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An Adaptive Sliding Mode Control based Maximum Power Point Tracking method for a PV stand-alone System

Ameni KCHAOU¹, Assil AYADI¹, Aziz NAAMANE², Nacer M'SIRDI² and Yassine KOUBAA¹

Abstract— This paper presents a photovoltaic (PV) system with an adaptive sliding mode control based maximum power point tracking (MPPT) algorithm. The goal of this work is to maximize power extraction from the photovoltaic generator. This aim is achieved by using an adaptive sliding mode controller (ASMC) that drives a boost converter connected between the PV generator and the load. The robustness and stability of the proposed controller are investigated against weather changes. Simulation results with real data, under MATLAB-SIMULINK, are given to demonstrate the effectiveness of the proposed approach.

Index Terms—PV system, adaptive sliding mode control, MPPT, boost converter

NOMENCLATURE

V_{nv}	PV	array	voltage
V_{DV}	PV	array	vonage

- I_{pv} PV array current.
- *I_{ph}* light-generated current.
- I_d PV saturation current.
- I_{rr} saturation current at T_r .
- *I_{scr}* short-circuit current at reference condition.
- *T* cell temperature (K).
- T_r reference temperature.
- G solar irradiance (W/m^2) .
- G_n reference irradiation.
- *k_i* short-circuit temperature coefficient.
- k_b Boltzmann's constant.
- q charge of an electron.
- *A* ideality factor.
- V_s the voltage of the capacitance C_s .
- I_L the current on the inductance L.
- R_c the internal resistance on the capacitance C_e .
- V_D the forward voltage of the power diode.
- *R* load resistance.
- *U* duty ratio of the PWM control input signal.

I. INTRODUCTION

Nowadays, photovoltaic energy sources for power production are getting more and more interesting taking advantage of its availability everywhere and its environmental quality. Photovoltaic energy is more useful in remote sites such as deserts and rural zones where the difficulties to transport fuel and the lack of energy lines results in making the use of conventional resources impractical.

The efficiency of a PV system is highly dependent on weather conditions. That's why, extracting the maximum power from the photovoltaic system becomes a challenge. For these reasons, the design of Maximum power point tracking (MPPT) controller is essential in the device operation for successful PV applications.

Over the years, several MPPT algorithms have been developed and widely adapted to search the maximum power point [10] such as Perturb and Observe (P&O) algorithm [9], the Incremental Conductance (IC) algorithm [3]. There are other approaches based on the artificial intelligence method such as the fuzzy logic [5] and neural network methods [1]. Due to the rapid change of weather conditions, a robust controller seems to be very required to guarantee the tracking of optimal position with high accuracy.

The Sliding Mode Control (SMC) has recently attracted attention from researchers thanks to its advantages [8] which are its ease of implementation, robustness and great performance in different fields. Yet, its main drawback is chattering phenomena caused by the high frequency switching control. To get rid of this obstacle, authors in [4] propose an Adaptive Sliding Mode Control (ASMC). The gain obtained using the adaptive algorithm is not over estimated, so it reduces the oscillations and the chattering.

The main interest of this work is the use of ASMC in the PV system by maximizing the power generated from the PV panels. The proposed control methodology is built into two steps. The first step consists of determining V_{ref} which represents the maximum power voltage. The second is to perform the system tracking based on the SMC for a boost converter and according to the reference voltage value. The controller uses the error between the measured voltage of the PV module and the voltage generated by the voltage reference to adjust continuously the duty cycle of the DC-DC converter so that the error is removed.

The paper is organized as follows: a brief description of the photovoltaic power generation system is presented in Section 2. Section 3 is dedicated to the explanation of the proposed controller. Simulation results are carried out in Section 4. Finally, some conclusions are made up in Section 5.

II. ELECTRICAL CHARACTERISTICS OF PHOTOVOLTAIC POWER GENERATION SYSTEM

Generally, a photovoltaic generation system, shown in Fig. 1, contains the following main components:

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- Photovoltaic generator which converts solar energy into electric energy,
- 2) DC-DC converter exploiting the generated voltage by the PVG to feed the load voltage,
- 3) Digital controller that drives the converter commutations according to the MPPT capability,
- 4) Load.



Fig. 1. Synoptic diagram of the photovoltaic system

A. PV generator model

In literature, it exists several mathematical models [12] that describe the operation and behavior of the photovoltaic generator. In this paper, we use the one diode model.



Fig. 2. Simplified equivalent circuit of PV array

Its equivalent circuit, shown in Fig. 2, consists of a light generator source I_{ph} , a diode with a reverse saturation current I_d , a resistance R_{sh} in parallel expressing a leakage current and a serial resistance R_s describing an internal resistance to the current flow.

The main equation of the output current of an array is [11]:

$$I_{pv} = I_{ph} - I_d \left[\exp\left(\frac{qV_{pv}}{k_bTA}\right) - 1 \right] - \frac{V_{pv} + R_pI_{pv}}{k_bTA} \quad (1)$$

The photo-current expression is given by

$$I_{ph} = \left(\frac{G}{G_n}\right) \left[I_{scr} + k_i(T - T_r)\right]$$
(2)

The saturation current is expressed as

$$I_d = I_{rr} \left[\frac{T}{T_r} \right]^3 \exp\left[\frac{q}{k_b T A} \left(\frac{1}{T_r} - \frac{1}{T} \right) \right]$$
(3)



(a) under different temperature values and fixed irradiation= $1000W/m^2$



(b) under different irradiation values and fixed temperature = $25^{\circ}C$

Fig. 3. Power-Voltage characteristics

In fact, R_s is taken very large and R_{sh} is taken very small. The PV current becomes

$$I_{pv} = I_{ph} - I_d \left[\exp(\frac{qV_{pv}}{k_b T A}) - 1 \right]$$
(4)

The Power-Voltage characteristic of the PV panel is plotted in Fig. 3. Considering the first case when only temperature is changing as shown in Fig. 3(a), the photovoltaic power increases whenever the temperature is decreasing. However, for different irradiation levels, Fig. 3(b) shows that the photovoltaic power increases with high value of irradiation.

B. DC-DC converter

Photovoltaic system needs a boost type converter. It uses an MPPT controller to maintain the maximum output power. The circuit diagram of the converter and the load in shown Fig. 4.



Fig. 4. Simplified equivalent circuit of PV array

The converter [6] is assumed to operate in a continuous conduction mode with two states based on the switch status.

The dynamics of the boost converter are written as

$$\begin{cases} \frac{dV_{pv}}{dt} = \frac{1}{C_e} (I_{pv} - I_L) \\ \frac{dI_L}{dt} = \frac{1}{L} V_{pv} - \frac{R_c (1 - U)}{L (1 + \frac{R_c}{R})} I_L - \frac{1 - U}{L} V_D \\ + \frac{1 - U}{L} \left(\frac{R_c}{R + R_c} - 1 \right) V_s \\ \frac{dV_s}{dt} = \frac{1 - U}{C_s \left(1 + \frac{R_c}{R} \right)} I_L - \frac{1}{C_s (R + R_c)} V_s \end{cases}$$
(5)

Let $x_1(t) = V_{pv}(t)$, $x_2(t) = I_L(t)$, $x_3(t) = V_s(t)$, $x_{1d}(t) = V_{ref}(t)$. The system dynamics (5) can be rewritten as

$$\begin{cases} \dot{x_1} = \frac{1}{C_e} (I_{pv} - x_2) \\ \dot{x_2} = f_1(x) + g_1(x)U(t) \\ \dot{x_3} = f_2(x) + g_2(x)U(t) \end{cases}$$
(6)

where $\mathbf{x} = \begin{bmatrix} x_1 & x_2 & x_3 \end{bmatrix}^T$

$$\begin{cases} f_{1}(x) = \frac{x_{1}}{L} - \frac{R_{c}}{L(1 + \frac{R_{c}}{R})} x_{2} + \frac{1}{L} \left(\frac{R_{c}}{R + R_{c}} - 1\right) x_{3} - \frac{1}{L} V_{D} \\ g_{1}(x) = -\frac{R_{c}}{L(1 + \frac{R_{c}}{R})} x_{2} - \frac{1}{L} \left(\frac{R_{c}}{R + R_{c}} - 1\right) x_{3} + \frac{1}{L} V_{D} \\ f_{2}(x) = \frac{1}{C_{e}(1 + \frac{R_{c}}{R})} x_{2} - \frac{1}{C_{e}(R + R_{c})} x_{3} \\ g_{2}(x) = -\frac{1}{C_{s}(1 + \frac{R_{c}}{R})} x_{2} \end{cases}$$

$$(7)$$

III. CONTROLLER DESIGN

The SMC-MPPT algorithm is divided into two steps:

- In the first step: the reference voltage V_{ref} value, at which the system reaches its maximum power, is determined via the Incremental Conductance algorithm.
- While in the second step: both controllers, Classical Sliding Mode (CSMC) and Adaptive Sliding Mode (ASMC), use the error between the measured voltage of the photovoltaic module and the reference voltage.

These steps ensure that the system is operating at its optimal point.

A. MPP searching: Incremental Conductance method (IC)

The Incremental Conductance method (IC) is used to search the MPP voltage V_{ref} . The power slope $\frac{dP_{pv}}{dV_{pv}}$ can be expressed as

$$\frac{dP_{pv}}{dV_{pv}} = I_{pv} + V_{pv} \frac{dI_{pv}}{dV_{pv}}$$
(8)

In the case When the power slope $\frac{dP_{PV}}{dV_{pv}} = 0$, i.e., $\frac{dI_{PV}}{dV_{pv}} = -\frac{I_{PV}}{V_{pv}}$, the photovoltaic system is at the maximum power point. Therefore, the update law for V_{ref} is given by the following rules

$$\begin{cases} V_{ref}(k) = V_{ref}(k-1) + \Delta V &, for \quad \frac{dI_{pv}}{dV_{pv}} > -\frac{I_{pv}}{V_{pv}} \\ V_{ref}(k) = V_{ref}(k-1) - \Delta V &, for \quad \frac{dI_{pv}}{dV_{pv}} < -\frac{I_{pv}}{V_{pv}} \end{cases}$$
(9)

where $V_{ref}(k)$ is the reference maximum power voltage at k^{th} step and ΔV is the update parameter. The flowchart of the searching procedure can be concluded as Fig. 5. After iterative adjustment of V_{ref} , the maximum power condition is achieved only when $\frac{dP_{PV}}{dV_{PV}} = 0$.



Fig. 5. Flow chart of the maximum power voltage searching algorithm

Thus, the problem is changed to control the PV array voltage V_{pv} to follow the reference maximum power voltage V_{ref} which is the role of the classical sliding mode and the adaptive sliding mode.

B. Classical Sliding Mode Controller (CSMC)

To achieve the MPP, the sliding mode controller is introduced. Once V_{pv} always follows V_{ref} , the PV power system will move to the maximum power point along the incremental conductance adjusting. The voltage tracking error and its time derivative are given below:

$$\begin{cases} e_1(x) = x_1 - x_{1d} \\ \dot{e}_1(x) = -\frac{1}{C_e} \left(-x_2 + I_{pv} \right) - \dot{x}_{1d} \end{cases}$$
(10)

Taking x_2 as a virtual control input, the auxiliary tracking error $e_2 = x_2 - x_{2d}$ with $x_{2d} = I_{pv} - C_e \dot{x}_{1d}$. The new dynamics becomes:

$$\begin{cases} \dot{e}_1(x) = -\frac{e_2}{C_e} \\ \dot{e}_2(x) = f_1(x) - \dot{x}_{2d} + g_1(x)U(t) \end{cases}$$
(11)

where $\dot{x}_{2d} = \dot{I}_{pv} - C_e \ddot{x}_{2d}$.

To gain benefit of a controller, a PID sliding surface is

designed as in [2]:

$$S = k_p e_1 + k_i \int e_1 + k_d \dot{e}_1$$
 (12)

where k_p , k_i and k_d are positives constants. These parameters are chosen to engender a Hurwitz polynomial. Taking the time derivative of (12) yields

$$\dot{S} = k_p \dot{e}_1 + k_i e_1 + k_d \ddot{e}_1 \tag{13}$$

Substituting (11) into (13) yields

$$\dot{S} = k_p \dot{e_1} + k_i e_1 - \frac{k_d}{C_e} \dot{e_2}$$

$$\dot{S} = k_p \dot{e_1} + k_i e_1 - \frac{k_d}{C_e} [f_1(x) - \dot{x}_{2d} + g_1(x)U(t)] \quad (14)$$

The SMC law is designed as

$$U = U_{eq} + U_{sw} \tag{15}$$

Forcing $\dot{S} = 0$, the equivalent control is obtained as

$$U_{eq} = \frac{1}{g_1(x)} \left[\frac{k_p}{k_d} C_e \dot{e}_1 + \frac{k_i}{k_d} C_e e_1 - f_1(x) + \dot{x}_{2d} \right]$$
(16)

The switching term U_{sw} is given by

$$U_{sw} = \frac{1}{g_1(x)} U_{disc} \tag{17}$$

with

$$U_{disc} = \eta \ sign(S) \tag{18}$$

where η is a positive constant.

- -

The sliding mode control law can be written as

$$U = \frac{1}{g_1(x)} \left[\frac{k_p}{k_d} C_e \dot{e}_1 + \frac{k_i}{k_d} C_e e_1 - f_1(x) + \dot{x}_{2d} + \eta \ sign(S) \right]$$
(19)

C. Adaptive Sliding Mode Controller (ASMC)

1) Control law: The discontinuous term of the classical sliding mode is replaced by an adaptive Proportional Integral term.

$$U_{sw} = \frac{1}{g_1(x)} U_{PI}$$
(20)

The adaptive controller is given in [7] the following expression:

$$U_{PI} = K_P S(t) + K_I \int S(t)$$
(21)

where K_P and K_I are the computed control gains. The adaptive PI term derived from (21) can be rewritten

$$U_{PI} = \boldsymbol{\theta}^T \boldsymbol{\psi}(\boldsymbol{S}(t)) \tag{22}$$

where θ and $\psi(S(t))$ are, respectively, the adjustable parameters vector and the regressive vector given by $\theta = [K_P K_I]^T$ and $\psi(S(t)) = [S(t) \int S(t)]^T$.

Hence, the global control law U can be expressed as:

$$U = \frac{1}{g_1(x)} \left[\frac{k_p}{k_d} C_e \dot{e}_1 + \frac{k_i}{k_d} C_e e_1 - f_1(x) + \dot{x}_{2d} + U_{PI} \right]$$
(23)

The adjustable parameters vector is calculated by the following dynamic equation :

$$\hat{\theta} = \gamma_k S \psi(S(t)) \tag{24}$$

where γ_k is a positive constant.

2) Stability analysis: The approximation error W_{PI} is defined as

$$W_{PI} = \eta sign(S) - \theta^T \psi(S(t))$$
(25)

We note that $||W_{PI}|| \leq W_{PI_{max}}$.

By replacing the control law U by its expression (14), the time derivative of S can be rewritten as :

$$\dot{S} = -\frac{k_d}{C_e} U_{PI} \tag{26}$$

The Lyapunov candidate function is chosen as:

$$V = \frac{1}{2}S^2 + \frac{1}{2\delta_k}\tilde{\theta}^T\tilde{\theta}$$
(27)

where $\tilde{\theta} = \theta - \hat{\theta}$.

The time derivative of the lyapunov function is:

$$\dot{V} = S\dot{S} + \frac{1}{\delta_k}\tilde{\theta}^T\dot{\tilde{\theta}}$$
(28)

Replacing the time derivative of the sliding surface given by (26) and adding (25) in the derivative of V, it results :

$$\dot{V} = S \frac{k_d}{C_e} \left[-U_{PI} + W_{PI} - \eta sign(S) + \theta^T \psi(S(t)) \right] + \frac{1}{\delta_k} \tilde{\theta}^T \dot{\tilde{\theta}} = S \frac{k_d}{C_e} \left[-\hat{\theta}^T \psi(S(t) + W_{PI} - \eta sign(S) \right] + \theta^T \psi(S(t)) + \frac{1}{\delta_k} \tilde{\theta}^T \dot{\tilde{\theta}} = S \frac{k_d}{C_e} \left[\tilde{\theta}^T \psi(S(t) + W_{PI} - \eta sign(S)) \right] + \frac{1}{\delta_k} \tilde{\theta}^T \dot{\tilde{\theta}}$$
(29)

Baring in mind that $\hat{\theta} = -\hat{\theta}$, (29) can be rewritten as

$$\dot{V} = S \frac{k_d}{C_e} \Big[\tilde{\theta}^T \psi(S(t) + W_{PI} - \eta sign(S) \Big] - \frac{1}{\delta_k} \tilde{\theta}^T \dot{\theta} = \tilde{\theta}^T \frac{k_d}{C_e} (S \psi(S(t) - \frac{1}{\delta_k} \dot{\theta}) - \eta \frac{k_d}{C_e} S sign(S) + S \frac{k_d}{C_e} W_{PI}$$
(30)

By substituting (24) in (30), we get

$$\dot{V} = -\eta \frac{k_d}{C_e} Ssign(S) + S \frac{k_d}{C_e} W_{PI}$$

$$\dot{V} \leq -\eta |S| \frac{k_d}{C_e} + |S| \frac{k_d}{C_e} W_{PI_{max}}$$

$$\dot{V} \leq |S| \frac{k_d}{C_e} (W_{PI_{max}} - \eta)$$
(31)

Finally, we obtain $\dot{V} < 0 \forall \eta > W_{PI_{max}}$

Applying Barbalat's lemma, the sliding surface converges asymptotically to zero in finite time.

IV. SIMULATION RESULTS

The PV array contains 36 cells connected in series. The specifications of the PV panel are stated in Table. I. The boost converter operates with L = 10mH and $C = 470\mu F$. The switching frequency of the converter is set to $f_{sw} = 20$ kHz. The frequency of the searching algorithm is also set as 20 kHz.

TABLE I PV SPECIFICATION

Parameters	Value
Saturation current at T_r (I_{rr})	$5.981 \times 10^{-8} A$
Short circuit current at reference condition (I_{scr})	3.81 (A)
Reference Temperature (T_r)	298 (K)
Ideality Factor (A)	1.2
Charge of an electron (q)	$1.6 \times 10^{-19} (C)$
Temperature coefficient (k_i)	0.0024
Boltzman's constant (k_h)	1.3806×10^{-23}
Maximum Photovoltaic Power (P_{mpp})	60.27 (W)
Maximum Photovoltaic Voltage (V_{mpp})	16.85 (V)
Maximum Photovoltaic current (I_{mpp})	3.57 (A)

In the following, two scenarios including standards conditions and varying temperature and irradiation are simulated to verify the proposed scheme.

A. Standards conditions: $T = 25^{\circ}C$ and $Ir = 1000 W/m^2$

PV voltage V_{pv} is provided in Fig. 6 along with PV power P_{pv} is shown in Fig. 7.

The system response is shown in Fig. 6(a) with CSMC and ASMC in Fig. 6(b). With ASMC, the PV system shows a fast response and a good tracking performance. In fact, the tracking errors based on MAE (32) and MSE (33) given in Table II, are minimum for ASMC. Furthermore, PV voltage converges to the desired voltage within 0.01 sec. However, by using CSMC, the time convergence is about 0.02 sec. ASMC also presents less oscillation comparing to CSMC.

PV power is also maintained at its optimum after 0.009 sec for ASMC in Fig. 7(b) and 0.015 sec for CSMC in Fig. 7(a).

TABLE II Comparative study of SMC and ASMC

	MAE	MSE	Time of convergence
CSMC	0.3127	1.3764	0.02 sec
ASMC	0.1771	1.1179	0.01 sec



$$MSE = \frac{1}{T} \int_{0}^{T} e^2(t) dt \tag{33}$$



(b) Adaptive SMC

Fig. 6. PV voltage (V)





(b) Adaptive SMC

Fig. 7. PV power P_{pv} (W)

B. Real data analysis

In this simulation, we take real data measured for one day (16/11/2016) in the region of Sfax in Tunisia. The data is varied each 3 hours. Irradiation and temperature profiles are given in Fig. 8.

The PV power is given in Fig. 9. Under the simultaneous variation of temperature and irradiation, as it shown in Fig. 9(b), ASMC tracks perfectly the maximum power. However, CSMC tracks the maximum power but with oscillations around it as it given by Fig. 9(a).

V. CONCLUSIONS

In this paper, sliding mode controller based MPPT algorithm has been introduced for the maximum power tracking of PV systems. By combining the ASMC controller and the incremental conductance method, the MPP is successfully achieved even considering rapidly changing atmosphere. Via simulations, the better performance has been obtained compared to CSMC. Furthermore, the ASMC-based MPPT control method assures better tracking performance and high robustness.

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(a) Solar irradiance Ir (W/m^2)



Fig. 8. Solar irradiance and temperature taken for one day



(a) Classical SMC



(b) Adaptive SMC

Fig. 9. PV power $P_{pv}(W)$