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Performance of Range-Only TMA

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Abstract—Range-only target motion analysis (ROTMA) is the topic of this paper: we focus our study on the numerical aspect and performance of the maximum likelihood estimates (MLE) for some scenarios when the noise polluting the measurements is additive and Gaussian. The performance is compared to the Cramér–Rao lower bound (CRLB).

I. INTRODUCTION

Range-only target motion analysis (ROTMA) has been treated in the literature for various applications, the target having a constant velocity (CV) motion: for example in [1], [2] and [3], maritime surveillance radar systems, ISAR (inverse synthetic aperture radar), are studied. It offers also an efficient way to calibrate a sonar array [4]. ROTMA is encountered in the robotic domain by radio-frequency [5] [6]. Local observability was analysed by the rank of the Fisher information matrix (FIM) [7]. Global observability conditions were proposed recently in [8] and [9]. In the same vein, we present here some aspects of estimation (which was not addressed in [8] and [9]), in particular for scenarios where observability is not acquired and for which the FIM is fullranked, or conversely for scenarios where the trajectory of the target is observable, but the FIM is singular. This motivates the structure of our paper.

In section II, we present the assumptions and notations. Section III is devoted to the special case where the observer is in CV motion too. In section IV, the observer's trajectory is composed of two legs. Here, the target's trajectory can be observable or not [8]. Section V presents a case where the order of the observer's kinematic model is greater than that of the target, and still the trajectory of the target is unobservable [9]. We end with a more favourable case: the observer's trajectory contains an arc of a circle and this suffices to guarantee observability [9]. The conclusion follows.

II. HYPOTHESES, DEFINITIONS AND NOTATIONS

A. Model of Target's and Observer's Kinematics

A target (T) and an observer (O) move in the same plane, given a Cartesian system. The target has a CV motion all along the scenario, while the observer maneuvers (the term "maneuver" is employed when the observer is not in CV motion).

For the observer, the position and velocity at time t are respectively $P_o(t)$ and $V_o(t) = \frac{dP_o(t)}{dt}$. Both are concatenated

into the vector $X_O(t) = \begin{bmatrix} P_O^{\mathsf{T}}(t) & V_O^{\mathsf{T}}(t) \end{bmatrix}^{\mathsf{T}}$. For the target, the notations are similar: $P_T(t)$, $V_T = \frac{dP_T(t)}{dt}$, and $X_T(t) = \begin{bmatrix} P_T^{\mathsf{T}}(t) & V_T^{\mathsf{T}} \end{bmatrix}^{\mathsf{T}}$. Obviously, $P_T(t) = P_T(0) + tV_T$. Note that whatever t, $X_T(t)$ entirely defines the target's trajectory. For a chosen t^* , the state vector $X_T(t^*)$ will be simply denoted $X = \begin{bmatrix} x & y & \dot{x} & \dot{y} \end{bmatrix}^{\mathsf{T}}$. The motion of the target relative to the observer is given by $P_{OT}(t) = P_T(t) - P_O(t)$ and by $V_{OT}(t) = \frac{dP_{OT}(t)}{dt}$. We define the vector $X_{OT}(t) = X_T(t) - X_O(t)$. All the angles are clockwise-positive: the angle (North, W) is denoted $\angle W$. The range and the bearing at time t are given respectively by $r(t) = \|P_{OT}(t)\|$ and $\theta(t) = \angle P_{OT}(t)$.

B. Measurements Model and Estimate

For the sake of simplicity, the notations r_k and θ_k will stand for $r(t_k)$ and $\theta(t_k)$, respectively. In order to emphasize the functional link of r_k with the state vector X, we use the notation $r_{i}(X)$. The range measurement collected at $t_k = (k-1)\Delta t$ and denoted $r_{m,k}$ obeys the equation $r_{m,k} = r_k(X) + \varepsilon_k$ (1), where ε_k is the measurement noise assumed to be Gaussian, temporally white and zero mean; its standard deviation is $\sigma_{r,k}$. The set of N available range measurements is $r_m = \{r_{m,1}, r_{m,2}, \dots, r_{m,N}\}$. The aim of the RO-TMA is to estimate the state vector X given the measurements r_m . Note that in all the scenarios, the observer starts from $P_{O}(0) = \begin{bmatrix} 0 & 0 \end{bmatrix}^{\mathsf{T}}$. The chosen estimate is the MLE (or equivalently the LSE since the noise is additive and Gaussian). Its empirical covariance matrix will be compared to the Cramér-Rao lower bound (CRLB), which is the inverse of the FIM for unbiased estimators.

III. THE OBSERVER'S TRAJECTORY CONSISTS OF ONE LEG ONLY

In [8], we showed that when the observer is in CV motion, the trajectory of the target is observable up to an isometry (rotation or axial symmetry). We characterized the set of targets (true target and ghost-targets) \mathfrak{O} in the same range as the target of interest:

$$\mathfrak{O} = \left\{ \begin{bmatrix} \mathbf{I}_2 \otimes \mathbf{H} \end{bmatrix} \begin{bmatrix} P_{OT}(0) \\ V_{OT} \end{bmatrix} + \begin{bmatrix} P_O(0) \\ V_O \end{bmatrix}, \mathbf{H} \text{ being an orthogonal matrix} \right\}.$$

 \mathfrak{O} can be defined by a 3-dimensional state vector

 $Z = \left[\left\| P_{OT}(t^*) \right\|^2 \quad 2V_{OT}^T P_{OT}(t^*) \quad \left\| V_{OT} \right\|^2 \right]^{\mathsf{T}}.$ Indeed, for any t^* , we

have $r_k^2 = \mathbf{A}_k Z$, with $\mathbf{A}_k = \begin{bmatrix} 1 & t_k - t^* & (t_k - t^*)^2 \end{bmatrix}$. Therefore, the range $r_k(X)$ is reparametrized into $r_k(Z)$. This property allows us to define a linear estimate.

A. Linear Estimate

Let us consider the measurement equation (1) and express the squares of its two elements: $r_{m,k}^2 = r_k^2 + 2r_k \varepsilon_{r,k} + \varepsilon_{r,k}^2$. The noise intervening in this new equation is then $2r_k \varepsilon_{r,k} + \varepsilon_{r,k}^2$ whose first two moments are $E(2r_k \varepsilon_{r,k} + \varepsilon_{r,k}^2) = \sigma_r^2$ and $Var(2r_k \varepsilon_{r,k} + \varepsilon_{r,k}^2) = 2\sigma_r^2(2r_k^2 + \sigma_r^2)$ (since ε_{rk} is Gaussian). We introduce then another "measurement": $\rho_{m,k} \Delta r_{m,k}^2 - \sigma_r^2$.We define also the "noise": $\eta_k \triangleq 2r_k \varepsilon_{r,k} + \varepsilon_{r,k}^2 - \sigma_r^2$ whose first two moments are now $E(\eta_k) = 0$ and $Var(\eta_k) = 2\sigma_r^2 (2r_k^2 + \sigma_r^2) = \sigma_{\sigma_k}^2$. So, we end up of measurement with set the equations $\rho_{m,k} = r_k^2 + \eta_k = \mathbf{A_k} Z + \eta_k$ for $k = 1, \dots, N$. Note that η_k is zero-mean but no longer Gaussian. Still, it is legitimate to compute the weighted linear least squares estimator of Z that minimizes the criterion $C(Z) = \sum_{k=1}^{N} \frac{1}{\sigma_{p,k}^2} (\rho_{m,k} - \mathbf{A}_k Z)^2$: $\hat{Z}_{WLS} = \left[\sum_{k=1}^{N} \frac{1}{\sigma_{\rho,k}^{2}} \mathbf{A}_{k}^{\mathsf{T}} \mathbf{A}_{k}\right] \left[\sum_{k=1}^{N} \frac{1}{\sigma_{\rho,k}^{2}} \mathbf{A}_{k}^{\mathsf{T}} \rho_{m,k}\right]$

which is unbiased. Its covariance matrix

$$Cov\left(\hat{Z}_{WLS}\right) = \left[\sum_{k=1}^{N} \frac{1}{\sigma_{\rho,k}^{2}} \mathbf{A}_{k}^{\mathrm{T}} \mathbf{A}_{k}\right]^{-1} = 4\sigma_{r}^{2} \left[\sum_{k=1}^{N} \frac{1}{r_{k}^{2}} \frac{1}{1 + \frac{\sigma_{r}^{2}}{2r_{k}^{2}}} \mathbf{A}_{k}^{\mathrm{T}} \mathbf{A}_{k}\right]^{-1}$$

The computation of \hat{Z}_{WLS} assumes the knowledge of r_k^2 . To alleviate this, in practice, we replace r_k^2 by $r_{m,k}^2$:

$$\hat{Z}_{WLS} \cong \left[\sum_{k=1}^{N} \frac{1}{\sigma_{\rho,m,k}^{2}} \mathbf{A}_{\mathbf{k}}^{\mathrm{T}} \mathbf{A}_{\mathbf{k}}\right]^{-1} \left[\sum_{k=1}^{N} \frac{1}{\sigma_{\rho,m,k}^{2}} \mathbf{A}_{\mathbf{k}}^{\mathrm{T}} \boldsymbol{\rho}_{m,k}\right], \text{ with}$$
$$\sigma_{\rho,m,k}^{2} = 2\sigma_{r}^{2} \left(2r_{m,k}^{2} + \sigma_{r}^{2}\right).$$

B. Efficiency of the Linear Estimate

The FIM is given by $\mathbf{F}_{ROTMA}(Z) = \sum_{k=1}^{N} \frac{1}{\sigma_r^2} \nabla_Z r_k \nabla_Z^T r_k$ with

$$\nabla_Z r_k = \frac{1}{2r_k} \mathbf{A}_k^{\mathbf{T}}.$$

Hence
$$\mathbf{F}_{ROTMA}(Z) = \frac{1}{4\sigma_r^2} \sum_{k=1}^N \frac{1}{r_k^2} \mathbf{A}_k^{\mathrm{T}} \mathbf{A}_k$$
 and the CRLB is

 $\mathbf{B}_{ROTMA}(Z) = [\mathbf{F}_{ROTMA}(Z)]^{-1}$. The theoretical Cramér–Rao inequality is respected:

$$4\sigma_r^2 \left[\sum_{k=1}^N \frac{1}{r_k^2} \mathbf{A}_k^{\mathrm{T}} \mathbf{A}_k \right]^{-1} \leq 4\sigma_r^2 \left[\sum_{k=1}^N \frac{1}{r_k^2} \frac{1}{1 + \frac{\sigma_r^2}{2r_k^2}} \mathbf{A}_k^{\mathrm{T}} \mathbf{A}_k \right]^{-1},$$

that is, $\mathbf{B}_{ROTMA}(Z) \leq Cov(\hat{Z}_{WLS})^{-1}.$
When $\frac{\sigma_r^2}{r_k^2} <<1$, for any k , then $\mathbf{B}_{ROTMA}(Z) \cong Cov(\hat{Z}_{WLS}).$

 r_k^2

The proposed estimator \hat{Z}_{WLS} is hence approximately efficient. Numerous simulations (not reported here) have confirmed this conclusion.

IV. THE OBSERVER'S TRAJECTORY CONSISTS OF TWO LEG

Now, the observer's trajectory is composed of two legs, not necessarily traveled with the same speed: the velocities are $V_{o,1}$ when $t \le \tau$ and $V_{o,2}$ when $t > \tau$. The motion equation is $P_O(t) = P_O(\tau) + (t - \tau) V_{O,i}$. We know from Proposition 3 of [8] that one ghost at most exists whose trajectory is defined by $X_G = \left[\mathbf{I}_2 \otimes \mathbf{S}_{\angle(V_{o,2}-V_{o,1})}\right] (X - X_O) + X_O$, where X_O stands for $X_O(t^*)$, and $\mathbf{S}_{2\angle(V_{o,2}-V_{o,1})}$ is the matrix of the symmetry around the line spanned by the vector $V_{O,2} - V_{O,1}$. To minimize $C(X) = \sum_{k=1}^{N} \left[\frac{r_{m,k} - r_k(X)}{\sigma_{R,k}} \right]^2$, we have

recourse to the Gauss–Newton algorithm which will return \hat{X} or $\hat{X}_{G} = \begin{bmatrix} \mathbf{I}_{2} \otimes \mathbf{S}_{\angle(v_{o,2}-v_{o,1})} \end{bmatrix} (\hat{X} - X_{o}) + X_{o}$, in unobservable cases. Two scenarios have been considered: in the first one, the target's trajectory is observable, and in the second one, proposed in [3], the target's trajectory is unobservable. For each scenario, 500 Monte Carlo simulations have been run. For each simulation, we compute the MLE \hat{X} and, if existing, the corresponding ghost \hat{X}_{G} . The performance of the MLE is evaluated by its empirical bias and the comparison of the empirical standard deviations of its components with the square roots of the diagonal elements of the CRLB.

A. Observable Scenario

is

The first leg of the observer is characterized by a heading of 45° and a speed of 4 m/s. The instant of its heading change is $\tau = 780s$. During its second leg, the speed and the heading of the observer are equal to 8.49 m/s and -70.53° , respectively. The target starts at $P_T(0) = [4,000 \ 0]^T$ (m), its speed is 5.74 m/s, and its heading is 60.5°, corresponding to velocity $V_T = \begin{bmatrix} 5 & 2\sqrt{2} \end{bmatrix}^T$ (m/s). The duration of the scenario is

¹ Let **A** and **B** be two symmetric matrices, $\mathbf{A} \leq \mathbf{B}$ means that the matrix $\mathbf{B} - \mathbf{A}$ is a non-negative matrix.

26 min. The measurements are acquired every 4 s ($\Delta t = 4s$), and the standard deviation of the noise is $\sigma_r = 50$ m. The estimates and the performance are given at the final time. Fig. 1 depicts the scenario and the 500 estimates (O and T are for the initial positions of the observer and the target, respectively). Because the FIM is singular [8], the CRLB cannot be computed; therefore in Table I the column " σ_{CRLB} " contains no value. We observe that the sets of MLEs are "croissant-shaped". This is why we present the results in Cartesian coordinates for the estimated target's position $[x \ y]^{T}$ and in polar coordinates $[r \ \theta]^{T}$ for the estimated relative position of the target w.r.t. the observer.

 TABLE I

 PERFORMANCE OF THE MLE AT FINAL TIME

X	Bias	$\sigma_{\it CRLB}$	$\hat{\sigma}$
x = 11780 m	18.87	-	30.14
y = 4401	82.69	-	803.47
$\dot{x} = 5 \text{ m/s}$	0.006	-	0.04
$\dot{y} = 2.828 \text{ m/s}$	0.17	-	0.46
<i>r</i> = 15825 m	1.74	-	7.54
$\theta = 90^{\circ}$	0.3	-	2.91
Rectify (ma)	* * *		

-4 -2 0 2 -4 6 8 10 12Fig. 1. The scenario and the estimates in an observable leg-by-leg case

Numerous other simulations with various scenarios allow us to conclude that the MLE is unbiased. But we cannot claim that the MLE reaches the CRLB, because for such scenarios, the FIM is singular.

B. Unobservable Scenario(see [3])

In [3] the authors proposed the following scenario whose duration is 30 min to test a particle filter. The first heading and the speed of the observer are respectively -80° and 2.57 m/s. At *t*=15 min, it changes its course and the second heading is 146° and keeps the same speed. At the very beginning, the target is at $P_T(0) = [7,071 \ 7,071]^T$ (m), its heading is -135° and its speed is 7.72 m/s (see Fig. 2(a)). The sampling rate is equal to 60 s and the standard deviation is $\sigma_r = 20$ m. As in [3], the estimates are given at time t*=26 min. In Table II, we give the estimate of the state vector at this time. Fig. 2(b) depicts the 90%-confidence ellipsoid (in red) together with the cloud of the position estimates (in blue), and their corresponding ghost-estimates (in red). Here, despite the presence of a ghost, the MLE is efficient. Note that adding a third leg does not guarantee observability [8].

TABLE II PERFORMANCE OF THE MLE AT TIME t*=26 min.

X	Bias	$\sigma_{\scriptscriptstyle CRLB}$	$\hat{\sigma}$
x = -1444.8 m	6.84	10.93	11.12
y = -1444.8 m	15.21	12.84	12.86
$\dot{x} = -5.46 \text{ m/s}$	0.001	0.03	0.03
$\dot{y} = -5.46 \text{ m/s}$	0.002	0.04	0.04
<i>r</i> = 455.05 m	0.49	11.09	11.99
θ = 165.31 °	0.11	1.60	1.64

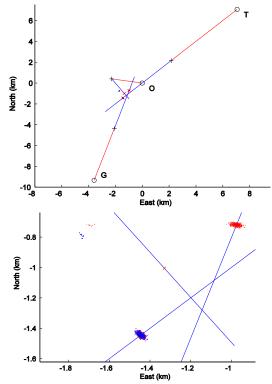


Fig. 2. (a) The scenario and the estimates in Clark's scenario [3], (b) magnification around the estimates.

V. THE OBSERVER IS IN CONSTANT ACCELERATION MOTION

In the two scenarios presented hereafter, the initial velocity vector of the observer is $\begin{bmatrix} 10 & 2 \end{bmatrix}^T$ (m/s). Its acceleration vector is $\begin{bmatrix} -0.0416 & 0 \end{bmatrix}^T$ (m/s²). In both scenarios, we choose $\sigma_r = 20m$ and $\Delta t = 1s$.

A. Example of Observable Case

The target starts at $\begin{bmatrix} -4000 & 0 \end{bmatrix}^T$ (m), with a velocity equal to $\begin{bmatrix} 10 & 2 \end{bmatrix}^T$ (m/s). Note that the observer and the target are on a rendezvous route. In this case the FIM is singular [9].

The estimates and the performance are given in Table III.

TABLE III PERFORMANCE OF THE MLE AT FINAL TIME

X	Bias	$\sigma_{\scriptscriptstyle CRLB}$	$\hat{\sigma}$
x = -410 m	2.31	-	5.58
y = 710 m	85.30	-	78.48
$\dot{x} = 10 \text{ m/s}$	0.02	-	0.04
$\dot{y} = 2 \text{ m/s}$	0.43	-	0.48
<i>r</i> = 1319 m	2.80	-	3.13

	$\theta = -90^{\circ}$	3.70	-	3.41
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B. Example of Unobservable Case

The target starts at $[2000 \ 3464]^T$ (m) with a velocity $[14.6 \ 16.3]^T$ (m/s). The observer and the target are not on a rendezvous route and the bearings are not constant. Three ghosts exist (the maximum number of ghosts). Fig. 3 depicts the result: the estimates of the initial and final position of the target (T), and the couples of estimates of the three ghost-targets' positions (G). Note that the three other solutions are computed from the MLE returned by the algorithm [9].

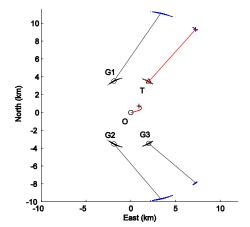


Fig. 3. The scenario and the estimates in an unobservable case.

The estimate and its performance are given in Table IV.

X	Bias	σ_{CRLB}	$\hat{\sigma}$
x = 7241.4 m	14.47	53.58	59.29
y = 9315.7 m	10.22	37.19	41.84
$\dot{x} = 14.6 \text{ m/s}$	0.02	0.39	0.39
$\dot{y} = 16.3 \text{ m/s}$	0.03	0.21	0.21
r = 10678 m	0.09	3.73	3.70
$\theta = 36^{\circ}$	0.1	0.35	0.39

TABLE IV PERFORMANCE OF THE MLE AT FINAL TIME

VI. THE OBSERVER'S TRAJECTORY CONTAINS AN ARC OF A CIRCLE

Now the observer's trajectory is composed of two legs linked by an arc of a circle. The target's trajectory was proved to be observable in [9]. No problem of convergence is indicated in our numerous simulations, provided the number of measurements during the arc of a circle is greater than 50 (otherwise, the routine can be stalled in a local minimum). In the scenario presented here, the initial position of the observer is $[-1000 \ 10,000]^T$ (m) with speed equal to 4 m/s. Its first heading is 90°. At time $\tau_1 = 700$ s, it begins its circular maneuver and finishes it at time $\tau_2 = 980$ s. At this time its new heading is equal to 225° . Meanwhile, the target has started at $[-2000 \ 25,000]^T$ (m), with a speed equal to 2 m/s following a route equal to 180° . The total duration of the scenario is 26 minutes. The standard deviation is 50 m. The performance is summarized in Table V: we observe again that the MLE is efficient. Numerous simulations, not reported here, confirm this claim.

TABLE V PERFORMANCE OF THE MLE AT FINAL TIME

X	Bias	$\sigma_{\scriptscriptstyle CRLB}$	$\hat{\sigma}$
x = -2000 m	0.85	138.56	146.68
y = 21888 m	0.25	49.58	53.04
$\dot{x} = 0 \text{ m/s}$	0.003	0.14	0.15
$\dot{y} = -2 \text{ m/s}$	0.0005	0.04	0.05
r = 15030 m	0.31	8.23	8.98
$\theta = -17.35^{\circ}$	0.0025	0.56	0.59

VII. CONCLUSION

Three types of scenario were used to study the MLE in ROTMA: observable scenarios with nonsingular FIM, observable scenario with singular FIM and unobservable scenario with nonsingular FIM. For the first one, the MLE is efficient. For the second, the MLE is unbiased, but we cannot compute the CRLB. For the last, the MLE restricted to the local solution corresponding to the true target is efficient too. When several solutions exist (presence of ghost-targets), we are able to give the other solution(s) from the one returned by the algorithm. This study could be extended to the case of maneuvering targets as in [10].

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