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Optimal Slot Opening Width for Magnetic Noise Reduction in Induction Motors

J. Le Besnerais, *Student Member, IEEE*, V. Lanfranchi, M. Hecquet, R. Romary, and P. Brochet, *Member, IEEE*

Abstract—This paper presents a method to characterize the main magnetic force waves occurring in a sinusoidally-fed induction machine. Three main force types are identified: slotting force waves, winding force waves and saturation force waves. Slotting force waves are characterized in terms of number of nodes, velocity, propagation direction and magnitude. On the ground of the expression of these forces magnitude, a method to cancel a given magnetic force wave by properly choosing the rotor slot or stator slot opening width is presented. This new method is validated with both simulations and experiments.

Contrary to the common design rule that advices to decrease rotor and stator slot openings width in order to reduce magnetic noise, it is shown that a wider slot opening can lower the global noise level when properly chosen.

Index Terms—Induction machine, magnetic noise, vibrations, Maxwell forces.

NOMENCLATURE

b_r	Rotor slot opening width
b_s	Stator slot opening width
d_f^r	Rotor fictitious slot depth
d_f^s	Stator fictitious slot depth
f_c	PWM switching frequency
f_s	Fundamental stator supply frequency
f_{mm}^s	Stator magnetomotive force
F_s	Stator mmf magnitude
g	Air-gap width
p	Number of pole pairs
P_r, P_s	Rotor and stator slotting permeance harmonics magnitude
s	Fundamental slip
Z_r	Number of rotor slots
Z_s	Number of stator slots
α_s	Angular position in stator steady frame
μ_0	Air-gap magnetic permeability
τ_r	Rotor slot pitch
τ_s	Stator slot pitch

I. INTRODUCTION

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AS acoustic comfort becomes increasingly important in electrical transport systems, and especially in subways and light-rail vehicles where both passengers and frontage residents are exposed to noise, the understanding of magnetic noise generation becomes crucial. This source of noise, mainly due to the air-gap radial Maxwell forces that excite the stator in the audible range [1], creates unpleasant tonalities that are penalized by IEC 60349-2 standard [2].

Active noise-reduction technique of current injection [3], [4], [5] is not able to cancel magnetic force harmonics of spatial order different from 0 and $2p$: as the elliptical stator mode is usually the one that radiates the most, this technique cannot be applied to traction motors with 2 or 3 pole pairs. Other active techniques generally require expensive control loops and electromechanical devices. There is therefore a special need to find some efficient low-noise rules that can be applied during the motor design stage. Closing rotor slots, enlarging the air-gap or skewing the rotor are techniques that efficiently decrease magnetic noise but also significantly degrade motor performances.

This paper first presents a way to analytically characterize the main sources of magnetic noise in sinusoidally-fed induction motors. Three main sources of magnetic vibrations are identified, due to air-gap slotting harmonics, stator magnetomotive force (mmf) harmonics, and saturation harmonics. Slotting vibrations characteristics are detailed, and experimentally validated by visualizing the stator stack deflections at some given frequencies. The expression of slotting magnetic forces magnitude is then derived, and it is shown that it can be canceled by properly choosing the rotor or the stator slot opening width in some sets of optimal values. To validate this effect, some simulation results are then presented, and a new rotor prototype is built and successfully tested.

II. MAGNETIC NOISE CHARACTERIZATION

A. Expression of radial Maxwell forces

Neglecting the tangential component of the Maxwell tensor and magnetostrictive effect, the radial exciting pressure P_M that is supposed to be responsible for magnetic noise can be approximated by [6], [7], [8]

$$P_M = B_g^2 / (2\mu_0) \quad (1)$$

where B_g is the radial air-gap flux density. Assuming that the rotor is not skewed, and neglecting end effects, this force is independent of the axial direction and can therefore only excite some circumferential modes of the stator stack, which can be modeled by an equivalent ring as a first approximation.

Developing the magnetic pressure (1) in two-dimensional Fourier series, it can be expressed as a sum of progressive force waves of time frequency f and space frequency m (also called spatial order):

$$P_M(t, \alpha_s) = \sum_{m,f} A_{mf} \cos(2\pi ft - m\alpha_s + \phi_{mf}) \quad (2)$$

A resonance occurs at two conditions [9]: the order of the force harmonic must be the same as the circumferential mode number of the stator, and the frequency of the force harmonic must be the same as the frequency of the natural frequency of the stator mode under consideration. The former condition is not reported in [10], but it is as important as the frequency match condition. In variable-speed motors, this frequency match condition is more easily satisfied as the frequencies of magnetic forces due to fundamental current vary proportionally to the supply frequency f_s , and therefore sweep a wide frequency range during starting and braking.

To predict resonances, one must therefore analytically calculate the Fourier development of P_M . It can be done using a permeance / mmf decomposition of the radial flux density [11], [12]. In the no-load case, this decomposition is given by

$$B_g = \Lambda f_{mm}^s = \frac{\mu_0}{g_f} f_{mm}^s \quad (3)$$

where g_f is the air-gap "magnetic length", i.e. the mean length of flux density lines that equals g , $g + d_f^s$, $g + d_f^r$ or $g + d_f^s + d_f^r$ according to the respective position of stator and rotor slots. The Fourier development of both permeance and mmf can be found in [13], [14], as well as the flux density spectrum resulting from their product, and the radial force spectrum obtained from the product of flux density harmonics.

B. Characterization of main Maxwell slotting harmonics

All these combinations give numerous force waves. However, the higher their spatial order is, the lower stator static deflection is [7]. Moreover, some of them have very low magnitude as they come from the multiplication of low magnitude harmonics (e.g. a high order mmf space harmonic combined with a high order permeance harmonics gives a very low flux density harmonic). Finally, some of these harmonics have low frequencies (less than 400 Hz), far from human's ear maximal sensitivity range.

Neglecting these force waves, one can find that they can be reduced to three main families assuming that currents are sinusoidal [15], [16]:

- 1) slotting force harmonics, coming from the interaction of some rotor and stator slotting permeance harmonics with twice the stator mmf fundamental (magnitude $P_s P_r F_s F_s / (2\mu_0)$)
- 2) "winding force" harmonics, coming from the interaction of some rotor and stator slotting permeance harmonics with the stator mmf fundamental, and with one stator mmf space harmonic (magnitude $P_s P_r F_s F_h / (2\mu_0)$)
- 3) saturation force harmonics, coming from the interaction of a slotting permeance harmonic with a saturation

permeance harmonic, and with the square stator mmf fundamental (magnitude $P_{sr} P_a F_s F_s / (2\mu_0)$)

Saturation of teeth indeed flattens the air-gap flux density, which modifies the space harmonic content of Maxwell forces, and can change magnetic noise level [7], [17]. This effect can be modeled by adding to the permeance function the additional permeance harmonics due to saturation with spatial order $2pk_a$, where k_a is a positive integer [11], [18], [19].

In a moderately saturated short-pitched induction machine, winding and saturation noise are negligible [16], and the main source of magnetic noise comes from slotting force harmonics. They can be represented by three families, whose characteristics (spatial orders and frequencies) are presented in Table I. All the frequencies of these force waves are here positive, so their propagation direction is encoded with negative spatial orders.

TABLE I
SLOTING FORCE HARMONICS CHARACTERIZATION.

Name	Frequency f	Spatial order m
F_{slot}^-	$f_s(k_r Z_r(1-s)/p - 2)$	$k_r Z_r - k_s Z_s - 2p$
F_{slot}^0	$f_s(k_r Z_r(1-s)/p)$	$k_r Z_r - k_s Z_s$
F_{slot}^+	$f_s(k_r Z_r(1-s)/p + 2)$	$k_r Z_r - k_s Z_s + 2p$

k_r and k_s are strictly positive integers appearing in the Fourier series of permeance distribution: they respectively account for rotor slotting and stator slotting. The three families F_{slot}^- , F_{slot}^0 and F_{slot}^+ therefore stand for an infinite number of force harmonics, but the higher are k_r and k_s , the lower are rotor and stator slotting permeance harmonics, and the lower is the corresponding force harmonic. The highest magnitude force harmonics are given by $k_s = k_r = 1$, but they do not necessarily create high vibrations as their associated order $m = k_r Z_r - k_s Z_s \pm 0, 2p$ can be very high. Note that as the only rotating part is the rotor, k_s and Z_s do not appear in the frequency expression of slotting force harmonics.

The force waves magnitude F_{slot}^- and F_{slot}^+ are the same, but F_{slot}^0 force waves are twice higher as they represent the interaction of two different force waves of frequencies $f_s(k_r Z_r(1-s)/p + 1 - 1)$ and $f_s(k_r Z_r(1-s)/p - 1 + 1)$ [16]. However, their magnitude F_{slot} is always proportional to [14], [20]

$$F_{slot} \propto P_s P_r \propto \frac{\sin(\pi k_r s l_r)}{k_r} \frac{\sin(\pi k_s s l_s)}{k_s} \quad (4)$$

where the slotting ratios $s l_s$ and $s l_r$ are given by

$$s l_s = 1 - \frac{b_s}{\tau_s} \quad s l_r = 1 - \frac{b_r}{\tau_r} \quad (5)$$

All these force waves characteristics have been validated by experimentally visualizing the stator stack deflection at a given frequency [21]. As an example, a motor with $Z_s = 27$, $Z_r = 21$ and $p = 2$ creates a slotting Maxwell force harmonic for $k_s = k_r = 1$ of order $Z_r - Z_s + 2p = -2$ with frequency $f_s(Z_r(1-s)/p - 2)$. This was validated by measuring the acceleration of 16 points around the stator median circumference, when feeding the motor with 50 Hz sinusoidal currents, and visualizing the operational deflection shape of the stator

with Pulse Labshop at frequency $f_s(Z_r(1-s)/p-2) \approx 375$ Hz (Fig. 1).

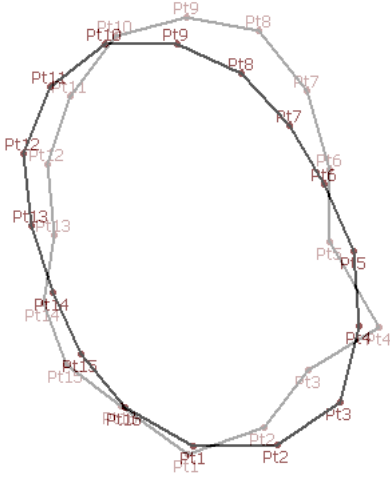


Fig. 1. Stator deflection of order $-2 = Z_r - Z_s + 2p$ due to a slotting vibration. The grey deflection stands for a previous time, showing that the vibration wave travels in counter-clockwise direction as its spatial order is negative.

III. MAGNETIC NOISE REDUCTION TECHNIQUE

A. Principle

Two methods can be used to avoid high levels of magnetic noise: the first one consists in avoiding resonances between the exciting forces and the excited structure, by properly choosing the slot combinations that have an influence on both the exciting force frequencies and spatial orders (cf. Table I). This is what is done for instance in [17] for magnetic noise due to saturation harmonics. A second method consists in reducing the exciting forces magnitude by choosing properly the slot geometry. In this paper, it is assumed that the designer has already chosen the motor slot numbers, and wants to reduce the magnitude of the existing slotting magnetic forces.

Once a low-order slotting force harmonic linked to integers k_{r0} and k_{s0} is known to possibly resonate with the corresponding stator mode, it is possible to cancel its magnitude by properly choosing the rotor or stator slot opening value. Equation (4) indeed contains sine functions that can equal zero if

$$k_{r0}sl_r = i_0 \quad \text{or} \quad k_{s0}sl_s = j_0 \quad (6)$$

where i_0 and j_0 are non-zero relative integers. It is theoretically sufficient to cancel either P_r or P_s permeance harmonic magnitude, but the designer can try to cancel both in order to make the design more robust, in particular to minimize the effect of manufacturing errors. It is easier to fulfill both conditions when designing a new motor from scratch : when trying to minimize magnetic noise of a given motor, manufacturing a new rotor is less expensive, and the aimed equality is then reduced to $k_{r0}sl_r = i_0$.

If two dangerous slotting force harmonics are identified linked to integers (k_{r0}, k_{s0}) and (k_{r1}, k_{s1}) , the designer can also optimize the stator slot geometry in order to obtain the condition $k_{s0}sl_s = j_0$ that cancels the first vibration, and independently choose the rotor geometry to obtain the condition $k_{r1}sl_r = j_1$, so that the second vibration is canceled.

To precise these conditions, as sl_r and sl_s values lie between 0 and 1, they can be expressed as

$$b_r = \tau_r \left(1 - \frac{i_0}{k_{r0}}\right), \quad i_0 \in [1, k_{r0} - 1] \quad (7)$$

and

$$b_s = \tau_s \left(1 - \frac{j_0}{k_{s0}}\right), \quad j_0 \in [1, k_{s0} - 1] \quad (8)$$

For $k_{r0} = k_{s0} = 1$, there does not exist any slot opening values canceling the slotting vibration, apart the particular cases of $sl_r = 0$ or $sl_s = 0$ (no rotor or stator teeth), and $sl_r = 1$ or $sl_s = 1$ (fully closed rotor or stator slots). This technique is only applicable when $k_{r0} \geq 2$ or $k_{s0} \geq 2$, which is the more common case. Note that this technique gives a set of optimal slot opening values, which allows the designer choosing among these best values. However, the lower k_{r0} and k_{s0} are, the higher is the slotting vibration magnitude to reduce, and the smaller are the numbers of optimal slot opening values.

This technique can lead to relatively wide slot opening values, especially when k_{s0} and k_{r0} are low, as

$$b_r \geq \tau_r/k_{r0} \quad b_s \geq \tau_s/k_{s0} \quad (9)$$

Consequently, the reduction of a slotting vibration on a given motor can lead to wider slot opening widths, which increases some other slotting vibrations magnitude. The technique must therefore be applied to the noisiest slotting vibration in order to be sure that the enlargement of slot opening widths up to the smallest optimal value will globally reduce magnetic noise.

At the rotor, the smallest optimal value of slot opening is given by

$$b_r^{opt} = \tau_r/k_{r0} \quad (10)$$

This configuration is illustrated in Fig. 2 for trapezoidal semi-closed rotor slots, a slot geometry often used in traction motors. Notice that equation (10) also cancels all the slotting vibrations linked to k_r that are multiples of k_{r0} as $sl_r k_{r0}$ becomes an integer.

Assuming that stator slots are opened rectangular slots (as used in railway traction application, where nominal output power lie between 150 and 250 kW), the best stator slot opening optimal value is not the smallest one because enough room must be left for windings. The ratio between air and iron in stator slotting is generally close to one, i.e. $b_s \approx \tau_s/2$. If k_{s0} is even ($k_{s0} = 2m_{s0}$), one can easily see that the optimal value of stator slot opening can be reached by $j_0 = m_{s0}$ and give

$$b_s^{opt} = \tau_s/2 \quad (11)$$

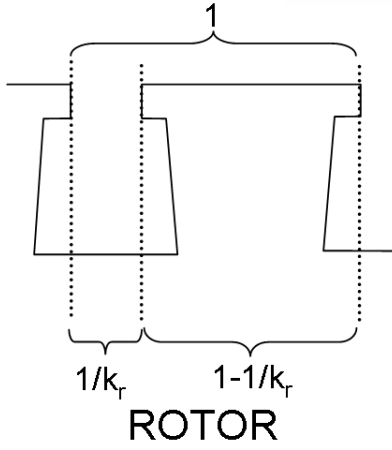


Fig. 2. Illustration of the smallest optimal rotor slot opening value cancelling a slotting vibration linked to the rotor permeance slotting harmonic number k_r ($k_r = 4$ is used in this example).

Similarly to rotor slot case, if $b_s = \tau_s/2$, all the slotting harmonics linked to even k_{s0} are automatically canceled as $sl_s k_{s0}$ is an integer. Such a configuration is illustrated in Fig. 3.

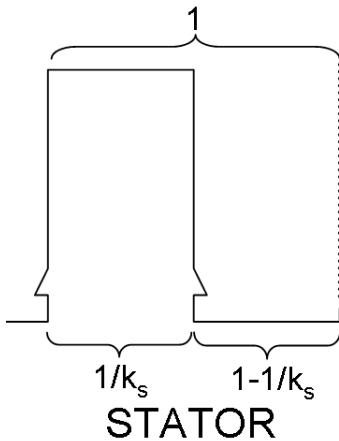


Fig. 3. Illustration of the smallest optimal stator slot opening value canceling a slotting vibration linked to the stator permeance slotting harmonic number k_s ($k_s = 2$ is used in this example, it also gives a unitary air/iron ratio that cancels all the slotting harmonics linked to even k_s).

On the contrary, if k_{s0} is odd ($k_{s0} = 2m_{s0} + 1$), one can see that the two optimal opening width values that give an air/iron ratio the closest from the unity are

$$b_s^{opt1} = \tau_s \frac{m_{s0}}{k_{s0}}, \quad b_s^{opt2} = \tau_s \frac{m_{s0} + 1}{k_{s0}} \quad (12)$$

If possible, the smallest value b_s^{opt1} is the best one as it limits the other slotting harmonics magnitude. If the designer does not want the closest air/iron ratio to one at the stator, and needs more room for winding, he can use some wider stator slot optimal widths, but he must be aware that it will make stator teeth thinner, enlarging tangential magnetic vibrations [22]. Some stiffer wedges are then recommended in order to limit these new vibrations.

The choice of rotor and stator slot opening value for magnetic noise reduction has also an influence on slot leakage flux. Nevertheless, as explained before, the strongest magnetic noise lines are associated to low k_{r0} and k_{s0} , leading to relatively wide optimal slot openings, so that magnetic noise and slot leakage can be both reduced: the proposed technique does not penalize the motor starting torque and current.

B. Numerical simulation

In this part are presented some simulation results using a simulation tool called DIVA [14], which is able to determine the acoustic noise of magnetic source emitted by an induction machine. This vibro-acoustic simulation software has been already validated on several motors [16], [23], [21], [24], [25].

Let's consider an induction machine with $Z_s = 48$, $Z_r = 36$ and $p = 2$. By computing all the slotting vibrations for k_r and k_s going from 1 to 10, one can find the only low-order slotting vibrations of Table II.

TABLE II
MAIN SLOTTING FORCE HARMONICS CHARACTERIZATION FOR $Z_s = 48$,
 $Z_r = 36$ AND $p = 2$.

Name	k_r	k_s	f	m
F_{slot}^-	4	3	$f_s(4Z_r(1-s)/p - 2)$	$-4 = 4Z_r - 3Z_s - 2p$
F_{slot}^0	4	3	$f_s(4Z_r(1-s)/p)$	$0 = 4Z_r - 3Z_s$
F_{slot}^+	4	3	$f_s(4Z_r(1-s)/p + 2)$	$4 = 4Z_r - 3Z_s + 2p$
F_{slot}^-	8	6	$f_s(8Z_r(1-s)/p - 2)$	$-4 = 8Z_r - 6Z_s - 2p$
F_{slot}^0	8	6	$f_s(8Z_r(1-s)/p)$	$0 = 8Z_r - 6Z_s$
F_{slot}^+	8	6	$f_s(8Z_r(1-s)/p + 2)$	$4 = 8Z_r - 6Z_s + 2p$

In that example, we can see that all the slotting vibrations are linked with k_r multiples of 4. All these lines can be theoretically canceled by choosing b_r according to equation (10), i.e. with $b_r = \tau_r/4$ (cf. Fig. 2). This fact has been checked by simulations, comparing the noise spectrum radiated by an induction with a non-optimal rotor slot opening ($\tau_r = 26$ mm, $b_r = 3.5$ mm) with a new one where the rotor slot opening width has been changed according to equation (10) ($\tau_r = 26$ mm, $b_r = 6.5$ mm). Results are displayed in Fig. 4, where the chosen supply frequency creates a resonance between the exciting slotting force harmonic F_{slot}^0 and the stator breathing mode number 0: main slotting lines are canceled in agreement with theory, decreasing the global magnetic noise of 20 dB, and the other magnetic noise spectrum lines are slightly increased due to a larger rotor slot opening. This technique therefore significantly decreases magnetic noise level at resonance.

Some other simulations have been run in order to quantify how much errors on the optimal slot opening value affect the magnetic sound power level. The sensitivity of the optimal b_r value is illustrated in Fig. 5, where the noise associated to the slotting line F_{slot}^0 ($k_{s0} = 3$, $k_{r0} = 4$) has been computed in function of b_r . We can see that a 5% error on the optimal value higher the noise level from 0 to 57 dB, the maximum noise level being 73 dB. Such an error can be relativised as a magnetic noise line inferior to 60 dB may be covered by some higher magnetic lines, ambient noise or other sources of noise (fan noise, gearbox noise, etc).

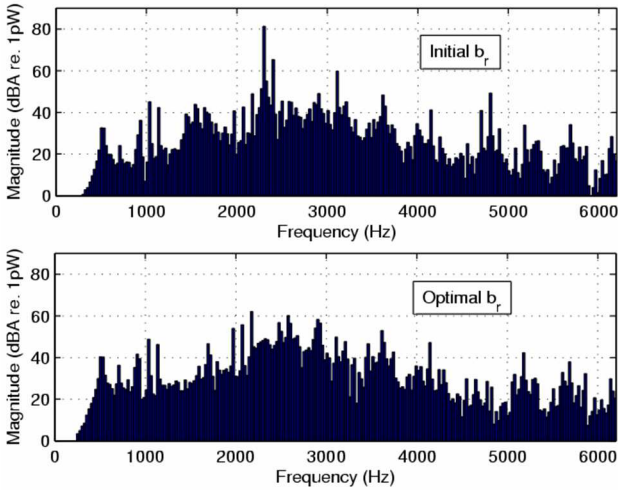


Fig. 4. A-weighted sound pressure level spectrum, for the initial rotor slot opening value (upper figure) and the optimal value (lower figure).

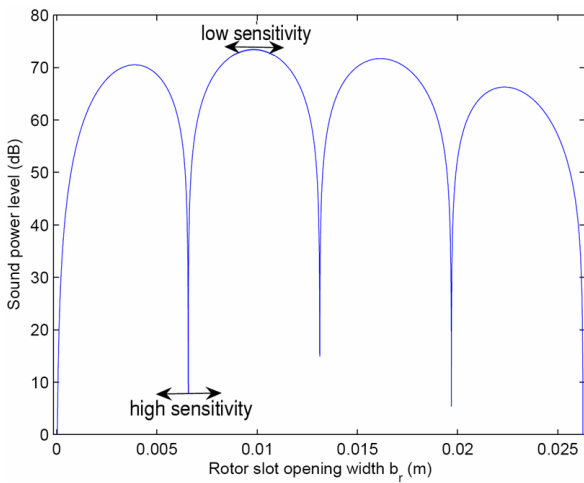


Fig. 5. Sound power level radiated by the slotting line F_{slot}^0 associated to $k_{s0} = 3$ and $k_{r0} = 4$ in function of the rotor slot opening b_r varying from 0 to τ_r . The second to the fourth local minimums correspond to the three b_r values of equation (7); they do not totally cancel noise due to the finite discretization step used for b_r in simulations.

C. Experimental validation

A new rotor with $b_r = 6.5$ mm has been built to check the efficiency of this technique. In agreement with simulations, the main slotting lines identified in Table II were the largest lines observed in the acoustic spectrum. Moreover, they were very low (≈ 55 dBA for the three slotting lines linked to $k_r = 4$ and $k_s = 3$, close to the ambient noise level), showing that the technique has successfully weakened the aimed slotting vibrations.

Slotting lines were not completely canceled due to saturation effects that tend to enlarge the rotor slot openings. Consequently, the optimal value of equation (10) should be slightly underestimated to account for saturation effect. This effect can be quantified using for instance the analytical law proposed in [26].

Some other acoustic tests have been run feeding the motor with asynchronous Pulse-Width Modulation (PWM) at

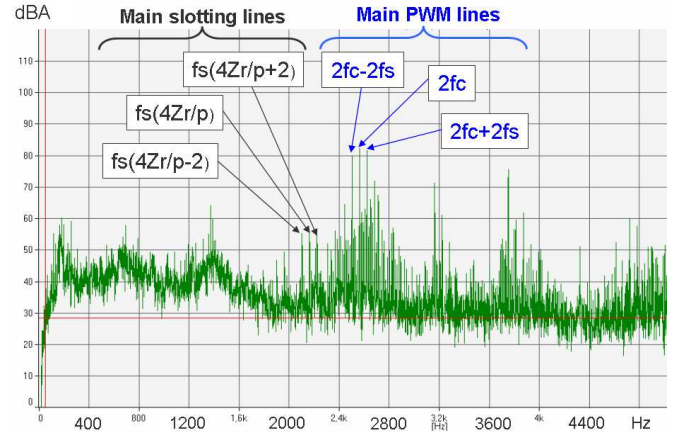


Fig. 6. Sound pressure level spectrum of new prototype with $b_r = 6.5$ mm (asynchronous PWM at 1280 Hz, $s \approx 0$).

$f_c = 1280$ Hz switching frequency. PWM enriches the Maxwell force spectrum by adding current harmonics; as the fundamental current remains unchanged, magnetic noise due to PWM is always superior to magnetic noise in sinusoidal case.

In our experiments, it was observed that PWM acoustic lines completely dominate the overall sound power level (see Fig. 6 where canceled slotting lines only reach 55 dBA, in agreement with a 5% error on b_r optimal value as shown by simulations): slotting lines have been significantly reduced, and the only significant lines near $2f_c$ and $4f_c$ frequencies are due to PWM [15]. Other lines at f_c , $3f_c$ are also linked due to PWM, as well as the line near 3200 Hz that comes from the combination between slotting and PWM harmonics [16], [21].

The differences between Fig. 6 experimental spectrum and Fig. 4 simulation results are mainly explained by the mechanical, aerodynamic, ambient noise and PWM noise due to switching harmonics in experiments that were not accounted for in simulations.

IV. CONCLUSION

A new magnetic noise reduction technique is demonstrated and validated, relying on the optimal choice of rotor or stator slot opening widths once the slotting vibrations to cancel have been analytically characterized. This technique do not increase slot leakage inductance ; it can be applied during the design stage of induction machines, and let a degree of freedom to the designer who can choose the quiet slot opening width in a set of different values. It shows that contrary to the common design rule that advices to decrease rotor and stator slot openings width in order to reduce magnetic noise, a wider slot opening can lower the noise level if properly chosen.

Furthermore, this technique can be applied to any magnetic force wave related to permeance harmonic: besides slotting vibrations, it can efficiently cancel a "winding vibration", or a saturation vibration (cf. section II-B where their magnitude are proportional to $P_s P_r$ or P_{sr}) that can be noisy in starting traction motors. As it leads to relatively large slot openings, this technique also decreases slot leakage inductances.

Once that technique is used, PWM noise dominates slotting noise, so further work aims at finding new design rules reducing PWM vibrations.

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