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# Groundwater flow and heat transport for systems undergoing freeze-thaw: Intercomparison of numerical simulators for 2D test cases

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#### 1 Abstract

In high-elevation, boreal and arctic regions, hydrological processes and associated water bodies can be strongly influenced by the distribution of permafrost. Recent field and modelling studies indicate that a fully-coupled multidimensional thermo-hydraulic approach is required to accurately model the evolution of these permafrost-impacted landscapes and groundwater systems. However, the relatively new and complex numerical codes being developed for coupled non-linear freeze-thaw systems require verification.

8 This issue is addressed by means of an intercomparison of thirteen numerical codes for two-9 dimensional test cases with several performance metrics (PMs). These codes comprise a wide 10 range of numerical approaches, spatial and temporal discretization strategies, and 11 computational efficiencies. Results suggest that the codes provide robust results for the test 12 cases considered and that minor discrepancies are explained by computational precision. 13 However, larger discrepancies are observed for some PMs resulting from differences in the 14 governing equations, discretization issues, or in the freezing curve used by some codes.

15 Keywords: numerical simulation, code benchmarking, thermo-hydrological coupling,
16 permafrost, sharp interface problems

17

#### 18 **1** Introduction

19 Climate change has been most pronounced at high latitudes (McBean et al., 2005; IPCC, 2013) 20 and high elevations (Pepin et al., 2015), and these trends are expected to continue in the coming 21 decades (IPCC, 2013). In these cold regions, hydrological processes are influenced by changing 22 precipitation regimes (e.g., Serreze et al., 2000; Hinzman et al., 2005) but are also very sensitive 23 to increasing air and ground temperatures because frozen ground stores and transmits water 24 very differently than unfrozen ground (Rowland et al., 2010; Walvoord and Kurylyk, 2016 and 25 references therein). Frozen ground retards or inhibits horizontal and vertical groundwater flow 26 due to the influence of pore ice on hydraulic conductivity. Thus, permafrost thaw or changing 27 patterns of seasonal subsurface ice can result in new or enhanced surface water distributions 28 (Connon et al., 2014) and can modify subsurface water pathways (Kurylyk et al., 2014a; 29 Frampton and Destouni, 2015) which can thereby affect the hydrologic and hydrogeologic 30 connectivity of a landscape. A number of studies note, for example, long-term increasing trends 31 in groundwater discharge (i.e. river baseflow) (e.g., Duan et al., 2017; Rennermalm et al., 2010;

St. Jacques and Sauchyn, 2009; Walvoord and Striegl, 2007) and decreases in seasonal variability (Frampton et al., 2011, 2013) due to permafrost thaw. Such behavior has a corresponding influence on ecosystem evolution and carbon storage and release (Schädel et al., 2016; Schuur et al., 2015; Vonk & Gustafsson, 2013). This context provides the impetus for developing an improved understanding of the interrelationships between climate change, permafrost thaw, and groundwater flow systems.

7 Over the past decade, a new class of hydrogeologic computer simulation codes has emerged 8 with specific functionality for cold regions. These codes enable predicting the impacts of 9 climate change on hydrological and hydrogeological systems (cf. special issue of *Hydrogeology* 10 *Journal*, Cold Regions Hydrogeology, in 2013). These new 'cryo-hydrogeology' codes couple 11 the groundwater flow equation to a heat transfer equation with dynamic freeze-thaw processes 12 (e.g. Coon et al., 2016; Nagare et al., 2015; Karra et al., 2014; Wellman et al., 2013; Grenier et al., 2013; Rowland et al., 2011; Dall'Amico et al., 2011; Frampton et al., 2011; Painter et al., 13 2011; Bense et al., 2009; McKenzie et al., 2007; Mottaghy and Rath, 2006; Hansson et al. 2004 14 15 ; Ippisch, 2001; Hwang et al. 1972).

16 The numerical solution to the set of coupled, non-linear thermo-hydrologic (TH) equations in 17 these emerging models can be quite challenging because the pore water phase change terms 18 (i.e. which describe freeze-thaw) lead to very narrow transition zones between the frozen and 19 unfrozen regions. These high temperature gradients induce strong non-linear effects due to 20 temperature-dependent thermal properties and hydraulic conductivities that depend on pressure, water content and temperature. The physical processes and solution strategies behind the 21 22 various cryo-hydrogeology models vary among codes (Kurylyk and Watanabe, 2013), which 23 provides the motivation for further code testing, comparison and validation. Furthermore, while 24 the results presented in the above-mentioned studies are qualitatively intuitive, their accuracy 25 and physical realism is unknown. A rigorous and widely accepted approach for properly 26 validating these codes is a prerequisite for applying these codes to study impacts of climate 27 change on hydrological and hydrogeological systems.

McKenzie et al. (2007) identified the need for such a code validation effort. They first considered an existing 1D analytical solution (the Stefan problem: a homogeneous system with conduction, phase change, and a partially frozen zone) and developed 2D test cases. More recently, Kurylyk et al. (2014b) revisited several 1D analytical solutions for ground freezing and thawing, and proposed that a solution for conduction and phase change with the addition of pore-water advection could be applied for cryo-hydrogeological code benchmarking. In an effort to optimize the type of 2D test cases introduced by McKenzie et al. (2007) for intercomparison purposes, two new complementary 2D benchmark cases with full TH coupling, and with more explicit performance measures than considered by McKenzie et al. (2007), are proposed in the present paper.

6 The InterFrost project (wiki.lsce.ipsl.fr/interfrost) was launched at the end of 2014 with the 7 intention of validating TH codes. The validation strategy proposes a progression from simple 8 test cases with analytical solutions to more complex laboratory and field-scale systems. The 9 first validation step is the Lunardini analytical solution used by McKenzie et al. (2007) (named 10 the "T1 Case") and the second is the Kurylyk et al. (2014b) case with constant advection (named 11 "TH1 Case"), where T refers to purely thermal conduction cases while TH refers to cases with 12 thermal and hydrodynamic (fluid flow) processes. Both cases consist of analytical solutions to the posed problems. The TH1 case is not a fully coupled system (i.e. water flow is independent 13 14 of the temperature field), and both analytical solutions are limited to 1D heat transfer.

The solutions to the new set of intercomparison cases presented here are obtained with numerical, rather than analytical, approaches. While numerical solutions do not inherently guarantee exact solutions to the stated mathematical problem as do analytical solutions, agreement among several numerical approaches (represented by the different codes used here) may build confidence that the solutions are correct.

The increased flexibility in the numerical approaches used here also allows for full TH coupling with 2D geometries. The next two intercomparison cases, herein named the "TH2 Case" and "TH3 Case", consider the evolution of more complex 2D systems with changing frozen and unfrozen regions under various hydraulic gradients. Evaluation of the numerical codes against these benchmarks is based on the intercomparison of simulation results through a set of performance metrics (PMs). Conclusions are drawn regarding similarities and differences among model responses over a range of parameters.

Thirteen codes developed and/or applied by research institutes from USA, Canada, Sweden, Germany, UK, the Netherlands, and France were compared in the InterFrost project. A brief presentation of the participating codes and laboratories is provided in Appendix A. All codes were successful in matching the T1 and TH1 analytical-solution test cases before being applied to the TH2 and TH3 test cases. This paper presents results of the TH2 and TH3 test cases as well as a detailed intercomparison of results from the thirteen codes. The initial work conducted for the T1 (McKenzie et al., 2007) and TH1 (Kurylyk et al., 2014b) test cases is not presented, as these tests were intended as a first validation step within InterFrost. However, these preliminary analyses helped to resolve a number of previously unanswered questions such as the appropriate spatio-temporal resolution for such simulations. The TH2 and TH3 results presented herein represent more complex scenarios than the seminal T1 and TH1 cases and should provide additional standards by which to verify future codes.

8 This verification effort will provide a basis for addressing more general challenges related to 9 numerical simulation of cold-region hydrogeological processes, including coupling with the 10 geo-mechanical processes of soil consolidation and frost heave (Painter et al., 2013). The results are directly relevant to many fields of research, including cold regions hydrology and 11 12 hydrogeology (see e.g. Lemieux et al, 2016; Nagare et al., 2015; Wellman et al., 2013; Rowland et al., 2011; Frampton et al., 2011; Bense et al., 2009; McKenzie et al., 2007), subsea permafrost 13 14 and evolution of methane hydrates (e.g. Frederick and Buffett, 2014), nuclear waste storage 15 (e.g. Vidstrand et al., 2013; Grenier et al., 2013; Holmen et al., 2011), fluvial geomorphology (Costard et al., 2014; Dupeyrat et al., 2011; Randriamazaoro et al., 2007), Mars studies (e.g. 16 17 Painter, 2011; Grimm and Painter, 2009; Aguirre-Puente et al., 1994; Clifford, 1993), climate modelling (1D models, see e.g. Gouttevin et al., 2012), terrestrial ecosystem changes (Kurylyk 18 19 et al., 2016; Briggs et al., 2011), artificial ground freezing in geotechnical engineering (e.g. 20 Zhou and Meschke, 2013; Pimentel et al., 2012), and acid mine drainage in cold regions 21 (Elberling, 2005).

International benchmarking exercises have proved very fruitful in the past to build confidence in numerical models and propel the development of a new generation of codes in closely related fields (e.g. Kolett et al. 2017; Pruess et al., 2014; Gustafson et al., 2009; Larsson, 1992).

25

#### 26 2 Theory, equations and numerical issues

The previously cited literature provides a wide range of expressions for water flow and heat transport equations in porous media. For the purpose of intercomparisons within the InterFrost group, a set of ad hoc TH equations was agreed upon with the intention of avoiding high levels of complexity that could preclude some developers from participating. The adopted option was to look for the simplest combination of equations and parameters while still maintaining the

1 important physical processes and interrelationships (conduction, advection, latent heat, 2 transient Darcy flow and first-order coupling).

3 Consequently, the set of equations used in this study is not intended as a reference system for all code developers. It should, however, provide a good platform for the seminal 4 5 intercomparison of TH code simulations.

6 This evaluation step first addresses the challenges of simulating the complex behavior of a 7 coupled non-linear set of equations with moving sharp interfaces (phase change regions). A more complete code validation project (as intended later with InterFrost) will include 8 9 comparisons with laboratory and field conditions. Although the set of equations required in 10 such a second phase may differ from those used here, the overall validation procedure would 11 be similar and would rely on the confidence gained from these simple 2D test cases. 12 Consequently, parameter simplicity is maintained in all comparison cases. For example, we 13 apply a simple empirical freezing curve with an impedance factor, although other options may 14 be preferred (e.g. based on a deduction from the unfrozen soil moisture characteristic curve or 15 heterogeneities, see discussions by Kurylyk and Watanabe, 2013; Painter and Karra, 2014, 16 Amiri et al., 2018).

17 The Darcy flow and energy transport equations considered for the benchmark are shown in Eqs. 18 (1) and (2), respectively, as:

19 
$$(S_w \epsilon \rho_w g \beta) \frac{\partial p}{\partial t} = \vec{\nabla} \cdot \left[ K_w \vec{\nabla} p \right] + \vec{\nabla} \cdot \left[ K_w \vec{\nabla} z \right] - \epsilon \left( \frac{\rho_w - \rho_i}{\rho_w} \right) \frac{\partial S_w}{\partial t} \quad (1)$$

20 
$$\left( \rho_w S_w c_w \epsilon + \rho_i S_i c_i \epsilon + (1 - \epsilon) \rho_s c_s - \epsilon \rho_i L \frac{\partial S_i}{\partial T} \right) \frac{\partial T}{\partial t}$$
21 
$$= \vec{\nabla} \cdot \left( \lambda_t \vec{\nabla} T \right) + \vec{\nabla} \cdot \left[ \rho_w c_w K_w T \vec{\nabla} p + \rho_w c_w K_w T \vec{\nabla} z \right]$$

All fixed parameters or functions corresponding to Eq. 1 and Eq. 2 are presented in Table 1 (or 22 23 in the development below). The porous medium is assumed fully saturated with water (liquid

24 or ice), and no source or sink terms are considered.

25 The heat transfer equation (Eq. 2) includes conduction and advection (with the Darcy velocity 26 split into two terms to solve with pressure head as the dependent hydraulic variable) as well as phase change (expressed with latent heat in the heat capacity term). Local (grain-fluid) thermal 27 28 equilibrium is assumed. Considering the small range of temperature variations, no density-29 driven convection is included (Table 2 & 3).

(2)

Eq. 1 corresponding to the water mass conservation was obtained after simplifying the water
mass conservation equation (Eq. 3):

$$\frac{\partial(\epsilon\rho_i S_i + \epsilon\rho_w S_w)}{\partial t} = -div(\rho_w \vec{U})$$
(3)

4 where  $\vec{U}$  is the Darcy velocity. All other variables and parameters are defined in Table 1. No 5 source term is included. Assuming that porosity does not evolve with time, since soil 6 consolidation, thaw settlement or frost heave is not considered (Bear and Bachmat, 1991), and 7 that  $S_w + S_i = 1$ , the system simplifies to:

8 
$$\epsilon S_{w} \frac{\partial \rho_{w}}{\partial t} + \epsilon (1 - S_{w}) \frac{\partial \rho_{i}}{\partial t} + \epsilon (\rho_{w} - \rho_{i}) \frac{\partial S_{w}}{\partial t} = -div \left(\rho_{w} \vec{U}\right)$$
(4)

9 In the absence of ice compressibility (negligible compared with water compressibility), the10 governing equation reduces to:

11 
$$\epsilon S_w \frac{\partial \rho_w}{\partial t} + \epsilon (\rho_w - \rho_i) \frac{\partial S_w}{\partial t} = -div (\rho_w \vec{U})$$
(5)

12 Considering that the water density depends primarily on pressure (and to a relatively negligible 13 extent on temperature in the ranges considered), and introducing the water compressibility 14 coefficient  $\beta = \frac{1}{\rho_w} \frac{\partial \rho_w}{\partial P}$ , the pressure head  $p = \frac{P}{\rho_w g}$ , and dividing both sides by  $\rho_w$ , Eq. 5 finally 15 yields Eq. 1 considered for the benchmark.

The initial development of the TH equations and solutions of the proposed InterFrost test cases were first completed with the Cast3M code (www-cast3m.cea.fr). Cast3M had already been applied to various 1D and 2D cases (Régnier, 2012; Grenier et al., 2012; Roux et al., 2017) based on a somewhat different system of equations.

20

3

#### 21 **3** Presentation of test cases

The TH2 and TH3 test cases were inspired by real-world conditions and from examples presented in the literature. These cases were specifically defined to enable testing the coupled system of equations, while remaining as simple as possible to allow running with the largest range of codes, without major code modifications. In particular, simple 2D geometries were considered to minimize meshing issues and to remove the need for specific mesh generators. Furthermore, all properties remained isotropic, and both cases could be run on a symmetric
 half-domain to save computational time.

3 These complementary cases address two levels of coupled TH complexity. The first case (Case 4 TH2) deals with the thawing of an initially frozen inclusion subject to a simple water flow regime with constant positive input temperature. The second (Case TH3) represents a simplified 5 6 talik (an unfrozen zone within permafrost) with competition between permafrost formation 7 (with imposed negative boundary temperatures) and permafrost thaw due to the inflow of warm 8 water. Inflow water temperature and flow rates are the controlling parameters for the evolution 9 of the talik which may expand or shrink depending on whether the head gradients and associated 10 water flow rates exceed a threshold. The threshold depends on the thermal properties, boundary 11 conditions, and system geometry.

12 Test cases TH2 and TH3 are presented in the following sections in more detail, with the purpose 13 of providing a basic understanding of the physics of the system evolution. Simulations obtained 14 with the Cast3M code are provided to support the presentation and analyses. The discretization 15 parameters associated with these reference simulations (e.g. meshing and time steps) were 16 selected after running convergence studies from which a compromise was found between "full" 17 convergence and computational efficiency. The spatial and temporal sensitivity analyses 18 conducted with the Cast3M code are presented in Appendix B. The analysis was used to check 19 the numerical convergence of the preliminary Cast3M simulations as well as to estimate the 20 spread in the performance metrics associated with various levels of space and time 21 discretization.

## 22 3.1 Case TH2: "Frozen Inclusion Thaw"

The conditions for Case TH2 ("Frozen Inclusion Thaw") are provided in Fig. 1 and Table 2. The parameter values applied in the benchmark are provided in Table 1. This case is inspired by the spherical inclusion problem in the heat transfer literature (e.g. Carslaw and Jaeger, 1959) and it simplifies the geometry of the frozen wall case of McKenzie et al. (2007), which considers similar effects but for freezing rather than thawing.

The initial frozen zone inclusion is square (Fig. 1a), with constant head flow boundaries along
the vertical sides (right and left) and no-flow conditions on the horizontal boundaries above and

30 below (Fig. 1b). The initial condition heads are assumed uniform, equal to the downgradient

boundary head. The thermal transport boundary conditions are an imposed temperature of 5 °C at the upgradient (left) inflow boundary, with zero temperature-gradient conditions (zero conductive fluxes) along all other boundaries (Fig. 1c). Outside the inclusion, the water temperature is initially uniform at 5 °C. The system is simulated with and without thermal advection. Evolution of the initial frozen zone depends on heat conduction from the transient temperature field surrounding it and on thermal advection from upgradient warm water driven by an imposed hydraulic gradient controlled by the boundary heads.

8 The head field (Fig. 2a) and the temperature field (Fig. 2b) simulated with Cast3M at time 9 22,860 s (6.4 hours), assuming a head gradient of 3%, are provided in Fig. 2 (as a color contour 10 plot (upper) and a line-contour plot (lower)). These fields are symmetrical relative to the 11 longitudinal x-axis through the center of the inclusion. The associated time is shortly before the 12 threshold time when the minimum temperature rises above 0°C. The initial frozen inclusion is now rounder in shape and warmer compared to the initial -5°C conditions, while a cooler 13 14 temperature plume has been transported downgradient (see Fig. 2b). The head and flow fields 15 show that water flows around the frozen inclusion and that hydraulic head gradients (p+z in Eq.)16 1) are higher (head contours are more densely spaced) within the frozen region due to its lower 17 hydraulic conductivity.

18 Figure 3 presents the time evolution of the temperature plume is for two different head 19 gradients. For a zero head gradient (without thermal advection), the -5°C inclusion gradually 20 thaws due to conductive heat transfer from the initially warmer 5°C temperature field around it 21 (Fig. 3a). The temperature profiles are symmetrical along the central longitudinal axis at early 22 times but become asymmetrical over time due to the greater distance to the right side boundary 23 condition (zero conductive heat flux) relative to the closer left (inflow) boundary where a 5 °C 24 condition was imposed. The minimum domain temperature increases as the initial inclusion 25 warms. For the simulation in which advection is included with an imposed head gradient of 9% 26 (Fig. 3b), thermal degradation due to the inflowing 5°C water accelerates the thaw process. 27 Because of its lower effective hydraulic conductivity, water initially flows around the inclusion 28 leading to a relatively colder downstream thermal plume and strongly asymmetrical 29 temperature profiles. At later times, when the inclusion has completely thawed, the remnant 30 cold water region is transported downstream by advection and thermal dispersion, forming the 31 lower amplitude temperature profiles such as the profile at 16.6 hours, shown in red (Fig. 3b).

#### 1 3.2 Case TH3: "Talik Opening / Closure"

2 The conditions for Case TH3 "Talik Opening / Closure" are provided in Fig. 4. The geometry 3 of the system and the initial conditions are defined by two frozen (-5°C) semi-circular zones 4 within a positive background temperature field of 5°C (Fig. 4a). Flow conditions (Fig. 4b) are the same as for Case TH2 with fixed heads along the upgradient (left) and downgradient (right) 5 6 faces, and zero-flux (no-flow) conditions elsewhere (compare Fig. 1b & 4b). Thermal boundary 7 conditions (Fig. 4c) are imposed temperatures of -5°C on the upper and lower boundaries, 5°C 8 on the (left) upstream boundary, and zero conductive flux on the (right) downstream boundary. 9 Heat thus exits the system from this right boundary through advection alone. The parameter 10 values are identical to Case TH2 (refer to Table 1).

11 This case represents the evolution of a talik - an unfrozen zone within permafrost. Such 12 conditions of heat exchange are found in the real world where water flows between two 13 permafrost zones. Horizontal internal taliks exist permanently within some permafrost regions 14 (e.g. Gagarine, 2012; Anisimova et al., 1973), while vertical flow-through taliks can often be 15 found below a lake or a large river and provide a direct connection with a sub-permafrost aquifer 16 (see for instance the cases of Wellman et al., 2013, Rowland et al., 2011, and Bense et al., 2009 17 ). Case TH3 (Fig. 4) can apply to both real-world cases as the simulations do not include density 18 effects, and thus the results are independent of orientation. TH3 is simulated under hydrostatic 19 (no-flow) conditions as well as under different background hydraulic gradients controlled by 20 the imposed boundary heads (similar to TH2).

The simulated head field (Fig. 5a) and temperature field (Fig. 5b) at time 19,860s (5.5 hours), assuming a head gradient of 3%, are provided in Fig. 5 (as a color contour plot (lower) and a line-contour plot (upper)). These fields are symmetrical relative to the central longitudinal xaxis. At the indicated time, and with this low head gradient of 3%, the talik is approaching closure as shown by the 0°C isotherm which already reaches the central axis (Figure 5).

The time evolution of the temperature plume is next shown for two different head gradients (Fig. 6). With a zero head-gradient (pure conduction, Fig. 6a), the two initially frozen zones merge across the central initially unfrozen part of the domain. The flow stops rapidly as the talik closes. The case including thermal advection (9% head gradient) is shown in Fig. 6b. In this case, cooling in the central part is progressively retarded due to the inflow of warmer water by advection, and the cooler plume is shifted downgradient (Fig. 5b). After this initial phase, further evolution of the system depends on the amount of heat advected into the talik zone. For
low rates of advection, the system eventually closes because conductive heat loss towards the
frozen boundaries in the upper and lower zones dominates, whereas for cases with more rapid
thermal advection, such as in the case with a 9% imposed head gradient corresponding to Fig.
6b, heat exchange widens the unfrozen central pathway until steady-state conditions are
established and the talik remains open.

7

#### 8 4 Performance measures

9 The performance measures (or performance metrics; PMs) are introduced to facilitate code 10 intercomparisons. With the aim of studying the importance of advection, all performance 11 measures are computed for each test case and for a range of imposed head gradients (see Table 12 2 and Table 3).

13 Table 4 provides an overview of the PMs, which include bulk (integrated) system parameters 14 as well as point values. The time evolution of these PMs is computed and displayed for all 15 simulation results and codes. The entire series of PMs provides an efficient coverage of all 16 physical thermal and hydrological conditions at various scales. The chosen PMs, which include 17 total heat, total liquid water volume and the minimum domain temperature, correspond to 18 several physical conditions of interest for applications in the real world (ex. computing total 19 fluxes across a boundary, talik evolution considering equivalent hydraulic conductivity) or are 20 necessary for numerical purposes to check heat and water budgets. The PMs reflect unique 21 system behaviors. It should be noted that the advective heat fluxes and the total sensible heat 22 are evaluated with 0 K as the thermal datum (e.g., Lee, 1998), although the choice of the thermal 23 datum will not influence the calculation of the net advective flux. A more detailed description 24 of these PMs follows.

#### 25 **4.1 Case TH2: frozen inclusion thaw**

For Case TH2, three performance measures are introduced, combining thermal and hydrodynamic information:

• The first PM (TH2\_PM1) is the minimum field temperature. Approaching complete thaw of the inclusion, the point of minimum temperature will remain within the inclusion, then will start to migrate downgradient with the cold water plume. The second PM (TH2\_PM2) is the net heat flux (Joules) leaving the system (J<sub>net</sub>). This
 heat flux is calculated as the flux density integral at the upstream (*u*) and downstream
 (*d*) vertical boundaries (note that no energy is transferred across the top and bottom no flow, perfectly insulating boundaries):

$$J_{out} = \int_{d} \left( \rho_{w} c_{w} T U_{x} - \lambda_{T} \frac{dT}{dx} \right) dy - \int_{u} \left( \rho_{w} c_{w} T U_{x} - \lambda_{T} \frac{dT}{dx} \right) dy$$

6 where  $U_x$  is the horizontal component of the Darcy flux. Heat flux leaving the system 7 is defined here as positive. Temperatures are expressed in kelvins taking 0K as the 8 reference. Note 0°C could be introduced as the reference. Such a 2D flux depends on a 9 third dimension, arbitrarily chosen here as unity (1 m).

5

• The third measure (TH2\_PM3) is the total volume of liquid water in the model domain. This measure corresponds to an integral over the total volume of the domain and is obtained by summing the product of the liquid water saturation, porosity, and representative volume for each node across the domain. As was assumed for PM2, the transverse width is set to 1m.

15 The PMs are here illustrated and analysed with the Cast3M simulations (Fig. 7). Special 16 attention is first placed on TH2\_PM1, the evolution of the minimum domain temperature (cf. 17 Fig. 5a), focusing on the case with a head gradient of 3% (purple line) for discussion of 18 evolution Phases 1 to 4. Within the first few minutes, the frozen inclusion rapidly warms due 19 to conductive heat loss to the surrounding flowing water, leading to a rapid rise in the 20 temperature of the center of the inclusion (refer to Phase 1 in Fig. 7a). The temperature curve 21 then reaches a slowly evolving plateau between -1 and 0 °C (Phase 2), corresponding to the 22 phase change region of the simulated porous medium, where adsorption of latent heat slows the 23 rate of temperature increase, known as the 'zero curtain effect' (Romanovsky & Osterkamp, 24 2000) (see Table 2). After reaching 0°C, phase change is complete, and the temperature increase 25 accelerates again (Phase 3). The warming rate then decreases as the cooler zone corresponding 26 to the initial inclusion becomes mobile and moves downstream through what has become a 27 uniform flow field (Phase 4). The evolution of the minimum field temperature is provided in 28 Fig. 7a for other rates of advection (head gradients from 0 to 20%). This broad range of 29 simulations is provided here for the sake of illustration, while the requirements for the task 30 participants were limited to a subset of 4 head gradient values (Table 4). The shape of the purely

1 conductive case (0% gradient) also displays a phase change domain of between -1°C and 0°C 2 and is typical of a diffusion (or equivalently conduction) process. Advection modifies the 3 profile by accelerating the early warming and providing a final rapid rise in the temperature 4 once the center of the advected thermal plume has exited the domain.

The times required for the minimum temperature to reach 0°C can be plotted as a function of
head gradient (Fig. 7b) integrating the TH2\_PM1 results over the entire range of head gradients.
Results show intuitively that the larger the head gradient, the narrower the peak and the quicker
the low-temperature plume exits the system (Fig. 7b).

9 The evolution of net heat flux leaving the system (TH2\_PM2) for Case TH2 (Figure 7c) exhibits 10 a rapid increase as the low-temperature plume resulting from the thawing of the initial frozen 11 zone crosses the downstream boundary. Net heat fluxes are negative as a result of the colder 12 inclusion and the convention of assuming positive heat fluxes when thermal energy (relative to 13 background temperature) is leaving the system. This performance measure is equivalent to the 14 total heat flux exiting the downstream (right) boundary, removing the base heat flux associated 15 with advection of the background 5°C temperature field.

The total unfrozen (liquid) water volume in the system (TH2\_PM3) increases as time proceeds until it stabilizes at a level of 1.11 m<sup>3</sup> when the minimum temperature of the system is above zero (Fig 7d). This performance measure provides information about the initial phase of thawing of the frozen inclusion. As expected, results show that the stronger the advection intensity, the quicker the thermal degradation of the frozen inclusion (Fig. 7d). (Showing the total heat content throughout the domain would be an alternative performance measure but would contain similar or redundant information).

## 23 4.2 Case TH3 "Talik Opening / Closure"

- 24 Three performance measures are considered here,
- The evolution of the bulk system equivalent hydraulic conductivity (TH3\_PM1). This
- is computed for each time step as the integrated Darcy flux  $(Q = \int q \, dx)$  at the right boundary divided by the imposed head gradient:  $K_{eq} = \frac{Q}{\Delta H/L_X}$

- The evolution of lateral heat flux (TH3\_PM2). This is calculated by integrating the
   conductive heat fluxes across the upper and lower boundaries and considering an
   arbitrary 1 m length for the transverse dimension.
  - The evolution of total sensible heat  $J_T$  (TH3\_PM3), which is computed as:  $J_T = \iint (\rho_w C_w \epsilon S_w + \rho_i C_i \epsilon (1 S_w) + \rho_s C_s (1 \epsilon)) T dxdy$ . The transverse dimension is again assumed to be 1 m.
- 7 8

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• The point temperature evolution at two fixed dedicated locations of the domain (TH3\_PM4).

9 The parameters associated with the reference simulation shown in the present section were 10 chosen after convergence studies as a compromise between "full" convergence and 11 computational efficiency (see Appendix B. The following text refers to Fig. 8 and simulations 12 with Cast3M code.

13 The equivalent hydraulic conductivity  $K_{eq}$  (TH3\_PM1) measures the hydraulic impedance 14 associated with the evolution of the talik. This conductivity is computed for each time step 15 based on the net water flux and the hydraulic gradient. For no or low levels of advection, the 16 system closes and the equivalent hydraulic conductivity decreases to near-zero as the system 17 becomes completely frozen. Sensitivity to the head gradients between 0 and about 6.3% shows 18 that the higher the advection, the slower the decrease in bulk  $K_{eq}$  (Fig. 8a). At higher flow rates (head gradients  $\geq 6.4\%$ ), the heat transferred by advection is sufficient to thaw increasing 19 20 portions of the initially frozen domain thus increasing the bulk hydraulic conductivity. The head 21 gradient threshold between both regimes (i.e. when the competing effects of conduction and 22 advection were equivalent) was found to be between 6.3 and 6.4 % (grey curves in Fig. 8a, 23 TH3\_PM1, and dotted line around 6.35% in Fig. 8b providing talik closure times for low head 24 gradients).

The evolution of the total conductive heat flux (TH3\_PM2) is also computed (Fig. 8c). As in TH2, the heat fluxes are assumed positive when exiting the system. Results show the greater the advection, the higher the absolute value of the heat flux entering the system (across the imposed fixed-temperature boundary). The total sensible heat (TH3\_PM3) exhibits the same dual behaviour as previous performance measures (Fig. 8d): before a threshold gradient is reached, the initial talik closes, reflecting the state where advection cannot transport enough energy in from the boundary and the total heat of the system subsequently declines. For greater levels of advection, the talik opens, leading to increasing levels of total sensible heat and to
 subsequent thawing.

3 Some locations in the domain record rapid temperature changes. The case presented in Fig. 8e 4 is the temperature evolution at the center of the system at Pt1 ( $x,y = 0.5, 0.5 \text{ m}, \text{TH3}_PM4_Pt1$ ). 5 For low imposed head gradients, the temperature drops below zero, reflecting the closure of the 6 talik, while for higher gradients, the talik opens. In the latter case, the temperature initially drops 7 due to high heat conduction from the nearby frozen zones before increasing again under the 8 influence of heat advection. Pt2 is located in the initially frozen zone (Table 4), the divide 9 between the initially frozen and unfrozen zones falling in the middle location between Pt1 and 10 Pt2 along the vertical axis.

The system evolves to reach a permanent equilibrium state where the 0°C isotherm becomes closer to the upper and lower boundaries for increasing head gradients (Fig. 8f) leading to wider central thawed zones. Such steady-state profiles could be considered as complementary performance measures. However, the 0°C interface is not sharp under steady-state conditions, thus its exact location is somewhat uncertain. Moreover, the computational effort becomes high when true steady-state conditions are desired.

17

#### 18 **5** Presentation of codes and participants

19 Participation in the InterFrost benchmark was promoted at scientific conferences and accepted 20 on a voluntary basis without dedicated funding. Thirteen codes have joined InterFrost. Several 21 codes were recently developed, but most were developed within existing simulation platforms 22 (i.e., software packages to simulate flow and transport in porous media) that were further 23 enhanced to account for phase change phenomena. The codes span a spectrum of numerical approaches: finite difference, finite element, finite volume, and hybrid approaches. Non-24 25 linearities and coupling of equations are dealt with by means of iterative approaches (Picard or 26 Newton schemes) or direct inversion. The meshing strategy is either fixed (structured and 27 unstructured meshes) or dynamically modified to follow steep temperature gradients. The time 28 step strategy is defined in advance or is inherently adaptive. Several of these codes are 29 massively parallel, while others only run on a single core. Information relative to each code is 30 provided in Table 5. More detailed information and a list of references is provided in Appendix 31 А

1 The simulation conditions considered for the reference calculations and the 13 participating 2 codes are provided in Table 6 (TH2 Case) and Table 7 (TH3 Case). Most codes used 3 convergence studies for refinement of the spatial discretization and time step size. The influence 4 of convergence criteria was investigated as well. As a result, the reference simulations provided 5 are expected to be spatially and temporally converged, and finer discretizations would give the 6 same results. Tables 6 & 7 show that a vast majority of codes simulated domains that contained 7 on the order of tens of thousands of elements or cells, with some taking advantage of spatial 8 symmetry.

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#### 10 6 Results of inter-code comparison

In the absence of any available reference simulation (compared to the analytical solution benchmarks that could be solved directly), solutions for TH2 and TH3 were obtained via an inter-code comparison of the simulation results as well as by using the convergence studies noted above. The inter-code comparison is first developed by comparing the results obtained by all codes for each PM (Section 6.1) and then enhanced by a detailed analysis of specific PMs in the cases where thresholds appear (Section 6.2). A more detailed analysis of the results, as well as a study of the sources of discrepancies, is treated in detail in Appendix C.

18 The complete series of PMs accounts for 32 comparable metrics (Table 4), composed of 3 PMs 19 associated with TH2 under 4 head gradients (0, 3, 9, 15%) and 5 PMs for TH3 under 4 head 20 gradients (3, 6, 9, 15%). Furthermore, additional plots representing threshold values (see Table 21 4) and times to reach steady state are provided for the complete series of head gradients. 22 Although the analyses are built upon the full set of PMs, for the sake of saving space, only a 23 representative subset of the PMs is provided in the present paper. Interested readers will find 24 all of the raw plots and data for each PM on the InterFrost web site (wiki.lsce.ipsl.fr/interfrost/). 25 A detailed analysis of the results produced by each code is not included because most codes 26 behaved similarly. Overall conclusions are drawn about the intercomparison project, which 27 provide a general and robust evaluation of the code performance.

It should, however, be noted that some codes taking part in the intercomparison could not fully comply with all the test case requirements within the short time of the project. For instance, simulations with PFLOTRAN-ICE remained bounded to a power law freezing function and thus could only apply an approximation of the exponential expression required in the specifications (see Table 2). However, their simulations were kept in the intercomparison results to illustrate the sensitivity of the simulations to the freezing function. This sensitivity was high as demonstrated in the sensitivity analysis carried out with the Cast3M code, considering an exponential freezing curve and a range of parameters (see Appendix B). Other codes also had somewhat different terms in the equations or expressions for bulk properties but which did not have a significant influence on the results.

#### 7 6.1 Visual illustration of PM results

Fig. 9 provides two PM compilations including all 13 codes for the TH2 case: the evolution of the minimum temperature within the simulated domain (TH2\_PM1, Table 4) and the associated total unfrozen water content (TH2\_PM3, Table 4). Both plots in Fig. 9 are for the case of a head gradient of 3%, a realistic value for a hydrogeological setting. The evolution of the PMs is qualitatively intuitive and follows the results proposed using Cast3M and analyzed in Section 4.1.

14 Intercomparison results show that all curves in Fig. 9 have the same qualitative pattern. From a 15 quantitative perspective, some of the code results differ slightly from the group that achieved 16 essentially identical results. This is especially visible for the minimum temperature curve where 17 some codes show a discrepancy in the negative temperature region, especially in the transition range from -1°C to 0°C corresponding to the phase change. With PFLOTRAN-ICE (light blue 18 19 curve), for example, this discrepancy in thawing dynamics (Fig. 9a) originates from the 20 different freezing curve that is implemented in the code (cf. Table 1). However, the influence 21 of the different freezing curves is not very apparent in the plot of the total liquid water volume 22 (see Fig. 9b). This is due to the integrative nature of TH2\_PM3 (integral of liquid water over 23 the whole domain), a measure which is less discriminating than TH2 PM1. The same general 24 resilience to slight differences in the freezing curve is also evident for TH2\_PM2 (total flux 25 exiting the system, which is not presented here). The influence of the freezing curve range on 26 TH2\_PM1 and TH3\_PM1 is further discussed by means of a sensitivity analysis in Appendix 27 Β.

Although the spatially averaged PMs do not provide discriminating power for the system dynamics, they do provide another level of information. For example, the spread of the simulation curves in TH2\_PM3 (Fig. 9b) for the initial conditions shows that all codes do not represent exactly the same initial liquid water volume. This point will be further examined below (refer to discussions regarding Fig. C.2 in Appendix C), and highlights differences in the meshing strategy which creates slightly different initial conditions. Fig. 9 further indicates that the same level of discrepancy is maintained throughout the simulation time until the total disappearance of the frozen inclusion (at threshold times around  $7 \times 10^4$  s).

Fig. 10 provides compilations for TH3\_PM4 at points Pt1 and Pt2 and for the 3% head gradient 5 6 case. Since both points are located close to the initial boundary between the frozen and the 7 unfrozen zone (see Table 4), the point temperatures rapidly evolve (4 to 5 °C difference over about  $10^4$  s). Intercomparison results show that the difference in the freezing function changes 8 9 the temperature evolution for PFLOTRAN-ICE, but for all other codes the results are very consistent, even at early times (before  $10^4$  s,). Temperatures in this central region (where Pt1 10 and Pt2 are located) are especially sensitive to the competing effects of advective vs. conductive 11 12 heat transfer, and this competition leads to either opening or closing of the talik. In coupled thermo-hydraulic (advective-conductive) cases (hydraulic gradients >0), non-linearities could 13 14 lead to instabilities and oscillations between the frozen and thawed regimes. The similarity of 15 results in Fig. 10 suggests that the codes are sufficiently robust to deal with such difficult conditions and confirms that they have converged to accurate solutions. 16

17 While Figure 11 (right axis) provides the total sensible heat of the system (TH3 PM3), it only 18 represents a 2D averaged measure where, except for two cases (PFLOTRAN-ICE and Ginette), 19 all heat evolution curves are effectively identical. Fig. 11 (left axis) provides another overview of the performance of the 13 codes, specifically, it presents the equivalent hydraulic 20 21 conductivity (TH3\_PM1) which is more discriminating. This PM is a key parameter which 22 clearly reflects the closure versus the opening of the talik. All codes predict system closure for times ranging from 6.5 to  $7.5 \times 10^4$  s except in one case (see Fig. 12 as well). Once again, the 23 24 PFLOTRAN-ICE results are slightly different due to the different applied freezing curve. Three 25 other curves (codes FEFLOW, and to a lesser extent GEOAN and SMOKER) display somewhat 26 different evolution while the remaining nine are nearly identical. Initial conditions for both PMs 27 (Fig. 11, initial time and Fig. C.2d) appear similar and do not explain the discrepancies. The 28 differences for these three curves are partly attributed to coarse meshing and insufficient 29 accuracy in the convergence of the non-linear coupling and partly to the method of computing 30 the equivalent hydraulic conductivity. The same reasons, especially coarse meshing (refer to 31 Table 7) would explain the results by Ginette for the total heat (Fig. 11). The sensitivity tests 32 done by some participants have shown that the discrepancies between equivalent hydraulic conductivity computed with steady-state flow fields and transient flow fields are negligible.
 Similarly, other sources of discrepancies involving somewhat different equation sets, for
 instance specifically incorporating pressure terms associated with the water to ice volume
 change, proved negligible through additional sensitivity tests.

5 The general conclusion from visual analysis of these TH2 and TH3 results is that all curves 6 provide qualitatively similar results or trends, except for PFLOTRAN-ICE which uses a 7 different freezing curve. Such results are indeed intuitive and follow from the preliminary study 8 with Cast3M analyzed in Section 4. From a quantitative perspective, the results among the other 9 codes differ to only a limited extent.

A more quantitative measure of the spread among the curves associated with each PM was introduced in the form of a standard deviation curve. This provided insights into the level of discrepancies among the 13 codes which likely resulted from different initial conditions (as a consequence of meshing strategies), or from incomplete spatial convergence of the simulation results. Further, results showed that there was no significant difference in the spread of the results among codes with increasing head gradients for both TH2 and TH3. The reader is referred to Appendix C for a detailed presentation of these issues.

#### 17 6.2 Effects of thresholds associated with the PMs

The conclusions drawn on the convergence of results do not apply for the case of TH3 at the 6% head gradient value, thus the special case of PMs associated with TH2 and TH3 thresholds is further discussed here. For TH2\_PM1, the threshold time was defined as the time for the minimum temperature to reach 0°C. For TH3\_PM1, the threshold time is associated with the time to reach 0.1 % of the initial equivalent hydraulic conductivity.

23 Fig. 12a shows the threshold times computed for TH2. The standard deviation of TH2 PM1 24 was at a maximum in this time interval for all head gradients (Fig. C.1, see Appendix C), 25 indicating that obtaining accurate simulations for this time period is challenging. The time for 26 the initially frozen zone to reach 0°C and the time to reach steady-state were computed by each 27 code. All requested head gradients are represented (vertical dots: 0, 3, 9, and 15 %) as well as 28 other head gradients when participants simulated intermediate cases. The threshold time 29 decreases as head gradients increase due to the thermal degradation from advection. The range 30 of results also decreases with increasing head gradients, with a moderate spread along the average general trend. Fig. 12b displays the time required to reach steady-state conditions. The
 general trend is identical (reduction in difference between codes with increasing head
 gradients), although the overall spread along this general trend is much lower.

4 The threshold times appear to be sensitive to the individual simulation set-ups (e.g. mesh size) 5 and individual codes, although results are consistent in the case of the steady-state times. For 6 TH3, the important threshold does not correspond to a distinct time during the thermal 7 degradation process, but is associated with a change in the system's hydrologic regime that is 8 controlled by the head gradient. Fig. 13b displays the equivalent hydraulic conductivity 9 (TH3\_PM1) for a head gradient of 6 %, for which four codes predict talik opening while nine codes predict talik closure. A refined study conducted with the Cast3M code provided a 10 11 threshold head gradient between 6.3 % and 6.4 %. Based on this information, the 6 % head 12 gradient appears critical for this particular test problem. The large spread of observed results is primarily a result of simulating this threshold correctly. Even for the 9 codes predicting talik 13 14 closure, the spread in the closure times is quite wide as seen from Fig. 13a (6%). A similarly 15 large dispersion of talik closure times is observed for 3 % (in the same plot). This was already 16 discussed with respect to Fig. C.1 plots (see Appendix C), where closure time differences were 17 attributed to differences in the computation of this PM, in addition to a divergence in the initial 18 conditions. The somewhat different evolution obtained with GEOAN was attributed to specific 19 difficulties met in this case (6%) to converge in the non-linear coupling associated with the 20 latent heat term.

The threshold case therefore appears to be the most challenging problem for accurate quantitative simulations. The simulated characteristic times (time to reach 0°C or steady state) generally had very small standard deviations. However, the talik closure times are apparently difficult to accurately simulate, making predictions challenging.

25

#### 26 7 Discussion and perspectives

The main conclusion focuses on the similarity of results, showing that the participating codes performed well in solving the TH benchmark problems. However, several important points are worth discussing and putting in perspective.

The conclusions of the paper are drawn from intercomparison of results from 13 simulation codes. This large number of codes, in addition to the diversity of numerical approaches, is a valuable basis for drawing conclusions. Nevertheless, increasing both the number of codes and
their diversity is important, and other modelers are invited to run these same cases to both test
their codes and to complement the present dataset.

4 The approach taken here relies on an intercomparison of codes. A more reliable approach that 5 actually verifies that a code is working correctly is to compare simulated results with an 6 analytical solution. No analytical solution have been published that simultaneously considers 7 multidimensional spatial groundwater flow and heat transfer with the freeze/thaw process. 8 Thus, intercomparison of a variety of numerical simulation codes is the second best approach 9 to verifying such codes for these types of cryo-hydrogeological problems. In a group process, 10 where there is no pre-existing criterion for assessing which code is 'correct' (i.e. providing a 11 numerical solution that is equivalent to the analytical solution, should one exist), arbitrarily 12 choosing one model output as the correct reference solution is not advisable. No code can provide such a non-challengeable numerical solution. It remains, however, an interesting 13 14 challenge for modelers and mathematicians to produce such an improved or reference solution 15 in the future.

16 We adopted a code intercomparison strategy based on performance measures. The strategy 17 combines real physical parameters, sometimes integrated to handle practical issues, and allows 18 simple intercomparisons. Another strategy for intercomparing could have been considered 19 based on direct comparison of the full 2D fields of the simulation variables (e.g. T, p). Rühaak 20 et al. (2015) attempted to compare 2D field results which showed similar results to those 21 demonstrated here. However, their comparison proved to be highly time consuming even with 22 only 4 participating codes, and would be impractical for 13 codes. An extension of this approach 23 to study the transient evolution of specific patterns or behavior associated with specific key 24 processes would require adapted simulation outcomes, including a common file exchange 25 standard, the development of associated interface tools, and a powerful tool for projecting 26 results (given the range of meshing methods). Although promising and complementary, this is 27 beyond the reach of our current project.

Another point concerns our conclusions about the general convergence of the results over the 13 participating codes while discrepancies within the results do exist. Their sources are discussed now. Discrepancies found in the intercomparison results among codes are likely in part associated with differences in the simulation set-up when implementing individual problems. Over the course of the study, some implementation errors were identified and

1 corrected by participants. Other differences from the specified conditions agreed on by all 2 participants (e.g. related to equation formulation) could not be easily explained. The test cases 3 were designed to be as simple and reproducible as possible. However, some codes could not be 4 fully adapted to the different implementations of freezing characteristic curves and/or 5 equivalent properties. Therefore discrepancies occur where differences in the basic 6 relationships differed to some extent (e.g. methods used for calculating average bulk, water and 7 ice properties). Furthermore, a remaining small difference in the simulations likely results from 8 a lack of computing precision. Several sources were identified, especially coarse or non-9 dedicated spatial representation of the initial system conditions which can lead to subsequent 10 code divergence, in addition to weakly converged simulations requiring more demanding 11 conditions in terms of the number of internal non-linear iterations and spatial and temporal 12 refinement. The latter more specifically concerns the computation of the non-linear latent heat 13 term in Eq. 2 for which large non-linearities occur, leading to oscillations and/or difficulties 14 obtaining high precision at low computational costs. Furthermore, the latent heat term requires 15 the derivative of ice saturation as a function of temperature. This can be achieved in various 16 ways (e.g. taking directly the analytical expression into account or a linear or higher order 17 expression of the derivative) producing similar though quantitatively different results. 18 Guidelines for such choices should be found first in the mathematical formulations associated 19 with each specific numerical scheme considered. They should then be tested against 1D basic 20 cases providing analytical expressions (e.g. Stefan problem with Lunardini analytical solution 21 in the Introduction Section). Although the extrapolation of discretization rules obtained from 22 1D cases is not straightforward to 2D and 3D cases, ad hoc spatial and temporal strategies have 23 been developed from such convergence studies, and are easy to implement on 1D geometries. 24 The same is true for the choice of some key control parameters (e.g. convergence criteria for 25 non-linear loops, parameters considered in under-relaxation algorithms for reducing the 26 amplitude of the oscillations).

All these issues were studied to some extent with the Cast3M or PermaFOAM codes as reported in Appendix B or by other participants (not reported here) by means of sensitivity analyses. The latter issues (examined separately) showed more or less minor influences on the results. However their combined effects are more complex, possibly cumulative, and difficult to address within a reasonable period of time. The cases associated with the code results that differ the most have already been addressed in the results section. The primary limitations appeared when comparing threshold predictions, especially for TH3\_PM1 in the case of the tipping point between the talik opening and closure regimes that occurred for gradients close to 6 %. A better intercomparison strategy could have been associated with the prediction of the head gradient threshold but would have required all participants to sample the domain of head gradients which would have substantially increased the work load. The TH3 Case is more demanding than the TH2 Case, further challenging code capabilities – an important factor for code comparison exercises.

8 Beyond the code intercomparison presented in this study, other evaluation elements could be 9 included in a more global verification procedure. InterFrost is considering a verification of the 10 numerical solutions to test cases through cold-room experiments. For example, the TH2 experiment has been attempted in the laboratory, however the experimental set-up and 11 12 measurements have been very challenging. Simulations of experimental laboratory results will require additional modelling effort and adaptations. Some level of calibration will probably be 13 14 required as well, making the approach not as straightforward as first envisioned, but more 15 realistic with respect to how codes are applied to real field problems.

16 This effort, however, including real world cases, can be a valuable part of the code verification 17 process considered by InterFrost and is complementary to the existing intercomparison 18 exercises. Comparison of code results with carefully-measured experimental (or field) data can 19 help provide 'validation' of a code (a stronger context than 'verification'). This means that not 20 only does a code solve the governing equations correctly (definition of 'verification'), but also, 21 that the governing equations correctly describe the physical processes and external conditions 22 that drive the system. InterFrost members are further planning the incorporation of field cases 23 into future test cases.

Relatively favorable conditions were used in both test cases for reducing computational loads associated with time and space discretization. This will not necessarily be the case for all realworld applications. Simulating large spatial systems with small-scale heterogeneities, for example, will be challenging. Similarly, the temporal discretization needs to satisfy stability criteria for such cryo-hydrological systems, but also needs to be practical for realistic computation times. These questions may be considered in the future within the InterFrost project.

1 Applying our modelling approaches to real world cases will also cast the present discussions 2 about numerical simulation precision in a practical context. The representation of the coupled 3 TH processes in the real world will require constraining parameter values associated with 4 properties that are subject to variations in heterogeneous media. The precision in the 5 measurements and the spatial variability added to the difficulty to constrain some parameters 6 (e.g. the freezing curve is often calibrated) will probably result in relatively high levels of 7 uncertainty. These sources of error and uncertainty will have to be compared to the 8 discrepancies resulting from the numerical simulation bounds identified in the present study. 9 Preliminary simulations applied to the experimental case with the frozen inclusion already show 10 that the numerical errors associated with the simulation are low compared to the uncertainties 11 resulting from parameter values.

12

#### 13 8 Conclusions

The development of coupled multi-dimensional TH numerical groundwater models with dynamic phase change for cold region applications is relatively recent. The simulation of such systems is challenging due to the coupled and non-linear structure of the equations, creating a complex evolution between frozen and unfrozen zones. The present study attempts to improve the quality and confidence in such codes through intercomparison of results from synthetic 2D test cases.

20 The present InterFrost intercomparison exercise was valuable for gathering a critical number of 21 participants (13 participating codes) and examining a large variety of numerical approaches and 22 code implementations. Based on the two test cases (TH2 and TH3), most code simulation results 23 generally converged around a single (unique) solution; thus, a consensus was reached among 24 the participants. A group of these models, resolving the same equation sets and identical 25 characteristic curves, behaved similarly in all test cases, for all PMs (performance measures), 26 and over the given range of head gradients. This suggests that the codes are all solving the 27 governing equations equally well, although it is still not guaranteed that this solution is 28 equivalent to the correct analytical solution to the problem, should one exist. A measure of code 29 divergence was introduced in the form of a standard deviation function; normalized ranges of 30 the PMs are generally within a few percent, with a maximum of 17% for TH2\_PM1.

1 Reaching this general consensus with a high level of agreement of the simulation results is a 2 promising outcome, considering that these coupled and non-linear TH systems are difficult to 3 solve. Despite the prevailing differences in the code approaches, meshing strategies, mesh sizes 4 in the reference simulations, and apparent maturity of codes (e.g. some codes had already been 5 extensively tested while other codes were limited to, at most, testing only specific parts of the 6 system of equations), the results exhibited general agreement. The following guidelines are 7 intended for future model developers who decide to employ the present test cases for model 8 validation. 1) Numerical models should be tested against the 1D analytical solutions (e.g. T1, 9 Lunardini solution and TH1, see Kurylyk et al., 2014), before attempting the TH2 and TH3 10 cases. 2) Implementation of the advective-conductive system without phase change (equivalent 11 to Eulerian mass transport) could be tested in a step by step verification approach. In addition, 12 the simplicity of the 1D systems allows simple convergence studies and identification of 13 stability and accuracy parameters, including time and space discretization requirements. These 14 1D results will be beneficial to understand the more complex contexts. 3) When running TH2 15 and TH3, the averaged PMs should be tested first to allow quick error checks (e.g. TH2 PM3, 16 TH3\_PM3). 4) Convergence studies on the main PMs (spatial and temporal refinements) should 17 be used to provide the final reference simulations, considering a subset of the head gradient 18 values. An estimation of the accuracy of the results from the convergence tests will provide 19 added value when finally compared with the 2D temperature fields at given times and when 20 compared with the PMs in this study and with additional PMs published on the InterFrost web 21 site in electronic format (wiki.lsce.ipsl.fr/interfrost).

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# 1 Tables

2

Physical properties	Parameter values and expressions
Porosity, ε	0.37
Porous medium compressibility, $\beta$ (m s <sup>2</sup> kg <sup>-1</sup> )	10-8
Gravitational acceleration, g (m s <sup>-2</sup> )	9.81
Thermal conductivity of water, $\lambda_{\rm w}~(W~m^{\text{-1}}~K^{\text{-1}})$	0.6
Thermal conductivity of ice, $\lambda_i$ (W m <sup>-1</sup> K <sup>-1</sup> )	2.14
Thermal conductivity of solid matrix, $\lambda_s$ (W m <sup>-1</sup> K <sup>-1</sup> )	9.
Total or bulk thermal conductivity, $\lambda_T$ (W m <sup>2</sup> )	$\lambda_T = \epsilon S_w \lambda_w + \epsilon (1 \text{-} S_w) \lambda_i \text{+} (1 \text{-} \epsilon) \lambda_s$
Specific heat of water, cw (J kg <sup>-1</sup> K <sup>-1</sup> )	4182
Specific heat of ice c <sub>i</sub> (J kg <sup>-1</sup> K <sup>-1</sup> )	2060
Specific heat of solid grains, cs (J kg <sup>-1</sup> K <sup>-1</sup> )	835
Water density, $\rho_w$ (kg · m <sup>-3</sup> )	1000
Ice density, $\rho_i$ (kg m <sup>-3</sup> )	920
Solid grain density, $\rho_s$ (kg m <sup>-3</sup> )	2650
Dynamic viscosity of liquid water, $\mu$ (kg m <sup>-1</sup> s <sup>-1</sup> )	1.793×10 <sup>-3</sup>
Total volumetric heat capacity $(\rho c)_T (J m^3 K^{-1})$	$(\rho c)_T = \epsilon S_w \rho_w c_w + \epsilon (1-S_w) \rho_i c_i + (1-\epsilon) \rho_s c_s$
Latent heat of fusion, L (J kg <sup>-1</sup> )	334,000
Water saturation curve, $S_w(T)$	[McKenzie et al. 2007], exponential expression
For T > 273.15 K, $S_w(T) = 1$ For T < 273.15 K, $S_w(T)$ , exponential fct of T	$Sw(T) = (1 - S_{Wres}) \exp [-((T - 273.15) / W)^2] + S_{Wres}$
Residual saturation, S <sub>Wres</sub>	0.05
W (K)	0.5
Hydraulic conductivity, K <sub>w</sub> (m s <sup>-1</sup> )	$K_{w} = k_{r} \ k_{int} \ \rho_{w} \ g \ / \ \mu$
Relative permeability curve, k <sub>r</sub> (T)	[McKenzie et al. 2007], impedance factor expression $k_r(T) = max(10^{-6}, 10^{-\epsilon\Omega(1-Sw(T))})$
Intrinsic permeability, k <sub>int</sub> (m <sup>2</sup> )	1.3 x 10 <sup>-10</sup>
Ω	50.

Table 1: Physical parameter values and expressions considered for Case TH2 "Frozen inclusion" and for Case TH3 "Talik Opening/Closure". The compressibility  $\beta$  includes water and matrix compressibility.

6
Simulation domain, longitudinal extent (m), $L_x$	3.
Simulation domain, lateral extent (m), $L_y$	1.
Position of inclusion centre	
$L_{CX}(m)$	1.
$L_{CY}(m)$	0.5
Size of square shaped inclusion $L_{Sq}$ (m)	0.333
Temperatures	
T <sub>in</sub> (°C)	+5.
$T^+_{initial}$ (°C)	+5.
T <sup>-</sup> initial (°C)	-5.
Applied head gradients	0.
$\Delta H/L_X$	0.03
	0.09
	0.15

- 1 Table 2: Case TH2 "Frozen Inclusion", geometric parameter values, initial and imposed
- 2 boundary temperatures, and head gradients
- 3

Simulation domain, longitudinal extent (m), $L_x$	1.
Simulation domain, lateral extent (m), Ly	1.
Position of lower circle centre (symmetric for upper circle)	
$L_{CX}(m)$	0.5
$L_{CY}(m)$	0.1
Radius, R (m)	0.5099
Temperatures	
T <sub>in</sub> (°C)	+5.
$T^+_{initial}$ (°C)	+5.
T <sub>initial</sub> (°C)	-5.
	-5.
I imposed (C)	

- 4 Table 3: Case TH3 "Talik Opening / Closure", geometric parameter values, initial and imposed
- 5 boundary temperatures
- 6



Table 4: Overview of the TH2 and TH3 test cases and performance measures.

Code	Numerical scheme	Non- linearities	TH coupling	Linear solvers	Pre- conditioner	Time step strategy	Automatic mesh refinement	Parallel computing
Cast3M	FV	Picard	Picard & Under- relaxation	BiCGSTAB	ILUO	Prescribed	No	No
PermaFOAM	FV	Picard	Sequential operator splitting	PCG, BiCG	DIC, DILU	Adaptive	No	Mesh Partitioning, ~100-1000 cores
COMSOL	FE	Damped Newton	Damped Newton	MUMPS	ILU	Adaptive	No	shared-memory: 8 cores
DarcyTools	FV	Picard	Picard	GMRES	Multi-grid, ILUO	Prescribed	Yes	PM, 64 cores
MELT	FV	Picard, IMPES	Sequential	GMRES, CG	ASM, ILU	Adaptive	No	No
SMOKER	FE	Picard	Picard & relaxation	PCG (+LF)	ILU factorization	Prescribed	No	No
ATS	MFD	Non-linear Krylov acceleration	Simultaneous inversion	GMRES, CG	Boomer AMG	Adaptive	No	PM, 4 cores
SUTRA	Hybrid FE & IFD	Modified Iterative Method	Modified Iterative Method	CG, GMRES, Orthomin, Direct	ILU, Cholesky	Prescribed	No	No
PFLOTRAN-ICE	FV	Newton	Simultaneous inversion	GMRES	ILU	Adaptive	No	PM, thousands of cores
FEFLOW	FE	Newton	Newton	BICGstab, PARDISO (direct solver)	incomplete factorisation	Adaptive	Yes	Open MP (here 16 cores)
GEOAN	FD	Picard	Picard	Iterative Crank- Nicolson	Non standard	Prescribed Adaptive Mixed	No	Up to 48 cores
FlexPDE	FE	Newton	Newton	CG, GMRES	ILU, Cholesky	Adaptive	Yes	Up to 8 cores
Ginette	FV	Picard	Picard	PCG	BuGC	Adaptive	No	No

FV: Finite Volume; MHFE: Mixed Hybrid Finite Element; FE: Finite Elements; FD: Finite Differences, MFD: Mimetic Finite Differences;

6

Table 5: Basic information on all codes participating in the InterFrost benchmark.

<sup>1</sup> 2 3 4 DD: Domain Decomposition; IFD: Integrated Finite Difference; (Picard = sequential = iterative); PCG: Preconditioned conjugate-gradient; LF = Leismann & Frind (1989) scheme for symmetric transport matrix, MUMPS: Multifrontal massively parallel sparse direct solver, ILU:

Incomplete Lower-Upper.

Code	Mesh size, number of nodes	Mesh size, Number of elements	Element type	Domain modelled	
Cast3M	31,609	31,609	Quadrilateral	Half	
PermaFoam	963,202	480,000	Hexahedra (3D)	Full	
COMSOL	35,000	35,000	Quadrilateral	Full	
DarcyTools	14,810	14,786	Cartesian Hexa (3D)	Half	
MELT	30,000	30,000	Squares	Full	
SMOKER	60,802	30,000	Hexahedra	Full	
	L		(3D)		
ATS	1,728	1,728	Hexahedra (3D)	Full	
SUTRA	20,301	20,000	Quadrilateral	Half	
PFLOTRAN- ICE	30,000	30,000	Hexahedra (3D)	Full	
FEFLOW	55,213	105,144	Triangles	Full	
GEOAN	32,130	32,130	3D	Full	
FlexPDE	4,882	2,345	Triangles Full		
Ginette	21,600	21,600	Quadrilateral Half		

Table 6: TH2 simulation conditions

Code	Mesh size, number of nodes	Mesh size, Number of elements	Element type	Domain modelled	
Cast3M	8,848	17,272	Triangles	Half	
PermaFoam	1,283,202	640,000	Hexahedra (3D)	Full	
COMSOL	40,000	40,000	Quadrilateral	Full	
DarcyTools	18,076	16,050	Cartesian Hexa (3D)	Half	
MELT	10,000	10,000	Squares	Full	
SMOKER	20,402	10,000	Hexahedra (3D)	Full	
ATS	4,225	4,225	Hexahedra (3D)	Full	
SUTRA	45,451	45,000	Quadrilateral	Half	
PFLOTRAN- ICE	6,720	6,720	Prisms (3D)	Full	
FEFLOW	32,197	63,720	Triangles	Full	
GEOAN	40,804	40,804	3D	Full	
FlexPDE	90,586	45,127	Triangles	Half	
Ginette	5,000	5,000	Quadrilateral	Half	

## 1 Figure captions

2

Figure 1: Case TH2 conditions ("Frozen Inclusion"): (a) geometrical features, (b) hydrological
boundary conditions, (c) thermal initial and boundary conditions. The associated parameter
values and the applied head gradients are provided in Table 1 & 2.

- 6 Figure 2: Surface and contour plots at time 22,860 s (6.4 hours) of (a) the head field (m), and
- 7 (b) the temperature field (°C).
- Figure 3: Evolution of Case TH2 showing simulated temperature profiles along a horizontal
  line (left to right) through the centre of the system: (a) without advection (pure conduction,
  upper plot, blue curve for initial time, dotted line, time 1260 s, red line final simulation time
  5.9 d), (b) with advection (head gradient of 9%, lower plot, blue line for initial time, dotted line
- 12 for 930 s, red line for final simulation time 16.6 h). Black lines provide the profile evolution for
- 13 additional times.
- 14 Figure 4: Case TH3 conditions ("Talik closure / opening") (a) geometry, (b) hydrological
- boundary conditions, (c) thermal initial and boundary conditions. All parameters are providedin Table 2 & 3.
- 17 Figure 5: Case TH3: Contour line and contour colour plots at time 19,860 s (5.5 hours) of (a)
- 18 the head field (m), and (b) the temperature field (°C).
- Figure 6: Case TH3: Evolution of simulated temperatures along vertical profiles crossing the centre of the system: (a) without advection (blue curve for initial time, dotted line for 120 s, red line final simulation time 2.71 d) and (b) with a head gradient of 9% (blue line initial time, dotted line 765 s, red line final simulation time 2.07 d). Black lines provide the profile evolution for a constant time interval.
- Figure 7: Overview of all PMs associated with the TH2 Case and for head gradients ranging from 0 to 20%. (a) TH2\_PM1, minimum temperature, with 4 curve-evolution phases corresponding to the 2% head gradient conditions (blue curve), (b) Time to reach 0°C as a function of head gradient intensity, (c) TH2\_PM2, net heat flux, (d) TH2\_PM3, total liquid water content; all curves reach the plateau of 1.11 m<sup>3</sup> corresponding to the total system volume composed of liquid water.
  - 41

- 1 Figure 8: Overview of all PMs associated with the TH3 Case and for head gradients ranging
- 2 from 0 to 15%. (a) TH3\_PM1, equivalent hydraulic conductivity, (b) talik closure time as a
- 3 function of head gradient intensity, (c) TH3\_PM3, total sensible heat, (d) TH3\_PM2, total
- 4 lateral conductive flux, (e) TH3\_PM4\_Pt1, temperature evolution at the centre of the simulation
- 5 domain, (f) steady state 0°C isotherm profiles for selected head gradients above threshold.
- Figure 9: (a) Evolution of the minimum of the temperature field (TH2\_PM1) and (b) the total
  water volume in the domain (TH2\_PM3).
- 8 Figure 10: (a) Evolution of the temperature at point Pt1 in the middle unfrozen zone of the 9 simulated domain (TH3\_PM4\_Pt1) and (b) at point Pt2 in the initially frozen zone 10 (TH3\_PM4\_Pt2). A head gradient of 3% is considered.
- Figure 11: (a) Evolution of the equivalent hydraulic conductivity of the domain (TH3\_PM1)and (b) the total heat of the domain (TH3\_PM3).
- Figure 12: Threshold values for TH2. (a) Time for minimum domain temperature to reach 0°C and (b) time to reach steady state. The horizontal axis is head gradient. The test was based on 0, 3, 9, and 15 % head gradients for TH2, and some participants provided extra simulations for intermediate head gradients.
- Figure 13: (a) Threshold values for TH3, i.e. time for system closure (time when equivalent hydraulic conductivity reaches zero). The horizontal axis is head gradient. The test was based on 3, 6, 9, and 15 % hydraulic gradients for TH2, while some participants completed extra simulations for intermediate head gradients. (b) Evolution of hydraulic conductivity is plotted with time, showing the divergence of flow regimes between the different codes.
- 22
- Fig. B.1: Case TH2, sensitivity of minimum temperature evolution to the freezing curvetemperature range.
- 25
- Figure C.1: Standard deviation evolution for two cases issued from TH2: (a) TH2\_PM1, minimum temperature, and (b) TH3, TH3\_MP4\_Pt1, temperature evolution at point Pt2 for
- 28 hydraulic gradients (GH) of 0, 3, 9 and 15%.

1 Figure C.2: (a) Standard deviation evolution for the total liquid water volume (TH2\_PM3) and 2 (c) the total heat (TH3\_PM3); (b & c) the corresponding initial conditions where indexes refer 3 to related codes (1: Cast3M, 2: PermaFoam, 3: COMSOL, 4: DarcyTools, 5: MELT, 6: 4 SMOKER, 7: ATS, 8: SUTRA, 9: PFLOTRAN-ICE, 10: FEFLOW, 11: GEOAN, 12: FlexPDE, 5 13: Ginette). Convergence test information is provided in the left column (a & c) in addition to 6 the standard deviation curves for all head gradients (0, 3, 9, 15 % for TH2; 3, 6, 9, 15 % for 7 TH3). 8 Figure C.3: Standard deviation evolution for TH2\_PM1 (minimum temperature in solid lines)

- 9 with standard deviations issued from convergence studies from participants in dashed lines with
- 10 the colour associated to the specific head gradient.
- 11 Figure C.4: Integrals of standard deviation for the TH2 performance measures and head
- 12 gradients of 3, 9, and 15 %. To fit on the same plot, all curves are normalized by the maximum
- 13 value. For TH2\_PM1 & 3, curves decrease from an initial maximum 3 % gradient case. For
- 14 TH2\_PM2, the standard deviation is nearly constant regardless of the head gradient.

#### 1 Appendix A – Participating code information

2

3 The Advanced Terrestrial Simulator (ATS, github.com/amanzi/ats): ATS is a ecosystem 4 hydrology code focusing on solving problems of integrated surface/subsurface hydrology 5 including vegetation, surface energy balance, snow, and other environmental interactions with 6 hydrology (Painter et al., 2016). ATS was originally developed with permafrost applications 7 in mind, and includes models of flow in partially frozen, variably saturated soils that have been 8 extensively validated against laboratory experiments to capture both cryosuction and density 9 variations between ice and water (Painter 2014). Several groups have used ATS to characterize 10 cold region physics and field sites across the globe (Atchley et al., 2015, Sjoberg et al., 2016). 11 ATS builds on the Arcos multiphysics framework (Coon et al., 2016) and leverages 12 unstructured meshes, second-order, conservative mimetic finite difference discretizations, and 13 an extensive assortment of libraries for linear and non-linear solvers.

14 Cast3M (www-cast3m.cea.fr/): Cast3M is a multi-physics code dealing with various 15 applications, initially developed with a finite element scheme for nuclear reactor applications. 16 It consists of various elemental bricks called procedures that can be organized together for the 17 resolution of more complex problems or equations. Treated domains are solid and structural 18 mechanics, as well as fluid flow and heat transfer. Resolution of the governing equations for 19 transport in porous media has been under development since the 90s. Cast3M now provides 20 tools to resolve saturated flow, unsaturated flow (Richard's equation and multi-phase flow), 21 Eulerian and Lagrangian transport by means of finite volume and mixed hybrid finite element 22 schemes. The latter has proved accurate and efficient for nuclear waste storage applications 23 (flow and transport) within an intercomparison exercise (Bernard-Michel et al., 2004). Several 24 extensions have been developed for coupled physics, taking advantage of the modular 25 properties of the code. For instance, the approach for coupling between surface and sub-surface 26 transfer was part of a recent intercomparison exercise (Kollet et al., 2016). One may refer to 27 Grenier et al. 2013, Roux et al. 2017 and Grenier et al. (accepted PPP) for applications in cryo-28 hydrology.

29 **COMSOL** Multiphysics (www.comsol.com/comsol-multiphysics) is a general-purpose 30 software platform for numerical modelling of coupled and multiphysics problems. Here, the 31 equation-based modelling for general second-order systems of non-linear partial differential equations is used. The application for cryo-hydrology has been developed for paleo-permafrost
 simulations in Great Britain (Scheidegger et al. under review).

3 DarcyTools is a code for simulation of flow and transport in porous and/or fractured media. 4 The code implements a finite volume approach on adapted Cartesian grids with equivalent continuous porous medium upscaling techniques. It is intended to be applicable to a wide range 5 6 of groundwater flows although initially developed for the analysis of nuclear waste repositories. 7 DarcyTools is strongly coupled for thermo-hydraulics, hydro-mechanics, hydro-chemistry and 8 unsaturated flow. The coupling is achieved by modified Picard schemes and the sets of linear 9 equations are solved by a parallel multigrid preconditioned block-GMRES solver. For more 10 details one may refer to (Svensson & al. 2010; Svensson & Ferry 2014).

**FEFLOW** (Finite Element subsurface FLOW system) is a computer program for simulating groundwater flow, mass transfer and heat transfer in porous media and fractured media. The program uses finite element analysis to solve the groundwater flow equation under both saturated and unsaturated conditions as well as mass and heat transport, including fluid density effects and chemical reaction kinetics for multi-component reaction systems. Refer to (Diersch, 2014; Anbergen et al. 2014).

17 FlexPDE (www.pdesolutions.com) is a general purpose scripted finite element model builder 18 for partial differential equations. Developments and recent applications include the field of 19 coupled thermo-hydrological modelling (Bense et al., 2012; Bense et al., 2009) as well as geo-20 mechanical couplings (Rühaak et al., 2014).

21 The **GEOAN** computer code is a numerical model for calculation of groundwater head, flow 22 (saturated/unsaturated), and transport (solute concentration and heat) in three dimensions, as 23 well as surface water flow. The temperature calculations can include creation of ice and 24 permafrost. A simulation may also include density effects, deformation of the medium and 25 hydromechanical effects. The mathematical model is based on the continuum approach, the 26 finite difference method and a block centered flow approach. GEOAN includes solvers for 27 parallel processing and a model may include tens of millions of nodes/cells. Considering 28 permafrost simulations the GEOAN computer code was used in a paper that deals with the 29 impact of climate cycles and permafrost on future groundwater flow in the Paris Basin (Holmén 30 et al., 2011).

1 Ginette: Ginette was initially developed at Metis (UPMC) to deal with interactions between 2 streams and aquifers, as they fluctuate from a connected to a disconnected status. Numerical 3 simulations of experimental laboratory results reproducing such conditions provided the 4 opportunity to test the coupled 1D surface water - 2D variably saturated groundwater code 5 (Rivière et al., 2014). Ginette was then extended to include coupled heat transfer and water flow 6 in saturated porous media and is now jointly developed by Metis and MINES ParisTech (PSL 7 Research University). The code was compared to experimental data acquired on a complex 8 laboratory system to provide validation on the physical processes and mathematical 9 formulations, in particular for the representation of density change between frozen and liquid 10 water (Rivière et al., submitted). Real-world cryo-hydrogeological paleo-applications, which 11 have been presented in conferences (e.g. Jost, 2011; Jost et al., 2014), were also proposed using 12 Ginette, requiring some additional adaptation to the specific needs of basin-scale calculations.

13 **MELT** is a 2D multiphase flow and transport simulator developed for modelling freeze-thaw 14 processes in saturated porous media. It was designed specifically for modelling the interactions 15 of submarine permafrost, gas hydrate, and multi-phase submarine pore fluid flow, with specific 16 attention to density-driven flow of fresh and saline pore fluids at Arctic coastlines (e.g. 17 submarine groundwater discharge). It has been developed by Jennifer M. Frederick (now at 18 Sandia National Laboratories, NM, USA) over the course of her thesis work at U.C. Berkeley, 19 and post-doctoral studies at the Desert Research Institute, Reno, NV, USA. MELT uses the 20 finite volume method to solve for flow and scalar transport based on two-phase Darcy's Law, 21 conservation of mass (hydro), and conservation of energy (thermo). MELT is based on the 22 IMPES algorithm with up-winding (i.e., implicit pressure, explicit saturation) for the 23 pressure/flow solution, with scalar transport (i.e. heat and mass) solved sequentially. Refer to 24 Frederick and Buffet (2014).

25 PermaFoam: PermaFoam is an OpenFOAM® solver dedicated to cryo-hydrogeology 26 modelling. OpenFOAM® (openfoam.com and openfoam.org) is an open-source tool box for 27 computational fluid dynamics that is broadly used in both industrial and academic applications. 28 One of its main strengths is its capability to use efficient parallel computing techniques. The 29 PermaFoam solver, which deals with coupled heat transfer and water flow in variably saturated 30 and heterogeneous porous media, takes advantage of these parallel computational options to 31 handle the numerical difficulties associated with the strong couplings and non-linearities 32 encountered in cryo-hydrogeology modelling. A paper related to the application of PermaFoam to the study of the permafrost dynamics in an experimental watershed of central Siberia is currently under review (Orgogozo et al., submitted). Regarding resolution of the water flow equation, since PermaFoam is based on the RichardsFoam2 solver, the reader may refer to the publications associated with this latter solver (Orgogozo et al., 2014, Orgogozo, 2015) for additional numerical details.

6 **PFLOTRAN-ICE** refers to the **PFLOTRAN** code (http://www.pflotran.org/) with the 7 multiphase ice-water-vapor flow physics module enabled. PFLOTRAN is an open source, 8 massively parallel subsurface flow and reactive transport code which can solve a system of 9 generally non-linear partial differential equations describing multiphase, multicomponent and 10 multiscale reactive flow and transport in porous materials. The code is designed to run on 11 massively parallel computing architectures as well as workstations and laptops. Parallelization 12 is achieved through domain decomposition using the PETSc (Portable Extensible Toolkit for Scientific Computation) libraries. Capabilities in addition to ice-water-vapor flow physics 13 include modules for thermo-hydro-chemical interactions, supercritical CO2, surface flow, 14 15 sorption, precipitation and dissolution processes and reactive transport. Refer to Karra et al. (2014). 16

17 SMOKER is a finite element numerical model for solving complex density-dependent 18 groundwater flow, contaminant transport, groundwater age, and thermal energy transport 19 problems. The model can be used to solve one, two, or three-dimensional transport problems 20 within a variety of hydrogeological systems, including discretely-fractured porous media. 21 Originally developed as a research tool to study ATES (Aquifer Thermal Energy Storage) 22 systems, the model can be used for virtually any application involving the storage or transport 23 of thermal energy in the subsurface where temperatures remain < 100 °C. The SMOKER model 24 and related CHeat model (Chemistry & Heat) have been tested and applied to a variety of 25 hydrogeological systems, including applications to hydrothermal systems (e.g. "Black 26 Smokers", Yang et al. 1996), heat storage systems (Molson et al. 1992), groundwater age 27 (Molson & Frind, 2012), and permafrost degradation (Shojae-Ghias et al., 2016). For further 28 information, see: http://www.science.uwaterloo.ca/~molson/

29

30 SUTRA is an established USGS groundwater flow and coupled transport model (Voss and 31 Provost, 2002) that has been applied since the early 1980s to simulate density-driven 32 groundwater flow problems including saltwater intrusion and thermal convection. More

1 recently, the code has been enhanced to allow for pore water phase change in the governing 2 equations (McKenzie et al., 2007; McKenzie and Voss, 2013) to simulate hydrogeologic 3 systems that experience ground freezing and thawing. Various iterations of this expanded code 4 have been applied to simulate groundwater flow and coupled energy transport in environments 5 with permafrost or seasonally freezing ground (e.g., McKenzie et al., 2006; 2007; Ge et al., 6 2011; McKenzie and Voss, 2013; Wellman et al., 2013; Kurylyk et al., 2014; 2016; Briggs et 7 al., 2014). Recent advancements beyond the code described by McKenzie et al. (2007) include 8 freeze-thaw capabilities in the unsaturated zone, more complex density functions, and pre-9 programmed functions for soil freezing, relative permeability, and desaturation.

# Appendix B – Spatial and temporal sensitivity analyses, sensitivity to the freezing curve

#### 4 Spatial and temporal sensitivity analyses

5 In a preliminary convergence test, sensitivity analyses to spatial discretization (while keeping 6 the time step fixed as in the reference simulation) and to temporal discretization (while keeping 7 the mesh size fixed as in the reference simulation) were conducted for both benchmark cases 8 with the Cast3M code. PermaFoam (Orgogozo et al., 2016) was also used in a spatial 9 convergence study (using an automatically calculated time step), covering a large range of 10 elements from a few thousand to millions. In addition, a convergence study of the threshold 11 parameters for the non-linearities and coupling convergence loops was completed. Such tests 12 had been previously provided with the Lunardini case since its analytical solution provides a 13 useful reference.

Here, convergence studies carried out with Cast3M were first completed with Case TH3 since it has a smaller domain allowing the use of refined grids at limited computational cost. A head gradient of 3% was imposed corresponding to realistic values. The mesh size for Case TH2, with a larger simulation domain, was directly adapted from the Case TH3 convergence study.

18 The variability issued from the convergence tests and for the full set of performance measures 19 is provided in Table B.1 for Cases TH2 & TH3. Variability is expressed in percentage, as the 20 absolute range taken by the performance measure divided by the median value. A large range 21 of time and space increments were considered starting from relatively coarse conditions. 22 Results show variable sensitivities. For the spatial convergence study, the larger range in 23 variability corresponds to the Case TH3 performance measure of conductive fluxes through the 24 upper and lower boundaries (29.2%). This result highlights the need for accurately simulating 25 the interplay between advective heat flux (which requires a sufficiently refined longitudinal 26 discretization) and conductive heat flux from the imposed boundary conditions (which requires 27 a sufficiently refined transverse discretization to accurately capture the local thermal gradient 28 at the boundaries). The time for system closure is less impacted by the discretization (0.7 %). 29 For the time-step convergence study, the greatest variability (7.2 %) is obtained for the first 30 performance measure (time for total thaw). This punctual measure is clearly more sensitive to

the discretization strategy than the other performance measures which correspond to integrated
 averages (of flux or total water volume) over the entire domain.

3 These results present important consequences in terms of simulation intercomparisons. First, 4 these ranges provide a quantitative estimation of the maximum uncertainty associated with any simulation. For practical reasons, due to the high computational costs associated with 5 6 "converged" simulations, the reference simulations provided during the course of the 7 benchmark exercise will probably not be "fully converged". This evaluation of the associated 8 ranges, however, can provide insight to explain the discrepancies between the results of the 9 various codes running the same cases. Further, some performance measures that would appear 10 too sensitive to the spatial and temporal discretization should probably be discarded because they would not allow sufficient discrimination between simulation results. 11

Case TH2 – "Frozen Inclusion"	Time for total thaw	Total heat flux after 9.10 <sup>4</sup> s	Total water volume after $4.10^4$ s
Δx sensitivity range	1.4 %	1.2 %	0.015 %
$\Delta t$ sensitivity range	7.2 %	0.6 %	0.05 %
Case TH3 – "Talik Opening/Closure"	Closure time	Upper flux after 3.10 <sup>4</sup> s	Total heat after 3.10 <sup>4</sup> s
Δx sensitivity range	0.7 %	29.2 %	0.03 %
Δt sensitivity range	3.4 %	0.6 %	0.2 %
Case TH3 – Regular mesh	Closure time	Upper flux after 3.10 <sup>4</sup> s	Total heat after 3.10 <sup>4</sup> s
Δx sensitivity range	7.4 %	63.5 %	6.9 %

Table B.1: Variability of the performance measures for the full range of time steps and mesh sizes considered in the sensitivity study (Case TH2, "Frozen Inclusion"): for time convergence, time steps are 480, 240, 120, 60, 30, and 15 s. For spatial convergence, discretization ranges from  $1.96 \times 10^{-2}$  m to  $3.98 \times 10^{-3}$  m.

16

17 The reference case is run with a time step of 60 s and a mesh size of  $6.94 \times 10^{-3}$  m for a head

18 gradient of 3%. For Case TH3, "Talik Opening/Closure", the time steps considered are 1500,

1 600, 300, 120, 60, 30, 12, 6, and 2.4 s. Lateral spatial discretization ranges from  $1.96 \times 10^{-2}$  m to 2  $2.49 \times 10^{-3}$  m (with the circular interface explicitly reproduced using triangular element 3 automatic meshing). The reference simulations are completed with an average mesh size of 4  $5.4 \times 10^{-3}$  m. For Case TH3, a similar spatial convergence study was conducted, while 5 considering a regular mesh onto which the geometry of the initial condition is projected.

6 Another practical point related to the influence of the meshing strategy is now briefly discussed. 7 These simulations were first made on a regular mesh as in the previous test case (Case TH2, 8 "Frozen Inclusion"). The initial conditions were directly projected onto the regular mesh 9 without any special effort to match, for instance, the total initial heat requirements. Results 10 showed that a strict spatial convergence is more computationally demanding with such a 11 meshing strategy due to the variability of the actual simulated initial condition. A dedicated 12 discretization strategy was therefore preferred. Moreover, the total range of variability as previously studied notably increases: results are compared in Table B.1. For the codes taking 13 14 part in a benchmark for Case TH3 which had no dedicated meshing strategy, the simulations 15 could likely be improved by imposing greater control on the total initial heat and initial shape. 16

Following the convergence studies, the parameters associated with the Cast3M reference simulations presented below were chosen as a compromise between "full" convergence and computational efficiency. This allowed running accurate sensitivity cases (presented later) while maintaining manageable computational effort. The associated parameters are provided in Table B.2.

	Nb Elements	Δx	Δt	Nb time steps	Average Nb
					of iterations
Case TH2	31,014	6.94 mm	7.5 s – 60 s	3500 - 15000	20
Case TH3	17,272	(2.7 – 7.6) mm	7.5 s – 60 s	3500 - 20000	20

Table B.2: Parameters associated with the Case TH2 & Case TH3 reference simulations: number of elements, size of the square elements ( $\Delta x$ ), range of time step ( $\Delta t$ ) varied depending on head gradients, and number of iterations within a time step in the initial phase change period

#### **1** Sensitivity to the saturation curve parameters

2 All test cases consider a saturated porous medium with an exponentially shaped freezing curve 3 varying over approximately 1°C between the start of freezing at 0°C and complete freezing by 4 about -1°C (leaving a residual saturation of liquid water) (Table 2). For real world applications, a large range of other freezing functions could also be considered (e.g. linear, exponential, 5 6 power law) as well as smaller or larger freezing ranges. A recent discussion on this issue is 7 provided by Kurylyk and Watanabe (2013). The 1°C freezing range chosen for the benchmark 8 was intended as a good compromise between very steep freezing fronts, which are numerically 9 hard to handle (with large changes in unfrozen water content over small temperature ranges), 10 and smooth fronts with smaller changes in unfrozen water content over larger temperature 11 ranges.

12 The influence of the freezing curve for the simulations appears very important from a sensitivity 13 analysis conducted on Case TH2. In these cases, the W parameter in Table 2 controlling the 14 slope of the freezing curve was varied, resulting in freezing ranges extending over temperature 15 intervals between 0.1°C and 4°C (Bt value in Figure B.1, the reference case is in **bold** and blue 16 color: 1°C), while keeping the residual water saturation (S<sub>Wres</sub>) fixed at 0.05. The corresponding 17 sensitivity of TH2 PM1 for a head gradient of 3% is presented in Fig. B.1. Results show a 18 dramatic influence of the freezing range: phase change starts earlier for a large freezing range 19 which also modifies the times to reach the 0°C threshold. The relative threshold time variability 20 is 17.3 %. The impact on TH3\_PM1 was also significant (but not illustrated here), leading to a 21 variability of the relative threshold times for talik closure of 103.5%. 22 The freezing range thus has a major control on the temperature evolution curves and any

The freezing range thus has a major control on the temperature evolution curves and anydeparture from the benchmark specifications clearly induces large discrepancies.

- 24
- 25

# Appendix C – Quantitative assessment of PM results, sources of discrepancies, sensitivity to head gradients

4 Reassessment of PM results with quantitative measurements: standard
5 deviation evolution

6 We introduce here a measure of the spread of the curves to obtain a more rigorous quantitative 7 assessment of the PM dispersion. The standard deviations of all curves, or equivalently the 8 square root of the L2 norm, based on the average of all curves, are computed to quantify the 9 divergence in the results. As mentioned earlier, since no reference simulation can be proposed, 10 the results among the participants themselves were employed to compute the mean. The sample 11 mean and sample standard deviation are expressed below (Eq. C.1 & C.2) where each PM time 12 evolution curve is the  $S_i(t)$  signal, with *i* varying from 1 to N = 13.

13 
$$Mean(t) = S(t) = \frac{1}{N} \sum_{i=1}^{N} S_i(t) \qquad (C.1)$$

3

15 
$$Standard Deviation (t) = \sqrt{\frac{1}{N} \sum_{i=1}^{N} (S_i(t) - S(t))^2} \qquad (C.2)$$

These statistical parameters are useful to (i) visualize and discuss the time evolution of major discrepancies throughout the various PMs, (ii) obtain a quantitative basis to understand the impact of spatial and temporal convergence on the results and their effect on the general spread of the curves, and (iii) discuss the influence of the advective flux on the different model results.

20 Figure C.1 provides the evolution of the discrete (i.e. not integrated) PMs for TH2 and TH3 21 (TH2\_PM1 and TH3\_PM4\_Pt1). For example, the green curve in Fig. C.1a (TH2\_PM1) 22 displays the changes in standard deviation with time for a hydraulic gradient (GH) of 3% (refer 23 also to corresponding results shown in Fig. 9a, TH2 PM1). All of the codes begin with the 24 correct minimum temperature of 5°C, and thus the initial standard deviation is zero (Fig. C.1). 25 The discrepancies then increase to a maximum, followed by a local minimum value after  $10^4$  s 26 and subsequent plateau. The largest spread of the curves is observed close to the threshold time (when the minimum temperatures reach  $0^{\circ}$ C, at approximately  $7 \times 10^4$  s). Afterwards, the 27 standard deviation again generally declines, with a slight increase before the disappearance of 28

1 the plume. Finally, the standard deviation returns to near-zero as the simulations return to a 2 steady-state uniform temperature of 5°C after  $18 \times 10^4$  s.

3 The standard deviation is greatest around the threshold time as a result of the cumulative 4 thermal degradation by conduction, advection and phase change, from the initial inclusion. The first standard deviation maximum is related to how the initial conditions were managed. The 5 6 initial Boolean temperature conditions are numerically difficult to simulate, leading to 7 oscillations that have to be damped numerically. When reaching the phase change period, the 8 standard deviation plateau is a result of the impact of PFLOTRAN-ICE using a different 9 freezing function while other codes are almost identical. The later-stage standard deviation 10 evolution (after  $10^5$  s) probably results from accumulated shorter time differences or from differences in advection and dispersion of the colder temperature plume evolving from the 11 12 initial inclusion.

Similar standard deviation variations are observed for the other imposed head gradients but correspond to shorter time frames (Fig. C.1). The final steady-state condition is reached more quickly for higher head gradients as a result of stronger advection leading to more rapid thermal degradation of the initial inclusion (refer to the blue and rose curves in Fig. C.1a, representing 9 and 15 % gradients). The structure for the 0 % case (red) is different and corresponds to longer simulation times due to purely conductive heat transfer.

19 Normalized standard deviations were also calculated to better compare the results among the 20 PMs (Table C.1). With TH2 PM1, for example, the standard deviations were divided by 10°C, 21 which represents the range of simulated temperatures (-5 to  $+5^{\circ}$ C). Similar procedures were 22 conducted to normalize all of the PMs listed in Table C.1, with the results indicating that the 23 models were in general agreement with low normalized standard deviations of below 5 % for 24 TH2\_PM3, TH3\_PM3, and TH3\_PM4. Standard deviations are above 10 % for TH2\_PM1 25 where the influence of the freezing curve expression is significant. No normalization was 26 performed for all flux-based PMs (TH2\_PM2 and TH3\_PM2), while the special sensitivity of 27 the 6% head gradient case, not included here, is further discussed in the main body.

28

Maximum	Norm	Gradient	Gradient	Gradient	Gradient
(Norm. Std.		= 0 %	= 3 %	= 9 %	= 15 %
Dev.)					
TH2_PM1	$\Delta T = 10^{\circ}C$	9	12	16	17
TH2_PM3	$\Delta V = 4 \times 10^{-2} \text{ m}^3$	3	3	3	3
TH3_PM1	$\Delta K = 4 \times 10^{-4} \text{ m/s}$	-	9.5	7	6
TH3_PM3	$\Delta E = 8 \times 10^7 \text{ J}$		2.3	4.7	5.2
TH3_PM4_Pt1	$\Delta T = 10^{\circ}C$		3.1	3.2	2.5
TH3_PM4_Pt2	$\Delta T = 10^{\circ}C$		1.9	3.9	4.3

Table C.1: Maximum values for the normalized standard deviation evolution (%)

### 2 Sources of discrepancies

A critical question for the code comparison exercise is to understand the origins and causes of
discrepancies. One source of discrepancy was already mentioned, being related to differences
of equation sets and characteristic curves.

6 Another important source of discrepancy is the codes' sensitivity to different initial conditions. 7 As seen from the total liquid water volumes (TH2\_PM3, Fig. C.2a) or total sensible heat initial 8 conditions (TH3\_PM3, Fig. C.2c), the standard deviation for this initial time propagates 9 throughout the entire simulation time. Steady-state conditions are a 5 °C uniform domain, which 10 all codes clearly agree on. Fig. C.2b displays the variability of the initial water volumes, and 11 Fig. C.2d shows the initial total heat, among all 13 codes, the dotted line giving the calculated 12 theoretical value. This variability results from different meshing strategies, in some cases mixed 13 with differences in the characteristic curve expressions. This is particularly the case for TH3, 14 in which specific meshing was required to represent the spherical-shaped initial conditions (see 15 Fig. 4). Some codes use a dedicated meshing routine which accurately represents the boundaries 16 of the frozen zone, whereas other codes project the initial temperature fields onto a regular 17 orthogonal mesh.

18 A third cause of discrepancy may be related to the convergence accuracy. Although participants 19 were asked to provide spatially and temporally converged simulations, all participants were

1 likely not able to complete a proper convergence study. Briefly, a convergence study is an 2 exercise to demonstrate that the mesh and time step size do not affect the simulation outcomes. 3 A full convergence study is ideally a pre-requisite for both test cases (TH2 & 3), and should 4 include all gradients considered. This exercise is very computationally intensive and was only 5 partially completed, for example it was not carried out for all head gradients. In an effort to 6 study the influence of mesh and time refinement, the convergence studies made available by 7 two participants are integrated into the analysis (see Fig. C.2a & b, dashed lines, Cast3M and PermaFoam codes). Mean and standard deviations were computed, based on Eq. C.1 & C.2, 8 9 and considering the PM curves obtained from various levels of spatial and temporal 10 discretizations (refer to Appendix B). The general conclusion is that these convergence studies 11 show similar evolution in time and amplitudes as compared with the intercomparison results 12 (compare plain and dotted lines in Fig. C.3). This is especially true for TH2\_PM1 (Fig. C.3) 13 where the similar standard deviation curves suggest that the spatial and temporal discretization 14 could be responsible for such spreads in the code results, in particular at the same times as the 15 systems undergo critical changes. The convergence studies conducted by both the Cast3M and 16 PermaFoam codes considered a large range of variability (including coarse meshes that were 17 not used for the final reference simulations) so that no direct conclusion can be drawn in terms 18 of relative amplitude contributions. These results, however, indicate the importance of 19 convergence studies, and how they affect the inter-code comparison results.

A fourth source of discrepancy could be related with the accuracy in the convergence of nonlinear loops, especially that associated with the latent heat term. Although not illustrated here, the influence of this accuracy was often referred to among modelers, especially in the case of TH3 where conflicting conditions lead to strong oscillations in the resolution of the temperature field. As suggested in the main text (Discussion and Perspective section), valuable rules to handle this difficulty can be obtained from running the 1D Lunardini analytical solutions.

#### 26 Effect of thermal advection

Advection is responsible for accelerated thermal degradation of frozen zones by heat exchange and heat transport. Difficulties were expected in representing advection since most of the numerical approaches (FE, FD, FV) are adapted primarily for solving conduction-dominated processes. The benchmark cases including advection were considered for various levels of head gradients (0, 3, 9, and 15 % for TH2; 3, 6, 9, and 15 % for TH3).

1 In all Figures C.1 to C.3, the maximum standard deviations associated with all gradients lie 2 within a factor of two, indicating that codes achieve a similar convergence independent of head 3 gradient levels. However, the maximum standard deviation may not be the most appropriate 4 measure. Another metric for assessing the impact of gradient on the results was proposed - the 5 integrals of the normalized standard deviation curves, computed over identical time frames. The 6 results for TH2 are plotted in Fig. C.4. The concept behind this metric is to normalize all 7 integrals to have all of the information on one plot. The same could not be done for TH3 because 8 the integration interval would encompass the entire transient period before reaching steady 9 state. The time was too long for low gradients and such long simulation times were not provided 10 by all participants. The same is true for TH2\_PM1, therefore the 0 % gradient is also not 11 represented in Fig. C.4. Results show that the spread of the curves is of the same order of 12 magnitude for the large range of flow velocities considered (imposed head gradients of 3, 9, 13 and 15 %) with a weak tendency for the spreading to be reduced as head gradients increase, 14 thus providing no clear and marked trend with increasing head gradients. 15 These results suggest that the advection term is apparently well handled or at least similarly

16 well between codes regardless of the rate of water flow. Though some codes applied an upwind

17 scheme for high advection levels, thus introducing some numerical dispersion, while others did

18 not, the convergence is not altered by high advection for the test cases considered.

19



























0.07





(f)


















Time (s)



Head Gradient