

The impact of finite-alphabet input on the secrecy-achievable rates for broadcast channel with confidential message

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Motivations and Objectives

- The broadcast channel with confidential message (BCCM): • In theory: the secrecy-capacity region of Gaussian BCCM is achieved
- using Gaussian codebook
- In practice: symbols belong to **finite size constellations** (*M*-PAM,..) and are used with equal probability
- Objectives
- Computation of secrecy-achievable rate region using finite input alphabet for various broadcast strategies
- Is using practical broadcast strategies sufficient to achieve good rates? or it leads to significant losses?

System Model

A broadcast channel with 2 receivers and a sender attempting to send 2 messages

• A common message w_0 for both receivers **2** A confidential message w_1 for receiver 1

(W_1, W_0)	Randomized	X^n	$P_{Y_1Y_2 X}$	Y_1^n	Decoder
	Encoder			Y_2^n	Decoder
					Decoder

Figure 1: The broadcast channel with confidential message (BCCM)

The secrecy capacity region for the degraded BCCM $X \leftrightarrow Y_1 \leftrightarrow Y_2$ is the set that includes all (R_0, R_1) such that:

$$R_1 \leq I(X; Y_1|U) - I(X; Y_2|U)$$

$$R_0 \leq I(U; Y_2)$$

for some $P_{UX} \cdot P_{Y_1|X} \cdot P_{Y_2|X}$.

- U is an auxiliary random variable carrying the *common information*.
- The cardinality of \mathcal{U} can be limited to $|\mathcal{U}| \leq \min\{|\mathcal{X}|, |\mathcal{Y}_1|, |\mathcal{Y}_2|\}$
- The secrecy-capacity region of the power constrained **Gaussian** BCCM is achievable using **Gaussian** input.

Broadcast Transmission Strategies

Strategies for transmitting both messages w_0 and w_1 separately in time (time sharing) or simultaneously (superposition modulation, superposition coding).

Broadcast Strategies

- In ascending order in complexity of implementation: **1** TIME SHARING (TS)
- **2** SUPERPOSITION MODULATION (SM)
- **3** SUPERPOSITION CODING (SC)

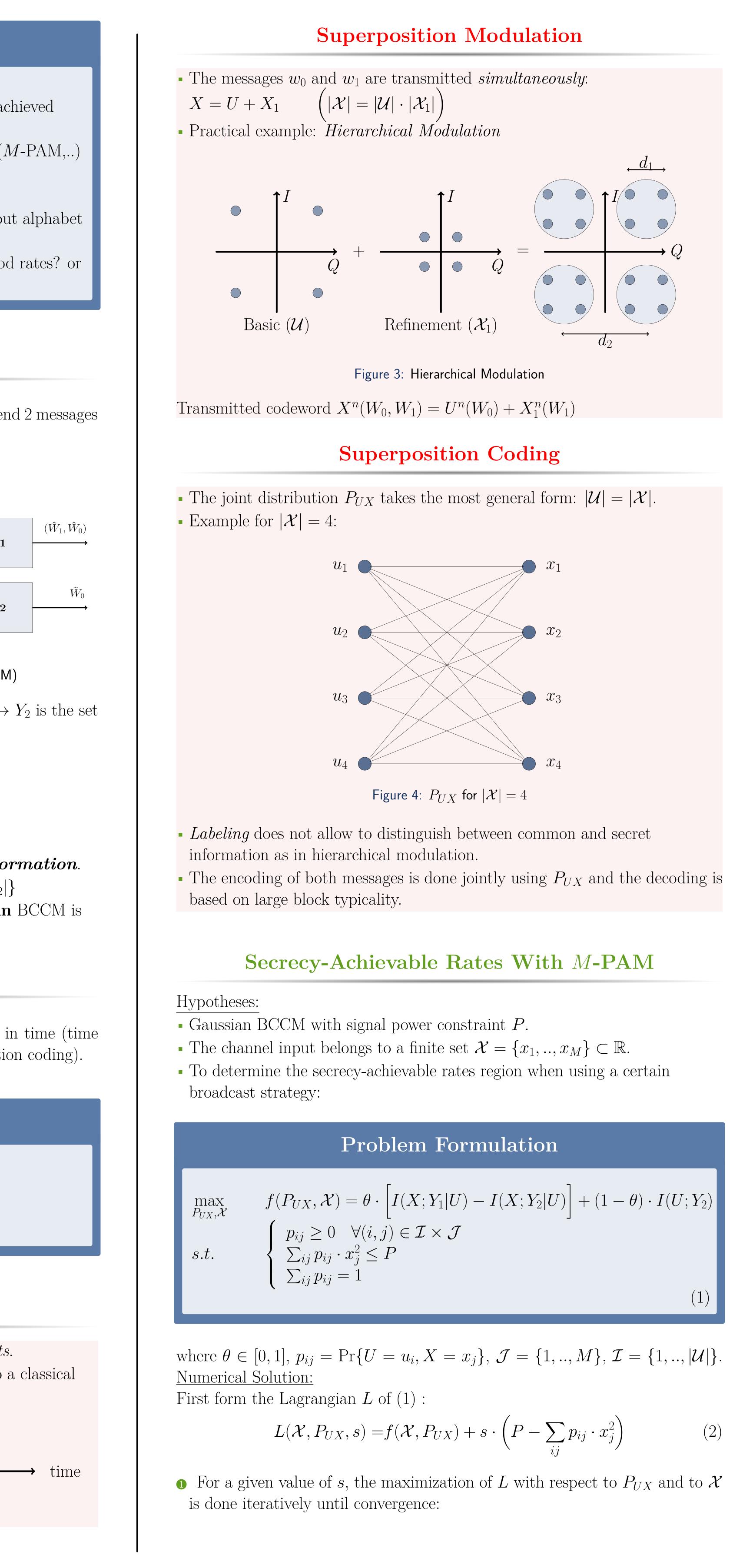
Time Sharing

• The messages w_0 and w_1 are transmitted in *different time slots*. • Simple implementation: in each slot the system is equivalent to a classical point-to-point communication system.

 w_0	w_1	w_0	•••
ΙΙ			Figure 2: Time sharing

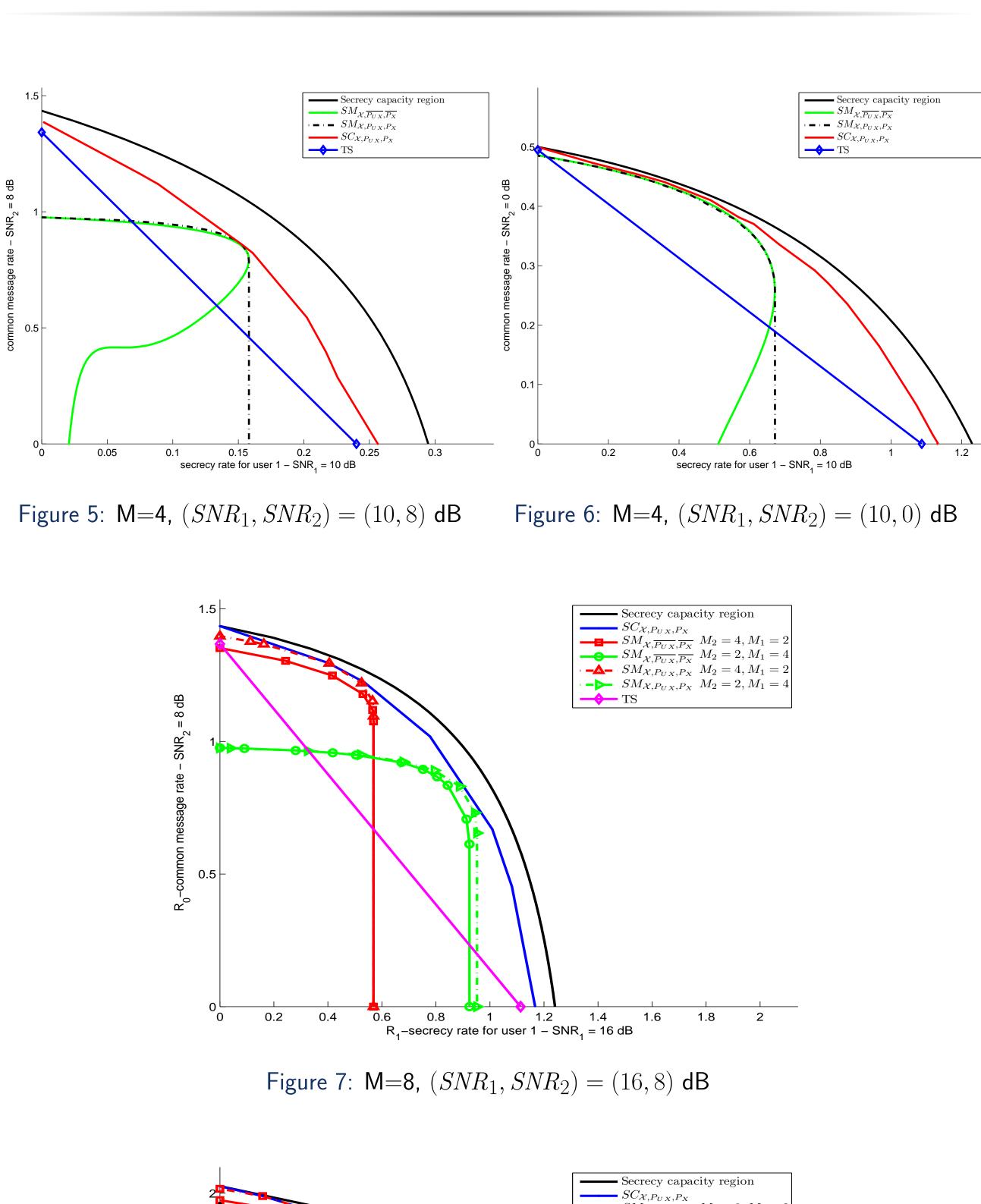
THE IMPACT OF FINITE-ALPHABET INPUT ON THE SECRECY-ACHIEVABLE RATES FOR **BROADCAST CHANNEL WITH CONFIDENTIAL MESSAGE**

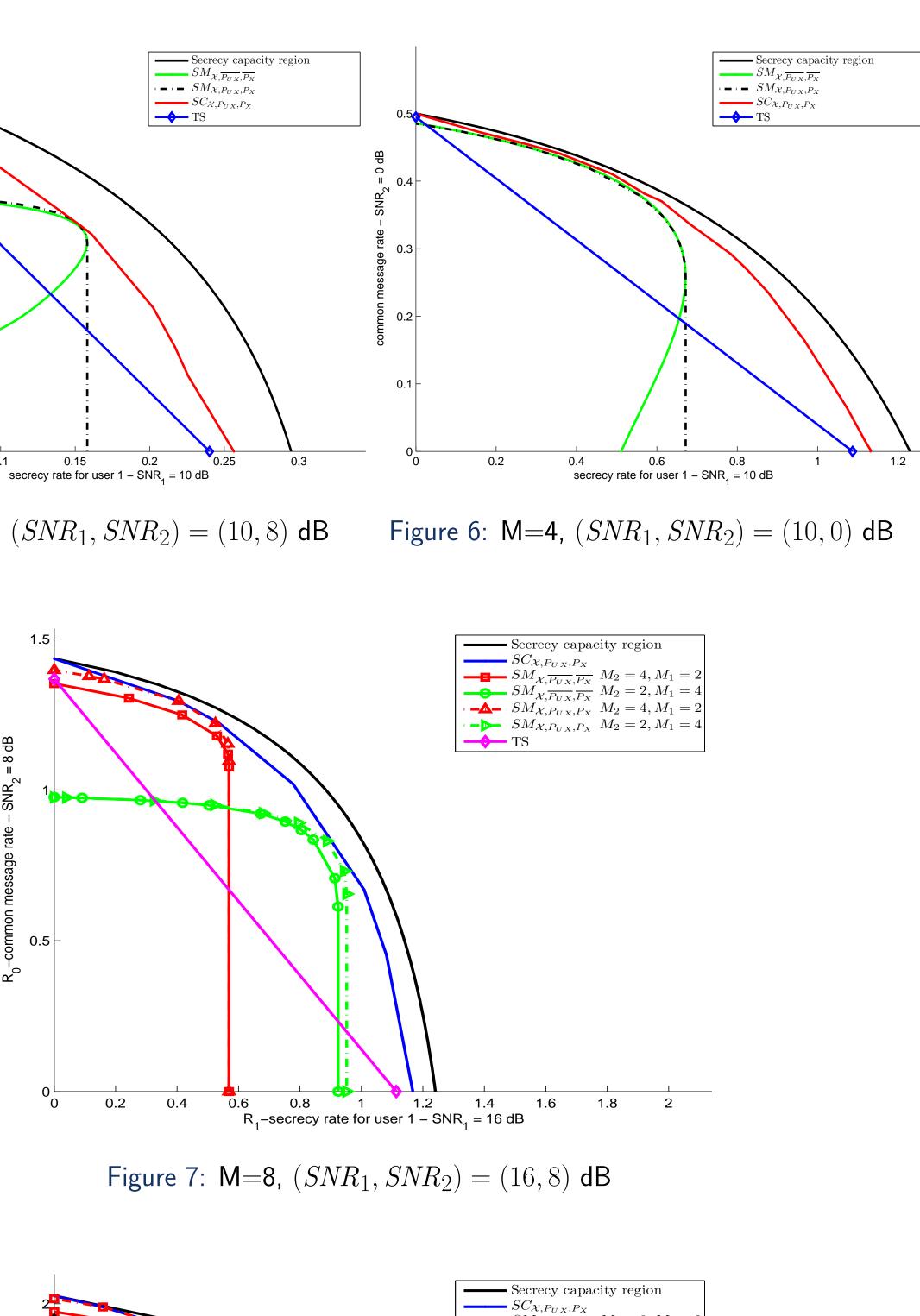
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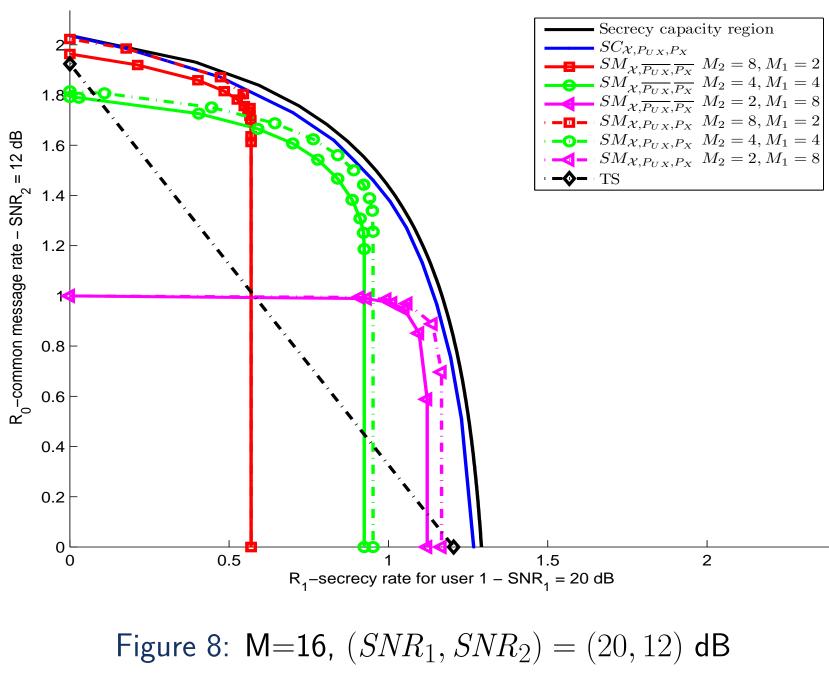


$$P - \sum_{ij} p_{ij} \cdot x_j^2$$
 (2)

- $P_{UX}^{(\ell)} = \arg \max_{P_{UX} \in \mathcal{C}} L(\mathcal{X}^{(\ell-1)}, P_{UX}, s)$ • We observe in experiments that $L(\mathcal{X}, P_{UX}^{(\ell)}, s)$ is a concave function if $\mathcal{X} \in \mathcal{D}$ where $\mathcal{D} = \{ \mathcal{X} \in \mathbb{R}^M : |x_i - x_j| > d \ \forall i, j \in \{0, ..., M-1\} \text{ and } i \neq j \} \text{ and } d \text{ depends on the size}$ of the constellation and on the SNR. • A simplex method can be used with initialization in \mathcal{D} . • $\mathcal{X}^{(\ell)} = \arg \max_{\mathcal{V}} L(\mathcal{X}, P_{UX}^{(\ell)}, s)$
- A Blahut-Arimoto-type algorithm is used. This algorithm converges if the initial guess lies in the domain where $L(\mathcal{X}, P_{UX}^{(\ell)}, s)$ is concave in P_{UX} .
- **2** To update the value of s, a gradient search method is used.







• The maximal achievable secrecy rate for SM is not necessarily obtained when the total transmission power is dedicated to the secrecy information.

General Conclusion

The general case of superposition coding can provide significant gains comparing to practical schemes (Time Sharing and Superposition Modulation). However in other cases, using practical schemes is sufficient to achieve good rates and provides a *compromise between complexity of implementation* and efficiency.



Experimental Results

- Remark: $\overline{P_{UX}} \equiv "P_{UX}$ is uniform" and $\overline{\mathcal{X}} \equiv "\mathcal{X}$ is a standard constellation"