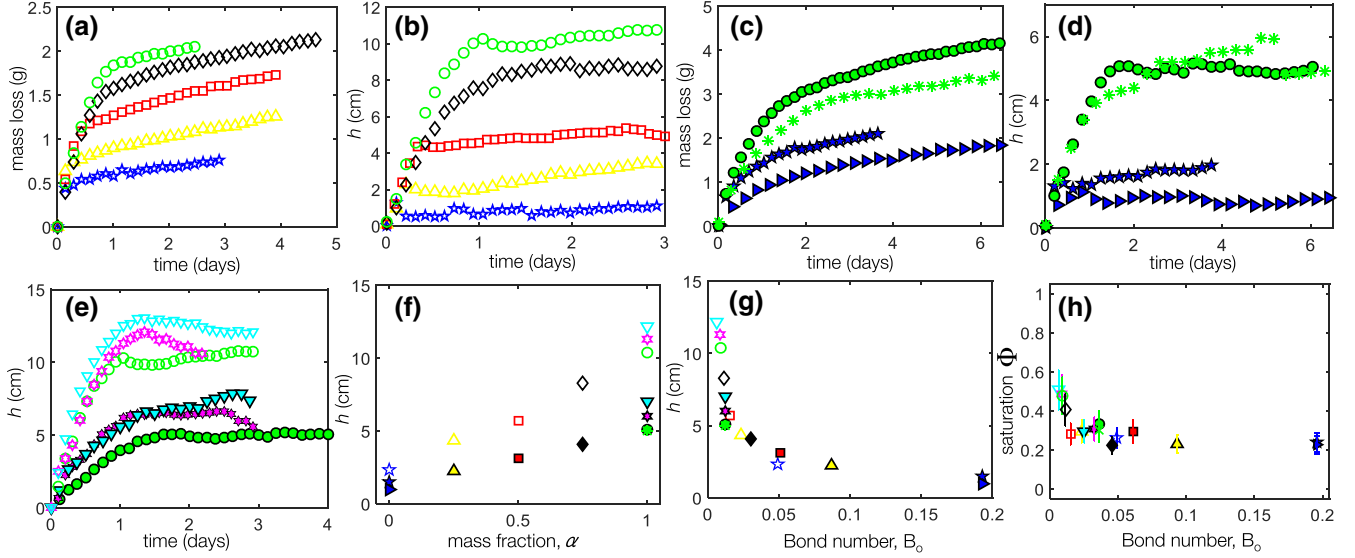


FIG. 2. (a) $m = \tilde{m}(t)$ for $d_1 = 500 \mu\text{m}$; (b) $h = \tilde{h}(t)$ for $d_1 = 500 \mu\text{m}$. (c) Experimental curves for $d_2 = 1 \text{ mm}$ of $m = \tilde{m}(t, H_R)$ for $H_R = 20.0 \pm 2.0\%$ and $H_R = 40.0 \pm 2.0\%$. (d) Experimental curves of $h = \tilde{h}(t, H_R)$ for two different H_R at $d_2 = 1 \text{ mm}$. (e) $h = \tilde{h}(t)$ for d_1 and d_2 for different θ_i . (f) $h = \tilde{h}(\alpha)$ for d_1 and d_2 , where h increases with α . (g) $h = \tilde{h}(B_o)$ for d_1 and d_2 . (h) Experimentally measured PSZ saturation, $\Phi_{\text{Expt}} = \tilde{\Phi}(B_o)$, for d_1 and d_2 . Legend: All performed at $H_R = 20\%$, $\theta_i = 90^\circ$, d_1 (hollow points): (\star) $\alpha = 0$; (\triangle) $\alpha = 0.25$; (\square) $\alpha = 0.50$; (\diamond) $\alpha = 0.75$; (\circ) $\alpha = 1$. All performed at $H_R = 20\%$, $\theta_i = 90^\circ$, d_2 (filled points): (\star) $\alpha = 0$; (\triangle) $\alpha = 0.25$; (\square) $\alpha = 0.50$; (\diamond) $\alpha = 0.75$; (\circ) $\alpha = 1$. All performed at $\alpha = 1$ and $H_R = 20\%$: (\circ) d_1 , $\theta_i = 75^\circ$; (∇) d_1 , $\theta_i = 45^\circ$; (\circ) d_2 , $\theta_i = 75^\circ$; (∇) d_2 , $\theta_i = 45^\circ$. All performed at $H_R = 40\%$ and d_2 : (\blacktriangledown) $\alpha = 0$; (\ast) $\alpha = 1$.

greater mass of water is lost in more-hydrophilic systems than in less-hydrophilic systems since more-hydrophilic particles maintain hydraulic continuity that favors evaporation. This is consistent with reported experimental [5] and simulation results [34]. The minimal h value observed in less-hydrophilic systems is attributed to the minimal presence of hydraulic continuity between the bulk and the surface [5].

The height or extent, h , of the PSZ is bound by the positions of the percolating front, z_{inf} , and the evaporating front, z_{sup} . The h value is a function of wettability mixture, $h = \tilde{h}(t, \alpha)$, whose results are presented in Fig. 2(b) (d_1) and Appendix A (d_2). From the figures, the different regimes are easy to distinguish, where h increases linearly during regime 1 and increases slightly in regime 2. With respect to regime 1, the growth of h remains “quasiconstant” during regime 2.

We also control the relative humidity, H_R , of the glove box. The curves in Fig. 2(c) and Fig. 2(d) show $m = \tilde{m}(t, H_R)$ and $h = \tilde{h}(t, H_R)$, respectively, for $H_R = 20.0 \pm 2.0\%$ and $H_R = 40.0 \pm 2.0\%$ using $d_2 = 1 \text{ mm}$. The relative humidity is a measure of the amount of moisture in the air. At low H_R , air is considered dry and thus water evaporates faster to maintain equilibrium. At higher H_R values, there is greater moisture content in the air and thus evaporation rates proceed slower. The extent of h is similar for the two different relative humidity values. This strongly suggests that h is independent of relative humidity. The relative humidity only changes the overall water content [Fig. 2(c)] inside the medium but not the extent, h , of the liquid film region [Fig. 2(d)].

In an evaporation experiment, water transport is driven and retarded by various forces. We therefore estimate the

dimensionless Bond, B_o , and capillary numbers, C_a , to determine which forces are dominant.

B. Dimensionless numbers

The capillary forces that transport water towards the evaporating surface are always opposed by viscous forces [7,9,12,31,35]. Because in these experiments the sample cells are oriented vertically, gravity also has an opposing against upward capillary flow. When gravity is part of drying, the pressure of the liquid is hydrostatic and the displacement pattern follows features of invasion percolation [10,11,16].

The interplay between these forces controls the dynamic aspects governing evaporation. To determine the relative dominance among the forces, we compute C_a and B_o , which provide the ratio between viscous and capillary forces (former) and between gravity and capillary forces (latter) and are defined as:

$$C_a = \frac{\mu v}{\sigma \cos \theta_{\text{equ}}} \text{ and } B_o = \frac{\rho g R^2}{\sigma \cos \theta_{\text{equ}}}, \quad (2)$$

where μ is the dynamic liquid viscosity, v is the characteristic liquid filtration velocity, σ is the interfacial tension, and g is the acceleration due to gravity. The parameter v in C_a is normally defined as the filtration velocity in regime 1 and is represented as $v = J_1/\rho$ [35]. While maintaining the same R , we can tune the value of B_o by tilting the sample cell at an angle relative to the direction of gravity, henceforth referred to as a tilt angle, θ_i . This effectively reduces gravity into a component given

TABLE III. Values of J_1 , B_o , and C_a for different experimental conditions.

Expt. No.	R (10^{-6} m)	H_R (%)	θ_t (deg)	α (no unit)	J_1 (g/day)	B_o (10^{-2})	C_a (10^{-8})
1	250	20	90	0	2.75	4.90	4.93
2	250	20	90	0.25	2.56	2.33	3.37
3	250	20	90	0.50	2.40	1.53	1.85
4	250	20	90	0.75	1.85	1.14	1.06
5	250	20	90	1	1.86	0.91	0.85
6	500	20	90	0	1.35	19.6	3.33
7	500	20	90	0.25	1.63	9.33	1.91
8	500	20	90	0.50	1.54	6.12	1.19
9	500	20	90	0.75	1.99	4.55	1.14
10	500	20	90	1	1.96	3.62	0.89
11	500	40	90	0	0.72	19.6	3.33
12	500	40	90	1	1.14	3.62	0.89
13	250	20	75	1	2.48	0.87	1.13
14	250	20	45	1	3.45	0.64	1.57
15	500	20	75	1	3.00	3.50	1.37
16	500	20	45	1	3.86	2.56	1.71

by $g \sin \theta_t$, where its effect on the extent of the PSZ, h , is shown in Fig. 2(e). Lower θ_t values result to higher h values. The experimental values for J_1 , B_o , and C_a are presented in Table III.

A summary of h results for all experiments is shown in Fig. 2(f) as a function of α , revealing that smaller particles, d_1 (hollow points), produce bigger h values than larger particles, d_2 (filled points). In addition, Fig. 2(f) also shows that h increases with hydrophilic fraction α . In Fig. 2(g), all the data collapse on a single curve as h is plotted as a function of B_o , revealing a sharp decrease. When plotted in log-log scale, the regression analysis shows a slope of -0.6 (see Appendix B), thereby giving a scaling law of $h \sim B_o^{-0.6}$. Furthermore, we calculate Φ_{Expt} , which is the ratio of the mass of water within the PSZ with respect to the initial mass of water, m_i , at the start of the experiment, while taking into account the geometry of the cell:

$$\Phi_{\text{Expt}} = \Phi_{\text{PSZ}} = \frac{m_f - (S\varphi\rho L^*)}{m_i}, \quad (3)$$

where m_f is the equilibrium total mass of water in the porous medium, which can be estimated from the mass curves, $L^* = L - z_{\text{inf}}$, where L is the vertical length of the medium from the cell surface to the bottom of the packing, and φ is porosity. The plot of PSZ saturation Φ_{Expt} as function of B_o is shown in Fig. 2(h). Four principal observations can be deduced from these data: (1) smaller particles hold more water content than larger particles; (2) PSZ saturation increases slightly with wettable fraction; (3) PSZ saturation is higher when gravity effects are diminished; and (4) PSZ saturation appears to be constant regardless of relative humidity.

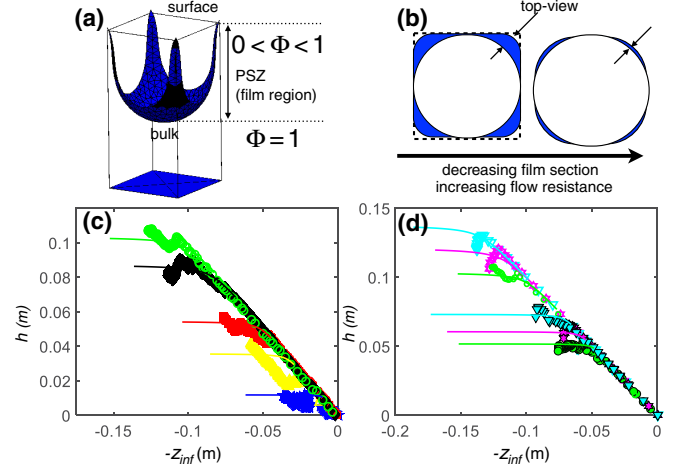


FIG. 3. (a) Scheme of corner liquid films of a square tube during evaporation. Image is from Surface Evolver simulations using the code of Berthier and Brakke [39]. (b) Top-view of liquid film thickness in a tube of square cross section. Corner films in pore walls are initially sharp but takes a more rounded shape [19] as evaporation proceeds. (c) Experimental results (points) of $h = \tilde{h}(z_{\text{inf}})$ for d_1 for different α fitted with the model (solid lines) of Yiotis *et al.* [19]. Comparison for d_2 is shown in Appendix A. (d) Experimental results (points) of $h = \tilde{h}(z_{\text{inf}})$ for d_1 and d_2 but performed at varying tilt angles, θ_t . Solid lines show the model of Yiotis *et al.* [19]. The extent of h is higher at smaller θ_t . Legend definitions are the same ones used in Fig. 2.

C. Continuous films, isolated pockets

Experimental images of the PSZ in Fig. 1(c) show varying compositions at different regimes. Figure 1(c) (left) shows a network of liquid films, which are a coalescence of pendular bridges between beads, trapped in pore spaces. Studies [6,12] have shown that liquid films pinned to the corners of the pore wall (corner film flow) contain menisci with varying radii of curvature that induce a capillary pressure gradient. This serves as the driving force for upward liquid flow from the bulk to the evaporating surface, thus assuring hydraulic continuity. In Fig. 1(c) (right), we observe droplets with positive curvature, which suggests they have been detached from the main film network. Most of the droplets start appearing later (during regime 2). Apart from droplets, disconnected films also appear because as water content in the liquid films continues to decrease due to evaporation, they eventually detach from the main liquid network.

To understand water repartition in the PSZ, we must first quantify the saturation of water contained in continuous liquid films, which contributes to the extent of h .

D. Corner film flow

Yiotis *et al.* [12] developed a model that predicts h and the saturation of liquid films in the PSZ during evaporation out of a porous medium by calculating the cross section of the corner liquid films. These corner films, when viewed from the top, resemble flow in a noncircular capillary tube [29,36] shown in Fig. 3(a). Studies [29,32,35,37] have demonstrated that evaporation of liquid from a square tube results to the

formation of corner liquid films [Fig. 3(b)], whose large cross-sectional area reduces flow resistance from the interior of the porous medium (bulk) to the evaporating surface. The corner films represent a more effective transport mechanism than simple vapor diffusion [37], which is the dominant mechanism in the evaporation of liquid from a circular tube. Transport via corner film flow holds true for any tube of polygonal cross section with sharp corners [6,12].

As liquid films begin to thin out towards the end of regime 1, the geometry of the films then adopt a more rounded shape during regime 2 [19] [Fig. 3(b)], thereby decreasing cross-sectional area and increasing flow resistance from the bulk to the evaporating surface. The flow resistance along the corner film is also a function of contact angle [38], where higher contact angles reduce the cross-sectional area of the film available for flow. Furthermore, during regime 2, recovery rates decrease continuously with time and the film region extent increases slightly as the interfaces recede in the pore space [12].

IV. RESULTS AND DISCUSSION

A. Prediction of PSZ height

To quantify the water saturation contained in liquid films, we first must calculate for h using the analytical model of Yiotis *et al.* [12,19] with data from Dong and Chatzis [36]. The model is straightforward, comprehensive, and widely covered in the literature. However, detailed discussion on its use is not the primary objective of this paper. We compare the analytical model with our experiments shown in Fig. 3(c) for d_1 (d_2 in Appendix A) and Fig. 3(d) for different θ_r . Comparison reveals excellent agreement. Apart from predicting h , their model also permits calculation of the saturation of water contained in liquid films in the PSZ but had been only developed for completely hydrophilic materials. Due to our mixed wettable system, we pursue a different avenue, through numerical simulations, to find out the quantity of water contained in connected liquid films and from that information, we deduce the quantity of water disconnected from the main network (droplets, pockets, etc.).

B. Simulations

We define the total water saturation within the PSZ in Eq. (3). We also define the saturation contained in continuous liquid films and saturation isolated from the main network, both with respect to initial mass, by performing numerical simulations using Surface Evolver [40]. The assumption of hydrostatic pressure for Surface Evolver calculations is a first-order estimate that does not account for pressure drop that results from viscous dissipation, which is a function of evaporation rate [41]. The pressure drop due to viscous dissipation results to a change in the interfacial curvature of the film [41,42]. But as can be seen from Ref. [41] and Ref. [42], it only contributes to a very small increase in PSZ, but most of it is accounted for by the balance between gravity and capillarity. Therefore, changes in curvature that result from viscous flow are negligible compared to capillary suction [42]. In addition, at low viscous dissipation, the total curvature is considered uniform along the hydraulic film interface [41].

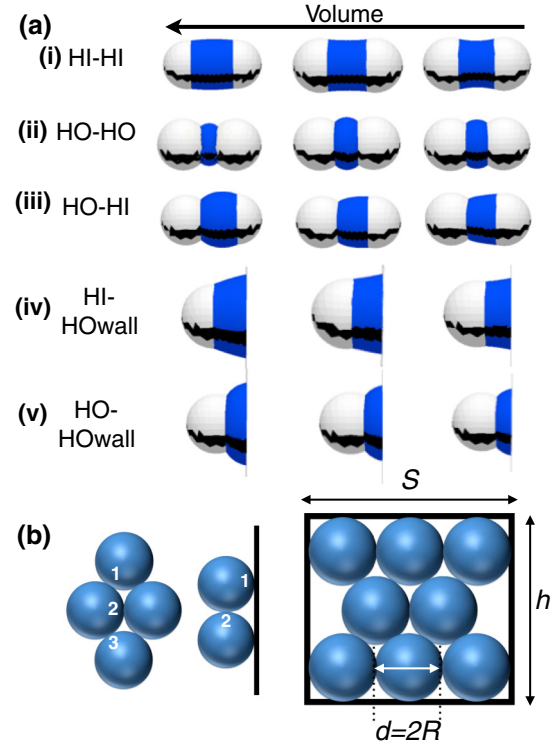


FIG. 4. (a) Surface Evolver results showing the evolution of bridge meniscus between two spherical bodies and between a sphere and a vertical plane of varying surface properties. (i) HI-HI; (ii) HO-HO; (iii) HI-HO; (iv) HI-HOwall; and (v) HO-HOwall, where HI refers to more-hydrophilic surface while HO refers to less-hydrophilic surface. (b) Illustration of the number of contact sites of a given sphere adjacent to other spheres or to a wall. Representation of the number of spheres that can be contained within a given space.

We consider h to be primarily determined by a series of interconnected pendular bridges between particles in contact with each other or with the wall. In a 2D granular system of mixed wettability, we can have different kinds of pendular bridges in Fig. 4(a): bridge between beads of the same R and of the same surface wetting properties, (i) HI-HI and (ii) HO-HO, where HI stands for more-hydrophilic particles while HO stands for less-hydrophilic particles; (iii) bridge between beads of the same R but of different wetting properties, HI-HO; (iv) bridge between a more-hydrophilic bead and the less-hydrophilic wall, HI-HOwall; (v) and, finally, a bridge between a less-hydrophilic bead and the less-hydrophilic wall, HO-HOwall. The shape of the meniscus depends on the wetting properties of the solids (sphere or plane) and also on the volume of the liquid body.

It is understandably difficult to assess the liquid bridges during regime 1, due to the rapid nature of its flux. Thus, in these simulations, we consider that the bridge is in equilibrium during the slower evaporation dynamics in regime 2—a fact supported by results in Fig. 2 showing the quasiconstant value of h . Earlier, we estimate the $B_o \sim 10^{-2}$ (see Table III). At equilibrium, the capillary force is the dominant force acting on the bridge since the liquid volumes are very small.

The menisci of pendular bridges have negative curvatures, whose pressure is hydrostatic along the extent of h . The

pressure value, P , is determined using Surface Evolver [39,40] by calculating the change in energy with respect to volume, $P = dE/dV$. The results from the numerical simulations establish a pressure-volume relationship, which can be used to evaluate the saturation of water contained in liquid bridges within the PSZ. Since a liquid film is, in essence, a coalescence of capillary bridges, it is then important to estimate the number of bridges that comprise this network in the PSZ as a function of wettability.

In the case of random-close packing, where the distribution is close to dense packing, each spherical bead has a maximum of six neighbors. Thus, the minimum number of contact sites between two beads is $3N_b$ while there are $2N_b$ contact sites between a bead and the wall as shown in Fig. 4(f), where N_b is the number of spheres. For a certain S and h , the parameter N_b can be estimated using principles associated with Kepler conjecture, which describes the maximum packing of spheres (or objects) achieved for a given space [43]. We then evaluate the saturation contained in continuous liquid films, V_C , along the extent of h , using the equation:

$$V_C = \frac{3N_b}{h} [\alpha^2 \Sigma_{II} + \alpha(1-\alpha) \Sigma_{IO} + (1-\alpha)^2 \Sigma_{OO}] + \frac{2N_b}{h} (\alpha \Sigma_{I-wall} + (1-\alpha) \Sigma_{O-wall}), \quad (4)$$

where the various Σ parameters refer to

$$\begin{aligned} \Sigma_{II} &= \int_0^h V_{II}(z) dz, & \Sigma_{IO} &= \int_0^h V_{IO}(z) dz, \\ \Sigma_{OO} &= \int_0^h V_{OO}(z) dz, & \Sigma_{I-wall} &= \int_0^h V_{I-wall}(z) dz, \\ \Sigma_{O-wall} &= \int_0^h V_{O-wall}(z) dz, \end{aligned} \quad (5)$$

where V_{II} , V_{IO} , V_{OO} , V_{I-wall} , and V_{O-wall} correspond to the volumes of the liquid trapped between two solid bodies. The subscripts refer to the surface coupling between two different wetting properties: “I” for more hydrophilic and “O” for less hydrophilic. The h values are those predicted by the model of Yiotis *et al.* [12,19], which we have shown to agree with experiments.

The total saturation of the liquid films in the PSZ can be obtained from simulation expressed in terms of Φ_{Evolver} defined as:

$$\Phi_{\text{Evolver}} = \frac{V_C}{V_{\text{empty}}}, \quad (6)$$

where V_C is the volume of the continuous liquid films calculated from Eq. (6) and V_{empty} is the free pore volume of the entire medium defined as $V_{\text{empty}} = SL\varphi$. Equation (6) shows the saturation of connected liquid films within the PSZ, taking note that the fully wet zone has no liquid-air interfaces. We show in Fig. 5(a) the plot of Φ_{Expt} [Eq. (3)] as function of B_o . The black line is a guide for the eye.

We also calculate the saturation contained in liquid films using the analytical model of Yiotis *et al.* [12,19] (graph in Appendix C), which was conceptualized for completely hydrophilic media and from a single tube. Thus, the value obtained from this model was then scaled with respect to 2D

porous medium, which can be seen as a bundle of equivalent capillary tubes [7]. We then compare in the main figure in Fig. 5(b) the results of the analytical model (now shown as a broken line) with results from the simulations (points), Φ_{Evolver} as function of B_o . The broken line in this figure is the best fit from the results of the analytical model [12,19] and serves as a guide (see Appendix C). From these results, the fact that there is still an offset in saturation contained in liquid films with respect to the experimentally measured PSZ saturation (solid line) strongly reflects the fact that the PSZ is not solely made up of connected hydraulic networks but also contains water in the form of droplets and disconnected pockets, which have actually also been observed using tomography [5,13].

Comparison between the results of Surface Evolver with that of analytical models [12,19] shows decent agreement in the framework of negligible viscous dissipation effects. Differences, however, still remain such as the role of ambient humidity. The numerical model does not account for changes in humidity and thus underestimates the saturation value at $R_H = 40\%$. The cited theory, however, considers this parameter and therefore predicts a value that is close to the experimentally measured PSZ value (Appendix C). This further confirms that greater quantity of connected liquid films is indeed present at higher R_H values.

Results in Fig. 5(c) and Fig. 5(d) first show that Φ_{Evolver} increases with α , suggesting that more-hydrophilic materials favor liquid films. Second, comparison of Fig. 5(e) and Fig. 5(f) show that packing of smaller particles hold more saturation than packing of larger ones due to the higher capillary pressures emanating from smaller liquid volumes. Both figures also show that the PSZ saturation seems to slightly increase with α , notably for smaller diameters, similarly to the variation of h with α in Fig. 2(f). This shows that increasing hydrophilicity favors saturation in continuous films while increasing hydrophobicity favors disconnected pockets. Third, PSZ saturation is generally higher at greater θ_t because the extent h also increases with reduced gravity effects. Last, PSZ saturation seems to be independent of relative humidity. This may appear misleading; however, if we take into account the fully wet zone (FSZ), which is larger at higher H_R , the overall water content remaining in the entire medium would still be greater at higher H_R , in accordance with observations in Fig. 2(a). In Fig. 5(g) and Fig. 5(h), we show Φ_{total} (PSZ + FSZ) as function of wettability. Greater quantity of water is globally retained in less-hydrophilic media in contrast to more-hydrophilic ones.

V. CONCLUSION

We have systematically investigated experiments on the evaporation of water from model soil systems using parameters such as surface treatment, particle size, and environmental humidity. We demonstrate through experiments and simulations that the partially saturated zone is not only a connected liquid film region but also a region containing droplets and clusters that have been disconnected from the main hydraulic network. We calculate the average global saturation in the partially saturated zone and find that the saturation of water in the continuous liquid films increases with overall hydrophilicity

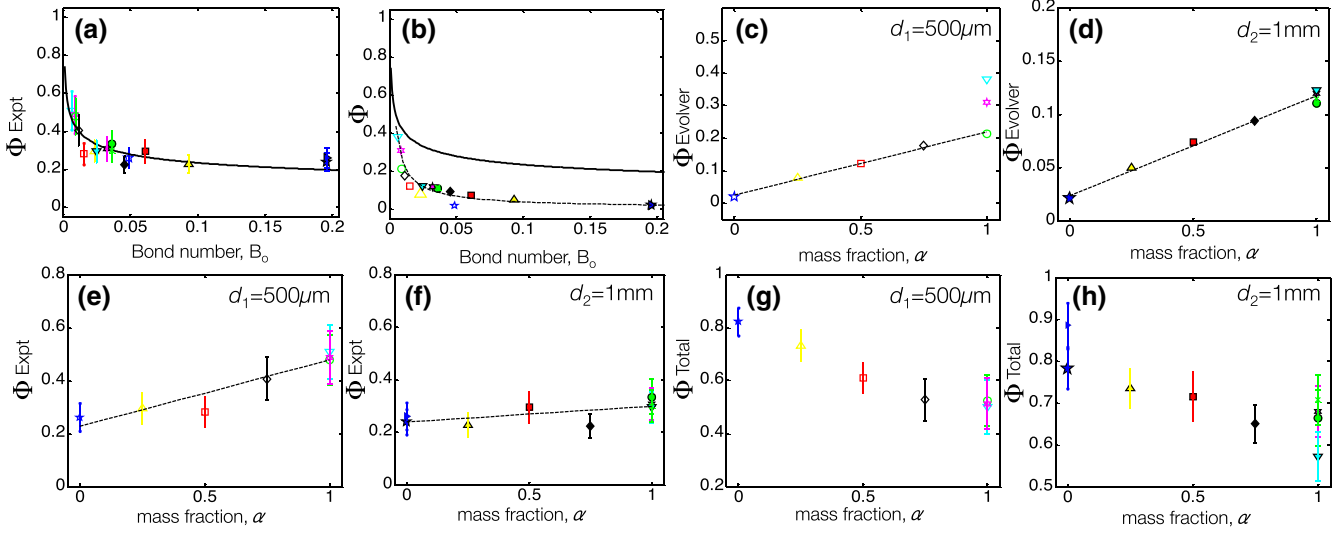


FIG. 5. (a) Saturation of the PSZ, Φ_{Expt} , as a function of Bond number, B_o , where the solid line is a guide for the eye. (b) Plot of simulation results from Surface Evolver, Φ_{Evolver} (points), as function of B_o compared to Φ_{Expt} (solid line). The broken line is the best fit of the results (Appendix C) of the analytical model [12,19] and serves as a guide. (c) Plot of Φ_{Evolver} as function of wettability, α , for d_1 . Broken line serves as guide. (d) Plot of Φ_{Evolver} as function of α for d_2 . Broken line serves as guide. (e) Plot of Φ_{Expt} as function of α for d_1 . Broken line serves as guide. (f) Plot of Φ_{Expt} as function of α for d_2 . Broken line also serves as guide. (g) Plot of Φ_{Total} (total saturation including Φ_{Expt} and saturation within fully wet zone) as function of α for d_1 . (h) Plot of Φ_{Total} as function of α for d_2 . Legend definitions in all graphs are the same ones used in Fig. 2.

since they favor formation of capillary networks. In contrast, less-hydrophilic systems do not favor liquid film continuity and thus greater quantity of disconnected clusters exist. The more disconnected clusters present in the porous medium, the less we lose water in the medium since evaporation now mainly proceeds via diffusion instead of capillary transport through the network.

These 2D results could have direct applications in soil additive design to control water repartition in soil during evaporation. Soil is essentially a mixture of hydrophilic and hydrophobic components. One way to achieve an optimal retention of water is to develop additives with dual wettability properties. The presence of hydrophobic (or less-hydrophilic) components breaks liquid film continuity and will result to more disconnected clusters, which evaporate at slower rates.

These experiments have been performed in 2D model systems. It would be a good contribution to the subject in the future to analyze the connectivity of films and appearance of liquid clusters in three-dimensional systems, since such systems most closely resemble real soil structures.

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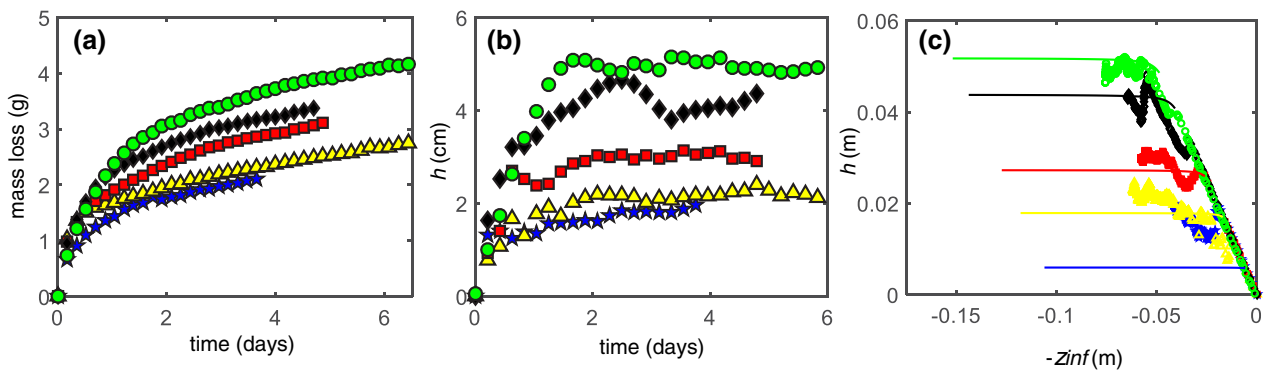


FIG. 6. (a) $m = \tilde{m}(t)$ for $d_2 = 1 \text{ mm}$; (b) $h = \tilde{h}(t)$ for $d_1 = 1 \text{ mm}$. (c) Experimental results (points) of $h = \tilde{h}(z_{\text{inf}})$ for d_1 for different α fitted with the model (solid line) of Yiotis *et al.* [12,19]. [Legends for (a) and (b)] All performed at $H_R = 20\%$, $\theta_i = 90^\circ$, d_2 (filled points): (\star) $\alpha = 0$; (\triangle) $\alpha = 0.25$; (\blacksquare) $\alpha = 0.50$; (\blacklozenge) $\alpha = 0.75$; (\bullet) $\alpha = 1$. [Legends for (c)] All performed at $H_R = 20\%$, $\theta_i = 90^\circ$, d_2 : (\star) $\alpha = 0$; (\triangle) $\alpha = 0.25$; (\square) $\alpha = 0.50$; (\diamond) $\alpha = 0.75$; (\circ) $\alpha = 1$.

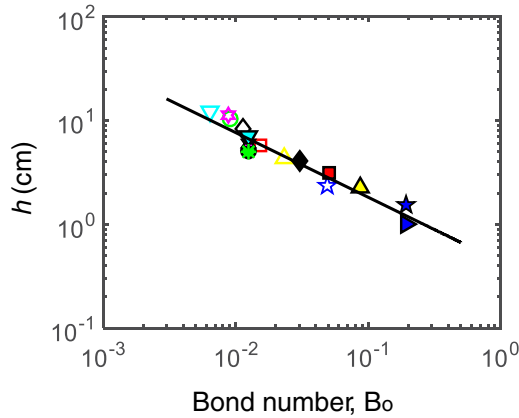


FIG. 7. (a) Plot of h as a function of B_o in log-log scale. The slope of the solid line is -0.6 . Legend: All performed at $H_R = 20\%$, $\theta_t = 90^\circ$, d_1 (hollow points): (\star) $\alpha = 0$; (\triangle) $\alpha = 0.25$; (\square) $\alpha = 0.50$; (\diamond) $\alpha = 0.75$; (\circ) $\alpha = 1$. All performed at $H_R = 20\%$, $\theta_t = 90^\circ$, d_2 (filled points): (\star) $\alpha = 0$; (\triangle) $\alpha = 0.25$; (\square) $\alpha = 0.50$; (\diamond) $\alpha = 0.75$; (\circ) $\alpha = 1$. All performed at $\alpha = 1$ and $H_R = 20\%$: (\ast) d_1 , $\theta_t = 75^\circ$; (∇) d_1 , $\theta_t = 45^\circ$; (\bullet) d_2 , $\theta_t = 75^\circ$; (\blacktriangledown) d_2 , $\theta_t = 45^\circ$. All performed at $H_R = 40\%$ and d_2 : (\blacktriangledown) $\alpha = 0$; (\ast) $\alpha = 1$.

APPENDIX A: ADDITIONAL DATA FOR PARTICLE SIZE DIAMETER, $d_2 = 1$ mm

In Fig. 6(a), we show additional results for $d_2 = 1$ mm. In Fig. 6(a), we present the water mass loss via evaporation as function of time for different wettabilities at constant particle size. In this figure, more mass of water is lost as we increase hydrophilicity. In Fig. 6(b), we show the extent (height), h , of the PSZ as a function of time. During regime 1, h increases rapidly but stabilizes around a quasiconstant value during regime 2. In Fig. 6(c), we show h as a function of the position of the percolating front, z_{inf} . The solid lines are the corresponding analytical predictions of h based on the analytical model of Yiotis *et al.* [12,19].

APPENDIX B: REGRESSION ANALYSIS OF EXTENT (HEIGHT), h , OF PSZ AS FUNCTION OF BOND NUMBER, B_o

When the extent h of the PSZ as a function of Bond number, B_o [Fig. 2(g) in the main paper] is plotted in log-log scale, regression analysis shows a slope of -0.6 as shown in Fig. 7.

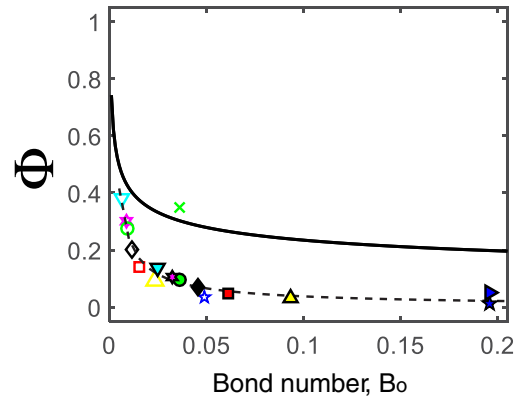


FIG. 8. (a) Plot of Φ as a function of Bond number, B_o . The points are results calculated from the analytical model of Yiotis *et al.* [12,19]. The broken line represents a best fit of the analytical results and also serves as a guide. The solid line represents the experimentally measured PSZ saturation, Φ_{Expt} . : All performed at $H_R = 20\%$, $\theta_t = 90^\circ$, d_1 (hollow points): (\star) $\alpha = 0$; (\triangle) $\alpha = 0.25$; (\square) $\alpha = 0.50$; (\diamond) $\alpha = 0.75$; (\circ) $\alpha = 1$. All performed at $H_R = 20\%$, $\theta_t = 90^\circ$, d_2 (filled points): (\star) $\alpha = 0$; (\triangle) $\alpha = 0.25$; (\square) $\alpha = 0.50$; (\diamond) $\alpha = 0.75$; (\circ) $\alpha = 1$. All performed at $\alpha = 1$ and $H_R = 20\%$: (\ast) d_1 , $\theta_t = 75^\circ$; (∇) d_1 , $\theta_t = 45^\circ$; (\bullet) d_2 , $\theta_t = 75^\circ$; (\blacktriangledown) d_2 , $\theta_t = 45^\circ$. All performed at $H_R = 40\%$ and d_2 : (\blacktriangledown) $\alpha = 0$; (\ast) $\alpha = 1$.

APPENDIX C: SATURATION OF WATER CONTAINED IN LIQUID FILMS CALCULATED FROM ANALYTICAL MODEL

The points in Fig. 8 represent the saturation of water contained in connected liquid films as calculated from the analytical model of Yiotis *et al.* [12,19]. The broken line serves as a guide for the observed general trend of the analytical results. There is an offset when the results are compared to those of the experimentally measured PSZ saturation, Φ_{Expt} , as indicated by the solid line [for the actual experimental points, kindly refer to Fig. 5(a) of the main paper]. The offset strongly reflects the fact that there is a quantity of water not accounted by the model and is therefore outside of or disconnected from the main liquid film network.

- [1] S. Herminghaus, *Adv. Phys.* **54**, 3 (2005).
- [2] R. Calvet, *Etudes sur les transferts d'eau dans le système sol-plante-atmosphère* (INRA France, Paris, 1988).
- [3] C. M. Cejas, L. A. Hough, J. C. Castaing, C. Fretigny, and R. Dreyfus, *Phys. Rev. E* **90**, 042716 (2014).
- [4] T. M. Shaw, *Phys. Rev. Lett.* **59**, 1671 (1987).
- [5] N. Shokri, P. Lehmann, and D. Or, *Water Resour. Res.* **45**, W10433 (2009).
- [6] M. Prat, *Int. J. Heat Mass Transf.* **50**, 1455 (2007).
- [7] P. Lehmann, S. Assouline, and D. Or, *Phys. Rev. E* **77**, 056309 (2008).
- [8] H. P. Huinink, L. Pel, M. A. J. Michels, and M. Prat, *Eur. Phys. J. E* **9**, 487 (2002).
- [9] J. B. Laurindo and M. Prat, *Chem. Eng. Sci.* **53**, 2257 (1998).
- [10] A. G. Yiotis, I. O. Tsimpanogiannis, and A. K. Stubos, *Dry. Technol.* **28**, 981 (2010).
- [11] M. Prat and F. Bouleux, *Phys. Rev. E* **60**, 5647 (1999).
- [12] A. G. Yiotis, D. Salin, E. S. Tajer, and Y. C. Yortsos, *Phys. Rev. E* **86**, 026310 (2012).
- [13] N. Shokri, P. Lehmann, P. Vontobel, and D. Or, *Water Resour. Res.* **44**, W06418 (2008).
- [14] D. Or, M. Tuller, and S. B. Jones, *SSAJ* **73**, 341 (2009).

- [15] A. G. Yiotis, I. O. Tsimpanogiannis, A. K. Stubos, and Y. C. Yortsos, *J. Colloid Interface Sci.* **297**, 738 (2006).
- [16] M. Prat, S. Veran-Tissoires, N. Vorhauer, T. Metzger, and E. Tsotsas, *Dry. Technol.* **30**, 1129 (2012).
- [17] J. Han and Z. Zhou, *Sci. World J.* **2013**, 240280 (2013).
- [18] R. J. Hunt, D. E. Prudic, J. F. Walker, and M. P. Anderson, *Ground Water* **46**, 551 (2008).
- [19] A. G. Yiotis, D. Salin, E. S. Tajer, and Y. C. Yortsos, *Phys. Rev. E* **85**, 046308 (2012).
- [20] L. Xu, S. Davies, A. B. Schofield, and D. A. Weitz, *Phys. Rev. Lett.* **101**, 094502 (2008).
- [21] C. M. Cejas, Y. Wei, R. Barrois, C. Fretigny, D. J. Durian, and R. Dreyfus, *Phys. Rev. E* **90**, 042205 (2014).
- [22] Y. Wei, C. M. Cejas, R. Barrois, R. Dreyfus, and D. J. Durian, *Phys. Rev. Appl.* **2**, 044004 (2014).
- [23] Y. Wei and D. J. Durian, *Phys. Rev. E* **87**, 053013 (2013).
- [24] A. Hunt and M. Manga, *Trans. Porous Media* **52**, 51 (2003).
- [25] I. Dror and B. Berkowitz, *Water Resour. Res.* **40**, W09203 (2004).
- [26] D. Ronen, B. Berkowitz, and M. Magaritz, *Trans. Porous Media* **4**, 295 (1989).
- [27] J. E. Christiansen, *Soil Sci.* **58**, 355 (1944).
- [28] P. Coussot, *Eur. Phys. J. B* **15**, 557 (2000).
- [29] F. Chauvet, P. Duru, S. Geoffroy, and M. Prat, *Phys. Rev. Lett.* **103**, 124502 (2009).
- [30] J. van Brakel, *Advances in Drying*, edited by A. S. Mujumdar (Hemisphere, New York, 1980).
- [31] P. Lehmann and D. Or, *Phys. Rev. E* **80**, 046318 (2009).
- [32] F. Chauvet, S. Cazin, P. Duru, and M. Prat, *Int. J. Heat Mass Transf.* **53**, 1808 (2010).
- [33] P. Schultz, *Chem. Eng. Tech.* **14**, 234 (1991).
- [34] H. Chraïbi, M. Prat, and O. Chapuis, *Phys. Rev. E* **79**, 026313 (2009).
- [35] M. Prat, *Chem. Eng. J.* **86**, 153 (2002).
- [36] M. Dong and I. Chatzis, *J. Colloid Interface Sci.* **172**, 278 (1995).
- [37] B. Camassel, N. Sghaier, M. Prat, and S. Ben Nasrallah, *Chem. Eng. Sci.* **60**, 815 (2005).
- [38] T. C. Ransohoff and C. J. Radke, *J. Colloid Interface Sci.* **121**, 392 (1988).
- [39] J. Berthier and K. Brakke, *The Physics of Microdroplets* (Elsevier, New York, 2012).
- [40] K. Brakke, *Surface Evolver Manual Version 2.50*, Susquehanna University (2010).
- [41] E. Keita, S. A. Koehler, P. Faure, D. Weitz, and P. Coussot, *Eur. Phys. J. E* **39**, 23 (2016).
- [42] S. Beyhaghi, S. Geoffroy, M. Prat, and K. M. Pillai, *AIChE J.* **60**, 1930 (2014).
- [43] T. C. Hales, *Ann. Math.* **162**, 1065 (2005).