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Extension of a Wide-Range Three-Step Hydrogen Mechanism to Syngas

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Previously [1] we have shown how a single species X can be introduced, representing either HO₂ for high-temperature ignition or H₂O₂ for low-temperature ignition, to develop an algorithm that covers the entire range of ignition, flame-propagation, and combustion conditions, without a significant degradation of accuracy, for hydrogen-air systems. By adding relevant CO chemistry to the hydrogen chemistry, this same approach can be applied to derive a comparably useful four-step reduced-chemistry description for syngas blends that have small enough concentrations of methane, other hydrocarbons, or other reactive species to be dominated by the elementary steps of the H₂/CO system. The present communication reports the resulting extended algorithm.

This work begins with the elementary steps of the detailed chemistry as listed in Table 1. We shall employ the numbering of the steps as given in the table, which identifies the 8 steps that are considered to be reversible and gives fitted parameters for the reverses of those steps. There are 18 entries in

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	Reaction		A^a	n	E^a		A^a	n	E^a
1	$\text{H} + \text{O}_2 \rightleftharpoons \text{OH} + \text{O}$	k_f	$3.52 \cdot 10^{16}$	-0.7	71.42	k_b	$7.04 \cdot 10^{13}$	-0.26	0.60
2	$\text{H}_2 + \text{O} \rightleftharpoons \text{OH} + \text{H}$	k_f	$5.06 \cdot 10^4$	2.67	26.32	k_b	$3.03 \cdot 10^4$	2.63	20.23
3	$\text{H}_2 + \text{OH} \rightleftharpoons \text{H}_2\text{O} + \text{H}$	k_f	$1.17 \cdot 10^9$	1.3	15.21	k_b	$1.28 \cdot 10^{10}$	1.19	78.25
4	$\text{H} + \text{O}_2 + \text{M} \rightarrow \text{HO}_2 + \text{M}^b$	k_0	$5.75 \cdot 10^{19}$	-1.4	0.0	k_∞	$4.65 \cdot 10^{12}$	0.44	0.0
5	$\text{HO}_2 + \text{H} \rightarrow 2\text{OH}$		$7.08 \cdot 10^{13}$	0.0	1.23				
6	$\text{HO}_2 + \text{H} \rightleftharpoons \text{H}_2 + \text{O}_2$	k_f	$1.66 \cdot 10^{13}$	0.0	3.44	k_b	$2.69 \cdot 10^{12}$	0.36	231.86
7	$\text{HO}_2 + \text{OH} \rightarrow \text{H}_2\text{O} + \text{O}_2$		$2.89 \cdot 10^{13}$	0.0	-2.08				
8	$\text{H} + \text{OH} + \text{M} \rightleftharpoons \text{H}_2\text{O} + \text{M}^c$	k_f	$4.00 \cdot 10^{22}$	-2.0	0.0	k_b	$1.03 \cdot 10^{23}$	-1.75	496.14
9	$2\text{H} + \text{M} \rightleftharpoons \text{H}_2 + \text{M}^d$	k_f	$1.30 \cdot 10^{18}$	-1.0	0.0	k_b	$3.04 \cdot 10^{17}$	-0.65	433.09
10	$2\text{HO}_2 \rightarrow \text{H}_2\text{O}_2 + \text{O}_2$		$1.03 \cdot 10^{14}$	0.0	46.2	+	$1.94 \cdot 10^{11}$	0.0	-5.9
11	$\text{HO}_2 + \text{H}_2 \rightarrow \text{H}_2\text{O}_2 + \text{H}$		$7.80 \cdot 10^{10}$	0.61	100.14				
12	$\text{H}_2\text{O}_2 + \text{M} \rightarrow 2\text{OH} + \text{M}^e$	k_0	$8.15 \cdot 10^{23}$	-1.9	207.62	k_∞	$2.63 \cdot 10^{19}$	-1.27	214.74
13	$\text{CO} + \text{OH} \rightleftharpoons \text{CO}_2 + \text{H}$	k_f	$4.4 \cdot 10^6$	1.5	-3.1	k_b	$2.41 \cdot 10^{13}$	0.22	104.60
14	$\text{CO} + \text{HO}_2 \rightarrow \text{CO}_2 + \text{OH}$		$6.03 \cdot 10^{13}$	0.0	96.0				
15	$\text{HCO} + \text{M} \rightleftharpoons \text{CO} + \text{H} + \text{M}^f$	k_f	$1.86 \cdot 10^{17}$	-1	71.13	k_b	$3.51 \cdot 10^{16}$	-0.77	5.35
16	$\text{HCO} + \text{H} \rightarrow \text{CO} + \text{H}_2$		$5.0 \cdot 10^{13}$	0.0	0.0				
17	$\text{CO} + \text{O}_2 \rightarrow \text{CO}_2 + \text{O}$		$1.0 \cdot 10^{12}$	0.0	199.6				
18	$\text{CO} + \text{O} + \text{M} \rightleftharpoons \text{CO}_2 + \text{M}^g$	k_0	$1.55 \cdot 10^{24}$	-2.8	17.6	k_∞	$1.80 \cdot 10^{11}$	0.0	23.8

Table 1: Rate coefficients in Arrhenius form $k = AT^n \exp(-E/R^oT)$ for the skeletal mechanism.

^aUnits are mol, s, cm³, kJ, and K.

^bChaperon efficiencies are 2.5 for H₂, 16.0 for H₂O, 1.2 for CO, 2.4 for CO₂, 0.7 for Ar and He and 1.0 for all other species; Troe falloff with $F_c = 0.5$

^cChaperon efficiencies are 2.5 for H₂, 12.0 for H₂O, 1.9 for CO, 3.8 for CO₂, 0.5 for Ar and He and 1.0 for all other species.

^dChaperon efficiencies are 2.5 for H₂, 12.0 for H₂O, 1.9 for CO, 3.8 for CO₂, 0.38 for Ar and He and 1.0 for all other species.

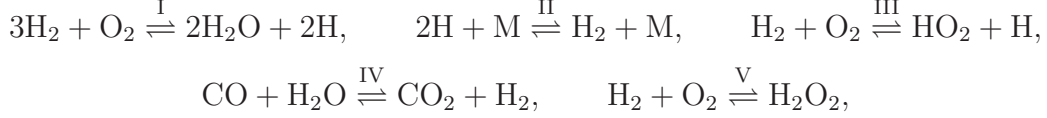
^eChaperon efficiencies are 2.0 for H₂, 6.0 for H₂O, 1.5 for CO, 2.0 for CO₂, 0.4 for Ar and He and 1.0 for all other species; $F_c = 0.265 \exp(-T/94\text{K}) + 0.735 \exp(-T/1756\text{K}) + \exp(-5182\text{K}/T)$

^fChaperon efficiencies are 1.9 for H₂, 12.0 for H₂O, 2.5 for CO, 2.5 for CO₂ and 1.0 for all other species.

^gChaperon efficiencies are 2.5 for H₂, 12.0 for H₂O, 2.0 for CO, 4.0 for CO₂, 0.7 for Ar and He and 1.0 for all other species.

this table, two more than in our previous work [2] on reduced chemistry for syngas, because we have found, since that earlier study, that at low H_2 levels entry 17 is important as an additional initiation step, and radical removal by entry 18 appreciably affects predicted laminar burning velocities at higher pressures. The listed rate parameters are up-dated values from previous work [3], now available on the same web site, employing more recent evaluations of elementary rate coefficients for hydrogen [4]. In particular, for step 10 we now realize that, to account properly for the two paths, a bi-Arrhenius expression is needed, employing the sum of two Arrhenius terms with the different sets of rate parameters listed.

Steady-state approximations are first introduced for O, OH, and HCO, resulting in a 5-step mechanism that can be written as:



with associated rates:

$$\begin{aligned} \omega_I &= \omega_1 + \omega_{5f} + \omega_{12f} + \omega_{14f} + \omega_{17f}, & \omega_{II} &= \omega_{4f} + \omega_8 + \omega_9 + \omega_{12f} - \omega_{15} + \omega_{18f}, \\ \omega_{III} &= \omega_{4f} - \omega_{5f} - \omega_6 - \omega_{7f} - 2\omega_{10f} - \omega_{11f} - \omega_{14f}, \\ \omega_{IV} &= \omega_{13} + \omega_{14f} + \omega_{17f} + \omega_{18f}, & \omega_V &= \omega_{10f} + \omega_{11f} - \omega_{12f}, \end{aligned} \quad (1)$$

where the ω_i refer to the rates of the i^{th} elementary step listed in Table 1. The concentrations of the steady-state species, needed for evaluating these rates, are given as supplementary material for OH (7), O (8) and HCO (9).

As explained previously [1, 2, 5, 6], the steady states for O and OH, which hold with reasonable accuracy in flames, do not apply during autoignition

and lead to significant underpredictions of induction times, with increasing errors for decreasing equivalence ratios. A correction to the branching rate therefore must be made and can be obtained by introducing the modified rates $\omega_I^*/\omega_I = \omega_{II}^*/\omega_{II} = \omega_{III}^*/\omega_{III} = \omega_{IV}^*/\omega_{IV} = \Lambda$, where the factor

$$\Lambda = [(1 + 2B)^{1/2} - 1]/B \quad (2)$$

depends on the forward rates of the shuffle reactions 1-3 and the CO-consumption reaction 13 through

$$B = \frac{4k_{1f}C_{O_2}(k_{1f}C_{O_2} + k_{2f}C_{H_2} + k_{3f}C_{H_2} + k_{13f}C_{CO})}{k_{2f}C_{H_2}(k_{3f}C_{H_2} + k_{13f}C_{CO})}, \quad (3)$$

the term in B arising from step 13, not needed for H_2 and not employed previously [2] for syngas, but having been found in the present study to improve predictions and to be preferable to an ad hoc revision introduced previously [7]. The modifications are switched off by setting $\Lambda = 1$ where the steady states for O and OH apply, that is, in hot regions with relatively high radical concentrations, where the HO_2 steady state also holds. For this reason, the need for the correction factor is linked to the failure of the HO_2 steady state; the rate of HO_2 production $\dot{C}_{HO_2P} = \omega_{4f} + \omega_{6b}$ and that of HO_2 consumption $\dot{C}_{HO_2C} = \omega_{5f} + \omega_{6f} + \omega_{7f} + 2\omega_{10f} + \omega_{11f} + \omega_{14f}$ are to be evaluated locally and checked to see if their fractional difference is sufficiently small (for example, less than 0.05), in which case the modifications are discontinued.

The first of the two adjacent 4-step mechanisms is obtained by assuming H_2O_2 to be steady state, an approximation applicable in the high-temperature regime, and the second is derived by assuming HO_2 to be in steady state, applicable in the low-temperature regime.

At high temperatures, the mechanism consists of steps I, II, III, and IV, with associated rates:

$$\begin{aligned}
\omega_I^+ &= \omega_1 + \omega_{5f} + \omega_{10f} + \omega_{11f} + \omega_{14f} + \omega_{17f}, \\
\omega_{II}^+ &= \omega_{4f} + \omega_8 + \omega_9 - \omega_{10f} - \omega_{11f} - \omega_{15}, \\
\omega_{III}^+ &= \omega_{4f} - \omega_{5f} - \omega_6 - \omega_{7f} - 2\omega_{10f} - \omega_{11f} - \omega_{14f}, \\
\omega_{IV}^+ &= \omega_{13} + \omega_{14f} + \omega_{17f},
\end{aligned} \tag{4}$$

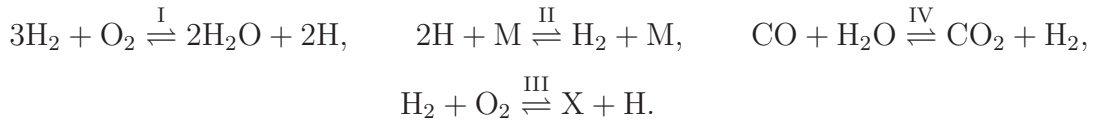
the expressions needed for steady-state concentrations being (7), (8), and (9), along with (11), all being provided as supplementary material.

The reduced mechanism applicable at low temperatures consists of steps I, II, IV, and V (step III disappearing with the HO_2 steady-state assumption), and the rate of step II must be modified from (1) to read

$$\omega_{II} = \omega_{4f} + \omega_8 + \omega_9 - \omega_{10f} - \omega_{11f} - \omega_{15} + \omega_{18f}.$$

The expressions for C_O , C_{OH} , and C_{HCO} steady states are the same as those for the 5-step description (7), (8), and (9). The HO_2 concentration, now needed in evaluating the global rates, is given by (10), the steady-state formula (11) for H_2O_2 having been discarded.

Despite not consisting of the same global steps, the two adjacent 4-step reduced mechanisms, can be written as a single universal reduced mechanism



Because the mass and diffusive properties of HO_2 and H_2O_2 are similar, X can represent either HO_2 , when the ω^+ of (4) are used as global rates, or

H₂O₂, in the low-temperature regime, when the rates ω^- , given below, are used. As discussed in [1], the global rates for the 4-step reduced mechanism at low temperatures cannot be used directly for the universal reduced mechanism because that would lead to an overproduction of H atoms – a byproduct of step III, not of V. This is avoided by turning the H overproduction into an overproduction of H₂, which we found negligible in all cases tested. The resulting applicable low-temperature rates for the universal reduced mechanism then become

$$\begin{aligned}\omega_I^- &= \omega_1 + \omega_{5f} + \omega_{12f} + \omega_{14f} + \omega_{17f}, \\ \omega_{II}^- &= \omega_{4f} + \omega_8 + \omega_9 - (\omega_{10f} + \omega_{11f} + \omega_{12f})/2 - \omega_{15} + \omega_{18f}, \\ \omega_{III}^- &= \omega_{10f} + \omega_{11f} - \omega_{12f}, \quad \omega_{IV}^- = \omega_{13} + \omega_{14f} + \omega_{17f} + \omega_{18f},\end{aligned}\quad (5)$$

to be evaluated with C_O , C_{OH} , C_{HCO} , and C_{HO_2} steady-state expressions (7), (8), (9), and (10). Following the strategy presented in [1], when the two mechanisms are merged into one,

$$\begin{cases} \omega = \omega^- & \text{if } (\omega_P - \omega_C)/\omega_P < \varepsilon, \\ \omega = \omega^+ & \text{if } (\omega_P - \omega_C)/\omega_P > \varepsilon, \end{cases}\quad (6)$$

with

$$\omega_P = 2\omega_{1f} + \omega_{6b} + \omega_{11f} + 2\omega_{12f} + 2\omega_{14f} + \omega_{17f}, \quad \omega_C = \omega_{4f} + 2\omega_{15b} + \omega_{18f},$$

which are approximations for the H-atom production and consumption rates, to be evaluated using the steady-state expression (10) for C_{HO_2} as an approximation. The value of ε must be sufficiently small (in our implementation, $\varepsilon = 0.05$).

This completes the specification of the algorithm that, for syngas, comprises a 4-step description that will produce results as accurate of those of the original 5-step reduced mechanism. The 4-step reduced description has the same applicability as our initial reduced mechanism [2] (ie. premixed and non-premixed combustion, as well as detonations and autoignition above the second explosion limit), now extended to include autoignition below the second limit as well. Computations from our initial contribution [2] were repeated as validation tests and are included as supplementary material.

Acknowledgements

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Source files

The source files for the mechanism are available at www.pierreboivin.info, in the “Reduced Kinetics” Section. A tutorial to implement reduced kinetics in Cantera [13] is also provided there.

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Supplementary material

Steady state formulas

The steady state formulas needed for the reduced descriptions read

$$C_{\text{OH}} = [(A_1^2 + 4A_0A_2)^{1/2} - A_1]/(2A_2), \quad (7)$$

$$C_{\text{O}} = \frac{k_{1f}C_{\text{H}}C_{\text{O}_2} + k_{2b}C_{\text{OH}}C_{\text{H}} + k_{17f}C_{\text{CO}}C_{\text{O}_2}}{k_{1b}C_{\text{OH}} + k_{2f}C_{\text{H}_2}}, \quad (8)$$

$$C_{\text{HCO}} = \frac{k_{15b}C_{\text{CO}}C_{\text{H}}C_{\text{M}}}{k_{15f}C_{\text{M}} + k_{16f}C_{\text{H}}}, \quad (9)$$

where the expressions

$$\begin{aligned} A_0 &= (k_{2f}C_{\text{H}_2} + k_{18f}C_{\text{CO}}C_{\text{M}})(2k_{1f}C_{\text{H}}C_{\text{O}_2} + k_{3b}C_{\text{H}}C_{\text{H}_2\text{O}} + 2k_{5f}C_{\text{H}}C_{\text{HO}_2} + k_{8b}C_{\text{M}}C_{\text{H}_2\text{O}} \\ &\quad + 2k_{12f}C_{\text{H}_2\text{O}_2}C_{\text{M}} + k_{13b}C_{\text{CO}_2}C_{\text{H}} + k_{14f}C_{\text{CO}}C_{\text{HO}_2}) + C_{\text{CO}}C_{\text{O}_2}(k_{2f}k_{17f}C_{\text{H}_2} - k_{1f}k_{18f}C_{\text{H}}), \\ A_1 &= (k_{2f}C_{\text{H}_2} + k_{18f}C_{\text{CO}}C_{\text{M}})(k_{3f}C_{\text{H}_2} + k_{7f}C_{\text{HO}_2} + k_{8f}C_{\text{M}}C_{\text{H}} + k_{13f}C_{\text{CO}}) \\ &\quad - k_{1b}(k_{3b}C_{\text{H}}C_{\text{H}_2\text{O}} + 2k_{5f}C_{\text{H}}C_{\text{HO}_2} + k_{8b}C_{\text{M}}C_{\text{H}_2\text{O}} + 2k_{12f}C_{\text{H}_2\text{O}_2}C_{\text{M}} \\ &\quad + k_{13b}C_{\text{CO}_2}C_{\text{H}} + k_{14f}C_{\text{CO}}C_{\text{HO}_2} + k_{17f}C_{\text{CO}}C_{\text{O}_2}) + k_{2b}k_{18f}C_{\text{H}}C_{\text{CO}}C_{\text{M}}, \\ A_2 &= k_{1b}(k_{3f}C_{\text{H}_2} + k_{7f}C_{\text{HO}_2} + (2k_{2b} + k_{8f}C_{\text{M}})C_{\text{H}} + k_{13f}C_{\text{CO}}). \end{aligned}$$

are to be used to evaluate the OH concentration from (7) prior to calculating the O concentration from (8).

$$C_{\text{HO}_2} = (B_2^2 + B_1)^{1/2} - B_2, \quad (10)$$

$$B_1 = (k_{6b}C_{\text{H}_2}C_{\text{O}_2} + k_{4f}C_{\text{H}}C_{\text{O}_2}C_{\text{M}_4})/(2k_{10f}),$$

$$B_2 = (k_{5f}C_{\text{H}} + k_{6f}C_{\text{H}} + k_{7f}C_{\text{OH}} + k_{11f}C_{\text{H}_2} + k_{14f}C_{\text{CO}})/(4k_{10f}),$$

$$C_{\text{H}_2\text{O}_2} = \frac{k_{10f}C_{\text{HO}_2}^2 + k_{11f}C_{\text{HO}_2}C_{\text{H}_2}}{k_{12f}C_{\text{M}}} \quad (11)$$

Validation

The applicability of the 4-step reduced mechanism is similar to that of our initial contribution [2], with additional inclusion of high-pressure (or low-temperature) autoignition thanks to the hybrid species description. Figures 1 and 2 repeat some validation computations from [2], showing a similar agreement. Flame velocities as obtained between the reduced and detailed description are within 20% at atmospheric pressures, and 15% at higher pressures, of interest for instance in gas-turbine combustion. Agreement between detailed and 4-step descriptions for ignition times is excellent for all conditions of practical interest.

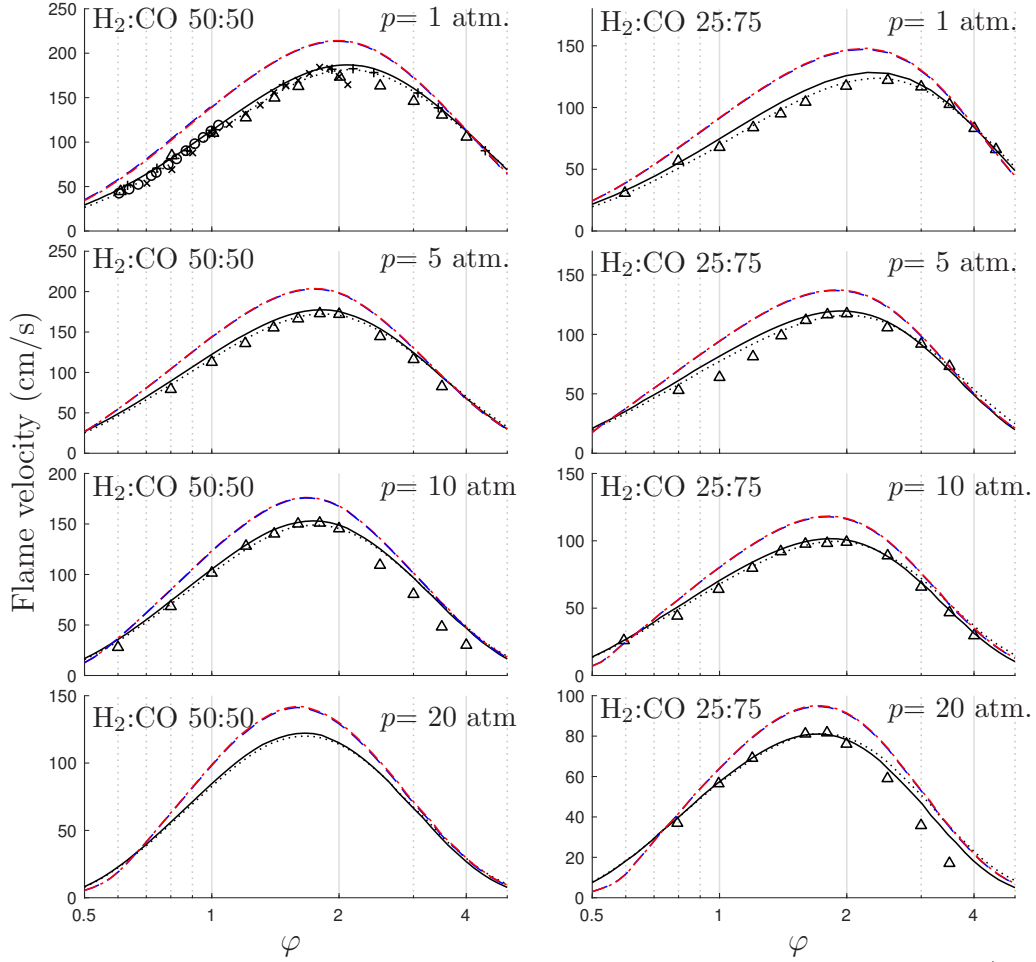


Figure 1: The variation with equivalence ratio of the laminar flame velocity for a CO/H₂-oxidizer mixture at initial temperature $T_u = 300$ K and for four different pressures and two different CO/H₂ ratios as obtained from numerical integrations with the latest detailed San Diego mechanism [8] (solid curves), 5-step (dashed curves), and 4-step (dot-dashed curves) chemistry descriptions and from laboratory measurements (triangles \triangle : [9]; crosses $+$: [10]; times \times : [11]); the oxidizer for $p = 1$ atm is air, while for $p = (5, 10, 20)$ atm it is an oxygen-helium mixture with mole-fraction ratio $X_{\text{He}}/X_{\text{O}_2} = 7$. [9]. Dotted curves correspond to the detailed San Diego mechanism [8] in its 2009-11-01 version (latest version at time of [2]). Note that the 5 and 4-step reduced chemistry descriptions lead to indistinguishable results. Flame velocities as obtained with the reduced and detailed description are within 20% at atmospheric pressures, and 15% at higher pressures.

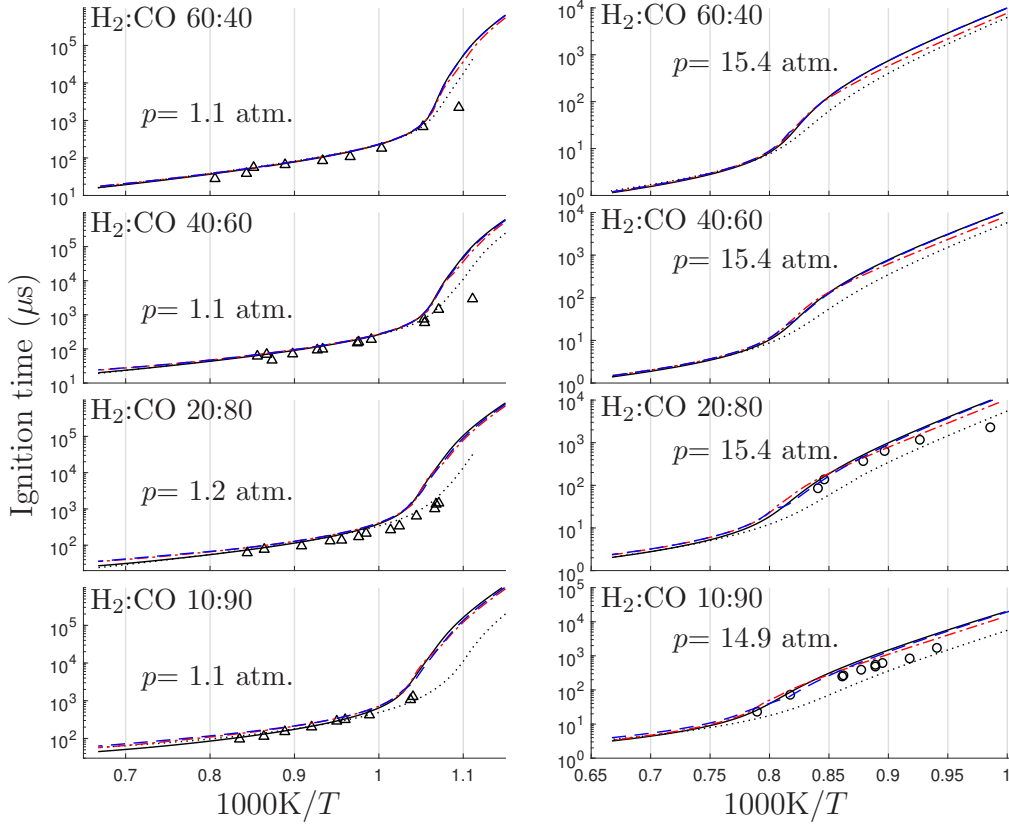


Figure 2: The variation with initial temperature of the induction time for a CO/H₂-air mixture with $\phi = 0.5$ as obtained from numerical integrations with the latest detailed San Diego mechanism [8] (solid curves), skeletal mechanism from Tab. 1 (dashed curves), and 4-step reduced (dot-dashed curves) chemistry descriptions and from laboratory measurements (symbols: [12]). Dotted curves correspond to the detailed San Diego mechanism [8] in its 2009-11-01 version (latest version at time of [2]).