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## Multi-hop, multi-route power minimisation in ad hoc network

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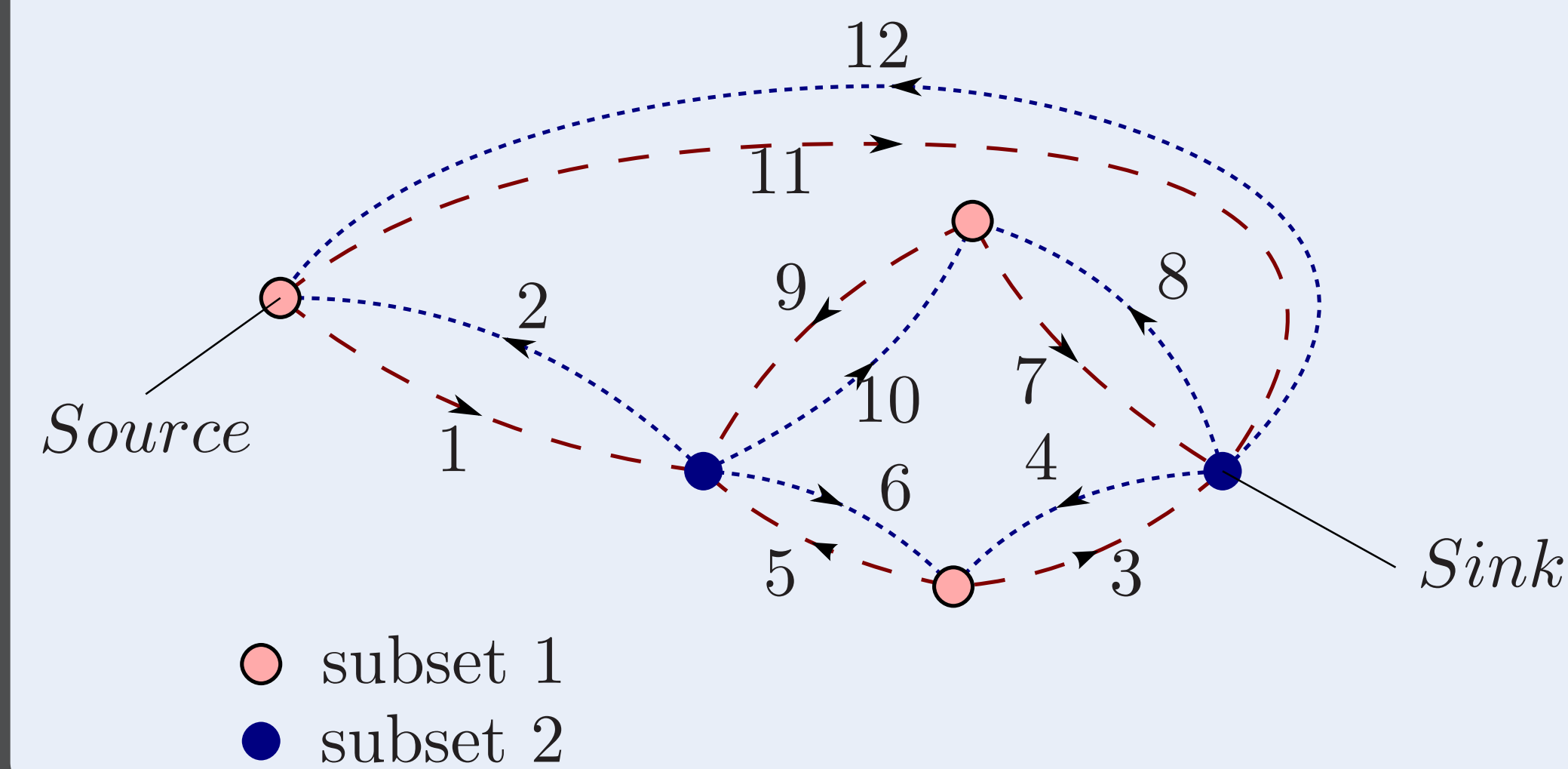


## Problem

This paper studies the problem of finding the optimal route of a stream between the transmitter and the receiver in an ad hoc network while minimizing the total power consumption. The main step of this work is modeling the transmissions as a graph, deduce the associated optimization problem and find a way to solve it.

Compared to previous approaches, we introduce more flexibility by allowing the stream to be split between several intermediate destinations, and we do not use the specific approximations (mainly high SNR) required to make the problem convex.

We illustrate our work using the following example where transmissions are splitted into two different channel to model the equivalent of downlink and uplink at each node. We call this graph  $\zeta$



## Model

As we attend to manage multiuser interference, we use a quite rough multiuser transmission scheme: a BCIM (Bit Interleaved Coded Modulation). So the node  $k$  receives at each time:

$$Y_k = \sqrt{G_{kk}}X_k + \underbrace{\left( \sum_{\substack{i \in \zeta \\ i \neq k}} \sqrt{G_{ik}}X_i + N \right)}_{\text{Supposed Gaussian noise}}$$

Where  $G_{kk}$  is the power gain of the link  $k$ , and  $G_{ik}$  the power of the link  $i$  interfering on  $k$ . So we derive a capacity from the well known Shannon capacity:

$$R_k^{\zeta} \leq \log \left( 1 + \frac{P_k \cdot G_k}{\sigma^2 + \sum_{\substack{i \in \zeta \\ i \neq k}} \Theta_{i,k} \cdot P_i \cdot G_{i,k}} \right)$$

## The routing constraint

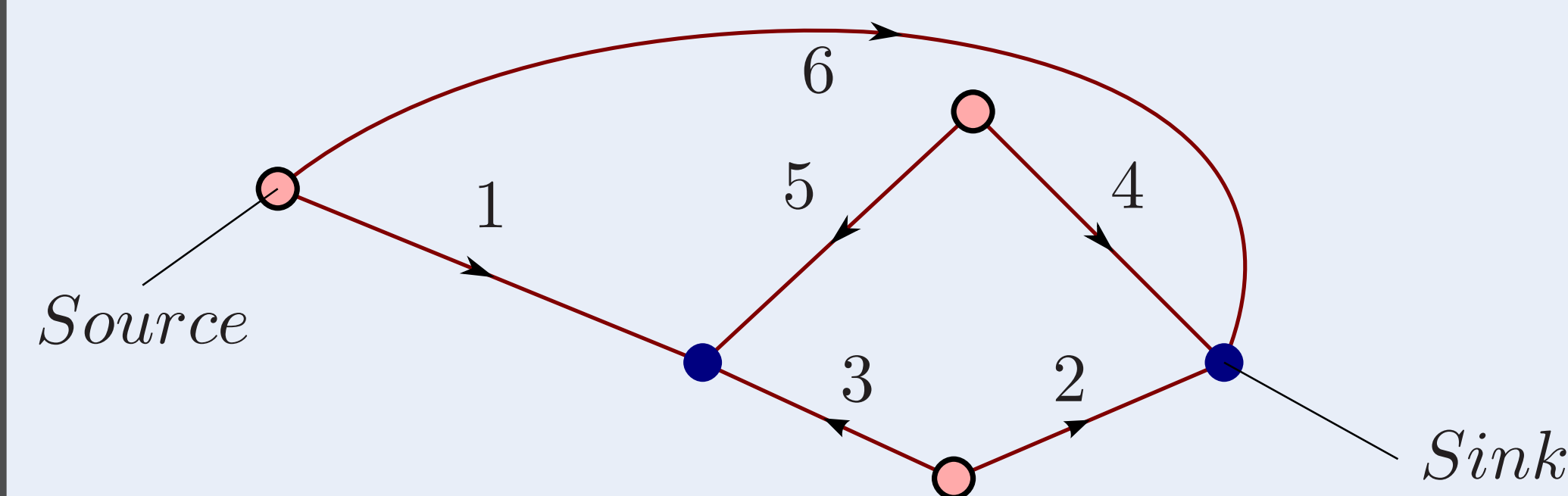
The data flow model we use to express the routing constraint could be expressed.

$$\mathbf{E} \cdot \mathbf{R}^{\mathcal{E}} = \mathbf{S}$$

Where  $\mathbf{E}$  is the incidence matrix of the graph and  $\mathbf{S}$  the source sink vector. This formulation lead to express  $\mathbf{R}^{\mathcal{E}}$  as a function of less but free variables.

$$\mathbf{R}^{\mathcal{E}} = \mathbf{M} \cdot \mathbf{R}_{cT}^{\mathcal{E}}$$

But this formulation have to be done in a slightly different graph: with the network flow graph, rate could be negative. So we route in the following graph noted  $\epsilon$  and then map into the  $\zeta$  graph.



## The optimization problem

The transmission at Shannon capacity could be written:

$$\mathbf{A}(\mathbf{R}^{\zeta}) \cdot \mathbf{P} = \mathbf{B}(\mathbf{R}^{\zeta})$$

with  $\mathbf{A} =$

$$\begin{bmatrix} G_{1,1} & - (2^{R_1^{\zeta}} - 1) G_{1,2} & \cdots \\ - (2^{R_2^{\zeta}} - 1) G_{2,1} & G_{2,2} & \cdots \\ - (2^{R_3^{\zeta}} - 1) G_{3,1} & - (2^{R_3^{\zeta}} - 1) G_{3,2} & \cdots \\ \vdots & \vdots & \ddots \end{bmatrix}$$

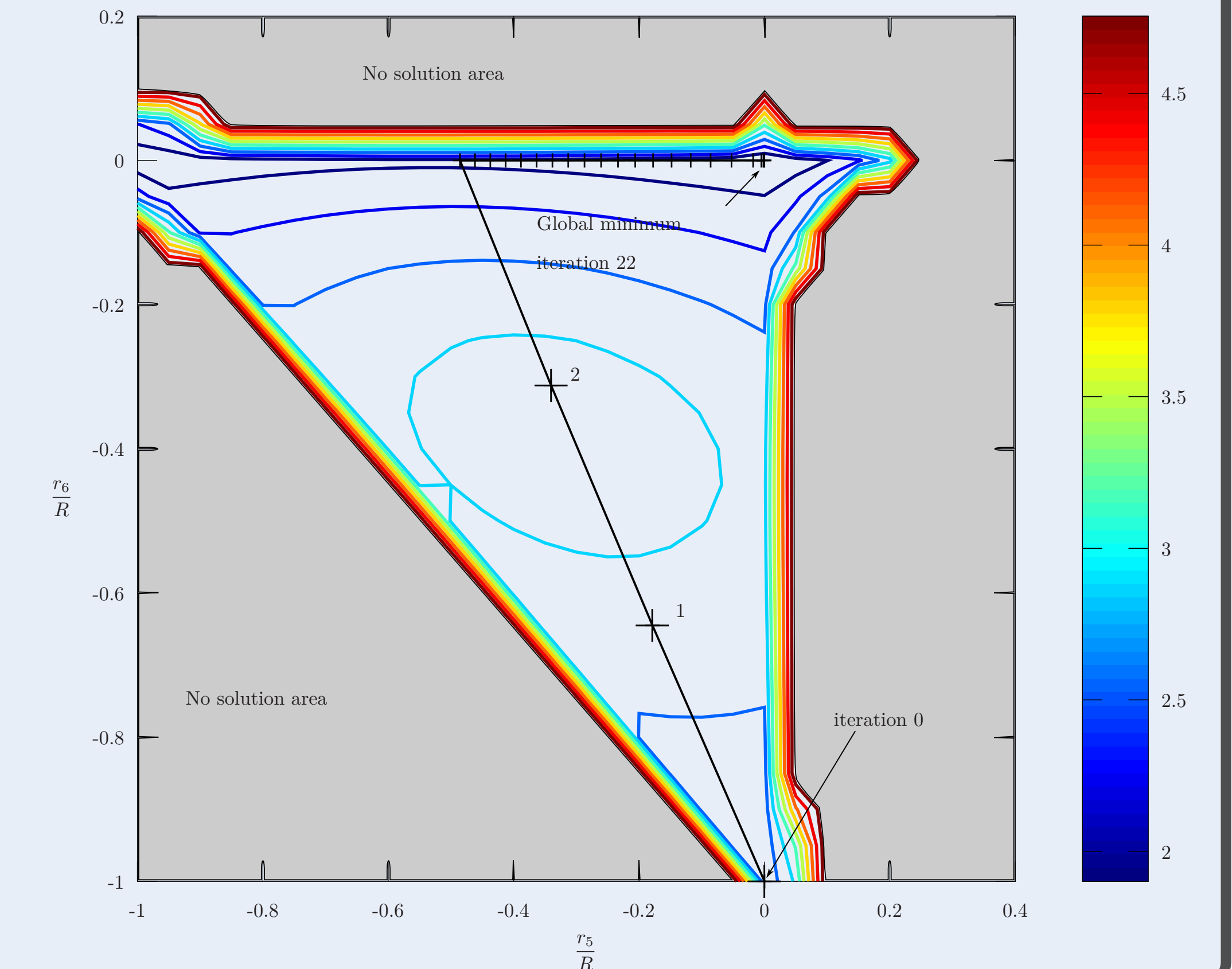
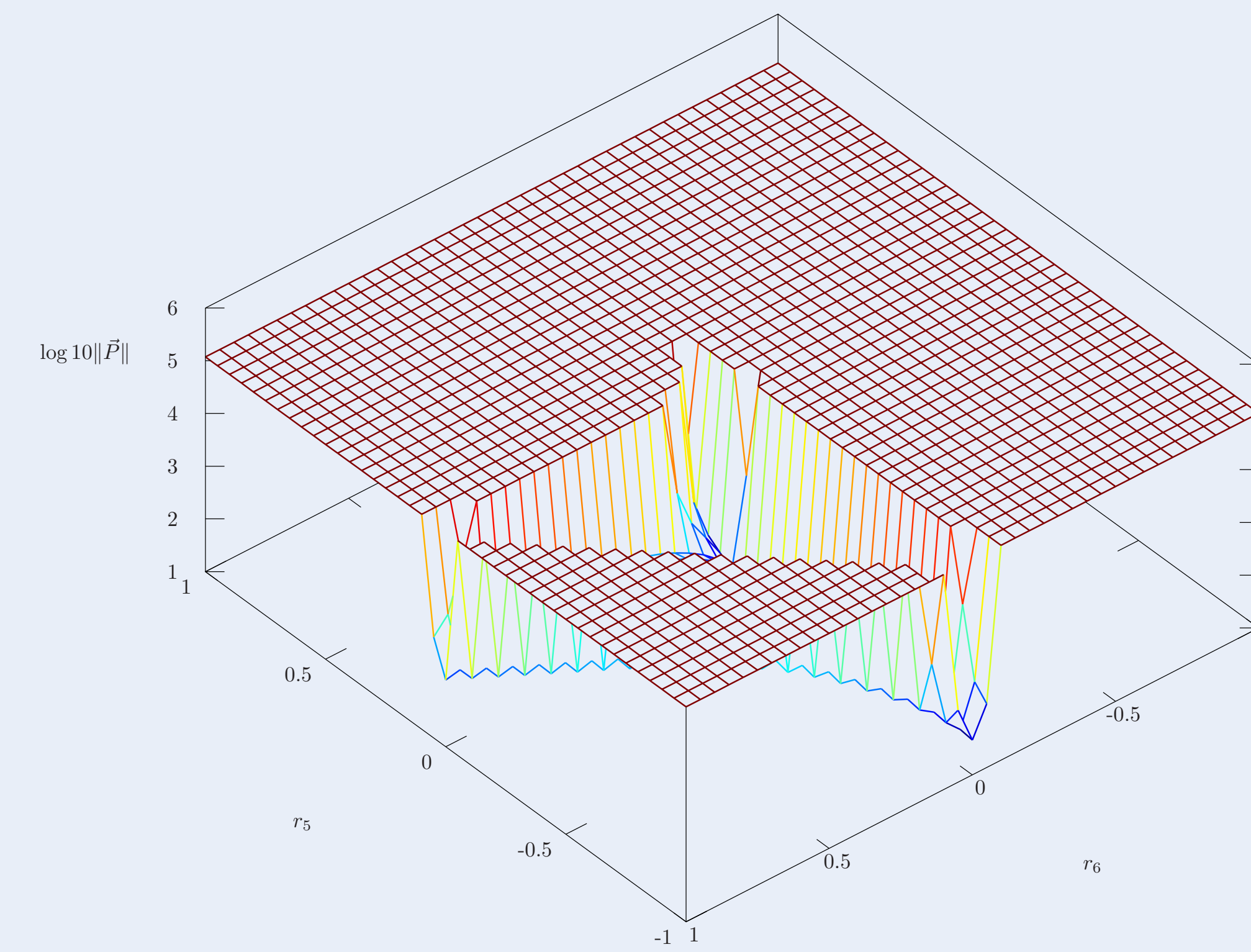
$$\mathbf{B} = \begin{bmatrix} (2^{R_1^{\zeta}} - 1) \cdot \sigma^2 \\ (2^{R_2^{\zeta}} - 1) \cdot \sigma^2 \\ \vdots \end{bmatrix}$$

Then, assuming  $\mathbf{A}$  is non-singular, we could formulate our problem on a matrix formulation:

$$\min_{\mathbf{R}_{cT}^{\mathcal{E}} \in \mathbb{R}^{L-N-1}} \|\mathbf{P}(\mathbf{A}^{-1}\mathbf{B})(\mathbf{R}_{cT}^{\mathcal{E}})\|_1$$

## Simulation

The simulation corresponds to our example. We plot the criterion  $\|\mathbf{P}(\mathbf{A}^{-1}\mathbf{B})(\mathbf{R}_{cT}^{\mathcal{E}})\|_1$  as a function of the relative rate of the co-tree (link 5 and link 6 on the  $\epsilon$  graph). Then, we plot the convergence of the algorithm to the global minimum on  $(0,0)$ .



## Optimization algorithm

We propose to solve this non-convex optimization problem using successive convex optimization. Let  $\mathbf{U} = \text{diag}(\mathbf{A}(\mathbf{R}^{\zeta}))$  and  $\mathbf{V}(\mathbf{R}^{\zeta}) = \mathbf{U} - \mathbf{A}(\mathbf{R}^{\zeta})$ , then optimization criterion becomes:

$$\mathbf{U} \cdot \underbrace{\mathbf{P}}_{\text{Variable}} - \mathbf{V}(\mathbf{R}^{\zeta}) \cdot \underbrace{\mathbf{P}_{cst}}_{\text{Constant}} = \mathbf{B}(\mathbf{R}^{\zeta})$$

$$\hat{\mathbf{P}} = \mathbf{U}^{-1} (\mathbf{B}(\mathbf{R}^{\zeta}) + \mathbf{V}(\mathbf{R}^{\zeta}) \cdot \mathbf{P}_{cst})$$

We showed the minimisation of  $\hat{\mathbf{P}}$  as a function of  $\mathbf{R}_{cT}^{\mathcal{E}}$  is a strictly convex optimisation problem.

**Algorithm 1.** 1. Choose an admissible  $\mathbf{R}^{\zeta}[i]$  (initialisation on direct transmission point, always a solution)

2. Solving problem on that point  
 $\mathbf{P}[i] = \mathbf{A}(\mathbf{R}^{\mathcal{E}}[i])^{-1} \cdot \mathbf{B}(\mathbf{R}^{\mathcal{E}}[i])$ .

3. We minimise power with fixed interference.

$$\hat{\mathbf{P}}[i+1] = \mathbf{U}^{-1} \cdot (\mathbf{V}(\mathbf{R}^{\mathcal{E}}[i]) \cdot \mathbf{P}[i] + \mathbf{B}(\mathbf{R}^{\mathcal{E}}[i]))$$

$$\mathbf{R}^{\mathcal{E}}[i+1] = \arg \left( \min_{\mathbf{R}^{\mathcal{E}} \in \mathbb{R}^{L-N-1}} \|\hat{\mathbf{P}}[i+1]\|_1 \right)$$

4. increment  $i$  by 1 and go to 2

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