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► **To cite this version:**

Mahaud Morgane, Zengqiang Zhai, Michel Perez, O. Lame, Claudio Fusco, et al.. Polymer Chain Generation for Coarse-Grained Models Using Radical-Like Polymerization. *Communications in Computational Physics*, 2018, 24 (3), pp.885-898. <10.4208/cicp.OA-2017-0146>. <hal-01803207>

HAL Id: hal-01803207

<https://hal.science/hal-01803207v1>

Submitted on 3 Sep 2019

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Polymer chain generation for coarse-grained models using radical-like polymerization

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Abstract. This paper presents major improvements in the efficiency of the so-called Radical-Like Polymerization (RLP) algorithm proposed in "Polymer chain generation for coarse-grained models using radical-like polymerization" [J. Chem. Phys. **128** (2008)]. Three enhancements are detailed in this paper: (1) the capture radius of a radical is enlarged to increase the probability of finding a neighboring monomer; (2) between each growth step, equilibration is now performed with increasing the relaxation time depending on the actual chain size; (3) the RLP algorithm is now fully parallelized and proposed as a "fix" within the "Lammmps" molecular dynamics simulation suite.

AMS subject classifications: 82D60

Key words: Molecular dynamics (MD); Coarse grained polymer model; LAMMPS; Polymer; Parallel computing.

Program Summary

Program title: Fix_rlp

Nature of problem: Implementing special fix file in parallelized LAMMPS code in order to create polymer system with the so-called Radical-Like Polymerization (RLP) algorithm proposed in [1] for coarse-grained models.

Software licence: GPL 2.0 GNU's GPL

CiCP scientific software URL: http://michel.perez.net.free.fr/fix_rlp.zip.

Distribution format: .zip

Programming language(s): C++/MPI

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Computer platform: Should run on any architecture providing a C++ compiler

Operating system: Linux or any other OS with C++ compiler and MPI library.

Compilers: C++ compiler

RAM: Depends on system size and how many CPUs are used

External routines/libraries: LAMMPS (<http://lammps.sandia.gov/>), FFTW (<http://www.fftw.org/>)

Running time: Seconds to weeks, depending on system size, speed of CPU and how many CPUs are used.

Restrictions: The code is based on a former version of LAMMPS.

Additional Comments: With the `Fix_rlp` LAMMPS program, you will find in the `.zip` detailed explanations in the `"fix_rlp.txt"` file, a `"README.txt"` file for the installation and a complete example of homopolymer generation with RLP algorithm in the form of a LAMMPS input file.

1 Introduction

Coarse-grained molecular dynamics is a well-adapted tool for studying the mechanical behavior of polymers [1, 2]. It is widely used for studying various mechanical properties (elastic constants [3, 4], strain hardening [5], failure [6, 7], *etc*) for various polymer structures (linear chains [8, 9], cross-linked chains [10], branched polymers [11, 12], co-polymers [13, 14], gels [15]). To create these structures, several methods have been developed. Equilibration of fully independent self-avoiding chains [16] is a rather simple method but requires equilibration times that are not tractable with long chains. The classical "push-off" method generates self equilibrated chains by Monte-Carlo scheme (random-walk). However, long equilibration times are required to relax overlapping particles [8]. This method has been improved by introducing soft potentials [17, 18]. The equilibration stage can itself be accelerated *via* the double-bringing method [17, 19–21] or by reducing the weak interaction cut-off at the beginning of this stage [22]. They are compatible with most creation methods since they act only on equilibration, yet they don't accelerate polymer creation stage. Another method to accelerate the equilibration *via* a hybrid MD/continuum model was proposed in two versions by Kroger [23] and by Senda *et al* [24], but is limited to rather short chains. Other kinds of methods propose simultaneous chain growth and equilibration. Subramanian recently submitted an original method where polymer chains are progressively extended by adding additional beads between two existing structural units [12, 25]. Fast algorithms, based on independent generation of chains and application of "slow push-off" potential (see *e.g.* [11]) lead to rather fast equilibration times, but used soft potentials are quite far from physics of polymerization and may not be used for generation of block-copolymers and/or semi-crystalline polymers.

The Radical-Like Polymerization (RLP) algorithm originally proposed by Gao [26] and later developed by Perez *et al* [27] establishes a physical framework (based on the

radical polymerization), where chain are partially relaxed simultaneously while polymerization is in progress. This method has been used successfully for generating different polymer morphologies (linear [18,28–30], branched [31], co-polymers [13,32,33]).

However the RLP algorithm was written on a in-house serial program, which hinders both its diffusion and efficiency. The aim of this paper is therefore to propose a parallelized and optimized version of the RLP algorithm in the form of a Lammmps “fix” [34], which can readily be used by a larger community. This paper (i) recalls the basis of the Coarse Grained Molecular Dynamics (CGMD) model, (ii) details the improved RLP algorithm, (iii) documents its use within the Lammmps framework and, (iv) demonstrates the efficiency gain brought by this new algorithm.

2 Coarse grained molecular dynamics model

The RLP algorithm is well suited for molecular dynamics models, in which atoms can move freely in space. It is used here on a CGMD model widely found in the literature [8]. In this model, units interact with each other through two potentials: one representing weak interactions and the other covalent bonds. A truncated Lennard-Jones potential is used for the weak interactions:

$$U_{LJ}(r) = \begin{cases} 4\epsilon \left[\left(\frac{\sigma}{r}\right)^{12} - \left(\frac{\sigma}{r}\right)^6 \right] & r \leq r_c \\ 0 & r > r_c \end{cases} \quad (2.1)$$

where ϵ and σ are the Lennard-Jones parameters and r_c the cut-off radius. Covalent bonds are represented at the beginning of the RLP by an harmonic potential (eq. 2.2) and at the end by a finite extensible nonlinear elastic potential (FENE) (eq. 2.3).

$$U_{harm}(r) = K(r - r_0)^2 \quad (2.2)$$

where $K = 100\epsilon/\sigma^2$ is the harmonic bond stiffness and $r_0 = 1.12\epsilon$ the bond length, chosen to be the same as the Lennard-Jones one.

$$U_{FENE}(r) = \begin{cases} -0.5kR_0^2 \ln \left[1 - \left(\frac{r}{R_0}\right)^2 \right] & r < R_0 \\ \infty & r \geq R_0 \end{cases} \quad (2.3)$$

where k is the FENE bond stiffness and R_0 its cut-off radius. Here, classical values are used to avoid high frequency modes and chain crossing. $k = 30\epsilon/\sigma^2$, $R_0 = 1.5\sigma$ and $r_c = 2.5\sigma$. ϵ and σ are set to 1 to simulate a generic polymer. Units are expressed as a function of ϵ and σ . For a parameter X , results are expressed as X^* with $x = x^*\sigma$, $T = T^*\epsilon/k_b$, $P = P^*\epsilon/\sigma^3$ and $t = t^*\sqrt{m/\epsilon\sigma^2} = t^*\tau$. The time step is $dt = 5 \times 10^{-3}\tau$. Calculations are made with the software Lammmps of Sandia labs [34].

3 Radical like polymerization algorithm

In this section, we briefly recall the basis of the original RLP algorithm published in ref. [27]. **New features of the algorithm are emphasized and written in bold characters.**

- **Liquid preparation:** Polymerization takes place in a Lennard-Jones liquid constituted of N_{monom} liquid beads. For the sake of polymerization efficiency, the total number of liquid bead exceed by around 25% the total number of beads that are meant to polymerize. For example, to prepare a melt of $M=500$ chains of $N=200$ units, *i.e.* 100000 units, the liquid is composed of $N_{monom}=128000$ monomers.
- **Nucleation:** M radicals are chosen randomly among the units to create M chains. Each unit has the same probability $p = M/N_{monom}$ to become a radical.
- **Propagation:** (i) Each radical selects a monomer bead to bond within a neighboring sphere of radius R_{neigh}^* . In the original RLP algorithm, the capture radius R_{neigh}^* was set to 1.5: the maximum bond length for the FENE potential. **In order to improve the efficiency of the algorithm (*i.e.* to increase the number of selectable neighbors), the capture radius is now set to 2.5. However, as this change is not compatible with FENE potential, the created bond is of harmonic type (see eq. 2.2). The harmonic bond is later changed to a FENE bond in the finalization step.** This neighbor becomes radical and the previous radical becomes part of the chain. Then, (ii) the system is allowed to relax during $t_{bG} = 1.5\tau$ within NPT ensemble (Nose-Hoover thermostat and pressostat) at $T^* = 2$ and $P^* = 0.5$. **Another improvement consisted in increasing the relaxation time between each growth step as chains grow, with a power law: $t_{bG} = N(t)^{1.4} dt$, where $N(t)$ is the actual chain length during polymerization.** This adaptive relaxation time account the non-linear evolution of the reptation time with chain length [35].
- **Termination:** Stages (i) and (ii) of the Propagation stage are repeated until all chains reach their desired length N .
- **Finalization:** Remaining monomers are removed. **Then, in order to transform all harmonic bonds into FENE bonds, the system is equilibrated $5 \times 10^2 \tau$ within NPT ensemble (Nose-Hoover thermostat and pressostat) at $T^* = 2$ and $P^* = 0.5$, quenched at 0K and the positions of all atoms are set to minimize the energy (conjugate gradient).** The system is finally equilibrated during $t_{eq} \tau$ within NPT ensemble (Nose-Hoover thermostat and pressostat) at $T^* = 2$ and $P^* = 0.5$. The equilibration duration depends on the chain length, as showed in table 1.

4 Software Installation and Numerical Examples

4.1 Integration of the Fix_rlp program in LAMMPS

In order to use this patch code, you need to copy the two files “fix_rlp.cpp” and “fix_rlp.h” to the \src folder of LAMMPS and then compile them as you compile LAMMPS (see detailed instructions in the “README.txt” file). You will get an executable file (here lammmps.exe) and you can run the job LAMMPS script (here test.txt), like this:

```
mpirun -np 8 ./lammmps.exe < test.txt
```

The “fix_rlp” command is based on the “fix bond/create” from Lammmps. It presents the following form (see detailed in the “fix_rlp.txt” file):

```
fix ID groupID rlp Nevery lontype radtype intype Rneigh bondtype lmax keyword values
```

- ID = function instance identifier
- groupID = identifier of the group on which the function apply
- Nevery = attempt bond creation every this many steps
- lontype = type of the units which do not belong to a chain
- radtype = type of the radical units and chains ends at the end of run
- intype = type of the units which belonged to a chain and are not radicals
- Rneigh = two atoms separated by less than R_{neigh} can bond (distance units)
- bondtype = type of created bonds
- lmax = maximal size of a molecule, radicals included

The optional keywords and their values are:

- maxbound bmax. bmax is the maximal number of bonds of type bondtype an atom can have
- prob proba seed. Create a bond with probability proba using seed for random number generation.

Below, an example of homopolymer generation with RLP algorithm, a LAMMPS input script file, starting with a initial structure file “Polymer2000.dat” that you can find in the .zip file:

```
#### STEP 1 : Creation of monomer bath
#----- Simulation box
dimension 3
units lj
boundary p p p
atom_style bond

#loading of the atom box created aside
read_data Polymer2000.dat
mass * 1.0

pair_style lj/cut 2.5
pair_coeff * * 1.0 1.0 2.5

#----- Output
thermo_style custom step temp etotal press
thermo 100

#----- Melting
velocity all create 2 123456789 dist gaussian
fix fix_melt all npt temp 2.0 2.0 100 iso 0.5 0.5 100
run 100000

print "monomer bath created"

#### STEP 2 : Creation of radicals
#----- Radicals activation
label loop_radical
variable M equal 50
variable k loop 1 ${M}
variable krad equal ${k}*35
set atom ${krad} type 2
set atom ${krad} mol ${k}
next k
jump test.txt loop_radical

print "radicals created"

#### STEP 3 : Radical-Like Polymerization
#----- Variables setting
#number of timestep between two growing steps
```

```

variable runstep equal 300
#maximal number of growing steps
variable numberofcycles equal 50
#maximal length of a polymer
variable N equal 10

#----- Bond setting
special_bonds fene extra 5
bond_style harmonic
bond_coeff 1 100 1.12

print "RLP environnement created"

#----- RLP
fix fixrlp all rlp ${runstep} 1 2 3 2 1 ${N} prob 0.5 12345
variable runrlp equal ${runstep}*${numberofcycles}
run ${runrlp}

print "RLP finished"

#### STEP 4 : delete loners
group delete_monomer type 1
delete_atoms group delete_monomer
unfix fixrlp
run 100000

print "loners erased"

#### STEP 5 : Harmonic to Fene
min_style cg
minimize 1e-4 1e-4 10000 10000
bond_style fene
bond_coeff 1 30 1.5 1 1
run 5000000

```

4.2 Characterization of generated melts

The Flory characteristic ratio $C_n(n)$, which is an important measure of the conformation and rigidity of individual chains, is defined as

$$C_n(n) = \frac{\langle r^2(n) \rangle}{n \langle l^2 \rangle}. \quad (4.1)$$

where l is the bond length. $\langle r^2(n) \rangle$ is the mean square internal distance, defined as

$$\langle r^2(n) \rangle = \sum_{i=1}^M \frac{\sum_{j=1}^{N^i-n} (r_j^i - r_{j+n}^i)^2 / (N^i - n)}{M} \quad (4.2)$$

where r_j^i is the position of j^{th} unit of the i^{th} chain and N^i the i^{th} chain length, and $\langle l^2 \rangle = \langle r^2(1) \rangle$.

In order to confirm that the melt is properly equilibrated, the characteristic ratio $C_n(n)$ is measured and compared to a target function which is an average from conformations of brute-force equilibrated melt from $5 \times 10^5 \tau$ to $10^6 \tau$ for the system of 200 chains of 500 units. $C_n(n)$ of four samples of different chain lengths are represented on figure 1 after stabilization and compared to the target function. We observe that all systems are well equilibrated with this procedure. We can notice a sizable deformation of the characteristic ratio of the chain of $N = 500$ for $n > 100$, which is due to poor statistic for large n . Note that the final equilibration duration is reduced compared to the reference of Auhl *et al*, e.g $t_{eq} = 2.6 \times 10^6 \tau$ for $N = 350$ versus $t_{eq} = 10^5 \tau$ for $N = 500$ in our case, see table 1.

Chain length N	10	50	200	500
t_{eq} (units of τ)	$< 2 \times 10^3$	2.5×10^3	2.5×10^4	10^5

Table 1: Final equilibration stage duration for different chain lengths.

The topology of the melt was also characterized by calculating the average contour length, $\langle L_{pp} \rangle$, the entanglement length, N_e , and the average number of interior kinks, $\langle Z \rangle$ using the Z1 code [36]. The entanglement length N_e was estimated by the classical S-coil formula, $N_e = (N-1) \langle r^2(N) \rangle / \langle L_{pp} \rangle^2$. In table 2, the values of $\langle L_{pp} \rangle$ and $\sqrt{\langle L_{pp}^2 \rangle}$, $\langle Z \rangle$ and N_e are reported for $N = 500$ after $t_{eq} = 10^5 \tau$ and compared to the brute force equilibrated melt. The agreement is satisfactory for all investigated variables, proving the correct equilibration of the $N = 500$ system for $t_{eq} = 10^5 \tau$.

	$\langle L_{pp} \rangle$	$\sqrt{\langle L_{pp}^2 \rangle}$	N_e	$\langle Z \rangle$
brute-force equilibrated melt	69.45	71.00	93.99	8.38
$t_{eq} = 10^5 \tau$ for $N = 500$	68.65	70.13	95.33	8.36

Table 2: Chain topology: average contour length, $\langle L_{pp} \rangle$ and $\sqrt{\langle L_{pp}^2 \rangle}$, entanglement length, N_e , and average number of interior kinks, $\langle Z \rangle$ for $N = 500$ after $t_{eq} = 10^5 \tau$ and for the brute force equilibrated melt.

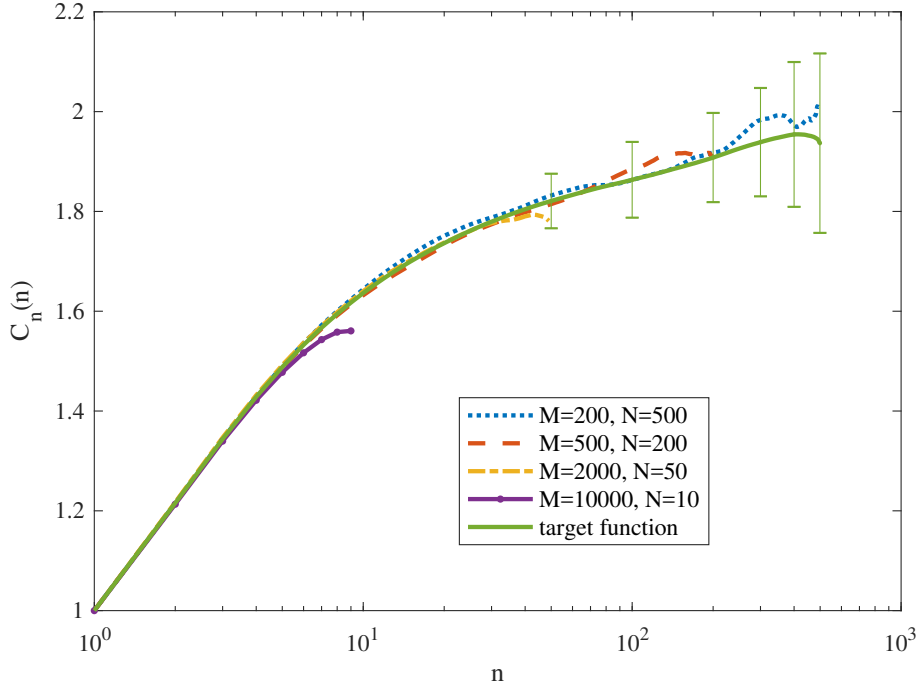


Figure 1: The characteristic ratio $C_n(n)$ for different chain lengths obtained with the updated RLP method and compared to the brute-force equilibrated melt (target function). The error bars of the target function have been added for $n=50, 100, 200, 300, 400$ and 499 .

4.3 Effect of capture radius

To obtain an estimation of the improvement due to the capture radius set in the propagation stage, capture radii R_{neigh}^* of 1.5, 2 and 2.5 have been tested. $R_{neigh}^* = 1.5$ corresponds to the cutoff value of the FENE bond, which is the value used in the original RLP paper [27]. $R_{neigh}^* = 2.5$ corresponds to the cutoff radius of the Lennard-Jones pair potential. A melt is prepared as described above. The chain length N is set to 200 and the number of chains M to 500. All simulations have been made on the same 32 processors. They include the nucleation, propagation and termination stages. Simulation times are presented in tab. 3.

As expected, increasing R_{neigh}^* leads to a simulation time drop, due to an improvement in the propagation stage efficiency. It can be noticed that this improvement is more

R_{neigh}^*	1.5	2	2.5
$t(s)$	477	386	359

Table 3: Effect of capture radius on simulation duration of RLP process (nucleation-propagation-termination). Simulations are performed on 32 processors.

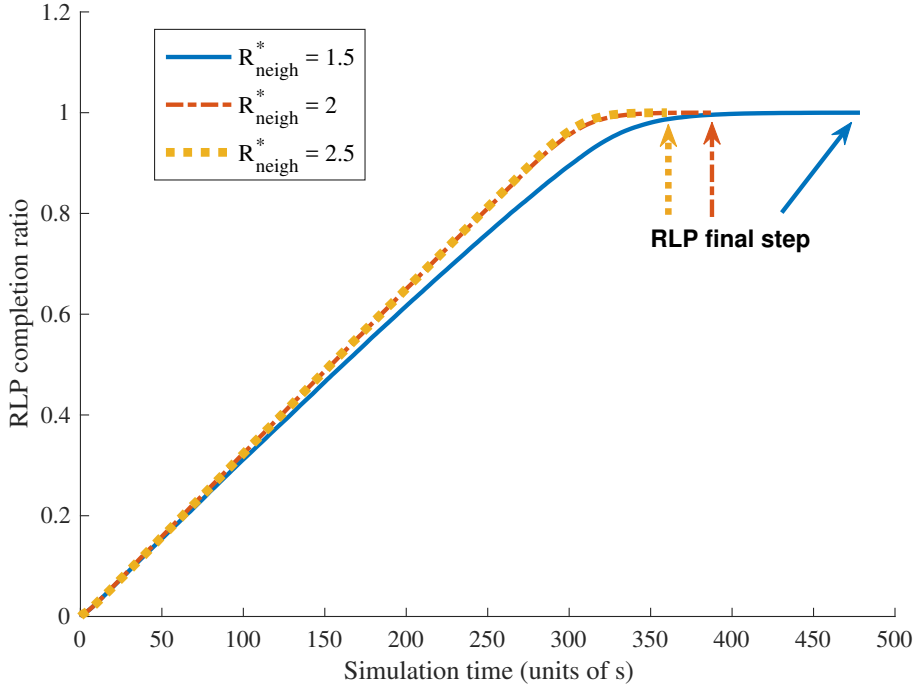


Figure 2: RLP process completion ratio as a function of capture radius $R_{neigh}^* = 1.5, 2$ and 2.5 . A larger capture radius decrease the total generation time.

important between 1.5 and 2 than between 2 and 2.5.

The RLP completion ratio (total polymerized units over NM) is represented as a function of time on figure 2. In a first stage, polymerization ratio is proportional with time (constant rate polymerization reaction). In a second stage, polymerization ratio reaches a plateau, the last few units to polymerize are the longest to capture. Whereas capture radius has a limited effect during the first stage, it has a strong impact on the second stage, facilitating the capture of new monomers when they start to be “rare” in the melt. Note that going to higher values than 2.5 would imply an increase of the Lennard-Jones cut-off radius, used by Lammers to calculate the neighbor list, which would lead to unnecessary additional computational time.

4.4 Effect of increasing relaxation time during polymerization

In order to optimize global simulation time for complete polymerization and equilibration, a non-constant, and increasing, relaxation time between each growth step (t_{bG}) has been introduced. In order to test this improvement, two simulations are compared for a system of $M = 500$ chains of $N = 200$ monomers: (1) a polymerization with constant $t_{bG} = 1.5\tau$ relaxation time between each growth step (corresponding a total of $4.5 \times 10^2\tau$) followed by an equilibration of $10^4\tau$ (like the original RLP algorithm); (2) a polymeriza-

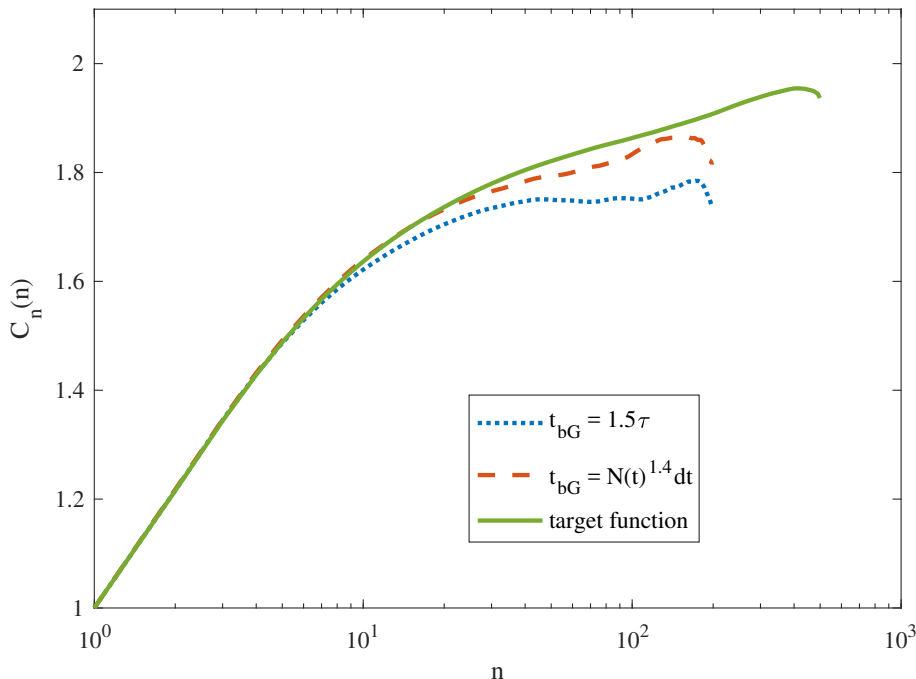


Figure 3: Effect of increasing relaxation time during polymerization: comparison between polymerization with constant ($t_{bG}=1.5\tau$) and increasing relaxation time ($t_{bG}=N(t)^{1.4}dt$ where $dt=5\times 10^{-3}\tau$) during polymerization. The upper curve is the brute-force equilibrated melt (target function). The increasing relaxation time clearly leads to a better equilibration.

tion with increasing relaxation time between each growth step $t_{bG}=N(t)^{1.4}dt$, where $N(t)$ is the actual size of the polymer chain during polymerization (corresponding a total of $1.5\times 10^3\tau$ followed by an equilibration of $8.5\times 10^3\tau$).

In figure 3, the characteristic ratio $C_n(n)$ of the two simulations are compared with the target function. It can be clearly seen that increasing the relaxation time t_{bG} during polymerization leads to a better equilibration compared to a constant one, *for the same total simulation time* including polymerization and equilibration.

4.5 Parallelisation efficiency

The original RLP algorithm was written as a in-house serial MD code. In order to improve (i) its ease of use and (ii) its computational efficiency, it has been adapted as a “fix” to the LAMMPS MD suite. One of the best feature of LAMMPS is its parallelization efficiency, which is almost linear. The parallelization efficiency of the RLP process implemented as a LAMMPS fix is tested on a sample of 500 chains of 200 units on 1, 2, 4, 8, 16, 32, 64 and 124 processors. A liquid containing $N_{monom}=128000$ monomers is created and the nucleation, propagation and termination phases are simulated with $R_{neigh}^*=2.5$. Results are shown fig. 4. They are compared to the ideal time improvement where the simulation

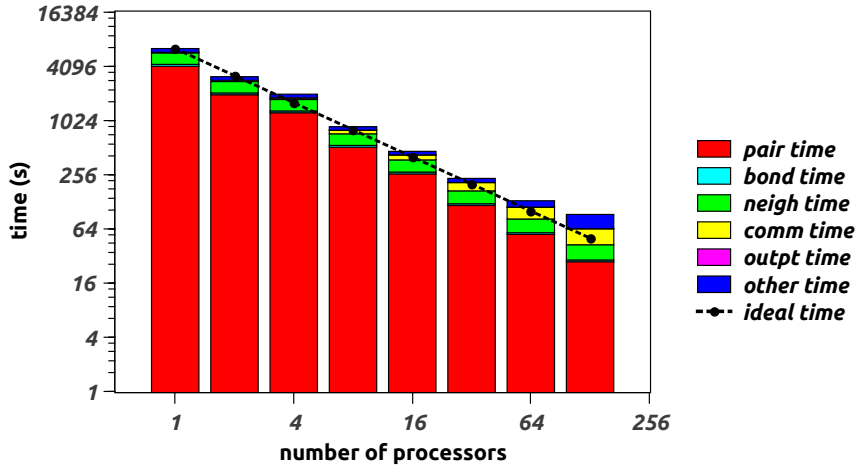


Figure 4: Benchmark of initialization and propagation stages. Simulation time as a function of the processors number. The dotted line represent an ideally parallelized algorithm.

time is divided by a factor 2 when the number of processors is doubled. We can notice the simulation time is close to the optimal time up to 32 processors, proving thus that the RLP algorithm is efficiently parallelized.

5 Conclusion

The radical-like polymerization algorithm described in the original article of Perez *et al* [27] has been extensively improved. Propagation step efficiency has been improved by enlarging the capture radius of radicals up to $R_{neigh}^* = 2.5$. RLP algorithm is now available as a LAMMPS “fix” that can be readily used by the whole LAMMPS community. The parallelization efficiency of RLP algorithm is almost linear, leaving the parallelization capability of LAMMPS intact. In this paper, only linear homopolymers are designed. Nonetheless the RLP algorithm can be used for poly-dispersed chains, branched polymers, or even block co-polymers.

Acknowledgments

This work was performed using HPC resources from the FLMSN, Fédération Lyonnaise de Modélisation et Sciences Numériques, partner of EQUIPEX EQUIP@MESO.

References

- [1] J. Padding, W. Briels, Systematic coarse-graining of the dynamics of entangled polymer melts: the road from chemistry to rheology, *Journal of Physics: Condensed Matter* 23 (23)

- (2011) 233101.
- [2] K. Binder, Monte Carlo and Molecular Dynamics Simulations Polymer, Oxford University Press, Inc., 1995.
URL <http://dl.acm.org/citation.cfm?id=526532>
- [3] M. Vladkov, J.-L. Barrat, Linear and nonlinear viscoelasticity of a model unentangled polymer melt: molecular dynamics and rouse modes analysis, *Macromolecular theory and simulations* 15 (3) (2006) 252–262.
- [4] M. Kroger, W. Loose, S. Hess, Rheology and structural changes of polymer melts via nonequilibrium molecular dynamics, *Journal of Rheology (1978–present)* 37 (6) (1993) 1057–1079.
URL <http://scitation.aip.org/content/sor/journal/jor2/37/6/10.1122/1.550409>
- [5] R. S. Hoy, M. O. Robbins, Strain hardening of polymer glasses: Effect of entanglement density, temperature, and rate, *Journal of Polymer Science Part B: Polymer Physics* 44 (24) (2006) 3487–3500.
- [6] S. W. Sides, G. S. Grest, M. J. Stevens, Large-scale simulation of adhesion dynamics for end-grafted polymers, *Macromolecules* 35 (2) (2002) 566–573.
- [7] J. Rottler, M. O. Robbins, Growth, microstructure, and failure of crazes in glassy polymers, *Physical Review E* 68 (1) (2003) 011801.
- [8] K. Kremer, G. S. Grest, Dynamics of entangled linear polymer melts: A molecular-dynamics simulation, *The Journal of Chemical Physics* 92 (8) (1990) 5057–5086.
- [9] K. Farah, A. C. Fogarty, M. C. Böhm, F. Müller-Plathe, Temperature dependence of coarse-grained potentials for liquid hexane, *Physical Chemistry Chemical Physics* 13 (7) (2011) 2894–2902.
- [10] Y. R. Sliozberg, T. L. Chantawansri, Computational study of imperfect networks using a coarse-grained model, *The Journal of chemical physics* 139 (19) (2013) 194904.
- [11] Y. R. Sliozberg, J. W. Andzelm, Fast protocol for equilibration of entangled and branched polymer chains, *Chemical Physics Letters* 523 (2012) 139–143.
- [12] G. Subramanian, An Iterative Method for Producing Equilibrated Symmetric Three-Arm Star Polymer Melts in Molecular Dynamics, *Macromolecular Theory and Simulations* 20 (1) (2011) 46–53.
URL <http://onlinelibrary.wiley.com/sci-hub.io/doi/10.1002/mats.201000062/full>
- [13] A. Makke, O. Lame, M. Perez, J.-L. Barrat, Influence of tie and loop molecules on the mechanical properties of lamellar block copolymers, *Macromolecules* 45 (20) (2012) 8445–8452.
URL <http://pubs.acs.org/doi/abs/10.1021/ma301286y>
- [14] J. R. Brown, Y. Seo, T. A. D. Maula, L. M. Hall, Fluids density functional theory and initializing molecular dynamics simulations of block copolymers, *The Journal of chemical physics* 144 (12) (2016) 124904.
- [15] Y. R. Sliozberg, T. L. Chantawansri, J. L. Lenhart, J. W. Andzelm, Structural and mechanical properties of advanced polymer gels with rigid side-chains using coarse-grained molecular dynamics, *Polymer* 55 (20) (2014) 5266–5275.
URL <http://www.sciencedirect.com/science/article/pii/S0032386114007666>
- [16] T. Vettorel, K. Kremer, Development of entanglements in a fully disentangled polymer melt, *Macromolecular Theory and Simulations* 19 (1) (2010) 44–56.
URL <http://onlinelibrary.wiley.com/doi/10.1002/mats.200900065/full>
- [17] R. Auhl, R. Everaers, G. S. Grest, K. Kremer, S. J. Plimpton, Equilibration of long chain polymer melts in computer simulations, *The Journal of chemical physics* 119 (24) (2003)

- 12718–12728.
- [18] L. A. Moreira, G. Zhang, F. Müller, T. Stuehn, K. Kremer, Direct equilibration and characterization of polymer melts for computer simulations, *Macromolecular Theory and Simulations* 24 (5) (2015) 419–431.
URL <http://onlinelibrary.wiley.com/doi/10.1002/mats.201500013/full>
- [19] N. C. Karayiannis, V. G. Mavrantzas, D. N. Theodorou, A novel Monte Carlo scheme for the rapid equilibration of atomistic model polymer systems of precisely defined molecular architecture, *Physical review letters* 88 (10) (2002) 105503.
URL <http://journals.aps.org/prl/abstract/10.1103/PhysRevLett.88.105503>
- [20] N. C. Karayiannis, A. E. Giannousaki, V. G. Mavrantzas, An advanced Monte Carlo method for the equilibration of model long-chain branched polymers with a well-defined molecular architecture: Detailed atomistic simulation of an H-shaped polyethylene melt, *The Journal of chemical physics* 118 (6) (2003) 2451–2454.
URL <http://scitation.aip.org/content/aip/journal/jcp/118/6/10.1063/1.1543580>
- [21] L. D. Peristeras, I. G. Economou, D. N. Theodorou, Structure and volumetric properties of linear and triarm star polyethylenes from atomistic Monte Carlo simulation using new internal rearrangement moves, *Macromolecules* 38 (2) (2005) 386–397.
URL <http://pubs.acs.org/doi/abs/10.1021/ma048364p>
- [22] Y. R. Sliozberg, M. Kröger, T. L. Chantawansri, Fast equilibration protocol for million atom systems of highly entangled linear polyethylene chains, *The Journal of Chemical Physics* 144 (15) (2016) 154901.
- [23] M. Kroger, Efficient hybrid algorithm for the dynamic creation of wormlike chains in solutions, brushes, melts and glasses, *Computer physics communications* 118 (2) (1999) 278–298.
URL <http://www.sciencedirect.com/science/article/pii/S001046559800160X>
- [24] Y. Senda, M. Fujio, S. Shimamura, J. Blomqvist, R. M. Nieminen, Fast convergence to equilibrium for long-chain polymer melts using a MD/continuum hybrid method, *The Journal of chemical physics* 137 (15) (2012) 154115.
URL <http://scitation.aip.org/content/aip/journal/jcp/137/15/10.1063/1.4759036>
- [25] G. Subramanian, A topology preserving method for generating equilibrated polymer melts in computer simulations, *The Journal of chemical physics* 133 (16) (2010) 164902.
URL <http://scitation.aip.org/content/aip/journal/jcp/133/16/10.1063/1.3493329>
- [26] J. Gao, An efficient method of generating dense polymer model melts by computer simulation, *The Journal of chemical physics* 102 (2) (1995) 1074–1077.
URL <http://scitation.aip.org/content/aip/journal/jcp/102/2/10.1063/1.469455>
- [27] M. Perez, O. Lame, F. Leonforte, J.-L. Barrat, Polymer chain generation for coarse-grained models using radical-like polymerization, *The Journal of chemical physics* 128 (23) (2008) 234904.
- [28] A. Makke, M. Perez, O. Lame, J.-L. Barrat, Mechanical testing of glassy and rubbery polymers in numerical simulations: Role of boundary conditions in tensile stress experiments, *The Journal of chemical physics* 131 (1) (2009) 014904.
- [29] A. Makke, M. Perez, J. Rottler, O. Lame, J.-L. Barrat, Predictors of Cavitation in Glassy Polymers under Tensile Strain: A Coarse-Grained Molecular Dynamics Investigation, *Macromolecular Theory and Simulations* 20 (9) (2011) 826–836.
- [30] K. Farah, H. A. Karimi-Varzaneh, F. Müller-Plathe, M. C. Böhm, Reactive molecular dynamics with material-specific coarse-grained potentials: growth of polystyrene chains from

- styrene monomers, *The Journal of Physical Chemistry B* 114 (43) (2010) 13656–13666.
- [31] Z. Zhang, L. Wang, Z. Wang, X. He, Y. Chen, F. Müller-Plathe, M. C. Böhm, A coarse-grained molecular dynamics–reactive monte carlo approach to simulate hyperbranched polycondensation, *RSC Advances* 4 (100) (2014) 56625–56636.
- [32] A. Makke, M. Perez, O. Lame, J.-L. Barrat, Nanoscale buckling deformation in layered copolymer materials, *Proceedings of the National Academy of Sciences* 109 (3) (2012) 680–685.
URL <http://www.pnas.org/content/109/3/680.short>
- [33] F. Léonforte, Evolution of entanglements during the response to a uniaxial deformation of lamellar triblock copolymers and polymer glasses, *Physical Review E* 82 (4) (2010) 041802.
- [34] S. Plimpton, Fast Parallel Algorithms for Short-Range Molecular Dynamics, *Journal of Computational Physics* 117 (1) (1995) 1 – 19. doi:<http://dx.doi.org/10.1006/jcph.1995.1039>.
URL <http://www.sciencedirect.com/science/article/pii/S002199918571039X>
- [35] P.-G. De Gennes, *Scaling concepts in polymer physics*, Cornell university press, 1979.
- [36] M. Kroger, Shortest multiple disconnected path for the analysis of entanglement in two- and three-dimensional polymeric systems, *Computer Physics Communications*, 168 (2005) 209.