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Can moons have moons?

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ABSTRACT

Each of the giant planets within the Solar system has large moons but none of these moons have their own moons (which we call *submoons*). By analogy with studies of moons around short-period exoplanets, we investigate the tidal-dynamical stability of submoons. We find that 10 km-scale submoons can only survive around large (1000 km-scale) moons on wide-separation orbits. Tidal dissipation destabilizes the orbits of submoons around moons that are small or too close to their host planet; this is the case for most of the Solar system's moons. A handful of known moons are, however, capable of hosting long-lived submoons: Saturn's moons Titan and Iapetus, Jupiter's moon Callisto, and Earth's Moon. Based on its inferred mass and orbital separation, the newly discovered exomoon candidate Kepler-1625b-I can in principle host a large submoon, although its stability depends on a number of unknown parameters. We discuss the possible habitability of submoons and the potential for subsubmoons. The existence, or lack thereof, of submoons may yield important constraints on satellite formation and evolution in planetary systems.

Key words: Moon-planets and satellites: dynamical evolution and stability-planets and satellites: physical evolution-planetary systems.

1 INTRODUCTION

In all known planetary systems, natural satellites occur in a restricted dynamical phase space: planets orbit stars and moons orbit planets. It is natural to ask, can moons have their own stable satellites (submoons)? If so, why do none of the known moons of the Solar system have their own submoons? One possibility is that the formation mechanism of planet-moon systems precludes their formation. Another possibility, is that these bodies are dynamically unstable and are rapidly scoured from their system after formation. Here, we investigate the latter hypothesis.

What are the requirements for stability of a submoon? To ensure dynamical stability, the host moon must have a Hill sphere that is larger than its physical radius as well as its Roche limit. The submoon must also survive any long-term dynamical effects such as tidal evolution.

Tidal stresses deform extended objects and internal dissipation leads to changes in the objects' rotation states and orbits (e.g. Darwin 1879; Goldreich & Soter 1966; Ferraz-Mello, Rodríguez & Hussmann 2008). Tidal evolution in a planet–moon system generally causes the moon's orbit to widen if the planet spins quickly or to shrink if the planet spins slowly (e.g. Peale, Cassen & Reynolds 1980; Burns & Matthews 1986).

Tidal evolution in star-planet-moon systems has been studied in the context of Venus and Mercury's lack of moons (Burns 1973; Counselman 1973; Ward & Reid 1973) and in the more general case of moons orbiting exoplanets on short-period orbits (Barnes & O'Brien 2002; Sasaki, Barnes & O'Brien 2012; Sasaki & Barnes 2014; Piro 2018). In a star-planet-moon system, stellar tidal friction acts to slow the planet's rotation, with a direct consequence for the moons' tidal migration (Burns 1973; Ward & Reid 1973). Depending on the configuration, moons may migrate inwards and crash into their host planets or migrate outwards until they reach the stability limit. In some cases moons can first migrate outwards, then change direction and migrate inwards as the planet spins down (Barnes & O'Brien 2002; Sasaki et al. 2012; Piro 2018).

Here we apply this concept to planet–moon–submoon systems. Barnes & O'Brien (2002) showed that under tidal evolution there is a maximum mass of a moon that can survive for a given time T around a close-in exoplanet. To allow for a comparison with the known moons, we re-frame their analysis to ask: what are the physical and orbital requirements for a moon to host a stable submoon with specified properties?

Our paper is structured as follows. We present simple calculations of submoon survival in Section 2. We then discuss the long-term stability of submoons (Section 3) as well as their potential habitability (Section 4). We conclude in Section 5, and discuss why

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subsubmoons – moons orbiting submoons – can only exist at very small sizes.

2 TIDAL CALCULATIONS

Our goal is to map the parameter space in which submoons may be stable under the action of planet–moon–submoon tides. We follow Barnes & O'Brien (2002), who derived a simple analytical approach that applies across different outcomes of tidally driven migration. We adapt equation 8 of Barnes & O'Brien (2002) to derive the critical size of a moon R_{moon} that can host a long-lived submoon. We find that

$$R_{\text{moon}} \ge \left[\frac{39M_{\text{sub}}\,k_{2,\text{moon}}\,T\sqrt{G}}{2\,(4\pi\rho_{\text{moon}})^{8/3}\,Q_{\text{moon}}}\left(\frac{3M_{\text{p}}}{(f\,a_{\text{moon}})^3}\right)^{13/6}\right]^{1/3},\tag{1}$$

where M_{sub} is the (fixed) mass of the submoon in question, R_{moon} , a_{moon} , ρ_{moon} , Q_{moon} , and $k_{2,moon}$ are the moon's radius, orbital radius, bulk density, tidal quality factor, and tidal Love number, respectively, M_p is the planet mass, T is fixed at 4.6 Gyr, and G is the gravitational constant. A submoon's orbit is stable out to a fraction f of its moon's Hill sphere; Domingos, Winter & Yokoyama (2006) showed that $f \approx 0.4895$ for prograde, low-eccentricity orbits. Equation (1) has the advantage of simplicity while capturing the basic mechanisms at play. However, we note that it inherently assumes that the submoon on the moon's rotation, the influence of the moon on the planet's rotation and the effect of the initial moon and planet rotation; see Sasaki et al. (2012) and Piro (2018) for a more comprehensive treatment.

Fig. 1 shows the regions of parameter space where a longlived, 10 km-scale submoon could exist under the action of planetmoon-submoon tides (see caption for parameter choices). Only large moons on wide-separation orbits can host long-lived submoons. This is mainly because massive, distant moons have larger Hill radii that provide more stable volume for submoons. Most of the large regular moons of the giant planets are too close to their host planets to host submoons. This is the case for all of Uranus and Neptune's moons. If submoons did form in these systems, they have since been removed by tidally induced migration.

Remarkably, Jupiter (Callisto), Saturn (Titan and Iapetus), and Earth (Moon) each have the potential to host long-lived submoons around their current moons. Based on its orbital separation and inferred mass and size, the new exomoon candidate Kepler-1625b-I (Teachey & Kipping 2018) also appears capable of hosting a large submoon. However, it is worth noting that Kepler-1625b-I has a significant orbital inclination which may affect the stability of submoons (e.g. Tremaine, Touma & Namouni 2009; Tremaine & Yavetz 2014; Grishin et al. 2017). We encourage detailed studies of the dynamical stability of submoons in this system in particular, but also in the general case of inclined orbits where additional dynamical effects may play a role in long-term submoon stability.

We use the Kepler-1625b system to illustrate the effect of relevant system parameters. Assuming the orbit of its candidate moon to be coplanar, Fig. 2 shows the effect of the submoon size/mass and the tidal quality factor Q_{moon} on the parameter space available for long-lived submoons for an adopted system age of 9 Gyr (Teachey & Kipping 2018). Smaller submoons are stable over a broader range of moon radius and distance from their host planet than larger submoons. As expected from equation (1), the 'survivability space'

for submoons increases with increasing Q_{moon} , and for decreasing submoon mass and density. At face value the exomoon candidate Kepler-1625b-I could in principle host a Vesta- to Ceres-like submoon. This is consistent with the results of Reid (1973), who found that a factor of $\sim 10^{-5}$ in mass serves as a rough guideline for the potential stability of a long-lived submoon. Of course, it is not clear that such a submoon could survive in the face of other dynamical effects. Indeed, no such submoons have survived in the Solar system, which leaves the open question: did they form and get removed by other effects than we have considered here, or did they never form at all?

3 LONG-TERM SURVIVAL OF SUBMOONS

Our calculations show that submoons may remain stable to tidal evolution in orbit around Callisto, Iapetus, and the Moon. So why do those moons *not* host submoons?

The tidal-dynamical stability described in Section 2 is only one criterion for long-term survival of a submoon. Of course, for submoons to exist they must have a formation pathway. The large moons of the gas giants are thought to have formed in circumplanetary discs (e.g. Canup & Ward 2006; Cilibrasi et al. 2018) or by spreading of dense primordial ring systems (Charnoz, Salmon & Crida 2010; Crida & Charnoz 2012). Earth's large moon is thought to have formed via a giant impact (e.g. Benz, Slattery & Cameron 1986; Canup 2004), whereas Mars' small moons may have been captured or created after a large impact (see Rosenblatt 2011).

Even within a moon's presumably stable region there are other sources of dynamical instability that may remove submoons on certain orbits. For example, the Moon has been found to have localized mass concentrations within its crust (Muller & Sjogren 1968) that destabilize the orbits of very close orbits around the Moon (Konopliv et al. 2001). More broadly, a range of orbits around the Moon are destabilized by perturbations from the Sun and Earth (Lidov 1963; Scheeres 1998; Elipe, Mart-egrave & Lara 2003). Such perturbations are likely to play a role in destabilizing the orbits of submoons such that the available parameter space for submoon stability is more restricted than what we derived in Section 2. Detailed calculations of this are beyond the scope of this work, but we note further work must be done to investigate these effects in any realistic system.

If primordial moons did form around Callisto, Iapetus, or the Moon they must later have been removed. One mechanism for submoon removal is its host moon's tidally induced migration, during which a submoon's orbit may shrink or grow (Namouni 2010) and can become trapped in an unstable evection resonance (Spalding, Batygin & Adams 2016). In addition, if a moon underwent significant outward migration then its ability to host a primordial submoon depends on its initial orbital radius rather than its final one. For instance, the Moon is thought to have migrated outwards from just a few Earth radii (e.g. Goldreich 1966; Touma & Wisdom 1994). Yet submoons of the Moon would only have been stable once the moon was beyond \sim 30 Earth radii. Thus, the Moon could only host a very young submoon.

Iapetus's equatorial ridge may provide evidence for a past submoon. Levison et al. (2011) and Dombard et al. (2012) proposed that a collision produced a submoon orbiting Iapetus. Levison et al. (2011) argued that the submoon-generating collision also produced a closer belt of debris. The submoon tidally evolved outwards whereas the debris was tidally pushed inwards to create Iapetus' ridge. In contrast, Dombard et al. (2012) proposed that the ridge



Figure 1. Moons of moons – The parameter space in which the moon of a specified planet could host a long-lived submoon under the action of planet–moon– submoon tides. A submoon would be stable for at least the age of the Solar system in the shaded region to the upper right of each panel. The default size of the submoon is 10 km in radius (solid curves), and we also show the critical limits for submoons of 5 km (dotted) and 20 km (dashed) in radius. The solid dots are each planet's actual satellites. This calculation assumes that all moons have bulk densities of 2.5 g cm⁻³, appropriate for most large satellites of the giant planets. We assume tidal Love numbers $k_{2,moon} = 0.25$ (Moore & Schubert 2000), and tidal quality factor Q = 100 (Lainey 2016). We assumed that all submoons have densities of 2 g cm⁻³, generally appropriate for smaller bodies. For the case of the Earth we assumed a moon density of the Lunar density of 3.34 g cm⁻³. For the case of Kepler-1625b, we assumed a planet mass of 4 M_J (Teachey & Kipping 2018), $k_{2,moon} = 0.12$ (appropriate for the ice giants; Gavrilov & Zharkov 1977) and a very uncertain Q_{moon} of 1000 (see Lainey 2016).

was created by the tidal in-spiralling and shredding of the submoon itself. It has also been proposed that primordial submoons of Earth's moon were destabilized and crashed into the Moon (Reid 1973; Conway 1986).

Dynamical interactions between moons could also have a destabilizing effect on submoons. Secular perturbations in compact planetary systems decrease the stability radius for moons, effectively decreasing the critical distance for satellite stability to $f \approx 0.4$ (Payne et al. 2013). By analogy, submoons could have less stable volume in multiple-moon systems, although we do not expect these effects to dominate, particularly at late times. In addition, dynamical scattering events between planets often destabilize the orbits of host

moons (Gong et al. 2013; Hong et al. 2018; Rabago & Steffen 2018). Moon-moon scattering events may be common in satellite systems (Perets & Payne 2014), particularly at early times, and may serve to destabilize submoons. Further calculations beyond the scope of this work are required to determine the amplitude of these effects for different primordial scenarios.

4 POTENTIAL HABITABILITY OF SUBMOONS AND OTHER SPECULATIVE SCENARIOS

Moons of gas giant planets have long been considered potential sites for extant life (Williams, Kasting & Wade 1997; Scharf 2006; Heller



Figure 2. Effect of the submoon size (left) and moon tidal quality factor Q_{moon} (right) on the ability of a moon to host a long-lived submoon. Submoons are long-term stable above and to the right of each curve. We assume $M_p = 4M_J$ (Teachey & Kipping 2018), $k_{2,\text{moon}} = 0.12$ (Gavrilov & Zharkov 1977), and T = 9 Gyr (Teachey & Kipping 2018). In the left-hand panel Q_{moon} is fixed at 1000 and in the right-hand panel the submoon is fixed at Ceres' size and mass.

et al. 2014; Forgan 2018). One may then wonder: *can submoons be habitable*?

If plate tectonics and a long-lived atmosphere are prerequisites for habitability, then there may be a lower limit on the mass of potentially habitable world. Williams et al. (1997) derived a rough lower limit of 0.23 M_{\oplus} (see also Raymond, Scalo & Meadows 2007). At twice the mass of Mars, this is far more massive than any submoons that appear to be stable around any Solar system moons or the Kepler-1625b-I exomoon candidate (see Figs 1 and 2).

How can we imagine a habitable system in which a large submoon is stable to tides? From equation (1) we can see that the mass of the maximum stable submoon $M_{\rm sub,max} \propto M_{\rm moon} Q_{\rm moon} (a_{\rm moon}^3/M_{\rm p})^{13/6}$. This is sensible: submoons should survive longer when tides are weak. Given the very strong scaling of tidal evolution with separation (e.g. Goldreich & Soter 1966; Ferraz-Mello et al. 2008), this implies that large-scale systems are the most likely to host large submoons. Submoons also are more likely to exist around moons on wide orbits around their planets that have large Hill spheres. Of course, the widest possible moon orbit is linked with a planet's Hill sphere such that, if we invoke a moon that orbits at a fixed fraction of its parent planet's Hill sphere, then $M_{\rm sub,max} \propto \left(a_{\rm p}^3/M_{\star}\right)^{13/6}$, where M_{\star} is the stellar mass. If we require the planet to be located in its host star's circumstellar habitable zone, scaled simply as $a_{\rm Hz} = 1 \text{au} \sqrt{L/L_{\odot}}$ (Kasting, Whitmire & Reynolds 1993; Selsis et al. 2007; Kopparapu et al. 2013), then can use the known stellar mass-luminosity relationship $(L_{\star}/L_{\odot}) \propto (M_{\star}/M_{\odot})^{\alpha}$, where α ranges from 2 to 4 for the main sequence stars of interest, to set the boundaries within which the submoon can be both dynamically long-lived and habitable:

$$M_{\rm sub,max,Hz} \propto \left(a_{\rm Hz}^3/M_{\star}\right)^{13/6}$$
 (2)

$$\propto M_{\star}^{\left(\frac{13\alpha}{4}-\frac{13}{6}\right)}.$$
(3)

This implies that the maximum submoon mass is a very strong function of the stellar mass (e.g. for $\alpha = 4$, $M_{\text{sub,max,HZ}} \propto M_{\star}^{65/6}$). This is a consequence of the strong scaling of tidal effects, compounded with the physical size of satellite systems. For more massive stars, the habitable zone is more distant and habitable zone planets have wider Hill spheres. Large moons can therefore survive on more distant orbits and have larger Hill spheres such that submoons can exist on wider orbits where submoon-moon-planet tidal evolution is far slower, as compared with lower mass stars.

The arguments above only apply if moons' orbital radii scale with their host planets' Hill radii. If, on the other hand, the orbital separations of moons is governed by a different process such that moons' orbital radii are independent of their planets' Hill radii, then the maximal submoon mass would be more or less independent of the stellar mass.

Our study also opens the tantalizing subject of the largest object that could be built (presumably by humans) around the Earth's moon and remain stable: a non-natural submoon. Such an outpost may be long-lived, provided its orbit is dynamically stable, and reasonably sized. We can calculate the maximum potential size of our non-natural submoon in a similar manner as above, although information about the material properties of such a structure would be required. Similarly, more sophisticated analysis would be required to determine the viability of such a structure from a materials point of view.

5 CONCLUSIONS

We have shown that, in the face of tidal evolution, submoons can only survive around massive moons on wide orbits around their host planets. We acknowledge the pioneering paper of Reid (1973), who was the first, to our knowledge, to study the stability of submoons under the effect of tides, and who derived an approximate mass ratio of 10^{-5} for the mass of a long-lived submoon. Our calculations are consistent with those results.

Given that some moons do appear capable of hosting submoons, one may further wonder whether submoons could host their own satellites, or *subsubmoons*. Using Reid (1973)'s rule of thumb, a subsubmoon would have to be less than roughly 10^{-5} times the submoon's mass. For the case of the exomoon candidate Kepler-1625b-I (Teachey & Kipping 2018) we showed in Fig. 2 that the largest stable submoon is Vesta- to Ceres-sized. The largest possible submoon would thus be roughly 5–10 km in radius. For much less massive, Solar system-like moons the largest stable submoon was ~10 km such that the largest possible subsubmoon would be sub-km-sized.

To conclude, we note that while many planet-moon systems are not dynamically able to host long-lived submoons, the absence of submoons around known moons and exomoons where submoons *can* survive provides important clues to the formation mechanisms and histories of these systems. Further studies of the potential formation mechanisms, long-term dynamical survival, and detectability of submoons are encouraged.

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