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# Comparing State Spaces in Automatic Security Protocol Analysis

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**Abstract.** There are several automatic tools available for the symbolic analysis of security protocols. The models underlying these tools differ in many aspects. Some of the differences have already been formally related to each other in the literature, such as difference in protocol execution models or definitions of security properties. However, there is an important difference between analysis tools that has not been investigated in depth before: the explored state space. Some tools explore all possible behaviors, whereas others explore strict subsets, often by using so-called scenarios.

We identify several types of state space explored by protocol analysis tools, and relate them to each other. We find previously unreported differences between the various approaches. Using combinatorial results, we determine the requirements for emulating one type of state space by combinations of another type.

We apply our study of state space relations in a performance comparison of several well-known automatic tools for security protocol analysis. We model a set of protocols and their properties as homogeneously as possible for each tool. We analyze the performance of the tools over comparable state spaces. This work enables us to effectively compare these automatic tools, i. e., using the same protocol description and exploring the same state space. We also propose some explanations for our experimental results, leading to a better understanding of the tools.

## 1 Introduction

Cryptographic protocols form an essential ingredient of current network communications. These protocols use cryptographic primitives to ensure secure communications over insecure networks. The networks are insecure in two ways: attackers may analyze or influence network traffic, and communication partners might be either dishonest or compromised by attackers. Despite the relatively small size of the protocols it is very difficult to design them correctly, and their analysis is complex. The canonical example is the famous Needham-Schroeder protocol [40], that was proven secure by using a formalism called BAN logic. Seventeen years

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later G. Lowe [33], found a flaw by using an automatic tool Casper/FDR. The flaw was not detected in the original proof because of different assumptions on the intruder model. However, the fact that this new attack had escaped the attention of the experts was an indication of the underestimation of the complexity of protocol analysis. This example has shown that automatic analysis is critical for assessing the security of such cryptographic protocols, because humans can not reasonably verify their correctness.

A few years later it was proven that the security problem is undecidable [1,28] even for restricted cases (see e.g. [20] for a survey). This undecidability is one of the major challenges for automatic analysis. For instance, in the tool used by Lowe, undecidability is addressed by restricting the type of protocol behaviors that were explored. The protocol that Lowe investigated has two roles. These roles may be performed any number of times, by an unbounded number of agents. Lowe used his tool to check a very specific setup, known as a *scenario*. Instead of exploring all possible protocol behaviors, the protocol model given to the tool considers a very small finite subset, in which there are only a few instances of each role. Furthermore, the initiator role is always performed by a different agent than the responder role. The attack that Lowe found exactly fits this scenario. However, if there would have been an attack that requires the intruder to exploit a large number of instances of the responder role, Lowe would not have found this particular attack with the tool. Addressing this problem, he provided a manual proof for the repaired version of the protocol, which states that if there exists any attack on that protocol, then there exists an attack within the scenario. Ideally, we would not need such manual proofs, and explore the full state space of the protocol automatically, or at least a significant portion of it.

Over the last two decades many automatic tools based on formal analysis techniques have been presented for the analysis of cryptographic protocols [2, 8, 11, 12, 19, 22, 35, 37, 39, 43, 44]. These tools address undecidability in different ways: either by restricting the protocol behaviors similar to the approach used by Lowe, or by using abstraction methods. However the restrictions put on the protocol behavior are rarely discussed or compared to the related work. Moreover, the tools provide very different mechanisms to restrict the protocol behaviors, and the relations between these mechanisms has not been investigated before.

This work started out as an investigation into the performance of protocol analysis tools. In contrast to the large number of tools, there are hardly any comparison studies between the different tools. In each tool paper the authors propose some tests about their tools' efficiency, by describing the performance of the tool for a set of protocols. These tests implicitly use behavior restrictions, which are often not specified and sometimes are designed specifically to include known attacks on the tested protocols. Choosing different restrictions has a very clear impact on the accuracy as well as the performance of the analysis process. In particular, imposing stronger restrictions on the protocol behavior implies that fewer behaviors need to be explored, which means that for most tools the time needed for the analysis will be exponentially lower.

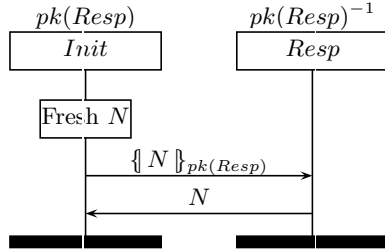
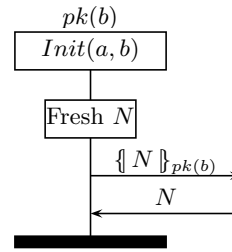
**Contributions:** In this paper we address two distinct, but very closely related problems. First, we discuss types of behavior restriction models used by protocol analysis tools, which we will also refer to as the explored *state space*. We show how these different state spaces are related to finding, or missing, attacks on protocols, and show how to match up certain state space types. Using mathematical results, we compute the number of concrete scenarios that needs to be considered in order to analyze all the possible behaviors involving up to  $n$  protocol role instances, or threads. Second, we use the knowledge gained about state spaces to perform a tool performance case study. We try to match up the exact restrictions used in each tool, and compare their performance on similar state spaces. We use our unfolding of symbolic scenarios to generate the input files for each tool in the test. This leads to new insights in the performance of the tools for secrecy and authentication properties.

**Related work:** To the best of our knowledge, the difference between state spaces in security protocol analysis has not been investigated before. However, some work exists on comparing the performance of different security protocol analysis tools. In [36] C. Meadows compares the approach used by NRL [37] and the one used by G. Lowe in FDR [42] on the Needham-Schroeder example [40]. She examines the difference and concludes that the two tools are complementary even though NRL was considerably slower. In [3], a large set of protocols is verified using the AVISS tool and timing results are given. In [47], a similar test is performed using the successor of AVISS, called the Avispa tool suite [2]. As the AVISS/Avispa tools consist of respectively three and four back end tools, these tests effectively work as a comparison between the back end tools. No conclusions about the relative results are drawn in these articles. A qualitative comparison between Avispa and Hermes [12] is presented in [30] and provides general advice for users of these tools. The comparison is not based on testing but on conceptual differences between the modeling approaches. In [15], a number of protocol analysis tools are compared with respect to their ability to find a particular set of attacks.

**Outline:** In Section 2 we describe and relate some of the different state spaces considered in symbolic protocol analysis. In Section 3 we determine the number of concrete scenarios needed to cover the same state space as a given symbolic scenario. In Section 4 we present our performance comparison experiments. We describe the choice of tools and test setup. We then discuss the results of the analysis before we move to the conclusions and future work in the last section.

## 2 State spaces in security protocol analysis

In the symbolic analysis of security protocol, one models both the agents that execute a security protocol, as well as the possible behavior of the active intruder. Combined these yield a system which should model (at some level of abstraction)

Fig. 1. An example protocol  $EX$ .Fig. 2. An example protocol instance for the initiator role of  $EX$ .

all possible behaviors of the agents in the presence of an active intruder. Verifying security properties of a protocol amounts to checking whether all possible behaviors of the resulting system satisfy the desired security property.

In such a model, agents may initiate a protocol or respond to incoming messages. Consider the example protocol  $EX$  shown in Figure 1. There are two roles  $Init$  (initiator) and  $Resp$  (responder). An agent  $a$  can initiate a session of the protocol at some point by starting to execute the initiator role. He chooses who he wants to communicate with, for example  $b$ . Next he generates a fresh random number  $N$ , and sends  $N$  encrypted with the public key  $pk(b)$  of the agent  $b$ . After that he waits until he receives from the network the number  $N$  back. The agent  $b$  accepts incoming messages encrypted with its public key  $pk(b)$ . Once such a message is received from an agent (for example, from  $a$ ),  $b$  starts an instance of the responder role. Following the model of the responder role,  $b$  will accept and decrypt the message, and send back the resulting number  $N$  to  $a$ .

In general, any number of agents may be running the protocol in parallel, and agents can also start multiple sessions with any other agent at the same time as responding to incoming messages.

## 2.1 Process model

We first give a high-level description of the protocol analysis problem in terms of processes. It is not our intent to go into full detail but only to provide the required knowledge for understanding the state space restrictions in the remainder of this paper. For further details we refer the reader to e. g. [21].

We recall some process calculus basics. A *process*  $P$  defines a possibly infinite number of possible behaviors, where each possible behaviour is represented as a sequences of events. A possible sequence of events is referred to as a *trace* of the system. All possible behaviors of a process  $P$  are denoted by its set of traces, denoted by  $\text{tr}(P)$ . We write  $X \parallel Y$  to denote the process consisting of the parallel composition of the process  $X$  and  $Y$ . We write  $!X$  to denote the replication of the process  $X$ , i.e.  $!X = X \parallel (!X)$ . We write  $+$  to denote the choice operator, which is generalized to  $\sum$  for choosing over a parameter range.

A security protocol is defined as a finite set of communicating processes, referred to as “roles”. More precisely, we define a *protocol* as a mapping from

role names to processes. In practical applications, these roles have names such as client/server/..., or initiator/responder. A role usually consists of a sequence of send and receive events, and implicit or explicit generation of messages or fresh values such as nonces or session keys. In this paper we will not go into details of the allowed actions in a role.

Roles are executed by agents. Upon execution, any identifiers referring to role names in the protocol are instantiated with concrete agent names. For a protocol  $Q$  with  $|dom(Q)| = n$  roles, where  $dom(Q) = \{r_1, \dots, r_n\}$ , we denote by  $Q(x)(a_1, \dots, a_n)$  the process that is the instantiation of the role  $x$ , where  $r_1$  is substituted by  $a_1$ , etc.. This notation is effectively used as a shorthand for the more commonly used substitution notation  $Q(x)[a_1, \dots, a_n/r_1, \dots, r_n]$ . For example, in Figure 2 we show the process  $EX(Init)(a, b)$ . We allow some parameters to be unspecified, notation  $-$ , which we interpret to be the unspecified choice between any of the possible agents from the set  $Agent$ . We will return later to exact the specification of the agent set, but remark here that a finite set will suffice for our purposes. In particular, we define for any protocol  $Q$  that

$$Q(x)(a_1, \dots, -, \dots, a_n) = \sum_{i \in Agent} Q(x)(a_1, \dots, i, \dots, a_n).$$

Hence for the example protocol  $Q$ ,  $Q(Resp)(-, -)$  denotes a single execution of the responder role, with any choice for the agent names.

An agent can perform any role any number of times in parallel. Thus, for any protocol  $Q$ , the behavior of the agents is defined by the process

$$\prod_{x \in dom(Q)} !Q(x)(-, \dots, -).$$

The messages are transmitted over a network that is considered to be insecure. It is insecure in the sense that an adversary or intruder can eavesdrop on any message, or insert his own messages. Furthermore, we assume an intruder may also have corrupted certain agents, for example because he has learnt their private keys, allowing him to impersonate the corrupted agents. Because agents may not know who has been corrupted, the non-corrupted agents may still start protocol sessions with corrupted agents.

This situation is commonly modeled by a single ‘‘intruder’’ who is represented by the process *Intruder*. The *Intruder* process can take messages from the network, manipulate them, insert messages into the network, or generate fresh values. Furthermore, the intruder has corrupted the agent  $e$ , thereby learning its long-term secrets, including the long-term private keys of  $e$ .

**Definition 1 (Sys).** *Given a protocol  $Q$ , the system describing the behavior of the agents in the context of the intruder is defined as*

$$Sys(Q) = Intruder \parallel \prod_{x \in dom(Q)} !Q(x)(-, \dots, -).$$

If there exists an attack on (a trace property of) a protocol  $Q$ , it is represented in the set of traces of the system  $Sys(Q)$ . Conversely, if no trace in  $tr(Sys(Q))$  exhibits an attack, there is no attack on the protocol  $Q$ .

## 2.2 Restricting the state space

Because of undecidability or efficiency concerns, protocol analysis tools usually apply some restrictions on the system and do not explore all elements from the set  $\text{tr}(\text{Sys}(Q))$ . More precisely, the system verified is not the full system  $\text{Sys}$  described earlier, but rather a system which exhibits a subset of the behaviors of the full model. Such a subset can be defined by using a *Scenario*.

A *Scenario* is a multi-set of processes.  $\mathcal{S}$  denotes the set of all possible scenarios and let  $\mathcal{S}_c$  denote the set of *concrete scenarios* in which no unspecified agents ( $\_$ ) occur. We write  $\{\{a, a, b\}\}$  to denote the multi-set containing the element  $a$  twice, and  $b$  once.

**Definition 2 (Scen).** *Let  $S$  be a scenario. Then,*

$$\text{Scen}(S) = \text{Intruder} \parallel \prod_{p \in S} p .$$

In this paper we require that the processes in a scenario  $S$  do not contain the replication operator. Observe that where  $\text{Sys}(Q)$  always contains an unbounded number of replications,  $\text{Scen}(S)$  contains only the intruder processes and the processes specified in  $S$ .

A generalization of the *Scen* system is the repeated scenario system.

**Definition 3 (RepScen).** *RepScen( $S$ ) is defined for any scenario  $S$  as*

$$\text{RepScen}(S) = \text{Intruder} \parallel \prod_{p \in S} !p .$$

In contrast, a  $\text{MaxRuns}(Q, m)$  system is defined by a protocol  $Q$  and a maximum count  $m$ . (The name derives from the term “run” referring to a role instance.) Where the system  $\text{Sys}(Q)$  contains any number of replications of each role, the  $\text{MaxRuns}$  system contains only a finite number of replications of each role.

**Definition 4 (MaxRuns).** *Let  $Q$  be a protocol, and let  $m$  be a non-negative integer. Then,*

$$\text{MaxRuns}(Q, m) = \text{Intruder} \parallel \prod_{i=1}^m \left( \sum_{x \in \text{dom}(Q)} Q(x)(\_, \dots, \_) \right) .$$

## 2.3 Relations between state space restrictions

Each restriction from the previous section effectively restricts the state space of the process model. We focus on trace-based security properties such as secrecy and authentication. Hence, when talking about correctness of a protocol, we refer to the full set of possible behavior histories (traces) of the system, denoted by  $\text{tr}(\text{Sys}(Q))$ . As we will see in Section 4, most tools do not explore this set.

Let  $Q$  be a protocol. For the set of all possible scenarios  $\mathcal{S}$ , we have:

$$\forall m \in \mathbb{N} : \text{tr}(\text{MaxRuns}(Q, m)) \subset \text{tr}(\text{Sys}(Q)) \quad (1)$$

$$\forall s \in \mathcal{S} : \text{tr}(\text{Scen}(s)) \subset \text{tr}(\text{Sys}(Q)) \quad (2)$$

$$\forall s \in \mathcal{S} : \text{tr}(\text{RepScen}(s)) \subseteq \text{tr}(\text{Sys}(Q)) \quad (3)$$

$$\exists s \in \mathcal{S} : \text{tr}(\text{RepScen}(s)) = \text{tr}(\text{Sys}(Q)) \quad (4)$$

*Proof.* The relations (1), (2) and (3) above are immediate consequences of the definitions, as the left hand sides imply restrictions on the full set  $\text{tr}(\text{Sys}(Q))$ . For relation (4) we have that if the scenario  $s$  includes all possible process descriptions, the repetition of the processes in  $s$  effectively amounts to the full set of behaviors without any restrictions.

We write  $|s|$  to denote the number of elements of the scenario  $s$ . Relating the scenario-based approaches to the bounding of runs, we find:

$$\forall s \in \mathcal{S} : \text{tr}(\text{Scen}(s)) \subseteq \text{tr}(\text{MaxRuns}(Q, |s|)) \quad (5)$$

Observe that if the scenario contains  $|s|$  runs, the resulting traces will never contain more, and thus this is included in  $\text{MaxRuns}(Q, |s|)$ .

The next formula expresses that there exist no concrete scenarios that correspond exactly to a  $\text{MaxRuns}$  trace set.

$$\forall n \in \mathbb{N}^+ : \forall s \in \mathcal{S}_c : \text{tr}(\text{Scen}(s)) \neq \text{tr}(\text{MaxRuns}(Q, n)) \quad (6)$$

*Proof.* For any  $n > 0$ ,  $\text{tr}(\text{MaxRuns}(Q, n))$  contains a trace with  $n$  role processes. In particular, it will also contain a trace containing  $n$  instances of the first role, and also a trace containing  $n$  instances of the second role. To match  $\text{tr}(\text{MaxRuns}(Q, n))$  to  $\text{tr}(\text{Scen}(s))$ ,  $s$  must also contain exactly  $n$  role processes. Because we are considering only concrete scenarios, we need to define in  $s$  the first case ( $n$  times the first role). However, by this definition of  $s$  we have excluded the second type of traces with only the second role.

Assuming a finite number of agents,

$$\forall n \in \mathbb{N}, \exists k : \exists s_1, \dots, s_k \in \mathcal{S}_c : \bigcup_{i=1}^k \text{tr}(\text{Scen}(s_i)) = \text{tr}(\text{MaxRuns}(Q, n)) \quad (7)$$

The last formula expresses that for a finite set of agents, we can enumerate all possible scenario descriptions of  $n$  role processes, and turn them into scenario sets. The result of this formula is that we can match up the trace sets of  $\text{MaxRuns}$  and  $\text{Scen}$  by unfolding. This opens up a way to make the state spaces uniform.

### 3 Generation of uniform state spaces

Starting from a state space described using  $\text{MaxRuns}(Q, n)$  for an integer  $n$ , we generate a set of concrete scenarios that exactly covers the same state space, by using Formula (7). Further parameters involved in the generation of this set of scenarios are the number of roles of the protocol and the number of agents.

#### 3.1 Required number of agents

In protocol analysis it is common to use two honest agents and a single untrusted (compromised) agent. The underlying intuitions are that the security properties



under consideration are invariant under renaming of the (honest) agents, and that a single intruder is as strong as multiple colluding intruders. In general, attacks might require more agents, depending on the protocol under investigation and the exact property one wants to verify. A number of results related to this can be found with proofs in [17]. We recall the results of this paper as we will use them in the context of this paper.

- Only a single dishonest (compromised) agent  $e$ , needs to be considered for the analysis of the class of properties under consideration here.
- For the analysis of secrecy, only a single honest agent  $a$  is sufficient.
- For the analysis of authentication for protocols with two roles, we only need two honest agents  $a$  and  $b$ .

For example, for a single honest agent  $a$  and a single compromised agent  $e$ , for a protocol with roles  $\{r1, r2\}$ ,  $\text{tr}(\text{MaxRuns}(Q, 1))$  is equal to

$$\left( \bigcup_{k \in \{a, e\}} \text{tr}(\text{Scen}(\{\{r1(a, k)\}\})) \right) \cup \left( \bigcup_{k \in \{a, e\}} \text{tr}(\text{Scen}(\{\{r2(k, a)\}\})) \right),$$

which yields a set of four scenarios.

### 3.2 Computing the number of concrete scenarios

For a given integer  $n$ , we can derive the size of a set  $M$  of concrete scenarios, such that  $\bigcup_{s \in M} \text{tr}(s) = \text{tr}(\text{MaxRuns}(Q, n))$ . This size of  $M$  corresponds to the value of  $k$  in Formula (7) under the assumption of a finite number of agents and trace equivalence under renaming.

For a single agent (involved in the verification of secrecy), the generation of a set of concrete scenarios is a trivial application of the binomial coefficient. For two agents or more the situation is not so simple, because the generation of the set is complicated by the fact that scenarios are considered equivalent up to renaming of the honest agents.

*Example 1 (Renaming equivalence).* Let  $P$  be a protocol with a single role  $r1$ . Consider the state space  $\text{MaxRuns}(Q, 2)$  for two honest agents  $a, b$ . Consider the following scenario set:

$$\{ \{\{r1(a), r1(a)\}\}, \{\{r1(a), r1(b)\}\}, \{\{r1(b), r1(b)\}\} \}$$

Because the names of the honest agents are interchangeable, the last scenario is equivalent up to renaming to the first one. In order to verify security properties, we would need only to consider the first two scenarios.

We generalize this approach by considering  $|R|$  roles in the protocol description. We assume that we have two agents  $a$  and  $b$  and one intruder. Let  $n$  be the parameter of  $\text{MaxRuns}(Q, n)$  for which we want to generate the equivalent set of scenarios. In order to choose a run description  $X(a_1, \dots, a_{|R|})$ , we have  $|R|$  choices for the role  $X$ , two choices for  $a_1$   $a$  or  $b$  and 3 possible values:  $a$ ,  $b$  or

the attacker for each  $a_2, \dots, a_{|R|}$ , and we find there are  $2 * |R| * 3^{(|R|-1)}$  different possible run descriptions. Now we have to choose a multi-set of  $n$  run descriptions among this set of all possible runs descriptions. We use the following formula:

$$\binom{2 * |R| * 3^{(|R|-1)} + n - 1}{n}$$

However, this does not take into account that scenarios are equal up to the renaming of the (honest) agents. For example, we observe that  $\{\{r1(a, b), r2(b, a)\}\}$  is equivalent to  $\{\{r1(b, a), r2(a, b)\}\}$  under the renaming  $\{a \rightarrow b, b \rightarrow a\}$ .

We now use group theory results to compute the number of scenarios needed. We first consider the case with two agents and use Burnside's lemma [13] then for the other cases we need to consider Polya's Theorem which is a generalization of Burnside's Lemma. In the rest of this section, we detail the case for two agents using Burnside and Polya then we present the case of three agents with Polya to give a flavor of the general case by this method.

### 3.3 Theoretical result for two agents

We recall that  $\binom{n}{k} = \frac{n!}{k!(n-k)!}$  and Burnside's lemma [13].

**Lemma 1 (Burnside's lemma).** *Let  $G$  be a finite group that acts on a set  $X$ . For each  $g$  in  $G$  let  $X^g$  denote the set of elements in  $X$  that are fixed by  $g$ . Then the number of orbits, denoted  $|X/G|$ , is:*

$$|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$$

where  $|X|$  denotes the cardinality of the set  $X$ .

Thus the number of orbits (a natural number or infinity) is equal to the average number of points fixed by an element of  $G$  (which consequently is also a natural number or infinity). A simple proof of this lemma was proposed by Bogard [9].

We have to consider all the renamings and compute the number of scenarios that are stable by this operation. Because we have only two agents, we have only two possible renamings:

1.  $\sigma_{Id} = \{a \rightarrow a, b \rightarrow b\}$  (the trivial renaming)
2.  $\sigma_1 = \{a \rightarrow b, b \rightarrow a\}$

Observe first that  $|G| = 2$  because we have two renamings. In the first case, all elements are fixed so we have  $\binom{2 * |R| * 3^{(|R|-1)} + n - 1}{n}$  possibilities. In the second case, the fixed elements are multi-sets of the size  $n$  where the terms are associated by two and of their arguments are of the form  $a, x_1, \dots, x_{|R|-1}$  or  $b, x_1, \dots, x_{|R|-1}$ . It corresponds to choosing a multi-set of  $\frac{n}{2}$  elements in a set where the first parameter is fixed, i. e., in a set of cardinality  $|R| * 3^{(|R|-1)}$ . Notice that if  $n$  is odd the second set is empty because in this case there is no way to get a fixed element using the second renaming.

Lemma 1 leads to the following formula, where  $\epsilon_n$  is 0 if  $n$  is odd and 1 otherwise.  $k(n, |R|)$  is the number of scenarios  $k$  for Formula (7).

$$k(n, |R|) = \frac{\binom{2*|R|*3^{(|R|-1)}+n-1}{n} + \epsilon_n \binom{|R|*3^{(|R|-1)}+\frac{n}{2}-1}{\frac{n}{2}}}{2} \quad (8)$$

For instance for a protocol with  $|R| = 2$  roles, the set of traces of the process  $\text{MaxRuns}(Q, 2)$  is equal to the union of the trace sets defined by  $k(2, 2) = 42$  different scenarios.<sup>1</sup> Note that if we would not have taken the renaming equivalence into account, we would instead generate  $\binom{2*2*3^{2-1}+2-1}{2} = 78$  scenarios.

### 3.4 Generalization using Polya's Theorem

We first explain the theory needed for the application of Polya's Theorem in our context. We then sketch the case of two agents (we obtain of course the same result as when using Burnside's Lemma), after which we present the case of three agents to provide intuition for the general case of  $|A|$  agents.

**Theory** We note  $PP(R, A)$  the set  $R \times A \times (A \cup \{e\})^{|R|-1}$ , where  $e$  is the compromised agent. For a given  $n$ , let  $MPP(R, A, n)$  be the multi-sets of size  $n$  of elements of  $PP(R, A)$ . We wish to compute the number  $k(n, |R|)$ , the number of orbits of  $MPP(R, A, n)$  under the action of renaming the agents. We managed to solve this question directly in the case of two agents with the help of Burnside's theorem, but for a general  $A$  there is no direct way to know how many fixed points a given renaming has on  $MPP(R, A, n)$ . Hence we use Polya's theorem, which leads to a more complicated but automatic way of computing  $k(n, |R|)$ .

For  $\sigma$  a permutation of a set, we denote by  $c_i(\sigma)$  the number of cycles of length  $i$  (the length of a cycle is the minimal number of applications of the cycle to get the identity back).

Suppose we have sets  $D$  (of finite cardinality  $|D| = d$ ) and  $E$ , with  $G$  a group of permutations acting on  $D$ . Let  $E^D$  be the set of functions from  $D$  to  $E$ . We say that  $f, g \in E^D$  are equivalent if there exists  $\sigma \in G$  such that  $f(\sigma(d)) = g(d)$  for all  $d \in D$ , and we note  $\mathcal{F}$  a set of representatives of the equivalence classes. Now let  $w$  be a function from  $E$  to a certain commutative ring  $\mathbf{k}$ , and let the weight of  $f \in E^D$  be  $W(f) := \prod_{d \in D} w(f(d))$ . One notes easily that if  $f$  and  $g$  are equivalent, then  $W(f) = W(g)$ . We define  $W(\mathcal{F}) = \sum_{f \in \mathcal{F}} W(f)$ , and the *cycle indicator polynomial*  $P_G(x_1, \dots, x_d) = \frac{1}{|G|} \sum_{\sigma} x_1^{c_1(\sigma)} x_2^{c_2(\sigma)} \dots x_t^{c_d(\sigma)}$ .

Then we can state *Polya's theorem* [18, p.252]:

$$W(\mathcal{F}) = P_G \left( \sum_{y \in E} w(y), \sum_{y \in E} w(y)^2, \dots, \sum_{y \in E} w(y)^d \right) \quad (9)$$

<sup>1</sup> This scenario can be inspected by running 'Scenario.py' in the test archive [24].

Let us now consider the application in our context. If  $\sigma$  is a renaming (i.e. a permutation of  $A$ ), we define  $\phi(\sigma)$  as the permutation that is induced on  $PP(R, A)$ , which is  $\phi(\sigma)(r_i(a_1, \dots, a_{|R|})) := r_i(\sigma(a_1), \dots, \sigma(a_{|R|}))$ . In our case,  $D$  is the set  $PP(R, A)$ , on which the group of permutations  $G = \{\phi(\sigma)\}$  acts, and  $E$  is the set  $\mathbb{N}$  of nonnegative integers. Then, a multiset  $m \in MPP(R, A, n)$  is equivalent to a function  $f \in E^D$  with  $\sum_d f(d) = n$ : the integer  $f(d)$  is the number of occurrences of  $d$  in the multiset. Note that two multisets are equivalent up to renaming precisely when the corresponding functions  $f, g$  are equivalent in the sense of Polya's theorem.

Let  $\mathbf{k}$  be the ring of power series in the variable  $q$ , and define  $w : E \rightarrow \mathbf{k}$  by  $w(i) = q^i$ ; if  $f \in E^D$  is a multiset of size  $n$ , we get  $W(f) = \prod_d w(f(d)) = q^{\sum_d f(d)} = q^n$ . From this we deduce easily that  $W(\mathcal{F}) = \sum_n k(n, |R|)q^n$ . We notice also that  $\sum_{y \in E} w(y)^i = \sum_{j \in \mathbb{N}} q^{ij} = \frac{1}{1-q^i}$ . Then Polya's theorem (9), in our context, says that if we perform the substitutions  $x_i := \frac{1}{1-q^i}$  in  $P_G$  for all variables  $x_i$ , and expand the result in terms of powers of  $q$ , the coefficient of  $q^n$  is exactly  $k(n, |R|)$ . Let us explicit the cycle indicator polynomial here:

$$P = \frac{1}{|A|!} \sum_{\sigma} x_1^{c_1(\phi(\sigma))} x_2^{c_2(\phi(\sigma))} \dots x_t^{c_t(\phi(\sigma))}, \quad (10)$$

We finally need to a way to compute the integers  $c_i(\phi(\sigma))$ , which is what the following formulas achieve

$$c_i(\phi(\sigma)) = \frac{1}{i} \sum_{d|i} \mu\left(\frac{i}{d}\right) c_1(\phi(\sigma^d)) \quad \text{for } i > 1 \quad (11)$$

$$c_1(\phi(\sigma^d)) = |R| \cdot \left( \sum_{i|d} i c_i(\sigma) \right) \cdot \left( \sum_{i|d} i c_i(\sigma) + 1 \right)^{|R|-1} \quad (12)$$

The first one can be found for instance in [32, p.95] (it is an instance of the *Möbius inversion formula*), the second one is an easy counting of the fixed points of  $\phi(\sigma^d)$ . We recall that the Möbius function  $\mu(n)$  is defined for all positive integers  $n$  as follows:  $\mu(n) = (-1)^k$  if  $n$  is the product of  $k$  distinct primes, and  $\mu(n) = 0$  otherwise.

We are now able to express concretely the polynomial  $P$  for any number of agents. We remind the reader of the following results for computing with power series:

$$\begin{aligned} \left( \sum_{n=0}^{+\infty} a_n q^n \right) \cdot \left( \sum_{n=0}^{+\infty} b_n q^n \right) &= \sum_{n=0}^{+\infty} \left( \sum_{i=0}^n a_i b_{n-i} \right) q^n \\ \left( \frac{1}{1-q} \right)^i &= \sum_{j=0}^{\infty} \binom{i+j-1}{j} q^j \end{aligned}$$

We will explicit the result for the case of 2 agents, and sketch the case for 3 agents to get an explicit formula.

**Two agents** Consider now the case of 2 agents  $a$  and  $b$ , so that we have only two renamings:  $\sigma_{Id} = \{a \rightarrow a, b \rightarrow b\}$  and  $\sigma_1 = \{a \rightarrow b, b \rightarrow a\}$ .

We first compute the polynomial  $P$  of Equation (10): using the formulas for the  $c_k(\phi(\sigma))$ , we have  $c_1(\phi(\sigma_{Id})) = |R| \cdot 2 \cdot 3^{|R|-1}$ ,  $c_2(\phi(\sigma_{Id})) = 0$ ,  $c_1(\phi(\sigma_1)) = 0$ , and  $c_2(\phi(\sigma_1)) = |R| \cdot 3^{|R|-1}$ . Hence, if we substitute  $x_1 := \frac{1}{1-q}$  and  $x_2 := \frac{1}{1-q^2}$ , we obtain:

$$\begin{aligned} P &= \frac{1}{2} (x_1^{2 \cdot |R| \cdot 3^{|R|-1}} + x_2^{|R| \cdot 3^{|R|-1}}) \\ &= \frac{1}{2} (\sum_{i=0}^{\infty} (2 \cdot |R| \cdot 3^{|R|-1+i-1}) q^i + \sum_{i=0}^{\infty} (|R| \cdot 3^{|R|-1+i-1}) q^{2i}) \end{aligned}$$

Now  $k(n, |R|)$  is given by the coefficient of  $q^n$  in this expression, so we have to distinguish the cases  $n$  even and  $n$  odd, and we find indeed the same result as with Burnside's Lemma.

**Three agents** For three agents  $a, b$  and  $c$ , we have  $|PP(R, A)| = 3 \cdot |R| \cdot 4^{|R|-1}$ . There are  $3! = 6$  renamings, and for each of them we have to compute the corresponding term in  $P$ . For instance, if we take  $\sigma_1 = \{a \rightarrow b, b \rightarrow a, c \rightarrow c\}$ , we have  $c_1(\phi(\sigma_1)) = |R| \cdot 2^{|R|-1}$ ,  $c_2(\phi(\sigma_1)) = (|R| \cdot 3 \cdot 4^{|R|-1} - |R| \cdot 2^{|R|-1})/2$  and  $c_3(\phi(\sigma_1)) = 0$ , which gives the corresponding term in  $P$ . Proceeding in the same way for all other renamings, we get

$$P = \frac{1}{6} (x_1^{3|R| \cdot 4^{|R|-1}} + 3x_1^{|R| \cdot 2^{|R|-1}} x_2^{(3|R| \cdot 4^{|R|-1} - |R| \cdot 2^{|R|-1})/2} + 2x_3^{|R| \cdot 4^{|R|-1}})$$

We now substitute  $x_i = \frac{1}{1-q^i}$  for  $i = 1, 2, 3$ , and then take the coefficient of  $q^n$  to obtain the value of  $k(n, |R|)$ ; this is easily done by the rules for computing with power series given above, and the result is the following: let  $\alpha_n := \binom{3|R| \cdot 4^{|R|-1} + n - 1}{n}$ ,  $\beta_n := \sum_{l=0}^{\lfloor \frac{n}{2} \rfloor} \binom{(3|R| \cdot 4^{|R|-1} - |R| \cdot 2^{|R|-1})/2 + l - 1}{l} \cdot \binom{|R| \cdot 2^{|R|-1} + n - 2l - 1}{n - 2l}$ , where  $\lfloor \frac{n}{2} \rfloor$  denotes the integer part of  $n/2$ , and  $\gamma_{3i} = \binom{|R| \cdot 4^{|R|-1} + i - 1}{i}$ , while  $\gamma_n = 0$  if 3 does not divide  $n$ . Then we get the following result for three agents

$$k(n, |R|) = \frac{1}{6} (\alpha_n + 3\beta_n + 2\gamma_n)$$

The formula for  $k(n, |R|)$  can be constructed similarly for any number of agents.

### 3.5 Practical implications

In general, tools can explore radically different state spaces. With protocol analysis, we are looking for two possible results: finding attacks on a protocol or having some assurance of the correctness of the protocol. If an attack on a protocol is found, any unexplored parts of the state space are often considered of little interest. However, if one is trying to establish a level of assurance for the correctness of a protocol, the explored state space becomes of prime importance. As established in the previous section, even for two honest agents, the simplest protocols already need 42 concrete scenarios to explore exactly all attacks involving two runs.

In many cases, protocol models increase the coverage of small attacks (i. e. involving few runs) by including a scenario with a high number of runs. This process is error prone: as an example we mention that in the Avispa modeling [5] of the TLS protocol [41] a large scenario is used in the example files, which covers many small attacks, but not scenarios in which an agent can communicate with itself. As a result, the protocol is deemed correct by the Avispa tools, whereas other tools find an attack. This is a direct result of the fact that the used scenario does not cover all attacks for even a small number of runs. One can discuss the feasibility of such an attack, and argue that an agent would not start a session with herself, but the fact remains that the protocol specification does not exclude this behavior, and therefore certainly means that the protocol does not meet the security properties for its specification.

When one uses a tool for the analysis of a protocol one should be aware of the impact the state space choices have on the result of the analysis, in order to avoid getting a false sense of security from a tool.

## 4 Experiments

In this section we use the state space analysis of Section 2 to perform a comparison between several tools on a set of well-known cryptographic protocols considering the same state space. In our experiments we automatically generate the necessary concrete scenarios according to the results obtained in Section 3. We first discuss some of the choices made for these experiments, after which we give the results of the tests.

### 4.1 Settings

**Tool selection and method of comparison** We compared tools that are freely available for download and for which a Linux command-line version exists. Consequently, we had to exclude some tools, e. g., we do not consider Athena [44] or NRL [37] as these tools are not available, and we do not consider Hermes [12] because its current version only has a web interface, making it unsuitable for performance comparisons. The tools we compare are the following:

*Avispa* (Version: 1.1 for Automated Validation of Internet Security Protocols and Applications consists of the following four tools that take the same input language called HLPSL [2]:

- **CL-Atse:** (Version: 2.2-5) Constraint-Logic-based Attack Searcher applies constraint solving with simplification heuristics and redundancy elimination techniques [46].
- **OFMC:** (Version of 2006/02/13) The On-the-Fly Model-Checker employs symbolic techniques to perform protocol falsification as well as bounded analysis, by exploring the state space in a demand-driven way. OFMC implements a number of optimizations, including constraint reduction, which can be viewed as a form of partial order reduction [6].

- **Sat-MC:** (Version: 2.1, 3 April 2006) The SAT-based Model-Checker builds a propositional formula encoding all the possible traces (of bounded length) on the protocol and uses a SAT solver [4] (notice that you can modify some parameters and in particular the choice of the SAT solver in the configuration file of Sat-MC, we use the default configuration in our experiments).
- **TA4SP:** (Version of Avispa 1.1) Tree Automata based on Automatic Approximations for the Analysis of Security Protocols approximates the intruder knowledge by using regular tree languages and rewriting to produce under- and overapproximations [10].

The first three Avispa tools (CL-Atse, OFMC and Sat-MC) take a concrete scenario (as required by the HLP SL language) and consider all traces of  $\text{Scen}(s)$ . The last Avispa back-end, TA4SP, also takes a HLP SL scenario, but verifies the state space that considers any number of repetitions of the runs defined in the scenario, yielding  $\text{RepScen}(s)$ . TA4SP is based on overapproximations and hence might find false attacks. As no trace is ever reconstructed by TA4SP, the user has no indication of whether the output “attack” corresponds to a false or true attack. Furthermore, there is a “level” parameter that influences whether just to use the overapproximation (level = 0), or underapproximations of the overapproximation (level > 0). In the Avispa default setting only level 0 is explored by default, which in our test cases would have resulted in never finding any attacks, finding in 57% of all cases “inconclusive”, and in the remaining 43% “correct”. For our tests, we start at level 0 and increase the level parameter until it yields a result that is not “inconclusive”, or until we hit the time bound. This usage pattern is suggested both by the authors in [10] as well as by the output given by the back-end when used from the Avispa tool.

*ProVerif:* (Version: 1.13pl8) analyzes an unbounded number of runs by using over-approximation and represents protocols by Horn clauses. ProVerif [8] accepts two kind of input files: Horn clauses and a subset of the Pi-calculus. For uniformity with the other tools we choose to model protocols in the Pi-calculus, which is closer than HLP SL (Avispa input language) than Horn clauses. ProVerif takes a description of a set of processes, where each defined processes can be started any number of times. The tool uses an abstraction of fresh nonce generation, enabling it performs unbounded verification for a class of protocols. Given a protocol description, one of four things can happen. First, the tool can report that the property is false, and will yield an attack trace. Second, the property can be proven correct. Third, the tool reports that the property cannot be proved, for example when a false attack is found. Fourth, the tool might not terminate. It is possible to describe protocols in such a way that  $\text{RepScen}(s)$  is correctly modeled, resulting in the exploration of  $\text{Sys}(Q)$ .

*Scyther:* (Version: 1.0-beta6) verifies bounded and unbounded number of runs, using a symbolic backwards search based on patterns [22, 23]. Scyther does not require the input of scenarios. It explores  $\text{Sys}(Q)$  or  $\text{MaxRuns}(Q, n)$ : in the first case, even for small  $n$ , it can often draw conclusions for  $\text{Sys}(Q)$ . In the second

Tools	State spaces	Constraints
Avispa (CL-Atse, OFMC, Sat-MC)	Scen( $s$ )	$s \in \mathcal{S}_c$
Avispa (TA4SP)	RepScen( $s$ )	$s \in \mathcal{S}_c$
Casper/FDR	Scen( $s$ )	$s \in \mathcal{S}_c$
ProVerif	Scen( $s$ )	$s \in \mathcal{S}$
Scyther	MaxRuns( $Q, n$ ), Sys( $Q$ )	$n \in \mathbb{N}$

**Table 1.** State spaces explored by the tools

case, termination is not guaranteed. By default Scyther explores  $\text{MaxRuns}(Q, 5)$ , is guaranteed to terminate, and one of the following three situations can occur. First, the tool can establish that the property holds for  $\text{MaxRuns}(Q, 5)$  (but not necessarily for  $\text{Sys}(Q)$ ). Second, the property is false, yielding a counterexample. Third, the property can be proven correct for  $\text{Sys}(Q)$ .

*Casper/FDR:* (Version: Casper 1.11 alpha-release, FDR 2.83) [35, 43] This tool uses consists of the Casper tool, which translates protocol descriptions into the process algebra CSP [29], and the CSP model checker FDR [42]. [27] provides a time based analysis of using the tool for analyzing a large collection of existing protocols. Lowe used Casper/FDR to find the man-in-the-middle attack on the Needham-Schroeder protocol [33].

A summary of the tools and their respective state spaces is given in Table 1.<sup>2</sup> In order to compare the tools fairly, we match up the state spaces. As a candidate for a common state space, any unbounded set ( $\text{Sys}(Q)$ ,  $\text{RepScen}$ ) is not suitable. Furthermore, as  $\text{Scen}$  can be used to simulate  $\text{MaxRuns}$ , but not the other way around, we choose  $\text{MaxRuns}$  as the common denominator of the selected tools. We automatically generate for each number of runs  $n$  the corresponding input files to perform a fair time comparison over  $\text{MaxRuns}(Q, n)$ . Note that the time measurements for the tools only include their actual running times, and does not include the time needed for the generation of the input files.

**Security properties** We consider the analysis of secrecy as well as authentication. Secrecy can be modeled in each of the tools considered. Authentication cannot be modeled by TA4SP. The tools provide support for various security properties, ranging from several forms of agreement [34] to synchronization [25], or equivalence-based properties (ProVerif).

**Protocol test set** We consider a number of well-known protocols found in the literature [5, 14, 16, 31]. We select a set that can be modeled in all tools, which excludes protocols that use e.g. algebraic properties. We have restricted ourselves to the following four protocols: the famous Needham-Schroeder [40] using public

<sup>2</sup> Note that the constraint for the Avispa tools is partly driven by its input language HLPSL. For example, OFMC is able to analyze  $s \in \mathcal{S}$  by modeling protocols in the IF language, which we do not consider here.



keys, and the corrected version by Lowe [33], EKE [7] which uses symmetric and asymmetric encryption, and finally TLS [41] as an example of a larger protocol.

**Final setup details** With respect to the analysis of multiple properties, we remark that some tools can test multiple properties at once, some cannot, and some stop the analysis at the first property for which an attack is found. We choose to analyze one security property at a time.

Guided by our results of the previous section, we automatically construct input files for the right scenarios for each protocol and for each tool. This involves the generation of all concrete scenarios to match the state space of a given number of runs. To this end we generate all scenarios (ignoring renaming equivalence) in the first phase, and filter out scenarios that are equivalent under renaming in the second phase. The number of generated scenarios is identical to the theoretical number computed in the previous section.

Our tests can be reproduced: all used scripts and models are downloadable from [24], and we have only used freely downloadable tools and well-known protocols. The tests have been performed using an Intel Core Duo processor, 2.0 GHz, with 1GB of ram using the Linux operating system.

## 4.2 Results

We use each tool to verify security properties of the selected protocols. In the first set of results we present the total analysis time, which corresponds to the total time needed for verifying all the properties of each protocol, for each tool. When a tool reaches the time limit, no conclusion can be drawn about the analysis time and hence no points (and connecting lines) are displayed for such cases. For a better visualization of the exponential behavior of some of the tools, we use a logarithmic scale.

We start our discussion of the results by presenting and analyzing the tests for secrecy for all tools. Afterwards we continue with the results for authentication for all tools which can deal with this property. Finally, we show a table which summarizes the unbounded verification performance for the tools which are able to deal with an unbounded number of runs, and the attack discovery performance for all tools.

**Secrecy time results** In Figure 3, we show the analysis time for the secrecy properties of the Needham-Schroeder-Lowe protocol (NSL3) as a function of the number of runs  $n$  of the state space explored, that is,  $\text{MaxRuns}(\text{NSL3}, n)$ .

We observe that (as expected from the underlying models) ProVerif and TA4SP follow a constant time. Surprisingly Scyther has the same curve as ProVerif (close to the x-axis). Sat-MC, OFMC and CL-Atse follow an exponential curve, where in this case CL-Atse is faster than OFMC. One other interesting point is that the curves of OFMC and Casper/FDR cross the Sat-MC curve: in other words, for larger numbers of runs, Sat-MC is more efficient. This result is confirmed by the results for the EKE protocol, which we show below. One final

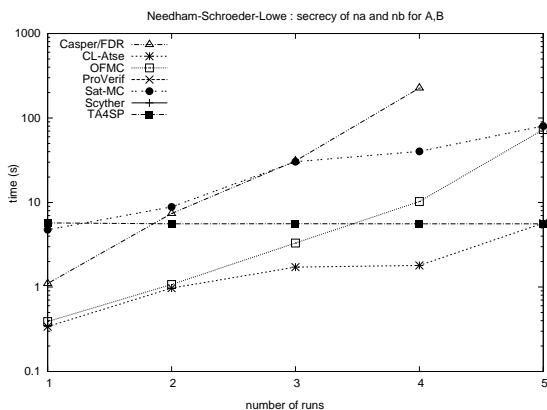


Fig. 3. Time efficiency comparison for Needham-Schroeder-Lowe [33], for secrecy

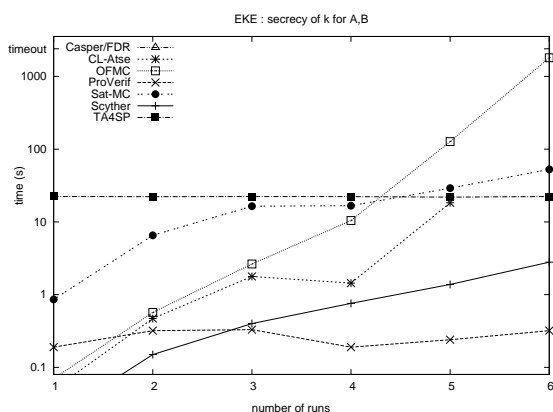


Fig. 4. Time efficiency comparison for EKE [7], secrecy

point to mention is that Scyther and ProVerif both show time performances of less than one second for all the security properties considered for this protocol. We also remark that Casper/FDR has an exponential curve and is slower than OFMC and CL-Atse, but faster than Sat-MC for a small number of runs.

In Figure 4, we present the efficiency results for the EKE protocol [7]. This protocol shows again that the bounded analysis tools (Sat-MC, OFMC, CL-Atse) follow an exponential curve, as well as the hybrid Scyther, which has for this particular protocol also an exponential curve, albeit with much lower times than the other bounded tools. We also observe that Sat-MC has a slower exponential curve than OFMC and CL-Atse. ProVerif is still constant (here fluctuations are due to millisecond noise during testing). We also notice that TA4SP has a constant analysis time but with an high time computation even for one process. This is due to the modeling of the protocol and to the fact that TA4SP has to construct in all cases of this protocol a complex tree automaton to perform its

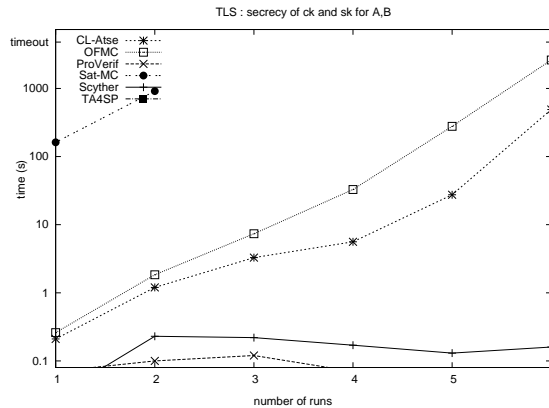


Fig. 5. Time efficiency comparison for TLS [41], secrecy

analysis. For this protocol, Casper/FDR already exceeds the time limit for the smallest state space.

The last protocol analyzed with respect to secrecy is presented in Figure 5. TLS [41] is a relatively complex protocol, and certainly the most complex protocol in this small test set. Hence, we expected the tools to spend some effort and time to get to a result. Our hypothesis was confirmed, as e.g. Sat-MC reaches the time limit for a fairly small state space. In this example, as in the previous one (EKE), we can also see the difference between OFMC and CL-Atse, where in this example CL-Atse is faster than OFMC. This protocol also confirms the results of Scyther which remains competitive with ProVerif and TA4SP. These three tools have all very fast time results and the variations on the curves are very small (less than 0.1 second).

**Authentication time results** In this section we present the results for the tools which can deal with authentication properties of the selected protocols.

In Figure 6, we analyze the performance of for authentication properties of the Needham-Schroeder protocol. ProVerif and Scyther are faster than the other tools used (results close zero second). Casper/FDR, CL-Atse and OFMC are very close and follow an exponential curve, with a minor advantage for Casper/FDR for a small number of runs.

In Figure 7, we see that the tools stop after having found an attack, which explains the flat shape for CL-Atse. In case of OFMC, there is still an exponential curve although an attack is found. We conjecture that this is caused by the specifics of the partial order reduction scheme, which effectively work like a heuristic: sometimes a non-optimal choice is made, causing the tool to explore a larger part of state space before the attack is found. The same explanation is valid for the smooth increasing of the Sat-MC curve towards the time limit. In this case Scyther is the fastest tool. ProVerif has constant time and is slower than all others for a small number of runs for this property of EKE.

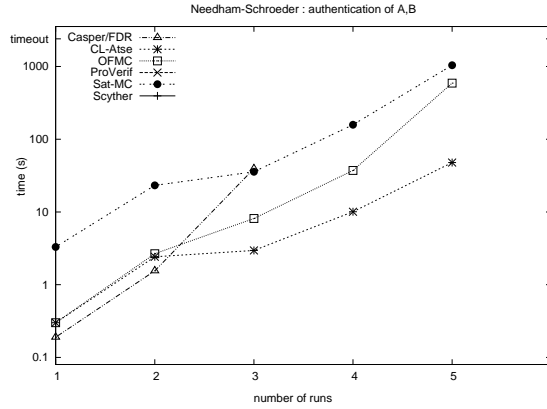


Fig. 6. Time efficiency comparison for Needham-Schroeder [40], authentication

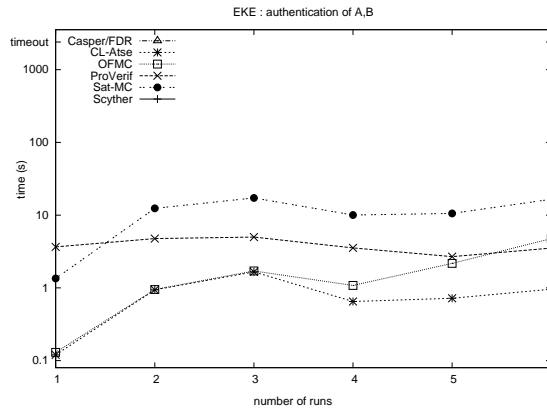


Fig. 7. Time efficiency comparison for EKE [7], for authentication

In Figure 8, we observe that Scyther is the most efficient with times of less than one second. For TLS we have that Sat-MC reaches the time limit for the two authentication claims when analyzed for one run, but quickly finds a flaw for state spaces with least two runs. For OFMC and CL-Atse we again observe very similar time results.

## 5 Results and discussion

We summarize the efficiency of finding attacks on the secrecy properties of the Needham-Schroeder protocol in Table 2. Next, we present a verification comparison for the tools capable of unbounded verification in Table 3. Finally we draw conclusions from our performance analysis.

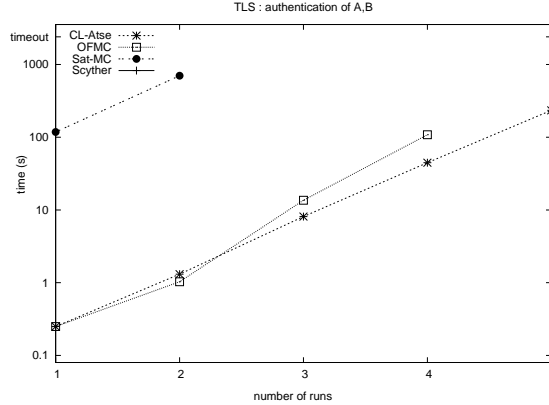


Fig. 8. Time efficiency comparison for TLS [41], for authentication

Secrecy	CL-Atse	Casper/FDR	OFMC	ProVerif	Sat-MC	Scyther	TA4SP
A na	no att	no att	no att	no att	no att	no att	no att
A nb	no att	no att	no att	0.00 (1!)	no att	no att	1.44 (1?)
B na	0.18 (2!)	0.65 (2!)	0.25 (2!)	0.00 (1!)	2.36 (2!)	0.00 (2!)	0.47 (1?)
B nb	0.25 (2!)	0.47 (2!)	0.24 (2!)	0.00 (1!)	2.34 (2!)	0.00 (2!)	0.47 (1?)

Table 2. Finding an attack on Needham-Schroeder for secrecy

**Comparison of attack finding efficiency** We first introduce the notation used in the Table 2: “no att” means the tool finds no attack, 0.12(2!) means that the tool finds an attack in 0.12 seconds with two processes, and 0.13(1?) means that the tool finds an attack in 0.13 seconds with two processes, but it might represent a false attack.

First we notice that ProVerif finds an attack on role *A* for the nonce *Nb*. If we use Scyther with the specific option (`-untyped`), the existence of the attack is confirmed. As we use the tools with their default setting, it is expected that some tools do not find this flaw. Unfortunately we have no way of knowing what the attack found by TA4SP looks like. This is an interesting result, because according to the specification of this tool it used a typed model as dictated by the HLPSL input specification, so the type flaw attack should not occur, and we would expect TA4SP not to find an attack. However, as we have no way to extract the TA4SP “attack” we assume it is a false attack in this case.

Second we can see that with our modeling, and using the results from [17] which state that considering one honest agent is sufficient for the analysis of secrecy, ProVerif can quickly find attacks. All the other tools need two runs to find the man-in-the middle attack, as expected.

Finally we find again our conclusion regarding efficiency that Scyther and ProVerif are the fastest, then TA4SP (but the status of the attacks remains unconfirmed), then CL-Atse and OFMC are second with a very small advantage

	Secrecy	ProVerif	Scyther	TA4SP
EKE	A k	0.07 (1)	-	11.16 (1)
	B k	0.12 (1)	-	11.20 (1)
Needham-Schroeder	A na	0.00 (1)	0.00 (3)	1.92 (1)
	A nb	attack!	0.00 (3)	attack?
	B na	attack!	attack!	attack?
	B nb	attack!	attack!	attack?
Needham-Schroeder-Lowe	A na	0.00 (1)	0.00 (3)	1.70 (1)
	A nb	0.00 (1)	0.00 (3)	1.85 (1)
	B na	0.00 (1)	0.00 (4)	attack?
	B nb	0.00 (1)	0.00 (3)	1.71 (1)
TLS	A ck	0.02 (1)	0.07 (2)	inconclusive
	A sk	0.01 (1)	0.06 (2)	inconclusive
	B ck	0.02 (1)	0.04 (2)	inconclusive
	B sk	0.02 (1)	0.06 (2)	inconclusive

Table 3. Performance of unbounded verification

to CL-Atse (which has been confirmed in the previous analysis with more runs), then Casper/FDR and finally Sat-MC.

**Comparison of unbounded verification performance** In this part we analyze the performance of tools which are able to prove the correctness of a protocol. This includes Scyther, ProVerif and TA4SP, where we have considered only the secrecy properties. We perform this analysis on the four selected protocols, and detail the results in Table 3. With respect to the used notation, we mention that 0.12(3!) denotes the fact that the tool proves the correctness of the protocol with 3 runs in 0.12 seconds, *attack?* means that the tool claims to find an attack (but which we could not check), *-* means that there is no answer for our testing, *inconclusive* is only for TA4SP, indicating that the tool does not state anything about the property. For TLS, TA4SP was not able to provide any answers. For EKE, Scyther could not establish unbounded verification, and provided bounded analysis for  $\text{MaxRuns}(Q, 7)$ .

**Time performance analysis conclusions** This time performance analysis shows that overall, the fastest tool is ProVerif, then Scyther, TA4SP, CL-Atse, OFMC, Casper/FDR and finally Sat-MC.

*ProVerif.* ProVerif shows the fastest performance. The abstraction of nonces allows the tool to obtain an efficient verification result quickly for an unbounded number of runs. The results for EKE in Figure 4 indicate that ProVerif does not support equational theories very well. In this case the resolution generates much more Horn clauses than in the case without equational theory. To confirm the efficiency of ProVerif, we performed a comparison with Scyther for the  $f^n g^n$  family of protocols from [38]. Members of this family are generated by an integer

parameter, corresponding to the number of instances required for an attack on the protocol. As a result, the complexity of verifying the protocol is related to this parameter. For this protocol, the time results for ProVerif increase, but are lower than the ones for Scyther.

*Scyther.* Scyther outperforms the other bounded tools and can often achieve the same performance as tools based on abstraction methods. For some protocols, no full verification can be performed, and the tool exhibits exponential verification time with respect to the number of runs.

*OFMC/CL-Atse.* The behaviors of OFMC and CL-Atse are mostly similar for the tested protocols. We observe that the curves produced by these two tools are exponential, which confirms the theoretical results for their underlying algorithms. Finally we observe that for the tested protocols, CL-Atse is somewhat faster than OFMC for higher numbers of runs.

*Casper/FDR.* Casper/FDR exhibits, for all examples that we tried, exponential behavior. In general, the analysis is slower than CL-Atse and OFMC.

*Sat-MC.* Sat-MC also has an exponential behavior and is slower than CL-Atse and OFMC for lower numbers of runs. In particular, Sat-MC has proven to be especially slow for the more complex protocol TLS. In contrast, for the smaller protocols we found that Sat-MC starts slower, but its time curve is less steep than that of CL-Atse OFMC and Casper/FDR, causing the curves to cross for particular setups. Consequently, for some protocols and a high number of runs Sat-MC can be more efficient than CL-Atse and OFMC, which can be observed in the graphs for the EKE protocol. Our results are confirmed by the findings in [26, 45], where the analysis of the PKCS#11 API could only be performed by Sat-MC, and not by the other Avispa tools (personal communication).

*General observations.* During these tests we ran into many peculiarities of the selected tools. We highlight some of the issues we encountered. In general, the modeling phase has proven to be time-consuming and error-prone, even though we already knew the abstract protocols well. Modeling the protocols in ProVerif took us significantly more time than for the other tools. Furthermore, in the description files provided with the tool, there are several models of the Needham-Schroeder protocol, none of which considers all the possible interactions between the different principals, but only examples which model some particular scenarios. For our tests we contacted the author of ProVerif, who provided alternative models for our protocols in order to consider all traces (Note that all used input files are generated by the scripts that are downloadable from [24]).

Avispa has a common input language called HLPSL for the four back-end tools. This has the benefit of allowing the user to use different tools based on a single protocol modeling. However, in HLPSL, the link between agents and their keys is usually hard-coded in the scenarios, making the protocol descriptions

unsuitable for unbounded verification, as one cannot in general predict how these links should be for further role instances (outside of the given scenario).

Even in this limited test, we found two instances where TA4SP indicates that a property of a protocol is false, where we expected the property to hold, which may be due to the type of underapproximation used.

Of course, each of the tools has its particular strengths in other features than just performance on simple protocols. However, the focus of this research is clearly on the efficiency only. Furthermore, our tests involve only one particular efficiency measure, and there are certainly other efficiency measures (e.g. mapping all state spaces to symbolic scenarios, and many others) that we expect would lead to slightly different results. However, given that no research has ever been performed before on this topic, we see our tests as a base case for others to work from.

## 6 Conclusion

We analyze state space models in automatic security protocol analysis. Our analysis shows the relations between the various models, revealing that protocol analysis tools by default explore very different state spaces. This can lead to a false sense of security, because if a tool states that no attack is found, only the explored state space is considered, and other attacks might have been missed.

We match up the state spaces to ensure different tools explore similar state spaces, taking in to account that traces are considered equal up to renaming of honest agents. This leads to a result relating the number of concrete scenarios needed to cover all traces of a protocol involving a particular number of runs, by applying mathematical results like Burnside’s Lemma or Polyá’s theorem.

We compare the performance several automatic protocol analysis tools. We model four well-known protocols for each tool, and verify the protocols using the tools on similar state spaces to obtain a fair performance comparison. The resulting scripts and data analysis programs are available from [24].

The performance results show that overall, ProVerif is the fastest tool for this set of protocols. Scyther comes in as a very close second, and has the advantage of not using approximations. CL-Atse and OFMC (with concrete sessions) are close to each other, and are the most efficient of the Avispa tools, followed by Sat-MC. Casper/FDR has an exponential behavior and is slower than OFMC and CL-Atse but faster than Sat-MC for a small number of runs. For a higher number of runs of simple protocols, it seems that Sat-MC can become more efficient than the two other tools. In some cases TA4SP can complement the other Avispa tools, but in general it is significantly slower than the other tools that can handle unbounded verification (Scyther and ProVerif), and has the added drawback of not being able to show attack traces.

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