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Gaia GraL: Gaia DR2 Gravitational Lens Systems

III. A systematic blind search for new lensed systems[★]

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ABSTRACT

Aims. In this work, we aim to provide a reliable list of gravitational lens candidates based on a search performed over the entire *Gaia* Data Release 2 (*Gaia* DR2). We also aim to show that the astrometric and photometric information coming from the *Gaia* satellite yield sufficient insights for supervised learning methods to automatically identify strong gravitational lens candidates with an efficiency that is comparable to methods based on image processing.

Methods. We simulated 106 623 188 lens systems composed of more than two images, based on a regular grid of parameters characterizing a non-singular isothermal ellipsoid lens model in the presence of an external shear. These simulations are used as an input for training and testing our supervised learning models consisting of extremely randomized trees (ERTs). These trees are finally used to assign to each of the 2 129 659 clusters of celestial objects extracted from the *Gaia* DR2 a discriminant value that reflects the ability of our simulations to match the observed relative positions and fluxes from each cluster. Once complemented with additional constraints, these discriminant values allow us to identify strong gravitational lens candidates out of the list of clusters.

Results. We report the discovery of 15 new quadruply-imaged lens candidates with angular separations of less than 6'' and assess the performance of our approach by recovering 12 of the 13 known quadruply-imaged systems with all their components detected in *Gaia* DR2 with a misclassification rate of fortuitous clusters of stars as lens systems that is below 1%. Similarly, the identification capability of our method regarding quadruply-imaged systems where three images are detected in *Gaia* DR2 is assessed by recovering 10 of the 13 known quadruply-imaged systems having one of their constituting images discarded. The associated misclassification rate varies between 5.83% and 20%, depending on the image we decided to remove.

Key words. gravitational lensing: strong – methods: data analysis – catalogs

1. Introduction

The last two decades have seen the advent of numerous large, deep sky and even time-resolved surveys such as the Two Micron All Sky Survey (2MASS; [Skrutskie et al. 2006](#)), the Catalina Real-Time Survey (CRTS; [Drake et al. 2009](#)), the Wide-field Infrared Survey Explorer (WISE; [Wright et al. 2010](#)), the Sloan Digital Sky Survey (SDSS; [Alam et al. 2015](#)), the Dark Energy Survey (DES; [Dark Energy Survey Collaboration et al. 2016](#)),

the Panoramic Survey Telescope and Rapid Response System (Pan-STARRS; [Chambers et al. 2016](#)), the *Gaia* mission ([Gaia Collaboration 2016](#)), and the Zwicky Transient Facility (ZTF; [Bellm & Kulkarni 2017](#)). Amongst these, *Gaia* stands out as the most accurate instrument performing a whole-sky survey at the present time thanks to its impressive astrometric uncertainties at the μ s level and excellent photometric sensitivity at the mmag level, down to a *G* magnitude of 20.7 if isolated point-like sources are considered.

Through all these surveys, hundreds of millions to billions of celestial objects are being continuously observed over multiple wavelength ranges. This large amount of information, covering the whole celestial sphere, naturally yields a greater chance

[★] The catalogue of clusters of *Gaia* DR2 sources from *Gaia* GraL is only available at the CDS via anonymous ftp to [cdsarc.u-strasbg.fr](ftp://cdsarc.u-strasbg.fr) (130.79.128.5) or via <http://cdsarc.u-strasbg.fr/viz-bin/qcat?J/A+A/622/A165>

of identifying rare objects such as $z > 7$ quasars (Bañados et al. 2018), L and T sub-dwarf stars (e.g. Kirkpatrick et al. 1999, 2014), Type Ia supernovae (e.g. Jones et al. 2018), and multiply-imaged quasars (e.g. Inada et al. 2012; Agnello et al. 2018a).

Strong gravitational lensing depicts the formation of multiple images of a background source whose light rays get deflected and distorted owing to the presence of a massive galaxy standing along the line of sight between the observer and the source. Although predicted by Einstein’s theory of gravitation (Einstein 1936), it was not until 1979 that the first gravitational lens (GL) was finally discovered by Walsh et al. (1979). Since then, strong gravitational lensing has found numerous applications in probing the nature of dark matter (Dalal & Kochanek 2002; Gilman et al. 2018), in determining the shape of the dark matter halos of galaxies (Shajib et al. 2019) or clusters of galaxies (Meneghetti et al. 2017; Jauzac et al. 2018), as natural telescopes for detecting otherwise unobservable sources (Peng et al. 2006; Zavala et al. 2018), or as a way to set constraints on cosmological parameters irrespective of the cosmic distance ladder (Refsdal 1964; Suyu et al. 2013; Tagore et al. 2018). Notwithstanding their crucial importance in cosmology, the number of known GLs still remains very limited with just ~ 200 spectroscopically confirmed GLs, of which only ~ 45 are composed of more than two lensed images (see e.g. Ducourant et al. 2018, Table 1). In addition to the fact that GLs are intrinsically rare, this scarcity is also due to the difficulty in identifying them in large astronomical catalogues.

Conscious of the unique opportunity brought by these modern large sky surveys, numerous methods were recently developed to systematically search for GLs (Bolton et al. 2008; More et al. 2016; Paraficz et al. 2016; Agnello et al. 2018a,b; Jacobs et al. 2017; Lee 2017; Pourrahmani et al. 2018; Lemon et al. 2019). At the state of the art of these identification techniques, the Strong Gravitational Lens Finding Challenge (Metcalf et al. 2018) is a recent effort to identify GLs in large scale imaging surveys such as the upcoming Square Kilometer Array (SKA)¹, the Large Synoptic Survey Telescope (LSST)², and the *Euclid* space telescope³. The solutions envisaged to fulfil the proposed challenge encompass visual inspection procedures (Hartley et al. 2017), arcs and rings detection algorithms (Alard 2006; More et al. 2012; Sonnenfeld et al. 2018), and supervised machine learning methods (Bertin et al. 2012; Avestruz et al. 2017; Lanusse et al. 2018). Because GLs are rare objects, all these techniques have as a common objective to minimize the rate of contaminants among the predicted GL candidates.

The *Gaia* space mission is mainly dedicated to the production of a dynamical three-dimensional map of our Galaxy (Gaia Collaboration 2016). In addition, it will provide valuable informations for millions of extragalactic objects (e.g. Tsalmantza et al. 2012; Krone-Martins et al. 2013; Bailer-Jones et al. 2013; de Souza et al. 2014), including the detection of new GLs (e.g. Agnello et al. 2018a; Wertz et al. 2018; Lemon et al. 2019; Ostrovski et al. 2018). Amongst the two billion objects that *Gaia* will observe, we expect ~ 2900 GLs to be present in the final data release, of which more than 250 should have more than two lensed images (Finet & Surdej 2016). This constitutes an order of magnitude increase compared to the number of currently known GLs.

In the present work, we aim to detect new GL candidates from a blind search performed over the second data release of the

Gaia catalogue (Gaia Collaboration 2018, hereafter *Gaia* DR2). To do so, we trained and applied a supervised learning method, called extremely randomized trees (ERTs; Geurts et al. 2006), whose input are the precise relative positions and fluxes from clusters of celestial objects extracted from the *Gaia* DR2. We concurrently show that these ERT models, despite their restricted input data (i.e. astrometry and photometry), can reach performance levels that are comparable to those of the best model from the Strong Gravitational Lens Finding Challenge (Lanusse et al. 2018). Specifically, we achieve a 90% identification rate of GLs with a misclassification rate of clusters of stars as GLs below 1%. A preliminary version of this method was already successfully used in Krone-Martins et al. (2018) in order to identify three GL candidates, of which two were spectroscopically confirmed: GRAL113100–441959 by our group and WGD2038–4008 by Agnello et al. (2018a) and independently selected by us. The present paper gives a detailed overview of the final method, of its performance, and its application to the whole *Gaia* DR2.

This study was carried out inside the *Gaia* Gravitational Lenses working group, or *Gaia* GraL, whose main objective is to unravel the possibilities offered by the ESA/*Gaia* satellite to identify and study GLs. This article is the third in a series of works produced based on *Gaia* DR2.

In Sect. 2 we present the methods we specifically developed for extracting clusters of objects out of the *Gaia* DR2. In Sect. 3.1, we detail the use we made of the relative image positions and flux ratios of simulated GL systems so as to train supervised learning models with a view of identifying GL candidates in list of clusters (Sect. 3.2). The performance of our classification algorithm is covered in Sect. 3.3. Based on the resulting ERT predictions, a sample of the most promising GL candidates is given in Sect. 3.4. Finally, we discuss our findings and conclude in Sect. 4.

2. Extraction of clusters of objects from *Gaia* DR2

Our blind search for new GL candidates first consists in the extractions of clusters of objects out of the entire *Gaia* DR2. The latter can be accessed through the *Gaia* Archive bulk retrieval data facility⁴. The details of this extraction is covered in the present section, while the resulting catalogue of clusters obtained from *Gaia* DR2 sources is presented in Appendix B.

Prior to this extraction, we recall that all deflected sources from strong GLs consist of extragalactic sources. We thus expect the lensed images to have negligible parallaxes, ϖ , and proper motions, $(\mu_{\alpha^*}, \mu_{\delta})$ where $\mu_{\alpha^*} = \mu_{\alpha} \cos \delta$. We thus beforehand filtered the *Gaia* DR2 using the soft astrometric test described in Ducourant et al. (2018). Specifically, we rejected observations having either $\varpi - 3\sigma_{\varpi} \geq 4$ mas or $|\mu| - 3\sigma_{\mu} \geq 4$ mas yr⁻¹ (where μ stands for μ_{α^*} and μ_{δ}). Adopting a conservative approach, we did not discard the observations when ϖ , μ_{α^*} , μ_{δ} , or their associated uncertainties were missing. The number of sources we used was then reduced from 1 629 919 135 that are present in the original *Gaia* DR2 down to 1 217 192 458 that passed the soft astrometric test. We note that two known GLs from Table 1 do not pass the soft astrometric test: DESJ0405–3308 (where the image having *Gaia* source identifier 4883180423151513088 has $\mu_{\alpha^*} = 16.44 \pm 1.723$ mas yr⁻¹ and $\mu_{\delta} = -13.43 \pm 2.143$ mas yr⁻¹) and RXJ0911+0551 (where the image having *Gaia* source identifier 580537092879166848 has $\mu_{\alpha^*} = -7.76 \pm 1.026$ mas yr⁻¹). The very large proper motions observed in DESJ0405–3308 can

¹ <http://skatelescope.org>

² <https://www.lsst.org>

³ <https://www.euclid-ec.org>

⁴ http://cdn.gea.esac.esa.int/Gaia/gdr2/gaia_source/csv/

Table 1. List of all spectroscopically confirmed quadruply-imaged systems having $N_{\text{img}} = 3, 4$ components detected in *Gaia* DR2.

Lens identifier	N_{img}	Size (mas)	ΔG (mag)	$\Delta(G_{\text{BP}} - G_{\text{RP}})$ (mag)	Field density (obj. deg ⁻²)	ERT probabilities				
						ABCD	ABC	ABD	ACD	BCD
2MASSJ11344050–2103230	4	3682	1.76	0.16(3)	18 335	1.00	0.97	0.66	0.72	0.31
J1606–2333	4	1723	0.76	0.07(2)	50 420	1.00	0.9	0.99	0.94	0.84
WGD2038–4008	4	2869	0.65		22 918	1.00	1.00	0.86	0.7	0.72
HE0435–1223	4	2539	0.73	0.29(2)	18 335	0.99	0.92	0.7	0.75	0.78
PG1115+080	4	2427	1.79	0.02(3)	18 335	0.99	0.98	0.99	0.75	0.69
B1422+231	4	1281	3.46		22 918	0.98	0.87	0.98	0.83	0.59
J2145+6345 ^{a,b}	4	2068	1.70		73 339	0.97	0.96	0.92	0.95	0.86
2MASXJ01471020+4630433	4	3262	2.37	0.10(2)	41 253	0.95	0.66	0.99	0.55	0.51
2MASSJ13102005–1714579	4	5735	1.21	0.21(3)	22 918	0.92	0.93	0.92	0.85	0.84
J1721+8842 ^c	4	3906	1.75	0.13(2)	27 502	0.91	0.32	0.99	0.65	0.84
WFI2033–4723	4	2533	1.18	0.04(2)	18 335	0.89	0.98	0.8	0.67	0.99
SDSS1004+4112 ^b	4	14 732	1.35	0.22(4)	22 846	0.88	0.99	0.24	0.99	0.19
RXJ1131–1231	4	3232	2.11		22 918	0.65	0.69	0.93	0.56	0.72
SDSSJ1433+6007	3	3754	0.38	0.04(2)	13 751		0.99	0.92	0.52	0.65
DESJ0405–3308 ^{a,b}	3	1416	0.20	0.32(3)	13 751		0.98	0.78	0.66	0.93
J0408–5354	3	4184	1.08	0.30(2)	22 918		0.42	0.56	0.97	0.95
HE0230–2130	3	2188	1.03		13 751		0.95	0.75	0.08	0.05
H1413+117	3	1111	0.25	0.12(2)	18 335		0.86	0.48	0.6	0.65
RXJ0911+0551 ^b	3	3260	1.11	0.04(2)	27 502		0.65	0.19	0.67	0.07
J0630–1201	3	1901	0.11	0.33(3)	36 669		0.58	0.1	0.09	0.3
WISE025942.9–163543	3	1577	0.76		13 751		0.32	0.45	0.16	0.32

Notes. The lens size and the maximum absolute difference in magnitude and colour, ΔG and $\Delta(G_{\text{BP}} - G_{\text{RP}})$, are computed over all combinations of the lensed images while the field density is estimated within a radius of $30''$ around the system. The numbers in parentheses in Col. $\Delta(G_{\text{BP}} - G_{\text{RP}})$ correspond to the number of images that were used in the computation of the maximum absolute difference in colour. Four image configurations are processed using the ERT model ABCD, as well as using all the ABC, ABD, ACD, and BCD models based on the appropriate combination of images (see Sect. 3). Three image configurations are processed using models ABC, ACD, ABD, and BCD. ^(a)J2145+6345 and DESJ0405–3308 are not contained in the original list of known gravitational lenses from Ducourant et al. (2018) as their discovery was announced after the list was compiled (see Lemon et al. 2019; Anguita et al. 2018, respectively). ^(b)J2145+6345, SDSS1004+4112, DESJ0405–3308, and RXJ0911+0551 are not part of the final catalogue of clusters (Appendix B) because they are found in regions of high stellar density (J2145+6345), because one of their images does not pass the soft astrometric test (DESJ0405–3308 and RXJ0911+0551), or because the angular size is too large (SDSS1004+4112). ^(c)For J1721+8842, we selected the configuration of four images out of the five images available for which the ERT probabilities was the highest (0.91). Alternative combinations implying image with *Gaia* source identifier 1729026466114871296 provide ERT probabilities between 0 and 0.05.

be presumably explained by the fact that this image has a large astrometric excess noise of $\epsilon = 5.791$ mas, and is hence not astrometrically well behaved.

Because an exhaustive analysis of all combinations of objects from *Gaia* DR2 is infeasible and not desirable, we restricted our search for clusters to those having a finite angular size and a limited absolute difference in magnitude between their components. Extraction criteria were accordingly based on the characteristics of known quadruply-imaged systems from Table 1. Amongst the listed GLs, all have angular sizes smaller than $5.8''$, with the exception of SDSS1004+4112. Also, none of them is composed of images having an absolute difference in G magnitude, ΔG , larger than 3.5 mag. Considering that the extraction of clusters comparable in size to SDSS1004+4112 (i.e. $\sim 15''$) would result in a too large fraction of fortuitous aggregations of stars in our final list of GL candidates, we finally adopted the following convention: clusters of celestial objects must have (i) three or four images in order to provide a sufficient number of constraints for identifying GL candidates out of these clusters and to enable their subsequent modelling, (ii) a maximum angular separation between any pair of images that is below $6''$, and (iii) an absolute difference in G magnitude between components lower than 4 mag.

Without any further constraints, we expect the vast majority of our GL candidates to naturally fall in regions of high stellar

densities such as the Galactic plane, the Magellanic clouds, or globular clusters. In order to identify these high density regions, we evaluated the local density of objects around each cluster based on the *Gaia* DR2. A mean density of objects was accordingly computed within a radius of $30''$ around each cluster. This radius was selected as a trade-off between its statistical significance and its locality property. From Table 1, nearly all known GLs reside in regions with a mean field density $\rho < 3 \times 10^4$ objects deg⁻², therefore avoiding globular clusters and dense regions of the Galactic plane (see Fig. 1). None of the known quadruply-imaged GLs, with the exception of J2145+6345 that was discovered after the submission of the present paper (Lemon et al. 2019), resides in regions with mean field density $\rho \geq 6 \times 10^4$ objects deg⁻². Accordingly, we set an upper limit on the density of objects surrounding each cluster of 6×10^4 objects deg⁻².

The production of the list of clusters is based on a search for neighbours around each of the *Gaia* DR2 sources that passed the soft astrometric test⁵. All combinations of three or four images were considered to produce the final list of clusters as the deflecting galaxy or contaminating stars might be present within the identified clusters.

⁵ For this purpose we used a subdivision of the celestial sphere based on the Hierarchical Triangular Mesh (Kunszt et al. 2001).

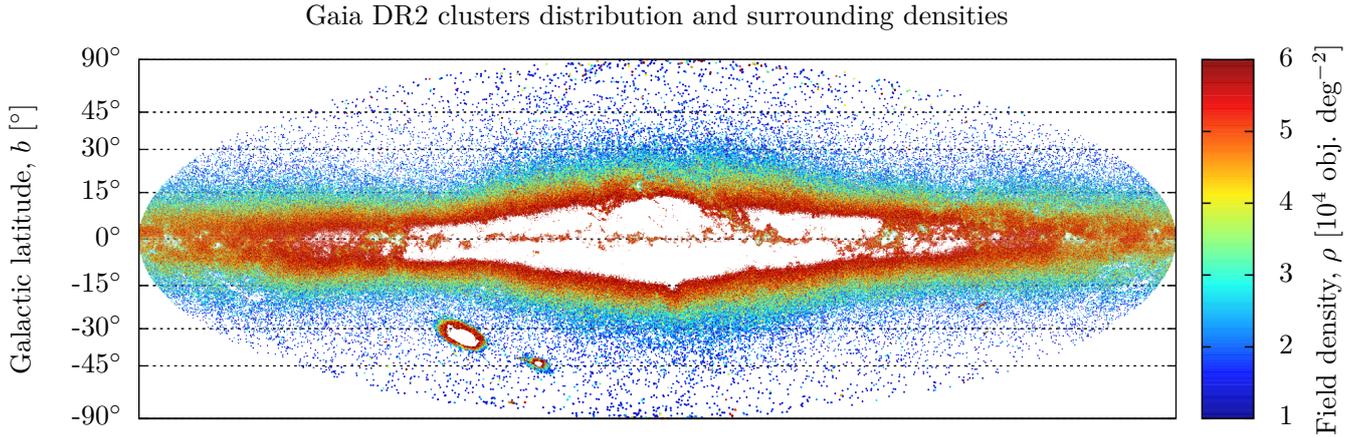


Fig. 1. Distribution of the 2 129 659 clusters of objects extracted from the *Gaia* DR2 catalogue. They are composed of three and four images that pass the soft astrometric test (see Sect. 2) that have a maximum angular separation between components that is smaller than $6''$, that have absolute differences in G magnitudes of <4 mag, and that are found in regions of the celestial sphere where the mean field density is lower than 6×10^4 objects deg^{-2} . Lower density regions near the galactic centre can be explained by the filtering occurring in the on-board processing in order to prevent memory from saturating in such very dense regions of the sky (Gaia Collaboration 2016).

Each cluster was then assigned a unique identifier based on the mean position of its constituent sources. The common convention of taking the position of the brightest image as an identifier for GL systems was not adopted here as it would lead to ambiguities in identifying clusters for which all combinations of images were explored. Figure 1 illustrates the distribution of the 2 129 659 clusters derived from *Gaia* DR2, amongst which 2 058 962 have three components and 70 697 have four components. Also depicted are the mean field densities that are associated with each of these clusters.

3. Identification of lens candidates from supervised learning method

After we defined the list of clusters, the second step in our methodology to perform a blind search for new GLs was the assignment of a discriminating value, called the extremely randomized trees (ERT) probability, to each cluster. These ERT probabilities, P , do not constitute probabilities in a mathematical sense and should rather be viewed as a figure of merit or as a score that reflects the ability of the clusters to be matched to the image positions and relative magnitudes produced from simulations of lens systems (see Sect. 3.1). They can, however, be translated into expected ratios of identification of GLs and to expected ratios of misclassification of groups of stars as GLs through the use of an appropriate cross-validation procedure.

3.1. Catalogue of simulated gravitational lenses

Supervised learning methods aim to automatically discover the relations that may exist between a set of input attributes and an associated outcome value based on a collection of training instances. The more complete and representative the learning set of observations, the fairer and more accurate the resulting predictions are (e.g. Beck et al. 2017). Training sets can be constructed either directly by using observational data or by using simulations. Regarding the specific problem of the identification of GL candidates, the limited number of 44 known quadruply-imaged systems from the list of Ducourant et al. (2018), of which only 19 have more than two

images that are detected in *Gaia* DR2, forces us to rely on simulations to cover the input space of attributes in a satisfying manner.

To construct our training set, we consider a non-singular isothermal ellipsoid lens model in the presence of an external shear (hereafter NSIEg lens model, Kormann et al. 1994; Kovner 1987, see Appendix A for a concise description). This model has been proven to be well suited for reproducing the relative positions and flux ratios of the lensed images when the deflector is a massive late-type galaxy. A consequence of choosing this specific model is that the GL candidates we can identify through supervised learning methods will be restricted to systems that can be described well by this particular model. However, this does not constitute a major drawback to our implementation as most of the known lens systems are generally described well by this particular model.

Accordingly, we simulated 106 623 188 GL systems having four observable images based on a plausible range of parameters for the NSIEg lens model as listed in Table 2. For completeness, we note that a redundancy exists amongst the produced simulated GL systems. This is a natural consequence of a NSIEg lens model as, for example, all lens models with a shear orientation of $\pi - \omega$ and source position $(-x_s, y_s)$ are the horizontal reflections of models with a shear orientation of ω and a source position of (x_s, y_s) .

3.2. Extremely randomized tree supervised learning models

Extremely randomized tree probabilities are derived from a tree-based machine learning algorithm that relies on the assumption that the aggregation of the predictions of several weak, strongly randomized trees can compete or even surpass more sophisticated methods like artificial neural networks (Haykin 1998) or support vector machines (Cortes & Vapnik 1995). This assumption was initially supported by Mingers (1989) and was later successfully implemented in the bootstrap aggregating meta-algorithm (Breiman 1996) and in random forests (Breiman 2001). The usual classification and regression trees (CARTs) select at each node of the tree the attribute and cut-value within this attribute that best split the learning set of observations associated with this node according to a given score measure (e.g. the reduction of the variance in regression problems or the

Table 2. Range of parameters explored to produce the simulated lens catalogues from a NSIEg lens model.

Explored range	NSIEg parameters					
	b	q	s	γ	ω	x_s, y_s
Range start	1	0.2	0	0	0°	-1
Step	-	0.05	0.01	0.01	5°	0.02
Range end	-	1	0.3	0.3	175°	1

Notes. A detailed description of these parameters is provided in Appendix A.

information gain in classification problems); instead, the ERT algorithm picks up a subset of K random attributes as well as a random cut-point within each of these attributes so as to select the split that maximizes the given score measure (Geurts et al. 2006). The algorithm ends when no more than n_{\min} training observations remain in all leaf nodes. The aggregation of the predictions of N trees (a majority vote in our case) then lessens the variance of the ERT, in the sense that it prevents the model from being too specific to the learning set of observation we used while not being able to generalize the learned relations over unseen observations.

As we expect some of the lensed images to be missing from *Gaia* DR2 (see Table 1 for examples), all combinations of three and four images were considered for building the ERT. Also, as the central and strongly de-magnified image produced in NSIEg-like GLs is often out of reach of the *Gaia* photometric sensitivity, it was not taken into account. These ERT models are referred to in the following as ABCD, ABC, ABD, ACD, and BCD, where A, B, C, and D identify the images we used during the learning phase of the corresponding ERT sorted in ascending order of G magnitude.

All ERT models were trained using a learning set (LS) of observations composed of half the number of simulations we described in Sect. 3.1, plus an equal number of contaminant observations for which both the image positions and magnitudes were randomly drawn from a uniform distribution. We note that these simulated contaminants are still restricted to have an absolute difference in magnitude (ΔG) lower than 4 mag, in agreement with the requirements we developed in Sect. 2. The other half of the simulations is then kept as a test set (TS) of observations for cross-validation purpose, after being complemented by the addition of simulated contaminants. It is important to note here that neither LS nor TS follows a realistic distribution of positions and magnitudes as this would require, for example, the distribution of the eccentricity of the lensing galaxy or the properties of clusters of stars to be taken into account. These sets were solely designed with the aim of identifying the regions of the input space of parameters (i.e. relative positions and fluxes) where GLs and contaminants are located through the use of the ERT.

We then added a Gaussian noise to the image positions, σ_{xy} , and magnitudes, σ_G , for each of the LS and TS configurations before discarding some of their images in order to create the input instances used in the ABCD, ABC, ABD, ACD, and BCD models. These configurations are then normalized through an orthogonal transformation and a scaling to have their brightest image (image A) repositioned at (0, 0) along with a magnitude of 0 and their faintest image (image C or D, depending on the number of images of the configuration) repositioned at (1, 0).

The addition of noise to the simulations in the present case is not designed to take into account the astrometric and

photometric uncertainties of *Gaia* DR2, which are actually much lower than the noise we introduced. Rather, this noise was added to deal with the possible imperfections of the NSIEg model, and to enable the machine learning method to deal with lenses that depart from this idealized model (e.g. due to substructures in the deflecting galaxies or to the inherent fact that the NSIEg lens model only constitutes an approximation of GLs whose deflectors are late-type galaxies). Similarly, the noise added to the magnitudes reflects the fact that micro-lensing events frequently occur due to galaxy substructures. Also, because of the difference in the optical paths of the lensed images, time delays exist between each of them, such that if the deflected source is a variable object, as quasars are, discrepancies would exist between our instantaneous noiseless simulations and real observations.

Regarding the ERT model ABCD, the set of input attributes is composed of the normalized images positions (x_B, y_B) and (x_C, y_C); of the normalized G magnitudes G_B, G_C, G_D ; and of their respective differences ($x_B - x_C, y_B - y_C$), $G_C - G_B, G_D - G_B$, and $G_D - G_C$. We recall that, because of the normalization procedure, $x_A = y_A = y_D = G_A = 0$, while $x_D = 1$. The attributes used in the ERT model ABC is then similarly given by (x_B, y_B), G_B, G_C , and $G_C - G_B$, from which the attributes used in the ABD, ACD, and BCD models can be easily extrapolated.

The parameters of the ERT models (i.e. N , K , and n_{\min}) as well as the level of noise we add to each of the LS and TS configurations, σ_{xy} and σ_G , were chosen in a heuristic way based on the identification performance of a validation set (VS) of observations, composed of the known lensed systems having four detections in *Gaia* DR2⁶ (see Table 1) and of 10^6 clusters we randomly extracted from *Gaia* DR2 with a size smaller than 30'' and $\Delta G < 4$ mag. Various combinations of these parameters were probed in the ranges $N \in [10, 1000]$, $K \in [2, 12]$, $n_{\min} \in [2, 8]$, $\sigma_G \in [0, 1]$, and $\sigma_{xy} \in [0, 0.1 s]$, where s stands for the lens size. The set of parameters we selected regarding the ABCD models, $N = 100$, $K = 12$, $n_{\min} = 2$, $\sigma_{xy} = 0.01 s$ and $\sigma_G = 0.25$, yield a satisfactory fraction of 75% of GLs that are correctly identified along with a misclassification rate of clusters of stars as GLs of 0.625% if $P > 0.9$. Not surprisingly, tests performed on the ABC, ABD, ACD, and BCD models lead to the same set of parameters, with the exception of $K = 5$, though the associated identification capabilities are now largely hampered.

3.3. Performance of the identification of known and simulated gravitational lenses

The performance of each model in classifying GL candidates were assessed by computing, for each of them, the fraction of GLs that are correctly identified (the true positive rate) and the fraction of clusters of stars that are misclassified as GLs (the false positive rate). By reporting the true and false positive rates (hereafter TPR and FPR, respectively) that are associated with all ERT probabilities in a graph, we obtain the receiver operating characteristics (ROC) curves, shown in Fig. 2. In the same figure, the area under the ROC curve (AUC) is a commonly used measure of the classification capability of each model. For completeness, we note that some simulated contaminants from our training set cannot be differentiated from the relative image positions and fluxes produced through NSIEg lens models. Regarding our ERT models, this has the effect of decreasing the TPR evaluated on the test set while increasing the associated FPR.

⁶ J2145+6345 was not used to build our ERT models or to determine the level of noise to add to our simulations as this lens had not been published at the time of submission.

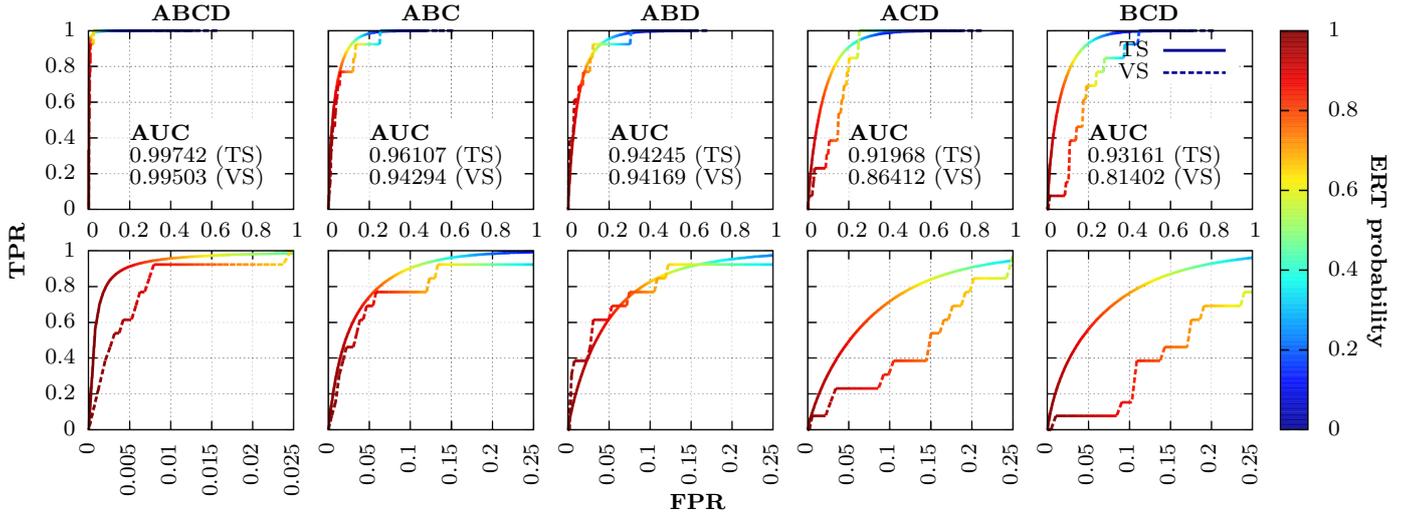


Fig. 2. Receiver operating characteristics (ROC) curve of the ABCD, ABC, ABD, ACD, and BCD models based on the test set (TS) and validation set (VS) of observations. The upper panels show the entire ROC curves, whereas the lower panels concentrate on the low FPR regions of each curve. The classification performances of each model is evaluated through the computation of the area under each of the TS–ROC and VS–ROC curves (AUC).

Even so, as this degeneracy is seen in real observations, we decided not to remove these ambiguous simulations from our training set.

We can see from Fig. 2 and Table 1 that the ERT model ABCD is able to identify 12 of the 13 known GLs (92.3%) and 92.5% of the simulated GLs along with a FPR that is below 1% if $P > 0.84$. The associated AUC (0.99503 if evaluated on the validation set or 0.99742 if evaluated on the test set) can be compared with the 0.98 obtained by the best lens classifier of the Strong Gravitational Lens Finding Challenge (Lanusse et al. 2018) where a FPR of 1% is associated with a TPR of 90% (Metcalf et al. 2018). However, these numbers should be taken with care given the difficulties in equitably comparing two models designed for different instruments, having different angular resolutions and photometric sensitivities, and working directly on images on the one hand and on reduced data on the other. In a more recent work, Wynne & Schechter (2018) achieve a TPR of 80% along with a FPR of 2% by directly modelling the quadruple lens systems through the fit of a right hyperbola to the observed relative positions of the lensed images (Witt 1996). Cuts on the resulting axis ratio, q , and on the scatter of the observed images around the fitted hyperbola being then used to select GL candidates. These comparisons demonstrate the efficiency of the approach adopted in the present work and more particularly of the ERT on this particular problem. These results also demonstrate the huge potential of *Gaia* regarding the identification of GLs, mostly coming from its impressive astrometric and photometric precision.

The ERT models ABC and ABD provide FPRs of 5.83% and of 7.48%, respectively, on the validation set if they are associated with a TPR of 75%. The FPR associated with the test set are 5.08% and of 7.74%, respectively, for the same TPR. Nevertheless, if a TPR of 75% is considered for the models ACD and BCD, then the corresponding FPR computed on the validation set rises to $\sim 20\%$ ($\sim 10\%$ on the test set). These larger FPRs apparently come from the intrinsic difficulty that the ERT have in identifying GLs for which the two brightest images are not seen together, as illustrated by the ROC curves computed on the test set. Also, the discrepancies noticed in the ROC curves computed based on the test set, on the one hand, and on the validation set,

on the other hand, can be explained by the statistical fluctuations due to the low number of known GLs present in the validation set (13) and by the fact that they contain different populations of lenses (i.e. the validation set contains a realistic population of lenses, whereas the test set contains a population of simulated lenses coming from a uniform coverage of the NSIEg parameters). We note that FPRs as low as a few per cent still lead to a large number of contaminant observations in the final catalogue, owing to the 2×10^6 clusters identified in *Gaia* DR2. The appropriate filtering of these numerous contaminants is described in Sect. 3.4.

In addition to the overall performance of our approach, some of the known lenses from Table 1 are still being assigned low ERT probabilities, P , namely J0630–1201 ($P_{ABC} = 0.58$), RXJ0911+0551 ($P_{ACD} = 0.67$), RXJ1131–1231 ($P_{ABCD} = 0.65$), and WISE025942.9–163543 ($P_{ABD} = 0.45$). The first of these, J0630–1201, is a recently discovered GL composed of five lensed images and two deflecting galaxies (Ostrovski et al. 2018), which can thus not be reproduced through a single NSIEg lens model. The GLs RXJ0911+0551 and RXJ1131–1231 have flux ratios that are difficult to reproduce without including microlensing by small-scale structures in the lens galaxy (Keeton et al. 2003). The fact that RXJ1131–1231 obtains an ERT probability of $P_{ABD} = 0.93$ once image C is discarded also supports this hypothesis. The study of the recently discovered GL WISE025942.9–163543 currently remains very limited, though the preliminary modelling performed by Schechter et al. (2018) using a non-singular isothermal sphere lens model in the presence of external shear (i.e. NSIEg lens model with $q = 1$ and $s = 0$) has already highlighted the difficulties in reproducing the observed flux ratios, even if the image positions can be fairly well reproduced by this kind of model (Wynne & Schechter 2018). The modelling that we have performed using a NSIEg lens model has led to the same conclusion.

We also note that two GL candidates, PS1J205143–111444 and WGD2141–4629, were already present in the original list of Ducourant et al. (2018). These candidates obtain maximum ERT probabilities of $P_{ABD} = 0.01$ and of $P_{ABC} = 0.62$, respectively. Whereas PS1J205143–111444 is probably not a GL that is reproducible through a NSIEg lens model, the lensing nature

of WGD2141–4629 remains uncertain though highly improbable because of the non-negligible, opposite proper motions of two of its images, while one of them is astrometrically well behaved (i.e. astrometric excess noise of $\epsilon = 0$ mas). More recently, [Agnello & Spiniello \(2018\)](#) discovered two new quadruply-imaged lens candidates, WG210014.9–445206.4 and WG021416.37–210535.3, that are not part of our input list of candidate lenses taken from [Ducourant et al. \(2018\)](#). These candidates obtain maximum ERT probabilities of $P_{ABC} = 0.4$ and $P_{ABC} = 0.94$, respectively. Even though the lensing nature of WG210014.9–445206.4 looks very promising, it was not recognized by our method. Possible reasons are the finite identification rate (TPR) of the ERT or the hardly reproducible relative positions and magnitudes of this system through a NSIEg lens model.

Finally, we mention that the ERT models described here differ significantly from those we built and used in Paper I ([Krone-Martins et al. 2018](#)) as we adjusted our model to known GLs contained in *Gaia* DR2, whereas only SDSS J1004+4112 had all its components detected in *Gaia* DR1.

3.4. Identification of new gravitational lens candidates

Finally, we applied the methodology developed in this work to the 2 129 659 clusters we extracted from the *Gaia* DR2 with a view of identifying GL candidates. The resulting catalogue of clusters, along with their associated ERT probabilities, is further described in Appendix B; the distributions of these ERT probabilities regarding the clusters and the known lenses they contain are also provided in Fig. 3. From this figure, we can see that most of the clusters have low ERT probabilities; for example, 43.34% of the clusters composed of three images and 89.52% of the clusters composed of four images have ERT probabilities $P < 0.2$. Conversely, 10 of the 11 known lenses composed of four *Gaia* detections and 36 of the 50 known lenses composed of three detections⁷ have an ERT probability $P > 0.8$. We note that the large number of clusters having high ERT probabilities amongst the clusters composed of three images is due to the choice we made to consider a single ERT probability that is taken as the maximum of the probabilities that are returned by the ABC, ABD, ACD, and BCD models. This choice is justified by the fact that if we observed a genuine quadruply-imaged quasar having only three detections in *Gaia* DR2, we do not know which of the images was unobserved and consequently, in a conservative approach, we have to consider the ERT model that worked best.

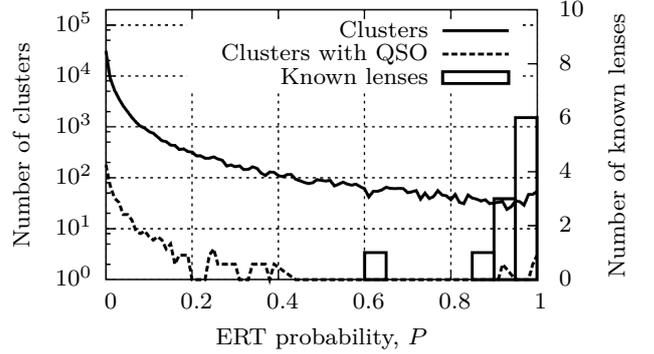
In the following, we do not aim to provide an exhaustive list of the GLs that are contained in this catalogue, but rather to provide the community with a very pure list of GL candidates at the expense of a lower completeness. We note again here that GLs having prominent substructures in the lensing galaxy, multiple lensing galaxies, and/or high variability will be hardly identified by the ERT as these are often not modelled well with NSIEg lens models.

3.4.1. Systematic blind search of gravitational lenses composed of four images

In this first approach, our aim was to systematically and blindly identify GL candidates that are composed of four *Gaia* detec-

⁷ Forty-four of the known gravitational lens systems composed of three images come from the combination of the images of the 11 known systems composed of four images while 6 are known systems for which an image was undetected (see Table 1 for details).

Distribution of clusters composed of four images



Distribution of clusters composed of three images

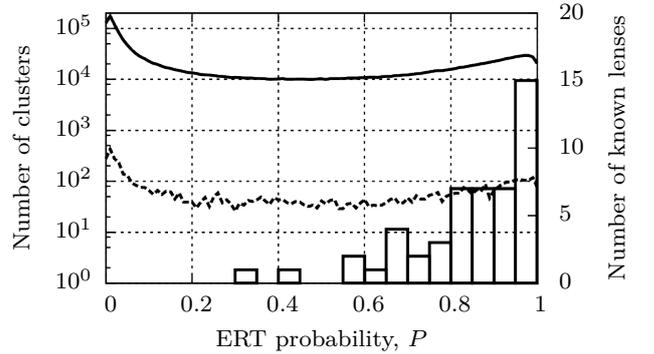


Fig. 3. Distribution of the 70 697 clusters composed of four images and 2 058 962 clusters composed of three images extracted from the *Gaia* DR2 (see Sect. 2) with respect to their ERT probabilities (solid line). The distribution of the known lenses are represented as boxes, whereas the distribution of the 6,944 clusters resulting from the cross-match we performed between our entire list of clusters and our compiled list of quasars is depicted as a dotted line in each graph (see Sect. 3.4.2). In cases where clusters are composed of three images, the ERT probability corresponds to the maximum of the ERT probabilities returned by the ABC, ABD, ACD, and BCD models.

tions while sharing common properties with the set of known lenses from Table 1. The reason for considering these four image candidates apart from those composed of three images lies first in the benefit we can draw from the excellent performance of the ABCD ERT model. Furthermore, it is impossible to have a systematic search for lenses in the triplet regime because of the relatively high FPR of the ABC, ABD, ACD, and BCD ERT models ($5\% \leq \text{FPR} \leq 20\%$) and because of the numerous clusters to which they will be applied (2 058 962 clusters composed of three images).

According to the mean density of objects found around known known GLs (see Table 1) and based on the maximum absolute difference in colour between their lensed images, $\Delta(G_{BP} - G_{RP})$, we first restricted our four-image candidates to regions where $\rho < 3 \times 10^4$ objects deg^{-2} , while having a maximum absolute difference in colour $\Delta(G_{BP} - G_{RP}) < 0.4$ mag, when available. Similarly, we also required our candidates to have an ERT probability of $P > 0.9$. Of the ten clusters satisfying these criteria, seven are known lenses (2MASS J11344050–2103230, WGD2038–4008, HE0435–1223, PG1115+080, B1422+231, 2MASS J13102005–1714579, and J1721+8842), while three clusters (numbered [4], [15] and [18] in the finding charts from Fig. 4 and Table 3) are new GL candidates. This first analysis already proved the identification capability of our approach based solely on data products

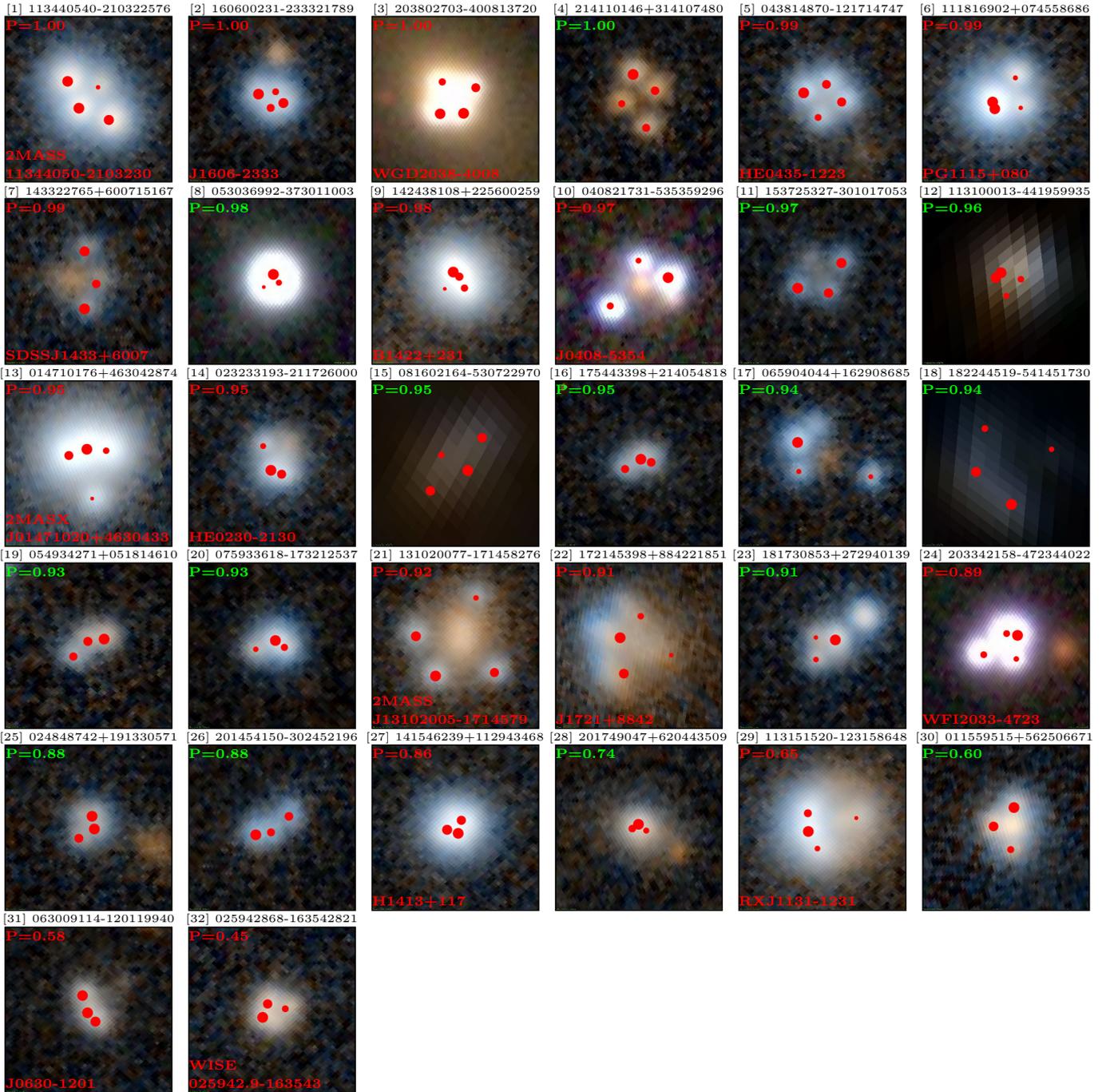


Fig. 4. Finding charts of the 17 known GLs and 15 GL candidates contained in our catalogue of clusters (Appendix B). They are ordered according to their ERT probabilities (upper left corner of each subplot). The common name of the known lenses is labelled in red in the lower left corner of each subplot, while the candidates we propose have their probabilities written in green fonts. Images [1], [2], [4–7], [9], [11], [13], [14], [16], [17], [19–23], [25–32] come from the Pan-STARRS survey (Chambers et al. 2016); images [12], [15], [18] come from the Digitized Sky Survey II (Lasker et al. 1996); and images [3], [8], [10], [24] come from the DES (Dark Energy Survey Collaboration et al. 2016). All images were collected from the ALADIN sky atlas (Bonnarel et al. 2000) in a field of view of $10.8'' \times 10.8''$ centred around the mean coordinates of the GL where east is to the left and north is up. Points are scaled according to the relative flux of the components with respect to the brightest image of each configuration.

from the *Gaia* DR2. Nevertheless, candidate number [4] is probably not a GL in our opinion, mostly because of the red colour of its constituent images. Similarly, the DSS2 images of candidates [15] and [18] do not have sufficient angular resolution to determine their lensing nature. Even so, their relative image positions and fluxes are compatible with those produced by NSIEg-like lenses.

3.4.2. Search for gravitational lenses around quasars and quasar candidates

A systematic blind search for new lensed systems where only three images are detected in *Gaia* is not feasible given the numbers we provided in Fig. 3. Instead, constraints from external catalogues have to be used so as to lessen the number

Table 3. List of GL candidates.

Num.	Candidate identifier	N_{img}	Right ascension ($^{\circ}$)	Declination ($^{\circ}$)	Size (mas)	Field density (obj. deg $^{-2}$)	ΔG (mag)	$\Delta(G_{\text{BP}} - G_{\text{RP}})$ (mag)	ERT prob.
[4]	214110146+314107480	4	325.292262	31.685426	3602	27 502	0.67		1.00
[8]	053036992-373011003	3	82.654147	-37.503067	1036	27 502	2.99		0.98
[11]	153725327-301017053	3	234.355552	-30.171385	3286	45 837	0.22	0.63(2)	0.97
[12]	113100013-441959935	4	172.750041	-44.333297	1631	36 669	0.99	0.02(2)	0.96
[15]	081602164-530722970	4	124.009037	-53.123042	4823	27 502	0.87	0.34(3)	0.95
[16]	175443398+214054818	3	268.680823	21.681869	1755	18 335	0.45		0.95
[17]	065904044+162908685	3	104.766823	16.485772	5249	36 669	1.47	0.14(2)	0.94
[18]	182244519-541451730	4	275.685519	-54.247701	5256	27 502	1.22	0.11(4)	0.94
[19]	054934271+051814610	3	87.392794	5.304042	2298	45 837	0.43		0.93
[20]	075933618-173212537	3	119.890101	-17.536806	1860	55 004	1.23		0.93
[23]	181730853+272940139	3	274.378545	27.494468	1796	36 669	1.79		0.91
[25]	024848742+191330571	3	42.203097	19.225140	1677	13 751	0.30	0.06(2)	0.88
[26]	201454150-302452196	3	303.725615	-30.414491	2465	13 751	0.48	0.32(2)	0.88
[28]	201749047+620443509	3	304.454360	62.078774	916	36 669	0.99		0.74
[30]	011559515+562506671	3	18.997963	56.418524	2756	45 837	0.70		0.60

Notes. The finding charts depicting all of these candidates are given in Fig. 4. The numbers in parentheses in Col. $\Delta(G_{\text{BP}} - G_{\text{RP}})$ correspond to the number of images that were used in the computation of the maximum absolute difference in colour.

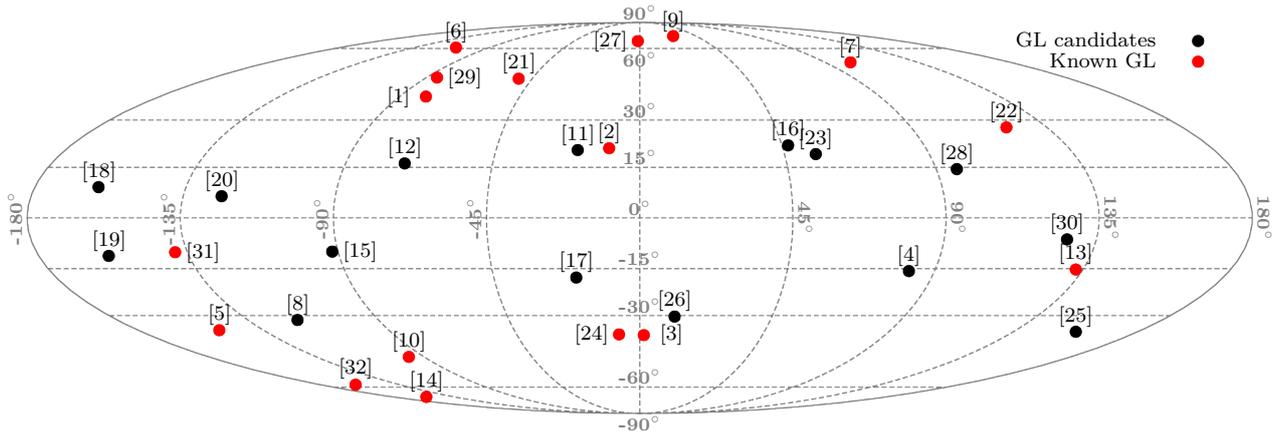


Fig. 5. Distribution of the known and new candidate GLs in Galactic coordinates. The numbers in square brackets refer to the candidate numbers from Table 3 and Fig. 4.

of candidate clusters. We know that lensed sources from GLs are always extragalactic objects, either active galactic nuclei (AGN) or galaxies. The latter, however, are extended objects of low surface brightness that will accordingly not be detected by *Gaia*. We thus performed a cross-match between our entire list of clusters, the compiled quasars list from Krone-Martins et al. (2018), and the C75 and R90 WISE AGN catalogue from Assef et al. (2018). The first of these lists consists of 3 112 975 candidate quasars compiled from the Million Quasars catalogue (Flesch 2015, 2017), from a photometric selection of WISE AGN (Secrest et al. 2015), from the third release of the Large Quasar Astrometric Catalogue (Souchay et al. 2015) and from the twelfth data release of the SDSS quasar catalogue (Pâris et al. 2017). The R90 and C75 catalogues consist of 4 543 530 and 20 907 127 WISE AGN candidates, respectively, selected across the whole extragalactic sky based solely on mid-infrared colours. The R90 catalogue has a reliability of 90%, while the C75 catalogue has a completeness of 75%.

This cross-match resulted in 6944 clusters composed of three or four images for which at least one of them has a counterpart in our compiled list of quasars. Figure 3 gives the distributions

of the ERT probabilities of these clusters. We note that these distributions are simply scaled versions of the distributions we obtained if no cross-match was performed, meaning that the vast majority of the clusters remain contaminants and not gravitational lens systems. Based on the same figure, we decided to set a threshold on the ERT probability of $P \geq 0.6$, which ensures that most of the known lenses will be detected, with the exception of four over a total of 61 known systems: 11 with four *Gaia* detections, 44 combinations of three images from these 11 systems, and 6 with three *Gaia* detections). A visual inspection of the 2572 resulting clusters composed of more than two images then yielded the GL candidates numbered [8], [11], [12], [16], [17], [19], [20], [23], [25], [26], [28], and [30] from Fig. 4 and Table 3. Despite the low cut we set on the ERT probability ($P \geq 0.6$), we note that out of the 12 candidates we propose, 10 have ERT probabilities higher than or equal to 0.88, assessing the interest of the ERT for identifying GL events, even in the case where only three images are detected.

Finally, we note that candidate number [12] was already present in Krone-Martins et al. (2018) and has since been spectroscopically confirmed as a GL (Wertz et al. 2018). Five

other candidates were also spectroscopically confirmed through Keck/LRIS observations after the submission of this paper (candidates numbered [11], [17], [23], [25], and [26], Krone-Martins et al., in prep.). Three of these new GLs (numbered [11], [23], and [26]) were also independently confirmed by Lemon et al. (2019). Candidate number [26], however, is a doubly-imaged quasar that should thus be considered a false positive from the ERT. On the other hand, the lensing nature of two candidates were denied (candidates numbered [16] and [30]) and led to inconclusive results regarding two others (candidates numbered [19] and [28]). The lensing nature of other candidates currently remains uncertain but plausible.

4. Conclusions

In this work, we aimed to discover quadruply-imaged lens candidates through the use of a supervised learning method, called extremely randomized trees (ERT), applied over the whole *Gaia* DR2. To train the ERT models, we simulated the relative positions and flux ratios of 106,623,188 quadruply-imaged systems based on a non-singular isothermal ellipsoid lens model in the presence of external shear. The performance of our ERT models were probed using simulations and real observations from *Gaia* DR2. From the known quadruply-imaged systems having all components detected in *Gaia* DR2, 12 out of 13 are successfully recovered by our method along with a misclassification rate of fortuitous clusters of stars as lenses that is below 1%. Similarly, 92.5% of the simulated lens systems are identified with the same misclassification rate.

The performance of our ERT models in identifying quadruply-imaged systems where only three components are detected in *Gaia* DR2 is evaluated by removing one image from each of the simulated and known quadruply-imaged systems. This resulted in the correct identification of 10 out of 13 known lensed systems with a misclassification rate below 7.5% when the two brightest images of the lens were observed together and ~20% otherwise. For the same identification rate, tests performed on simulations provided a similar misclassification rate of 7.74% for configurations where the two brightest images are present and ~10% otherwise.

We applied our ERT models to 70 697 clusters composed of four images and to 2 058 962 clusters composed of three images we extracted from the *Gaia* DR2. Beforehand, a filtering of the *Gaia* DR2 sources was used in order to remove non-stationary objects based on the parallax and proper motions of each source. Clusters were also restricted to have a maximum separation between images of 6'', a maximum absolute difference of G magnitude between components below 4 mag, and locations in regions of the sky where the mean field density is below 6×10^4 objects deg⁻².

Benefiting from the high identification rate of our ERT model in cases where all four components from quadruply-imaged systems are detected, and from the low associated misclassification rate of clusters of stars as gravitational lens we succeeded in isolating seven known gravitational lenses composed of four images based on simple cuts in the mean field density, in the maximum absolute difference in colour, and in the discriminant value provided by the ERT model. Three clusters are also retrieved through this straight selection and are hence promoted as plausible lens candidates.

In addition to this *Gaia*-only approach, we performed a cross-match between our list of clusters from *Gaia* DR2 sources, and compiled lists of spectroscopically confirmed quasars and photometric quasar candidates. We visually inspected the

resulting 2572 clusters for which the ERT models predicted a reasonably good agreement between these clusters and the relative positions and flux ratios from a non-singular isothermal ellipsoid lens model in the presence of an external shear.

The method presented here succeeded in finding 15 highly probable quadruply-imaged quasar candidates, five of which have recently been spectroscopically confirmed. The low number of lens candidates we identified from *Gaia* data, with respect to the Finet & Surdej (2016) predictions, can mostly be explained by the fact that the majority of gravitational lenses present in *Gaia* DR2 have less than three lensed images published in the catalogue, as shown by Ducourant et al. (2018). We expect that *Gaia* DR3 and later DR4 will improve on this, due to a less stringent filtering of the published sources and improved processing. Meanwhile, this method can be used on other catalogues, as it solely relies on astrometric and photometric data. Applications are already foreseen for the upcoming *Gaia* DR3 and combinations of already available catalogues (e.g. PanSTARRS, DES, SDSS, and *Gaia* DR2).

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Appendix A: Non-singular isothermal ellipsoid lens model in the presence of an external shear

The non-singular isothermal ellipsoid lens model in the presence of an external shear (NSIEg) is characterized by κ , the dimensionless surface mass density projected in the lens plane and defined by

$$\kappa(x, y) = \frac{b}{2} \left(s^2 + x^2 + \frac{y^2}{q^2} \right)^{-\frac{1}{2}}, \quad (\text{A.1})$$

where the coordinates (x, y) locate a position in the lens plane, s corresponds to the deflector core radius, q is the ratio of the minor to the major axes of the elliptical isodensity contours, and b is considered here as a normalizing factor. From Keeton & Kochanek (1998), the two components of the corresponding scaled deflection angle, α , are given by

$$\alpha_x(x, y) = \frac{bq}{e} \tan^{-1} \left(\frac{ex}{\psi + s} \right), \quad (\text{A.2})$$

and

$$\alpha_y(x, y) = \frac{bq}{e} \tanh^{-1} \left(\frac{ey}{\psi + q^2s} \right), \quad (\text{A.3})$$

where $e = \sqrt{1 - q^2}$ is defined as the eccentricity of the isodensity contours, and $\psi^2 = q^2(s^2 + x^2) + y^2$. The contribution of more distant massive objects to the deflection is taken into account through an external shear term of the form

$$\alpha_\gamma(x, y) = \gamma \begin{pmatrix} \cos 2\omega & \sin 2\omega \\ \sin 2\omega & -\cos 2\omega \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}, \quad (\text{A.4})$$

where γ is the shear intensity and ω its orientation. Finally, the position $\theta_s = (x_s, y_s)$ of a point-like source is related to a lensed image position $\theta = (x, y)$ through the so-called lens equation

$$\theta_s = \theta - \alpha - \alpha_\gamma, \quad (\text{A.5})$$

and the associated magnification factor $\mu(\theta)$ is then defined by

$$\mu(\theta) = |\det \mathbf{A}(\theta)|^{-1}, \quad (\text{A.6})$$

where the Jacobian matrix $\mathbf{A}(\theta) = \partial\theta_s(\theta)/\partial\theta$ is called the amplification matrix.

Appendix B: *Gaia* GraL catalogue of clusters from *Gaia* DR2 sources

The *Gaia* GraL catalogue of clusters from *Gaia* DR2 sources is available at the CDS. The catalogue is composed of all 2 129 659 clusters identified in Sect. 2 along with the ERT probabilities computed for each of them (see Sect. 3). For ease of identifying the images constituting each cluster and to facilitate the cross-match against other catalogues based on the individual components of the clusters, each entry from the catalogue corresponds to a single *Gaia* DR2 source within the cluster. Consequently, clusters composed of three and four images have, respectively, three and four associated entries in the catalogue along with the fields that are common to the cluster they belong to. The fields constituting each row of the catalogue are detailed in Table B.1.

Our objective here is not to provide a list of GL candidates, as we do in Sects. 3.4.1 and 3.4.2, but to provide the user with a catalogue that can easily provide hints on the lensing nature of some of the observational targets, at least regarding GLs that are reproducible through a NSIEg lens model. This approach also justifies the inclusion of clusters located in regions of the sky we know to be densely populated and where the contamination rate of GL candidates will typically be very high. The removal of the clusters having a field density higher than $\rho > 3 \times 10^4$ objects deg^{-2} effectively reduces their number by a factor of ten (205 004 remaining clusters).

To our knowledge, the present catalogue is the first to provide a discriminating value associated with each cluster that reflects the ability for a given GL model to reproduce the observed configuration of images. These ERT probabilities can provide a straight binary classification as, for example, 96.31% of the four-image configurations have $P < 0.5$, whereas 86.11% of the three-image configurations have $P < 0.9$. The threshold we set on P are obviously application-dependent and should be set in agreement with the ROC curves we described in Sect. 3. Finally, in a conservative approach, we do not set any cut on the difference in colour between images of the clusters, $\Delta(G_{\text{BP}} - G_{\text{RP}})$. However, whenever they are available they provide an important criterion for identifying GLs as we do not expect the colours to vary much between the images of GLs (see Sect. 3.4 for examples).

Table B.1. Description of the fields contained in the *Gaia* GraL catalogue of clusters from *Gaia* DR2 sources.

Num.	Field name	Unit	Description
1.	row		Unique identifier of the row in the catalogue. Each combination of the name and the SourceId is always associated with a unique row.
2.	name		Unique identifier of the cluster. This identifier is based on the mean position of the images of the cluster taken in sexagesimal coordinates.
3.	nimg		The number of images constituting the cluster ($nimg \in \{3, 4\}$).
4.	size	($''$)	The maximum angular separation between any two images of the cluster ($size \leq 6''$).
5.	known		Identifier in the list of known and candidate lenses from Ducourant et al. (2018) . Empty if this cluster is not recognized as a known or candidate lens.
6.	density	(obj. deg $^{-2}$)	The mean density of objects surrounding the cluster, estimated by counting the <i>Gaia</i> DR2 objects falling in a $30''$ radius around one of its constituent members ($density \leq 6 \times 10^4$ objects deg $^{-2}$).
7.	dmag	(mag)	The maximum absolute difference in the <i>G</i> magnitude, ΔG , between the images of the cluster ($dmag \leq 4$ mag).
8.	dcolor	(mag)	The maximum absolute difference in colour, $\Delta(G_{BP} - G_{RP})$, between the images of the cluster. Empty if fewer than two images have colour information (i.e. BPmag or RPmag is empty).
9.	ncolor		The number of images having colour information that are used in the computation of dcolor.
10.	P		ERT probability associated with this cluster (see Sect. 3). If $nimg = 4$, then this parameter corresponds to the ERT probabilities computed based on the ABCD model. If $nimg = 3$, then this field is taken as the maximum of PABC, PABD, PACD, and PBCD.
11.	PABC		ERT probability computed based on the ABC model. Empty if $nimg = 4$.
12.	PABD		ERT probability computed based on the ABD model. Empty if $nimg = 4$.
13.	PACD		ERT probability computed based on the ACD model. Empty if $nimg = 4$.
14.	PBCD		ERT probability computed based on the BCD model. Empty if $nimg = 4$.
15.	SourceId		Unique source identifier from <i>Gaia</i> DR2.
16.	RA	($^{\circ}$)	Right ascension of the source in ICRS coordinates from <i>Gaia</i> DR2.
17.	Dec	($^{\circ}$)	Declination of the source in ICRS coordinates from <i>Gaia</i> DR2.
18.	Gmag	(mag)	<i>G</i> -band mean magnitude from <i>Gaia</i> DR2.
19.	BPmag	(mag)	Integrated BP mean magnitude from <i>Gaia</i> DR2. Empty if no BP magnitude is available.
20.	RPmag	(mag)	Integrated RP mean magnitude from <i>Gaia</i> DR2. Empty if no RP magnitude is available.