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Forecasting sovereign CDS volatility: A comparison of univariate GARCH-class models

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Abstract

Initially overlooked by investors, the sovereign credit risk has been reassessed upwards since the 2000's which has contributed to awaken the interest of speculators in sovereign CDS. The growing need of accurate forecasting models has led us to fill the gap in the literature by studying the predictability of sovereign CDS volatility, using both linear and non-linear GARCH-class models. This paper uses data from 38 worldwide countries, ranging from January 2006 to March 2017. Results show that the CDS markets are subject to periods of volatility clustering, nonlinearity, asymmetric leverage effects and long-memory behavior. Using 7 heteroskedastic and no heteroskedastic-robust statistic criteria, results show that the fractionally-integrated models outperform the basic GARCH-class models in terms of forecasting ability and that allowing flexibility regarding the persistence degree of variance shocks significantly improves the model's suitability to data. Despite the divergence in the economic status and geographical positions of the countries composing our sample, the FIGARCH and FIEGARCH models are mainly found to be the most accurate models in predicting credit market volatility.

JEL Classification: G15, G17, C58.

TEL Classification: G15, G17, C56.

Keywords: CDS volatility, Predictability, Forecasting models, Loss functions criteria.

1 Introduction

Understanding the fluctuations' dynamic of financial assets has always been of a particular interest in the academic and non-academic spheres. The considerable number of studies focusing on the stock prices' mechanism point out several stylized facts characterizing the financial markets such as: the volatility clustering, the non-stationarity... (See for example Niu and Wang (2013) for a study of the statistical behaviors of the Shanghai Composite Index and Hang Seng Index). Besides the stock markets widely studied, analyzing the characteristics of the credit market, and particularly the sovereign CDS market, is likewise interesting especially when it comes to investigating the impact of financial properties on the suitability of the CDS volatility modeling and forecasting ability.

The curious increase in the empirical studies dealing with modeling CDS data during the last decade can be explained by several reasons: (i) the constantly evolving outstanding amount of the CDS contracts reaching its highest values during the crisis periods, (ii) the need of more clear understanding of the role played by this market in the spread of crises and (iii) and the requirement of identifying the main explaining factors of credit risk. Furthermore, the use of CDS contracts no more as hedging instruments but rather as diversification, trading and speculation instruments has legitimized the usefulness of CDS volatility forecasting to investors for both risk management and portfolio management.

Despite the relevance of the volatility forecasts particularly in the decision process and considering the grown interest in predicting credit spreads, the nonexistence of papers in the literature of CDS spreads dealing with the ability of GARCH models to accurately forecast the volatility of the CDS is completely outrageous^[1]. The literature on CDS is mainly composed by studies that focus on the determinants of these credit spreads (Oliveira et al., 2012; Costantini et al., 2014; Fontana and Scheicher, 2016) or the Granger Causal relationship between CDS markets and related markets Coudert et al. (2010); Longstaff et al. (2011); Coudert and Gex (2013); Sabkha et al. (2017). The very few papers that investigate the forecasts of CDS spreads (Krishnan et al., 2010; Sharma and Thuraisamy, 2013; Avino and Nneji, 2014; Srivastava et al., 2016) only focus on the first moment order, while the predictability of the CDS volatility remains understudied. Yet, these studies try to forecast the CDS spreads based on the commonly known economic and financial determinants and not based on the predictive ability of the econometric models. Considering the foregoing gaps, this study aims to extent the literature by investigating the forecasting performance of 9 GARCH-class models in the sovereign CDS markets from January 2^{nd} , 2006 to March 31^{st} , 2017.

Our study contributes to the existing literature in several ways: first, as far a we are concerned, none of the previous studies has focused on the predictability of CDS volatility, especially when it comes to the sovereign market. Second, our paper contributes as well to the literature by implementing a larger set of statistical loss function criteria -taking into account the nonzero mean and the heteroscedasticity of the forecast errors - to assess the out-of-sample predictive ability of the models in comparison with existing forecasting papers on financial assets. Third, the comparative study between linear and non-linear ARCH-class

^[1]The majority of papers dealing with the predictive power of GARCH models, only focus on the major stock indexes and exchange rates (Poon, 2005)

models provides a better and clearer comprehension of the in-sample and out-of-sample fit of the CDS data. Finally, our data set allows us to draw more robust and worldwide conclusions, as it is composed by CDS spreads for 38 countries from all over the world covering the recent two economic and financial crises when the volatility of asset prices have reached their highest unexpected levels.

Our empirical findings show that the sovereign CDS market is characterized by the same stylized facts as the stock market: volatility clustering, leverage effects and long memory behavior. The results of the diagnostic tests on the in-sample modeling generally show that no model outperforms all the others in terms of fitting. Based on the results the 7 loss functions, the predictive performance of the fractionally-integrated models seems to be more accurate, emphasizing the importance of taking into account the long-range memory and the nonlinear behavior of CDS spreads while forecasting volatility. Among the fractionally-integrated models, our results show that the FIGARCH and the FIEGARCH are the most accurate models, providing the best out-of-sample performances in most cases.

The rest of the paper is organized as follows. A brief literature review of the previous studies predicting financial assets is section 2. Section 3 presents the sample and data used to compare the predictive ability of the models and displays the 9 volatility forecasting models studied. Results of the in-sample and out-of-sample analysis are reported is Section 4. Section 5 concludes the paper.

2 Literature review

Investigating the degree to which financial time series can be accurately forecast has always been in the limelight of researchers' issues. The empirical literature on the modeling and predicting volatility processes is extensive and takes into account more and more financial markets properties. Engle (1982) is the first researcher to model financial data through a time-varying stochastic process characterized by a nonconstant correlated variance so-called ARCH model. A generalization of this Autoregressive Conditional Heteroscedaticity model is then proposed by Bollerslev (1986) with more parsimonious and less overparametrization and biasedness in the estimates. Some extensions of this model are afterwards proposed, taking into account more stylized facts of the financial markets: leverage effects (Nelson, 1991; Glosten et al., 1993), stationarity issues (Engle and Bollerslev, 1986), long memory Ding et al. (1993); Baillie et al. (1996); Bollerslev and Mikkelsen (1996); Tse (1998); Davidson (2004)....^[2].

These GARCH-class volatility models have been widely used to forecast various financial data, based on their predictive power. The great focus in these studies has been primarily given to stock returns (Keim and Stambaugh, 1986; Poon, 2005; Guidolin et al., 2009; Ferreira and Santa-Clara, 2011; Niu and Wang, 2013), in which recent past information is found to help forecast the future variance. Similar studies are conducted using commodity market data, especially oil data (Agnolucci, 2009; Wei et al., 2010; Chkili et al., 2014; Charles and Darné, 2017). Generally, these studies show no model outperforms all the others in capturing the time series financial and statistical features, while the non-linear GARCH-class models

^[2] For an exhaustive survey of the proposed ARCH-class models, see Poon (2005)

are found to be more relevant in terms of forecasting accuracy^[3].

Unlike stock markets, exchange rates and oil market data, not many studies have been conducted to assess the predictive performance of the volatility GARCH-type models using CDS data. Despite Krishnan et al. (2010), Sharma and Thuraisamy (2013), Avino and Nneji (2014) and Srivastava et al. (2016) whose aim is to predict the future changes in the CDS spreads based on some macroeconomic and marketwide variables, the literature on CDS spreads focuses generally on the key drivers and determinants of these credit spreads (Oliveira et al., 2012; Costantini et al., 2014; Fontana and Scheicher, 2016) or rather on the interaction and comovement between CDS markets and the other related financial markets (Coudert et al., 2010; Longstaff et al., 2011; Coudert and Gex, 2013; Sabkha et al., 2017).

Among the first authors who are interested in the prediction of credit spreads, Krishnan et al. (2010) construct credit-spread curves, based on several macroeconomic and firm-specific variables, for 241 highly and lowly credit-risky firms from 1990 to 2005. Results show that only the information contained in the riskless yield curve significantly improve the out-ofsample forecasts. Focusing more precisely on the CDS as proxy for the credit risk level, Sharma and Thuraisamy (2013) investigates the forecastability of the CDS spreads of 8 Asian sovereign from 2005 to 2012. In-sample and out-of-sample evidences reveal that the oil price uncertainty provides valuable information for predicting the future fluctuations in the sovereign CDS spreads. Avino and Nneji (2014) use some economic and financial factors to investigate whether the iTraxx index spreads are forecastle. Based on the results of the predictive ability of some linear (Structural OLS model and AR(1)) and non-linear (Markov-switching) models, these authors show that the daily changes in the CDS index can be predictable from the yield curve, the equity returns and the changes in the VSTOXX volatility index. Using an error correction model before, during and after the subprime crisis, Srivastava et al. (2016) show that the VIX predicts the future changes in 98% of the studied sovereign CDS markets.

These few studies on the forecastability of CDS spreads rely on the information contained in the theoretical determinants - widely used in the empirical literature - and its ability to predict future fluctuations in the CDS market. Yet, he accuracy of these CDS predictions is assessed through some loss functions criteria that are subject to nonzero mean noise and serial correlation (such as RMSE, MAE...). Furthermore, the data studied so far only cover the period of the subrpime crisis and end before or right after the outbreak of the Sovereign debt crisis, which is quite a weak point given that all the unexpected changes in the market behavior are not taken into account in their forecasting models. Finally, the most important shortcoming of the aforementioned studies, is that they focus on the first moment order neglect the Variance in forecasting the CDS spreads.

3 Data and methodology

This section introduces one of our paper contributions: the sample under study, composed by countries around the world, allowing us to provide international evidences and data time

^[3] For a complete theoretical and empirical survey on the use of univariate ARCH processes in financial studies, see Bollerslev et al. (1992).

line covering the both recent two financial and economic crises. Volatility forecasting models are as well presented in this section.

3.1 Sample and data description

Our study focuses on a sample composed by 38 worldwide countries belonging to five different geographical areas: Eastern and Western Europe, North and South America and Asia. Besides the developed countries and the emerging countries, the sample under study in this paper includes some Newly Industrialized Countries (such as Brazil, Mexico, Philippines and Thailand...) and some low economic growth countries with the highest credit risk levels (such as Portugal, Ireland, Greece and Spain...). The sample details with the economic and geographical status of each country are given in Table 1.

The dataset used is composed by daily 5-year sovereign CDS spreads, denominated in US dollars and collected from Thomson Reuters®. The extracted series cover a period spanning from January 2006 to March 2017, during which the world financial and credit markets have been affected by two major crises, namely the Global Financial Crisis and the Sovereign Debt Crisis. Thus, modeling, forecasting the CDS volatility and comparing models performances are particularly interesting during this period during which we observed some unexpected fluctuations on the credit market.

3.2 Marginal volatility processes: univariate ARCH-type models

The financial markets are generally characterized by periods of volatility clustering, during which the assets' second moment order remains high before regaining its normal levels. Engle (1982) proposes an Autoregressive Conditional Heteroscedasticity (ARCH) model able to capture such financial phenomenon. This volatility persistence is as well observed in the Credit Default Swap market and the use of ARCH-class models to model the variance of the CDS spreads is thus legitimate. As an extension of the ARCH model, Bollerslev (1986) proposes a generalized high-order ARCH process that is more parsimonious and allows for less overparametrization and biasedness in the estimates. This GARCH model is given by:

$$x_{i,t} = \mu_{i,t} + u_{i,t} \quad / \quad u_{i,t} = \sigma_{i,t} \varepsilon_{i,t}, \quad \varepsilon_{i,t} | \mathcal{P}_{t-1} \leadsto \mathcal{N}(0,1);$$

$$\sigma_{i,t}^2 = V(x_{i,t} | \mathcal{F}_{t-1}) = \alpha_{i,0} + \sum_{k=1}^{q_i} \alpha_{i,k} a_{i,t-1}^2 + \sum_{h=1}^{p_i} \beta_{i,h} \sigma_{i,t-1}^2. \tag{1}$$

with $x_{i,t}$ is a financial time series, i is a given country from the sample and $\mu_{i,t}$ and $\sigma_{i,t}$ are respectively conditional mean and conditional volatility. To satisfy the positive-definite condition, some restrictions are imposed: $p \geq 0$, $q \geq 0$, $\alpha_{i,k} \geq 0$ for $k = 1, \ldots, q_i$, $\beta_{i,h} \geq 0$ and $\alpha_{i,0} \geq 0$ for $h = 1, \ldots, p_i$.

For sake of simplicity and suitability, only models with process orders $(p_i \text{ and } q_i)$ equal to 1 are estimated. In fact, the simplest GARCH(1,1) specification is the most useful and fitted for financial time series (Bollerslev, 1986; Wei et al., 2010).

The GARCH(1,1) process, as proposed by Bollerslev (1986) is given by the following formula:

$$\sigma_{i,t}^2 = \alpha_{i,0} + \alpha_{i,1} + \alpha_{i,1} a_{i,t-1}^2 + \beta_{i,1} \sigma_{i,t-1}^2.$$
 (2)

Table 1: Sample and countries classification into economic categories and geographical positions

Country	Geographical position	Country	Geographical position
$\overline{}$	ped countries (20)	Newly in	ndustrialized countries (6)
Austria	Western Europe	Brazil	South America
Belgium	Western Europe	China	Asia
Denmark	Western Europe	Mexico	North America
Finland	Western Europe	Thailand	Asia
France	Western Europe	Turkey	Asia
Germany	Western Europe	Em	$erging \ countries \ (11)$
Ireland	Western Europe	Bulgaria	Eastern Europe
Italy	Western Europe	Croatia	Eastern Europe
Japan	Asia	Czech	Eastern Europe
Latvia	Eastern Europe	Hungary	Western Europe
Lithuania	Eastern Europe	Greece	Western Europe
Netherlands	Western Europe	Indonesia	Asia
Norway	Western Europe	Poland	Eastern Europe
Portugal	Western Europe	Romania	Eastern Europe
Slovakia	Eastern Europe	Russia	Asia
Slovenia	Eastern Europe	Ukraine	Eastern Europe
Spain	Western Europe	Venezuela	South America
Sweden	Western Europe		
UK	Western Europe		
USA	North America		

The countries' economic classification is made according to the NU, the CIA World Factbook, he IMF and the World Bank criteria,

in order to have a sample with a sufficient number of countries in each category.

Furthermore to the previous model restrictions, $\alpha_{i,1}$ and $\beta_{i,1}$ parameters must satisfy the condition of $\alpha_{i,1} + \beta_{i,1} < 1$ to comply with the stationarity in the broad sense.

A more restrictive version of the GARCH(1,1) is proposed by Engle and Bollerslev (1986) where the equivalent of the unit root in the mean is included in the variance so we can handle for the stationarity of the variance. The Integrated GARCH(1,1) takes into account the persistence of conditional volatilities^[4]. The main difference with the GARCH(1,1) is that the IGARCH requires the parameters α_1 and β_1 to respect the equality of $\alpha_1 + \beta_1 = 1$. Thus, the IGARCH(1,1)^[5] can be written as follows:

$$\sigma_{i,t}^2 = \alpha_{i,1} a_{t-1}^2 + (1 - \alpha_{i,1}) \sigma_{i,t-1}^2. \tag{3}$$

Besides the aforementioned linear models, there exist some nonlinear GARCH-class of models taking into account the other financial markets properties. The Exponential GARCH,

^[4]Today's shocks on a financial asset (future contracts for example) have a significant impact on the conditional volatility several periods in the future.

^[5] The IGARCH(1,1) is equivalent to the Exponentially Weighted Moving Average(EWMA) model developed by Morgan (1996).

as proposed by Nelson (1991), is one of these models that accounts for the leverage effect and the asymmetry of the error distribution. While the nonnegativity of linear GARCH model is ensured by several parameters restrictions, the EGARCH model proposes another formulation allowing for a positive volatility without any restrictive constraints. The EGARCH(1,1) is expressed as follows:

$$ln(\sigma_{i,t}^2) = \alpha_{i,0} + \alpha_{i,1-1}ln(\sigma_{i,t}^2) + \beta_{i,1}g(\varepsilon_{i,t-1}),$$
where $g(\varepsilon_{i,t}) = \theta_i \varepsilon_{i,t} + \gamma_i [|\varepsilon_{i,t}| - E(|\varepsilon_{i,t}|)].$ (4)

The asymmetric relation between assets' fluctuation and volatility changes is depicted by the θ_i and γ_i representing respectively the sign and the magnitude of $\varepsilon_{i,t}$.

Glosten et al. (1993) propose a model that allows the sign and the amplitude of the innovations (ε_t) to affect the conditional volatility separately. The asymmetric leverage effect^[6] is represented in the following formulation of the GJR-GARCH(1,1)^[7] model:

$$\sigma_{i,t}^2 = \alpha_{i,0} + \alpha_{i,1} a_{i,t-1}^2 + \gamma_i I_{i,t-1} a_{i,t-1}^2 + \beta_{i,1} \sigma_{i,t-1}^2, \tag{5}$$

with I_t is a dummy variable equals to 0 when a_t is positive and 1 otherwise.

The first model accounting for the long-range persistence of financial assets variance is developed by Ding et al. (1993). This asymmetric power ARCH model allows the volatility to be long-memory^[8]. The APARCH(1,1) model is:

$$\sigma_{i,t}^2 = \alpha_{i,0} + \alpha_{i,1} (|a_{i,t-1}| - \gamma_i a_{i,t-1})^{\delta} + \beta_{i,1} \sigma_{i,t-1}^{\delta}.$$
(6)

where δ depicts the Box-Cox power transformation of the conditional volatility (σ_t) and satisfies the condition of $\delta \geq 0$.

A more flexible class of GARCH models is proposed by Baillie et al. (1996) who introduce a new feature of the unit root for the variance. In fact, the fractionally integrated GARCH model (FIGARCH) highlights the fact that - unlike stationary processes where the persistence of volatility shocks is finite - in unit root processes, the impact of lagged errors occurs at a slow hyperbolic rate of decay. The FIGARCH model allows, thus, to capture the long memory in financial volatility with a complete flexibility regarding the persistence degree. In fact, the FIGARCH(1,d,1) formulation depends on fractional integration parameter (d) as follows:

$$\sigma_{i,t}^2 = \alpha_{i,0} + [1 - (1 - \beta_i(L))^{-1} (1 - \phi(L))(1 - L)^d] a_{i,t}^2 + \beta_i \sigma_{i,t-1}^2.$$
 (7)

with 0 < d < 1. When d=1, the FIGARCH(1,d,1) is equivalent to an IGARCH(1,1) where the persistence of conditional variance is supposed to be complete, while when d=0, it is rather equivalent to a GARCH(1,1) and no volatility persistence is taken into consideration. L is the lag operator and $(1 - L)^d$ is the financial fractional differencing operator.

^[6]Positive and negative financial shocks revamp asymmetrically the variance. Furthermore, bad news (shocks) generate greater volatility than good news.

^[7] The volatility's different reactions to signs and sizes of past innovations are also suggested in the Threshold Heteroskedastic model (TGARCH) of Zakoian (1994). The major difference is that in the TGARCH model the conditional standard deviation (σ_t) is considered rather than the conditional variance (σ_t^2).

^[8] The autocorrelation function of time series returns decreases gradually.

Other ARCH formulations are extended to the fractionally integrated GARCH, including asymmetric leverage effect presented in the EGARCH model. Bollerslev and Mikkelsen (1996) propose a new class of model combining characteristics of the FIGARCH and the EGARCH models so-called FIEGARCH(p,d,q). Financial assets' volatilities are, thus, better explained and depicted by a mean-reverting fractionally integrated process. The FIEGARCH(1,d,1) model is written as follows:

$$ln(\sigma_{i,t}^2) = \alpha_{i,0} + \phi(L)^{-1} (1 - L)^{-d} [1 + \psi(L)] g(\varepsilon_{i,t-1}).$$
(8)

where $\phi(L)$ and $\psi(L)$ are lag polynomials, and - as in the EGARCH(1,1)^[9] - $g(\varepsilon_t)$ is a quantization function of information flows such as:

$$g(\varepsilon_{i,t}) = \theta_i \varepsilon_{i,t} + \gamma_i [\mid \varepsilon_{i,t} \mid -E(\mid \varepsilon_{i,t} \mid)].$$

An extension of the conventional fractionally integrated GARCH model is proposed by Tse (1998) so-called FIAPARCH(1,d,1). The new approach combines the long-range dependencies feature and the asymmetric impact of lagged positive and negative shocks on future volatilities in one fractionally integrated model. The FIAPARCH(1,d,1) is written as follows:

$$\sigma_{i,t}^{\delta} = \alpha_{i,0} (1 - \beta_i)^{-1} + [1 - (1 - \beta_i(L))^{-1} \phi(L) (1 - L)^d] (|a_{i,t}| - \gamma_i a_{i,t})^{\delta}.$$
 (9)

More recently, another linear GARCH model, called hyperbolic GARCH (HYGARCH) is proposed by Davidson (2004) who argues that the impact of lagged errors on the conditional variance discloses near-epoch dependence feature. The main contribution of this model is that the fractional integration parameter is negative (-d) instead of positive and that d increases rather when it approaches zero^[10]. The statistical properties included in the HYGARCH make it the most successful and used approach by financial practitioners in modeling time series volatilities. The HYGARCH(1,d,1) is defined under the following formulation:

$$\sigma_{i,t}^2 = \alpha_{i,0} + \left[1 - (1 - \beta_i(L))^{-1} (1 - \phi(L)) \left[1 + \alpha_i ((1 - L)^d - 1)\right]\right] a_{i,t}^2.$$
(10)

The volatility estimation of the CDS log returns of the 38 countries is computed for 9 GARCH-class models taking into account, each time, different financial stylized facts such as long-run properties in the conditional mean and volatility clustering and long-memory behavior in the conditional variance. The BFGS-BOUNDS method (Broyden, 1970) is used to optimize the likelihood function rather than the conventional numerical optimization, in order to respect the parameters constraints, notably the stationary and the nonnegativity constraints.

In addition to the widely used Box-Pierce tests and the LM ARCH effects test, several other diagnostic tests are reported here, namely the Nyblom test, the adjusted Pearson goodness-of-fit test and the Residual-Based Diagnostic (as suggested by Fantazzini (2011)). The Joint Nyblom (Nyblom, 1989) is a stability test under the null hypothesis of parameters joint constancy over time against the alternative of parameters shift at an undefined

^[9]When the memory parameter, d=0, the FIEGARCH formulation is equivalent to the conventional EGARCH(1,1) (FIEGARCH(1,0,1) \simeq EGARCH(1,1)).

^[10] When d of the HYGARCH is positive, it is considered as a unit root process.

breakpoint. According to Palm and Vlaar (1997), The adjusted Pearson goodness-of-fit test verifies whether the residuals' empirical distribution matches or not the theoretical distribution (namely Gauss, Student or G.E.D depending on the country). The Residuals-Based Diagnostic test (Tse, 2002) checks for conditional Heteroscedasticity, by complementing and filling the gaps of the Box-Pierce Q statistics.

3.3 Loss functions criteria

Following Wei et al. (2010), the forecasting process of the CDS volatility is implemented as follows: the 38 CDS times series' timeline is divided into two subperiods: the in-sample volatility estimation is conducted from January 2^{nd} , 2006 to March 31^{st} , 2014 (2152 observations), and the out-of-sample model forecasts concerns the last three years, i.e. from April 1^{st} , 2014 to March 31^{st} , 2017 (783 observations). The twenty-day out-of-sample forecasting are used to assess and compare the predictive performance of the 9 studied models.

The comparison of the volatility models' forecasting ability is not straightforward. Several measures of the predictive ability are suggested in the literature based on some loss functions. According to Poon (2005), Wei et al. (2010) and Pilbeam and Langeland (2015), we can not conclude with certainty the superiority of one model over another in terms of forecasting performance, based solely on the result of a single error statistic since each criterion may be more and less relevant from one case to another^[11]. That's why the conclusions made in this study are based on the results of rich set composed by the 7 most popular and relevant ones, including:

• The Mean Square Error (MSE):

$$MSE = \frac{1}{N} \sum_{t=1}^{N} (\hat{\sigma}_t - \sigma_t)^2,$$
 (11)

• The Mean Absolute Error (MAE):

$$MAE = \frac{1}{N} \mid \hat{\sigma}_t - \sigma_t \mid, \tag{12}$$

• The Heteroscedatiscity-adjusted Mean Square Error (HMSE). As suggested by Boller-slev and Ghysels (1996), the HMSE is calculated as follows:

$$HMSE = \frac{1}{N} \sum_{t=1}^{N} \left(\frac{\sigma_t}{\hat{\sigma}_t} - 1 \right)^2, \tag{13}$$

• The Heteroscedatiscity-adjusted Mean Absolute Error (HMAE). Andersen et al. (1999) proposes a loss function that better accommodates the heteroskedasticity in the forecast bias . The HMAE is calculated as follows:

$$HMAE = \frac{1}{N} \sum_{t=1}^{N} \left| \frac{\sigma_t}{\hat{\sigma}_t} - 1 \right|, \tag{14}$$

^[11] Diebold and Mariano (2002) argue that allowing for forecast errors to be non-Gaussian, nonzero mean and autocorrelated produces better tests' results.

• The QLIKE loss function (QLIKE). This is a test of forecast bias implied by a Gaussian likelihood (see Wei et al. (2010) for a further details.)

$$QLIKE = \frac{1}{N} \sum_{t=1}^{N} \left(LN(\hat{\sigma}_t) + \frac{\sigma_t}{\hat{\sigma}_t} \right), \tag{15}$$

• The R²LOG loss function (R²LOG): This loss function assess the goodness-of-fit of the out-of-sample forecasts based on the regressions of Mincer and Zarnowitz (1969)

$$R^{2}LOG = \frac{1}{N} \sum_{t=1}^{N} \left(LN(\frac{\sigma_{t}}{\hat{\sigma}_{t}}) \right)^{2}, \tag{16}$$

• The Mean Logarithm of Absolute Errors (MLAE): As proposed Pagan and Schwert (1990), the MLAE criterion is written as follows:

$$MLAE = \frac{1}{N} \sum_{t=1}^{N} LN \mid \hat{\sigma_t} - \sigma_t \mid .$$
 (17)

With N is the number of predicted data and $\hat{\sigma}_t$ is the volatility forecasts. The latent daily CDS spreads volatility σ_t is not observed and is thus proxied by the squared daily logarithmic returns^[12]. Previous studies (Lopez, 2001; Poon, 2005) report that the use of such a proxy produces unbiased estimates, even though it remains questionable (noisy estimator because of its asymmetric distribution).

4 Empirical results

This section presents the summary statistics for the 38 studied time series. The modeling, estimation and testing of the forecasting ability of the 9 GARCH-class models are presented, as well, in this section.

4.1 Descriptive statistics

Descriptive statistics, displayed in Table 2, show that the studied countries present dissimilar credit risk levels with CDS spreads ranging from 1 bp to 37081.41 bp. The average daily spreads highlights, as well, this divergence in sovereign financing conditions with the largest value recorded, as expected, in Greece (9508.85 bp) and the smallest value recorded in the USA (24.01 bp). The high levels of standard deviations reveal, on the other side, that the worldwide financial and economic troubles impacted the public finances of the countries under study, doubtlessly with different magnitudes. The least volatile CDS market is Germany (24.50). According to the Augmented Dickey-Fuller test (Dickey and Fuller, 1981), all the time series present a unit root, implying that the CDS spreads of the 38 countries are non-stationary at 5% statistical level at least.

^[12] More methods exist in the literature to proxy the volatility of financial assets, such as, the high-low measure and the realized volatility estimate. For a complete survey of these methods, see Poon (2005).

Table 2: Descriptive statistics and ARCH effect tests for the CDS time series

			CD	S spreads						C	DS log	g returns			
	Obs.	Min	Mean	Max	Std.	AD.	F	ARCH	-LM	ARCH	-LM	ARCH	-LM	GPF	I
					Dev	statis	tics	(2))	(5)	(10))		
Austria	2936	1.40	36.13	132.77	24.96	-2.45		249.75	***	127.05	***	72.58	***	0.29	***
Belgium	2936	2.05	72.39	398.78	74.62	-1.67		508.94	***	237.99	***	120.84	***	0.18	***
Brazil	2936	61.50	178.55	606.31	94.86	-2.46		25.01	***	43.70	***	37.71	***	0.11	***
Bulgaria	2936	13.22	180.37	692.65	121.88	-2.25		12.71	***	10.36	***	6.72	***	0.08	***
China	2936	10.00	82.44	276.30	43.56	-2.82	*	120.85	***	63.09	***	39.00	***	0.22	***
Croatia	2936	24.88	244.20	592.50	128.47	-2.15		137.90	***	58.87	***	47.62	***	0.26	***
Czech	2936	3.41	66.89	350.00	49.54	-2.62	*	62.52	***	46.01	***	29.50	***	0.14	***
Denmark	2936	11.25	36.65	157.46	32.94	-2.17		87.27	***	41.66	***	24.36	***	0.21	***
Finland	2936	2.69	26.85	94.00	19.24	-2.33		13.79	***	7.98	***	4.43	***	0.05	***
France	2936	1.50	54.30	245.27	50.56	-1.71		276.95	***	120.56	***	62.86	***	0.20	***
Germany	2936	1.40	28.77	118.38	24.50	-2.05		252.46	***	128.31	***	73.27	***	0.29	***
Greece	2936	5.20	9508.85	37081.41	15351.1	-1.46		5.E-04		4.E-04		6.E-04		-4.E-04	
Hungary	2936	17.34	225.98	729.89	153.05	-2.18		14.48	***	15.20	***	8.67	***	0.10	***
Indonesia	2936	118.09	219.29	1240.00	116.83	-2.63	*	139.82	***	105.31	***	61.49	***	0.23	***
Ireland	2936	1.75	188.89	1249.30	234.02	-1.36		218.63	***	103.01	***	63.33	***	0.18	***
Italy	2936	5.575	151.7504	586.7	127.38	-1.79		127.35	***	60.46	***	35.18	***	0.19	***
Japan	2936	2.13	49.26	152.64	33.28	-1.94		71.53	***	31.30	***	21.68	***	0.13	***
Latvia	2936	5.50	210.89	1176.30	216.13	-1.62		152.57	***	68.47	***	35.36	***	0.26	***
Lithuania	2936	6.00	169.21	850.00	154.01	-1.90		56.75	***	26.91	***	13.56	***	0.15	***
Mexico	2936	64.17	141.89	613.11	59.36	-3.03	*	356.35	***	160.17	***	127.50	***	0.39	***
Netherlands	2936	7.67	37.13	133.84	29.50	-2.00		10.79	***	4.33	***	5.59	***	0.05	***
Norway	2936	10.59	30.95	62.00	17.82	-1.68		3.22	***	2.46	***	2.06	***	0.05	**
Philippines	2936	78.30	188.72	840.00	101.70	-1.77		154.83	***	127.66	***	90.03	***	0.23	***
Poland	2936	7.67	101.35	421.00	73.12	-2.32		311.98	**	135.64	**	75.78	**	0.21	***
Portugal	2936	4.02	289.89	1600.98	323.68	-1.60		53.57	***	42.23	***	22.61	***	0.17	***
Qatar	2936	7.8	83.13518	390	53.89	-2.12		37.65	***	17.33	***	9.55	***	0.09	***
Romania	2936	17.00	204.20	767.70	144.17	-2.09		57.88	***	33.74	***	17.50	***	0.17	***
Russia	2936	36.88	209.09	1106.01	147.84	-2.95	*	258.09	***	117.58	***	65.50	***	0.29	***
Slovakia	2936	5.33	77.52	306.01	66.71	-2.03		25.14	***	24.62	***	19.31	***	0.11	***
Slovenia	2936	4.25	131.24	488.58	114.88	-1.65		13.23	***	9.82	***	34.88	***	0.11	***
Spain	2936	2.55	144.63	634.35	135.01	-1.56		195.02	***	78.80	***	39.98	***	0.19	**
Sweden	2936	1.63	27.17	159.00	25.70	-2.64	*	69.49	***	30.82	***	20.72	***	0.16	***
Thailand	2936	51.01	120.94	500.00	41.89	-3.64	*	81.52	***	120.36	***	96.33	***	0.17	***
Turkey	2936	109.82	217.65	835.01	72.41	-3.72	*	69.04	***	86.65	***	46.84	***	0.21	***
UK	2936	16.50	42.89	165.00	28.11	-2.07		27.33	***	21.12	***	23.19	***	0.11	***
Ukraine	2936	1.00	2173.76	15028.76	3969.27	-2.15		60.42	***	32.53	***	17.13	***	0.11	***
USA	2936	10.02	24.01	90.00	11.11	-3.58	*	94.96	***	46.67	***	24.57	***	0.11	***
Venezuela	2936	124.62	1771.08	10995.67	1869.79	-2.00		36.17	***	38.56	***	22.73	***	0.11	***
, chezacia	2000	124.02	1111.00	10000.01	2000.10	-2.00		00.11		00.00		22.10		0.11	

The table reports descriptive statistics for the daily sovereign CDS spreads of 38 countries. Min., Max. and Std. Dev. denote respectively to the minimum, the maximum and the standard deviation. The Augmented-Dickey Fuller (Individual intercept included in the test equation) is a unit root test that informs about the stationary of time-series with a null hypothesis of the presence of a unit root in the process. The Engle's ARCH-LM test with 2, 5 and 10 lag orders informs about the presence of ARCH effects in the series under the null hypothesis of no autocorrecations in the squared residuals. GPH is the log periodogram test of Geweke and Porter-Hudak (1983) with d-parameter (m=1467). This test is applied to the squared logarithmic returns (as proxy for unconditional volatility) to detect any long-range dependence under the null assumption of no long-memory behavior in the volatility process. *, ** and *** refer to the statistical significance at respectively 10%, 5% and 1% levels.

Focusing on the evolution of the CDS log returns (computed as $x_t = log(\frac{S_t}{S_{t-1}})$) over the studied period, as presented in Figure 1, some volatility clustering periods are detected. Results of the ARCH-LM test in Table 2 confirm that the data used clearly exhibit heteroscedastic properties and support the appropriate use of GARCH-class processes to model the conditional volatility. The GPH test (Geweke and Porter-Hudak, 1983) conducted on the squared CDS log returns rejects the null hypothesis of no long-memory behavior in the series' volatility process, suggesting the use of the fractionally-integrated models^[13]. Figure 2 reports the density estimation and show that the series, composing our international sample, exhibit dissimilar statistical behaviors as to their empirical distribution. The majority of the data returns distribution does not overlay the Gaussian reference, which indicates that the residuals should be allowed to follow a Gaussian, a student and a Generalized Error Distribution (G.E.D)^[14].

^[13] Another commonly used long-range test is the Gaussian semi-parametric (GSP) (Robinson, 1995). Results of the GSP are not reported here because they are similar to those of the GPH.

 $^{^{[14]}}$ Other statistical distribution should, as well, be taken into account in further studies, such as the Skewed t-student...

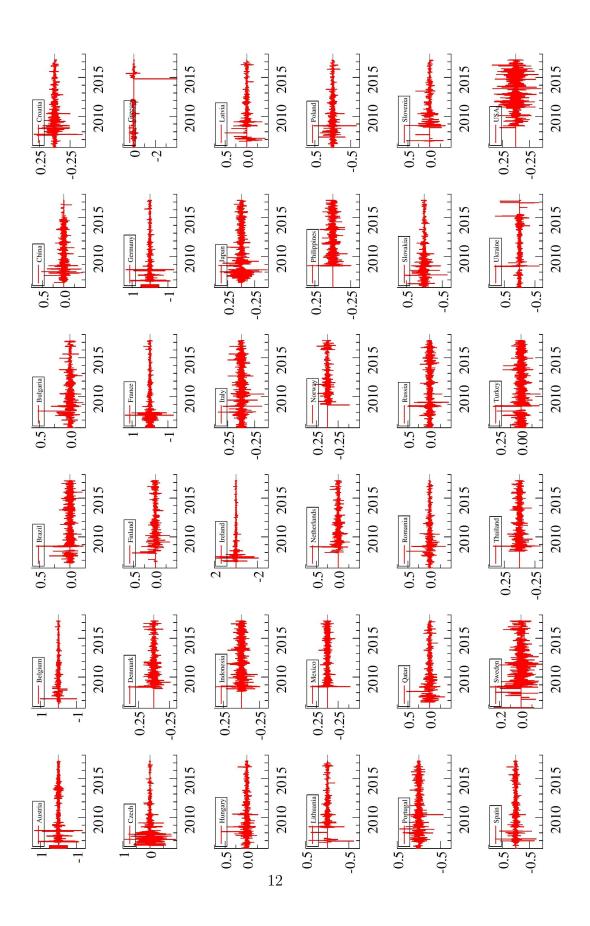


Figure 1: Daily CDS log returns for 38 worldwide countries

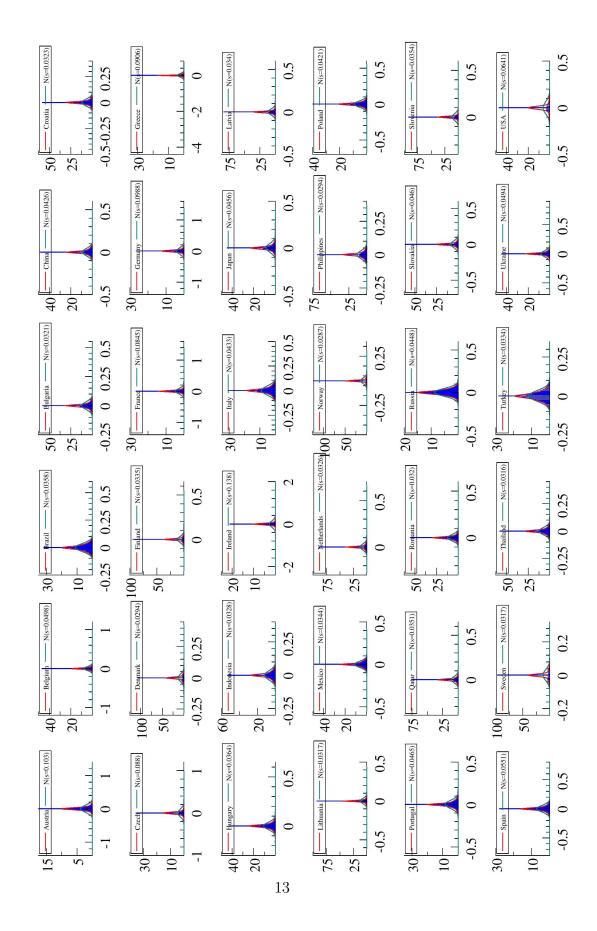


Figure 2: Daily CDS log returns for 38 worldwide countries

4.2 Models estimation and diagnostic tests

Results of the 9 GARCH-class model estimates are not reported here but are available upon request. Even though some models are difficult to optimize, no miss-convergences are recorded for any time series. However, at first sight, the major conclusion that could be drawn regarding the models estimation process is that taking into account several financial markets' stylized facts (long memory characteristic, shock persistence and asymmetric leverage effects...) does not necessarily improve the models performances since the more the model is over-parametrized, the more its computation and its convergence are complicated. In fact, different inconsistency and inaccuracy of the estimator parameters in some countries and for some model can result from the complexity of the model's statistical specifications. At the opposite, the models that great perform as to strong numerical convergence and computing-time delay are the GARCH, the IGARCH, FIGARCH and FIEGARCH.

Results of the univariate misspecification tests applied on the standardized residuals are presented in Table 5 (Appendix A). The Q portmanteau empirical statistics with 20 lags of both standardized residuals in levels and squared show that the null hypothesis of no serial correlation is accepted in most cases for all the studied models. The LM-ARCH test up to 10 lag orders shows, as well, that there is no heteroschasticity in the conditional variance equations of most of time series. The GARCH, IGARCH and FIGARCH models pass this in 100% of cases, whilst the least performant model, in terms of serial correlation, in the FIAPARCH with ARCH effects detected in 6 countries. Moreover, testing for conditional heteroscadticity through the Residual-Based Diagnostic (RDB) for conditional heteroscedasticity (Tse, 2002) gives better results, with absolutely no detected serial correlation in all series for the APARCH, IGARCH and FIGARCH. Based on the Nyblom test, proposed by Nyblom (1989), no possible shifts are detected and the 9 models parameters coefficients are found to be constant over time for all countries. One of the recommended steps in modeling financial data process is to evaluate the goodness of fit (D'Agostino, 2017). The fitting of our models are thus assessed, in this paper, through the adjusted Pearson goodness-of-fit test. Statistics indicate that mostly there is no difference between the empirical distribution of the residuals and the theoretical one. Interestingly, the basic GARCH model seems to have the highest number (12 over the 38 studied series) of unconformity and discrepancy of the data from the data from the hypothesized probability distribution.

In addition to the diagnostic tests, Table 5 displays the Akaike information criterion (AIC) for each model and country. Result do not allow us to unanimously select only one most appropriate model. AIC results of the studied models are mitigated across the 38 countries of the sample. By minimizing the AIC, the APARCH turns out to be the best fitted model for the CDS data of 34% of the sample, while HYGARCH, IGARCH and FIAPARCH provide the best in-sample fit for respectively 26%, 18% and 11% of the studied countries. However, these results are not in line with the preliminary analysis where all the studied CDS log returns are found to be subject to long-memory feature in the variance. By only focusing in the fractionally integrated subset of models, the HYGARCH is found to majority outperform in 53% of cases, followed by the FIAPARCH in 40% of cases. These results divergence points out the limits of using the 'minimizing loss of information' technique in comparing models appropriateness. Thus, this approach seems to be, in this case, not totally consistent and should only be used tentatively, at least if it is not associated with any other

approaches. Hence the importance of rather rely on the forecasting ability to select the best performant volatility model.

4.3 Forecasting performance

Results of the twenty-day out-of-sample volatility forecasts are reported in Table 3 and Table 4. As mentioned before, the forecasting robustness and reliability of the 9 models is studied through 7 error statistics, namely the MSE, MAE, HMSE, HMAE, QLIKE, R²LOG and MLAE. Even though there is no unanimous dominant model in terms of forecasting ability according to all the comparison measure, it is clearly seen that the fractionally-integrated class of model outperforms the basic GARCH models - not taking into account long-memory in volatility process. Ranked in the last position by 5 out of the 7 criteria, the least forecasting performant model for CDS volatility is the EGARCH with the largest recorded errors.

The lowest values of MSE, MAE and R²LOG are recorded for the FIGARCH, whilst the lowest values of HMSE, QLIKE and MLAE are reported for the FIEGARCH, making them preferable, in terms of accurate forecasting abilities, to the other studied models. On another side, and according to the results of the MSE, MAE, HMAE, R²LOG and MLAE criteria, the HYGARCH produce the highest errors, probably due to its computational complexity.

These findings empirically reveal the nonlinear predictability pattern of CDS volatility. In general, our results are in line with the findings of other financial markets: the non-linear GARCH-class models, that allows for leverage effects, nonsymmetrical dependencies and long-range memory in the volatility model provide a more accurate in-sample performance and a more reliable out-of-sample forecasting ability. The improvement of the forecasting power of the studied models depends, thus, on their ability to capture a maximum of financial stylized facts while estimating the CDS volatility of future days.

APARCH IGARCH FIGARCH FIEGARCH FIAPARCH HYGARCH GARCH EGARCH GJR MSE MAE HMSE HMAE QLIKE \mathbb{R}^2 LOG MLAE

Table 4: Summary of the number of selected models according to each criterion

5 Conclusion

This paper aimed to assess the performances of 9 linear and non-linear volatility models. Using daily sovereign CDS data, GARCH, IGARCH, EGARCH, GJR, APARCH, FIGARCH, FIEGARCH, FIAPARCH and HYGARCH are estimated, allowing to take into account different financial markets properties such as the leverage effect, the asymmetric reaction to good and bad news and long-range persistence. The performance comparison being made upon several loss functions criteria and several multivariate diagnostic tests, a certain number of conclusions can be drawn.

Table 3: Results of the loss functions criteria for the twenty-day out-of-sample volatility predictions

Control (Control (Ctatictic critoria					MCE									MARE				
Month Mon	Countries	GARCH	EGARCH	GJR	APARCH				1	HYGARCH	GARCH	EGARCH	GJR	APARCH	IGARCH		- 20	_	HYGARCH
10,0002 0,1121 0,0009 0,0001 0,0000	Austria	0,0168	0,2640	0,0181	0,0483	0,0189	0,0189	0,1318	11	0,0194	0,0597	0,1335	0,0603	0,1620	0,0643	0,0643	0,1249	II .	0,0636
0.00029 0.1133 0.00099 0.0014 0.00029 0.0003 0.01799 0.0004 0.01799 0.00029 0.0129 0	Belgium	0,0051	0,1971	0,0050	0,0073	0,0000	0,0050	0,6694	0,0058	0,0095	0,0313	0,2422	0,0323	0,0450	0,0324	0,0325	0,2595	0,0332	0,0577
000029 0.1818 0.00099 0.0019 0.00009 0.0109 0.00009 0.0109 0.01099 0	Brazil	0,0012	0,1120	0,0014	0,0020	0,0010	0,0010	0,9925	0,0010	0,0027	0,0249	0,1668	0,0276	0,0326	0,0222	0,0219	0,5846	0,0216	0,0381
100022 0.0046 0.0023 0.0047 0.0056 0.0004 0.0004 0.0004 0.0004 0.0049	Bulgaria	6000'0	0,1813	6000'0	0,0010	0,0008	8000'0	0,1759	0,0008	0,0022	0,0174	0,1050	0,0174	0,0206	0,0105	0,0159	0,0159	0,0156	0,0277
 COODE OLOGAE OL	China	0,0042	0,3349	0,0047	0,0000	0,0055	0,0044	0,0003	0,0044	0,0046	0,0322	0,3501	0,0342	0,0375	0,0410	0,0346	0,0270	0,0361	0,0342
0.0027 0.0128 0.0452 0.0452 0.0452 0.0452 0.0452 0.0454 0.0454 0.0454 0.0454 0.0542 0.0543 0.0542 0.0543 0.0543 0.0543 0.0544 0.0543 0.0544 0.0543 0.0544 0.0544 0.0543 0.0548 0.0549 0.054	Croatia	0,0025	0,0046	0,0023	0,0461	0,0008	0,0007	0,0004	0,0008	0,5356	0,0304	0,0418	0,0291	0,1430	0,0161	0,0160	0,0409	0,0166	0,1537
(1) (2) </th <th>Czech</th> <th>0,0082</th> <th>0,9185</th> <th>0,0089</th> <th>0,0092</th> <th>0,0081</th> <th>0,0082</th> <th>0,9067</th> <th>0,0077</th> <th>0,0010</th> <th>0,0380</th> <th>0,6732</th> <th>0,0372</th> <th>0,0504</th> <th>0,0455</th> <th>0,0369</th> <th>0,2705</th> <th>0,0441</th> <th>0,0404</th>	Czech	0,0082	0,9185	0,0089	0,0092	0,0081	0,0082	0,9067	0,0077	0,0010	0,0380	0,6732	0,0372	0,0504	0,0455	0,0369	0,2705	0,0441	0,0404
0.00047 0.7343 0.00056 0.00043 0.00056 0.00056 0.00056 0.00040 0.00496 0.04396 0.0431 0.04089 0.04040 0.04090 0.04040 0.04099 0.04040 0.04099 0.04040 0.04099 0.04040 0.04099 0.04040 0.04099 0.04040 0.04099 0.04040 0.04099 0.04090 0.04090 0.04090 0.04090 0.04090 0.04090 0.04090 0.04090 0.04090 0.04090 0.04090 0.04099 0.04090 0.04090 0.04090 0.04090 0.04090 0.04090 0.04090 0.04099 0.04090 0.04090 0.04099 0.04090 0.04099 0.04090 0.04090 0.04099 0.04090 0.0409	Denmark	0,0070	0,2619	0,0053	0,0076	0,0052	0,0052	0,3797	0,0046	0,0051	0,0456	0,1950	0,0481	0,0621	0,0487	0,0476	0,1142	0,0578	0,0471
 4.00182 0.01287 0.0114 0.0237 0.0053 0.0053 0.01297 0.0048 0.0239 0.0259 0.0259 0.0259 0.056	Finland	0,0067	0,7343	0,0065	0,0051	0,0059	0,0065	0,0165	0900'0	0,0064	9680'0	0,4611	0,0408	0,0368	0,0390	0,0400	0,0913	0,0410	0,0402
 4 0,0182 0,0165 0,0170 0,0170 0,0131 0,0132 0,0135	France	0,0104	0,0237	0,0114	0,0378	0,0057	0,0055	0,0237	0,0048	0,0290	0,0483	0,0654	0,0504	0,1088	0,0371	0,0370	0,0654	0,0358	0,0828
1 4 4 5 4 5 4 5 4 5 4 5 4 5 4 5 4 5 4 5	Germany	0,0182	0,0165	0,0170	0,0197	0,0171	0,0183	0,1753	0,0205	0,0194	0,0552	0,0603	0,0548	0,0597	0,1203	0,0554	0,0548	0,0585	9990'0
0,0022 0,0035 0,0035 0,0035 0,0035 0,0035 0,0035 0,0035 0,0035 0,0035 0,0035 0,0035 0,0035 0,0035 0,0035 0,04590 0,4589 0,4589 0,4589 0,4589 0,4589 0,4589 0,4589 0,4589 0,4589 0,4589 0,4589 0,4589 0,4589 0,4589 0,4589 0,4589 0,4589 0,4889 0,0034 0,0035 0,0035 0,0035 0,0035 0,0034 0,00	Greece	0,4862	0,6709	0,4788	0,4704	0,4758	0,4814	0,2765	0,4754	0,4775	0,1550	0,2466	0,1490	0,1483	0,1643	0,1511	0,9744	0,1472	0,1496
1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,	Hungary	0,0032	0,0055	0,0031	0,0012	0,0011	0,0010	0,0049	0,0015	0,0008	0,0367	0,0301	0,0361	0,0200	0,0203	0,0190	0,0306	0,0259	0,0173
10,0028 0,0089 0,0020 0,0037 0,0048 0,0032 0,0048 0,0032 0,0044 0,0049	Indonesia	0,4590	0,4590	0,4588	0,4585	0,4587	0,4585	0,6687	0,4586	0,4588	0,1924	0,1925	0,1926	0,1928	0,1925	0,1926	0,1539	0,1925	0,1930
1 0,00043 0,00048 0,00038 0,00043 0,00043 0,00043 0,00043 0,00044 0,00049 0,0	Ireland	0,0228	0,0889	0,0206	0,0375	0,0197	0,0189	0,7325	0,0175	0,0919	0,0487	0,0625	0,0477	0,0637	0,0477	0,0439	0,5391	0,0439	0,1077
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 10,0052 0,1550 0,0054 0,00054 0,0054 0,00054 0,000			0,6015	0,0023	0,0033	0,0022	0,0022	0,5609	0,0022	0,0044	0,0290	9988'0	0,0290	0,0374	0,0284	0,0284	0,1798	0,0283	0,0448
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 6,0024 0,0034 0,0034 0,0026 0,0028 0,0028 0,0023 0,0257 0,0028 0,0031 0,0394 0,0384 0,0367 0,0381 0,0389 0,0385 0,0395 0,0394 8,0039 0,0439 0,0448 0,0419 0,0418 0,0	Lithuania	0,0073	0,4946	0,0076	0,0074	0,0067	0,0063	0,4168	0,0079	0,0075	0,0389	0,3211	0,0401	0,0405	0,0398	0,0381	0,1271	0,0401	0,0396
odd 0,0139 0,0029 0,0039 0,0003 <th>Mexico</th> <th>0,0024</th> <th>0,0034</th> <th>0,0026</th> <th>0,0026</th> <th>0,0028</th> <th>0,0023</th> <th>0,2575</th> <th>0,0028</th> <th>0,0031</th> <th>0,0397</th> <th>0,0384</th> <th>0,0367</th> <th>0,0381</th> <th>0,0398</th> <th>0,0365</th> <th>0,2979</th> <th>0,0395</th> <th>0,0409</th>	Mexico	0,0024	0,0034	0,0026	0,0026	0,0028	0,0023	0,2575	0,0028	0,0031	0,0397	0,0384	0,0367	0,0381	0,0398	0,0365	0,2979	0,0395	0,0409
65 0,00675 0,20646 0,00668 0,00693 0,3232 0,06773 0,0273 0,1284 0,12849 0,12873 0,10873 0,00873 0,0088 0,0003 0,00040<	Netherlands	0,0199	0,0184	0,0179	0,0182	0,0177	0,0178	0,1028	0,0181	0,0184	0,0743	0,0758	0,0739	0,0754	0,0732	0,0731	00000	0,0747	0,0765
es 0,0008 0,0008 0,0008 0,0009 0,0001 0,0001 0,0001 0,0001 0,0001 0,0001 0,0002 0,0004 0,0003 0,0004 0,0003 0,0004	Norway	0,0675	0,2614	0,0668	0,0693	0,3232	0,0673	0,3232	0,0677	0,0675	0,1514	0,2985	0,1484	0,1575	0,1050	0,1480	0,1050	0,1488	0,1489
0,0029 0,0048 0,0029 0,0049 0,0029 0,0049 0,0029 0,0049 0,0029 0,0049 0,0029 0,0049 0,0029 0,0049 0,0029 0,0049 0,0034 0,0014 0,0014 0,0014 0,0014 0,0029 0,0049 0,0014 0,0014 0,0029 0,0049 0,0014 0,0014 0,0044 0,0253 0,0044 0,0253 0,0059 0,0044 0,0044 0,0353 0,0018 0,0044 0,0044 0,0034 0,0049 0,0009 0,0009 0,0004 0,0014 0,0018 0,0018 0,0041 0,0018 0,0018 0,0018 0,0018 0,0019 0,0049 0,0009 0,0009 0,0004 0,0018 0,0019 0,0018 0,0019 0,0018 0,0019 0,0018 0,0019 0,0018 0,0019 0,0019 0,0019 0,0019 0,0019 0,0019 0,0019 0,0019 0,0019 0,0019 0,0019 0,0019 0,0019 0,0019 0,0019 0,0019 0,0019 0,0019<	Philippines	0,0008	0,0032	0,0008	0,0007	6000'0	9000'0	0,2773	0,0010	0,0012	0,0226	0,0209	0,0206	0,0199	0,0231	0,0185	0,9723	0,0221	0,0236
0,00035 0,00068 0,00038 0,00048 0,00048 0,00048 0,00048 0,00048 0,00048 0,00048 0,00048 0,00048 0,00049 0,00049 0,00049 0,00042 0,00048 0,00049 <t< th=""><th>Poland</th><th>0,0029</th><th>0,0048</th><th>0,0029</th><th>0,0043</th><th>0,0012</th><th>0,0012</th><th>0,0088</th><th>0,0011</th><th>0,0010</th><th>0,0325</th><th>0,0471</th><th>0,0321</th><th>0,0401</th><th>0,0202</th><th>0,0201</th><th>0,0612</th><th>0,0197</th><th>0,0176</th></t<>	Poland	0,0029	0,0048	0,0029	0,0043	0,0012	0,0012	0,0088	0,0011	0,0010	0,0325	0,0471	0,0321	0,0401	0,0202	0,0201	0,0612	0,0197	0,0176
0,0042 0,0066 0,0043 0,0062 0,0044 0,0043 0,0044 0,0042 0,0042 0,0044 0,0043 0,0044 0,0044 0,0359 0,0044 0,0359 0,0044 0,0359 0,0044 0,0359 0,0044 0,0359 0,0044 0,0359 0,0044 0,0359 0,0048 0,0009 0,0009 0,0009 0,0009 0,0001 0,0012 0,0012 0,0014 0,0018 0,0018 0,0014 0,0018 0,0018 0,0018 0,0018 0,0018 0,0018 0,0018 0,0018 0,0018 0,0019 0,0019 0,0018 0,0018 0,0018 0,0019 0,0019 0,0018 0,0018 0,0018 0,0019 0,0019 0,0018<	Portugal	0,0035	0,0068	0,0038	0,0059	0,0015	0,0015	0,0113	0,0023	0,0015	0,0405	0,0545	0,0422	0,0557	0,0263	0,0260	0,0743	0,0334	0,0247
iii de dootde do	Qatar	0,0042	9900'0	0,0043	0,0062	0,0604	0,0043	0,0042	0,0045	0,0044	0,0349	0,0421	0,0353	0,0444	0,0350	0,0346	0,0835	0,0362	0,0357
600012 0,00012 <th< th=""><th>Romania</th><th>0,0016</th><th>0,0198</th><th>6000'0</th><th>6000'0</th><th>0,0008</th><th>0,0007</th><th>0,7783</th><th>0,0011</th><th>0,0026</th><th>0,0172</th><th>0,1187</th><th>0,0183</th><th>0,0184</th><th>0,0156</th><th>0,0154</th><th>0,1630</th><th>0,0188</th><th>0,0292</th></th<>	Romania	0,0016	0,0198	6000'0	6000'0	0,0008	0,0007	0,7783	0,0011	0,0026	0,0172	0,1187	0,0183	0,0184	0,0156	0,0154	0,1630	0,0188	0,0292
ia 0,0024 0,0339 0,0025 0,0264 0,0038 0,0025 0,0024 0,0039 0,0034 0,0035 0,0034 0,0035 0,0034 0,0035 0,0034 0,0035 0,0034 0,0035 0,0034 0,0035 0,0034 0,0035 0,0034 0,0035 0,0034 0,0035 0,0034 0,0035 0,0034 0,0035 0,0034 0,0035 0,0034 0,0035 0,0034 0,0035 0,0034 0,0035 0,0034	Russia	0,0012	0,0021	0,0012	0,0012	0,0012	0,0012	0,0021	0,0011	0,0012	0,0239	0,0259	0,0238	0,0237	0,0243	0,0243	0,0259	0,0235	0,0239
ia 0,0034 0,0405 0,0034 0,0034 0,0033 0,0034 0,0034 0,0034 0,0035 0,0034 0,0034 0,0034 0,0035 0,0034 0,0035 0,0034 0,0035	Slovakia	0,0024	0,0339	0,0025	0,0264	0,0018	0,0018	0,6179	0,0019	0,0067	0,0252	0,0633	0,0265	0,0752	0,0218	0,0218	0,2373	0,0220	0,0420
0,00028 0,02029 0,00249 0,00259 0,00028 0,02029 0,00029 <t< th=""><th>Slovenia</th><th>0,0034</th><th>0,0405</th><th>0,0034</th><th>0,0033</th><th>0,0034</th><th>0,0034</th><th>0,2103</th><th>0,0049</th><th>0,0044</th><th>0,0302</th><th>0,0426</th><th>0,0300</th><th>0,0297</th><th>0,0299</th><th>0,0298</th><th>0,8524</th><th>0,0312</th><th>0,0296</th></t<>	Slovenia	0,0034	0,0405	0,0034	0,0033	0,0034	0,0034	0,2103	0,0049	0,0044	0,0302	0,0426	0,0300	0,0297	0,0299	0,0298	0,8524	0,0312	0,0296
0,0055 0,1411 0,0066 0,0059 0,0059 0,0059 0,0059 0,0059 0,0059 0,0059 0,0059 0,0059 0,0059 0,0059 0,0059 0,0059 0,0059 0,0013 0,0059 0,0014 0,0059 0,0001 0,0002 0,0001 0,0001 0,0001 0,0001 0,0001 0,0001 0,0001 0,0001 0,0001 0,0001 0,0001 0,0001 0,0001 0,0001<	Spain	0,0028	0,0279	0,0027	0,0031	0,0025	0,0024	0,0279	0,0023	0,0061	0,0317	0,0827	0,0320	0,0351	0,0295	0,0285	0,0827	0,0282	0,0477
d 0,0013 0,2656 0,0014 0,0015 0,0013 0,0015 0,0014 0,0015 0,0014 0,0015 0,0014 0,0015 0,0014 0,0014 0,0014 0,0014 0,0014 0,0014 0,0014 0,0014 0,0004	Sweden	0,0055	0,1411	0,0060	0,0059	0,0056	0,0058	0,2944	0900'0	0,0058	0,0475	0,5913	0,0481	0,0481	0,0485	0,0464	0,4491	0,0473	0,0465
0,0008 0,0117 0,0009 0,0010 0,0007 0,0007 0,4182 0,0006 0,0013 0,0198 0,0583 0,0207 0,0221 0,0186 0,018 0,0185 0,0773 0,0185 0,0185 0,0018 0,0188 0,0189 0,0018 0,0189 0,0018 0,0189 0,0018 0,0189	Thailand	0,0013	0,2656	0,0014	0,0015	0,0013	0,0013	0,4255	0,0013	0,0016	0,0252	0,2061	0,0261	0,0271	0,0256	0,0252	0,3849	0,0259	0,0299
0,0015 0,0028 0,0017 0,0016 0,0016 0,0014 0,4541 0,0015 0,00298 0,0298 0,0296 0,0303 0,0292 0,0312 0,0284 0,3958 0,0281 aine 0,0042 0,1403 0,0049 0,0052 0,0043 0,0046 0,1388 0,0045 0,0067 0,0274 0,1164 0,0249 0,0290 0,0258 0,0250 0,4394 0,0244 0,0244 0,0241 0,0151 0,0151 0,0148 0,0146 0,0177 0,0147 0,0163 0,0949 0,0965 0,0949 0,0950 0,0929 0,0907 0,0965 0,0916 0,0009 0,0009 0,0009 0,0008 0,0007 0,0007 0,0062 0,0007 0,0018 0,0018 0,0187 0,0176 0,0176	Turkey	0,0008	0,0117	6000'0	0,0010	0,0007	0,0007	0,4182	9000'0	0,0013	0,0198	0,0583	0,0207	0,0221	0,0186	0,0185	0,0773	0,0185	0,0270
0,0042 0,1403 0,0049 0,0052 0,0043 0,0046 0,1143 0,0047 0,0154 0,0164 0,0249 0,0259 0,0259 0,0250 0,0250 0,0950 0,0950 0,0907 0,0916 0,0147 0,0143 0,0143 0,0143 0,0177 0,0147 0,0163 0,0949 0,0965 0,0949 0,0965 0,0949 0,0965 0,0949 0,0965 0,0949 0,0965 0,0949 0,0965 0,0949 0,0965 0,0949 0,0965 0,0949 0,0965 0,0949 0,0965 0,0949 0,0965 0,0949 0,0965 0,0949 0,0965 0,0949 0,0965 0,0949 0,0965 0,0949 0,0049 0,0207 0,0201 0,0965 0,0965 0,0007<	ň	0,0015	0,0028	0,0017	0,0016	0,0016	0,0014	0,4541	0,0015	0,0019	0,0298	0,0296	0,0303	0,0292	0,0312	0,0284	0,3958	0,0281	0,0330
0,0151 0,0177 0,0151 0,0154 0,0148 0,0146 0,0177 0,0147 0,0163 0,0949 0,0965 0,0949 0,0950 0,0929 0,0907 0,0965 0,0916 0,0009 0,0009 0,0009 0,0008 0,0007 0,0062 0,0007 0,0018 0,0218 0,0219 0,0239 0,0207 0,0209 0,0209 0,0018 0,0187 0,0454 0,0176	Ukraine	0,0042	0,1403	0,0049	0,0052	0,0043	0,0046	0,1388	0,0045	0,0067	0,0274	0,1164	0,0249	0,0290	0,0258	0,0250	0,4394	0,0244	0,0304
0,0009 0,0025 0,0009 0,0008 0,0007 0,0007 0,0662 0,0007 0,0018 0,0209 0,0239 0,0207 0,0201 0,0188 0,0187 0,0454 0,0176	NSA	0,0151	0,0177	0,0151	0,0151	0,0148	0,0146	0,0177	0,0147	0,0163	0,0949	0,0965	0,0949	0,0950	0,0929	0,0907	0,0965	0,0916	0660'0
	Venezuela	0,0009	0,0025	6000'0	0,0008	0,0007	0,0007	0,0662	0,0007	0,0018	0,0209	0,0239	0,0207	0,0201	0,0188	0,0187	0,0454	0,0176	0,0310

Numbers in bold refer to the models minimizing the loss function criterion.

Table 3: Results of the loss functions criteria for the twenty-day out-of-sample volatility predictions (Continued)

Statistic criteria				HMSE								HMAE				
Countries	GJR	APARCH	IGARCH	FIGARCH F	FIEGARCH FI	HAPARCH H	HYGARCH	GARCH	EGARCH	GJR	APARCH	IGARCH	FIGARCH	FIEGARCH	FIAPARCH	HYGARCH
Austria	0,1717	0,8324	0,8449	0,8449	0,5361	0,2306	0,1342	0,4810	0,9513	0,1400	0,1135	0,1160	0,1160	0,1014	0,1504	0,3334
Belgium	0,1511	0,6688	0,1655	0,2009	0,5731	0,4235	0,0048	0,3403	0,3789	0,2287	0,1332	0,9186	0,1058	0,1382	0,6533	0,5977
Brazil	0,3147	0,1508	0,3319	0,8107	0,1001	0,1605	0,1141	0,1071	0,1247	0,4636	0,1299	0,1570	0,8090	0,8774	0,1018	0,9637
Bulgaria	0,2566	0,1750	9866'0	0,2960	0,7895	0,1858	0,3913	0,3834	0,8154	0,4077	0,1066	0,2605	0,1725	0,0815	0,3563	0,3590
China	0,4046	0,3621	0,5312	0,3100	0,9334	0,3090	0,1973	0,1656	0,4026	0,4940	0,1455	0,4296	0,1343	0,1503	0,1302	0,3417
Croatia	0,7541	0,8237	0,1212	0,9844	0,6604	0,9817	0,9754	0,7310	0,7544	0,7297	0,8821	0,7854	0,7447	0,7559	0,7434	0,9875
Czech	0,3804	0,1615	0,1679	0,7687	0,3568	0,1866	0,1210	0,8474	0,9255	0,1102	0,8713	0,8982	0,1697	0,2686	0,9185	0,3290
Denmark	0,7105	0,9270	0,5294	0,7015	0,4449	0,1866	0,1334	0,4203	0,3393	0,4420	0,2553	0,5189	0,4186	0,9326	0,1785	0,5613
Finland	0,1419	0,7411	0,1322	0,1299	0,1036	0,1107	0,2654	0,5708	0,5239	0,1105	0,4776	0,3471	0,1356	0,2766	0,0150	0,4860
France	0,3916	0,3300	0,1807	0,1572	9086'0	0,1188	0,9758	0,2958	0,7225	0,4459	0,7253	0,7944	0,7757	0,7225	0,1098	0,7805
Germany	0,2565	0,4401	0,5318	0,8237	0,8339	0,4818	0,5216	0,1277	0,9793	0,7806	0,7225	0,7484	0,1438	0,1015	0,6760	0,2014
Greece	0,5632	0,1728	0,3808	0,1166	0,1101	0,1085	0,3914	0,1711	0,2910	0,4335	0,8196	0,4155	0,1881	0,1490	0,1759	0,3499
Hungary	0,3482	0,2020	0,1544	0,1241	0,8405	0,1136	0,1327	0,7520	0,7063	0,7510	0,7681	0,7416	0,7162	0,7102	0,7423	0,7524
Indonesia	0,6001	0,1478	0,1356	0,9473	0,2363	0,6628	0,4736	0,4057	0,1180	0,1912	0,1402	0,9120	0,1323	0,1130	0,8306	0,2002
Ireland	0,2727	0,5478	0,2666	0,8881	0,1456	0,2613	0,4427	0,1308	0,1289	0,1344	0,1949	0,3797	0,2469	0,9929	0,1316	0,1094
Italy	0,5332	0,5444	0,8795	0,6657	0,1005	0,7044	0,6773	0,6671	0,6652	0,6584	0,7089	0,6766	0,6411	0,6652	0,6588	0,6456
Japan H	0,1605	0,2312	0,2424	0,1800	0,1526	0,2020	0,7090	0,1814	0,2176	0,9274	0,1048	0,1202	0,9272	0,2593	0,8864	0,7186
Latvia	0,1466	0,4932	0,2723	0,2850	0,3223	0,4290	0,1014	0,1678	0,3185	0,4106	0,6083	0,1436	0,5743	0,1662	0,5234	0,3183
Lithuania	0,6748	0,9203	0,7588	0,8314	0,7358	0,0203	0,1169	0,2231	0,3007	0,9843	9656'0	0,3581	0,9213	0,2896	0,1487	0,3957
Mexico	0,2091	0,4638	0,3383	0,1779	0,4335	0,3150	0,1786	0,2657	0,4865	0,7087	0,3329	0,1242	0,5829	0,2816	0,2391	0,2095
Netherlands	0,0019	0,6496	0,3412	0,2072	0,0637	0,000	0,000	0,3186	0,8029	0,0619	0,3484	0,7852	0,6322	0,0961	0,000	0,0000
Norway	0,8095	0,3640	0,1293	0,1105	0,1105	0,5344	0,9276	0,9625	0,1405	0,4785	0,9825	0,1400	0,1836	0,1005	0,7092	0,1546
Philippines	0,1944	0,4249	0,4094	0,5997	0,1045	0,2713	0,1959	0,2934	0,7178	0,2247	0,1017	0,1411	0,1141	0,4089	0,3749	0,7089
Poland	0,1288	0,2891	0,5712	0,1017	0,6582	0,1118	0,1405	0,8264	0,7200	0,8248	0,1145	0,8328	0,7086	0,7477	0,7300	0,7939
Portugal	0,1711	0,4652	0,9779	0,9757	0,8876	0,9183	0,1444	0,9365	0,6933	0,9749	0,7071	0,7109	0,7116	0,7557	0,5761	0,7929
Qatar	0,1555	0,2364	0,5162	0,6170	0,4738	0,1086	0,1277	0,1042	0,1068	0,1197	0,2883	0,1930	0,7598	0,5004	0,3111	0,3036
Romania	0,2356	0,2481	0,4849	0,1579	0,2475	0,2162	0,7391	0,1133	0,8750	0,7715	0,7773	0,7664	0,7499	0,7592	0,8042	0,1228
Russia	0,5564	0,5567	0,5493	0,5487	0,5422	0,5583	0,5558	0,6024	0,5999	0,6010	0,6019	0,6011	0,6008	0,5999	0,6019	0,6018
Slovakia	0,1461	0,3172	0,1572	0,1572	0,2691	0,2237	0,1246	0,2604	0,7703	0,2627	0,1362	0,2946	0,2946	0,2534	0,3357	0,6022
Slovenia	0,1043	0,1004	0,9656	0,5711	0,3511	0,5791	0,2105	0,1349	0,1303	0,1343	0,1317	0,1338	0,1214	0,5795	0,1575	0,1595
Spain	0,1756	0,3023	0,1479	0,1879	0,8925	0,1131	0,1946	0,5370	0,7852	0,1700	0,2662	0,6153	0,7971	0,7852	0,1443	0,8480
Sweden	0,2442	0,6636	0,1900	0,4728	0,7608	0,9317	0,1547	0,2643	0,7898	0,6910	0,1042	0,8460	0,4014	0,8354	0,9885	0,1769
Thailand	0,1456	0,2096	0,4946	0,1019	0,2233	0,6441	0,4063	0,8256	0,9634	0,1751	0,2007	0,1378	0,1017	0,1734	0,3048	0,2604
Turkey	0,3787	0,3207	0,3749	0,1958	0,2613	0,6156	0,2767	0,1840	0,2208	0,9913	0,2780	0,9056	0,7166	0,8171	0,6053	0,3471
λ	0,2678	0,3819	0,3119	0,1041	0,4351	0,8048	0,1135	0,1085	0,1513	0,2461	0,9242	0,4022	0,1572	0,8956	0,4215	0,1596
Ukraine	0,1479	0,1547	0,1262	0,4541	0,1003	0,3017	0,3461	0,9458	0,9780	0,1663	0,1696	0,2055	0,9862	0,9370	0,1562	0,8165
USA	0,5874	0,5831	0,5456	0,5450	0,5131	0,5807	0,7764	0,4248	0,3882	0,4241	0,4244	0,4127	0,4116	0,3882	0,4194	0,7035
Venezuela	0.6039	0.6044	0.6700	0.6665	0.2341	0.1708	0.1064	0.6130	0.6045	0.6066	0.6017	0.6276	0 6244	0.1536	0 1/1/7	0.2678

Table 3: Results of the loss functions criteria for the twenty-day out-of-sample volatility predictions (Continued)

Statistic criteria					QLIKE									R2LOG				
Countries	GARCH	EGARCH	GJR	APARCH	IGARCH	FIGARCH	FIEGARCH	FIAPARCH	HYGARCH	GARCH	EGARCH	GJR	APARCH	IGARCH	FIGARCH	FIEGARCH	FIAPARCH	HYGARCH
Austria	0,3750	0,1801	0,3647	0,1122	0,0853	0,0853	0,2368	0,4388	0,2264	0,4459	0,7794	0,3746	0,1370	0,4488	0,4488	0,7341	0,4363	0,4395
Belgium	0,3249	0,2503	0,2132	0,1330	0,9026	9506'0	0,1228	0,4992	0,4427	0,1054	0,2292	0,1098	0,2206	0,1329	0,1001	0,1417	0,9336	0,1345
Brazil	0,9257	0,2236	0,4483	0,1299	0,1426	0,6683	0,7384	0,1017	0,8118	0,7850	0,1215	0,1084	0,2500	0,8061	0,0688	0,9786	0,2601	0,9204
Bulgaria	0,3663	0,9138	0,3905	0,1048	0,2435	0,1555	0,9137	0,3393	0,1829	0,8627	0,1904	0,0860	6800'0	0,8123	0,0809	0,1905	0,8050	0,1035
China	0,1481	0,2386	0,4922	0,1437	0,4296	0,1168	0,0789	0,1285	0,3236	0,9805	0,1314	0,1498	0,1259	0,5610	0,1031	0,8734	0,1774	0,1013
Croatia	0,1083	0,1065	0,1081	0,8651	0,9786	0,1022	0,1065	0,1028	0,0301	0,1315	0,1591	0,1290	0,2399	0,9687	0,1007	0,1578	0,1020	0,6233
Czech	0,6735	0,4635	0,9242	0,7804	0,7404	0,1523	0,9019	0,7355	0,1502	0,7963	0,3167	0,8417	0,1125	0,1092	0,8436	0,6036	0,1074	0,7744
Denmark	0,2878	0,3238	0,4243	0,2553	0,5189	0,4019	0,9147	0,1785	0,5447	0,1056	0,1821	0,1860	8,9493	0,1191	0,1809	0,3673	0,9240	0,1931
Finland	0,5708	0,3954	0,1089	0,3253	0,3324	0,1202	0,1426	0,4608	0,4697	0,2240	0,9955	0,1902	0,8405	0,1390	0,1120	0,1508	0,1576	0,1479
France	0,1680	0,5936	0,3170	0,9615	0,4206	0,4408	0,5936	0,4926	0,6442	0,8680	0,1060	0,8859	0,1270	0,7548	0,7518	0,1060	0,7389	0,1080
Germany	0,1148	0,2539	0,6543	0,7091	0,7356	0,1309	0,3156	0,6746	0,1885	0,7950	0,8545	0,7606	0,9179	0,8703	0,8189	0,1209	0,1020	0,9904
Greece	0,1711	0,2741	0,4335	0,6542	0,2582	0,1862	0,1472	0,1756	0,3319	0,9231	0,2916	0,3044	0,1760	0,2234	0,1340	0,1506	0,1627	0,1451
Hungary	9868'0	0,8885	0,8926	0,8866	0,8261	0,8524	0,7965	0,8634	0,8103	0,1249	0,1124	0,1238	0,9855	0,1046	0,9688	0,1137	0,1132	0,9037
Indonesia	0,1115	0,1167	0,1895	0,1385	0,8979	0,1307	0,4041	0,8149	0,2002	0,1362	0,3234	0,2156	0,2222	0,1270	0,2141	0,1169	0,1719	0,1636
Ireland	0,1150	0,1970	0,1187	0,1932	0,3638	0,2309	0,8289	0,1300	0,4509	0,1118	9656'0	0,1110	0,1807	0,1237	0,1165	0,1204	0,1527	0,1330
Italy	0,7739	0,7709	0,7740	0,6496	0,7049	0,6434	60,7709	6969'0	0,6980	0,8880	0,8694	0,8575	0,6427	0,5658	0,6196	0,8694	0,6496	0,6142
Japan	8 0,1677	0,8736	0,9131	0,1186	0,1065	0,9130	0,1034	0,8725	0,5747	0,8854	0,2290	0,1141	0,1226	0,8269	0,1080	0,1235	0,1013	0,9994
Latvia	0,1488	0,2997	0,3894	0,6083	0,1251	0,0393	0,0413	0,5231	0,3183	0,1304	0,1525	0,1490	0,5939	0,1431	0,1339	0,2170	0,2523	0,1506
Lithuania	0,2044	0,2832	0,8059	0,9593	0,1943	0,7515	0,2709	0,1485	0,3763	0,1440	0,1894	0,1353	9998'0	0,1400	0,1467	0,2463	0,2881	0,1599
Mexico	0,2510	0,3569	0,7069	0,3311	0,2391	0,5811	0,2799	0,1242	0,2095	0,1281	0,6893	0,3228	0,2731	0,1787	0,2829	0,4145	0,1144	0,2030
Netherlands	0,3186	0,7874	0,0602	0,3482	0,7697	0,6164	0,0943	0,0000	0,0000	0,1709	0,1953	0,1873	0,4355	0,1955	0,1852	0,2312	0,0005	0,0205
Norway	0,9625	0,9873	0,4605	0,9822	0,1382	0,1817	0,1382	0,7092	0,1546	0,1780	0,3609	0,2067	0,6787	0,4132	0,2810	0,4132	0,1752	0,6818
Philippines	0,2764	0,5689	0,4073	0,9985	0,1411	0,9867	0,2082	0,3731	0,7089	0,1427	0,8120	0,1290	0,2031	0,1566	0,9553	0,1075	0,1789	0,2175
Poland	0,7821	0,9163	0,7809	0,5306	0,7129	0,8302	0,9038	0,8112	0,7167	0,9412	0,1378	0,9352	0,8913	0,7587	0,8056	0,1298	0,7800	0,7594
Portugal	0,4618	0,7363	0,4295	0,6806	0,6288	0,6279	0,4300	0,6775	0,5410	0,9387	0,1244	0,9564	0,1147	0,7570	0,7513	0,1116	0,9194	0,6986
Qatar	0,8931	0,9255	0,1047	0,2883	0,1782	0,6127	0,3549	0,2950	0,2885	0,1012	0,1193	0,1063	0,5715	0,1140	0,9339	0,1519	0,1160	0,1245
Romania	0,9652	0,7679	0,8900	0,1095	9665'0	0,8822	0,9351	0,8511	0,1053	0,8422	0,2420	0,8845	0,1900	0,7781	0,8136	0,1131	0,8882	0,1068
Russia	0,7350	0,7483	0,7483	0,7356	0,7394	0,7396	0,7342	0,7346	0,7355	0,4808	0,5077	0,4789	0,4786	0,4858	0,4856	0,5077	0,4764	0,4806
Slovakia	0,8763	0,8667	0,8932	0,1168	0,1221	0,1220	0,7453	0,1612	0,4213	0,8999	0,1717	0,9302	0,1374	6608'0	6608'0	0,7402	0,7805	0,1089
Slovenia	0,3175	0,3700	0,3231	0,3431	0,3232	0,4420	0,3842	0,1575	0,1376	0,2210	0,2280	0,2209	0,2202	0,2200	0,2192	0,1958	0,4102	0,1607
Spain	0,4066	0,6002	0,1569	0,2526	0,4860	0,6670	0,6002	0,1314	0,7091	0,7214	0,1041	0,7774	0,8834	0,6883	0,7057	0,1041	0,7092	0,9179
Sweden	0,2641	0,6405	0,6727	0,1040	0,8460	0,4014	0,1769	0,9883	0,1595	0,3345	0,1262	0,1958	0,3440	0,1552	0,1162	0,3369	0,4645	0,1294
Thailand	0,8093	0,8193	0,1599	0,1990	0,8699	0,1228	0,1717	0,2893	0,2446	0,1665	0,9046	0,1089	0,2126	0,9387	0,1019	0,3224	0,1245	0,1270
Turkey	0,1695	0,2053	0,8470	0,2632	0,7646	0,5755	0,6912	0,7542	0,3322	0,0647	0,9940	0,6162	0,7366	0,5595	0,5477	0,7946	0,4184	0,7218
ž	0,1066	0,1342	0,2441	0,9221	0,4022	0,1400	0,8769	0,4213	0,1576	0,2285	0,1329	0,2740	0,3564	0,1378	0,1115	0,3719	0,4688	0,2560
Ukraine	0,9283	0,0917	0,1489	0,1544	0,4717	0,8153	0,4308	0,1525	0,8165	0,1233	0,5386	0,8248	0,1418	0,7089	0,7697	0,3086	0,7997	0,1493
NSA	0,3082	0,2732	0,3076	0,3077	0,2962	0,2956	0,2732	0,3036	0,5831	0,1617	0,1628	0,1621	0,1624	0,1574	0,1545	0,1628	0,1573	0,1809
Venezuela	0,8257	0,8405	0,8291	0,8315	0,7997	0,7998	0,0123	0,0011	0,1111	0,4877	0,5290	0,4847	0,4770	0,4530	0,4516	0,7244	0,4906	0,0751
Numbers in bold refer to the models minimizing the loss function criterion.	refer to the mod	els minimizing t	he loss function	on criterion.														

Table 3: Results of the loss functions criteria for the twenty-day out-of-sample volatility predictions (Continued)

					MLAE				
Countries	GARCH	EGARCH	GJR	APARCH	IGARCH	FIGARCH	FIEGARCH	FIAPARCH	HYGARCH
Austria	0,1624	0,1566	0,1630	0,9488	0,1566	0,1067	0,1110	0,1589	0,1588
Belgium	0,1863	0,1824	0,1836	0,1651	0,1833	0,1339	0,1484	0,1817	0,1469
Brazil	0,1796	0,1865	0,1750	0,1672	0,1860	0,1052	0,1930	0,1893	0,1591
Bulgaria	0,2087	0,1254	0,2091	0,1990	0,2131	0,2136	0,1253	0,2135	0,1873
China	0,1991	0,1922	0,2230	0,2163	0,2025	0,1741	0,1936	0,1756	0,2061
Croatia	0,1767	0,1567	0,1789	0,1092	0,2061	0,2034	0,1568	0,2014	0,0012
Czech	0,2128	0,6195	0,2197	0,1678	0,1717	0,2149	0,2106	0,1719	0,1999
Denmark	0,1664	0,1641	0,1784	0,1610	0,1652	0,1723	0,1604	0,1587	0,1707
Finland	0,1771	0,1743	0,1839	0,1809	0,1765	0,1840	0,1251	0,1777	0,1783
France	0,1662	0,1409	0,1643	0,1266	0,1754	0,1749	0,1409	0,1757	0,1426
Germany	0,1838	0,1603	0,1796	0,1759	0,1804	0,1832	0,1229	0,1821	0,1599
Greece	0,2184	0,1930	0,2217	0,1652	0,1427	0,2053	0,1288	0,2246	0,1799
Hungary	0,1651	0,1798	0,1659	0,1942	0,1904	0,1941	0,1789	0,1788	0,1987
Indonesia	0,1719	0,1723	0,1672	0,1601	0,1665	0,1633	0,1671	0,1641	0,1639
Ireland	0,1812	0,1743	0,1814	0,1641	0,1804	0,1860	0,1927	0,1813	0,1378
Italy	0,1445	0,1467	0,1481	0,1737	0,1841	0,1767	0,1467	0,1735	0,1773
Japan	0,1799	0,6318	0,1818	0,1678	0,1818	0,1826	0,1264	0,1852	0,1569
Latvia	0,2083	0,2026	0,2191	0,2075	0,2019	0,2029	0,1468	0,2280	0,2022
Lithuania	0,2013	0,1874	0,1961	0,2050	0,2178	0,1868	0,1892	0,1843	0,2069
Mexico	0,1763	0,1759	0,1708	0,1667	0,1653	0,1671	0,1679	0,1614	0,1675
Netherlands	0,1654	0,1684	0,1700	0,1744	0,1659	0,1615	0,1623	0,1727	0,1670
Norway	0,1437	0,1651	0,1523	0,1538	0,1503	0,1381	0,1503	0,1739	0,1646
Philippines	0,1795	0,1935	0,1903	0,1895	0,1784	0,1917	0,1560	0,1876	0,1968
Poland	0,1784	0,1484	0,1797	0,1742	0,1980	0,1951	0,1391	0,1965	0,2008
Portugal	0,1622	0,1432	0,1597	0,1456	0,1789	0,1790	0,1329	0,1632	0,1841
Qatar	0,1862	0,1694	0,1848	0,1849	0,1841	0,1904	0,1386	0,1877	0,1859
Romania	0,2064	0,9735	0,1975	0,1904	0,2119	0,2063	0,1761	0,1986	0,1834
Russia	0,1800	0,1776	0,1804	0,1799	0,1792	0,1794	0,1776	0,1805	0,1801
Slovakia	0,2046	0,2085	0,2005	0,1745	0,2107	0,2107	0,1445	0,2113	0,1864
Slovenia	0,1792	0,2325	0,1793	0,1805	0,1802	0,1810	0,1997	0,1744	0,2168
Spain	0,1740	0,1237	0,1731	0,1682	0,1774	0,1806	0,1237	0,1804	0,1557
Sweden	0,1690	0,1603	0,1873	0,1824	0,1660	0,1791	0,0519	0,1810	0,1814
Thailand	0,1873	0,1890	0,1884	0,1864	0,1849	0,1848	0,1811	0,1816	0,1763
Turkey	0,1901	0,1437	0,1887	0,1847	0,1927	0,1933	0,1416	0,1886	0,1728
Ν	0,1728	0,1788	0,1775	0,1804	0,1811	0,1772	0,1809	0,1692	0,1701
Ukraine	0,1969	0,5542	0,2127	0,2020	0,2016	0,2059	0,0591	0,2100	0,2195
NSA	0,1222	0,1218	0,1222	0,1221	0,1243	0,1268	0,1218	0,1265	0,1189
Venezuela	0,1926	0,1912	0,1943	0,1965	0,1980	0,1992	0,1737	0,1986	0,1716

First, the in-sample estimation shows that all the models almost always pass all diagnostic tests for the most cases, and that the smallest Akaike criterion does not allow us to choose only one best fitted model. Second, none of the volatility models studied in this paper is found to be more relevant than all the others in all situations, in terms of forecasting ability. The chosen model varies from one country to another and from loss function criterion to another. Third, in most cases and according to the majority of the errors statistics criteria, the non-linear GARCH-class models, that capture the long-memory behavior, the leverage effects and the asymmetric dependencies in the volatility process are more relevant in terms of out-of-sample forecasting ability than the others. Fourth, the FIGARCH and FIEGARCH models are found to be the most relevant and robust forecasting models.

Since comparing predictive performance of volatility models is of a paramount in assessing diversifiable risk, in dynamic asset pricing theory and in optimization of portfolio allocation, the economic implication of our findings concerns particularly policymakers, financial practitioners and financial market participants generally. The in-sample performances show that no model clearly outperforms all the others, and since the results are mitigated and differ from one country to another, no volatility model should be selected in an arbitrary way. The model selection should rather be based on the particular features of the data used and the country studied. When it comes to the forecasting performances, some models are preferable and seem to predict accurately and robustly the future volatility of the CDS market. Thus, after taking into account the transaction costs, investors can eventually take advantage of the market's relative inefficiency and generate extra-profits by putting in place a simple trading strategy to exploit the predictability of sovereign CDS volatility. Finally, our study shows that improving the volatility forecasts needs including the maximum of CDS market's stylized facts. However, in practice, the implementation of complex models generates additional costs that are not necessarily reflected in our comparison method, which may controvert the usefulness of using better volatility predictive models.

Our research line can be pursued in several ways. First, a further investigation on the performances of the volatility models can be done by carrying out a comparative study based of the superior predictive ability test rather than on the diagnostic tests and loss functions criteria as in our case. Second, our study can be applied to the corporate CDS market, in order to assess whether the nature of the reference entity impacts the performances of the studied models. Third, since there is a dynamic segmentation in financial markets, it can be interesting to check the robustness of our findings using a different sample from other regions and/or a CDS term structure with different maturity.

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A Appendix

Table 5: Results of the diagnostic tests for the 38 countries

Countries				Austria	_						Belgium	E						Brazil	_		
	Information Q(Criteria	Q(20) C	02(20)	ARCH(10)	Joint Nyblom	A. Pearson G.o.f (50 cells)	RDB(10)	Information Criteria	Q(20)	Q2(20)	ARCH(10)	Joint Nyblom	A. Pearson G.o.f (50 cells)	RDB(10)	Information Criteria	Q(20)	Q2(20)	ARCH(10)	Joint Nyblom	A. Pearson G.o.f (50 cells)	RDB(10)
GARCH(1,1)	-3,347 29,	+ 09/0/67	0,2384	0,0117		2082,67 ***	0,5595	-4,798	0,0826	0,0134	0,0007	210,80	7363,14 ***	* 3,68E-09	-4,841	0,0657	0,0286	0,0014	350,53	1362,83 ***	1,06E-07
ERGARCH(1,1)	-3,415 5,	5,0765	0,0271	0,0043	59,82	3088,26 ***	0,3902	-5,087	590,777 ***	456,839	68,8840 ***	651,05	*** 4087,95	* 66,3374	-4,721	1,1139	0,0241	0,0013	336,89		i
GJR(1,1)	-0,548 4,	4,8651	0,1230	0,0124	41,55	3348,04 ***	0,0044	-5,134	0,0271	0,0104	0,0005	274,01	4140,51 ***	 6,82E-10 	-5,045		0,0269	0,0013	303,95	1129,91 ***	3,13E-10
APARCH(1,1)	-3,851 5,	5,7814	0,0140	0,0014	181,32	1773,18 ***	0,0012	-5,339	0,0252	6600'0	0,0005	299,26	2471,35 ***	* 3,23E-15	-9,427	6900'0	6900'0	í	344,13		í
IGARCH(1,1)	-3,364 15,	15,8231 +	0,3135	0,0309	8,83	3206,35 ***	0,3850	-5,177	0,0494	0,0214	0,0011	202,39	3226,50 ***	• 5,49E-12	-4,970	0,0429	0,0288	0,0014	263,17	965,11 ***	4,00E-08
FIGARCH(1,1)	-3,362 15,	15,8233 *	0,3135	0,0309	18,05	3206,35 ***	0,3775	-4,978	0,1992	0,0214	0,0011	185,82	2173,43 ***	* 6,26E-08	-4,932	0,3063	0,0196	0,0010	236,35	*** 95'602	1,42E-06
FIEGARCH(1,1)	-3,407 23,	23,1804	0,7559	0,0058	38,20	2131,51 ***	0,3927	-4,977	0,0958	0,0127	9000'0	241,35	6964,53 ***	+ 1,02E-06	-1,601	0,0918	0,0140	0,0007	353,85	12945,72 ***	1,86E-10
FIAPARCH(1,1)			4,8655	0,0173	39,73		r	-4,776	386,283 ***	. 266,753 ***	32,6210 ***	306,75	2467,60 ***		-5,891	0,0197	0,0288	0,0014	284,42	1341,09 ***	
HYGARCH(1,1)	-3,355 53,	53,4004 ***	29,6438 **	0,1805	26,14	3427,08 ***	2,2517	-5,258	0,1010	0,0331	0,0016	242,27	*** 09'5899	* 8,98E-06	-5,087	0,0471	0,0289	0,0014	289,61	1219,48 ***	1,46E-07
Countries				Bulgaria	а						China	_						Croatia	ia		
	Information Q(Q(20) ((2(20)	ARCH(10)	Joint	A. Pearson G.o.f	RDB(10)	Information	Q(20)	Q2(20)	ARCH(10)	Joint	A. Pearson G.o.f	RDB(10)	Information	Q(20)	Q2(20)	ARCH(10)	Joint	A. Pearson G.o.f	RDB(10)
GARCH(1.1)	136	99000	0.0069	0 0003	73.69	4499 06 ***	5 34F-16	-5 448	0.5744	0.0443	0.0023	147 78	3162.01 ***	* 6.71F-07	-5 529	58 8880 ***	198615	1 1293	21.17	1624 25 ***	44 9519 ***
ERGARCH(1,1)	1.4	25,0836	0,0627	0,0028	77,44	3906,25 ***		-5,204	2,8891	0,0950	0,0048	298,22			-5,530			0,4670	51,15	1729,94	783,3480 ***
GJR(1,1)		6900'0	6900'0	0,0003	76,87	3546,85 ***	7	-6,390	37,8428 ***		0,0021	298,22			-5,529			1,0589	22,15	1651,28	38,4528 ***
APARCH(1,1)	-5,539 0	6900'0	6900'0	0,0003	39,92	4318,73 ***		-6,121	4,2686	0,0409	0,0019	233,25	7042,35 ***	* 1,74E-09	-5,609	103,421 ***	17,5633	0,7049	7,30		•
IGARCH(1,1)		0805,69	6900'0	0,0003	30,81	*** 09'0967		-6,964	6900'0	6900'0		263,50	7718,56 ***		-5,464	67,1915 ***	16,7475	0,8960	11,50	1870,74 ***	1,5691
FIGARCH(1,1)		6900'0	6900'0	0,0003	31,87	2971,07 ***	3,43E-14	-5,536	0,4017	0,0450	0,0023	86,17	1104,85			55,7512 ***		0,5925	12,58	2016,27 ***	10,2708
FIEGARCH(1,1)		25,0304	0,0627	0,0028	81,79	3886,62 ***	1,4868	-5,333	0,0058	6900'0	0,0003	202,05	10697,77 ***		-5,533			0,3932	49,41	1707,68 ***	S
FIAPARCH(1,1)		6900'0	6900'0	0,0003	20,12	2889,18 ***		-5,353	0,0085	6900'0	0,0003	204,24	11407,99	3,59E-10	-5,493			0,3538	13,46	2004,17	18,7316 **
HYGARCH(1,1)	0 805'5-	0,0078	6900'0	0,0003	66,07	4352,37 ***	2,41E-10	-6,230	3,8754	0,0485	0,0025	297,64	3817,47	1,08E-07	-5,554	54,0052 ***	12,9607	0,8576	8,44	1550,56 ***	1
2 cintain 2				door							Jacomaco	13						backi	3		
connuis				רצברוו							Delillie	4						I	2		
	Information Q(Criteria Q(Q(20) C	(02)20)	ARCH(10)	Joint Nyblom	A. Pearson G.o.f (50 cells)	RDB(10)	Information Criteria	Q(20)	(02)20	ARCH(10)	Joint Nyblom	A. Pearson G.o.f (50 cells)	RDB(10)	Information Criteria	Q(20)	Q2(20)	ARCH(10)	Joint Nyblom	A. Pearson G.o.f (50 cells)	RDB(10)
GARCH(1,1)	ı	1,1361	0,3438	0,0186	(1)	5073,43 ***	0,0013	-5,001	22,9743	1,1090	0,0486	4,68	34939,38 ***	* 0,4752	-11,208	0,0186	0,0110	ľ	460,24	32006,70 ***	1,02E-08
ERGARCH(1,1)	71 707,5-	178,713 ***	142,618 ***	7,4291 ***	75,39	11394,00 ***	51,2730 ***	6,320	8,2895	0,0250	0,0013	602,91	11332,87 ***	 3,84E-05 	-5,788	2,5689	0,0486	0,0025	367,73	30265,32 ***	0,0004
GJR(1,1)			0,0491	0,0024	14	2065,11	0,0040		11,1878	9026'0	0,0737	604,19	14714,60 ***	0,5105	-6,466		0,0683	0,0034	669,51	13822,82 ***	5,01E-08
APARCH(1,1)			29,8426 **	2,9599 ***		19300,08 ***	2,6905	-51,583	0,0012	0,0084	t	542,38			-4,432				2,03	37705,84 ***	1,0815
IGARCH(1,1)		16,2848	5,5208	0,5229	2,30	14895,55 ***	7,4466	-24,427	6900'0	6900'0	1	614,94	30376,46 ***		-6,434		0,0707	0,0036	440,48	30719,51	5,41E-07
FIGARCH(1,1)			0,1636	0,0083		8931,95	0,0015	-6,632	10,2966	0,4900	0,0178	585,49	10407,58 ***		1		1,9299	0,0287	503,83	31432,73 ***	0,0055
FIEGARCH(1,1)			95,3242 ***	9,9514 ***	7	8526,67 ***	9	-4,523	2,4864	0,0352	0,0019	401,82	6117,50	1,78E-05	-6,278					16195,14	0,0054
FIAPARCH(1,1)			34,6246 **	3,3487 ***	2,84	15533,45 ***	N,	-60,873	6900'0	6900'0	,	560,41	30616,72 ***		-6,604	w				13648,38 ***	
HYGARCH(1,1)	c 099,c-	5,5145	0,2789	0,0195	10,162	2/01,45 ***	0,1864	667'/-	3,8123	0,1021		708,00	14265,76 ***	* 6,25E-Ub	-D,/18	2,1983	0,0363	O,UUID	J6//95	29/30,18	8,63E-06
Countries				France							Germany	h						Greece	e,		
	Ę.	Q(20) (02(20)	ARCH(10)	Joint	A. Pearson G.o.f	RDB(10)	Information	Q(20)	Q2(20)	ARCH(10)	Joint	A. Pearson G.o.f	RDB(10)	Information	Q(20)	Q2(20)	ARCH(10)	Joint	A. Pearson G.o.f	RDB(10)
17 71100000	-1	ı	1		Nyblom	(SO cells)		Criteria	200 000	1		Nyblom	(50 cells)		Criteria	0.000			Nyblom	(50 cells)	
EPGAPCH(1,1)	-4,100 U,	0,5050	0,0008	0,0004	58.46	7012.75	71 A607 **	-4,45/	122,807	150,00	0,0115	2 23	3475.68	4,52E-04	-78,634	0,0018	0,0091	0.0003	437 08	10746.67	0,0004
GIR(1.1)	•	0.3972	0.0068	0,7788	101 48	6842 79 ***			18 4334	0,5478	0,134	245 61	6702 13	0.0125	-7 890		0,000	0,000	153.05	14825.81	0.023
APARCH(1.1)		0.0504	0.0069	0,0003	73.40	5469.24		-4.588	0.1859	0.0102	0.0005	277.64	7682.50	1.71F-06	-5.485		0.0120	0.0006	535.30	19611.06	0.0002
IGARCH(1,1)	-4.038 18	18,7233	5.7989	0,3162	10.14	4847.63 ***	1.8916	-4.580	0.0518	0,0100	0,0005	38.10	16685.33 ***		-6.595		0.0133	0.0007	86'006	15941.53	0.0001
FIGARCH(1,1)		17,1288	4,2451	0,2667	12,07	4735,22	1,7622	-4,528	38,5063 ***			26'09	14,82 ***		-5,701		0,0070	0,0003	446,12	88'66888	1,07E-11
FIEGARCH(1,1)		23,4623	23,7292	0,7788	68,83	7012,25	21,5068	-4,463	10,3676	0,3631	0,0243	37,88	16535,60	1,8196	-5,535		0,0068	0,0003	210,99	11070,29	1,60E-05
FIAPARCH(1,1)		18,2128	2,3464	0,1837	16,22	4221,79	2,3503	-4,560	0,0030	0,0077	0,0004	78,34	8513,85	7,18E-12	-6,633	0,0048	0,0070	0,0003	364,23	*** 96,36 ***	
HYGARCH(1,1)	-4,134 0,	0,8961	0,000,0	0,0004	90,94	5802,09	5,52E-09	ì	0,0535	0,0097	0,0005	156,04	8510,04	8,24E-08	-5,188		0,0072	0,0004	285,71	9807,51 ***	7,34E-09

Table 5: Results of the diagnostic tests for the 38 countries (Continued)

Information Criteria 4,926 4,925 4,240 5,167 5,188 5,089 4,204 5,724 5,113 Criteria 4,117 4,128 4,128	q(20) 1,5930 2,5,294 1,776 2,6,2051 2,5,3174 2,83,174 2,84870 2,5,174 3,3085 3,3085 4,20 1,3550 20,7651 18,3586	02(20) / (0.0152	ARCH(10) A ARCH(10) A ARCH(10) A A A A A A A A A A A A A A A A A A A	Upint 12,88 19,17 13,14 141,07 181,27 79,67	A. Pearson G.o.f (50 cells) 1586,45	RDB(10)		Q(20) 113,132 ***			Joint yblom 514,46	A. Pearson G.o.f (50 cells) 5146,61 ***	RDB(10)	Information Criteria	Q(20) 26,5312		ARCH(10) 0,0012	Joint Nyblom	A. Pearson G.o.f (50 cells)	RDB(10)
Criteria 4,926 4,926 4,925 4,925 4,925 4,925 4,925 4,926 4,926 4,926 4,926 4,926 4,926 4,926 4,926 4,926 4,930 4,930 4,930 4,926 4,9	Q(20) 1,6930 28,2994 1,7769 26,2051 29,3085 28,2774 28,4870 76,7774 59,3085 Q(20) 18,3560 20,7661 18,3586		│ <u>,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,</u>	8 4 4 4 4 8	(50 cells) 1586,45	0,0006		a(20) 113,132 ···	:		9	(50 cells) 5146,61 ***	RDB(10)	Criteria	Q(20) 26,5312	4	ARCH(10) 0,0012	_	(50 cells)	RDB(10)
4,956 4,926 4,926 4,240 5,187 5,5187 5,5089 5,5089 1) 5,5139 1) 5,5139 1,177 1,417 4,117 4,117 4,117 4,129 1,128	28,294 26,294 26,2051 29,9851 29,9851 29,774 20,777 29,3085 30,3085 30,3085 30,3085 30,3085			12,88 19,17 13,14 141,07 181,27 79,67 68,48	1586,45	9000'0		113,132 ***	18,8160 40,8243 ***	1,6382 1,4670	514,46	5146,61 ***	2002 27	950 5	26,5312	0,5981	0,0012	27.719	01 0010	
4,240 4,925 5,167 5,187 5,208 5,208 1) 4,208 1) 5,213 1) 6,417 4,117 4,117 4,117 4,118 1) 4,118 1,119 1,19	28,2994 1,769 1,769 29,9851 29,9851 28,487 6,777 59,3085 0(20) 0(20) 18,350 20,7661 18,350 20,7661			19,17 13,14 141,07 181,27 79,67 68,48					40,8243 ***	1,4670			40,0000	מרמיר-				CT'747	3194,19	6500'0
4,925 4,925 5,167 5,208 1) 4,204 1) 5,224 1) 5,224 1) 5,213 2,113 4,117 4,118 4,118 4,128 4,128 4,128 4,128 4,128 4,128 4,128 4,128 4,128 4,128 4,128 4,139 4,139 4,130 4,13	1,7769 26,2051 29,9851 29,9851 28,4870 76,7774 9,9,3085 0(20) 0(20)			13,14 141,07 181,27 79,67	1846 23 ***	106 9260	-5 236 2	23 6731	20,00	0 00 1	513 97	7204 41	6 1253	-4.659	27 3471 +	0 2699	0.0163	194 38	3262 90 ***	0 1951
5-1.67 5-1.67 5-1.88 5-5.08 1) 4-2.08 1) 5-2.13 1) 5-1.13 4-1.17 4-1.17 4-1.17 4-1.19 4-1.1	26,2051 29,9851 29,9851 28,4870 76,7774 59,3085 Q(20) Q(20) 18,3550 20,7661 18,356			141,07 181,27 79,67 58.48	1597 37	0,000		2 6780	0.0119	0,000	533.16	5776 80	0,000	4 938	23 5468	0 2775	0.0015	317.43	219153	0.0132
5-130 5-140 5-108 5-208 1) 5-224 1) 5-213 1) 5-113 1-412	26,2031 28,4870 28,4870 76,7774 59,3085 ··· (Q(20) 18,3550 20,7661 18,3560			141,07 181,27 79,67 58.48	10,1001	20000		1,0730	2000	0000	20,000	27.00	50000	2000	2,000	0,173	50000	00 000	10,000	20000
5.0138 5.024 1) 5.224 1) 5.224 1) 5.224 1) 5.4139 1 6.4137 1 6.4139 1 6.4292 1 6.4384 1 7.4392 1 6.4384 1 7.4392	29,3851 • 76,774 • • 59,3085 • • 59,3085 • • 69,3085 • • 60,700 •			79,67	70,1C/2	10000		1,0070	0,0074	0,000	70,000	00,6216	2000,0	15,237	2,5312	0,000	0,000	204,00	10,0101	1500,0
4-2089 4-2084 1) 4-4.204 2) 5,224 2) 5,213 6,4.128 4-4.128 4-4.202 4-4.203 4-4.203	28,4870 ·			79,67	1532,29	0,0325	7 669'5-	20,7126	6,2195	0,3/82	593,40	7.546,30	9,9/40	900,6-	3,1835	9/00/0	0,0003	161,35	7238,36	0,0001
4,204 -5,224 -5,224 -5,113 (4,117 -4,127 -4,128 -4,128 -4,129 -4,129 -4,129 -4,129 -4,129 -4,129 -4,129 -4,129 -4,129 -4,129 -4,129 -4,129 -4,129 -4,129 -4,129 -4,129 -4,128	28,4870 · 76,7774 ··· 59,3085 ··· 69,3085 ··· 60,3085			68 48	1681,68 ***	0,0755		1,4812	0,0064	0,0003	541,72	1828,68	0,0002	0	20,6532	0,2668	90000'0	193,01	2631,58	0,0003
5,224 -5,113 Information Criteria -4,117 -4,128 -4,292 -4,301 -4,128	Q(20) Q(20) Q(20) Q(20) 18,3550 20,7661 18,3538		≧	00,00	1766,78	0,7631		3,9180	0,0182	6000'0	429,26	10287,98 ***	9,47E-05	-1,922	74,7792 ***	74,0952 ***	0,0121	308,56	11417,77	0,0039
5,113 Criteria 4,117 4,118 4,128 4,128 4,128 4,128 4,128 4,128 4,128 4,128 4,128 4,128 4,128 4,127 4,128	Q(20) (18,3550 20,7661 18,5360 48,8710			145,79	1781,95 ***	15,9512	-6,467	11,7813	0,0349	0,0029	506,17	9721,04 ***	0,0369		0,6608	9900'0	0,0003	270,22	1324,35	2,11E-06
Information Criteria 4,117 4,129 4,129 4,301	Q(20) 18,3550 20,7661 18,5368		<u> </u>	104,79	3150,59	1,9650	-6,910 1	172,627 ***	104,791 ***	5,7026 ***	529,39	9136,52	62,3447 ***	-4,844	16,8009	0,0645	0,0025	231,19	2390,37	0,0395
Information Criteria 4,117 4,128 4,129 4,292 6,301 6,108 6,128	Q(20) 18,3550 20,7661 18,5368	1	<u></u>																	
Criteria Criteria Criteria Criteria Criteria CA 1128 -4,117 -4,117 -4,229 -4,2304 -4,120 -4,1	Q(20) 18,3550 20,7661 18,5368 48,8710 ***	:								Japan							Latvia			
Criteria 4,117 4,118 4,119 4,292 4,492 4,493 4,128	Q(20) 18,3550 20,7661 18,5368 48,8710 ***	1		Joint	A. Pearson G.o.f		Information		l		Joint A.	A. Pearson G.o.f		Information				loint	A. Pearson G.o.f	
711,4 711,4 711,4 711,4 711,4 71,4 71,4	18,3550 20,7661 18,5368	16,1005 10,6894 15,2346 84,9849 ***	1,0983	_	(50 cells)	RDB(10)		Q(20)	Q2(20) A	ARCH(10) N	_	(50 cells)	RDB(10)	Criteria	Q(20)	(02)20	ARCH(10)	_	(50 cells)	RDB(10)
4,128 4,117 4,292 4,292 4,117 4,1128	20,7661 18,5368 48,8710 ***	10,6894 15,2346 84,9849 *** 19,7886	0,7044	6,42	706,76 ***	79,1957	50	0,2421	0,0265	0,0013	289,80	2900,87	4,49E-07	-6,762	0,8951	0,0684	0,0035	518,40	5582,53	9,34E-05
4,117 4,292 4,292 301 104 118	18,5368	15,2346 84,9849 *** 19,7886	1 0355	20,93	701,34	78,4549	-4,838	4,0528	0,0111	0,0004	202,05	9224,14	0,0007	-6,422	0,1819	0,0192	6000'0	317,56	7264,60	5,75E-06
4,292 4,292 401,04 108,041	48 8710 ***	19,7886	L,0233	7,09	706,18	102,6090	-5,035	0,0229	0,0243	0,0012	202,05	4412,83	8,08E-10	-6,783	135,984 ***	112,715 ***	601,7120	601,71	10645,24	175,0040 ***
426 426 428 428 428	10,01	19,7886	7,6263 ***	173,33	2803,25	0,3320	-5,140	0,0240	6600'0	0,0005	268,30	3341,43	5,69E-10	-8,153	3,9882	0,0953	í	467,21		•
26° 178° 26° 26° 26° 26° 26° 26° 26° 26° 26° 26	37,9334 ***	2000		215,87	2121,04	34,0994		0,7752	0,0399	0,0021	165,41	2958,77	5,14E-06	-6,823	0,1178	0,0213	0,0011	385,26	6067,43	1,21E-06
9,128	19,8358	8058/	0,4515	4,36	742,72 ***	4,9326		0,0129	0,0159	0,0008	154,24	3052,91	1,56E-09	-6,591	25,6995	2,5939	0,0594	318,69	8478,85	0,7795
	20,7663	10,6893	0,7044	32,59	701,34	4,8578		15,8544	0,1658	0,0008	214,76	7362,93 ***	0,0048	-6,318	7,8609	0,0934	0,0059	308,06	11365,35	9690'0
FIAPARCH(1,1) -4,232	44,4320 ***	95,9543 ***	:	146,59	1124,49 ***	56,7892		0,0379	0,0070	0,0003	142,79	2069,07	5,32E-09	-7,147	0,0216	0,0184	600000	491,50	8126,94	2,93E-09
-3,814	19,4447	8,8074	0,4818	3,09	1547,15	4,8663	-5,016	11,9659	0,8543	0,0065	255,87	2500,80	7,60E-05	-6,050	0,0276	0,0273	0,0014	241,98	3930,96	6,78E-16
Countries			Lithuania	-						Mexico							Netherlands	sp		
Ę.	Q(20)	(02)20	ARCH(10)	Joint	A. Pearson G.o.f	RDB(10)	e.	Q(20)	Q2(20) A	ARCH(10)		A. Pearson G.o.f	RDB(10)	Information	Q(20)	(02(50)	ARCH(10)		A. Pearson G.o.f	RDB(10)
Criteria			ı	Nybiom	(SU cells)		- 1		ı	١	Nybiom	(SU CEIIS)		Criteria				Nybiom	(SIIS)	
986'9-	22,9839	0,5948	0,0027	626,88	8019,14	0,0016		42,1415 ***	0,0255	0,0018	628,12	7472,34	0,2978	-25,100	6900'0	6900'0	ï	553,51	23743,78	Ī
-6,493	0,0127	0,0243	0,0012	361,43	6720,50	1,41E-07		55,9448 ***	35,3469 ***	0,9119	575,62			-6,332	0,9895	0,0092	0,0005	466,90	25026,02	2,43E-06
-6,728	29,4856	1,2122	0,0062	48,72	12154,68	0,0331		0,0186	6900'0	0,0003	631,92	8368,05	1,24E-08	-6,404	35,8215 **	4,6167	0,0067	652,35	20888,56	0,0059
-7,589	0,0209	0,0224	0,0011	338,70	21762,97	9,09E-15		0,0659	6900'0	0,0003	652,20	7895,86	1,02E-07	-6,659	50,5043 ***	4,9283	0,0023	564,21	9962,05	
-47,880	35,5081 **	0,2251	0,0040	267,36	79526,05	×		6900'0	6900'0	1	681,00	8752,33	t	-6,395	1,0616	0,0208	0,0011	296,30	22535,77	2,37E-06
	2,2311	0,0548	0,0026	526,61	10417,77	4,21E-04		0,0376	6900'0	0,0003	761,49	8112,90	4,41E-08	-6,489	36,7613 ***	2,9217	0,0032	497,92	7366,89	0,0004
	0,3887	0,0381	0,0019	425,87	6323,87	3,41E-06		0,0350	0,0073	0,0004	618,85	10814,81	8,58E-09	-3,994	0,8355	0,0135	0,0007	493,78	6810,24	4,44E-05
.7,763	0,0364	0,0342	0,0017	548,06	6935,73	3,52E-07	-66,974	6900'0	1	1	536,51	9598,41		-6,320	19,9480	0,1904	0,0005	759,38	7247,08	1,48E-07
HYGARCH(1,1) -6,983	17,4218	0,2280	0,0023	736,56	19071,59	0,0046	-11,191	0,5601	0,1274		606,15	10556,06	2,13E-06	-6,124	15,7230	0,3814	0,0031	599,37	4646,54	0,0050
Countries			Norway							Philippines							Poland			
Information Criteria	Q(20)	(02)20	ARCH(10)	Joint Nyblom	A. Pearson G.o.f (50 cells)	RDB(10)	Information Criteria	Q(20)	Q2(20) A	ARCH(10) N	Joint A. Nyblom	A. Pearson G.o.f (50 cells)	RDB(10)	Information Criteria	Q(20)	(02)20	ARCH(10)	Joint Nyblom	A. Pearson G.o.f (50 cells)	RDB(10)
GARCH(1,1) -30,204	6900'0	6900'0	ε	646,42	35160,34	E		3,8317	0,0178	8000'0	713,13	13233,96	0,0013	-4,848	2,0980	0,0978	0,0052	20,42	2999,61	2,74E-04
(1,	0,4984	0,0160	8000'0	411,98	13618,65	4,54E-07	-5,646 9	92,5266 ***	0,9462	0,0919	696,82	8147,63	1,1129	-4,132	27,7586	7,8754	0,4914	11,27	234,00	3,48E+01
-6,799	28,7313	1,4934	0,0104	731,24	18536,04	0,0198		0,7813	0,0114	9000'0	632,62	9185,87	4,83E-06	-4,848	2,1334	6960'0	0,0051	21,12	2920,70	2,77E-04
(1,1) -8,543	46,8995 ***	1,2125	9000'0	664,89	14001,38	0,0001		0,0180	0,0080	0,0004	622,12	9278,99		-4,888	12,3081	0,0534	0,0036	36,52	1212,52	6,05E-02
-30,400	6900'0	6900'0		628'29	34622,64 ***			6900'0	6900'0		686,30	13230,25	,	-4.763	12,3977	0,2211	0,0074	18,45	2828,57	2,23E-02
~	1,1235	0,0122	9000'0	695,05	5532,87	2,59E-07		8,9322	0,0516	0,0024	590,67	7501,75	0,0183		26,1377	9,2676	0,4373	27,14	2379,12	2,82E+00
-	0,0444	0,0087	9	526,34	4376,50	2,99E-08		0,0173	0,0079	0,0004	526,10	8707,55	2,88E-10	-4,828		0,9354	0,0514	4,53		
FIAPARCH(1,1) -10,666	6900'0	6900'0	,	821,47	16500,80	7,33E-24		1,0833	0,0254	0,0013	462,53	14578,78	,	-4,794	22,8794	7,0298	0,3230	29,56	2354,31	8,05E+00
HYGARCH(1,1) -8,168	0,0410	0,0075	0,0004	818,18	17491,46	1,06E-13		24,8994	5,5387		632,05	14900,23	6,1970	-5,035	36,1529 **	8,9171	0,5005	492,06	4551,14	13,8160

Table 5: Results of the diagnostic tests for the 38 countries (Continued)

Countries				Portugal	_						Qatar							Romania	_		
	Information	(02)0	(02/20)	ARCH(10)	Joint	A. Pearson G.o.f	RDB(10)	E	(02)0	(02)20)	ARCH(10)		A. Pearson G.o.f	RDR(10)	Ę	(02)0	(02)20	ARCH(10)		A. Pearson G.o.f	RDR(10)
	Criteria	מוכח	מב(בה)	ARCHITO	Nyblom	(50 cells)	(OT)GOV	- 1	מוכח	מקוקה)	ארכח(בט)	Nyblom	(SO cells)	(or)anu	- 1	לוכח		- 1	Nyblom	(50 cells)	(OT)GOV
GARCH(1,1)	-4,213	8,1460	0,0211	0,0007	58,26	2148,92	0,0032	-5,730	0,4905	0,0187	6000'0	390,72	6144,22	7,14E-06		0,0063	6900'0	0,0003	65,55	2596,78	1,38E-13
ERGARCH(1,1)	-4,210	18,2045	55,8087 ***	0,5970	68,31		£	-5,497	0,0709	6600'0	0,0005	265,54	17904,04	4,73E-07		414,353 ***	86,8006 ***	9,1538 ***	710,67	2766,51	8,2466
GJR(1,1)	-4,213	5,7994	0,0140	0,0005	58,89	2148,55	0,0012	-5,420	0,8484	0,0182	6000'0	374,56	2428,71	4,36E-06		14,2707	0,0307	0,0017	710,67	5143,54	0,0003
APARCH(1,1)	-4,303	1,2002	0,0072	0,0004	87,59	2317,98	8,48E-06	-27,306	6900'0	6900'0		309,20				16,9822	0,0377	0,0022	58,57	1352,79	9000'0
IGARCH(1,1)	-4,153	15,9522	70,8632 ***	0,5714	5,59	2230,79	0,5644	-5,719	0,0357	0,0120	9000'0	334,22	9521,18	7,45E-08	-4,975	12,2667	0,0297	0,0016	130,78	1223,21	6000'0
FIGARCH(1,1)	-4,154	16,0789	74,7565 ***	0,6954	6,07	2257,34	1,4703	-5,621	4,6512	0,0953	0,0049	132,74	7661,36	0,0005	-5,439	6900'0	6900'0	0,0003	130,78	2853,53	1,27E-12
FIEGARCH(1,1)	-4,394	58,8919 ***	69,6413 ***	6,2972 ***	152,73	1115,63	116,2830 ***	-5,508	1,1313	0,0154	0,0007	245,86	12152,78	0,0018	-5,430	32,9755 **	0,2570	0,0172	14,80	2809,52	0,0062
FIAPARCH(1,1)	-4,672	29,5043 +	73,0205 ***	4,6828 ***	385,28	2650,32	10,4886		0,0717	0,0137	0,0007	240,42	9689,31	3,12E-07		6,1051	0,0244	0,0013	140,42	4615,76	0,0020
HYGARCH(1,1)	-4,559	36,9416 ***	49,9189 ***	1,0429	367,01	3579,22	26,7028	-5,922	0,0250	0,0118	9000'0	362,05	7443,30	1,52E-08		29,2195	0,1838	0,0029	181,41	1969,51	0,0223
Countries				Russia							Slovakia	_						Slovenia			
	Information				Joint	A. Pearson G.o.f		Information				Joint /	A. Pearson G.o.f		Information		l		Joint	A. Pearson G.o.f	
	Criteria	Q(20)	(02)20)	ARCH(10)	Nyblom	(50 cells)	RDB(10)	Criteria	Q(20)	(02)20	ARCH(10)	_	(50 cells)	RDB(10)		Q(20)	(02)20	ARCH(10)	_	(50 cells)	RDB(10)
GARCH(1,1)	666'8-	11,5329	20,5284	0,8859	1,61	115,86	126,4820	-5,927	1,2437	0,1159	0,0068	185,57	11600,19	1,21E-05	-4,772 2	24,7842	8,2290	0,1474	2,11	38119,51	1,5993
ERGARCH(1,1)	-3,991	11,9272	17,1360	0,5738	5,15	123,06	3,4639		16,3954	0,8987	0,0517	35,08	9232,98	2,2528		25,6910	0,7816	0,0436	53,05	9279,12	0,6477
GJR(1,1)	-4,003	11,5791	21,3905	0,8695	1,95	98'86	54,5139		1,3406	0,1297	0,0077	186,41	11357,85	1,36E-05		24,3340	8,6544	0,1186	2,61	19844,39	1,4358
APARCH(1,1)	-4,005	10,8970	21,0426	0,8779	1,89	117,02	2,0299	-5,965	20,9647	0,3732	0,0193	205,68	4500,97	0,0757	-4,780 2	23,5669	8,4562	0,1056	3,57	35336,01	1,2934
IGARCH(1,1)	-4,000	11,6009	20,8452	0.9494	1.53	115,63	14.5312		2,1215	0.1761	0.0111	9.87	13642.82	7.72E-05		32.4648 **	9.0434	0.2165	1.52	38756.52	2.3373
FIGARCH(1,1)	2	11,7362	20,1840	0,9201	3,56	112,15	16,1394	-5,861	2,1236	0,1763	0,0111	13,15	13694,25	7,74E-05		29,1249	8,5046	0,2446	2,30	38813,78	2,7887
FIEGARCH(1,1)	3,991	11,9273	17,1361	0,5739	5,53	121,93	3,4049	-4,342	34,7287 **	16,5740	0,5374	184,26	7317,98	12,2474		4,3473	0,0554	0,0032	392,92	7540,61	,
FIAPARCH(1,1)	4,004	11,3651	19,6115	0,7418	2,78	113,72	6,4765	-5,872	1,3533	0,1081	0,0063	14,90	12610,89	4,94E-05		1,0354	0,0343	0,0017	334,97	4494,23	4,29E-05
HYGARCH(1,1)	-3,998	11,6701	19,7961	0,8525	3,71	118,90	16,3329	-5,991	0,3934	0,1137	0,0060	155,07	7839,59	6,23E-07		23,3301	2,1289	0,0592	98'659	6649,50	1,3382
Countries				Spain							Sweden							Thailand	L		
	Information				loint	A December A		Information				loint	A Designation A		Information				loint	A December A	
	Criteria	Q(20)	Q2(20)	ARCH(10)	Nyblom	(50 cells)	RDB(10)		Q(20)	Q2(20)	ARCH(10)	_	4. Fedison 6.0.1 (50 cells)	RDB(10)		Q(20)	(02)20	ARCH(10)	_	(50 cells)	RDB(10)
GARCH(1,1)	-4,205	0,1149	0,0072	0,0004	123,66	1230,66	3,90E-07	-6,431	0,0011	0,0739	0,0037	513,78	10848,62	1,86E-13		1,7565	0,0071	0,0003	581,98	4923,16	0,0003
ERGARCH(1,1)	-4,105	11,8580	0,5806	0,0377	42,62	1542,01	20,6711	-5,793	2,6122	0,0910	0,0044	374,98	7896,91	0,0005		30,9012 **	0,4201	0,0175	459,32	5299,30	0,2655
GJR(1,1)	-4,208	0,0265	6900'0	0,0003	118,58	3360,48	5,96E-10	-0,658	133,390 ***	176,560 ***	17,2900 ***	542,42	10075,54	292,3860		24,6423	6/96'0	0,0885	548,26	5771,18	7,8470
APARCH(1,1)	-4,159	0,0269	0,0070	0,0003	224,62	1658,02	3,87E-08		14,1611	0,7800	0,0111	533,81	8622,64	5		0,3637	0,0078	0,0004	553,98	6412,52	4,65E-05
IGARCH(1,1)	-4,168	0,1050	0,0072	0,0004	74,75	1250,66	3,20E-07	-9,591	6900'0	6900'0		434,039	22159,64	1,14E-07		32,5837 **	1,5782	0,1525	570,66	5646,48	1,6670
FIGARCH(1,1)	-4,154		0,0080	0,0004	91,95	1098,28	1,32E-07		0,0080	6900'0	0,0003	149,21	18914,88	5,82E-11		18,9330	0,1015	0,0091	552,50	1333,21	0,1011
FIEGARCH(1,1)	-4,104		0,5806	0,0377	93,64	1541,60	16,4878		153,937 ***	74,9719 ***	5,8773 ***	332,10	8389,55	49,8163		0,0428	9/00'0	0,0004	455,17	10646,13	1,48E-08
FIAPARCH(1,1)	-4,199	0600'0	6900'0	0,0003	74,36	1331,34		-7,378	0,0750	0,0882	0,0044	608,11	22405,91	2,16E-06		212,707 ***	15,9829	1,6022	545,84	2692,58	0,4598
HYGARCH(1,1)	-4,316	0,0381	0,0114	9000'0	133,45	1042,58	2,02E-07	-6,300	8,5002	0,6284	0,0327	409,05	3540,58	0,1756	-6,258	2,3372	0,0084	0,0004	596,53	8097,17	0,0015
Countries				Turkey							UK							Ukraine			
	Information	Q(20)	Q2(20)	ARCH(10)	Joint	A. Pearson G.o.f	RDB(10)	Information	Q(20)	(02)20	ARCH(10)	Joint /	A. Pearson G.o.f	RDB(10)	Information	Q(20)	(20) /	ARCH(10)	Joint	A. Pearson G.o.f	RDB(10)
CABCU(4.1)	702 4	0.0467	00100	20000	0000	200 45	0 105 10	2000	2 5 4 3 6	32000	0000	02120	57130	775 17	2002	0000	0,000	0001	77.07	470074	2 205 14
ERGARCH(1,1)	4514	0,010,0	0,0135	70000	92,01	806.84	1,18E-10		167 760	5,6149	1 9385	616.09	7477 76	10 3849		884 481 ***	801 556 ***	105 8400 ***	970.74	47,96,74	139 62
C10(1.1)	420,4	0,000	0000	0,000,0	10000	250,03	2,535.00		130 077 ***	2,000	2,000	634 47	70,007	7 225 05		126,701	151 049 ***	00000	10001	10000,00	20,000
ABABCU(1.1)	787 1	0,0249	0,0064	0,0013	151 00	569.65	2,03E-09		276,661	7,4021	0,000	569.29	0876.87	7,22E-03		0.000	0.061	0,0030	183 33	2002,000 07 777 A	0,0002 9 30E-13
IGABCH(1.1)	101,4	0,0366	0,000	0,000	69 56	50,600 57,670	7,08E-11		22,00,00	2450,7	(000)	615 3180	12727 38	1 31E-14		2 0310	0.1073	0,0036	174.00	427,73	2 265-05
FIGARCH(1.1)	4,089	0,0300	0.0192	0,000	89 0917	738 4797	1,70E-03		103 137	73 0977	0.0046	663.73	2626 12	0 0006		4 1195	0,100,0	0,0037	83.57	5513 99	7,52E-03
FIEGARCH(1,1)	-4.420	1 3771	0,0120	0.0007	410 32	981.06	0.0021		4 0148	0.0142	0.0007	422 20	6955 95	2 75F-05		15 5804	0 3402	0.0318	62,30	10353.01	1 0228
FIAPARCH(1,1)	-4.208	17.3861	3.8679	0.1367	1.90	869.68	1.3664	-8.157	2,7105	0.0075	0.0003	701.51	13502,33	1.55F-12		0.2173	0.0339	0.0017	122.79	9309.59	7.34F-08
HYGARCH(1,1)	-4,721	0,0078	6900'0	0,0003	89,71	339,31	6,26E-14		15,8465	0,0864	0,0004	647,42	7236,52	7,66E-08	-7,350	-7,350 162,703 ***	187,622 ***	5,8859 ***	300,18	11230,89	63,1099 ***

Table 5: Results of the diagnostic tests for the 38 countries (Continued)

20000											-		
	Information	100,0	(00)00	40011/40)	Joint	A. Pearson G.o.f	101)000	Information (200)	100,00	40011/401	Joint	A. Pearson G.o.f	(10)
	Criteria	Q(20)	(dz(zn)	ARCH(10)	Nyblom	(20 cells)	KDB(10)	Criteria (1/20)	(0z)zh	ARCH(10)	Nyblom	(SO cells)	(DE)
GARCH(1,1)	-3,343	22,1954	0,6640	0,0343	2,10	30069,34	0,3515	-4,433 16,8322	7,8329	0,4800	2,83	738,70	4,5171
ERGARCH(1,1)	-3,219	20,9911	0,6783	0,0249	70,44	10179,22	0,3611	-4,335 22,2545	8,0298	0,2973	96'69	86'065	4,5980
GJR(1,1)	-3,343	22,6308	0,6768	0,0361	2,90	30020,77	0,3693	-4,433 16,1177	9,7585	0,6520	2,68	905,20	4,3576
APARCH(1,1)	-3,343	23,2446	0,7894	0,0441	3,33	2994,64	0,4664	-4,450 16,2001	51,5638 ***	4,2005 ***	2,39	1071,96	2,1091
IGARCH(1,1)	-3,333	25,8119	1,2310	0,0762	1,73	29578,64	0,8526	-4,409 16,9461	23,4663	1,7687	1,5400	1025,57	33,6120
FIGARCH(1,1)	-3,385	21,7770	1,0326	0,0392	18,30	29371,73	0,2184	-4,410 18,3256	13,0599	0,7184	75,83	720,43	14,4391
FIEGARCH(1,1)	-3,218	20,9958	0,6784	0,0249	134,90	10202,40	0,3621	-4,518 84,5941 ***	0,1977	0,0138	238,36	200,46	0,1152
FIAPARCH(1,1)	-3,394	18,9781	0,5677	0,2338	40,45	29411,16	0,2197	-4,771 44,4650 ***	** 81,4568 ***	* 8,4904 ***	149,77	340,07	4,0510
HYGARCH(1,1)	-3,475	-3,475 21,4223	0,2415	0,0196	15,65	27477,49	0,1690	-4,861 183,998 *** 32,3894 **	* 32,3894 **	3,2795 ***	237,86	403,25	169,0970
Q(20) and Q^2(20) are the Box-Pierce Q statistics under the null hypothesis of no serial correlation in the 20^{th} lag order of respect	9 Box-Pierce Q stat	istics under t	he null hypoth	nesis of no seria	al correlation	in the 20^{th} lag orde	er of respective	ly the standardized residua	ils and the squa	ared standardize	d residuals. A	RCH (10) is the Engl-	ARCH-LIM testandardized residuals and the squared standardized residuals. ARCH (10) is the Engle's ARCH-LIM test with 10 lag orders, used to detect ARCH effects in the series under the null hypothesis of no
autocorrecations in the squared residuals. The Joint Nyblom is a stability test under the null hypothesis of parameters joint constancy	quared residuals. To	he Joint Nybl.	om is a stabilit	y test under th	no null hypoti	hesis of parameters joi.	nt constancy or	ver time against the alterna	itive of parame	eters shift at an u	undefined bre.	akpoint. The A. Pear.	over time against the alternative of parameters shift at an undefined breakpoint. The A. Pearson G.o.f is the adjusted Pearson goodness-of-fit test that verifies whether the residuals' empirical distribution matches
or not the theoretical distr	ribution (namely G	ริลนรร, Studen	t or G.O.D dep	vending on the	country). RI	OB denotes the Residua	als-Based Diagn	ostic test that checks for α	anditional Hete	eroscedasticity, t	by complemer	iting and filling the g	or not the theoretical distribution (namely Gauss, Student or G.O.D depending on the country). RDB denotes the Residuals-Based Diagnostic test that checks for conditional Heteroscedasticity, by complementing and filling the gaps of the Box-Pierce Q statistics. *, ** and **** denote the statistical significance at respectively 1%, \$5% and 10% levels.