

Self-energies in itinerant magnets: A focus on Fe and Ni 2

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Self-energies in itinerant magnets: A focus on Fe and Ni

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We present a detailed study of local and nonlocal correlations in the electronic structure of elemental transition metals carried out by means of the quasiparticle self-consistent GW (QSGW) and dynamical mean field theory (DMFT). Recent high resolution ARPES and Haas-van Alphen data of two typical transition metal systems (Fe and Ni) are used as a case study. (i) We find that the properties of Fe are very well described by QSGW. Agreement with cyclotron and very clean ARPES measurements is excellent, provided that final-state scattering is taken into account. This establishes the exceptional reliability of QSGW also in metallic systems. (ii) Nonetheless QSGW alone is not able to provide an adequate description of the Ni ARPES data due to strong local spin fluctuations. We surmount this deficiency by combining nonlocal charge fluctuations in QSGW with local spin fluctuations in DMFT QSGW+"magnetic DMFT". (iii) Finally we show that the dynamics of the local fluctuations are actually not crucial. The addition of an external static field can lead to similarly good results if nonlocal correlations are included through QSGW.

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High-resolution spectroscopy is limited in transition met-25 als, in part because it is difficult to make sufficiently 26 high quality samples. Fe and Ni are elements of which 27 high quality films have been grown, and high-resolution 28 angle-resolved photoemission spectroscopy (ARPES) per-29 formed [1]. These experiments provides a good reference to 30 test the validity of different approximations of the electronic 31 structure. 32

There are also not many calculations of spectral func-33 tions in these materials. Fe has been studied in the local-34 density approximation (LDA) [2] and with corrections through 35 dynamical-mean field theory (DMFT) [3]. It is not surprising 36 that the LDA does not track the ARPES experiment well [4], 37 but it has been found that LDA+DMFT also fails to properly 38 account for ARPES data [3]. The GW approximation [5] is 39 widely applied to many kinds of insulators, but how well it 40 describes 3d transition metals is much less established. 41

Through quasiparticle self-consistency (QSGW) one de-42 termines the noninteracting Green's function G_0 which is 43 minimally distant from the true Green's function G [6–8]. 44 Within QSGW many electronic properties are in excellent 45 agreement with experiment [6], most notably the quasiparticle 46 band structures. Moreover, at self-consistency the poles of 47 QSGW $G_0(\mathbf{k},\omega)$ coincide with the peaks in $G(\mathbf{k},\omega)$. This 48 means that there is no many-body "mass renormalization" 49 of the noninteracting Hamiltonian, which allows for a direct 50 association of QSGW energy bands $E(\mathbf{k})$ with peaks in the 51 52 spectral function $A(\mathbf{k},\omega)$. Thus, QSGW provides an optimum framework to test the range of validity and the limitations to 53 the GW approximation. 54

In this Rapid Communication, we compare QSGW results 55 to various experimental data in elemental 3d materials in the 56 Fermi liquid (FL) regime, with a heavy focus on Fe because 57 of the high quality of ARPES [1] and de Haas-van Alphen 58 (dHvA) [9,10] data available. We will show that QSGW $_{59}$ and ARPES spectral functions agree to within experimental 60 resolution, with the proviso that the final state scattering 61 is properly accounted for in interpreting the experimental 62 data. By contrast, discrepancies appear in Ni-a classical 63 itinerant ferromagnet. This can be attributed to the lack of spin 64 fluctuations in GW diagrams. However we find out that there 65 is no need to include finite-energy spin fluctuations, instead 66 a static correction to the QSGW self-energy is sufficient to 67 correct for the size of the local moment. This findingopens 68 up an avenue to test the validity of a similar argument for 69 other transition metals. The LDA or LDA+DMFT should be 70 problematic, as nonlocality in the self-energy can be important 71 (see Supplemental Material). 72

I. FE IN THE FERMI LIQUID REGIME

Figure 1 compares the calculated QS*GW* band structure of ⁷⁴ Fe to peaks in ARPES spectra of Ref. [1], along with some ⁷⁵ inverse photoemission data [11]. While agreement appears ⁷⁶ to be very good, there are some discrepancies, particularly ⁷⁷ along the Γ -H line [see also Fig. 2(a)]. As noted earlier, the ⁷⁸ QS*GW* band structure reflects the peaks of $A(\mathbf{k},\omega)$ with no ⁷⁹ renormalizations from the ω or \mathbf{k} dependence of Σ .

In the FL regime, ARPES spectra $I(\mathbf{k},\omega)$ are generally ⁸¹ thought to be a fairly direct measure of $A(\mathbf{k},\omega)$. But the two ⁸²

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FIG. 1. Left: QSGW band structure of Fe (solid lines), LSDA (gray dashed), *k*-point averaged QSGW (black dotted, see text), ARPES spectra [1] (diamonds), and inverse photoemission spectra [11] (squares). Right: Fermi surface. Symbols denote FS crossings reported in Ref. [1]. Red and green depict majority and minority *d* character, respectively.

⁸³ are not identical even in the FL regime, independently of the precision of the experimental setup. Assuming a one-step model [12] for the photoemission process (initial and final state coupled through Fermi's golden rule [12,13]) $I(\mathbf{k},\omega)$ can be written as

$$I(\mathbf{k},\omega) \propto \int dk_{\perp} |T_{fs}|^2 |M_{fi}(\mathbf{k}_{\perp})|^2 A_f(\mathbf{k}_{\perp}) A(\mathbf{k},\omega),$$

where $A_f(\mathbf{k}_{\perp}) = \frac{\Delta k_{\perp}/2\pi}{(\Delta k_{\perp}/2)^2 + (k_{\perp} - k_{\perp}^0)^2}$ (1)

⁸⁸ is the spectral function of the final state, broadened by scat-⁸⁹ tering of the photoelectron as it approaches the surface [14]. ⁹⁰ T_{fs} is the final-state surface transmission amplitude and M_{fi} ⁹¹ the photoexcitation matrix element (taken to be constant and



FIG. 2. (a) The Γ -H line of Fig. 1 in high resolution. Labels correspond to traditional assignments of Fermi surface pockets [1,9]. (b) Dashed line is QSGW spectral function $A(k,\omega)$ for various points on the Γ -H line, with k = 0 and k = 1 denoting Γ and H. Solid line is $A(\omega)$ modified according to Eq. (1). (c) The analog of (b) at $k = 0.77 \times H$ where the I_M band crosses E_F . E_{QP} indicates the QSGWQP level, and E_{ARPES} the experimental ARPES peak at 0.77H. (d). dispersion in the QSGW II_M band on a line $\mathbf{k}_{\perp} + [0,0,0.77H]$ normal to the film surface.

PHYSICAL REVIEW B 00, 001100(R) (2017)

k independent [15]). Thus the final state is considered to ⁹² be a damped Bloch wave, taking the form of a Lorentzian ⁹³ distribution centered in k_{\perp}^{0} and broadened by $\Delta \mathbf{k}_{\perp}$ [14], ⁹⁴ while the initial state is an undamped Bloch function with an ⁹⁵ energy broadening ΔE , obtained through the QS*GW* spectral ⁹⁶ function. This approximation is reasonable since in the FL ⁹⁷ regime $A(\mathbf{k},\omega)$ is sharply peaked around the QP level. $\Delta \mathbf{k}_{\perp}$ ⁹⁸ is directly related to the inverse of the electron mean free ⁹⁹ path. For photon energy in the range 100–130 eV, $\Delta \mathbf{k}_{\perp} \approx 100$ 0.2 Å^{-1} [16,17].

The final-state scattering broadens $I(\omega)$, but it also can 102 shift the peak $\bar{\omega}$ in $I(\omega)$. The most significant discrepancy 103 between ARPES and QSGW is found in the V_m band, Fig. 2(a) 104 between k = 0 and $0.4 \times H$. Figure 2(b) shows $A(\mathbf{k}, \omega)$ 105 calculated by QSGW, and the corresponding $I(\mathbf{k},\omega)$ calculated 106 from Eq. (1). Estimating the peak shift change from $\delta \bar{\omega} = 107$ $\int d\omega \,\omega I / \int d\omega I - \int d\omega \,\omega A / \int d\omega A$, we find $\delta \bar{\omega} < 0.01 \text{ eV}$ 108 at Γ , increasing to $\delta \bar{\omega} \approx 0.06$ eV for k between 0.1H and 109 0.3H. $\delta \bar{\omega} = 0.06$ eV tallies closely with the discrepancy 110 between the V_m band and the measured ARPES peak for 111 0.1H < k < 0.3H. There is also a significant discrepancy in 112 the II_M band near $k = 0.77 \times H$. Where it crosses E_F , the 113 QSGW bands deviate from the ARPES peak by nearly 0.15 eV. 114 But ARPES simulated by Eq. (1) is much closer to experiment 115 [Fig. 2(c)]. This is understood from Fig. 2(d), which plots the 116 QSGW dispersion along a line $\Delta \mathbf{k}_{\perp}$ normal to the film surface, 117 passing through [0,0,0.77H]. A measurement that includes 118 contributions from this line biases the ARPES peak in the 119 direction of E_F since E_{qp} is minimum at $k_{\perp}=0$. Thus we 120 attribute most of the discrepancy in the Fermi surface crossing 121 [red star in Fig. 1(b)] to an artifact of final-state scattering. 122

To better pin down the errors in QSGW, we turn to de 123Haas-van Alphen (dHvA) measurements. Extremal areas of 124 the FS cross sections can be extracted to high precision from 125 dHvA and magnetoresistance experiments. Areas normal to 126 [110] and [111] are given in Table I, along with areas calculated 127 by QSGW. Figure 1 shows the QSGW Fermi surface, which 128 closely resembles the one inferred by Lonzarich (version 129 B) [19]. There is some ambiguity in resolving the small VIII_{m 130} pocket at N because its tiny area is sensitive to computational ¹³¹ details. Discrepancies in the extremal areas are not very 132 meaningful: It is more sensible to determine the change ΔE_{F} 133 in Fermi level needed to make the QSGW area agree with 134 dHvA measurements. This amounts to the average error in the 135 OSGW OP levels, assuming that the bands shift rigidly. This 136 assumption is well verified for all pockets, except for the small VI one owing to strong electron-phonon coupling [20]. 138

Some limited cyclotron data for effective masses are also available [18], which are expected to be more reliable than 140 ARPES data. It is seen that agreement is excellent (Table I, 141 bottom panel) except for the small VI pocket. We get a better comparison by accounting for the electron-phonon coupling 143 with a simple model [20,21]. From the model, v_F is renormalized by a factor $1+\lambda = 1.6$, which reasonably accounts 145 for discrepancy between the QS*GW* and the cyclotron mass in 146 pocket VI. The other pockets are much larger [Fig. 1(b)], making v_F much larger on average and the renormalization smaller. 148

Such a perfect agreement with experiments could not $_{149}$ be possible without the accurate description of nonlocal $_{150}$ components in the QSGW self-energy. To prove this statement $_{151}$

SELF-ENERGIES IN ITINERANT MAGNETS: A FOCUS ...

PHYSICAL REVIEW B 00, 001100(R) (2017)

FS pocket	dHvA [110]			dHvA [111]		
	QSGW	expt. [9]	ΔE_F	QSGW	expt. [9]	ΔE_F
Ι	3.355	3.3336	0.01	3.63	3.5342	0.04
II				3.694		
III	0.2138	0.3190	0.05	0.1627	0.2579	0.06
IV	0.0897	0.1175	0.04	0.0846	0.1089	0.02
VI	0.3176	0.5559	-0.13	0.2799	0.4986	-0.14
VII	0.0148	0.0405	0.04			
	<i>m*/m</i> [110]			<i>m*/m</i> [111]		
	QSGW	LDA	expt. [18]	QSGW	LDA	expt. [18]
Ι	2.5	2.0	2.6			-
V				-1.7	-1.2	-1.7
VI				2.0	1.5	2.8

TABLE I. de Haas-van Alphen measurements of extremal areas A on the [110] and [111] Fermi surfaces, in Å⁻². ΔE_F is an estimate of the error in the QP level (eV), as described in the text. Bottom panel: cyclotron mass, $m^*/m = (\hbar^2/2\pi m) \partial A/\partial E$.

we computed the band structure with a local potential obtained 152 from a k-point average of the QSGW self-energy. The result is 153 reported as a dotted black curve in Fig. 1, to be compared with 154 the pale gray lines of LSDA and the solid lines of QSGW. 155 The k-averaged potential reproduces a band structure that 156 is much closer to the LSDA one than to the QSGW results. 157 This results in the overestimation of the binding energy, 158 e.g., of most states close to Fermi (for instance at Γ), or in 159 the range between -2 and -3 eV (see at Γ , P, and H). An 160 additional verification that local physics is not relevant in the 161 description of the quasiparticle structure of Fe can be found 162 in the Supplemental Material [20]. 163

164 II. NI: AN ARCHETYPICAL ITINERANT MAGNET

Less detailed information is available for other elemental 165 transition metals. We have extracted some experimental band-166 widths and also the exchange splitting ΔE_x in the magnetic 167 elements. Figure 3(a) shows that both seem to be very well 168 described by QSGW, except that ΔE_x deviates strongly from 169 experiment in Ni. QSGW significantly improves not only on 170 the LSDA, but also on fully self-consistent GW[22] because of 171 loss of spectral weight in fully self-consistent G that is avoided 172 in OSGW[6]. 173

Figure 4(a) compares the QS*GW* band structure of Ni to ARPES data [23]. Agreement is excellent in the minority



FIG. 3. (a): *d* bandwidth (top panel) and exchange splitting ΔE_x (bottom panel) in the 3*d* elemental metals. (b): Magnetic moment of several compounds

channel, but ΔE_x is uniformly too large on the symmetry 176 lines shown. Also the band near -1 eV at L (consisting of *s* 177 character there) is traditionally assumed to be a continuation 178 of the *d* band denoted as white and green diamonds, but the 179 calculations show that at it is a continuation of the Ni *s* band. 180 The corresponding LSDA band (light dotted lines) crosses L 181 at E_F -0.44 eV; also the *d* bands are much wider. 182

 ΔE_x is about twice too large in both QSGW and the LSDA, and for that reason spin wave frequencies are also too large [24]. Spin fluctuations $\langle M^2 \rangle$ are important generally in itinerant magnets but they are absent in both LSDA and QSGW. One important property they have is to reduce the average magnetic moment $\langle M \rangle$ and hence to quench ΔE_x [25,26]. Figure 3(b) shows this trend quite clearly: Systems such as Fe, Co, and NiO are very well described by QSGW, but Mis always overestimated in itinerant magnets such as FeAl, Ni₃Al, and Fe based superconductors such as BaFe₂As₂. Ni is



FIG. 4. (left) Band structure of Ni in QSGW (solid lines) and LDA (dotted) and ARPES data [23] (the circle at -1.3 eV was taken from Ref. [27]). Red arrows highlight the discrepancy in the exchange splitting ΔE_x at near L and X. (right) QSGW+LSDMFT bands (solid) and QSGW+B^{eff} (dashed). (inset) ΔE_x at L as a function of M obtained by adding an external magnetic field to the QSGW or LSDA potential (see text).

TABLE II. Magnetic moment *M* and exchange splitting ΔE_x for the different levels of the theory (see text) against experiment.

	M (Bhor)	$\Delta E_x @ L (eV)$
LSDA	0.62	0.71
QSGW	0.75	0.77
QSGW+DMFT	0.51	0.30 ^a
QSGW+SLDMFT	0.53	0.30
$QSGW + B^{eff}$	0.57	0.32
Experiment	0.57	0.31

^aValue estimated from Maximum entropy analytic continuation.

¹⁹³ also itinerant to some degree (unlike Fe, its average moment ¹⁹⁴ probably disappears as $T \rightarrow T_c$), and its moment should be ¹⁹⁵ overestimated. This is found to be the case for QS*GW*, as ¹⁹⁶ Fig. 3(b) shows.

Local spin fluctuations are well captured by localized 197 nonperturbative approaches such as DMFT. We can reasonably 198 expect that the addition of spin-flip diagrams to QSGW would 199 be sufficient to incorporate these effects. A G_0W_0 +DMFT 200 study of ferromagnetic Ni can be found in Ref. [28], but the 201 dependency of $G_0 W_0$ on the starting point, together with all 202 the advantages mentioned at the beginning, motivated us to 203 devise a QSGW-based approach. 204

Here we adopt an implementation merging QSGW with 205 DMFT. We adapted Haule's continuous time quantum Monte 206 Carlo solver [29,30] with the projection and embedding 207 schemes described in Ref. [31], and which are outlined in 208 the Supplemental Material [20]. In this sense, this method is 209 close to the one introduced by some of us in [32], but based 210 on a different self-consistent scheme for the solution of the 211 weakly correlated part. 212

The fully consistent QSGW+DMFT calculation is com-213 posed by alternately repeated DMFT and QSGW loops. First 214 the QSGW Green's function is converged at fixed density, 215 then it is projected on the Ni d orbitals and finally, within the 216 DMFT loop, the local self-energy is obtained. Updating the 217 total density with the locally corrected Green's function and 218 repeating the procedure leads to complete self-consistency. 219 This method fully takes into account the dynamics of the local 220 spin fluctuations included in the DMFT diagrams. Results are 221 reported in Table II and they confirm that DMFT adds the 222 correct local diagrams missing in the OSGW theory. Moreover 223 by carefully continuing the resulting Green's function on the 224 real-frequency axis, we find an exchange splitting of ~ 0.3 eV 225 and a satellite at $\sim 5 \text{ eV}$ [20]. 226

In order to investigate the importance of the dynamics in 227 the local spin-spin channels, we carry out a QSGW+DMFT 228 calculation by retaining only the static limit of the DMFT 229 loop (we call it QSGW+"SLDMFT"). Once the DMFT loop 230 converges, we take the zero frequency limit of the magnetic 231 part of the DMFT self-energy and add it to the spin-averaged 232 QSGW Hamiltonian [20]. As it is clearly shown in Table II 233 and Fig. 4, this static Hamiltonian reproduces very accurately 234 magnetic moment and details of the band structure. This 235 is a strong indication that for Ni the dynamics of local 236 spin fluctuations is not crucial. This will be the case if the 237 quasiparticle picture is a reasonable description of Ni, even 257

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PHYSICAL REVIEW B 00, 001100(R) (2017)

if QSGW alone does not contain enough physics to yield an ²³⁹ optimum quasiparticle approximation. ²⁴⁰

To verify this further, we model spin fluctuations by 241 carrying out the QSGW self-consistent cycle in the presence 242 of a magnetic field B^{eff} , and tuning B^{eff} to reduce M (see 243) inset, Fig. 4) Our key finding is that when B^{eff} is tuned to 244 make M agree with experiment, ΔE_x does also, reproducing 245 ARPES spectra to high precision in the FL regime, as clearly 246 reported in Fig. 4 and Table II. Both the OSGW and LSDA 247 overestimate M for itinerant systems, but the latter also 248 underestimates it in local-moment systems [Fig. 3(b)]. In the 249 LSDA treatment of Ni, these effects cancel and render the 250 moment fortuitously good. When spin fluctuations are folded 251 in through B^{eff} , the LSDA moment becomes too small. This 252 finding must be interpreted as a sign of the superior level 253 of internal consistency in the QSGW theory with respect to 254 LSDA. Without such a degree of consistency spin fluctuations 255 could not be approximated by a static field. 256

III. CONCLUSIONS

We have performed detailed QSGW calculations of the 258 electronic band structure of several 3d metallic compounds to 259 assess the reliability of this theory in the Fermi liquid regime and the importance of the nonlocal terms in the self-energy. 261

—Fe: Through de Haas-van Alphen and cyclotron measurements we established that QS*GW* QP levels at E_F have an error of ~0.05 eV, and effective masses are well described. Comparable precision is found below E_F by comparing to ARPES data, provided final state scattering is taken into account. The QS*GW d* bandwidth falls in close agreement with ARPES and is approximately 0.75 times that of the LDA (Fig. 1).

If Σ is *k*-averaged to simulate a local self-energy, the QSGW ²⁷⁰ band structure changes significantly and resembles the LDA. ²⁷¹ Thus nonlocality in the self-energy is important in transition ²⁷² metals, and its absence explains why LDA+DMFT does not ²⁷³ yield good agreement with ARPES [3]. ²⁷⁴

-Ni: QSGW d bandwidths, the $t_{2g}-e_g$ splitting, the s-d 275 alignment, are all in excellent agreement with experiment, 276 while $\langle M \rangle$ and ΔE_x are too large. However through the 277 addition of a uniform static external field QSGW can give 278 both in good agreement, indicating a high level of consistency 279 in the theory, contrary to LSDA in which it is not possible to 280 have both quantities correct at the same time. 281

To account for spin fluctuations in an *ab initio* framework, ²⁸² we constructed a QS*GW*+DMFT implementation and we ²⁸³ utilized it at different degrees of approximations demonstrating ²⁸⁴ that in itinerant magnets as Ni (i) the dynamics of fluctuations ²⁸⁵ is irrelevant and (ii) their effect can be very well approximated ²⁸⁶ by a static field as long as the nonlocal correlation part is ²⁸⁷ treated accurately. ²⁸⁸

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PHYSICAL REVIEW B 00, 001100(R) (2017)

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Supplementary material for Self-energies in itinerant magnets: A focus on Fe and Ni

SURVEY ON THE QSGW THEORY

Quasiparticle self-consistency is a construction that determines the noninteracting Green's function G_0 that is minimally distant from the true Green's function G. A measure of distance, or metric is necessary; a good choice [1] results in an effective static potential:

$$\bar{\Sigma}^{\rm xc} = \frac{1}{2} \sum_{ij} |\psi_i\rangle \left\{ \operatorname{Re}[\Sigma(\varepsilon_i)] + \operatorname{Re}[\Sigma(\varepsilon_j)]_{ij} \right\} \langle \psi_j|.$$
(1)

 $\Sigma_{ij}(\omega)$ is the self-energy in the basis of single-particle eigenstates $|\psi_i\rangle$, which becomes iG_0W in the GW approximation. Starting from a trial G_0 , e.g. the LDA, $\bar{\Sigma}^{\mathrm{xc}}$ is determined through GW, which determines a new G_0 . The cycle is repeated until self-consistency.

Recently Ismail-Beigi showed that Eq. 1 also minimizes the gradient of the Klein functional, $|\delta F|^2$, where F is evaluated in the subspace of all possible static $\bar{\Sigma}^{\text{xc}}$ [2].

Another key property of Eq. 1 is that, at selfconsistency, the poles of $G_0(\mathbf{k}, \omega)$ coincide with the peaks in $G(\mathbf{k}, \omega)$. Therefore the band structure generated by V^{xc} coincides with the peaks of the specral function $A(\mathbf{k}, \omega)$. This is significant, because it means there is no many-body "mass renormalization" of the noninteracting hamiltonian. In other words, the attribution of mass renormalization to correlation effects, a concept widely used in the literature [3], is ill-defined: it depends on an arbitrary reference, e.g. the LDA. The absence of mass renormalization is a very useful property: we can directly associate QS*GW* energy bands $E(\mathbf{k})$ with peaks in the spectral function $A(\mathbf{k}, \omega)$.

ELECTRON-PHONON RENORMALIZATION OF EFFECTIVE MASSES

In comparing the areas of electron pockets in the Fermi surface of Fe, we pointed out the small discrepancy between measured and simulated values. As a measure of the discrepancy we provide the rigid shift of the Fermi energy that would lead the computed area to equate the measured one (see Table II in main text). This measure is justified under the assumption that QSGW shift rigidly, which is actually not the case for pocket VI, for which the agreement is poorer.

According to a Thomas-Fermi model of screening [4], the electron-phonon interaction renormalizes v_F by a factor $1+\lambda$. Band VI is roughly spherical, enabling us to evaluate λ analytically:

$$\lambda = \frac{e^2}{\hbar v_F} \left[\frac{1}{2} \ln \frac{k_{TF}^2}{k_{TF}^2 + k_F^2} + \frac{k_F}{k_{TF}} \arctan \frac{k_F}{k_{TF}} \right] \qquad (2)$$

Estimating $k_F = 1.71$ Å⁻¹ from the Fe electron density, this leads to a renormalization factor of 1.6.

Remembering that $v_F \propto 1/m^*$, we can compare this factor with the ratio $m^*_{\rm QSGW}/m^*_{\rm exp} = 1.4$, which is close to the estimated contribution from the electron-phonon interaction.

COMPUTATIONAL DETAILS

QSGW

For the high resolution needed here, computational conditions had to be carefully controlled.

In both QS*GW* calculations of Fe and Ni, a k mesh of $12 \times 12 \times 12$ divisions was found to be sufficient for calculating Σ . The one-body part was evaluated on a $24 \times 24 \times 24$ mesh.

Fe 3p and 4d states were included through local orbitals: omitting these and treating 3p as core levels [1] can shift QP levels by as much as 0.1 eV in the FL regime. Other parameters [1], such as broadening the pole in G in constructing $\Sigma = iGW$, the basis of eigenfunction products, and the energy cutoff for the off-diagonal parts of Σ , were also carefully monitored. When set to tight tolerances QP levels near E_F were stable to a resolution of 0.05 eV. QP levels are calculated including spin-orbit coupling (SOC), though it is omitted in the calculation of Σ . The effect of SOC on Σ was found to make small changes to $\overline{\Sigma}^{\text{xc}}$.

Similar parameters were used in the $\mathrm{QS}\, GW$ calculation for Ni.

Our QSGW+DMFT implementation

Concerning the QSGW+DMFT calculation on Ni, we projected the lattice problem on the Ni *d* orbitals following the prescription of Haule [5]. We compute higher level diagrams locally using the hybridization expansion version of the numerically exact continuous time QMC method [6, 7].

In order to single out the correlated subspace, a procedure of projection/embedding which was originally introduced in [5] in the LAPW basis of the Wien2k package, is developed in the Full-Potential Linear Muffin-Tin Orbitals (FP-LMTO) basis [8]. This projector maps the full space Green's function G_{ijk} (with band and k-point label $\{ijk\}$) to the local Green's function $G_{LL'}^{loc}$ defined only on the correlated subspace. The compact index $L := \{\tau, R, \sigma, \ell, m\}$, collects information on the atom type τ , site R, spin coordinate σ , and angular momentum components ℓ and m. The projection operation can be cast in the following form:

$$G_{LL'}^{\text{loc}} = \sum_{\mathbf{k},ij} U_{i\mathbf{k}}^L G_{ij\mathbf{k}} U_{j\mathbf{k}}^{L'^{\dagger}} \quad \text{with} \quad U_{i\mathbf{k}}^L \propto \sum_u \mathcal{A}_{i\mathbf{k}}^L \Phi_{R\ell}^u ,$$

where the coefficients $\mathcal{A}_{i\mathbf{k}}^{L}$ account for localization inside the sphere, while $\Phi_{R\ell}^{u}$ gives an estimate of correlations relative to the specific orbital component ℓ . More specifically $\mathcal{A}_{i\mathbf{k}}^{L}$ are linear combinations of spherical harmonics $Y_{\ell m}$ and the QS*GW* quasiparticle eigenfunctions in the FP-LMTO basis. The terms $\Phi_{R\ell}^{u}$ are radial integral of the kind $\langle \varphi_{R\ell}^{u} | \varphi_{R\ell} \rangle$ where the index u in $\varphi_{R\ell}^{u}$ indicates the possibility of selecting the radial solution $\varphi_{R\ell}$ of the Schrödinger equation inside the MTO, its energy derivative $\dot{\varphi}_{R\ell}$, and its local orbitals contributions $\varphi_{R\ell}^{z}$ [1]. By means of these definitions we ensure that the localized orbitals are centred on the correlated atom corresponding to the muffin-tin site *R*.

The transformation matrices U have been orthonormalised in such a way that $\sum_{i\mathbf{k}} U_{i\mathbf{k}}^L U_{i\mathbf{k}}^{L'^{\dagger}} = \delta_{LL'}$. The local Green's function is defined on a grid of Mat-

The local Green's function is defined on a grid of Matsubara frequencies $i\omega_n = i\pi(2n+1)/\beta$ and it is employed to calculate the hybridization function of the system, which feeds the CTQMC impurity solver. The result of the impurity solver is the local impurity self-energy $\Sigma_{LL'}^{\text{loc}}(i\omega_n)$ also defined on the Matsubara axis. In order to update the full Green's function $G_{ij\mathbf{k}}$ with this local self-energy, so to iterate the DMFT loop to selfconsistency, an embedding procedure is needed. Because of the specific properties of the transformation U, the embedding procedure $\Sigma_{ij\mathbf{k}}^{\text{loc}}(i\omega_n) = \sum_{LL'} U_{i\mathbf{k}}^{L\dagger} \Sigma_{LL'}^{\text{loc}}(i\omega_n) U_{j\mathbf{k}}^{L'}$ can be operated by means of the same matrices, even though this is not a general requirement of the theory [5].

The charge double-counting contribution has been included by means of the standard formula

$$E_{dc} = U(n - 1/2) - J(n/2 - 1/2)$$

where n is the nominal occupancy of the 3d shell.

Analytical continuation through Maximum entropy

The output of the DMFT loop is the impurity selfenergy $\Sigma_{LL'}^{\text{loc}}(i\omega)$ and the corresponding impurity Green's function $\mathcal{G}_{LL'}(i\omega)$. At self-consistency they correspond to the local self-energy and local Green's function of the correlated subset (*d*-electrons of the metal in this case).

Though, since the CTQMC solver works in the Matsubara's frequency space extrapolations to zero-energy or some kind of analytical continuation has to be employed to extract physically meaningful quantities.

We evaluated the scattering rate from the intercept at $\omega = 0$ of a forth-order polynomial obtained from a fit of $\text{Im}\Sigma_{LL'}^{\text{loc}}(i\omega)$ in the vicinity of $\omega = 0$. The coefficient C_1 of

the linear term is then related to the quasiparticle weight $\mathcal{Z} = 1/(1+C_1)$. The intercept being Γ/\mathcal{Z} where Γ is the scattering rate, we have been able to evaluate Γ between 10^{-3} and 10^{-4} for both Fe and Ni, corresponding to a coherent charge-scattering regime.

The spectral function of the correlated subset can be obtained by continuing on the real-frequency axis the quantity $A(i\omega) = -\text{Im}G_{LL'}(i\omega)/\pi$. In order to do that, we utilised a statistical technique based on the Maximum Entropy Method [9]. As model function we used the magnetic QS*GW* spectral function of the *d* orbitals.

The resulting spectral function $A(\omega)$ contains all the effects of the dynamical local response including features beyond the quasiparticle peaks, as satellites at higher energy. This is indeed the case for Fe, reported in Figures 2.

Applications to Ni

In our application to Ni, the projectors used for the Ni 3d are constructed from 5 bands below E_F and 3 bands above E_F , which correspond to a window of $\sim \pm 10$ eV. By choosing a wide energy window, U becomes nearly static [10]. The corresponding on-site Coulomb parameters were chosen to be U=10 eV and J=0.9 eV, as calculated by constrained RPA [10]. The Matsubara frequency grid is defined over 2000 points with an inverse temperature $\beta = 50$ eV⁻¹.

In the case of Ni we applied the method at two different degrees of approximation.

Standard procedure: We first perform a full QSGW loop. Then we extract the spin-averaged Green's function from which the local hybridization function $\Delta(i\omega_n)$ is obtained. The DMFT solver uses $\Delta(i\omega_n)$, U and J to produce the local self-energy $\Sigma_{LL'}^{\text{loc}}(i\omega_n)$. By keeping the QSGW part of the Green's function fixed, the calculation of the selfenergy is repeated until convergence of the magnetic moment (DMFT loop). Then a new density $\rho(\mathbf{r})$ is recomputed summing over all Matsubara's freequencies according to

$$\rho(\mathbf{r}) = \sum_{\mathbf{k},l} \left\{ \frac{1}{\beta} \sum_{n=-\infty}^{+\infty} \frac{\psi_{l\mathbf{k}}^{R}(\mathbf{r}, i\omega_{n})\psi_{l\mathbf{k}}^{L*}(\mathbf{r}, i\omega_{n})}{i\omega_{n} + \mu - \varepsilon_{l\mathbf{k}}(i\omega_{n})} \right\}, \quad (3)$$

where $\psi_{l\mathbf{k}}^{X}(\mathbf{r}, i\omega_{n})$ are the right (X = R) and left (X = L) eigenfunctions of the DMFT Hamiltonian $H_{\mathbf{k}}(i\omega_{n})$ with corresponding eigenvalues $\varepsilon_{l\mathbf{k}}(i\omega_{n})$. A new QSGW loop is then converged by keeping the density fixed, that produces a new QSGW Green's function. The output is used to initialise a new DMFT loop and so on until QSGW self-energy and DMFT updated density are self-consistent.

The number of iterations in each DMFT loop varies between 10 and 20, and the number of



FIG. 1: Spin-resolved DOS of Ni 3d states obtained from Maximum entropy method.

random moves per iteration are roughly 10^{10} . This method is basically the equivalent of stateof-the-art DMFT implementations in the framework of DFT+DMFT. We believe it is superior to other G_0W_0 +DMFT implementations because of the possibility to close the full self-consistent loop and because of the higher quality of the low-level theory chosen. This calculation allowed us to compute the spin-resolved density of state of local Ni 3*d* orbitals through Maximum entropy method, here reported in Figure 1, from which we were able to estimate the QS*GW*+DMFT exchange splitting to 0.30 eV (cfr. Table II in the main text).

QS*GW*+**SLDMFT:** From the converged DMFT selfenergy, we first extrapolate the static limit of $\Sigma_{LL'}^{\text{loc}}(i\omega_n)$, then we embed it into the lattice problem and we keep only its symmetrized real part

$$\bar{\Sigma}_{ij\mathbf{k}}^{\text{loc}} = \text{Re}\left[\Sigma_{ij\mathbf{k}}^{\text{loc}}(0) + \Sigma_{ji\mathbf{k}}^{\text{loc}}(0)\right]/2.$$
(4)

This is done for the spin-up and spin-down channels separately. We finally retain only the spin-flip component $\Sigma_2 = \bar{\Sigma}^{\text{loc}} - (\bar{\Sigma}^{\text{loc}}_{\uparrow} + \bar{\Sigma}^{\text{loc}}_{\downarrow})/2$ and we add it to the charge component $\Sigma_1 = (\bar{\Sigma}^{\text{xc}}_{\uparrow} + \bar{\Sigma}^{\text{xc}}_{\downarrow})/2$ computed at QS*GW* level. This procedure allowed us to prevent counting twice the magnetic contributions to the self-energy.

Applications to Fe

To further confirm that the local momentum is not relevant in the description of Fe, we applied the fully dynamical QSGW+DMFT approach also to Fe. The parameters U = 5 eV and J = 0.8 eV used are the same as in[11], where they have been derived from GW within the same projection scheme. Four valence and four conduction bands have been used to project onto the correlated



FIG. 2: Total DOS of Fe 3d states obtained from Maximum entropy method.

system. The resulting magnetic moment M=2.20 Bohr, as the QSGW prediction, confirming that local corrections are absolutely negligible in Fe.

We extract the scattering rate Γ from the intercept and the linear term of a forth-order polynomial fitting $\text{Im}\Sigma(\omega)$ in the vicinity of $\omega = 0$ as explained above. We find that Fe has extremely coherent charge scattering. We also present the analytically continued $\text{Im}G(i\omega)/\pi$ for Fe reported in Figure 2.

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