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▶ To cite this version:

Stéphane Caron, Abderrahmane Kheddar, Olivier Tempier. Stair Climbing Stabilization of the HRP-4 Humanoid Robot using Whole-body Admittance Control. 2019. hal-01875387v2

HAL Id: hal-01875387 https://hal.science/hal-01875387v2

Preprint submitted on 1 Mar 2019 (v2), last revised 8 Oct 2021 (v7)

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Stair Climbing Stabilization of the HRP-4 Humanoid Robot using Whole-body Admittance Control

Stéphane Caron, Abderrahmane Kheddar and Olivier Tempier

Abstract—We consider dynamic stair climbing with the HRP-4 humanoid robot as part of an Airbus manufacturing use-case demonstrator. We share experimental knowledge gathered so as to achieve this task, which HRP-4 had never been challenged to before. In particular, we extend walking stabilization based on linear inverted pendulum tracking [1] by quadratic programming-based wrench distribution and a whole-body admittance controller that applies both end-effector and CoM strategies. While existing stabilizers tend to use either one or the other, our experience suggests that the combination of these two approaches improves tracking performance. We demonstrate this solution in an on-site experiment where HRP-4 climbs an industrial staircase with 18.5 cm high steps, and release our walking controller as open source software.

I. Introduction

Recently, humanoid robotics has reached a level of maturity that allows considering deployments in large-scale manufacturing (e.g. aircraft and shipyard), construction sites and nuclear power plants. These environments are populated with stairs. In the case of aircraft manufacturing and shipyards, they allow workers to travel between different shop-floor levels where assembly tasks are required, which makes them a key challenge for any mobile robotics application. Stair climbing was demonstrated as early as the first release of the Honda humanoid robot in 1997 [2], yet it is still a challenging task that humanoids rarely perform untethered. Robust stabilization is a critical issue, not only to prevent robot falls, but for the safety of human co-workers that are present and share the same working space².

In order to correct the deviation of their floating base from a reference pattern, position-controlled robots adjust their contact forces with the environment via *admittance control*. To the exception of Honda humanoid robots³, controllers found in the literature implement admittance either at the level of end-effectors [1], [6], [7], [8] or at the level of the CoM [9], [10], [11], [12]. Yet, these two strategies are not mutually exclusive. In this work, we investigate a whole-body admittance controller where both end-effector and CoM

The authors are with the Montpellier Laboratory of Informatics, Robotics and Microelectronics (LIRMM), CNRS-University of Montpellier, France. A. Kheddar is also with the CNRS-AIST Joint Robotics Laboratory (JRL), UMI3218/RL, Tsukuba, Japan. This work is supported in part by the H2020 EU project COMANOID http://www.comanoid.eu/, RIA No 645097. Corresponding author: stephane.caron@lirmm.fr

¹https://github.com/stephane-caron/lipm_walking_controller/

²Performance and safety certification requirements are yet to be defined ³Controllers reported by Honda include the *model ZMP control* strategy [2], [3] where saturation of ZMP constraints triggers recovery CoM accelerations and a corresponding update of the walking pattern [4], [5]. This integration of a switching control law with replanning behavior makes these controllers more advanced than linear feedback controllers.



Fig. 1. HRP-4 humanoid climbing an industrial staircase at the Airbus factory in Saint-Nazaire, France. Step height is 18.5 cm. The experiment was reproduced time and again over the course of two weeks spent on-site, and deemed robust enough to let the robot climb without safety ropes.

strategies are applied simultaneously. Preliminary analysis in stair climbing simulations and experiments suggests that a combination of these two approaches can improve tracking performance.

Figure 2 illustrates the components implemented in our walking and stair climbing controller. The two main components for stabilization are:

- DCM Feedback Control (Section II), which computes desired contact wrenches to compensate deviation from the walking pattern.
- Whole-body Admittance Control (Section III), which allows a position-controlled robot to realize the desired contact wrenches.

We illustrate the performance of this controller in an onsite experiment in the Airbus Saint-Nazaire site where the HRP-4 humanoid climbs a staircase with 18.5 cm steps. To the best of our knowledge, this is the first time that dynamic stair climbing is demonstrated with HRP-4. The controller used in this experiment is also open source and open to comments.¹

II. DCM FEEDBACK CONTROL

The goal of this first component is to regulate the robot's first-order dynamics assuming control of its second-order dynamics. This amounts to decide a *net contact wrench* that compensates deviations from the walking pattern.

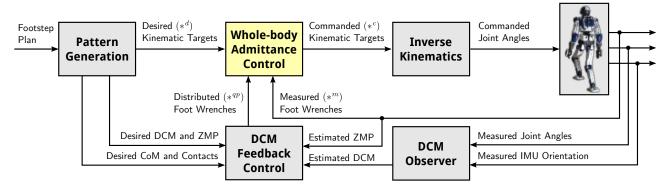


Fig. 2. Overview of the walking and stair climbing controller for position-controlled robots based on feedback control of the divergent component of motion (DCM). The main contribution of this work lies in the combination of end-effector and CoM strategies to realize whole-body admittance control.

Within the equations of motion of an articulated robot [13], the centroidal dynamics is governed by the Newton-Euler equation:

$$\begin{bmatrix} m\ddot{c} \\ \dot{\mathbf{L}}_c \end{bmatrix} = \begin{bmatrix} f \\ \tau_c \end{bmatrix} + \begin{bmatrix} mg \\ 0 \end{bmatrix} \tag{1}$$

where m denotes the total robot mass, g is the gravity vector, c the position of the center of mass (CoM) and \mathbf{L}_c the angular momentum around c. The net contact wrench (f, τ_c) consists of the resultant f of external contact forces applied to the robot and their moment τ_c around c. The left-hand side of this equation corresponds to the net motion of the robot, while the right-hand side represents its interaction with the environment. The gist of locomotion is to leverage these interaction forces to move the CoM (or similarly the translation of the floating base) to a desired location.

A. Linear Inverted Pendulum Mode

A general walking pattern generator [14] can provide both a CoM trajectory c(t) and an angular-momentum trajectory $\mathbf{L}_{c}(t)$. Alternatively, this output can be reduced to the single CoM trajectory by considering solutions where $\mathbf{L}_{c}=\mathbf{0}$. The resulting model, known as the Inverted Pendulum Mode (IPM) [15], is expressive enough for walking or stair climbing. It simplifies eq. (1) to:

$$\ddot{c} = \lambda(c - z) + g \tag{2}$$

where the contact wrench is now characterized by a scaling factor $\lambda \geq 0$ and a zero-tilting moment point (ZMP) z.

Another working assumption acceptable for walking over a horizontal surface is that of a constant CoM height $c_z = h$ above that surface. This gives rise to the Linear Inverted Pendulum Mode (LIPM) [16]:

$$\ddot{\boldsymbol{c}} = \omega^2 (\boldsymbol{c} - \boldsymbol{z}) \tag{3}$$

where $\omega = \sqrt{g/h}$, and we drop from now on the gravity vector by considering only horizontal coordinates. The LIPM linearizes the dynamics (2) of the IPM by turning the variable λ into a constant. Its contact wrench is characterized by the position z of the ZMP on the contact surface.

These simplifications come at the expense of balance recovery strategies: the IPM sacrifices the hip strategy [17]

while the LIPM sacrifices the height-variation strategy [18], [19]. Accordingly, the dimension of the contact wrench decreases from six to three in the IPM and two in the LIPM. A LIPM-based stabilizer such as the one reported in the present paper can leverage these two force coordinates to control two position coordinates, for instance the horizontal position of the center of mass [1] or equivalently the rolling and pitching angles of the floating base [3].

B. Feedback of the Divergent Component of Motion

The divergent component of motion (DCM) of the LIPM is defined by $\xi = c + \dot{c}/\omega$. It allows a decomposition of the second-order eq. (3) into two coupled first-order systems [4]:

$$\dot{\boldsymbol{\xi}} = \omega(\boldsymbol{\xi} - \boldsymbol{z}) \tag{4}$$

$$\dot{\boldsymbol{c}} = \omega(\boldsymbol{\xi} - \boldsymbol{c}) \tag{5}$$

While the DCM naturally diverges away from the ZMP by eq. (4), eq. (5) shows that the CoM is guaranteed to converge to the DCM without being controlled. It is therefore sufficient for locomotion to control only the DCM, rather than *e.g.* both the CoM position and velocity.

Walking pattern generation provides a trajectory $c^d(t)$ in the linear inverted pendulum mode (3), from which one can derive $\xi^d(t)$ and $z^d(t)$. The DCM can be controlled around this reference by proportional feedback [20], [21], [22]:

$$\dot{\boldsymbol{\xi}} = \dot{\boldsymbol{\xi}}^d + k_p (\boldsymbol{\xi}^d - \boldsymbol{\xi}^m) \tag{6}$$

where k_p is a positive feedback gain and the $*^m$ superscript denotes estimated quantities.

An integral term can be added to eliminate steady-state error [7], which would correspond here to an offset between the CoM and ZMP positions when the robot is in static equilibrium:

$$\dot{\xi} = \dot{\xi}^d + k_p(\xi^d - \xi^m) + k_i \int (\xi^d - \xi^m)$$
 (7)

The integral term can include an anti-windup strategy such as saturation. We used an exponential moving average, also known as leaky integrator:

$$\int x = \frac{1}{T_i} \int_{t=0}^{T} x(t) \exp\left(\frac{t-T}{T_i}\right) dt$$
 (8)

where T_i is the integrator time constant. This average does not wind up by construction, and its implementation takes a single floating-point number in memory.

Finally, a derivative term can be added to damp potential oscillations. From eq. (4), it can be implemented indifferently by adding $k_d(\dot{\boldsymbol{\xi}}^d - \dot{\boldsymbol{\xi}}^m)$ or substracting $k_z(\boldsymbol{z}^d - \boldsymbol{z}^m)$ to the commanded ξ . We choose the latter in what follows.

From eq. (4), DCM feedback control can then be written in terms of the commanded ZMP:

$$oldsymbol{z} = oldsymbol{z}^d - \left[1 + rac{k_p}{\omega}\right] (oldsymbol{\xi}^d - oldsymbol{\xi}^m) - rac{k_i}{\omega} \int (oldsymbol{\xi}^d - oldsymbol{\xi}^m) + rac{k_z}{\omega} (oldsymbol{z}^d - oldsymbol{z}^m)$$

Note that the fact that the commanded z and measured z^m appear on both sides of this equation comes from the unmodeled delay of admittance control.⁴ This commanded ZMP is equivalent to a commanded net contact wrench:

$$\begin{bmatrix} f \\ \tau_c \end{bmatrix} = m \begin{bmatrix} \omega^2(c-z) - g \\ 0 \end{bmatrix}$$
 (9)

Thus, DCM feedback is a way to determine a net contact wrench that includes both a feedforward term from the walking pattern and a feedback term to correct CoM position and velocity deviations from their reference.

C. Contact Wrench Distribution

While stabilizers based on CoM admittance control [9], [11], [12], [23] take the net wrench as only input, those that include foot force control need to distribute this wrench among contacts. This operation corresponds to the ZMP distributor of the stabilizer by Kajita et al. [1]. Meanwhile, the net wrench obtained by DCM feedback is saturated in order to account for feasibility constraints such as keeping the ZMP inside its support area. Both distribution and saturation operations can be handled at once by formulating the wrench distribution problem as a quadratic program (QP).

We will make use of spatial vector algebra [24] to describe this program. Let us denote by ${}^0\boldsymbol{w}_{dcm}$ the net contact wrench coordinates from eq. (9) expressed in the inertial frame 0. Define ${}^{lc}w_{left}$ and ${}^{la}w_{left}$ the left foot contact wrench expressed respectively in the left sole center frame lc and ankle frame la (sole frame closest to the ankle joint). Wrenches ${}^{rc}w_{right}$ and $r^a w_{right}$ are defined similarly.

1) Constraints: in double support, the wrench distribution QP consists of two constraints: contact stability, and a minimum pressure at each contact:

$$\mathbf{U}^{lc} \mathbf{w}_{left} \leq 0 \qquad \qquad \mathbf{U}^{rc} \mathbf{w}_{right} \leq 0 \qquad (10)$$

$$\mathbf{e}_{fz}^{lc} \mathbf{w}_{left} \geq p_{min} \qquad \mathbf{e}_{fz}^{rc} \mathbf{w}_{right} \geq p_{min} \qquad (11)$$

$$e_{fz}^{lc} w_{left} \ge p_{min}$$
 $e_{fz}^{rc} w_{right} \ge p_{min}$ (11)

where U is the 16×6 matrix of the contact wrench cone [25]. This matrix includes all three components of the contactstability condition: the Coulomb force friction cone, centerof-pressure support area and net yaw moment boundaries. Meanwhile, e_{fz} is the basis vector that selects the resultant pressure of a wrench, and p_{min} is a small threshold such as 15 N. This constraint avoids sending low-pressure targets to the foot force controller, as fixed-gain admittance control tends to oscillate around contact switches for such targets.

2) Costs: the cost function of the wrench distribution QP weighs three objectives:

$$\left\| {}^{0}\boldsymbol{w}_{left} + {}^{0}\boldsymbol{w}_{right} - {}^{0}\boldsymbol{w}_{dcm} \right\|^{2} \tag{12}$$

$$\left\| {^{la}\boldsymbol{w}_{left}} \right\|_{\mathbf{W}_{ankle}}^{2} + \left\| {^{ra}\boldsymbol{w}_{right}} \right\|_{\mathbf{W}_{ankle}}^{2} \tag{13}$$

$$\left\| (1 - \rho) e_{fz}^{lc} \boldsymbol{w}_{left} - \rho e_{fz}^{rc} \boldsymbol{w}_{right} \right\|^2$$
 (14)

First and foremost, the solution should realize the net contact wrench as close as possible (12). Second, it should minimize ankles torques (13), where W_{ankle} is a diagonal weight matrix with 1 for ankle torques and a small value ϵ for all other components. Finally, the pressure ratio should be as close as possible (14) to a prescribed value ρ . This last term regularizes the discontinuity in force output that occurs in acceleration-based whole-body controllers when adding or removing contacts [26], [8]. The prescribed pressure ratio ranges from $\rho_{init} \in \{0,1\}$ at the beginning of the double support phase to $1 - \rho_{init}$ at the end of it.

Although we presented and implemented it as a quadratic program, this optimization is in essence a lexicographic optimization [27] whose four levels are (10)–(11), (12), (13) and (14). We approximate this behavior by setting cost weights to 10000 for (12), 100 for (13) and 1 for (14). Note that the latter two costs are omitted during single support where there is no force redundancy and the net-wrench cost (12) is enough to define a single optimum.

III. WHOLE-BODY ADMITTANCE CONTROL

Whole-body admittance control implements feedback control of the desired force targets issued by DCM feedback and wrench distribution, while otherwise following the position targets prescribed by the walking pattern.

A. Foot damping control

Admittance control applied at the ankle joint has been referred to as ground reaction force control [2], [3], foot damping control [1], or foot adjusting control [11]. It implements the first stabilization strategy from Section 4.5.1 of the Introduction to Humanoid Robotics [28].

Let us denote by (θ_r^c, θ_p^c) the *commanded* (see Figure 2) roll and pitch angles of the ankle joint of a foot in contact with the environment. We apply the following damping control law⁵ to track a desired CoP:

$$\begin{bmatrix} \hat{\theta}_{c}^{c} \\ \dot{\theta}_{p}^{c} \end{bmatrix} = \mathbf{A}_{cop}(\boldsymbol{p}^{qp} \times \boldsymbol{f}^{m} - \boldsymbol{\tau}^{m})$$
 (15)

$$\mathbf{A}_{cop} \equiv \begin{bmatrix} A_{cop,y} & 0 & 0\\ 0 & A_{cop,x} & 0 \end{bmatrix} \tag{16}$$

where $p^{qp} = [p_x^{qp} \ p_y^{qp} \ 0]$ denotes the target CoP position in the foot frame provided by the wrench distribution QP, and (f^m, τ^m) is the measured contact wrench expressed at the origin of the foot frame. The matrix A of admittance gains $(A_{cop,x}, A_{cop,y})$ is used to tune the responsiveness of

⁴DCM feedback gains can be chosen by pole placement based on an estimate of this delay [1], [7].

⁵Damping control is a shorthand for first-order admittance control.

the task: a higher $A_{cop,y}$ implies that the foot will roll faster in reaction to lateral CoP deviations, and similarly a higher $A_{cop,x}$ implies that the foot will pitch faster in reaction to sagittal CoP deviations.

The above eq. (15) is adapted from [1], with the slight difference that we track the desired CoP rather than a desired torque. The two approaches are equivalent under accurate foot pressure difference tracking, but in situations where the latter is degraded, the CoP formulation naturally defines the pressure-dependent admittance coefficients identified in [29]. This task can also be extended to include integral and derivative terms of the measured wrench [8]. Importantly, it can also be improved by a model of the flexibility located between the ankle joint and foot sole [3], [30], which we do not include yet.

B. Foot force difference control

In a walking gait, double support phases are used to transfer the net ZMP from one support foot to the next. It is therefore helpful to servo not only the CoP targets provided at each foot, but also their pressure. For this purpose, Kajita et al. [1], [31] introduced foot force difference control (FFDC). Denoting by (v_{Lz}, v_{Rz}) the respective velocities of the left and right foot in their sole frames, FFDC can be implemented as:

$$v_{Lz}^c = v_{Lz}^d - 0.5v_{\delta fz} + 0.5v_{vdc}$$
 (17)

$$v_{Rz}^{c} = v_{Rz}^{d} + 0.5v_{\delta fz} + 0.5v_{vdc}$$
 (18)

$$v_{\delta fz} \equiv A_{\delta fz} \left[(f_{Lz}^{qp} - f_{Rz}^{qp}) - (f_{Lz}^{m} - f_{Rz}^{m}) \right]$$
 (19)

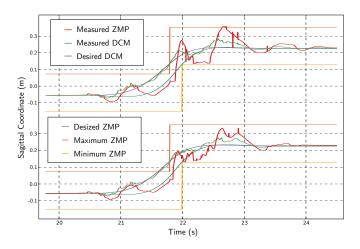
$$v_{vdc} \equiv T_{vdc}^{-1} \left[(p_{Lz}^d + p_{Rz}^d) - (p_{Lz}^c + p_{Rz}^c) \right]$$
 (20)

The velocity term $v_{\delta fz}$ implements a damping control that lifts the foot in excess of pressure and lowers the other one. It is tuned by the admittance gain $A_{\delta fz}$. The second velocity term v_{vdc} is added for vertical drift compensation. It retrieves the same average foot altitude as in the walking pattern, tuned by a frequency gain T_{vdc}^{-1} set to 1 Hz in practice. This choice of a velocity formulation (17)–(20) of FFDC rather than the position one from [1] is contingent to our inverse kinematics and yields the same behavior.

An implicit side effect of FFDC is that it increases CoM compliance. To illustrate this remark, consider the example of a constant external push applied to laterally: with only foot damping control, the robot will resist it by tilting its feet, while with FFDC it will lift the leg opposite to the push, resulting (as gravity maintains contact) in a CoM displacement toward that leg. As such, we may venture to say that our reference controller [1] implicitly included a form of CoM admittance control.

C. CoM Admittance Control

Admittance control applied at the CoM has been referred to as ZMP compliance control [9], ZMP damping control [11], position-based ZMP control [12] or horizontal compliance control [23]. It implements the third stabilization strategy from Section 4.5.1 of the Introduction to Humanoid Robotics [28], and should not be confused with the model



Effect of applying CoM admittance control in combination with foot damping control. Top: $A_{com,x}=0$ and $A_{com,y}=0$. Bottom: $A_{com,x}=20$ and $A_{com,y}=10$. In this simulation, the robot steps on an 18.5 cm step but tilts back on its heel during left-foot support. CoM admittance control (bottom) helps mitigate this effect.

ZMP control (fifth strategy) applied on Honda robots [2], [3], [5]. The former adds CoM accelerations at all times, the latter only upon saturation of a ZMP constraint.

We apply the following admittance control law:

$$\ddot{\boldsymbol{c}}^c = \ddot{\boldsymbol{c}}^d + \mathbf{A}_{com}(\boldsymbol{z}^m - \boldsymbol{z}^{qp}) \tag{21}$$

$$\ddot{\mathbf{c}}^{c} = \ddot{\mathbf{c}}^{d} + \mathbf{A}_{com}(\mathbf{z}^{m} - \mathbf{z}^{qp})$$
(21)
$$\mathbf{A}_{com} \equiv \begin{bmatrix} A_{com,x} & 0 & 0 \\ 0 & A_{com,y} & 0 \end{bmatrix}$$
(22)

where \ddot{c}^d is the feedforward CoM acceleration from the walking pattern, z^m is the ZMP of the measured net contact wrench and z^{qp} is the ZMP of the net contact wrench output by the distribution QP (Section II-C). The matrix \mathbf{A}_{com} of admittance gains $(A_{com,x}, A_{com,y})$ is used to tune the responsiveness of the task: the higher the gain, the faster the CoM will accelerate toward the measured ZMP so as to move it back towards the desired one.

Figure 3 shows a simulation example of step climbing without and with CoM admittance control, both foot damping control laws being active. The CoM admittance law does not seem to conflict with the end-effector ones. On the contrary, it improves both DCM and ZMP tracking noticeably.

D. Inverse Kinematics

Commanded velocities and accelerations are sent to a weighted task-based inverse kinematics solver [8], [26]. The following tasks are considered simultaneously:

- Maintain foot contact(s) (weight: 10000)
- CoM position and velocity tracking (weight: 1000)
- Swing foot position and velocity tracking (weight: 500)
- Bend the chest to a prescribed angle (weight: 100)
- Keep the pelvis upright (weight: 10)
- Regularizing half-sitting joint configuration (weight: 10)

Each task implements an acceleration-based tracking law:

$$\ddot{\boldsymbol{x}} = K(\boldsymbol{x}^c - \boldsymbol{x}) + B(\dot{\boldsymbol{x}}^c - \dot{\boldsymbol{x}}) + \ddot{\boldsymbol{x}}^c \tag{23}$$

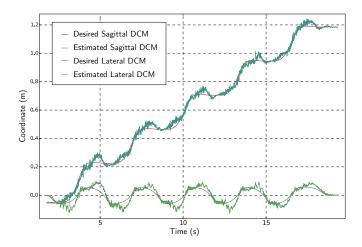


Fig. 4. DCM tracking performance while climbing a staircase with 18.5-cm steps. Swing leg motions are not accounted for in the walking pattern and drive the DCM away from its reference at each step. These disturbances are compensated by the stabilizer in both sagittal and lateral directions.

Task damping coefficients B are set by default to their critical value $2\sqrt{K}$, with the exception of foot contact tasks where we use B=300 Hz and K=1 Hz². In single support where foot force difference control is disabled, the translation stiffness of the support foot task is increased to K=1000 Hz² for vertical drift compensation.

For a foot $F \in \{L, R\}$ in contact, the target velocity \dot{x}_F^c of the corresponding foot contact task is defined from eq. (15) and (17)–(18). At present, we kept $\ddot{x}_F^c = \mathbf{0}$ and x_F^c fixed to the desired contact location. For an improved behavior, the latter can be updated by an integral of the \dot{x}_F^c so that all targets x_F^c , \dot{x}_F^c , \ddot{x}_F^c become consistent [8].

IV. EXPERIMENTS

We implemented our controller in the *mc_rtc* framework (see the Appendix for details on other components) and carried out experiments with the HRP-4 humanoid robot [32].

A. Demonstration environment

Experiments were carried out on-site at the Airbus factory located in Saint-Nazaire, France. In the final demonstration, the robot walked to the staircase, climbed it, walked to a designated area inside the fuselage of an A350 aircraft and performed an assembly task before walking out. The staircase climbed to access the assembly area had five steps of length 24 cm and height 18.5 cm.

In preliminary experiments with varying step heights, shown in the accompanying video, we also used a cable-driven parallel robot to act as safety crane for HRP-4. This robot was developed in our laboratory and consists of eight actuators, four of which were used. Cables were attached to a taylored holder connecting safety ropes to the shoulders of the humanoid. The system was remote-controlled by a human operator, making sure that the ropes stay loose while trying to avoid hitting the robot as it climbs (bonus robustness checks otherwise).

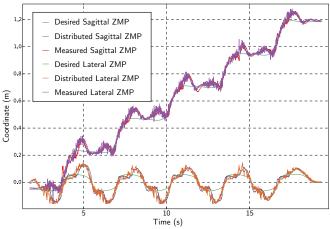


Fig. 5. ZMP tracking performance while climbing a staircase with 18.5-cm steps. During leg swings, the distributed ZMP is driven away from the walking pattern reference to compensate for DCM errors. Whole-body admittance control successfully regulates the ZMP to the distributed one.

B. Results

We confirmed that HRP-4 can dynamically climb the industrial staircase, as shown in Figure 1 and in the accompanying video. The performance was reproduced time and again over the course of two weeks spent on-site at the Airbus site, and deemed robust enough to let the robot climb without safety ropes in the latter experiments. The robot climbs the stairs in 18 s with 1.4 s single-support and 0.2 s double-support durations. DCM feedback was tuned as follows:

k_p [Hz]	k_i [Hz]	k_z [Hz]	T_i [s]
5	20	2	20

Meanwhile, admittance control parameters were set to the following values (in $[s.kg^{-1}]$ and $[kg^{-1}]$ respectively):

$A_{cop,x}$	$A_{cop,y}$	$A_{\delta fz}$	$A_{com,x}$	$A_{com,y}$
0.1	0.1	0.0001	20	10

DCM and ZMP tracking performance are reported in Figure 4 and 5 respectively.

The overall run time of a controller cycle on a consumer laptop computer is around 1.0 ± 0.4 ms, which fits within the 5 ms of HRP-4's control loop. Most of this time is spent solving the inverse kinematics QP $(0.4 \pm 0.1 \text{ ms})$ and the wrench distribution QP $(0.3 \pm 0.1 \text{ ms})$ during double support) using the LSSOL least-squares solver for both. Running at a lower frequency, the model predictive control QP is solved in 0.3 ± 0.1 ms using the QLD solver.

To avoid collisions, the apex of swing foot trajectories for each step is set to 24 cm, which is a first source of DCM disturbance. The second main cause are the CoM height variations at each step that disturb the horizontal ZMP backwards. We mitigated this by delaying CoM lift to the end of the step, unfortunately thus increasing knee torques as well. A better way to improve this in future work will be to switch to a pattern generation method taking height variations into account [19], [21], [33].

⁶https://www.youtube.com/watch?v=vFCFKAunsYM

C. Practicalities

One of the most precious tools at our disposal during our trials and errors was the Choreonoid environment and its dynamics simulator [34], in which we could reproduce most of the phenomena encountered in practice. The ability to test controllers in fast simulations rather than slow experiments is a serious enabler, and for humanoid robotics, Choreonoid outperformed alternatives like V-REP or Gazebo in terms of both realism and real-time performance.

During our first experiments, the robot would systematically servo-off during the second (most knee-torque intensive) swing phase of step climbing. This was caused by a drop of voltage due to a maximum current setting of 5 A on the power supply. We increased this threshold and observed peak current draws reaching up to 13 A. We estimate the peak power consumption to be around 750 W. For comparison, ASIMO consumes 600–900 W when its servomotors are turned on, and around 1000 W during stair climbing [35]. The consumption gap between the two robots is mostly owed to the design of HRP-4 [32], which is both lighter (40 kg versus 50 kg) and taller than its Honda sibling (1.5 m versus 1.3 m), allowing it to bend its knees less while climbing.

Our initial plan was to climb (i) a single step, then (ii) the staircase with double-support phases at each step, and finally (iii) a more human-like stair climbing with exactly one foot contact per step. We presently report on (ii) but not (iii), as a mechanical transmission issue prevents our robot from performing with its right leg the motions that it achieves with the left one, even for lower step heights.

V. RELATED STAIR CLIMBING WORKS

Stair climbing for bipeds with ZMP-based stabilizers started as early as 1993, when the Honda E6 prototype climbed staircases thanks to the stabilization strategies developed by Takenaka [35]. This method was showcased in 1997 for the public release of the P2 humanoid robot [2]. Stair climbing was also demonstrated in 2002 on the prototype HRP-1S of the HRP series [11].

However, the stabilizer component provided with robots of the HRP series is mainly designed for walking on overall level ground. Climbing over small staircases with 10 cm steps has been reported on HRP-2 [14], [36], walking with bent knees to avoid undesired behavior close to the knee kinematic singularity. In [6], KHR-2 climbed stairs with 12 cm steps. In [14], HRP-2 also climbed stairs with 15 cm steps while grabbing a handrail.

Step heights above 20 cm have been demonstrated, yet with slower gaits. In [37], HRP-4 climbed a 24 cm step, but without stabilization and with a quasi-static motion lasting more than 80 s. During the DARPA Robotics Challenge, six teams successfully climbed a staircase with four 23 cm steps, yet with slow motions and doing frequent pauses as a result of the challenge's conditions. Shank collisions also become a concerning problem for higher step heights. To deal with this issue, team KAIST climbed stairs backwards [38] while teams IHMC and ESCHER used partial footholds [39], [22].

VI. CONCLUSION

In this paper, we reported on the state-of-the-art of walking stabilization by DCM feedback control and suggested two improvements: a wrench distribution quadratic program, and a whole-body admittance controller combining both endeffector and CoM strategies. We applied the resulting controller in a dynamic stair climbing experiment over 18.5 cm steps, performed in an industrial environment at the Airbus Saint-Nazaire site.

Our stabilizer has a number of gains to tune, some of which interact with each other. For instance, lowering foot CoP admittances allows one to raise the DCM feedback gain k_p to larger values before reaching the unstable regime. The elephant in the room hindering our understanding here is the unmodeled flexibility below foot ankles, modeled as a first-order ZMP delay in [1], [7]. Future work will require us to investigate this question, and at least another one: how to prevent or mitigate touchdown impacts?

ACKNOWLEDGMENTS

The authors warmly thank Kevin Chappellet for his help with robot hardware, Pierre Gergondet for developing mc_rtc , Daniele De Simone and Arnaud Tanguy for their assistance with experiments, Tomomichi Sugihara and Pierre-Brice Wieber for helpful and friendly discussions, as well as Junhyeok Ahn and Andrea Del Prete for their feedback on GitHub. The cable-driven parallel robot used during preliminary experiments was realized thanks to the support of the European Union through FEDER Grant No 49793.

APPENDIX

A. Walking Pattern Generation

We generate walking patterns by linear model predictive control [40] over pre-defined footstep locations. The corresponding QP minimizes three weighted costs:

- ZMP deviation from a reference (weight: 1000)
- CoM velocity deviation from a reference (weight: 10)
- CoM jerk (weight: 1)

The reference ZMP trajectory $z_{ideal}(t)$ consists of straight lines connecting foot ankle frames. The QP also enforces the following three constraints:

- Feasibility: ZMPs lie in their support polygons
- Terminal constraint 1: the ZMP ends on $z_{ideal}(T)$
- Terminal constraint 2: the DCM ends on $z_{ideal}(T)$

where $T=1.6~{\rm s}$ is the duration of the predictive horizon and the sampling period is set to $100~{\rm ms}$. We let predictive control update the CoM reference $c^d(t)$ and its derivatives by openloop integration rather than a closed-loop approach [41].

B. DCM observer

Although we plan to evaluate methods that take into account foot flexibilities [42], [43], for now we use a simple kinematics estimator based on Kalman filtering to estimate the orientation of the floating-base and an anchor-point assumption to estimate its translation. The CoM position is then derived by forward kinematics of joint-encoder readings, and its velocity by low-pass filtering.

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