

# Off-axis electron holography for the quantitative study of magnetic properties of nanostructures.

*From single nano-magnets to complex devices*

Etienne SNOECK, Christophe GATEL,  
Robin Cours, Aurélien Masseboeuf



CEMES-CNRS

*29 rue Jeanne Marvig, 31055,  
Toulouse, France*



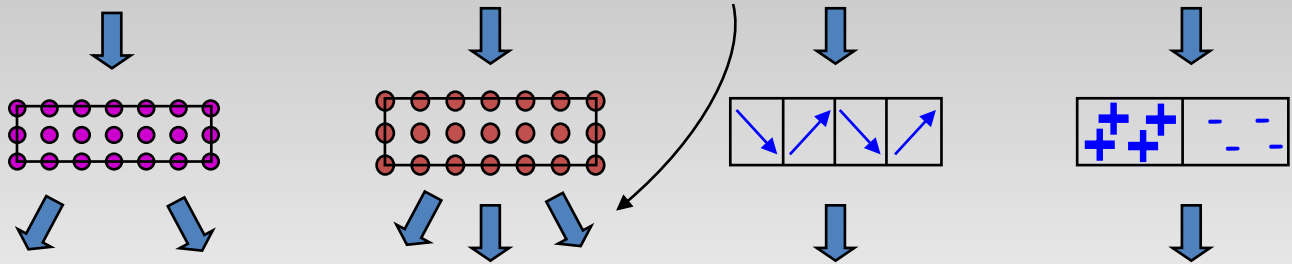
1. Spin configurations in size controlled single Fe nanomagnets => 0D
2. *In situ* electron holography of the dynamic field emanating from a HDD writer => 3D

# Electron Holography : Mapping fields

Interaction  
electron-matter

$$\psi(\mathbf{r}) = \sum_{\mathbf{g}} \tilde{\psi}_{\mathbf{g}}(\mathbf{r}) e^{2\pi i \mathbf{g} \cdot \mathbf{r}}$$

$\tilde{\psi}_{\mathbf{g}}(\mathbf{r})$  ← amplitude and phase



Phase shift

**Geometric**

**Crystalline**

**Magnetic**

**Electric**

$$\varphi =$$

$$\varphi_{\text{geom}}$$

+

$$\varphi_{\text{cryst}}$$

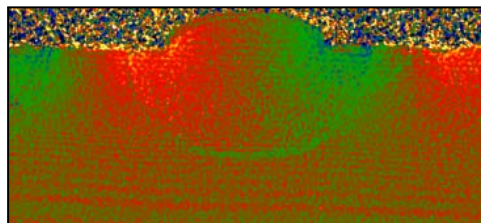
+

$$\varphi_{\text{mag}}$$

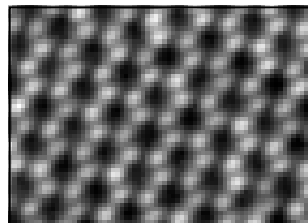
+

$$\varphi_{\text{elec}}$$

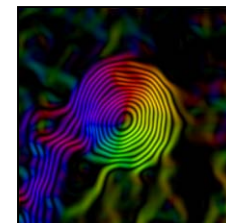
**Strain field**



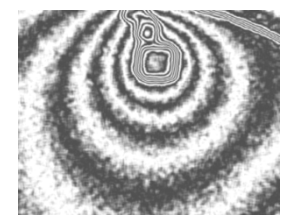
**Crystal structure**



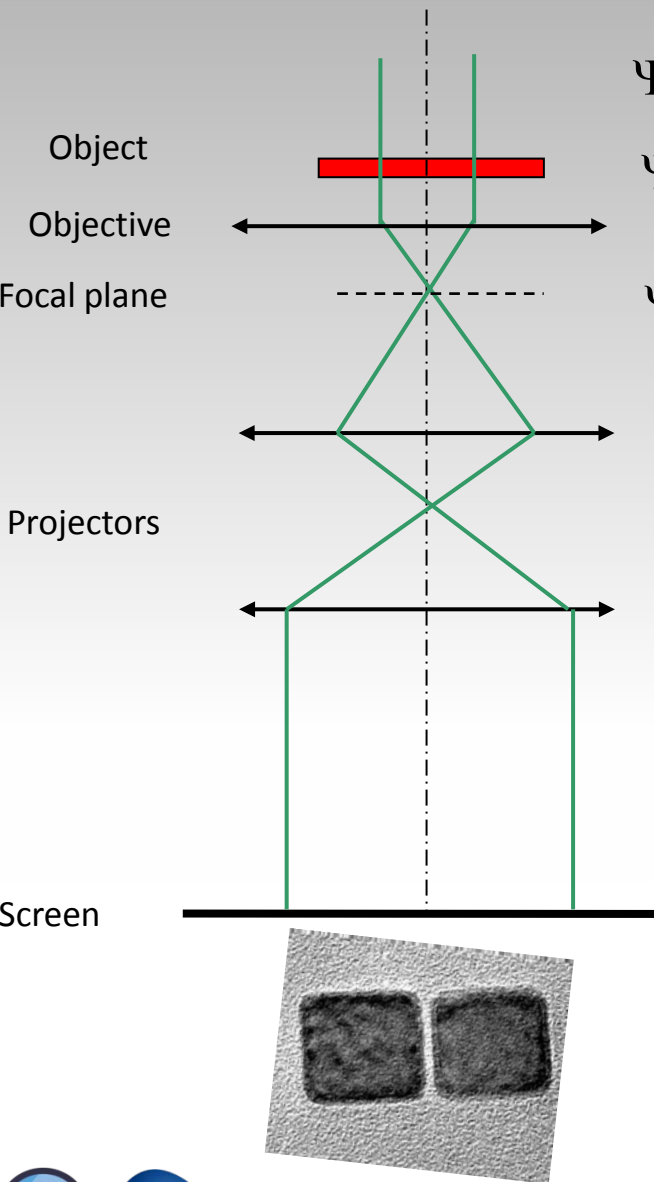
**Magnetic field**



**Electrostatic field**



# Electron wave in a TEM



$$\Psi_0 = \exp(i\mathbf{k} \cdot \mathbf{r})$$

$$\Psi_{obj} = a_0(\mathbf{r}) \exp(i\mathbf{k} \cdot \mathbf{r} + \phi_0(\mathbf{r}))$$

$$\Psi_s = a_s(\mathbf{r}) \exp(i\mathbf{k} \cdot \mathbf{r} + \phi_s(\mathbf{r}))$$

Phase shift after interaction with the object

Phase shift below the objective

$$I(x, y) \propto |\Psi_s|^2 \propto a_s^2(\mathbf{r}) \longrightarrow \phi_s(\mathbf{r}) \text{ is lost!}$$

# What information is carried by $\phi_s(\vec{r})$ ?

$$\Psi_0 = \exp(i\vec{k} \cdot \vec{r})$$



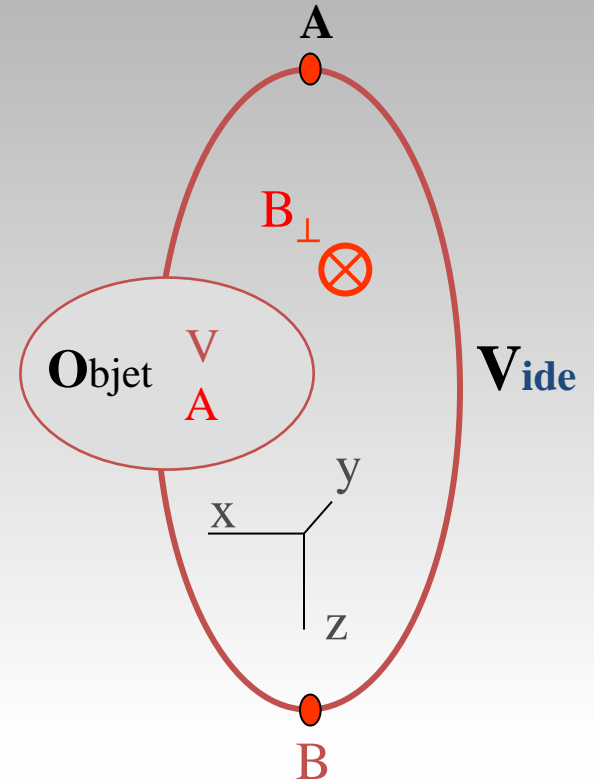
Electromagnetic field

- Electrostatic potential :  $V$
- Magnetic Potential vector :  $\vec{A}$



*Aharonov-Bohm*

$$\Psi_s = a_s(\vec{r}) \exp(i(\vec{k} \cdot \vec{r} + \phi_s(\vec{r})))$$

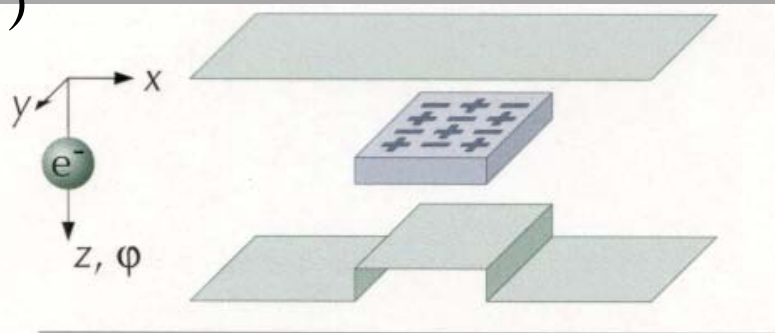


$$\begin{aligned} \phi_s(x, y) &= C_E \int V(x, y, z).dz - \frac{e}{\hbar} \int A_z(x, z).dz \\ &= C_E \int V(x, y, z).dz - \frac{e}{\hbar} \iint B_{\perp}(x, z).dx.dz \end{aligned}$$

$$C_E = \left( \frac{2\pi}{\lambda} \right) \left( \frac{E + E_0}{E(E + 2E_0)} \right)$$

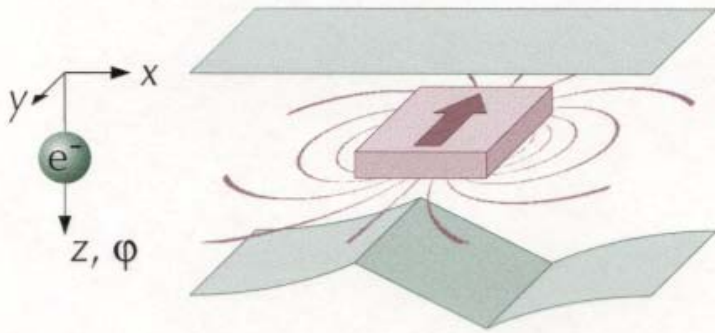
Electrostatic potential contribution to the phase shift

Magnetic contribution to the phase shift



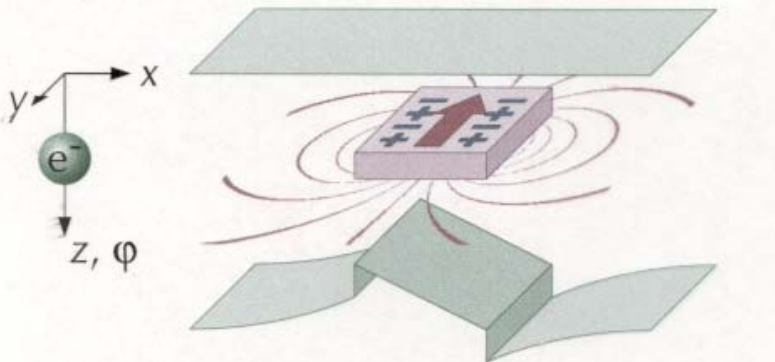
Phase shift induced by the local electrostatic potential:

$$\phi_{Elec}(x) = C_E \int V(x, y, z). dz$$



Phase shift induced by the local magnetic field :

$$\phi_{Mag}(x) = -\frac{e}{h} \iint B_{\perp}(x, z). dx. dz$$



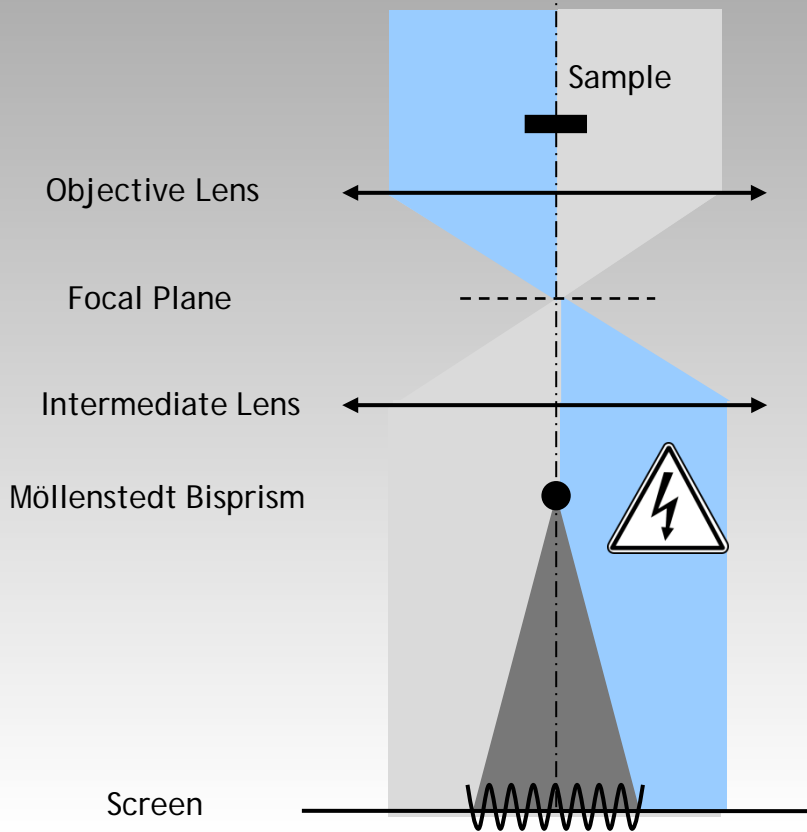
Total phase shift

$$\phi_{Total}(x) = \phi_{Elec}(x) + \phi_{Mag}(x)$$

But phase image  $\phi(x, y) = \phi^C(x, y) + \phi^M(x, y)$

→ Need to separate different contributions to the phase shift

## 2. Off-axis Electron Holography



$$\psi_0 = \exp(i\mathbf{k}\cdot\mathbf{r})$$

$$\psi(\mathbf{r}) = A(\mathbf{r}) \exp(i((\mathbf{k}\cdot\mathbf{r}) + \varphi(r)))$$

$$\Psi(\mathbf{r}) = A_s(\mathbf{r}) \exp(i((\mathbf{k}\cdot\mathbf{r}) + \varphi_s(r)))$$

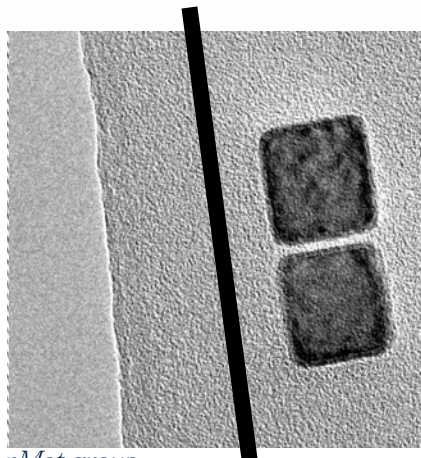
Incident beam



After the sample

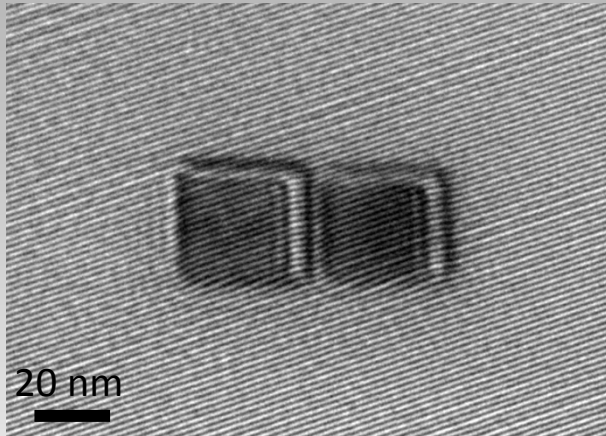


After the objective lens



$$\begin{aligned}
 I_{Holo} &= |\Psi_0 + \Psi^*|^2 + \text{background} \\
 &= 1 + A_s^2(x, y) \\
 &\quad + 2A_s(x, y) \cdot \cos(2\pi R_0 \cdot x + \varphi_s(x, y)) \\
 &\quad + I_{Inelast}(x, y)
 \end{aligned}$$

30nm Fe nanocubes

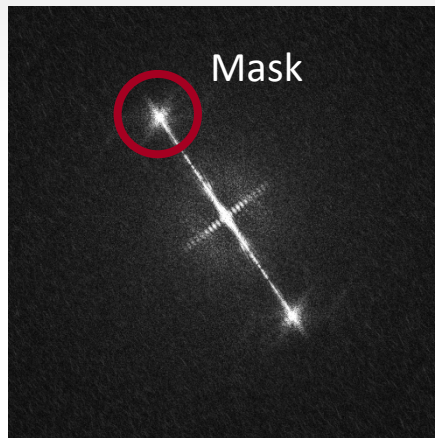


Hologram Image

Interference between a reference wave and the wave through the sample



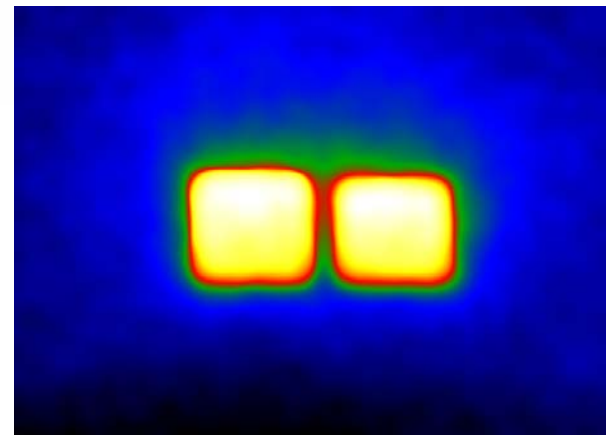
FFT



FFT<sup>-1</sup>



Amplitude image

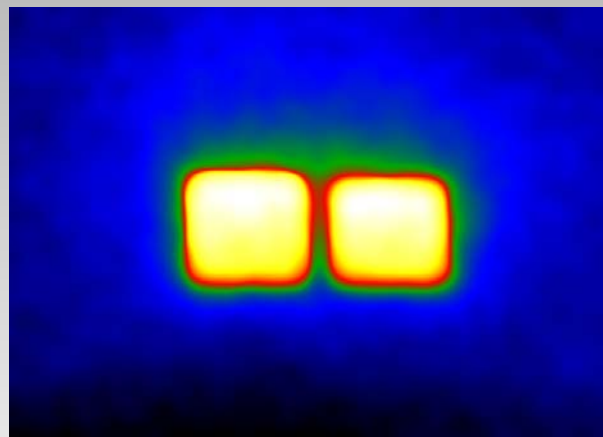
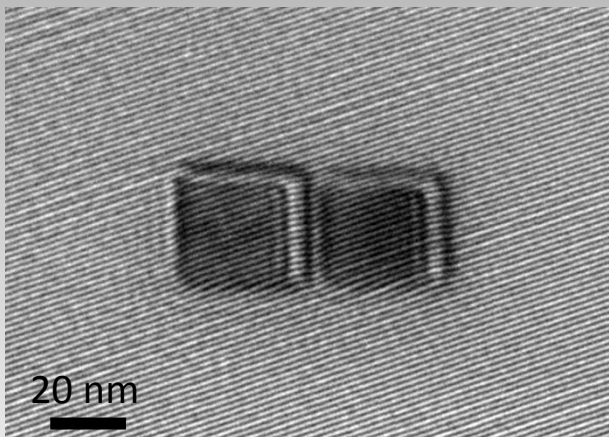


Phase image

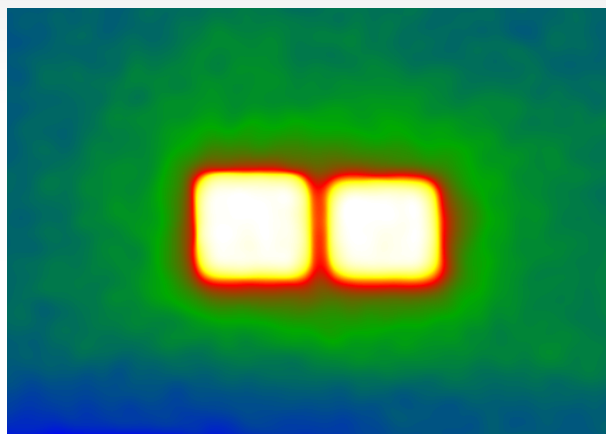
# Phase shift extraction and different contributions

30nm Fe nanocubes

$$\phi(\mathbf{R}) = \phi_{MIP,Elec}(\mathbf{R}) + \phi_{Mag}(\mathbf{R})$$



- Different methods to separate the contributions
- Need to record many holograms

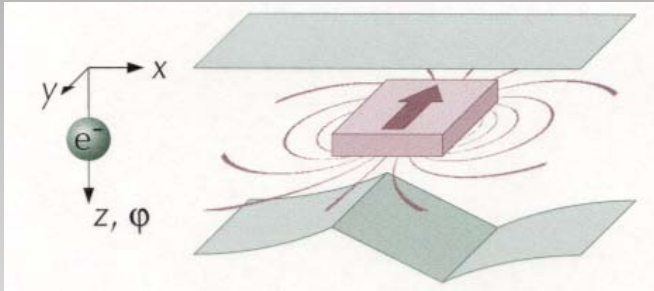


$$\phi_{MIP,Elec}(\mathbf{R}) = C_E \int V(\mathbf{r}) dz$$



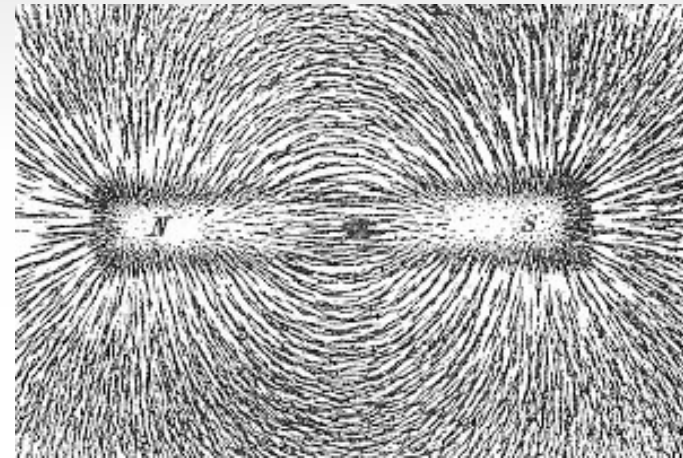
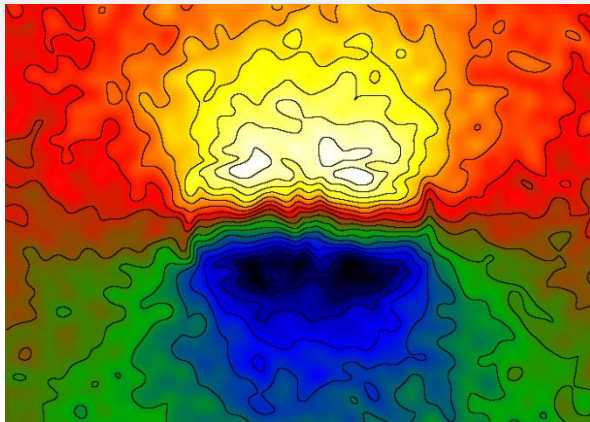
$$\phi_{Mag}(\mathbf{R}) = -\frac{e}{h} \iint \mathbf{B}_R(\mathbf{R}_\perp, z) dR dz$$



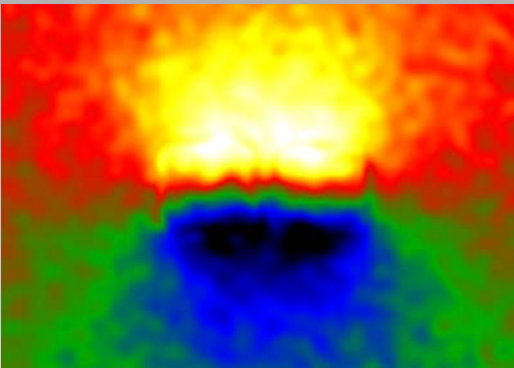


$$\phi_{Mag}(x) = -\frac{e}{h} \iint B_{\perp}(x,z).dx.dz$$

- The equiphase contours give the  $B_{\perp}$  direction  $\rightarrow$  contours lines = in-plane projection of the magnetic flux



# Magnetic components from $\phi^M$



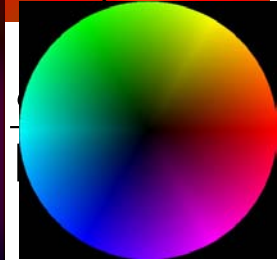
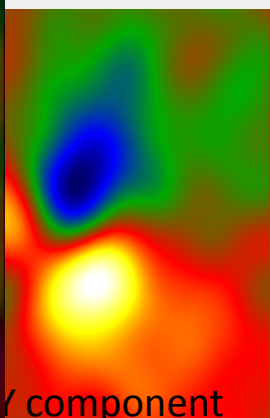
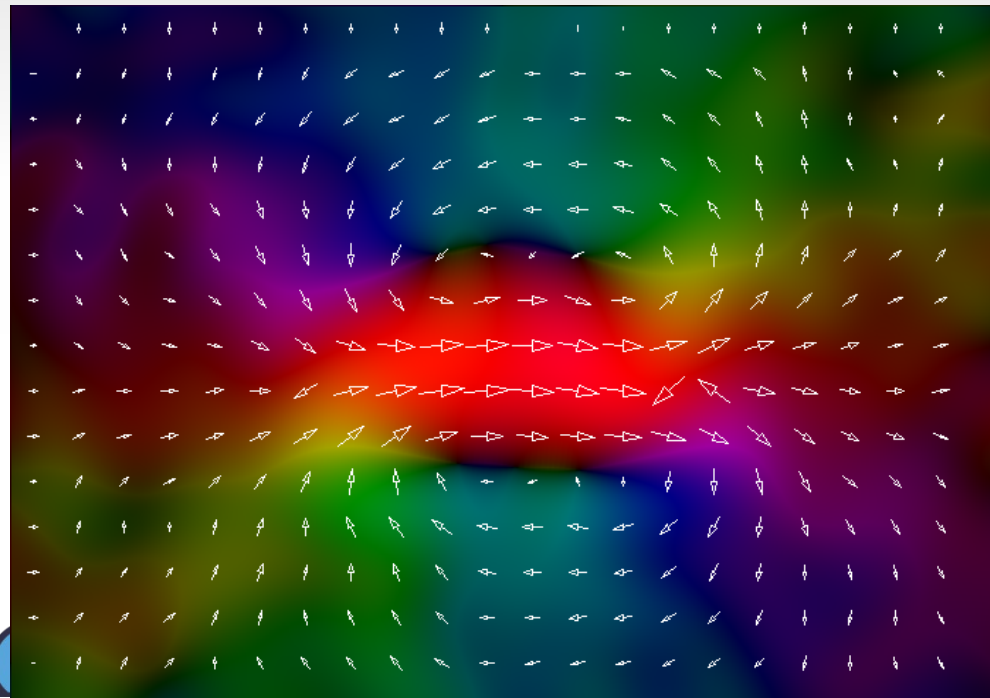
- The phase gradient is proportional to the in-plane  $B_{\perp}$  components of the induction

→  $B_x, B_y$  components

$$\frac{\partial \phi_{Mag}(y)}{\partial y} = \frac{e}{\hbar} B_x(y).t$$

( $t$  = thickness)

$$\frac{\partial \phi_{Mag}(x)}{\partial x} = \frac{e}{\hbar} B_y(x).t$$

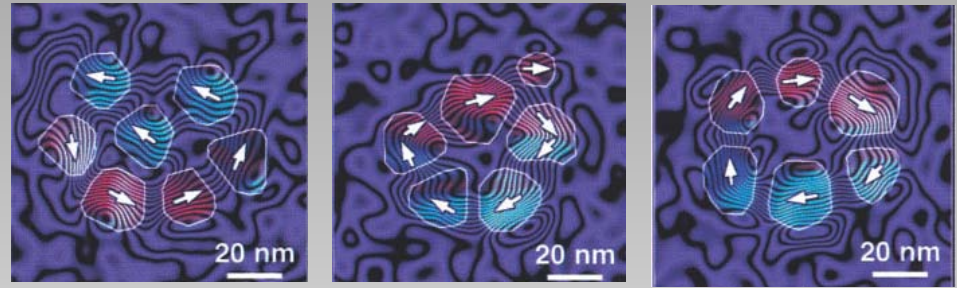


- Only planar components of the induction can be measured

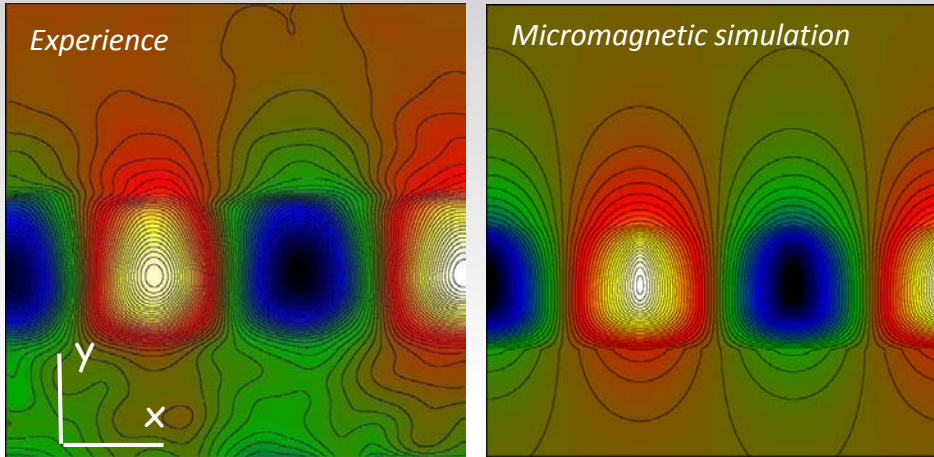
# Magnetic nanomaterials



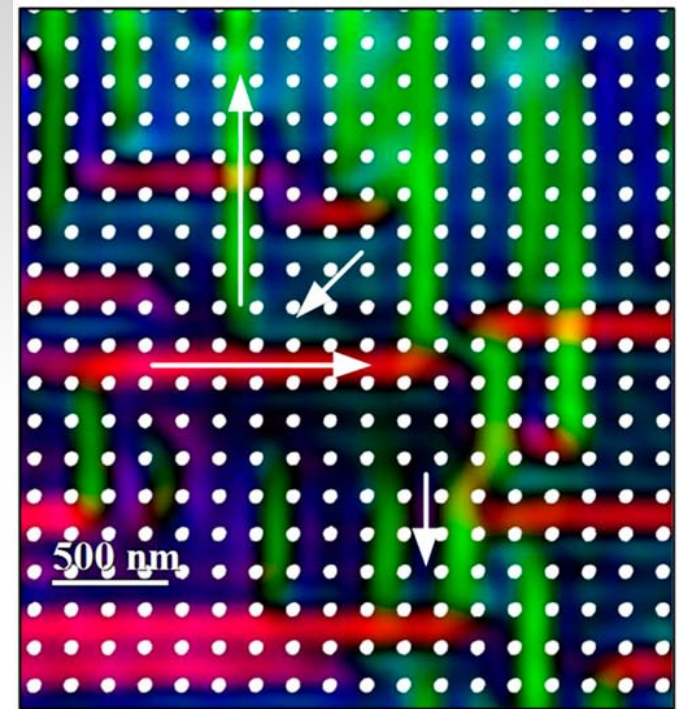
Hybrid DW in Ni nanocylinder - N. Biziere *Nano Lett* 2013



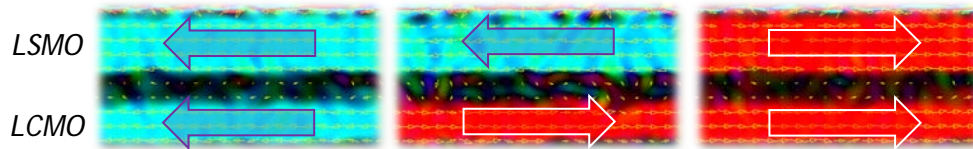
Magnetic coupling in polycrystalline Co nano-rings (*Rafal DB*)



Magnetic bits in FePd epitaxial thin with perpendicular magnetic anisotropy - A. Masseboeuf et al. *Nano Lett.*, 2009, **9** (8), pp 2803



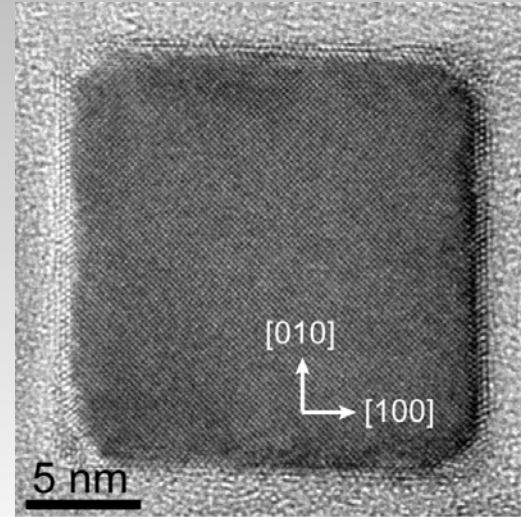
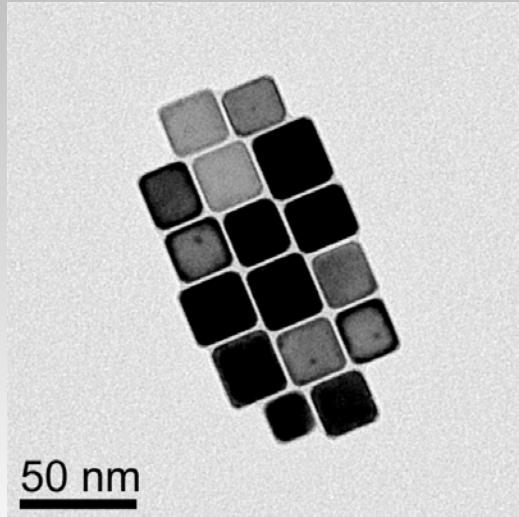
Super domain configuration in antidot array of FeNi - L.A Rodriguez *Nanotechnology*. 2014



LSMO/STO/LCMo Magnetic tunnel junction reversal

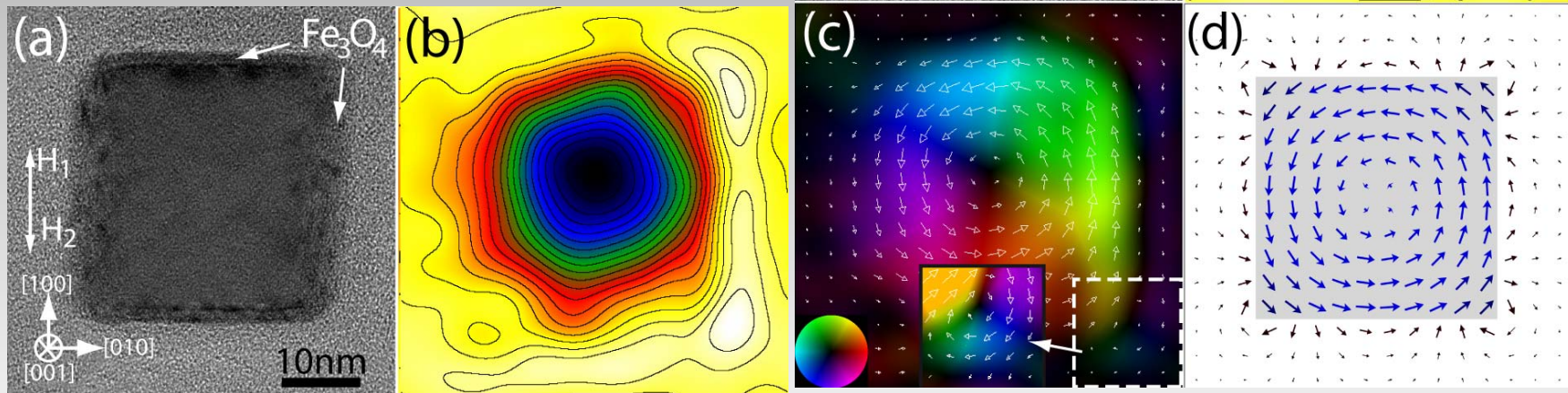
## Fe nanoparticles synthesized in liquid phase by organometallic chemistry

→ « Model » objects for the study of magnetic transition as a function of the size



- Nanocube: single-crystal *bcc* structure with {100} facets
  - $\langle 100 \rangle$  edges = magnetocrystalline easy axis.
- ~1 nm layer of  $\text{Fe}_3\text{O}_4$  shell resulting from the air exposition during sample transfer.
- Magnetometry experiments on powders of nanocubes showed the **same saturation magnetization  $M_s$  than bulk Fe (2.2 T)**.

## Magnetic configuration of a single 30nm Fe cube

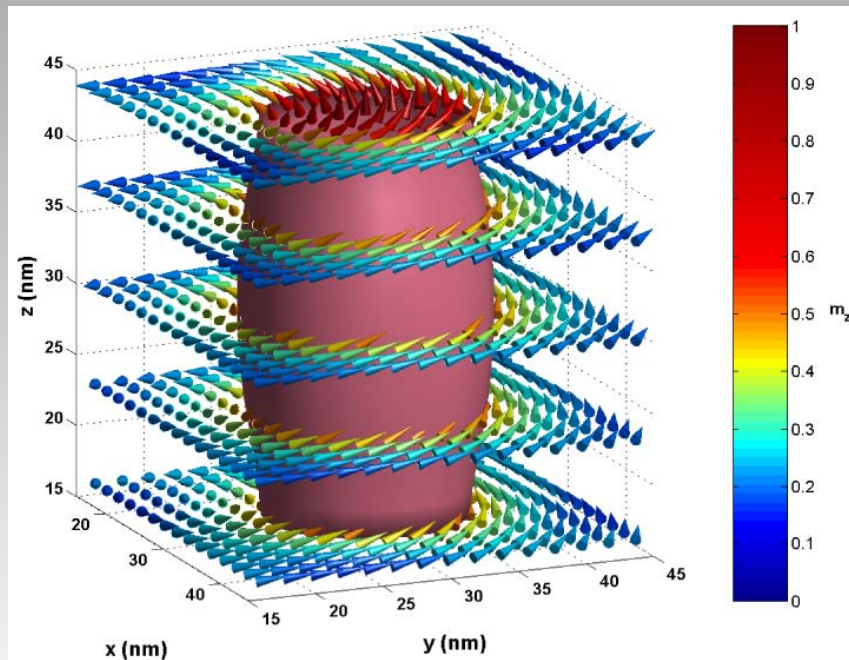


Spatial resolution on phase image  $\approx 5$  nm

Tecnai F20 in Lorentz mode

*Nanoletters*, **8**, 4293-4298 (2008)

- Axial symmetry of the induction: axis perpendicular to the (001) face.
- Complete flux closure in the vortex plane to minimize the magnetostatic energy.
- Agreement between simulation and experimental results.



- 3D view of a micromagnetic simulation of the vortex
- Competition between dipolar interactions and exchange energy
- Diameter : 16 nm at the centre  
14 nm at the surfaces

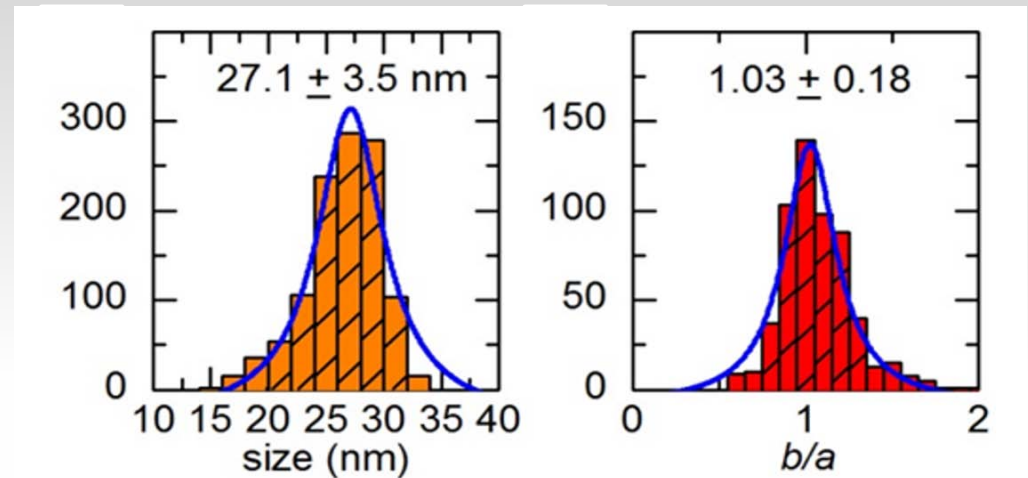
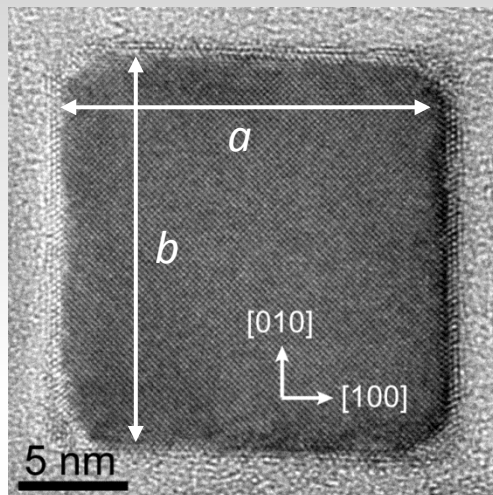


To study the Vortex -> SD transition, 2 main issues have to be solved:

- Determination of the 3<sup>rd</sup> dimension:

Evaluation of the squareness distribution, defined as  $a/b$  ratio : 18%

Nanocube thickness assumed as similar thickness to length  $c/a$  ratio, led to a thickness estimation  $c = (1 \pm 0.18) \times a$ .



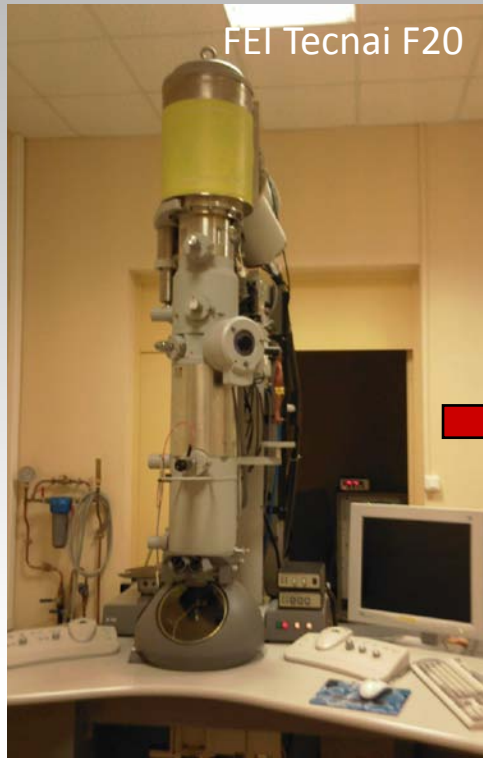
- Sensitive to the magnetic phase shift:

Decrease the size from 30 nm to 25 nm corresponds to a magnetic volume decay of more than 40%

**=> Need to increase the phase sensitivity ...**



Tecnai F-20



Spatial resolution  $\approx 5$  nm  
in Lorentz mode

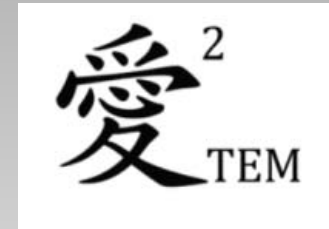
Schottky-FEG

Hitachi HF3300



Double stage: Normal Stage and Lorentz Stage

- Spatial resolution  $\approx 0.5$  nm in Lorentz mode
- Sample in free field space  $\Rightarrow$  1-2 Oe (I2TEM) vs 150 Oe (Tecnai)

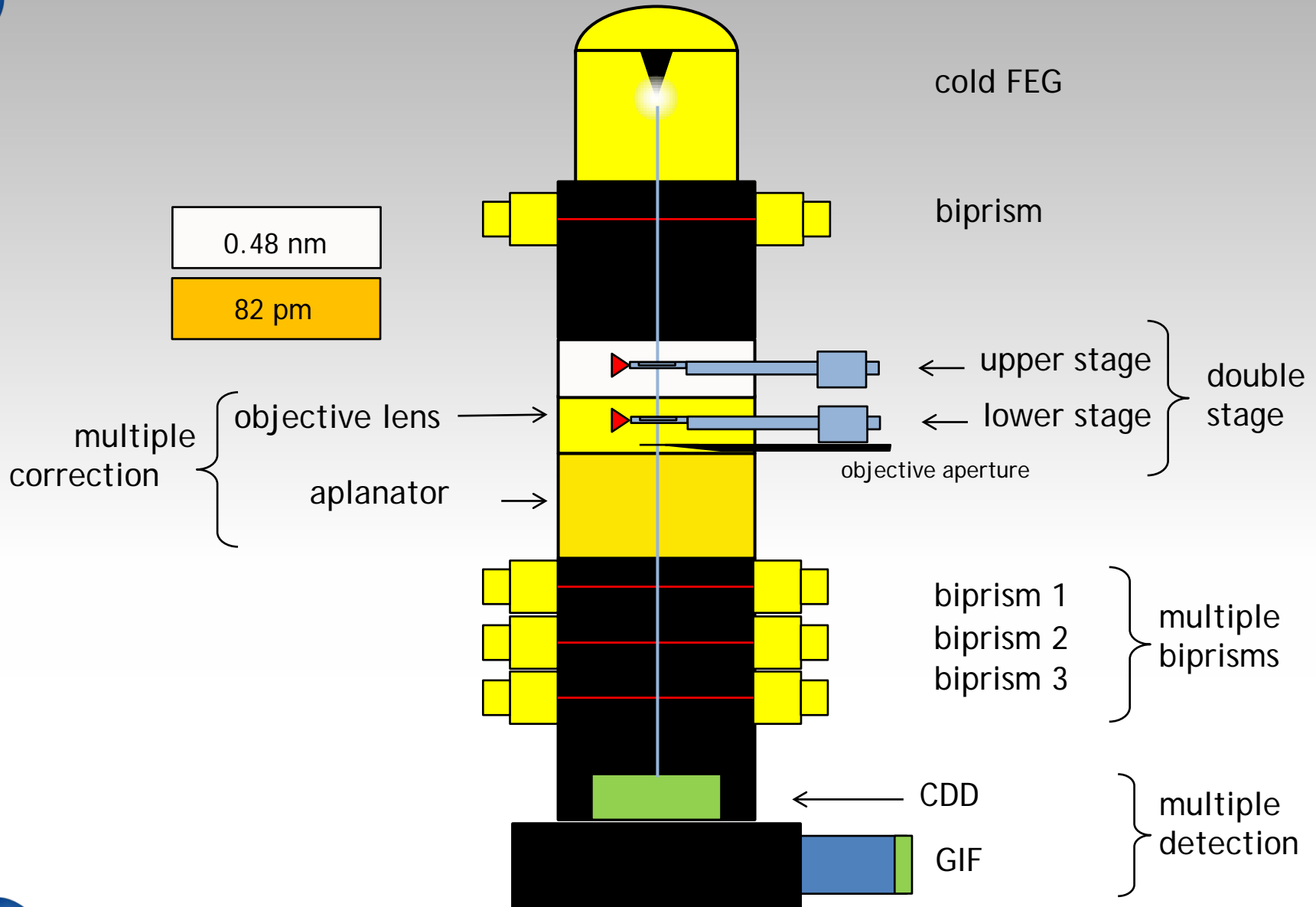


Cold FEG  $\Rightarrow$  Signal/Noise  $\nearrow$

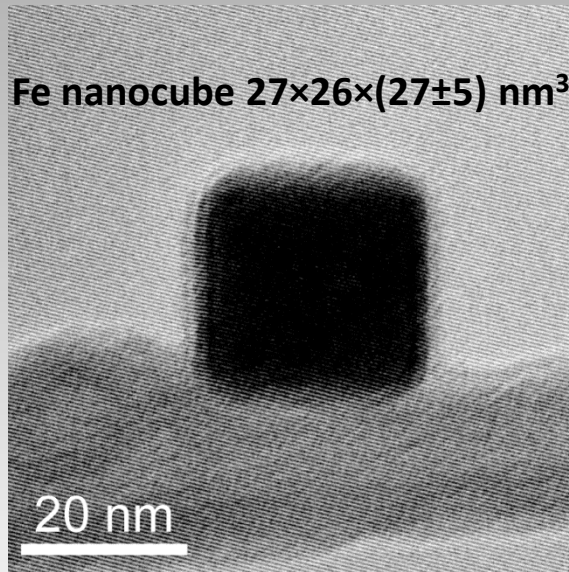
Multiple biprisms:  
 $\Rightarrow$  No Fresnel fringes

New corrector (B-COR) with  
dedicated lorentz mode

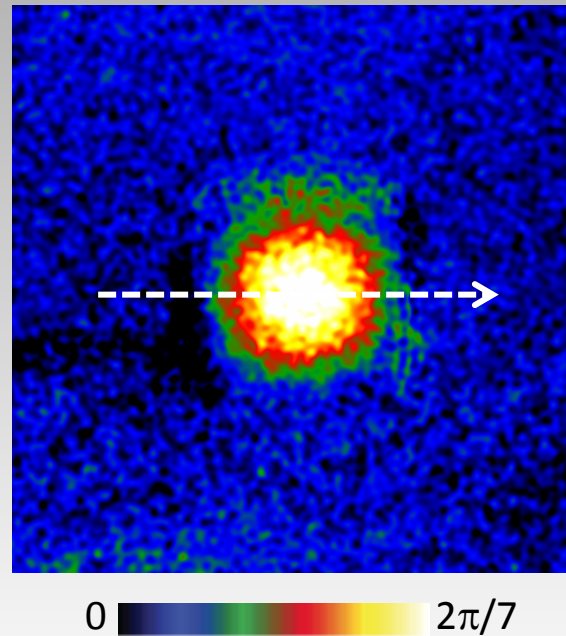
# I2TEM: TEM dedicated to holography and "in-situ" TEM



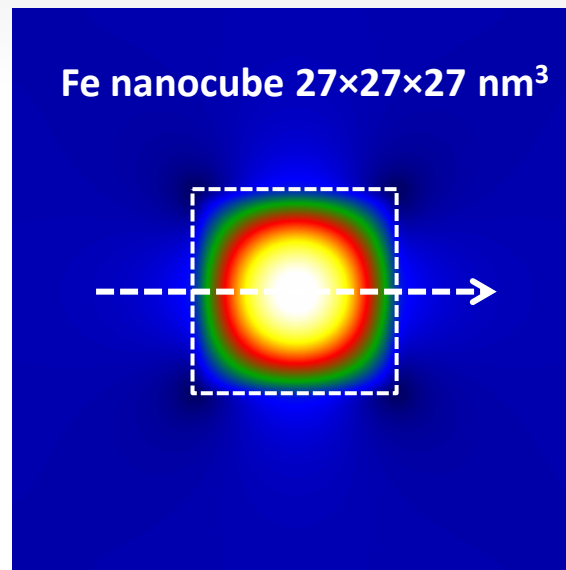
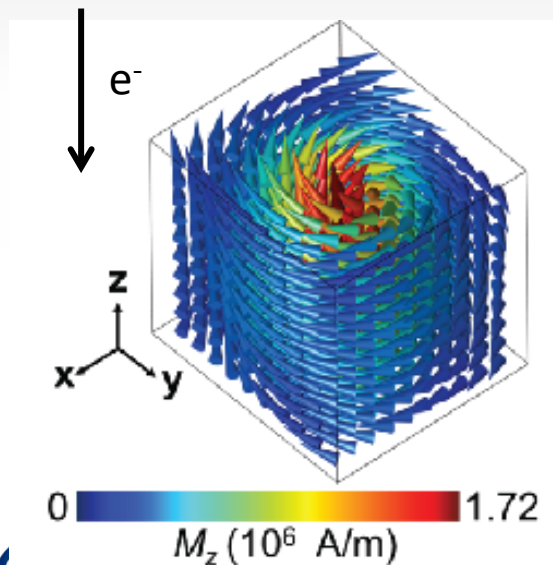
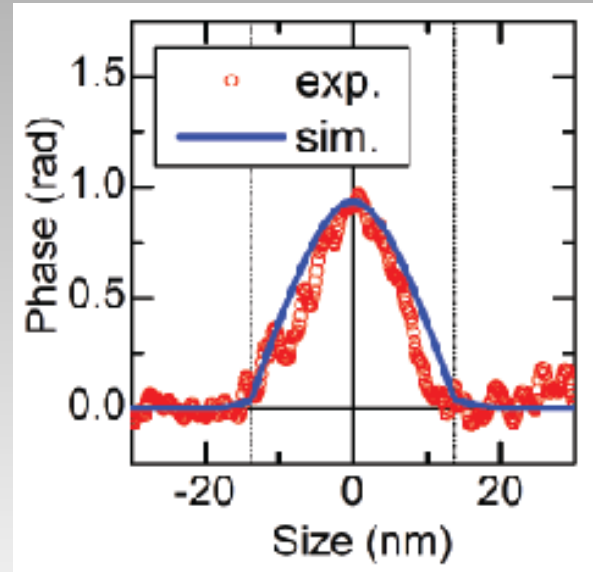
Hologram



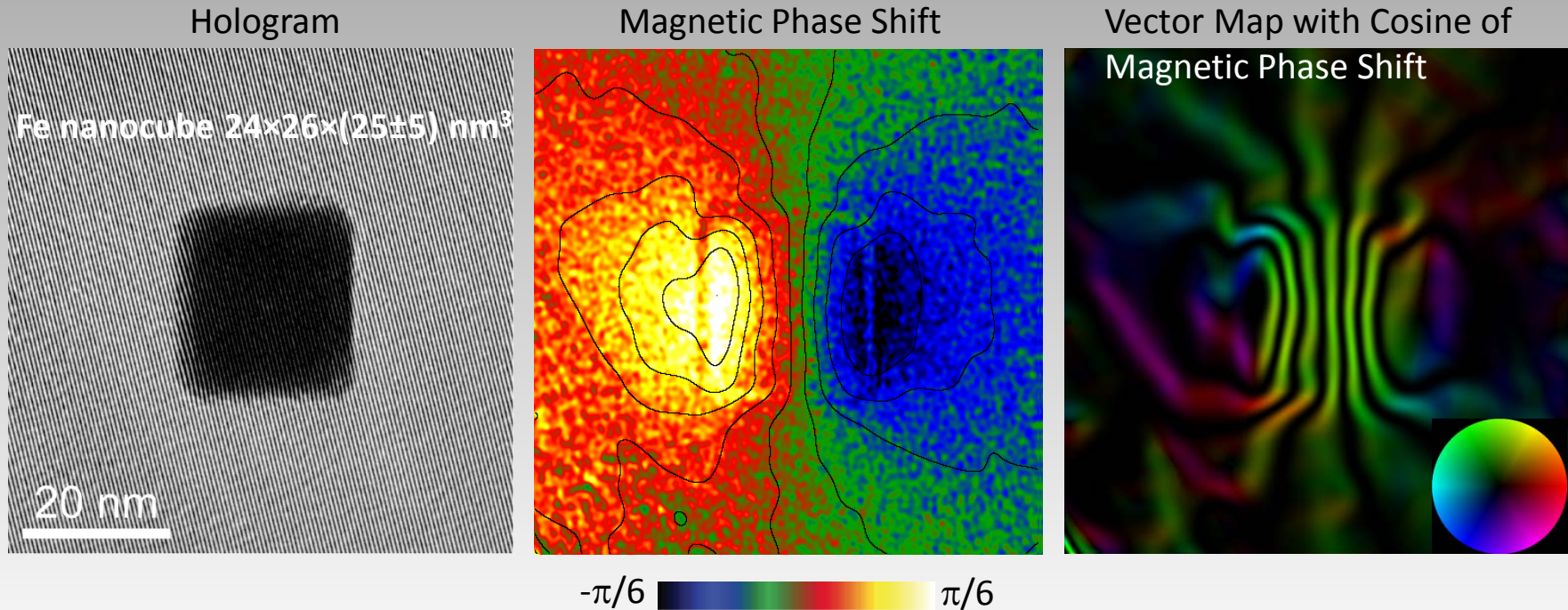
Magnetic Phase Shift



Vector Map with Cosine of



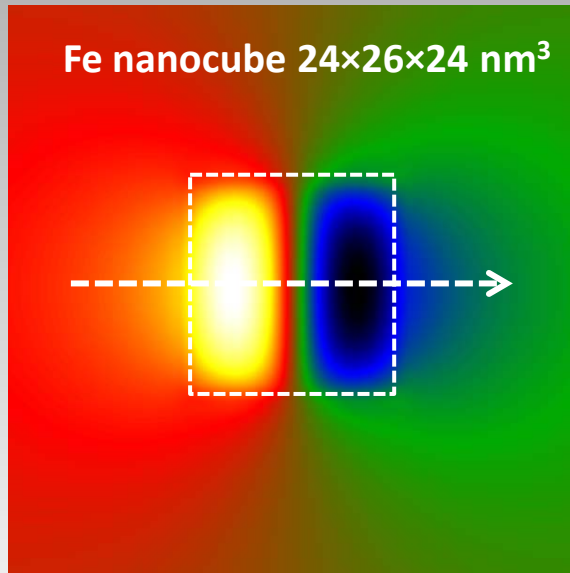
- Axial symmetry of the induction: axis  $\perp$  to the (001) face
- Complete flux closure in the vortex plane
- Perfect quantitative agreement with simulated phase shift calculated from 3D micromagnetic simulation integration along the electron path



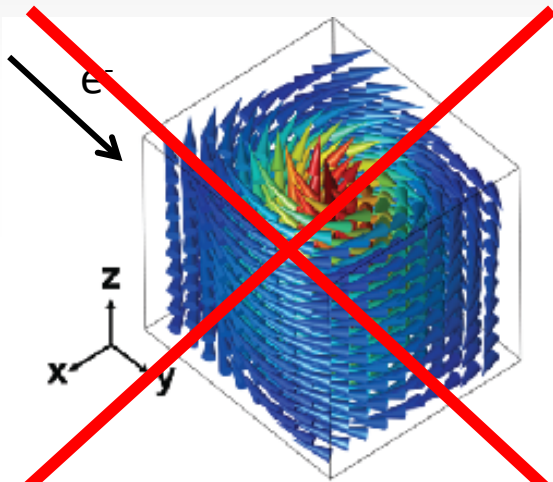
- Magnetic induction lines fairly aligned within the cube.
- They tend to curl outside in order to close the induction flux.
- Magnetic configuration: Single Domain or Vortex with core // in-plane  $\langle 001 \rangle$  directions  
**=> Micromagnetic simulations are then mandatory to unambiguously distinguish between both configurations.**

# Spin configurations in size controlled single Fe nanomagnets

Simulated Vortex

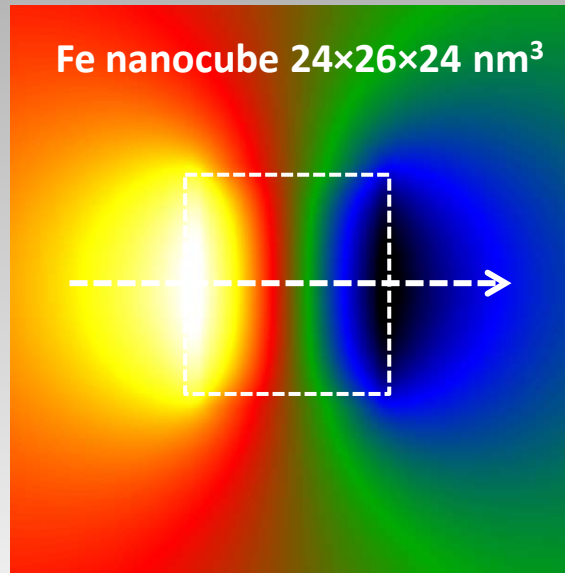


$-\pi/25$   $\pi/25$

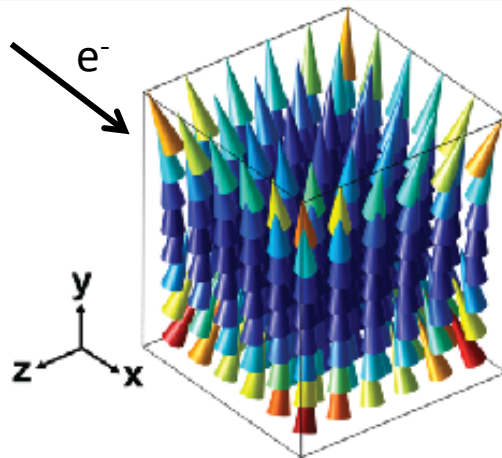


$0$   $1.72$   
 $M_z$  ( $10^6 \text{ A/m}$ )

Simulated Single Domain

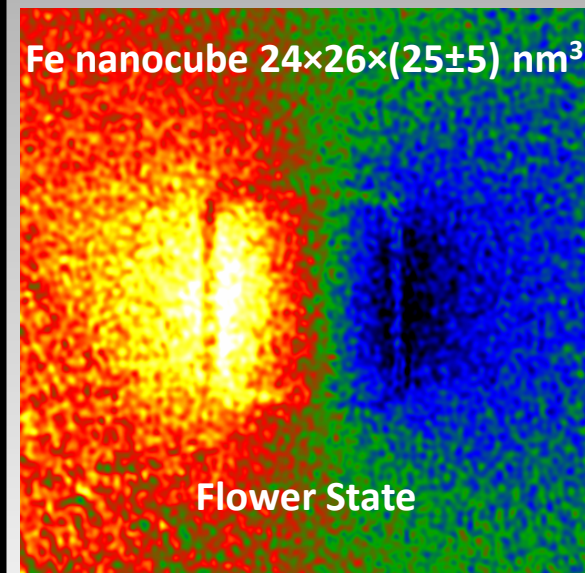


$-\pi/6$   $\pi/6$

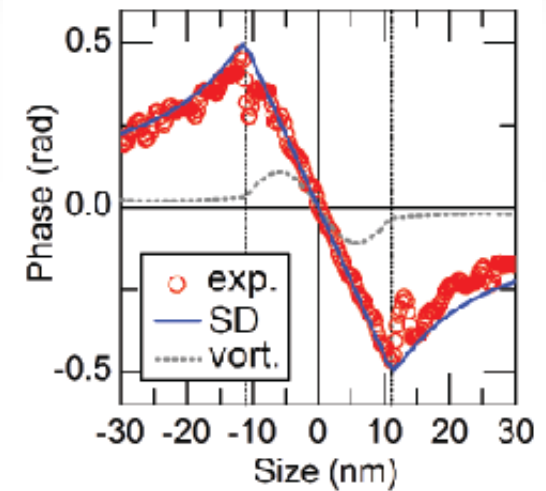


$1.5$   $1.72$   
 $M_y$  ( $10^6 \text{ A/m}$ )

Experimental Phase Shift

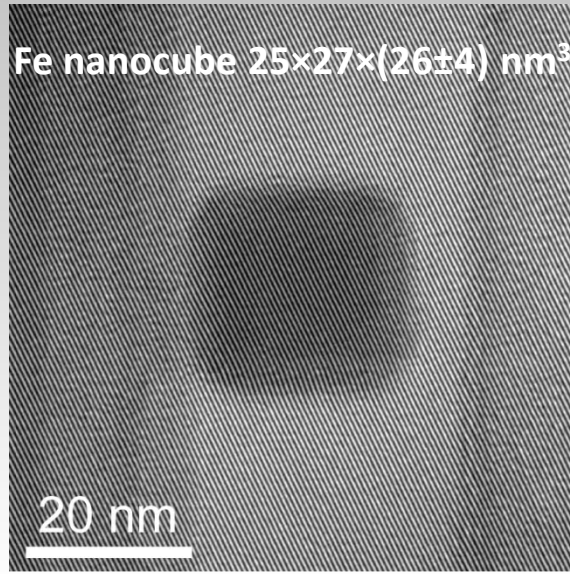


$-\pi/6$   $\pi/6$

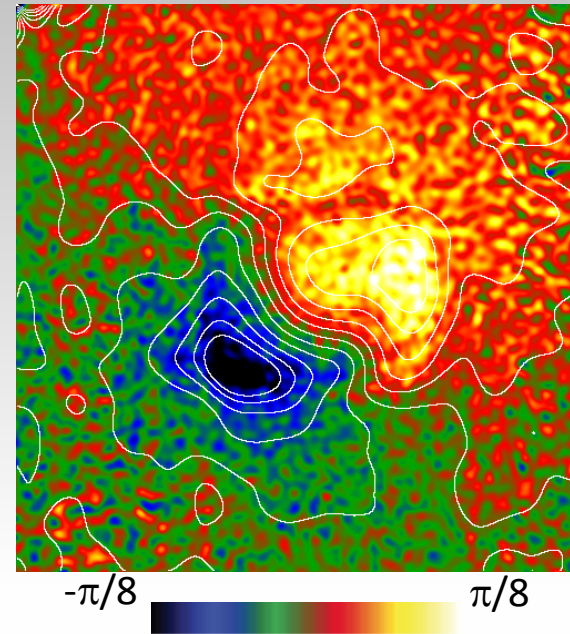


## A surprisingly magnetic state...

Hologram

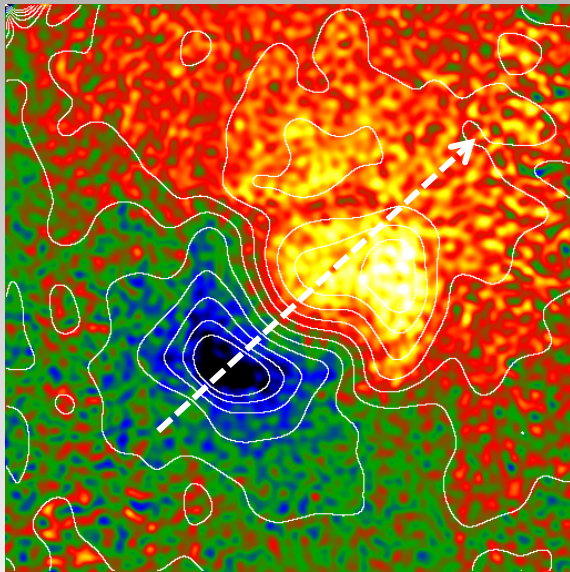


Experimental Phase Shift



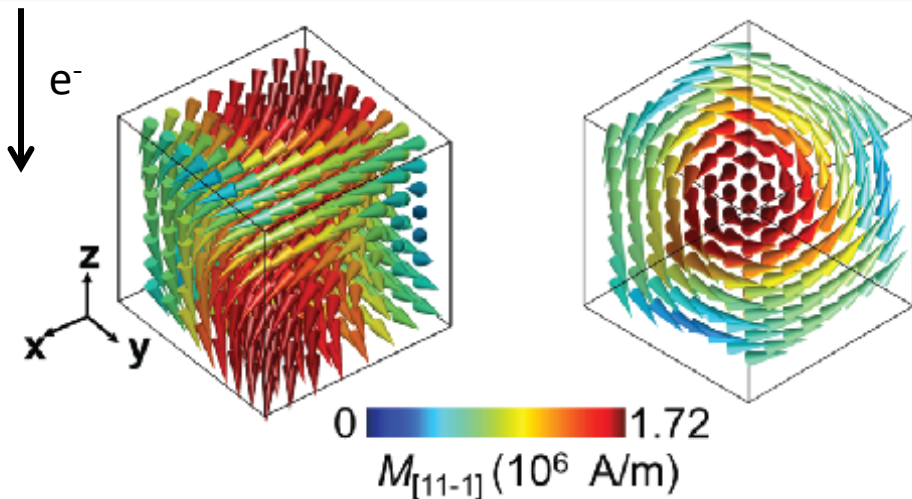
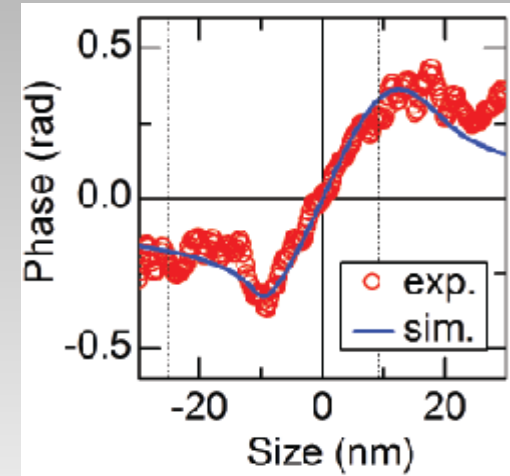
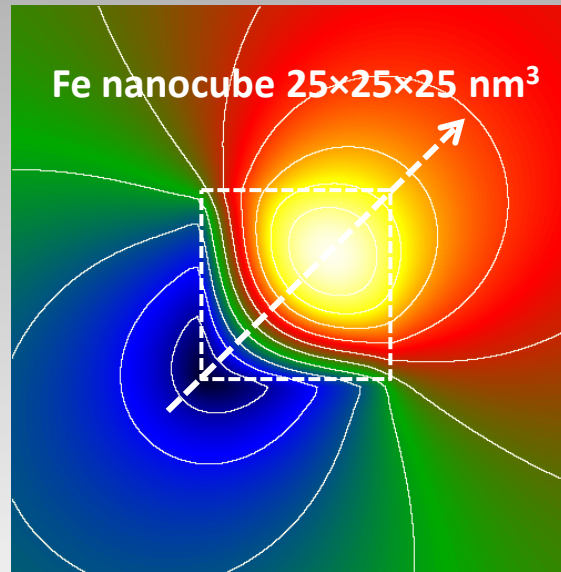
- Some cubes give an unexpected magnetic configuration for intermediate size
- Complex pattern which cannot be directly interpreted:
  - Low phase shift of the integrated induction
  - C state ?

Experimental Phase Shift



$-\pi/8$    $\pi/8$

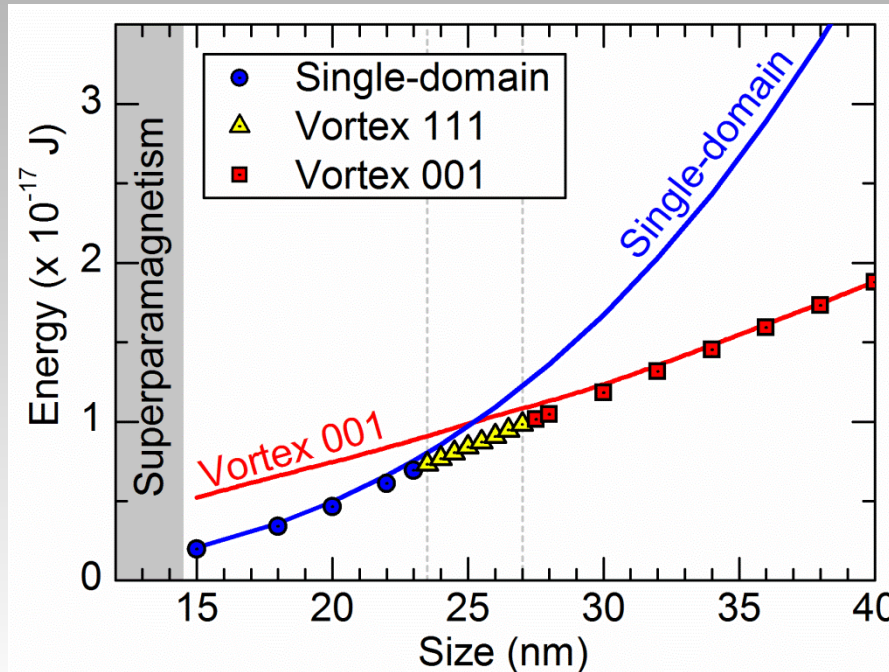
Simulated Phase Shift



- Very good quantitative agreement between experimental and simulated magnetic phase shift
- Projection along the cube diagonal reveals that spins curl around  $\langle 111 \rangle$  direction
- Vortex whose core axis is aligned along the diagonal of the cubes

**=> Vortex  $\langle 111 \rangle$**

### Magnetic phase diagram of a perfect Fe nanocube

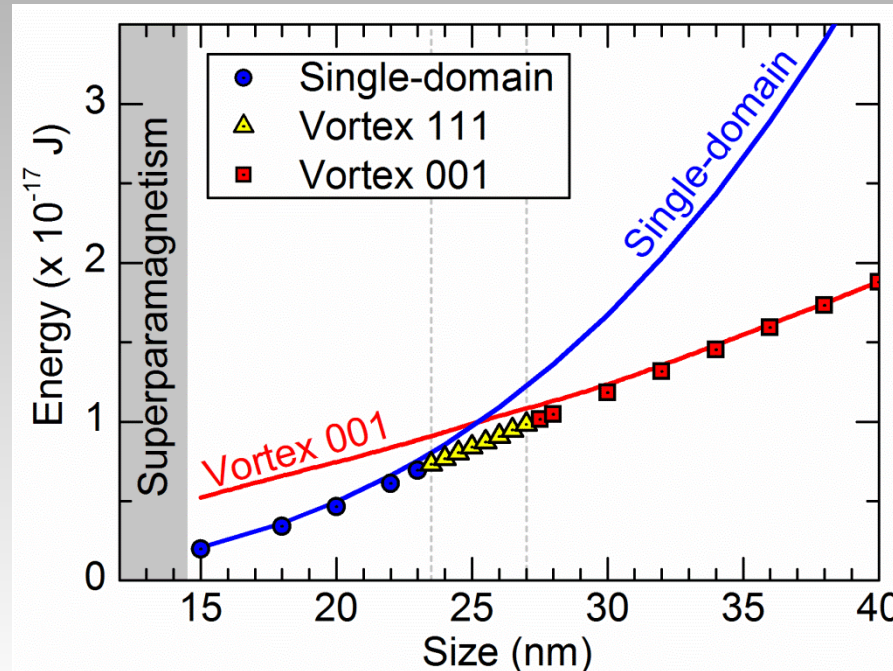


**1<sup>st</sup> approach:** Fixe Initial spin configuration (uniform SD or V<001>) imposed: resulting energy vs size.

	Exchange energy	Magnetostatic energy
Single Domain	↘	↗
Vortex <001>	↗	↘



## Magnetic phase diagram of a perfect Fe nanocube



### 2<sup>nd</sup> approach:

Random spin configuration originally introduced: Relaxation of the spins will lead to the stable configuration and the corresponding energy

→ Stable SD configurations below 23.5 nm

→ V<001> obtained within cubes above 27 nm (same energies with <001>core axis)

- Between 24 and 27 nm, **<111> vortex is the most stable configuration.**

=> Balancing exchange and magnetostatic interactions, at the expense of the magneto-crystalline energy (quite low in Fe).

## Summary

- Clear description of equilibrium states of a nanomagnet of cubic anisotropy.
- Deeper understanding of the single domain limit, more complex than expected with the appearance of an unreported  $\langle 111 \rangle$  vortex state.
- Optimization of nanomagnets in the perspective of various applications: hyperthermia, data storage,...

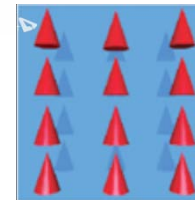
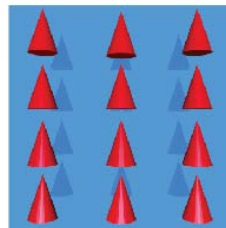
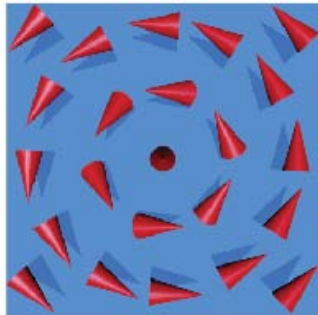
→ **Future:** Next transition SP/SD ? What is the limit ? Other type of materials morphologies?

If the nanocube size decreases:

300K : Vortex => Single Domain => Superparamagnetism

25 nm

15nm



## Size-Specific Spin Configurations in Single Iron Nanomagnet: From Flower to Exotic Vortices

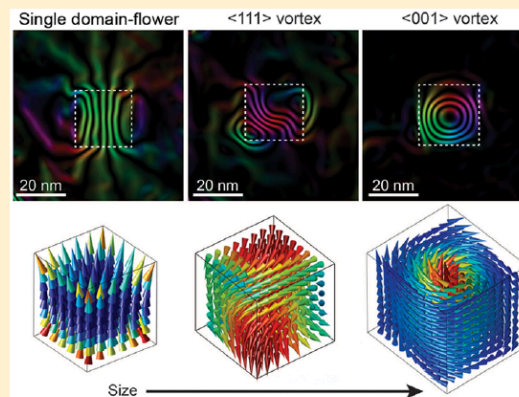
Christophe Gatel,<sup>\*,†</sup> Francisco Javier Bonilla,<sup>‡</sup> Anca Meffre,<sup>‡</sup> Etienne Snoeck,<sup>†</sup> Bénédicte Warot-Fonrose,<sup>†</sup> Bruno Chaudret,<sup>‡</sup> Lise-Marie Lacroix,<sup>‡</sup> and Thomas Blon<sup>\*,‡</sup>

<sup>†</sup>Centre d'Elaboration de Matériaux et d'Etudes Structurales, CEMES-CNRS, 29 rue Jeanne Marvig, B.P. 94347, 31055 Toulouse, France

<sup>‡</sup>Laboratoire de Physique et Chimie des Nano-Objets, LPCNO, UMR5215 INSA-UPS-CNRS, Université de Toulouse; Institut National des Sciences Appliquées, 135 avenue de Rangueil, 31077 Toulouse, France

### Supporting Information

**ABSTRACT:** The different spin configurations in the vicinity of the single-domain/vortex transition are reported in isolated magnetic nanoparticles. By combining chemical synthesis, electron holography in a dedicated transmission electron microscope and micromagnetic simulations, we establish the “magnetic configurations vs size” phase diagram of Fe single-crystalline nanocubes. Room temperature high resolution magnetic maps reveal the transition between single-domain and vortex states for Fe nanocubes from 25 to 27 nm, respectively. An intermediate spin configuration consisting of an  $\langle 111 \rangle$  vortex is for the first time evidenced.



**KEYWORDS:** magnetic configuration, electron holography, vortex state, single domain state, flower state, nanocube

# *In situ* electron holography of the dynamic field emanating from a HDD writer

Etienne SNOECK, C. GATEL,  
A. Masseboeuf, R. Cours, F. Houdellier



*CEMES - CNRS*  
29 rue J. Marvig,  
31055 Toulouse (France)



J. Einsle, R. Bowman  
*Centre for Nanostructured Media*  
*School of Maths and Physics,*  
*Queens University Belfast (UK)*

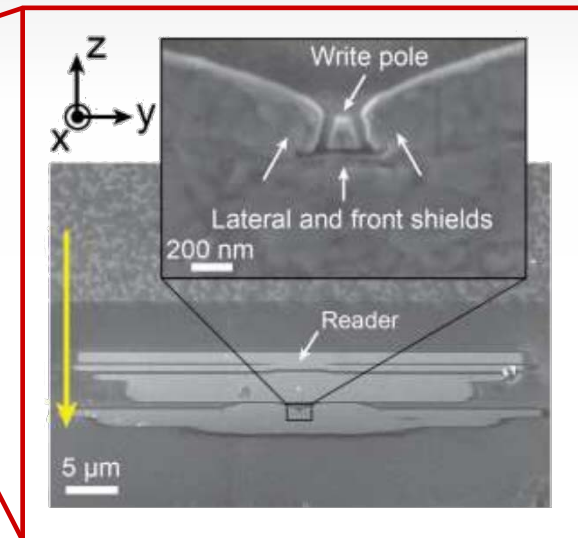
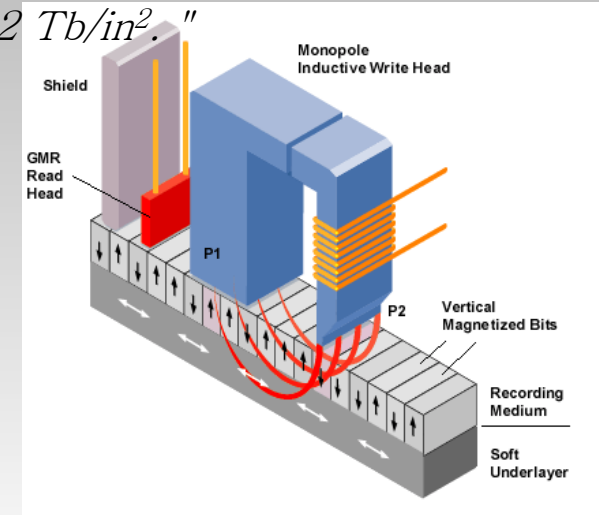
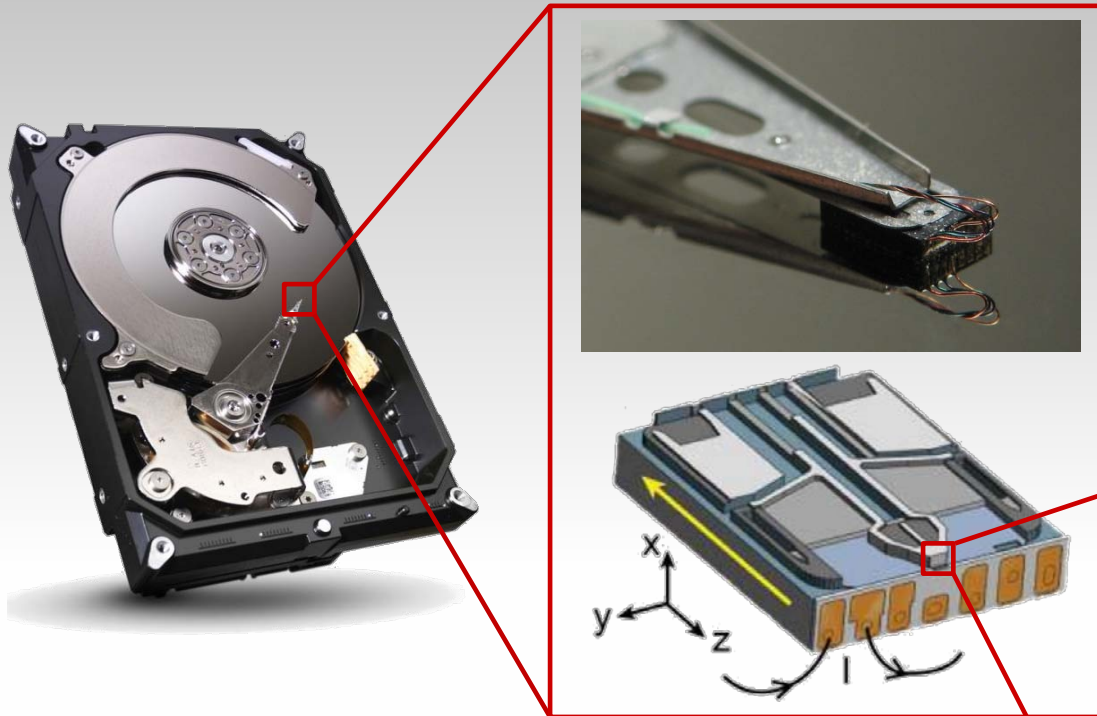


M. Bashir, M. Gubbins  
*Seagate Tehnology (Ireland)*  
*Londonderry (UK)*

# In situ electron holography of the dynamic field emanating from a HDD writer



"Forecasts are that areal densities will need to increase by as much as 35% compound per annum and by 2020 cloud storage capacity will be around 7 zettabytes ( $7 \cdot 10^{21}$ ) corresponding to areal densities of 2 Tb/in<sup>2</sup>."



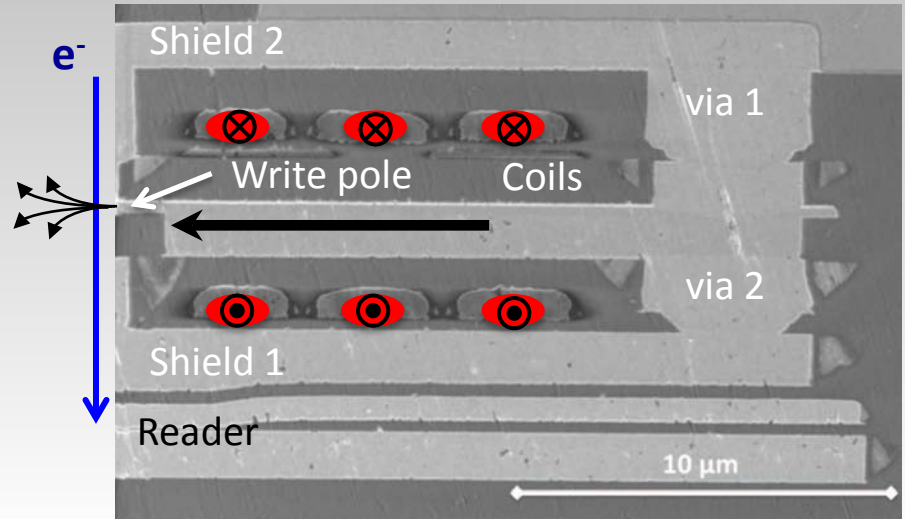
"A hard drive head can be seen as a spaceship

- flying at a speed of Mach 2,
- 10 cm above the ground,
- counting grass by 10-stalks packages
- over a field as big as Ireland."

John Chapman

# In situ electron holography of the dynamic field emanating from a HDD writer

"Forecasts are that areal densities will need to increase by as much as 35% compound per annum and by 2020 cloud storage capacity will be around 7 zettabytes ( $7 \cdot 10^{21}$ ) corresponding to areal densities of 2 Tb/in<sup>2</sup>. "

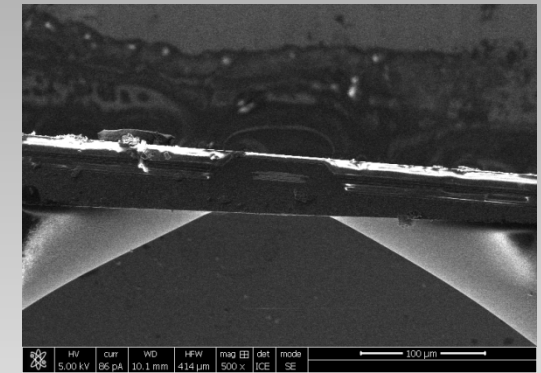
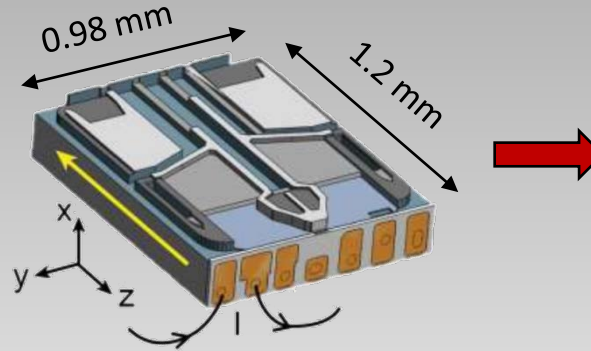


Electron beam phase shift measured in front of the write pole while applying a current through the device.

- Directional field
- No field for no current (no remnant state)
- Large saturation range

## Sample preparation: 18 months !

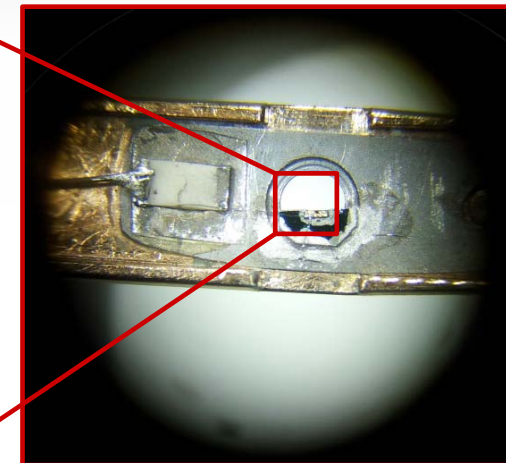
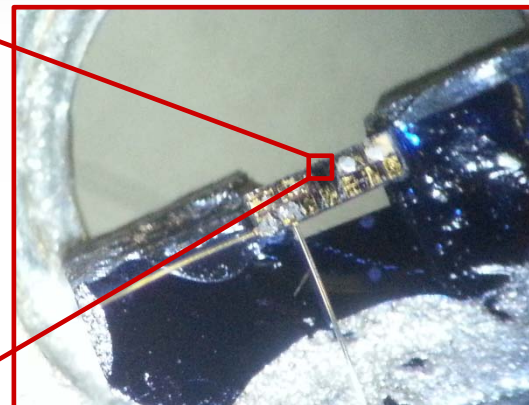
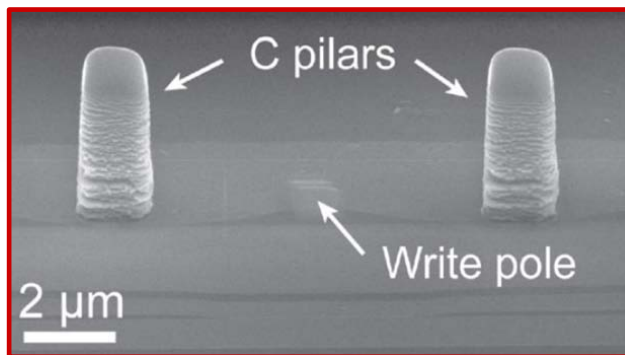
1. Mechanical polishing down to 30  $\mu\text{m}$  by tripod



2. Growth of two carbon pillars by Ion Beam Induced Deposition using FIB on both sides of the write pole

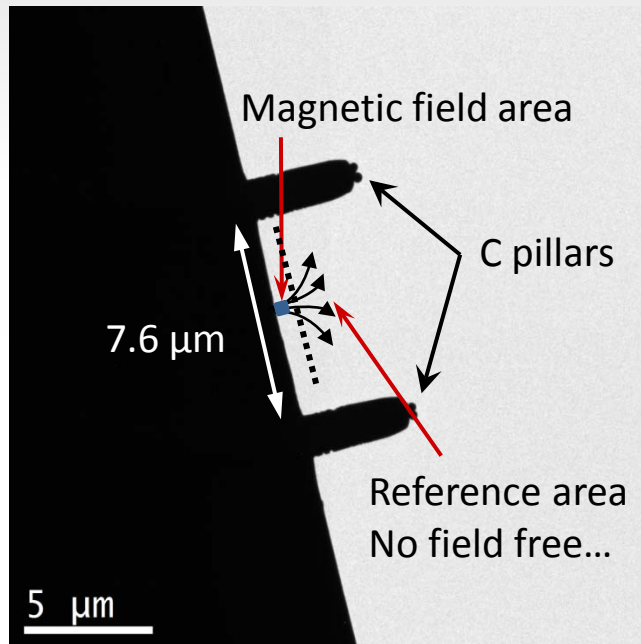
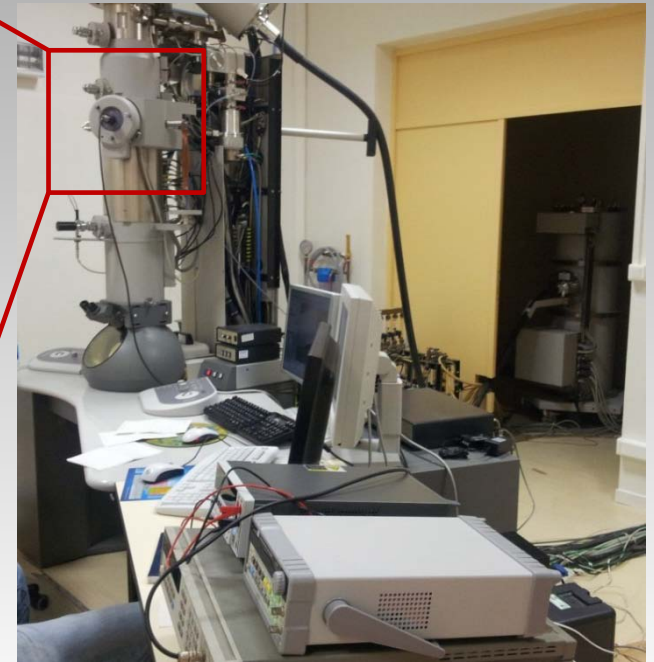
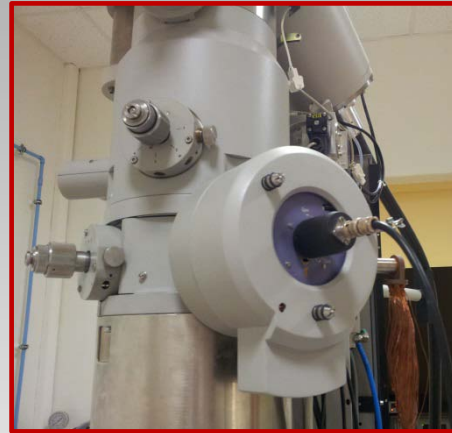
3. Mounting the device into a home-made sample holder for electrical connections

4. Wedge bonding to connect the pads of the slider toward the dedicated contacts of the sample holder



Microscope Set-up:

- Tecnai F20 – Cs corrected
- Lorentz mode
- Biprism voltage = 140 V
- Setting time: 7 hours
- Experiment time: 12 hours



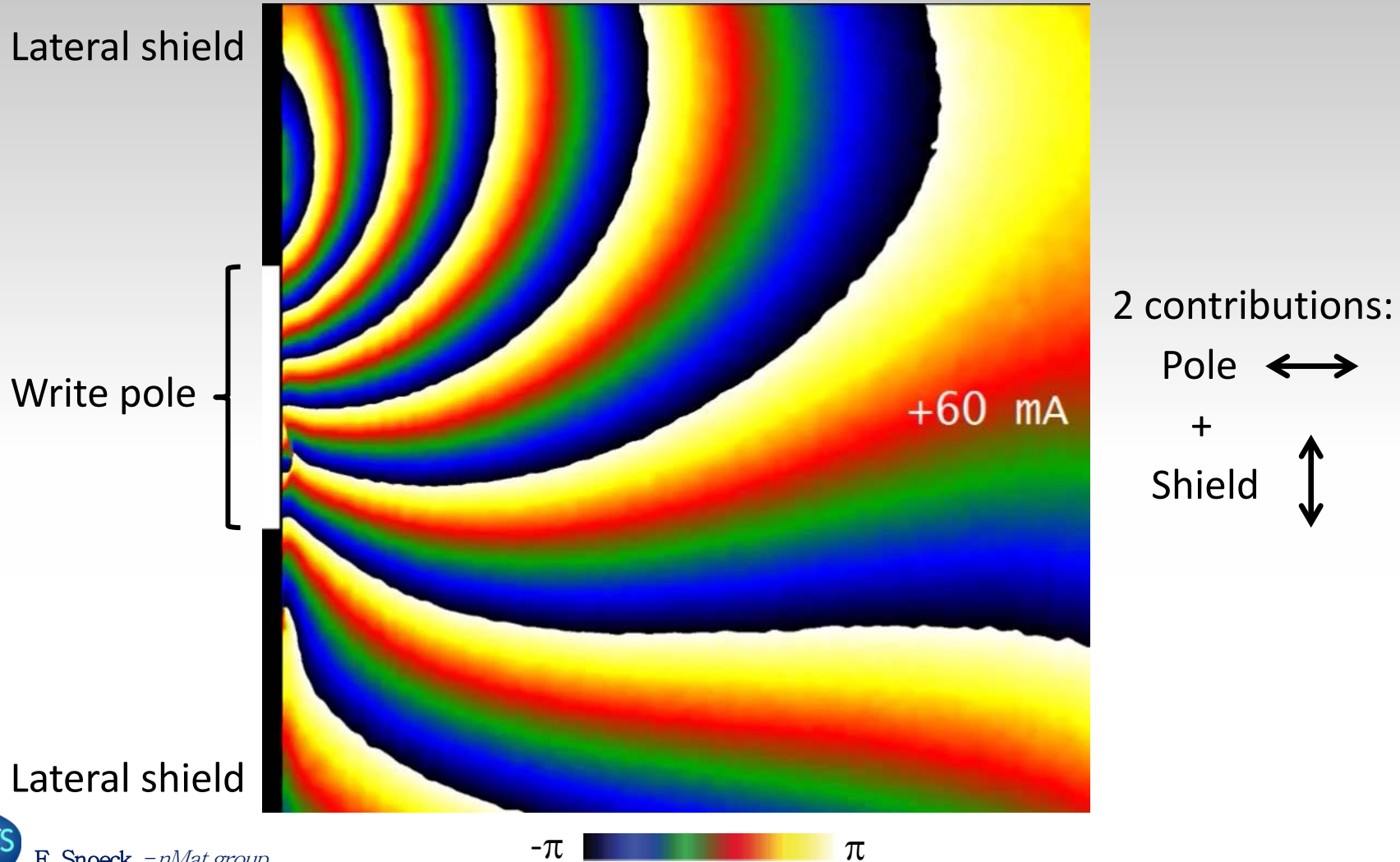
Slight magnetic field in the reference area  
**=> Need of simulations to take into account the phase variation**



Variable steps of current adjusted on the switching process. Static measurement.

2 symmetric datasets of 44 images each (+ 15 reference images at 20  $\mu\text{m}$  from the head):

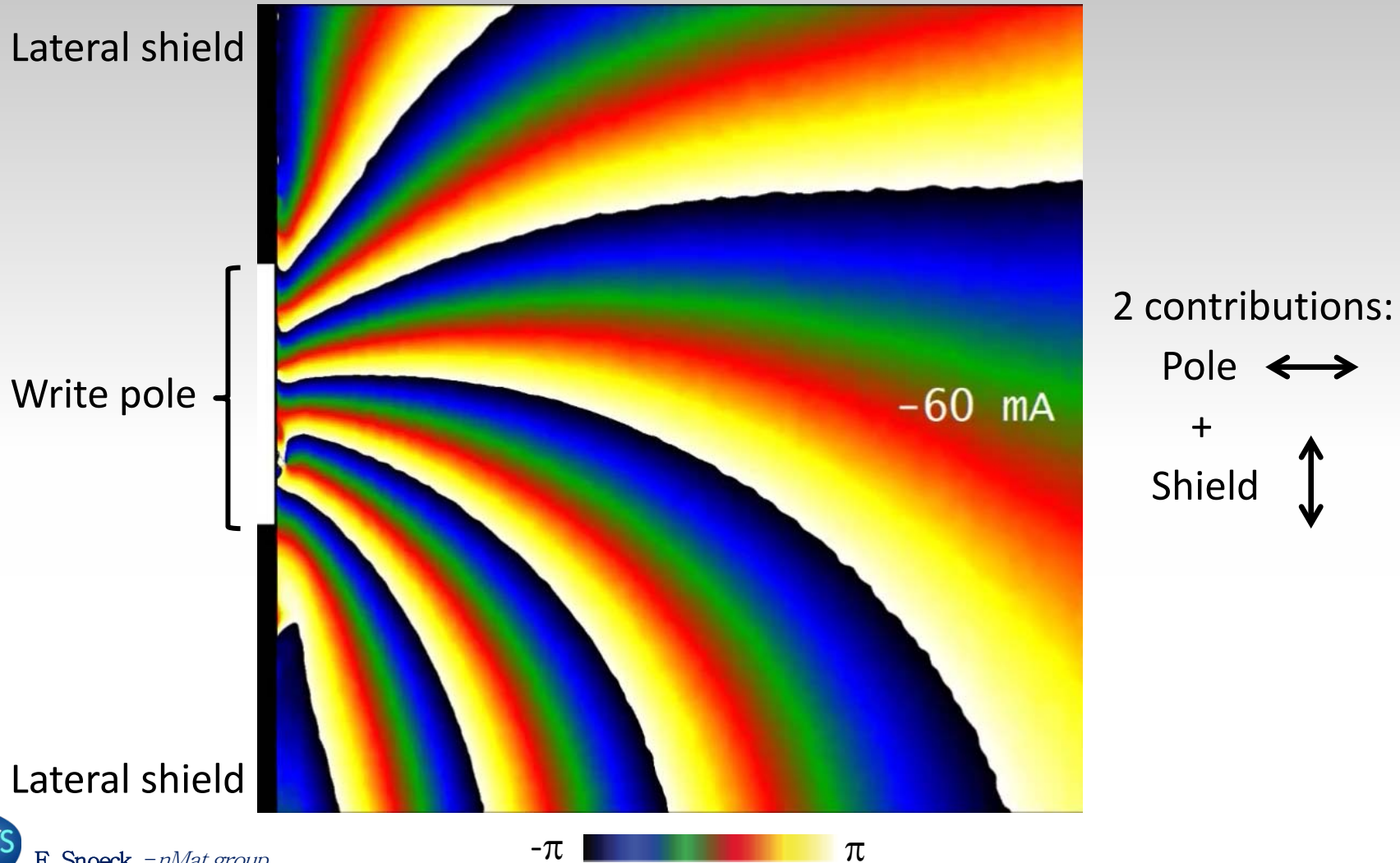
**+60 to -60 mA: Current decreasing**



Variable steps of current adjusted on the switching process. Static measurement.

2 symmetric datasets of 44 images each (+ 15 reference images at 20  $\mu\text{m}$  from the head):

**-60 to +60 mA: Current increasing**



From phase images to magnetic components

$$\phi_{Mag}(\mathbf{r}) = -\frac{e}{h} \iint B_{\perp}(\mathbf{r}_{\perp}, z) dr dz$$

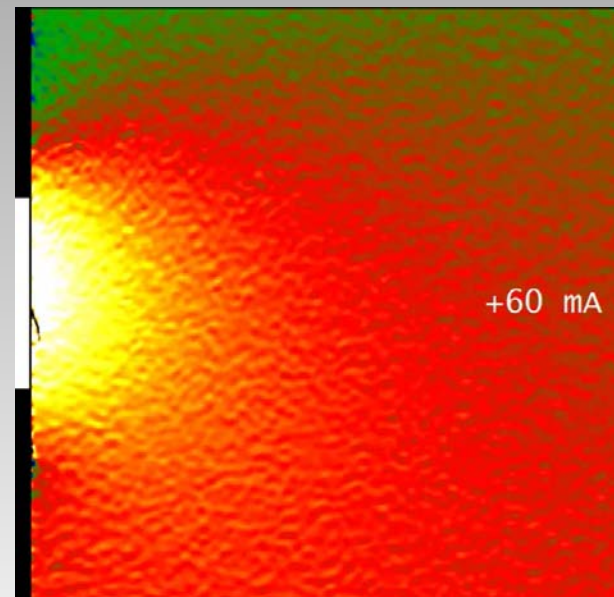
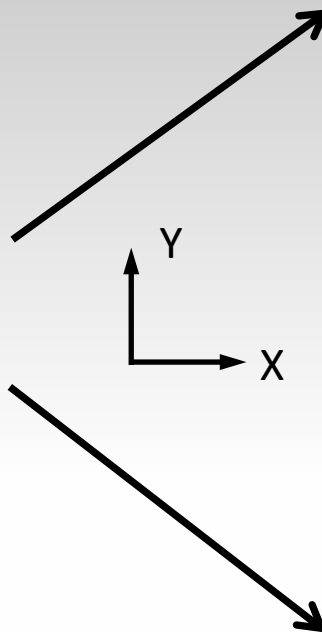
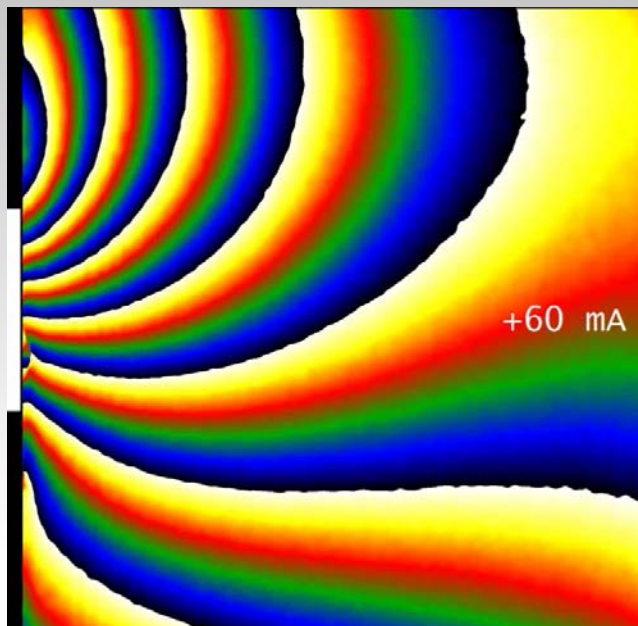
{	$\int_{-\infty}^{\infty} B_x(r_{\perp}, z) dz = -\frac{h}{e} \frac{\partial \phi_{Mag}(\mathbf{r})}{\partial y}$	X component
	$\int_{-\infty}^{\infty} B_y(r_{\perp}, z) dz = \frac{h}{e} \frac{\partial \phi_{Mag}(\mathbf{r})}{\partial x}$	Y component

→ Projected in-plane magnetic induction

→ Magnetic unit in T.m

→ Magnetic flux in Wb

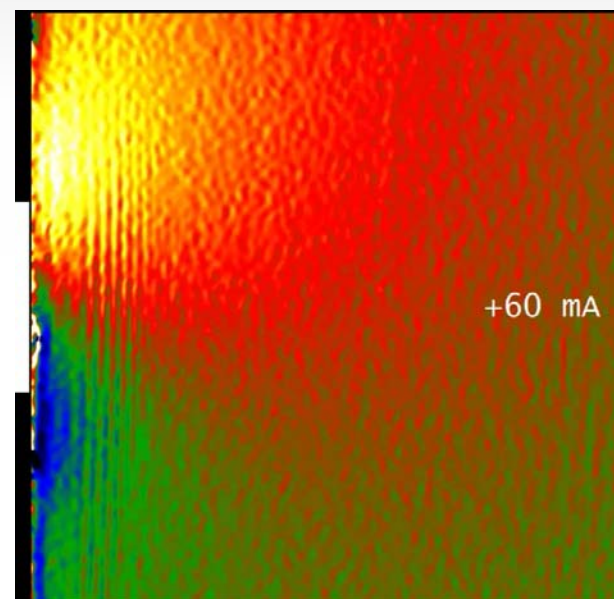
$$\text{X component: } \int_{-\infty}^{\infty} B_x(r_{\perp}, z) dz = -\frac{\hbar}{e} \frac{\partial \phi_{Mag}(\mathbf{r})}{\partial y}$$

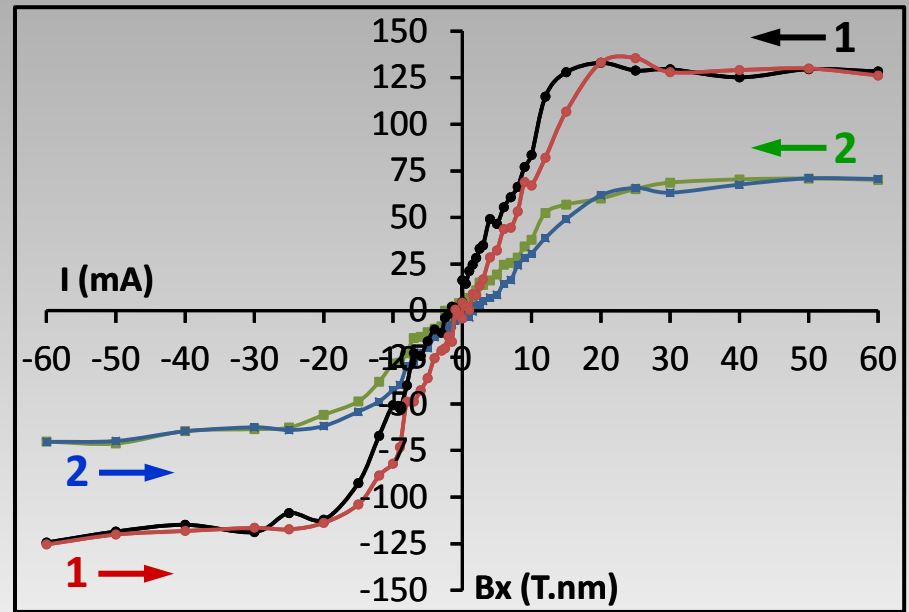
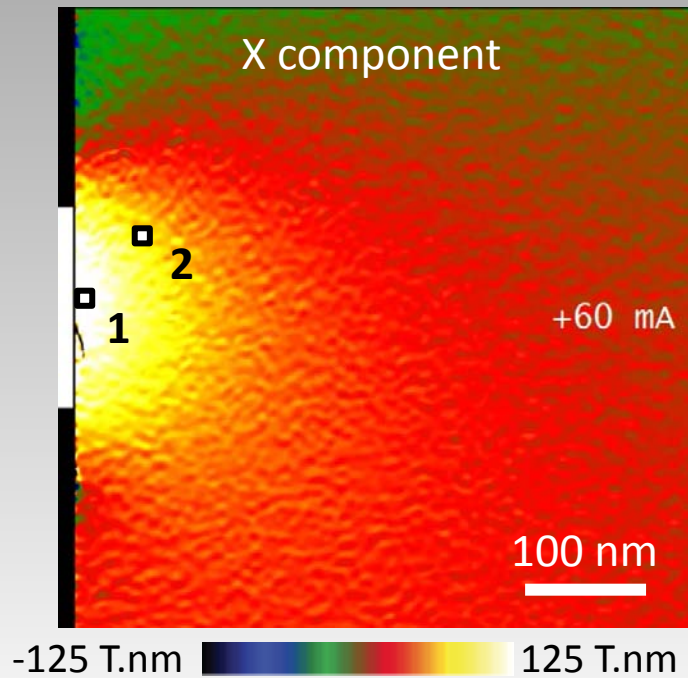


-125 T.nm  125 T.nm

$$\phi_{Mag}(\mathbf{r}) = -\frac{e}{\hbar} \iint B_{\perp}(\mathbf{r}_{\perp}, z) dr dz$$

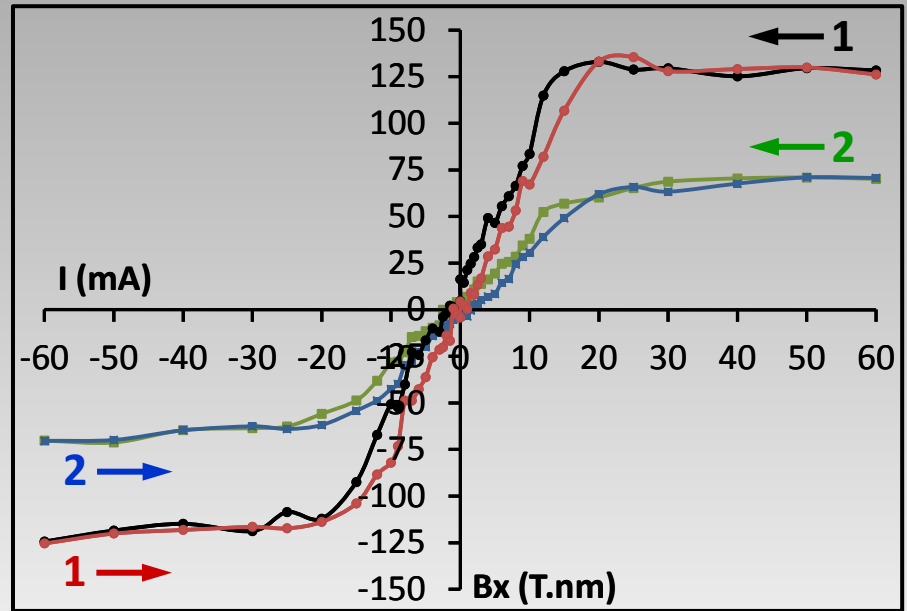
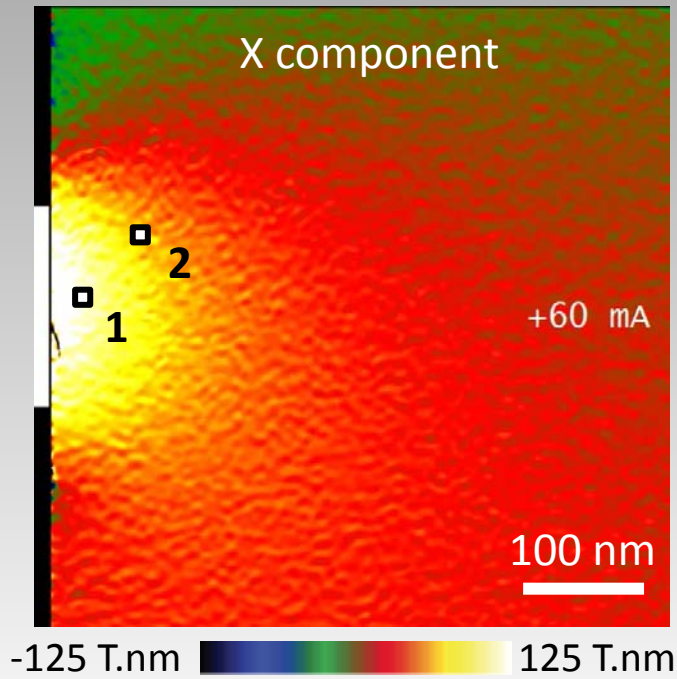
$$\text{Y component: } \int_{-\infty}^{\infty} B_y(r_{\perp}, z) dz = \frac{\hbar}{e} \frac{\partial \phi_{Mag}(\mathbf{r})}{\partial x}$$



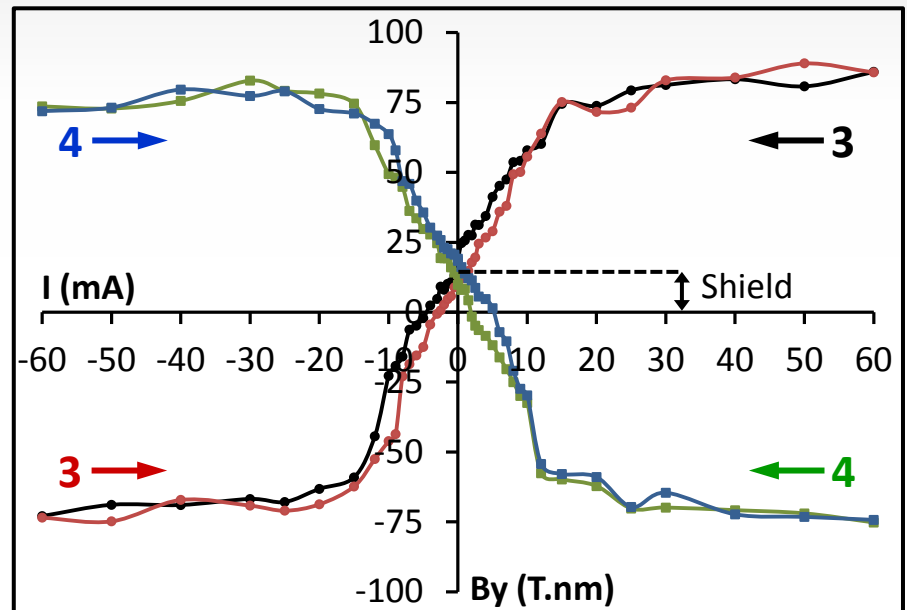
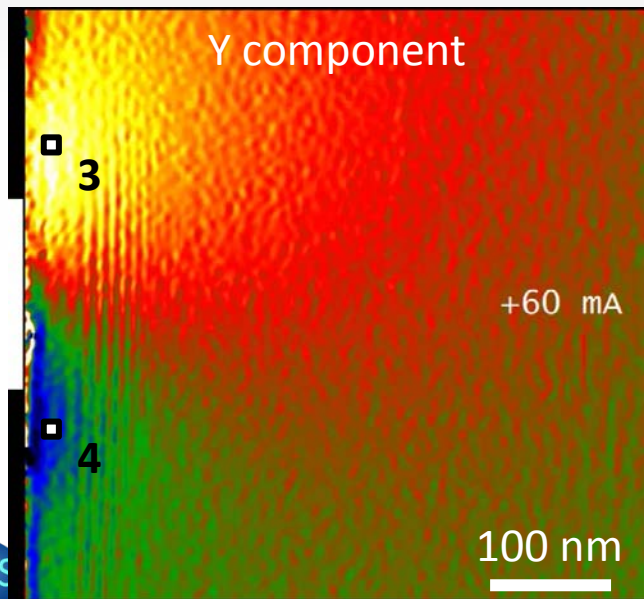


Cell used for the measurement:  $5 \times 5 \text{ nm}^2$

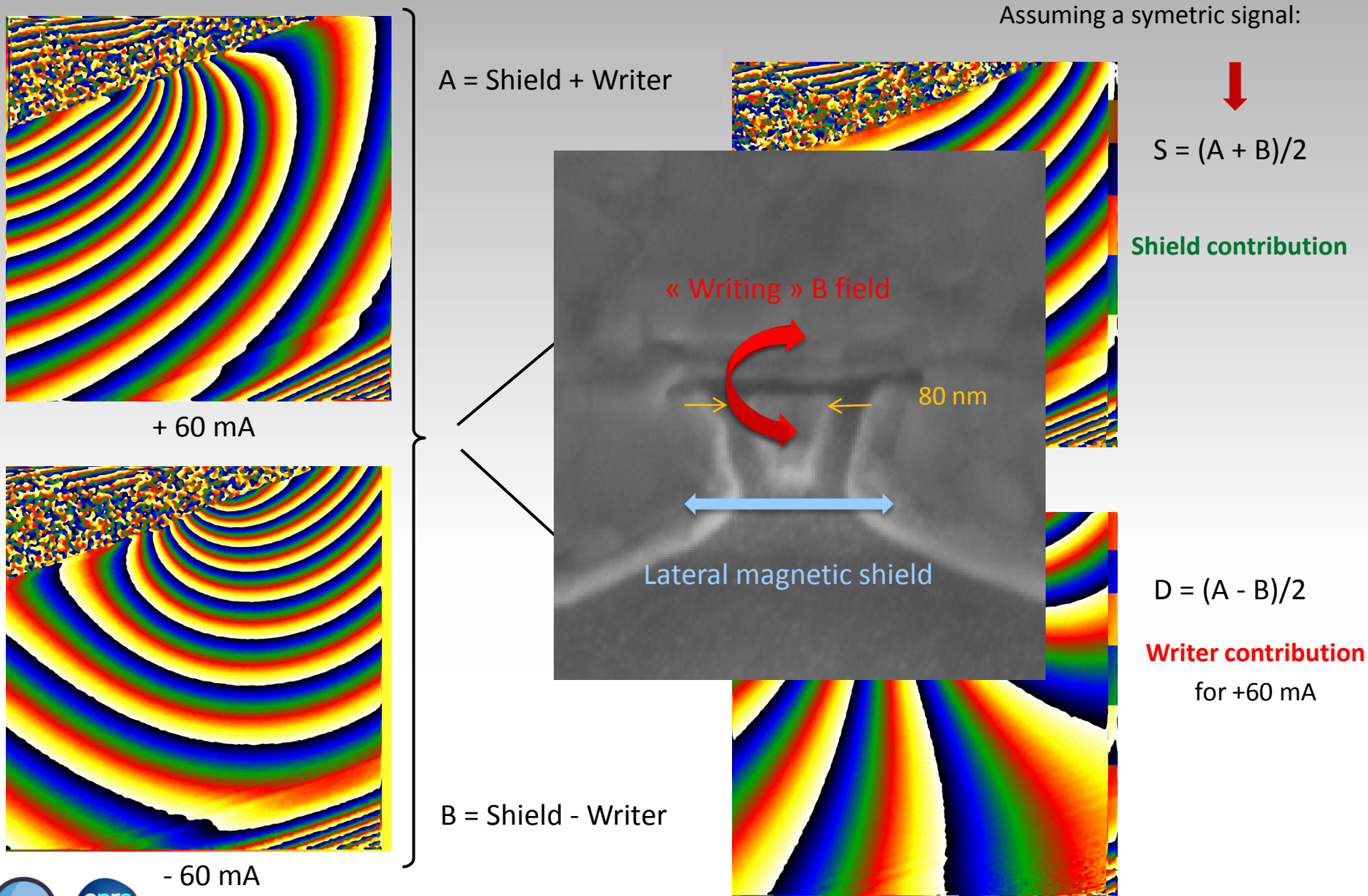
# In situ electron holography of the dynamic field emanating from a HDD writer



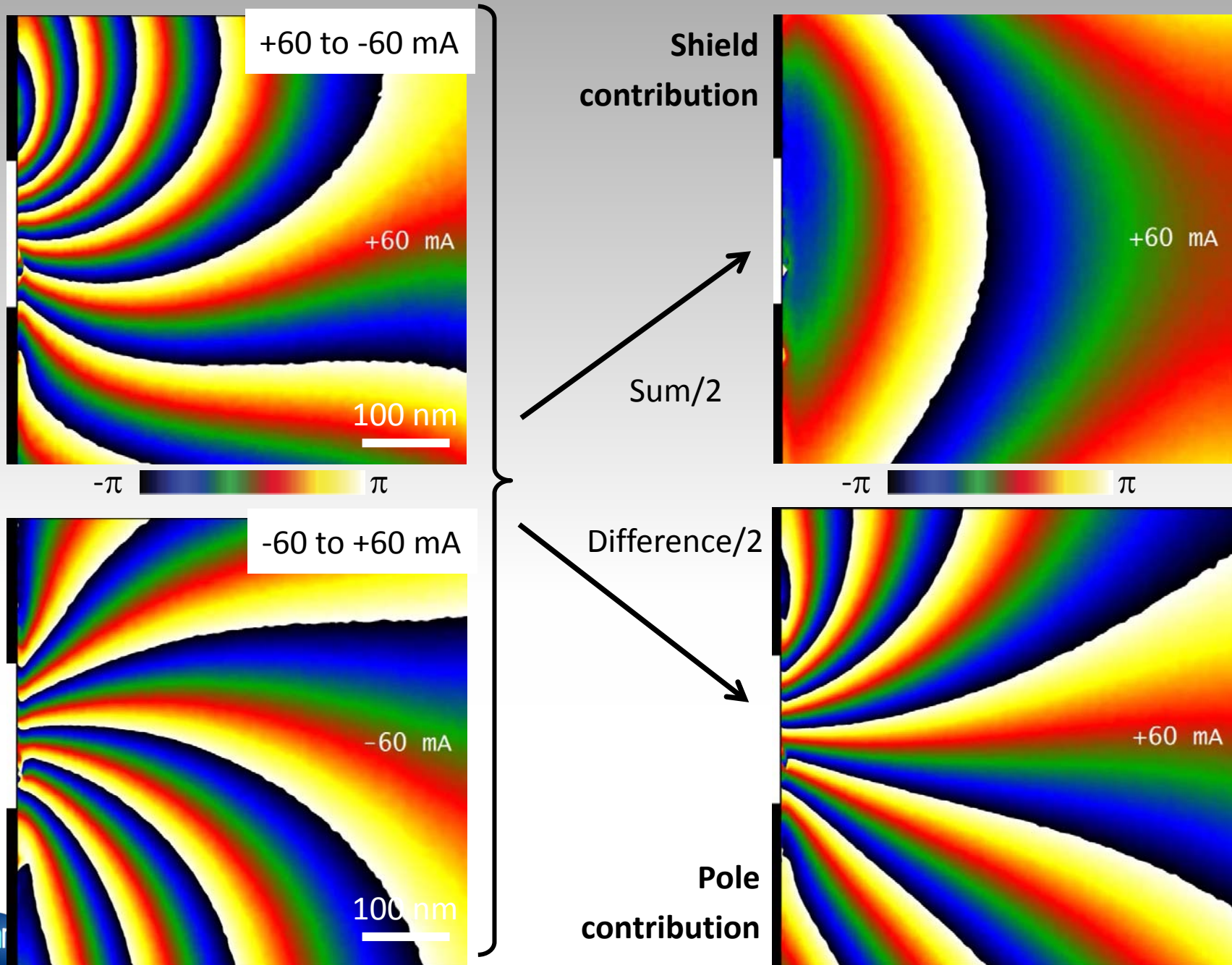
Cell used for the measurement:  $5 \times 5 \text{ nm}^2$



→ Separate the lateral shield contribution from the writer part using « + i » and « - i » phase images

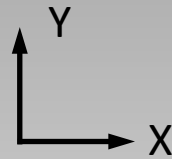
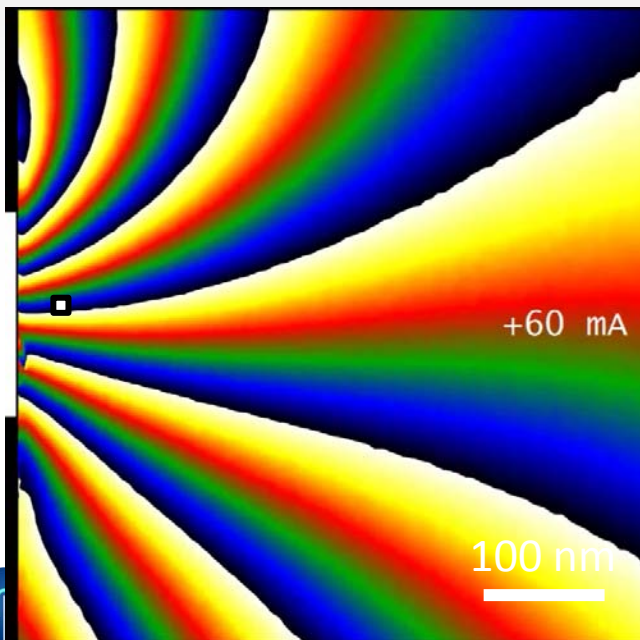
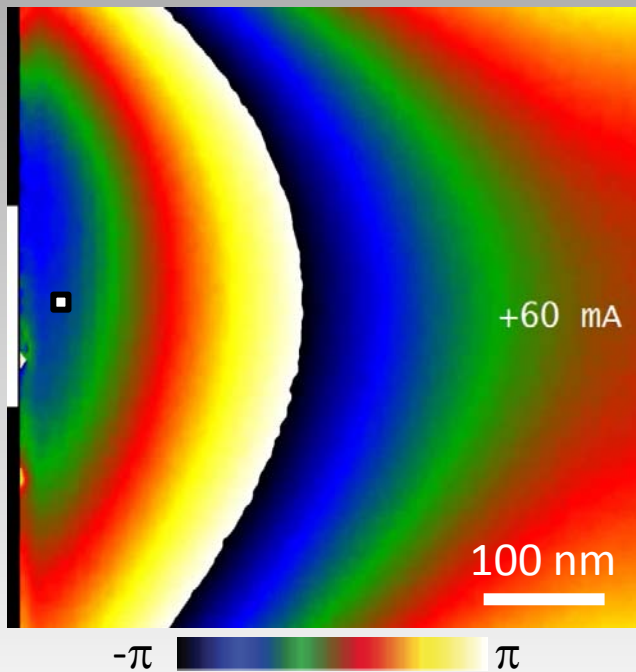


*In situ electron holography of the dynamic field emanating from a HDD writer*

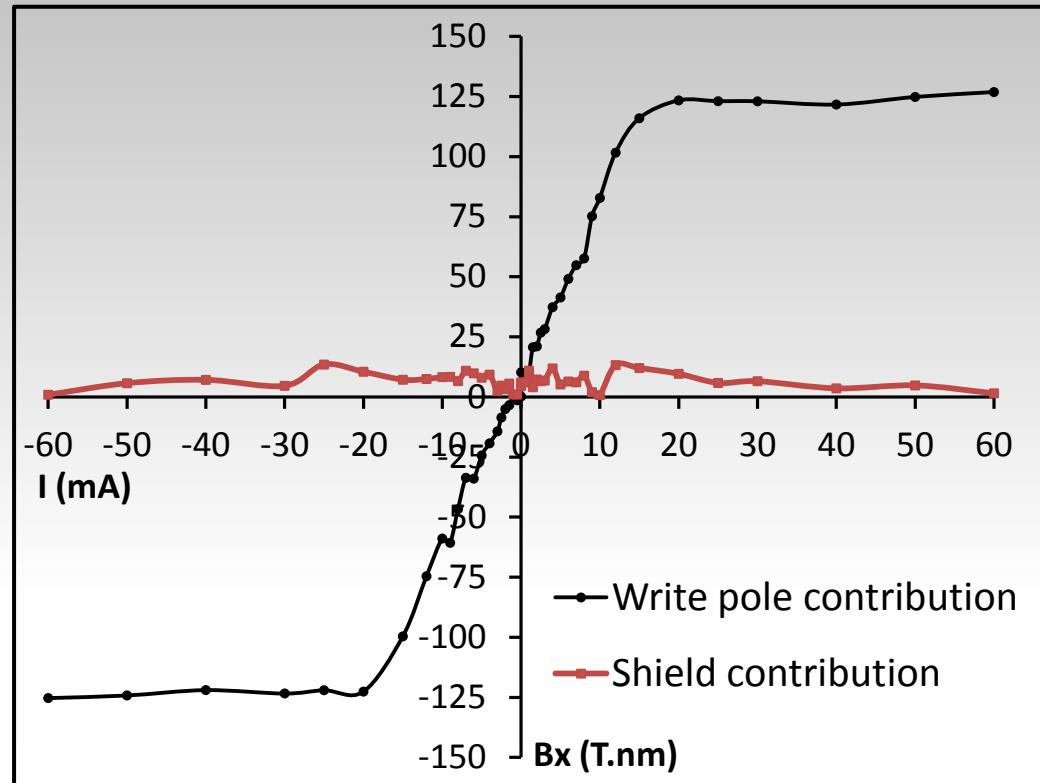




# In situ electron holography of the dynamic field emanating from a HDD writer



Hysteresis loop along the X direction  
(from the X component)

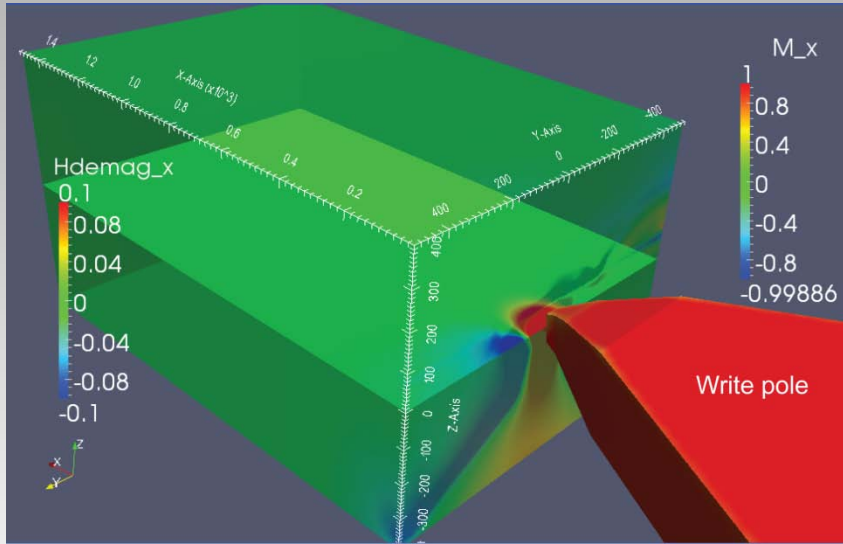


- Perfect symmetric signal for the pole contribution:  
No remnant state, linear increase with a large plateau of saturation
- No shield contribution



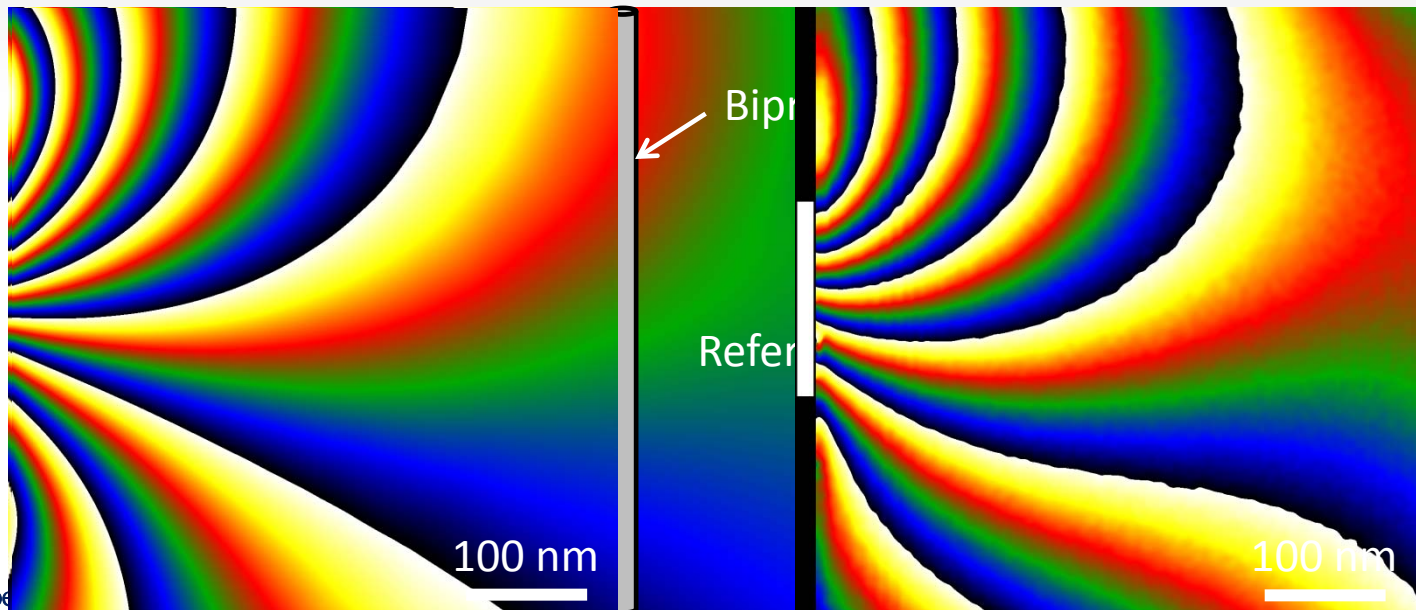
CR

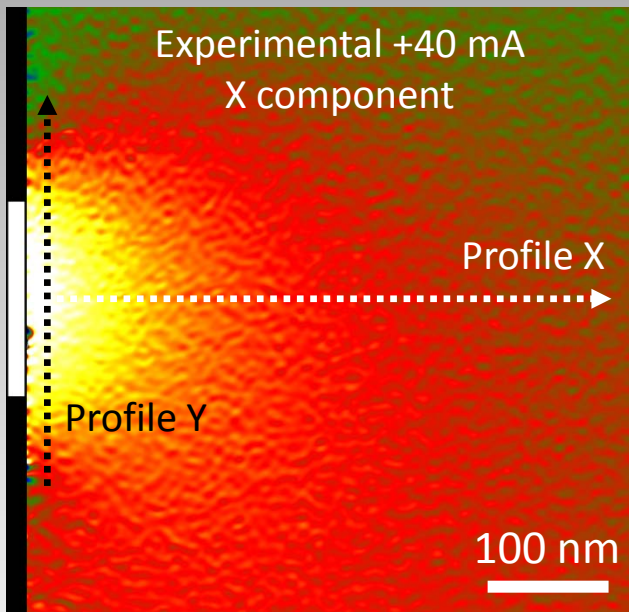
### 3D micromagnetic simulations using Magpar package



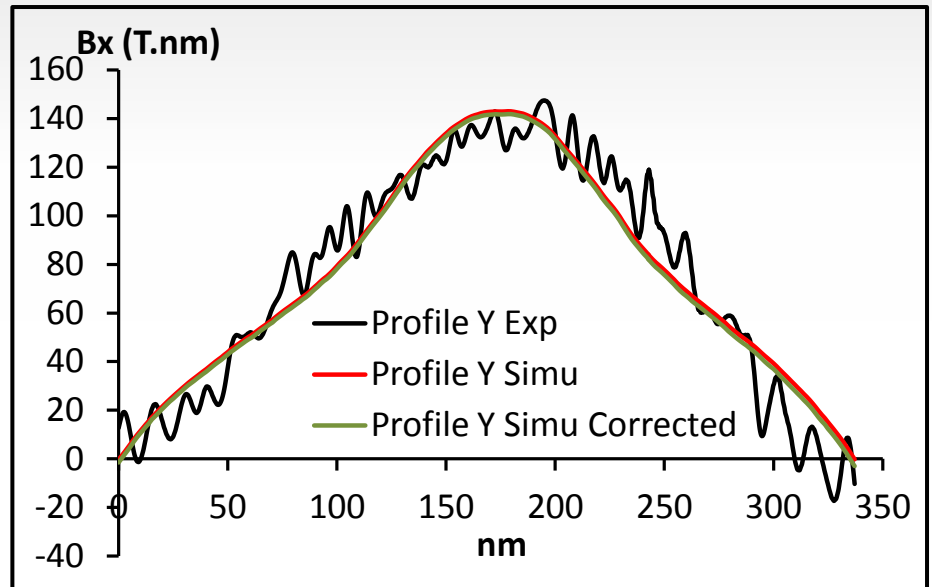
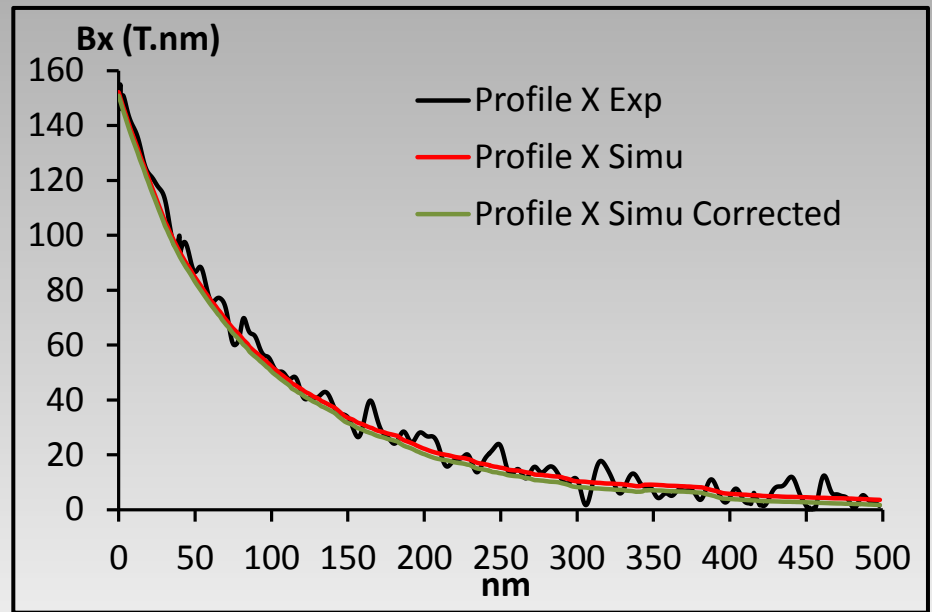
- Box of (1.5 $\mu\text{m}$  x 1  $\mu\text{m}$  x 0.8  $\mu\text{m}$ )
- Integration of the in-plane magnetic field components along the electron path
- Simulated phase shift calculated from Aharonov-Bohm equations
- Slight perturbation in the object wave area

Simulated phase +40 mA corrected      Simulated phase +40 mA      Experimental phase +40 mA



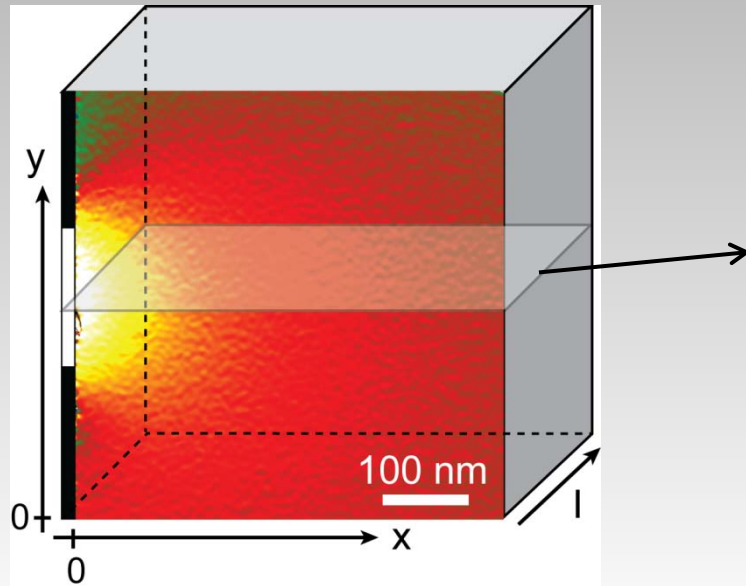


-125 T.nm  125 T.nm

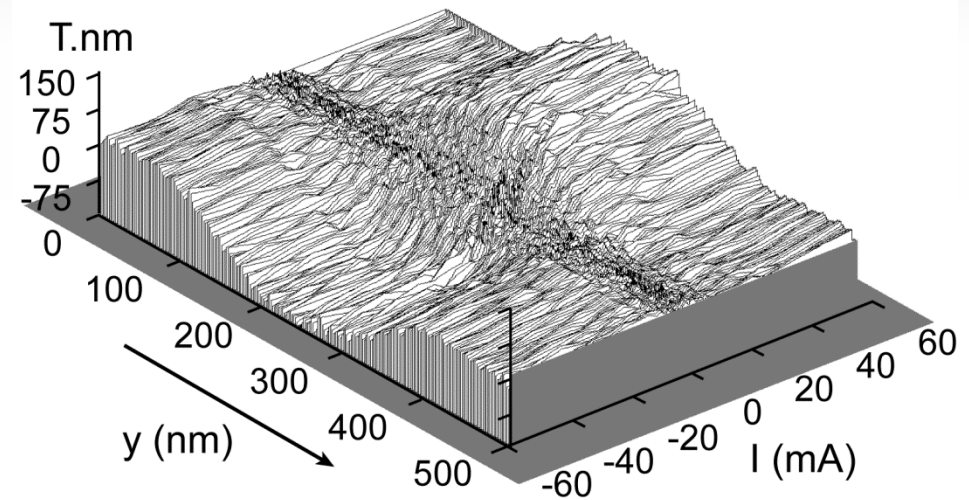
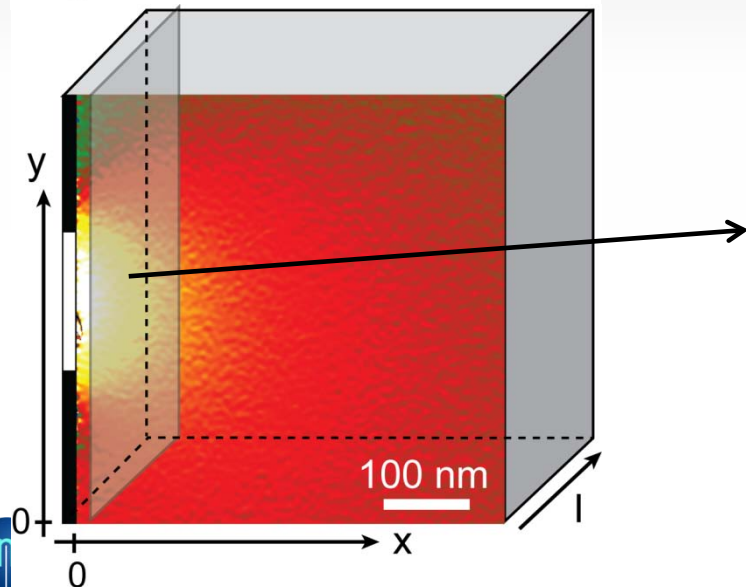
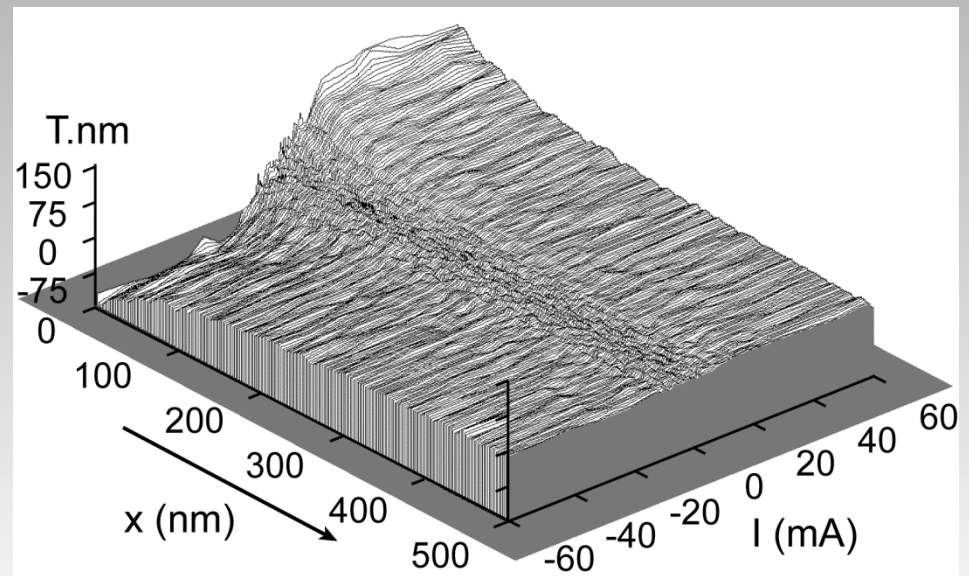


• Negligible effect of the field within the reference area

Experimental data cube of the write pole contribution (X component)

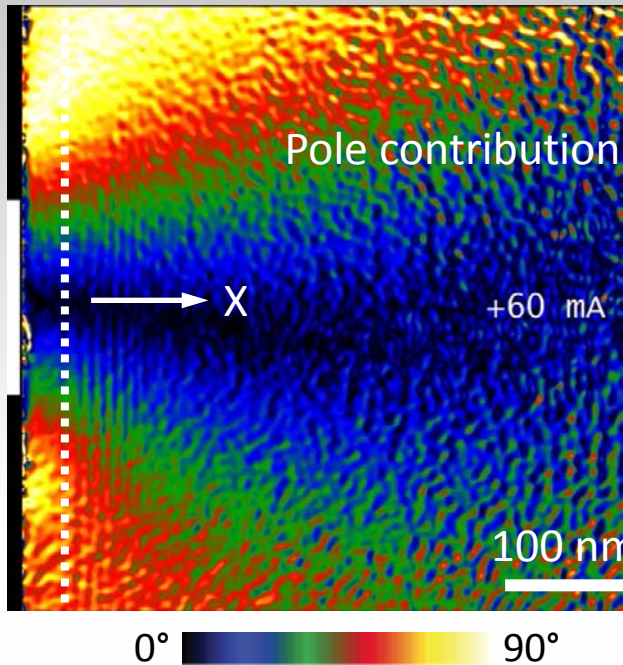


Surface plot of the hysteresis loops

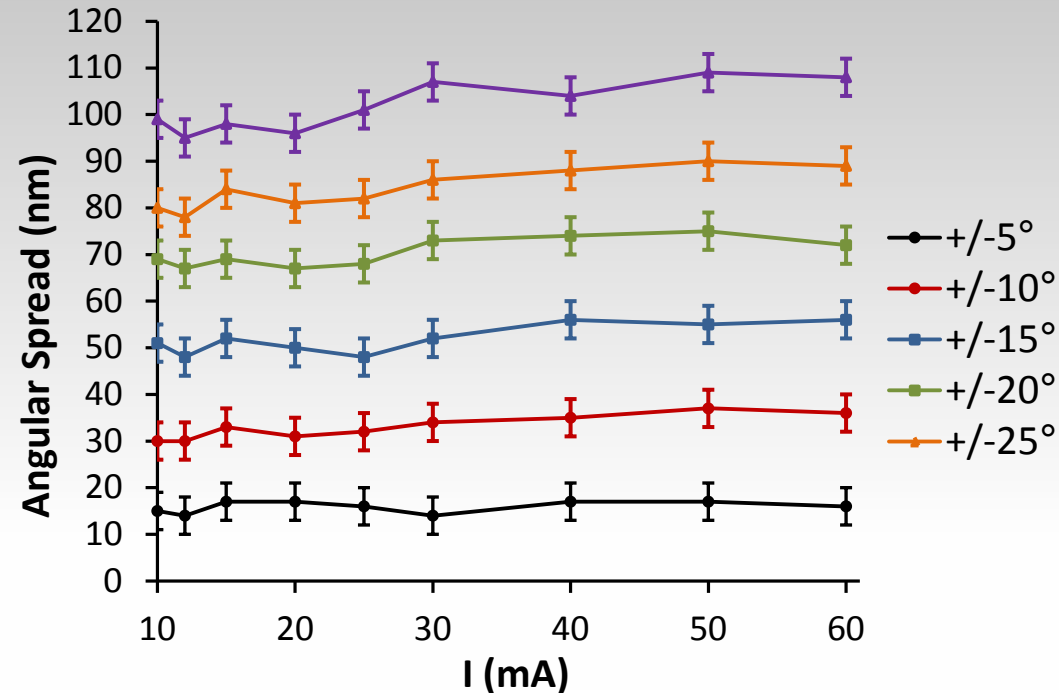


Variation of the radiated regions located at 5 nm in front of the pole as a function of the applied current and for various flux divergences.

### Divergence from the X direction



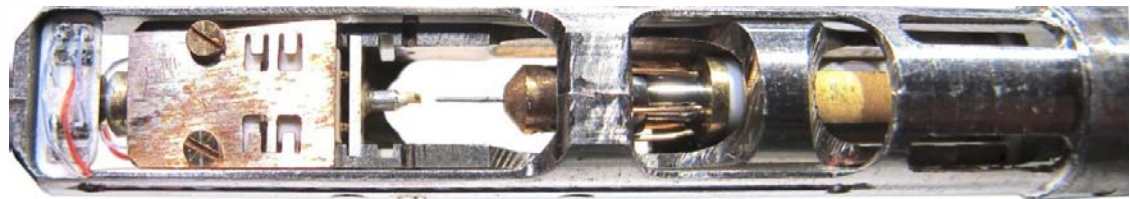
### Angular spread



- Demonstration of the efficiency of the shields for focusing the field onto the media
- From the HDD application point of view, illustration that only the media directly under the write pole will experience any significant magnetic interaction for writing/erasure processes.

## Summary

- Quantitative mapping of the magnetic field generated by the writer part as a function of applied electrical current up to +/-60 mA in real conditions.
- Specific sample preparation to extract the active part of the device, without damaging the magnetic shields and the necessary elements for the current injection.
- The resulting field maps demonstrate the key features requested in magnetic recording, namely a highly directional magnetic field with a low angular spread.
- ***Use the write pole as a in situ magnet to apply a local magnetic field in a TEM.***  
***Mounting on the tip of a sample holder with piezo-electric displacements and moved close to a magnetic sample to be studied.***



**nanoFACTORY**<sup>™</sup>  
INSTRUMENTS

➔ **Perfect tool for performing double exposure interferometry: square signal for the current injection, frequency and amplitude can be tuned.**

# Double exposure interferometry using a HDD writer

JOURNAL OF APPLIED PHYSICS

VOLUME 37, NUMBER 2

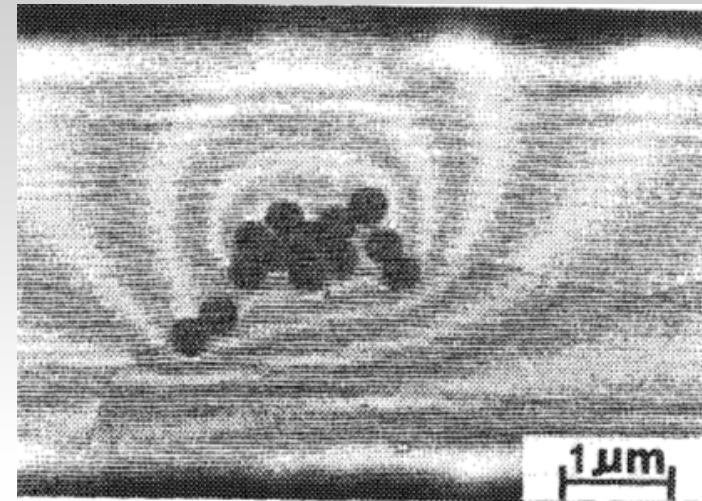
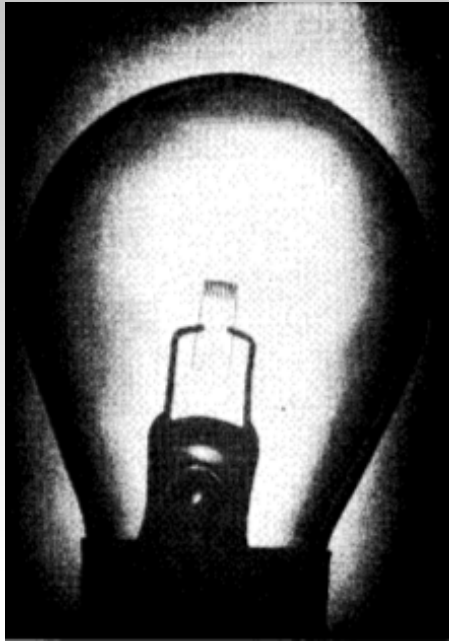
FEBRUARY 1966

## Holographic Interferometry\*

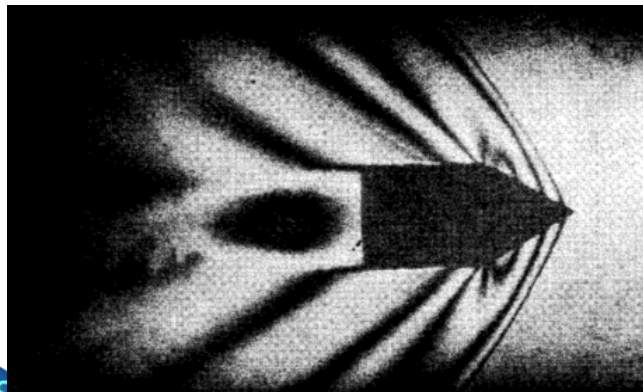
L. O. HEFLINGER, R. F. WUERKER, AND R. E. BROOKS

TRW Systems, Redondo Beach, California

(Received 30 August 1965)



S. Frabboni, G. Matteucci & G. Pozzi  
*Ultramicroscopy* **23**, 29–37 (1987).

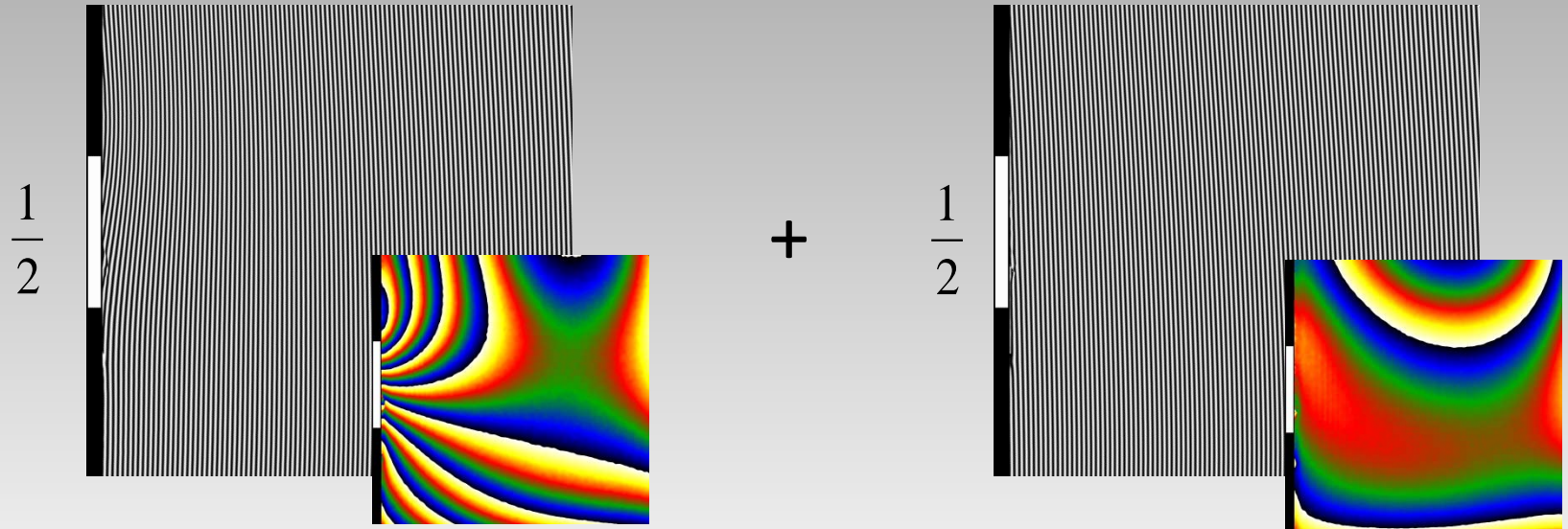


Moiré effect

# Double exposure interferometry using a HDD writer

$\phi_1(\mathbf{R})$  : Pole (+60 mA) + Shield + Distortions

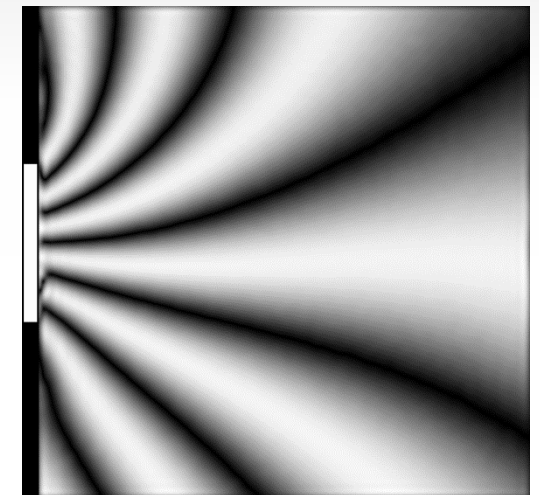
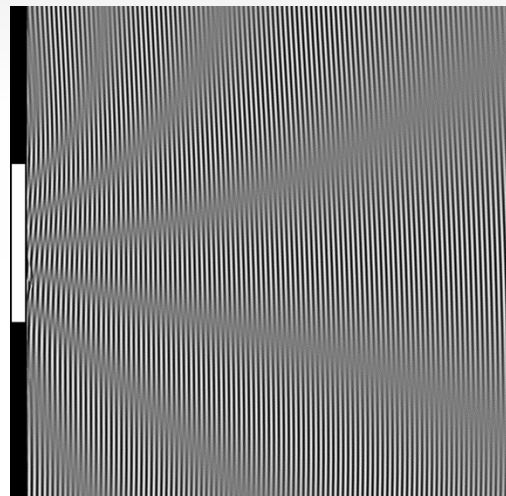
$\phi_2(\mathbf{R})$  : Shield + Distortions



$$I_1(\mathbf{R}) = |A_0|^2 + |A(\mathbf{R})|^2 + 2 A_0 A(\mathbf{R}) \cos(k \cdot \mathbf{R} + \phi_1(\mathbf{R}))$$

$$I_1(\mathbf{R}) = |A_0|^2 + |A(\mathbf{R})|^2 + 2 A_0 A(\mathbf{R}) \cos(k \cdot \mathbf{R} + \phi_2(\mathbf{R}))$$

=



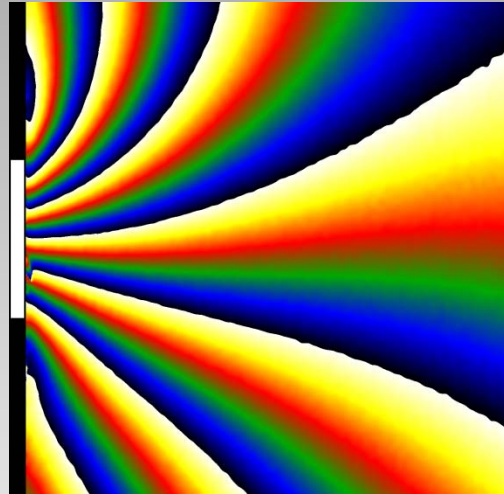
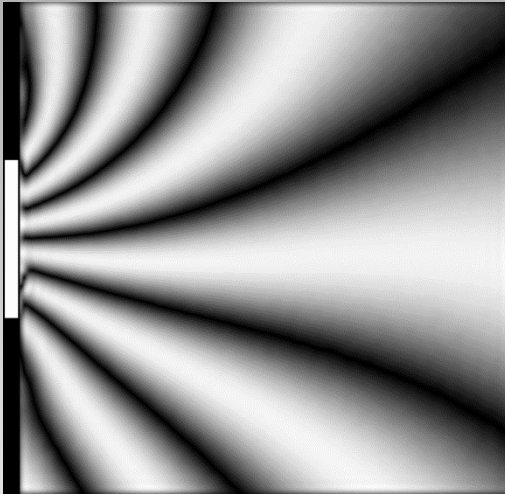
Amplitude

$$I_{1+2}(\mathbf{R}) = |A_0|^2 + |A(\mathbf{R})|^2$$

$$+ 2 A_0 A(\mathbf{R}) \cos\left(\frac{\phi_1(\mathbf{R}) - \phi_2(\mathbf{R})}{2}\right) \cos\left(k \cdot \mathbf{R} + \frac{\phi_1(\mathbf{R}) + \phi_2(\mathbf{R})}{2}\right)$$



# Double exposure interferometry using a HDD writer

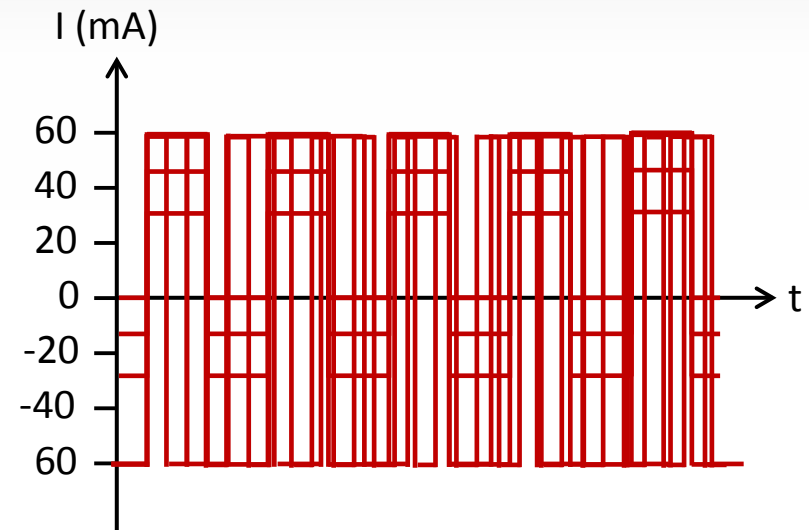


- Direct information from only pole contribution
- Other constant contributions (shield, distortions) removed

$$\begin{aligned} \text{Amplitude} &\propto \cos\left(\frac{\phi_1(\mathbf{R}) - \phi_2(\mathbf{R})}{2}\right) \\ &\propto \cos\left(\frac{\text{Pole (+60 mA)}}{2}\right) \end{aligned}$$

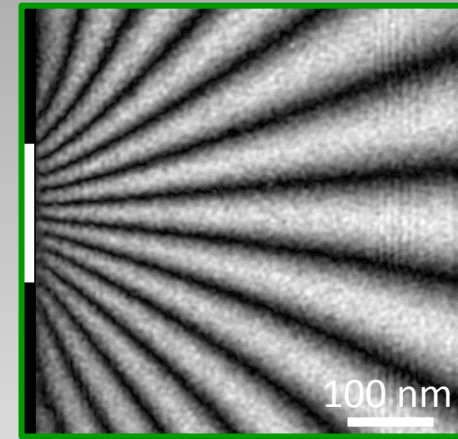
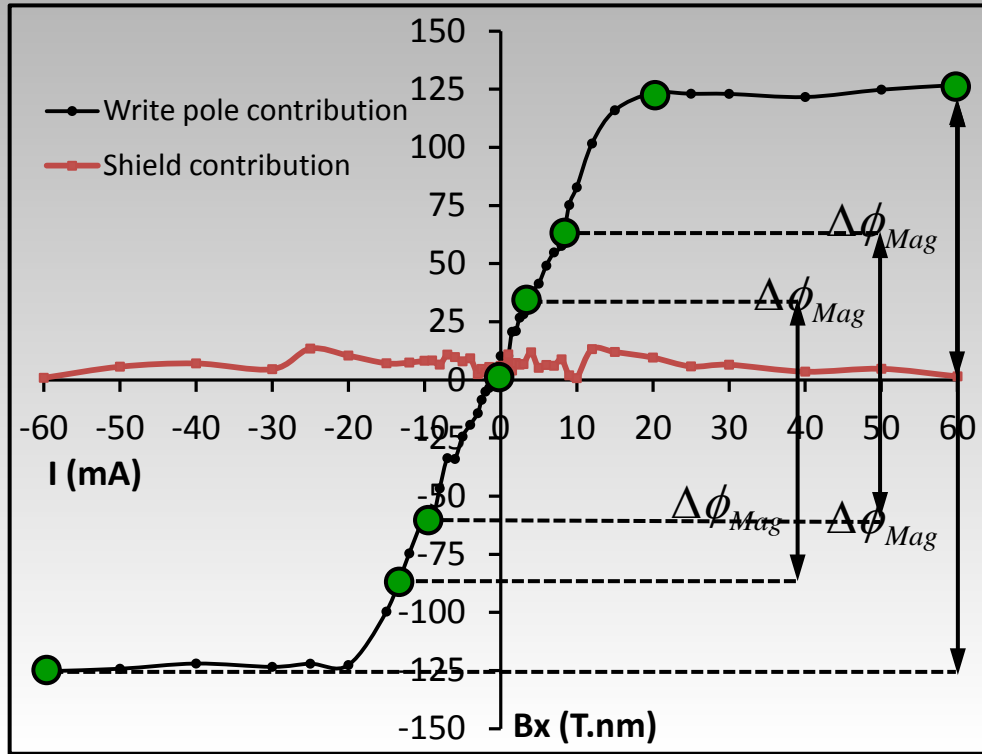
Phase of pole contribution +60 mA

- Need to superimpose 2 states during the exposure time  
=> **Square signal for current injection**
- Possibility to change:
  - the offset
  - the amplitude
  - the frequency

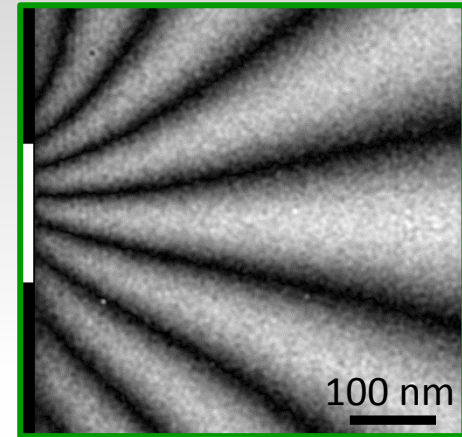


# Double exposure interferometry using a HDD writer

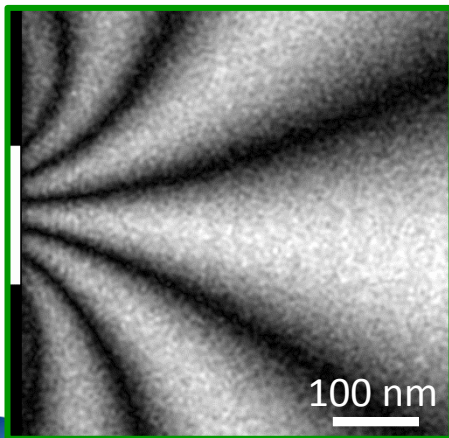
Freq = 1kHz, 4s acquisition time



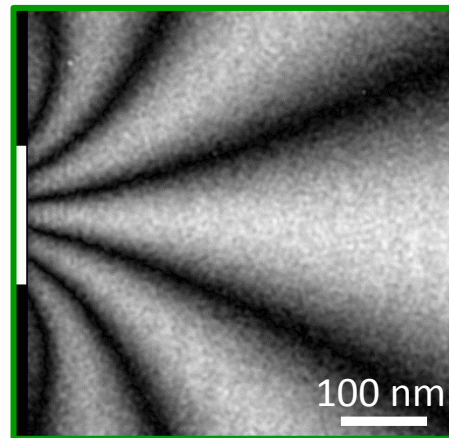
-60 to +60 mA



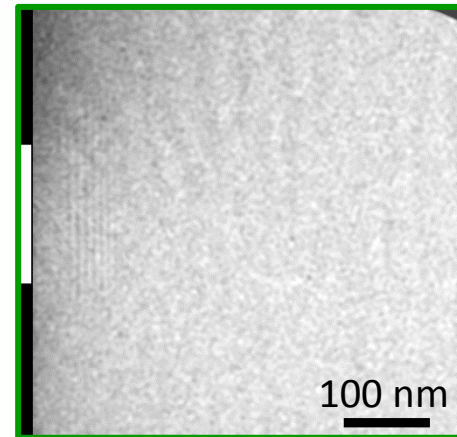
0 to +60 mA



-15 to +15 mA

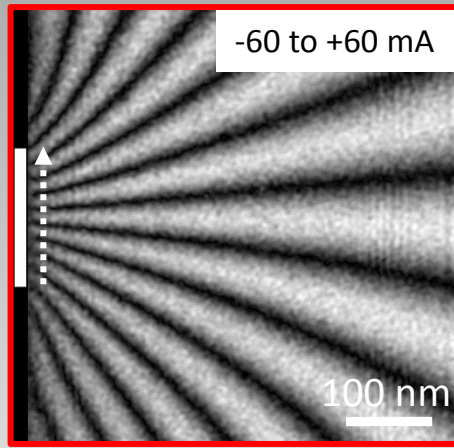


-10 to +10 mA

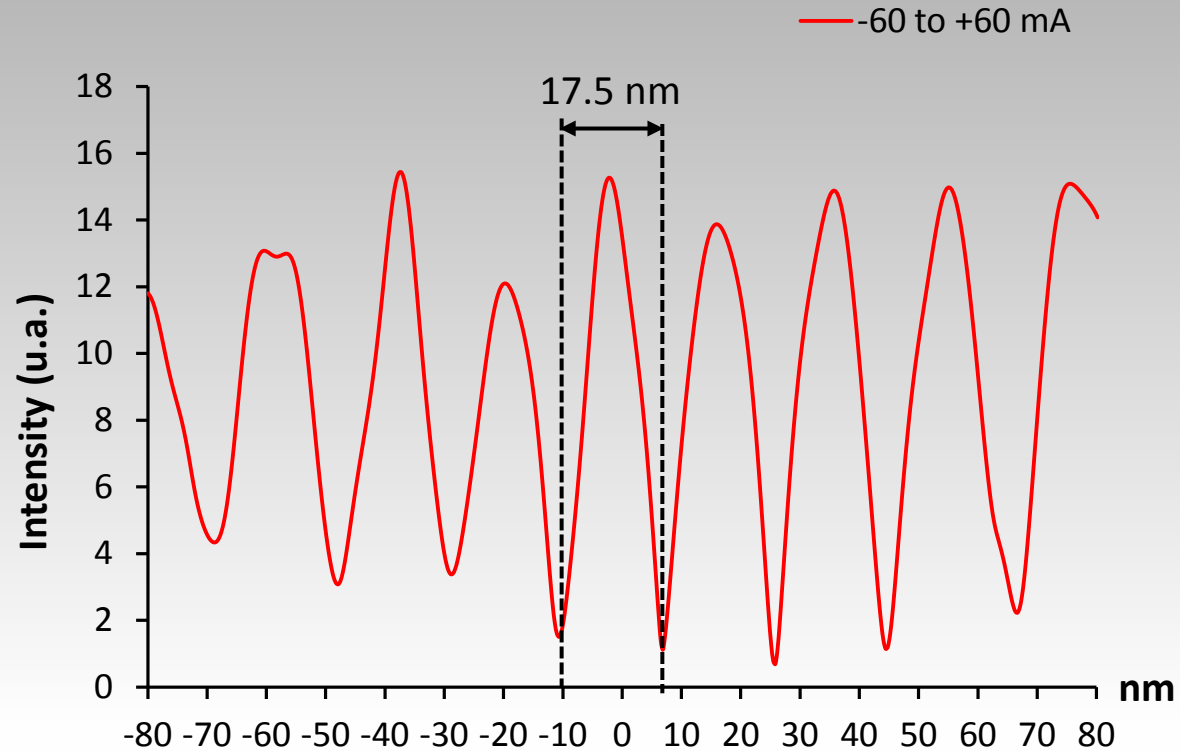


20 to +60 mA

# Double exposure interferometry using a HDD writer



Freq = 1kHz, 4s acquisition time



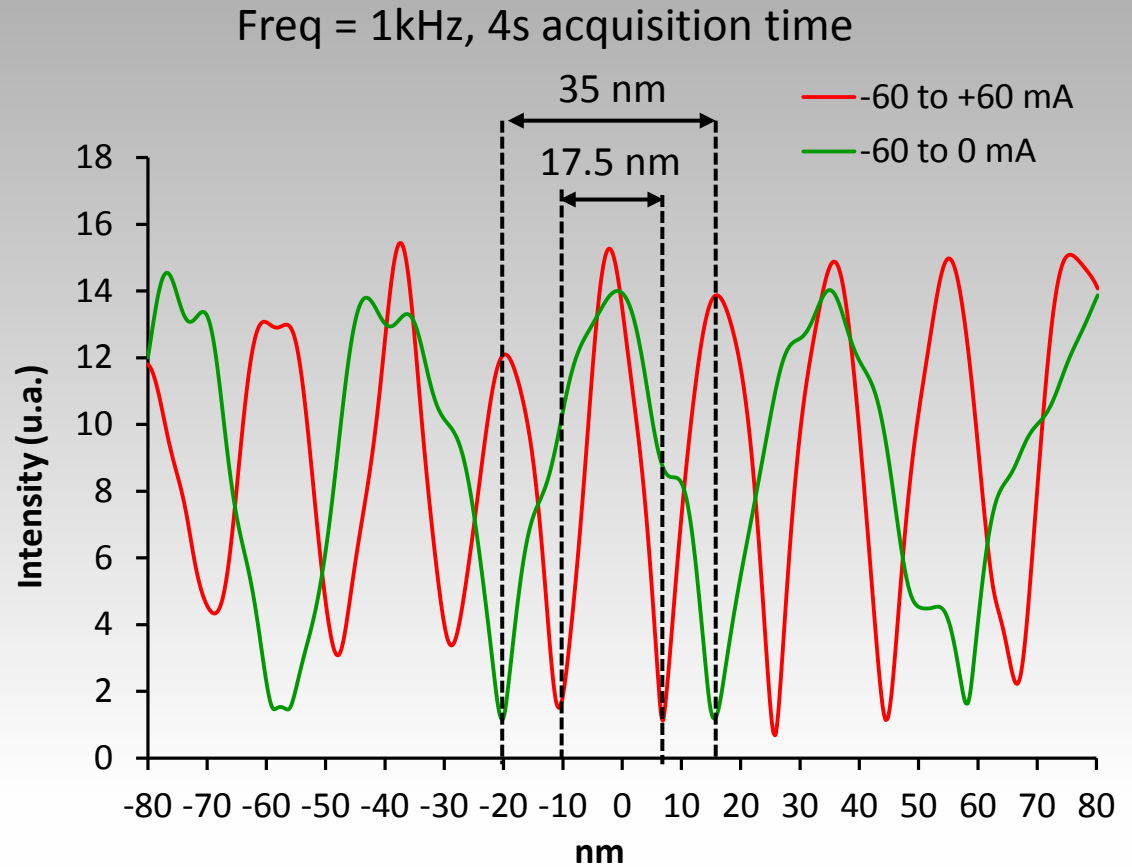
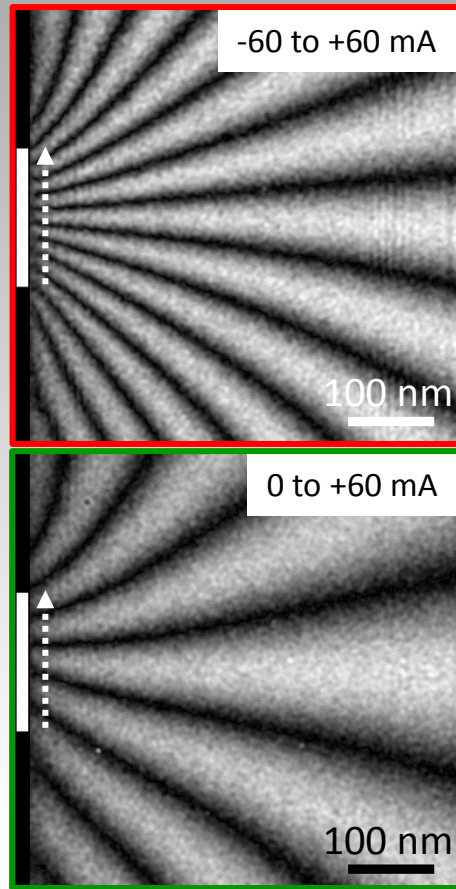
- $2\pi$  phase jump between 2 minima (or maxima)

$$\iint B_{\perp}(\mathbf{r}_{\perp}, z) dr dz = -\frac{h}{e} \Delta\phi_{Mag}(\mathbf{r}) = -\frac{h}{e} = 4.136 \cdot 10^{-15} \text{ Wb}$$

$$\text{Length} = 17.5 \text{ nm} \Rightarrow \int_{-\infty}^{\infty} B_y(r_{\perp}, z) dz \approx 236 \text{ T.nm}$$

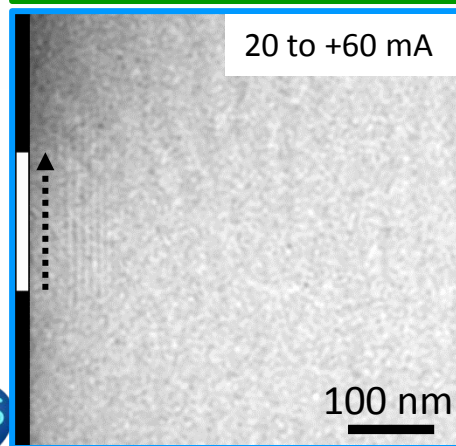
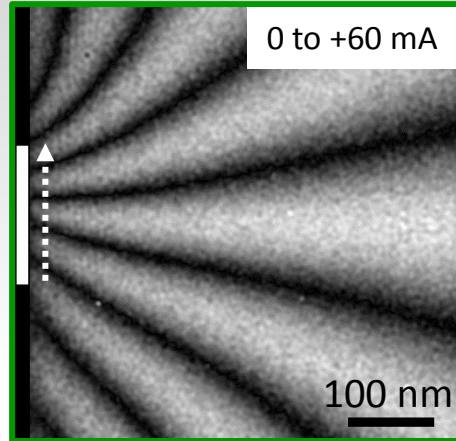
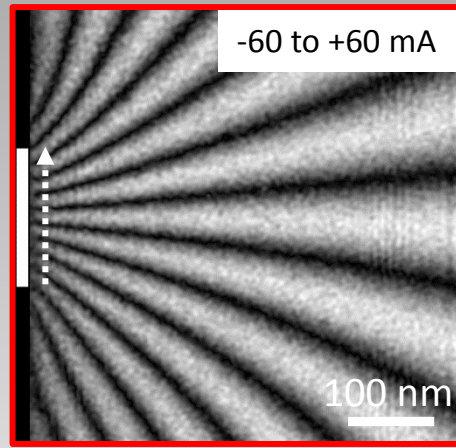
-60 to 60 mA: 2 x Saturated magnetic flux  $\Rightarrow$  118 T.nm

# Double exposure interferometry using a HDD writer

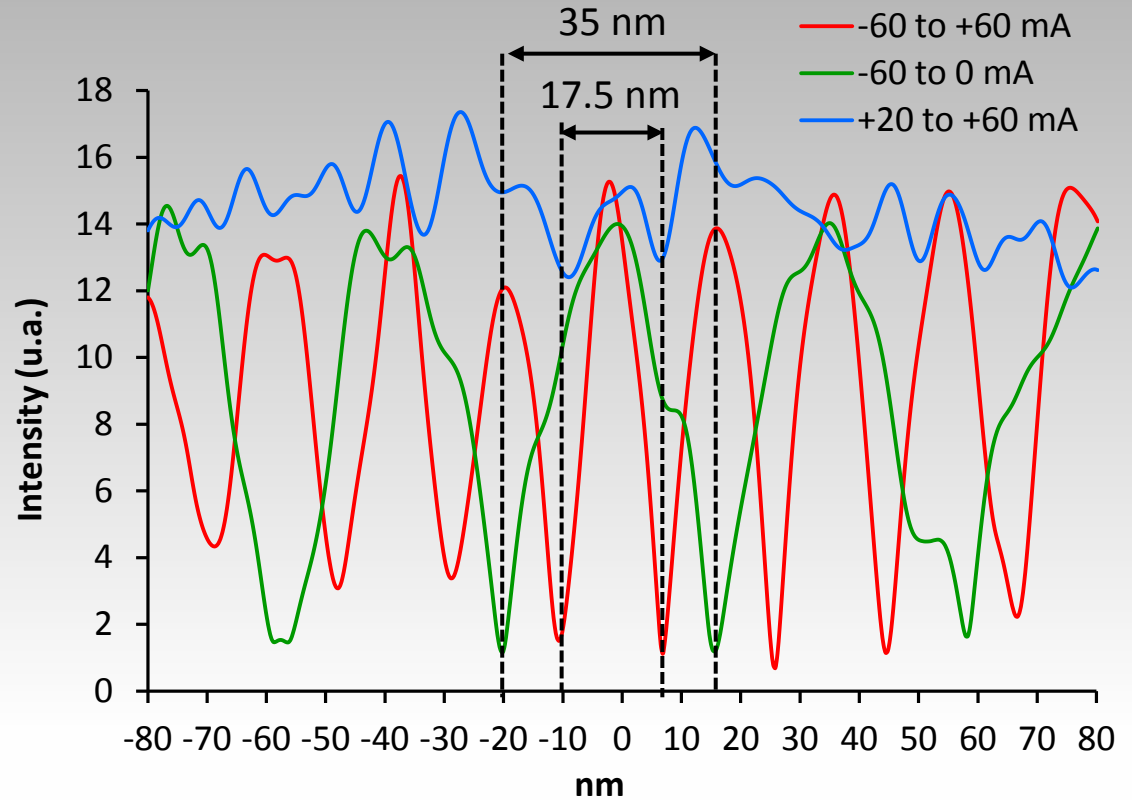


- If the amplitude of the current is divided by 2, distance between 2 minima multiplied by 2  
=> Magnetic flux divided by 2

# Double exposure interferometry using a HDD writer



Freq = 1kHz, 4s acquisition time



- If no variation of magnetic flux (saturation), amplitude is constant (no pronounced minima or maxima)

=> Magnetic induction can be measured and a magnetic map is obtained without reference problem

# Double exposure interferometry using a HDD writer

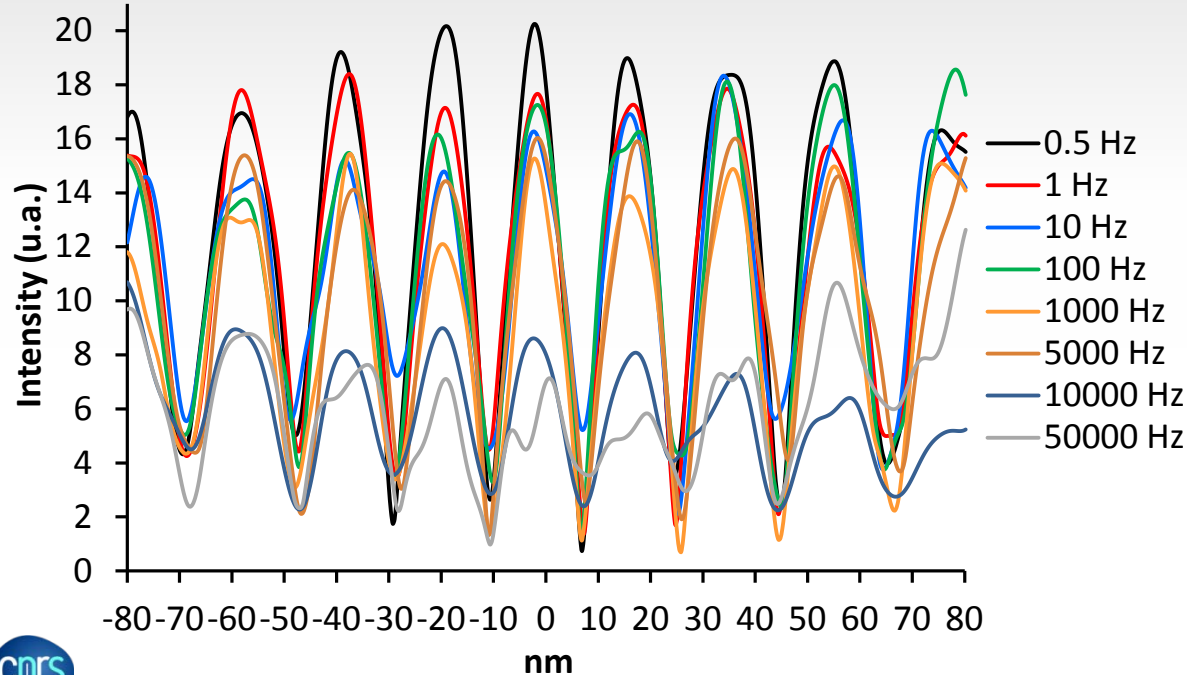
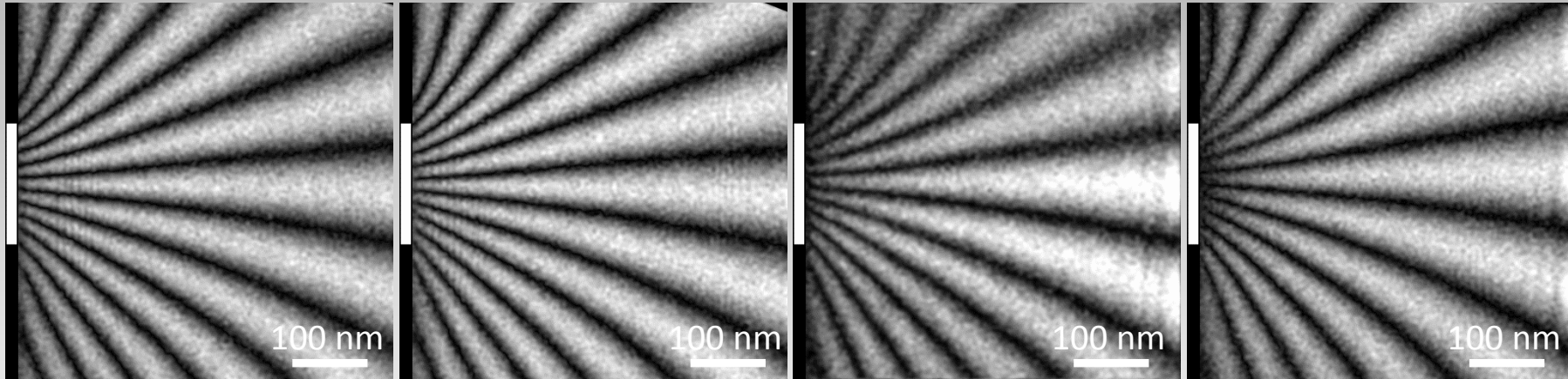
-60 to 60 mA, 4s acquisition time

1 Hz

100 Hz

10000 Hz

50000 Hz

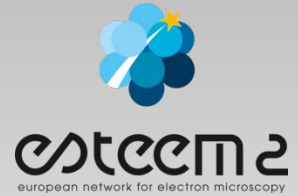


- No effect of the frequency on the amplitude of the magnetic flux
- Decrease of the amplitude of the fringes (vibration ?)
- Limitation of the electrical contacts, sample holder and source meter



## Acknowledgments

- European Union under the Seventh Framework Programme under a contract for an Integrated Infrastructure Initiative Reference 312483-**ESTEEM2**.
- French National Research Agency under the "Investissement d'Avenir" program reference No. ANR-10-EQPX-38-01": **MIMETIS**.
- This work is supported by the French national project **EMMA** (ANR12 BS10 013 01).



# 14

## European schools and workshops

to provide training in innovative methods in electron microscopy and a forum for discussing emerging techniques.  
(including QEM2013: [www.qem2013.com](http://www.qem2013.com))

## ESTEEM2 research program

focuses on the further development of :

- electron diffraction
- imaging
- spectroscopy
- 3D methods
- time-resolved microscopy

ESTEEM2 is an  
**INTEGRATED  
INFRASTRUCTURE NETWORK**  
of electron microscopy facilities providing access for the academic and industrial research community in materials science to the most powerful TEM techniques available at the nanoscale.





## Free transnational access

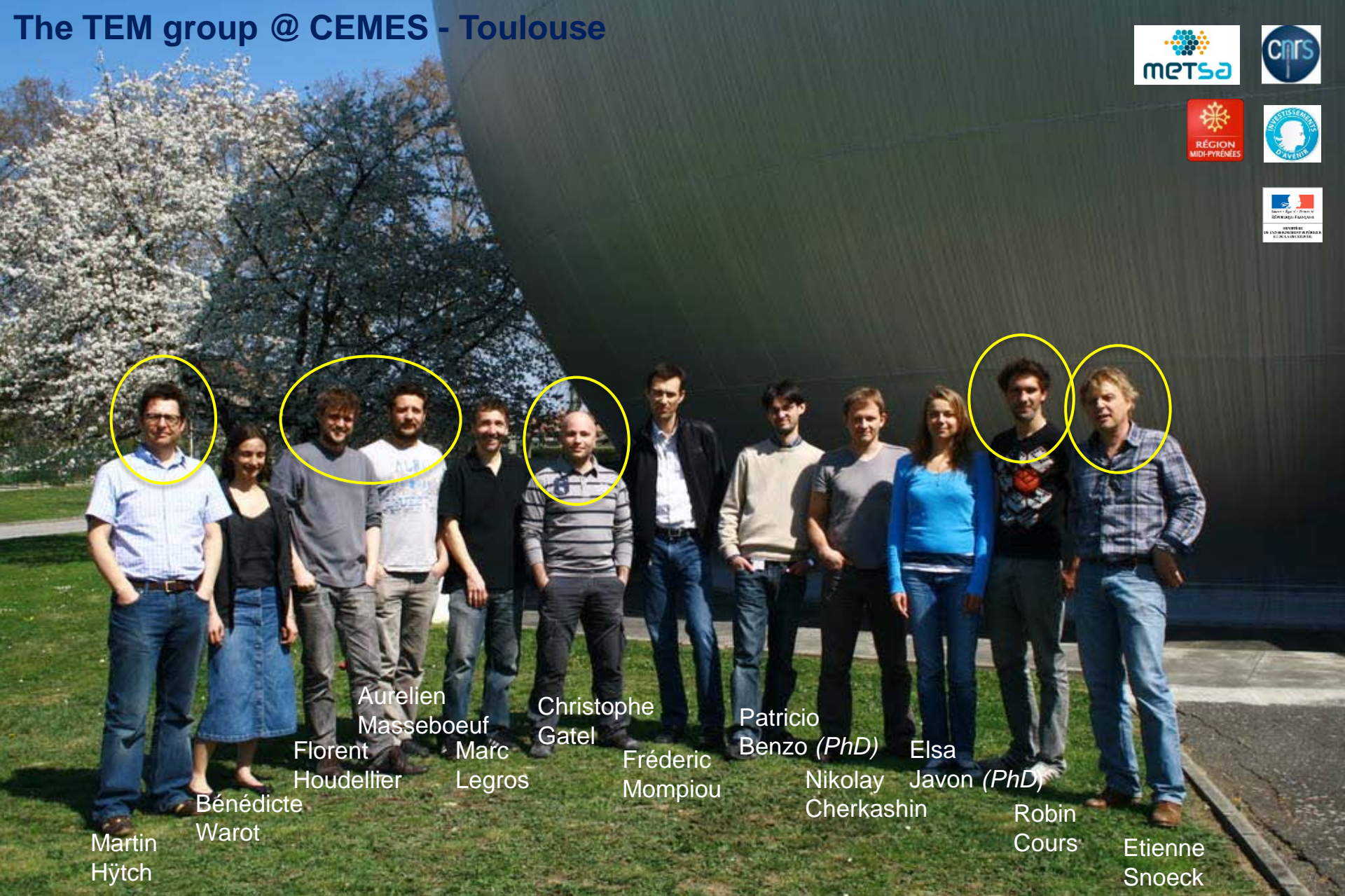
to the most advanced TEM equipment and skilled operators for HR(S)TEM, EELS, EDX, Tomography, Holography and various in-situ state-of-the-art experiments.

### ESTEEM2 available equipment includes:

- 19 FEI-Titan 60-300 and Tecnai G2 aberration corrected microscopes
- 6 JEOL aberration-corrected TEM
- A NION probe corrected Ultrastem 200
- The ZEISS SESAM
- The HITACHI I2TEM Cs corrected C-FEG
- Extensive FIB and sample preparation facilities.



# The TEM group @ CEMES - Toulouse



Martin  
Hýtch

Bénédicte  
Warot

Florent  
Houdellier

Aurelien  
Masseboeuf

Marc  
Legros

Christophe  
Gatel

Frédéric  
Momprou

Patricio  
Benzo (PhD)

Nikolay  
Cherkashin

Elsa  
Javon (PhD)

Robin  
Cours



Etienne  
Snoeck



emc2016  
Lyon • France  
www.emc2016.fr

The 16<sup>th</sup> European  
**MICROSCOPY CONGRESS**

Convention Center - 28<sup>th</sup> August - 2<sup>nd</sup> September

Organised by  and under the auspices of  & IFSM



UNIVERSITÉ DE LYON



Rhône-Alpes

# Double exposure interferometry using a HDD writer

JOURNAL OF APPLIED PHYSICS

VOLUME 37, NUMBER 2

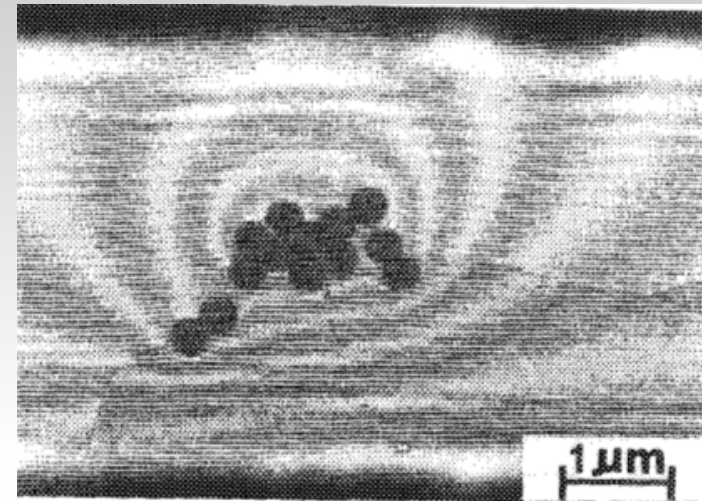
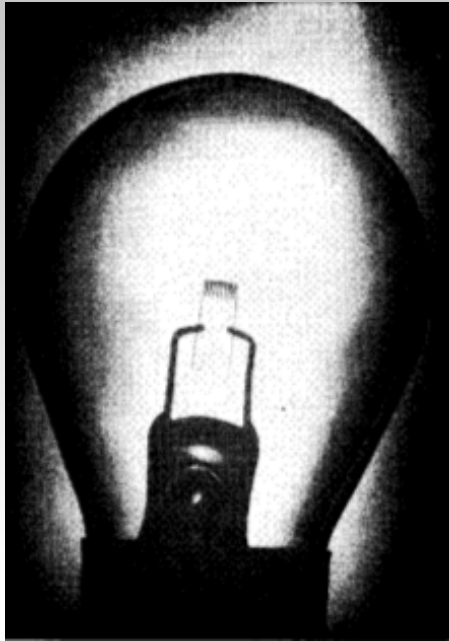
FEBRUARY 1966

## Holographic Interferometry\*

L. O. HEFLINGER, R. F. WUERKER, AND R. E. BROOKS

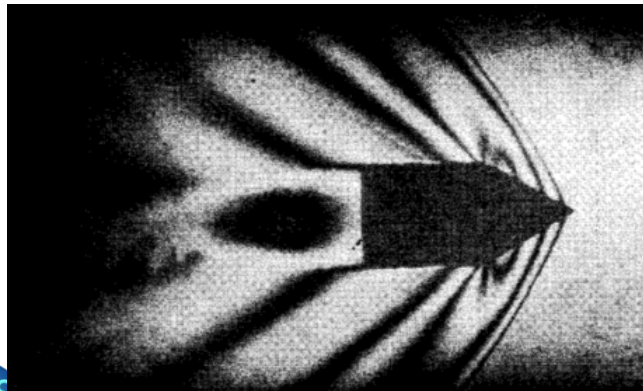
TRW Systems, Redondo Beach, California

(Received 30 August 1965)



S. Frabboni, G. Matteucci & G. Pozzi  
*Ultramicroscopy* **23**, 29–37 (1987).

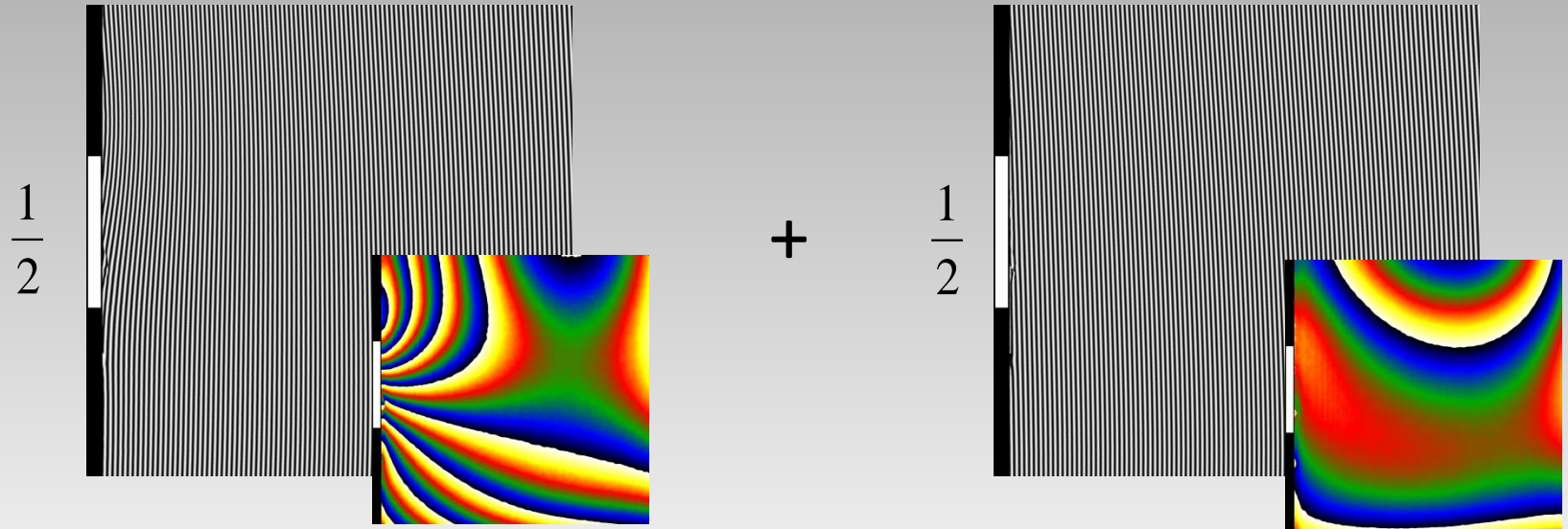
Moiré effect



# Double exposure interferometry using a HDD writer

$\phi_1(\mathbf{R})$  : Pole (+60 mA) + Shield + Distortions

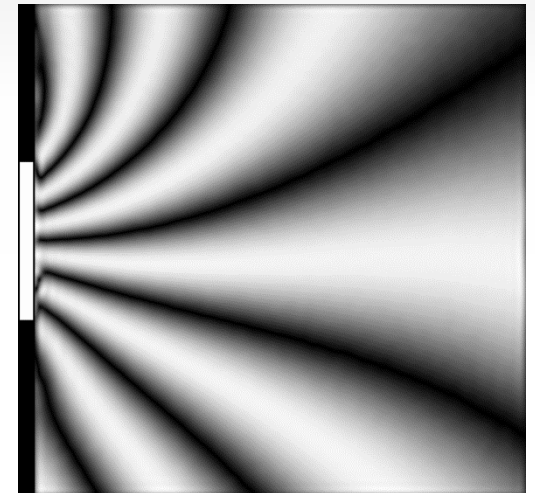
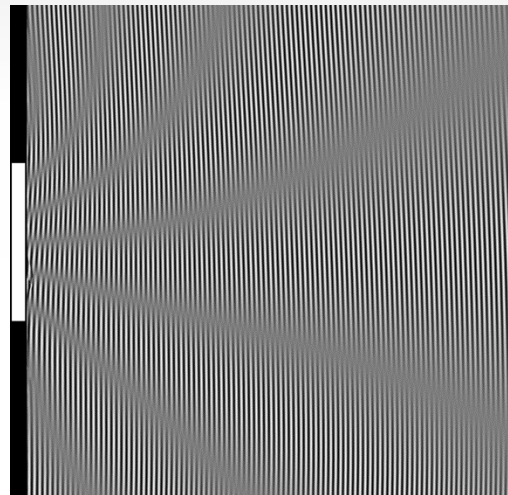
$\phi_2(\mathbf{R})$  : Shield + Distortions



$$I_1(\mathbf{R}) = |A_0|^2 + |A(\mathbf{R})|^2 + 2 A_0 A(\mathbf{R}) \cos(k \cdot \mathbf{R} + \phi_1(\mathbf{R}))$$

$$I_1(\mathbf{R}) = |A_0|^2 + |A(\mathbf{R})|^2 + 2 A_0 A(\mathbf{R}) \cos(k \cdot \mathbf{R} + \phi_2(\mathbf{R}))$$

=

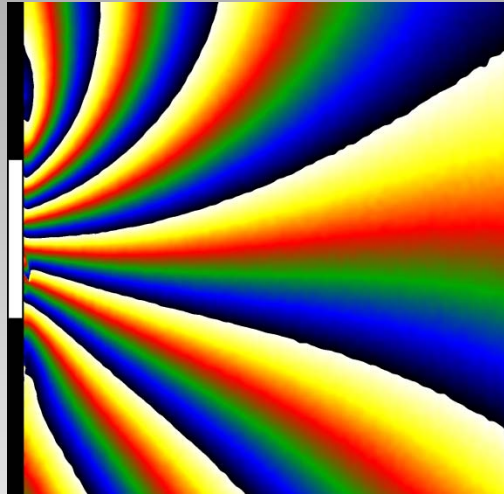
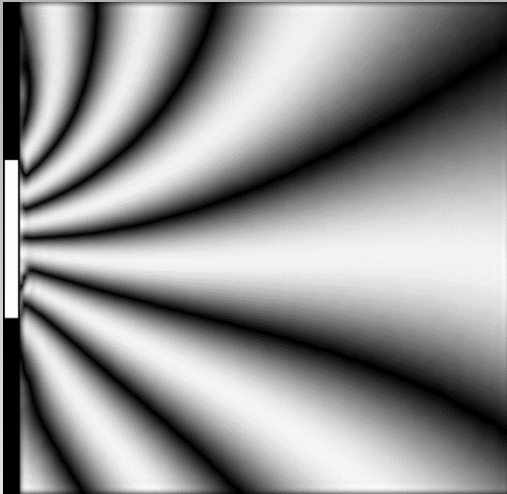


Amplitude

$$I_{1+2}(\mathbf{R}) = |A_0|^2 + |A(\mathbf{R})|^2$$

$$+ 2 A_0 A(\mathbf{R}) \cos\left(\frac{\phi_1(\mathbf{R}) - \phi_2(\mathbf{R})}{2}\right) \cos\left(k \cdot \mathbf{R} + \frac{\phi_1(\mathbf{R}) + \phi_2(\mathbf{R})}{2}\right)$$

# Double exposure interferometry using a HDD writer



- Direct information from only pole contribution
- Other constant contributions (shield, distortions) removed

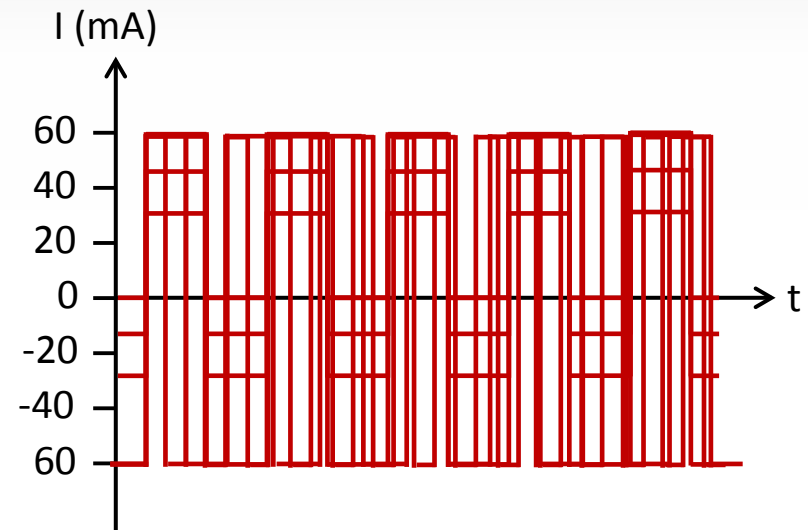
$$\text{Amplitude} \propto \cos\left(\frac{\phi_1(\mathbf{R}) - \phi_2(\mathbf{R})}{2}\right)$$
$$\propto \cos\left(\frac{\text{Pole (+60 mA)}}{2}\right)$$

Phase of pole contribution +60 mA

- Need to superimpose 2 states during the exposure time

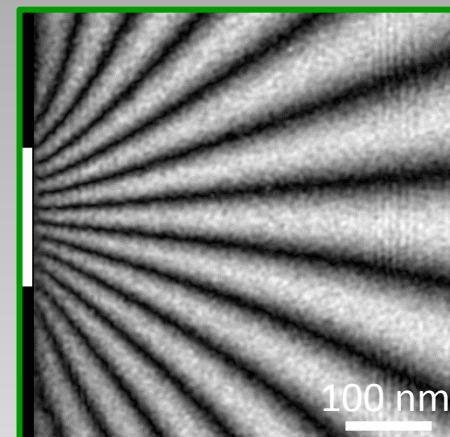
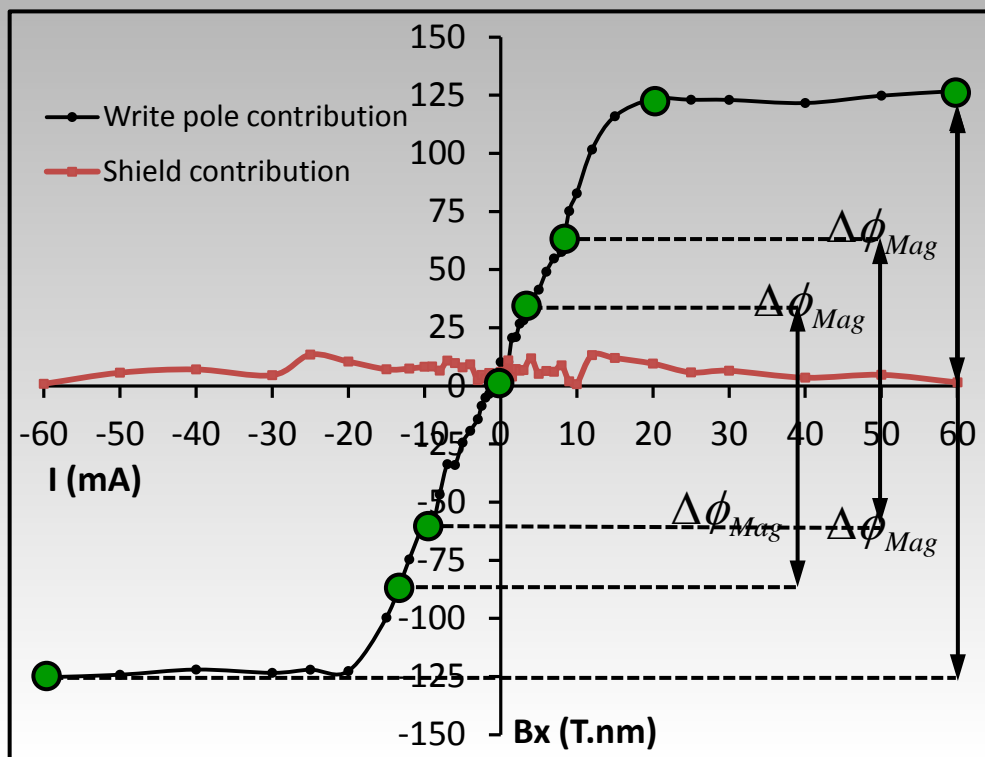
=> **Square signal for current injection**

- Possibility to change:
  - the offset
  - the amplitude
  - the frequency

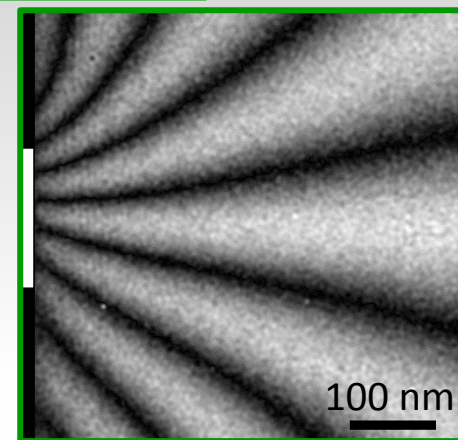


# Double exposure interferometry using a HDD writer

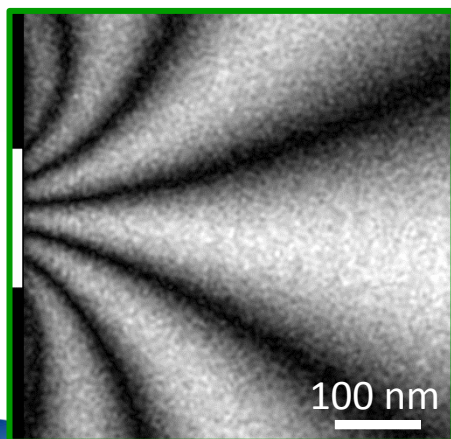
Freq = 1kHz, 4s acquisition time



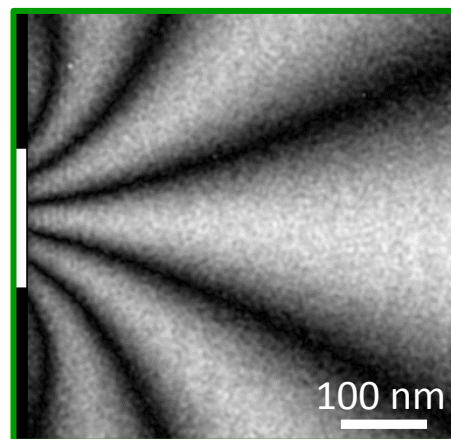
-60 to +60 mA



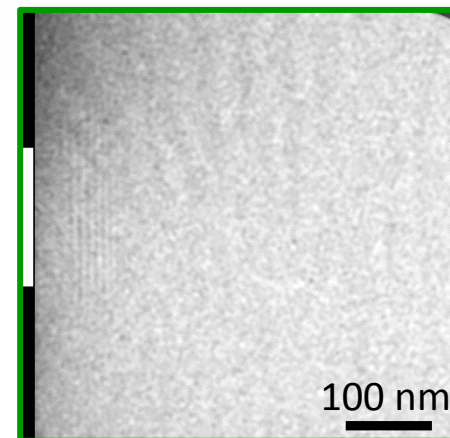
0 to +60 mA



-15 to +15 mA



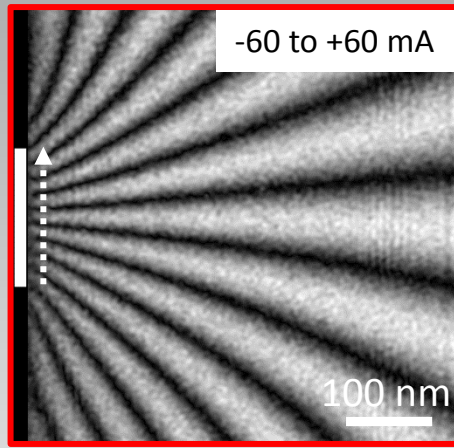
-10 to +10 mA



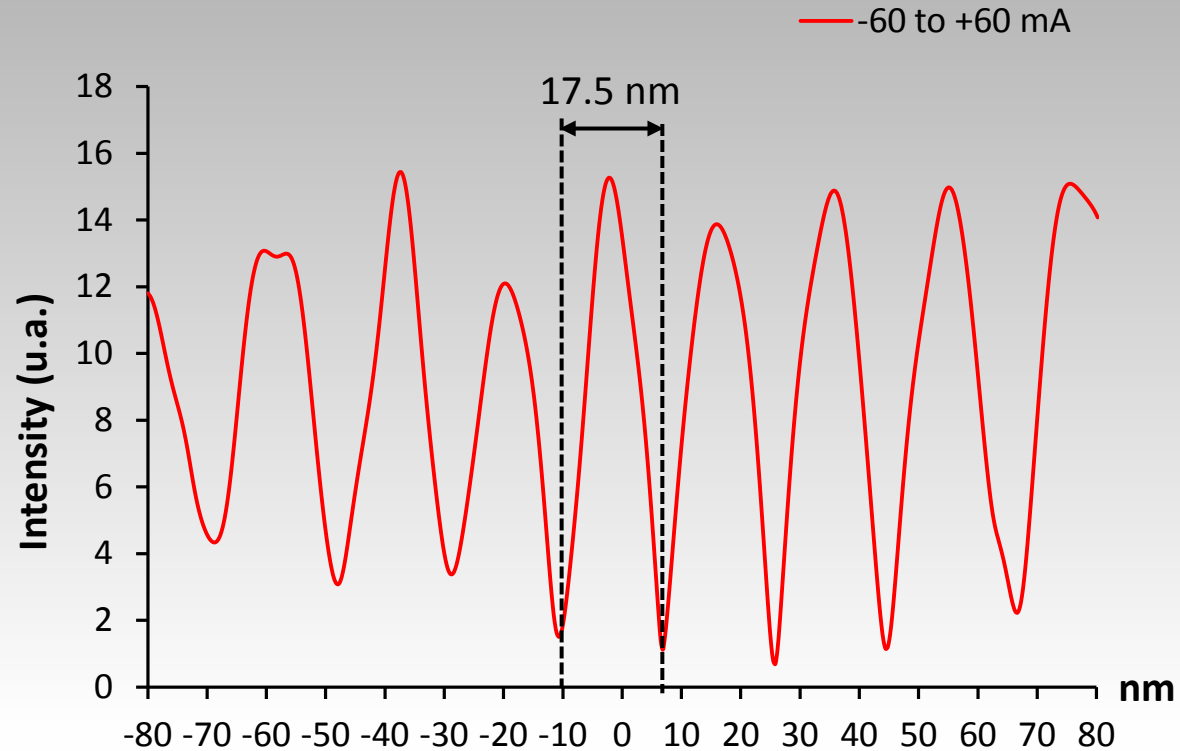
20 to +60 mA



# Double exposure interferometry using a HDD writer



Freq = 1kHz, 4s acquisition time



- $2\pi$  phase jump between 2 minima (or maxima)

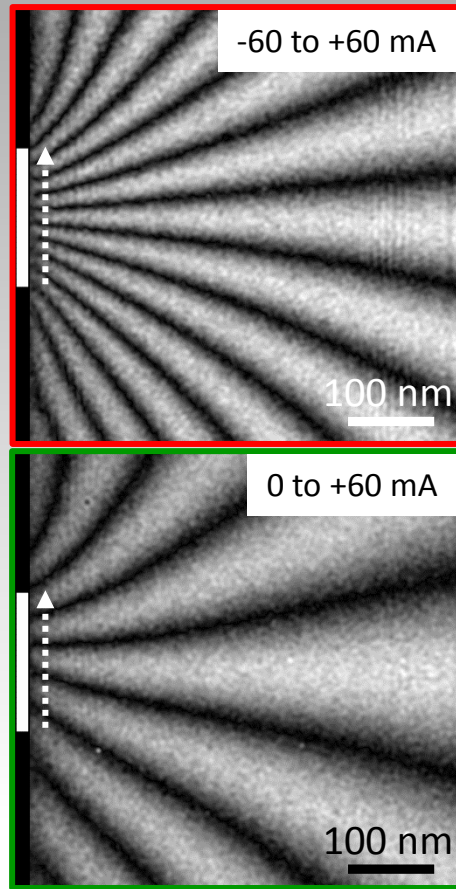
$$\iint B_{\perp}(\mathbf{r}_{\perp}, z) dr dz = -\frac{h}{e} \Delta\phi_{Mag}(\mathbf{r}) = -\frac{h}{e} = 4.136 \cdot 10^{-15} \text{ Wb}$$

$$\text{Length} = 17.5 \text{ nm} \Rightarrow \int_{-\infty}^{\infty} B_y(r_{\perp}, z) dz \approx 236 \text{ T.nm}$$

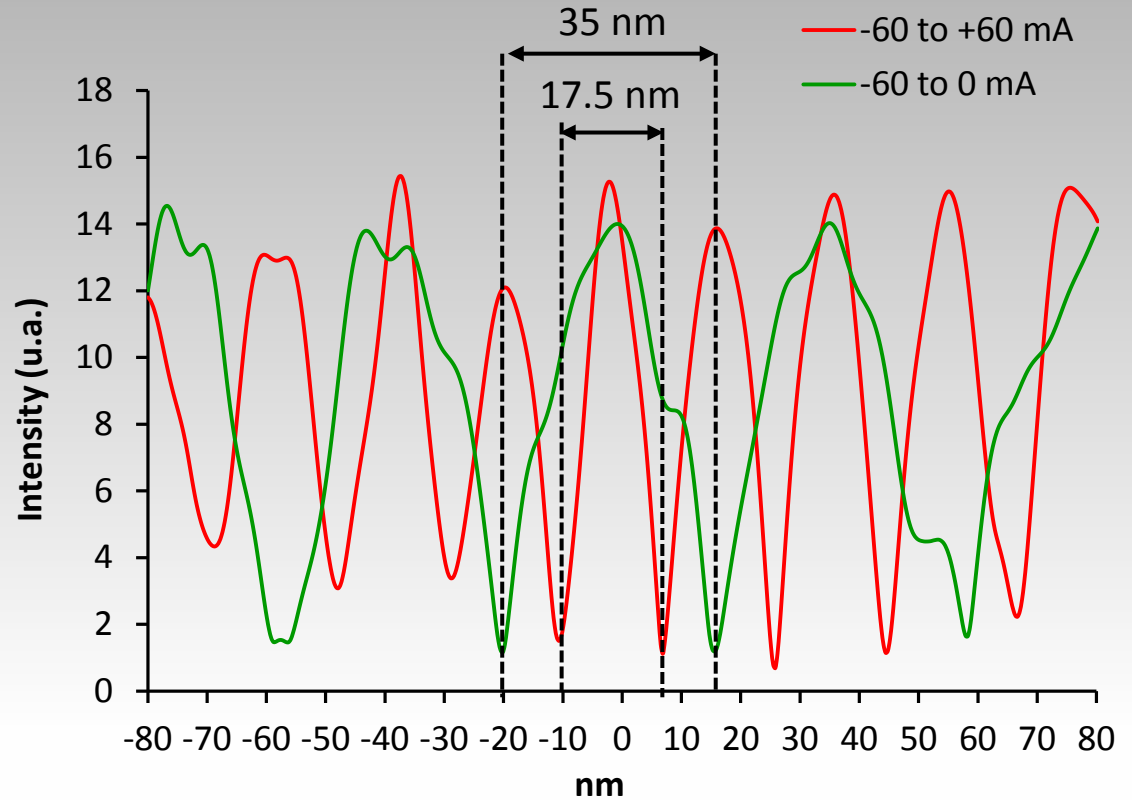
-60 to 60 mA: 2 x Saturated magnetic flux  $\Rightarrow$  118 T.nm



# Double exposure interferometry using a HDD writer

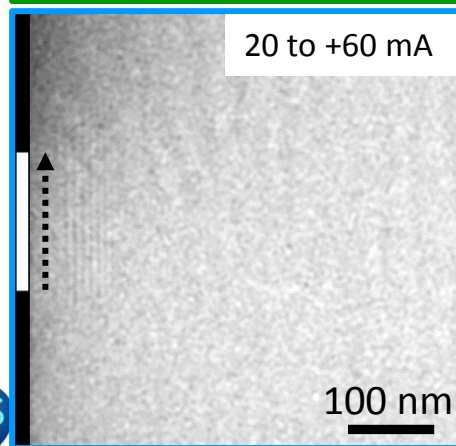
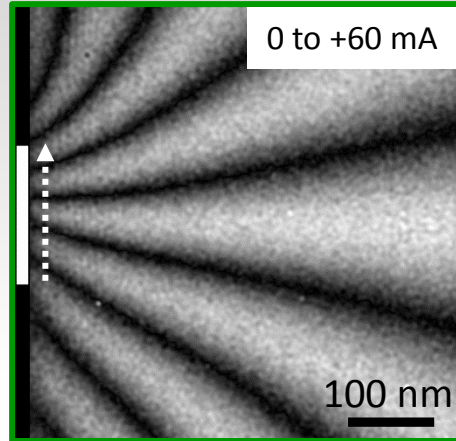
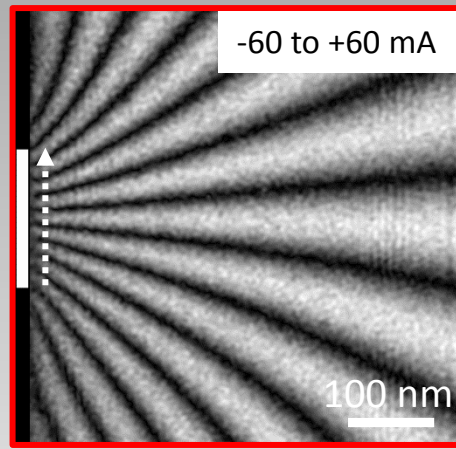


Freq = 1kHz, 4s acquisition time

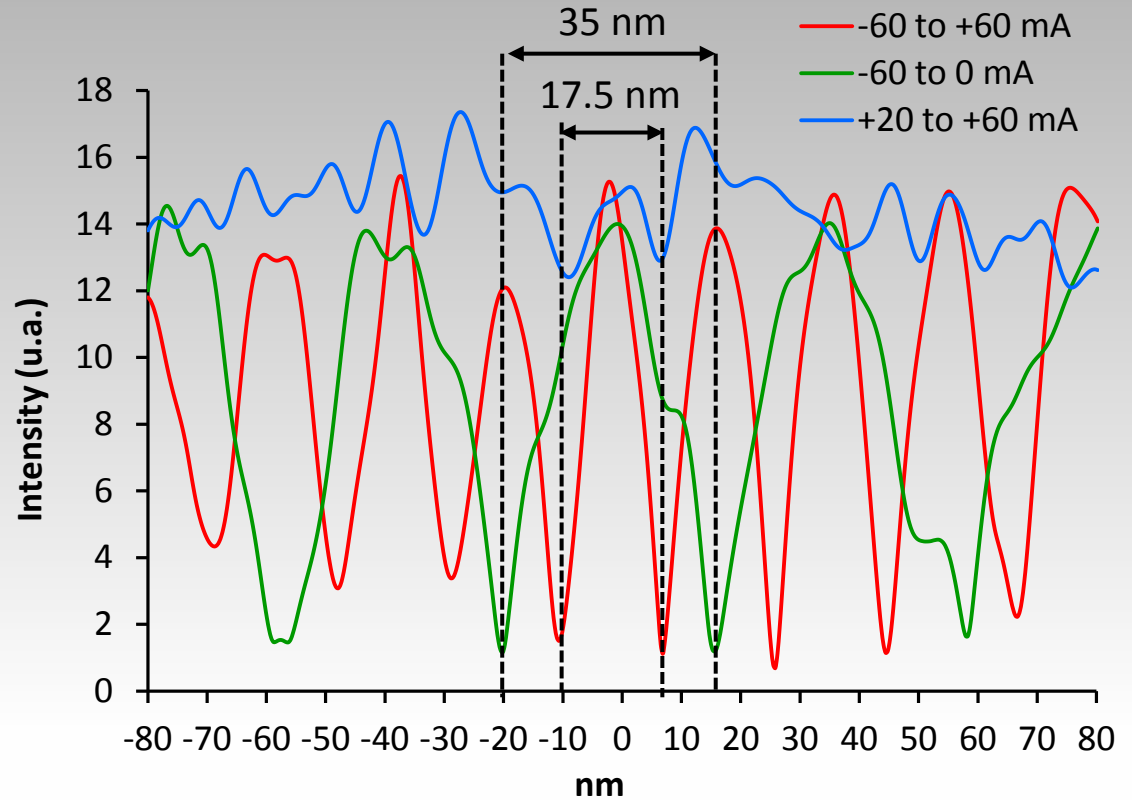


- If the amplitude of the current is divided by 2, distance between 2 minima multiplied by 2  
=> Magnetic flux divided by 2

# Double exposure interferometry using a HDD writer



Freq = 1kHz, 4s acquisition time



- If no variation of magnetic flux (saturation), amplitude is constant (no pronounced minima or maxima)

=> Magnetic induction can be measured and a magnetic map is obtained without reference problem

# Double exposure interferometry using a HDD writer

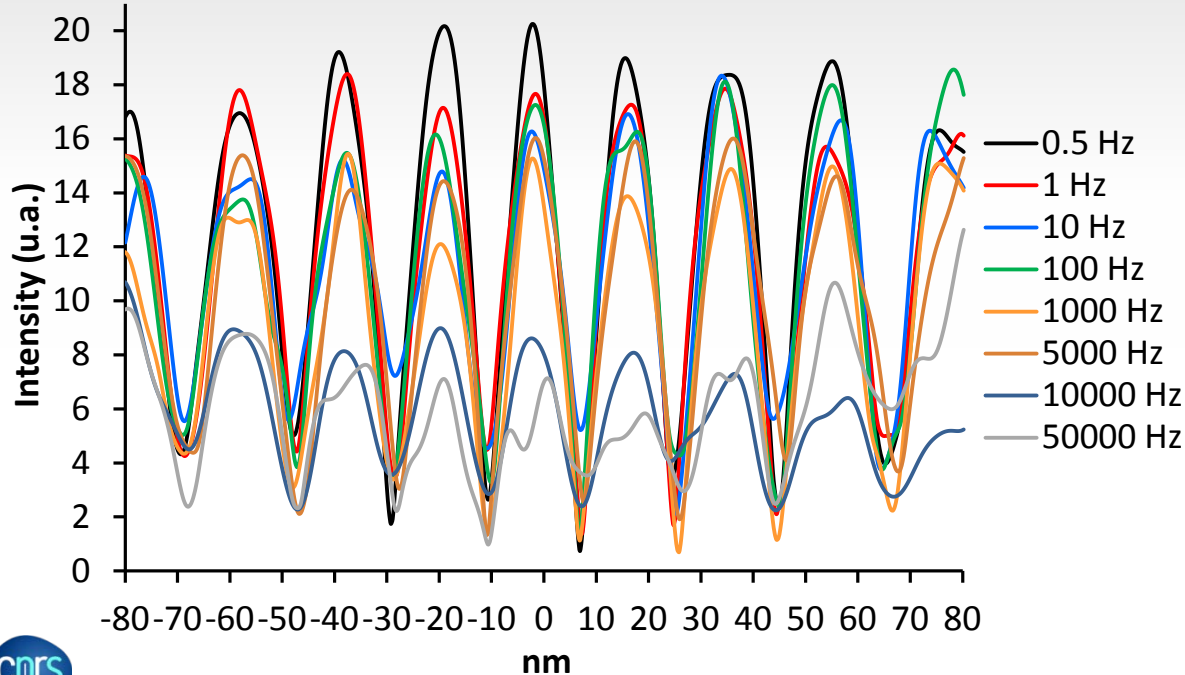
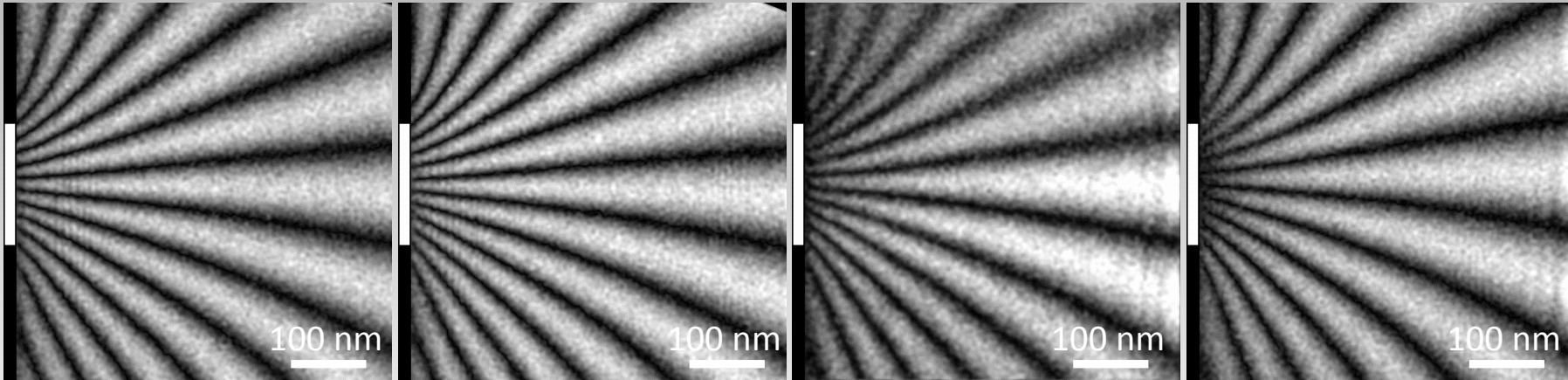
-60 to 60 mA, 4s acquisition time

1 Hz

100 Hz

10000 Hz

50000 Hz



- No effect of the frequency on the amplitude of the magnetic flux
- Decrease of the amplitude of the fringes (vibration ?)
- Limitation of the electrical contacts, sample holder and source meter



# Spin configurations in size controlled single Fe nanomagnets

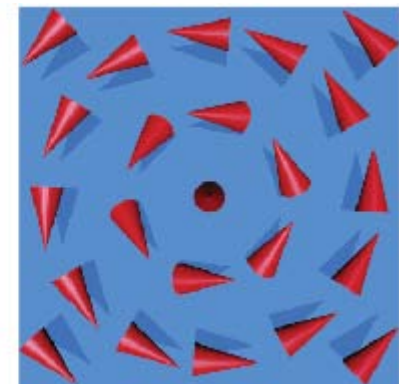
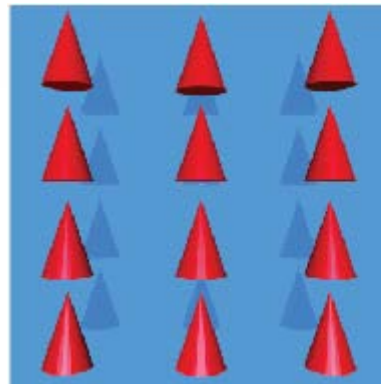
Magnetic configuration depends on the energy minimization considering:

- the magneto-crystalline anisotropy
- the exchange constant
- the magneto-static energies

3 typical configurations in a magnetic material as a function of the size at the remnant state:

- Multidomain state: adjacent domains with magnetic walls
- Vortex (V) state: external spins rotate to achieve a flux closure, while in the vortex core, spins tilt out-of-plane
- Single-domain (SD) configuration : uniform arrangement of magnetic moments

Size  $\searrow$

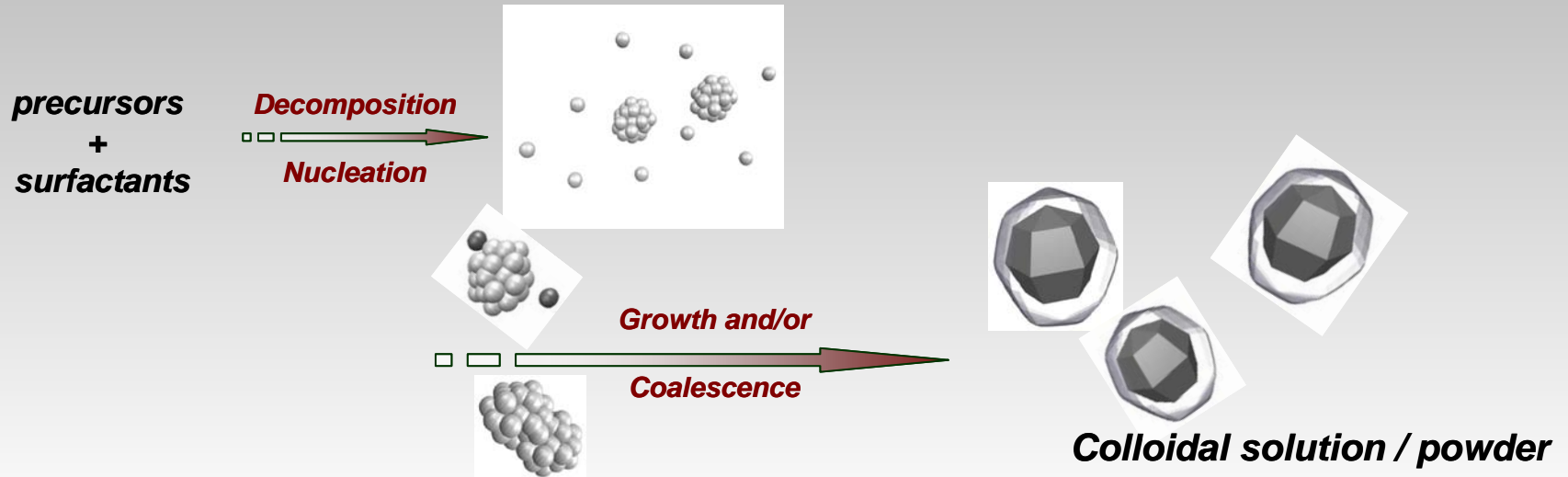


→ Size  $\searrow$

# Spin configurations in size controlled single Fe nanomagnets

Need of model objects for the study of magnetic transition as a function of the size

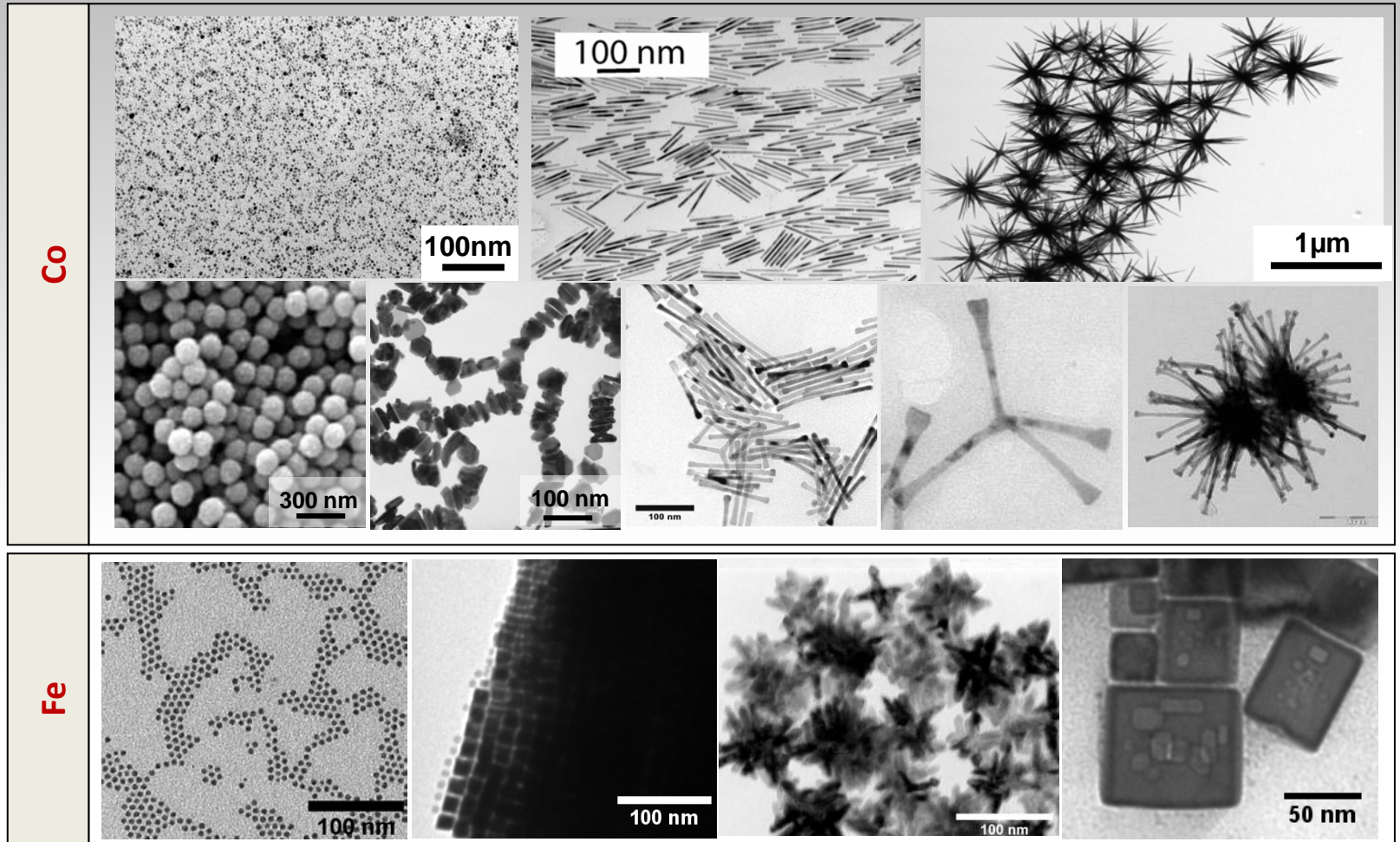
=> Nanoparticles synthesized in liquid phase by organometallic chemistry



- Shape and size control through the reaction conditions : ligands, temperature, products concentration... => Spherical NPs, nanocubes, nanorods, multipods,...
- The surfactants control the nucleation and growth steps, and prevent the coalescence of the nanocrystals.
- Defect-free nanomagnets with controlled and reproducible magnetic properties allow accurate modeling and comparison with experimental investigations.

# Spin configurations in size controlled single Fe nanomagnets

## Examples for Co and Fe nanoparticles

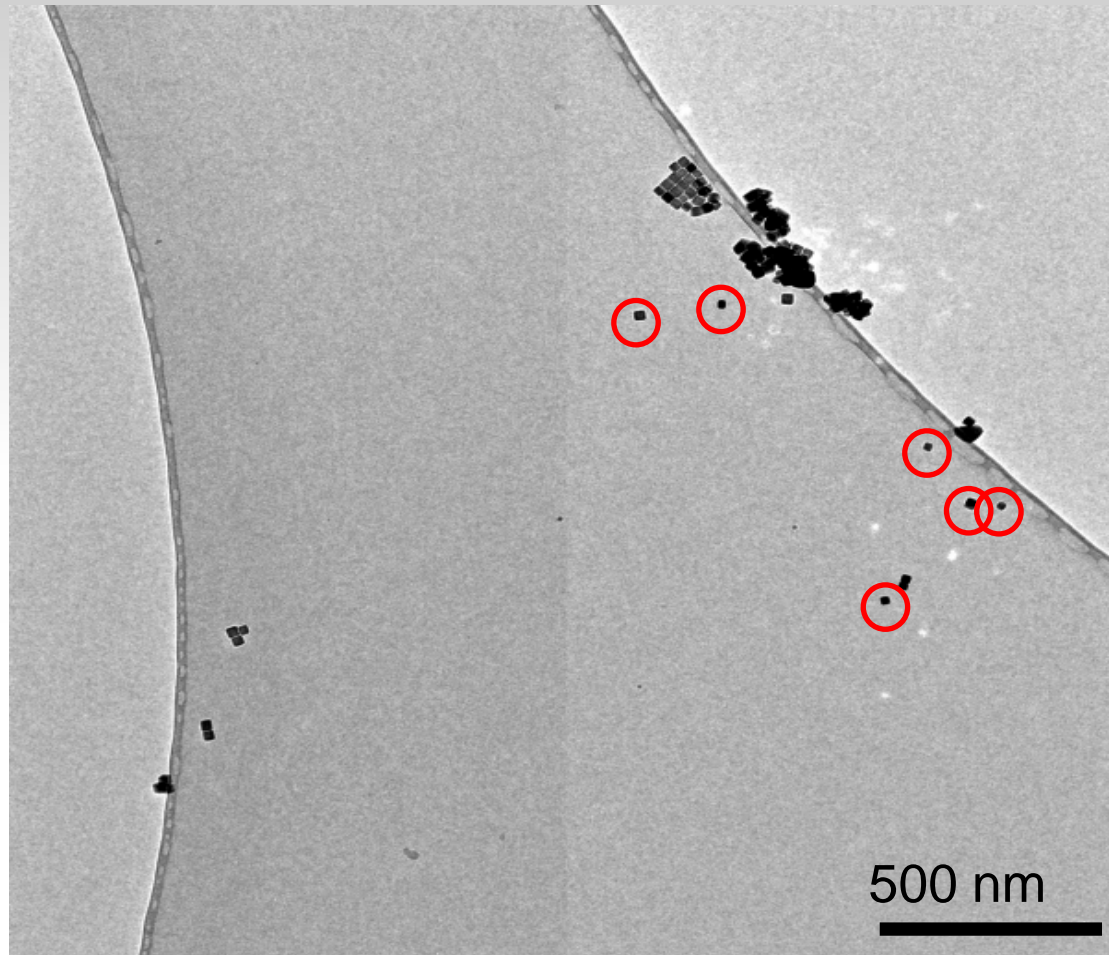


# Spin configurations in size controlled single Fe nanomagnets

To study the Vortex -> Modomain transition, 3 issues have to be solved:

- Isolated nano-objects are mandatory to prevent any artefacts in the transition determination such as dipolar interactions

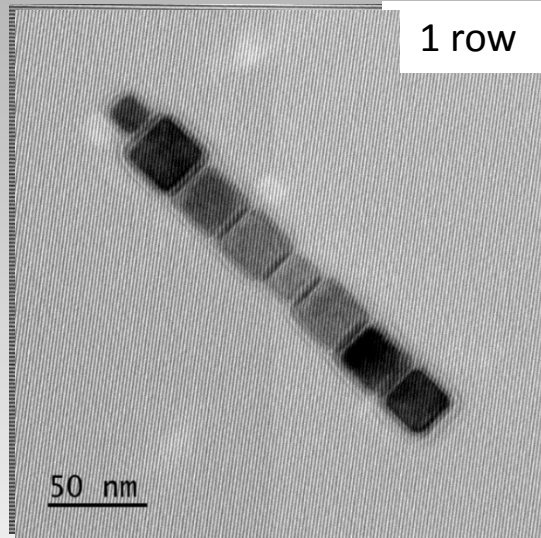
**=> Need to find isolated magnetic particles**



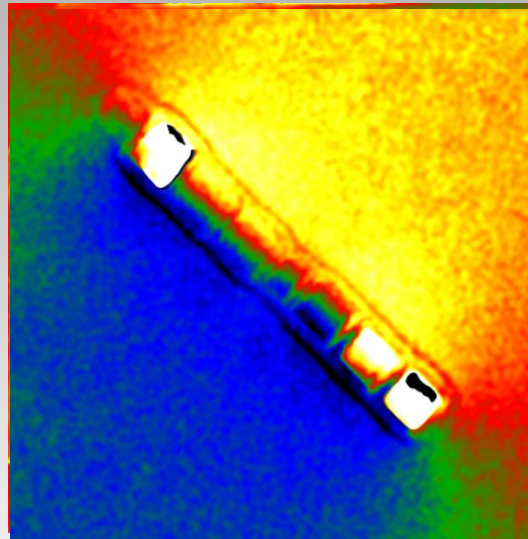


# Spin configurations in size controlled single Fe nanomagnets

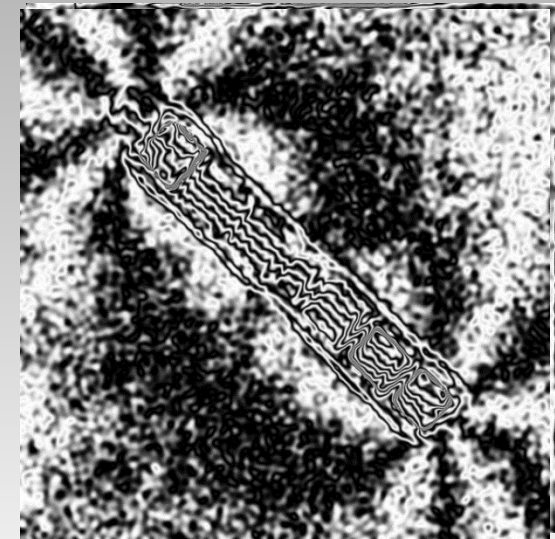
Several configurations of nanocubes: Study of their dipolar interactions



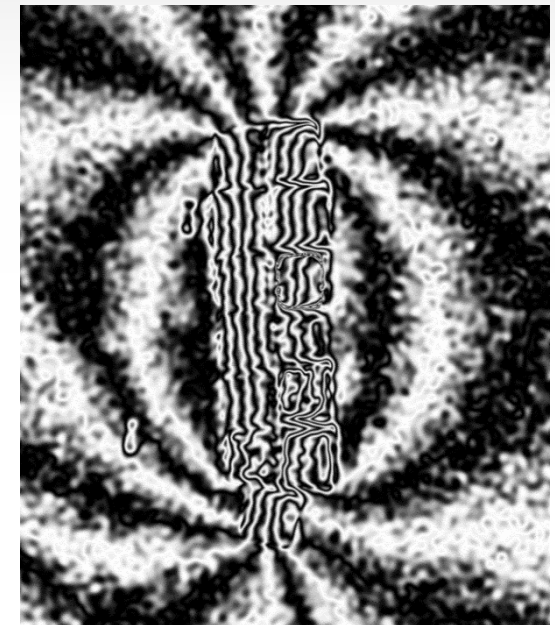
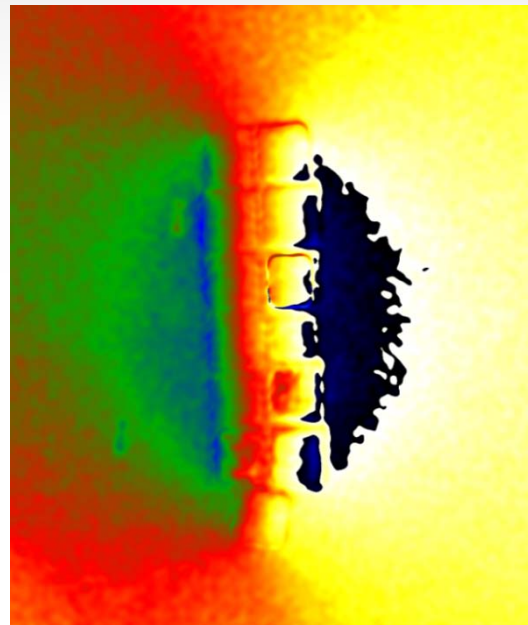
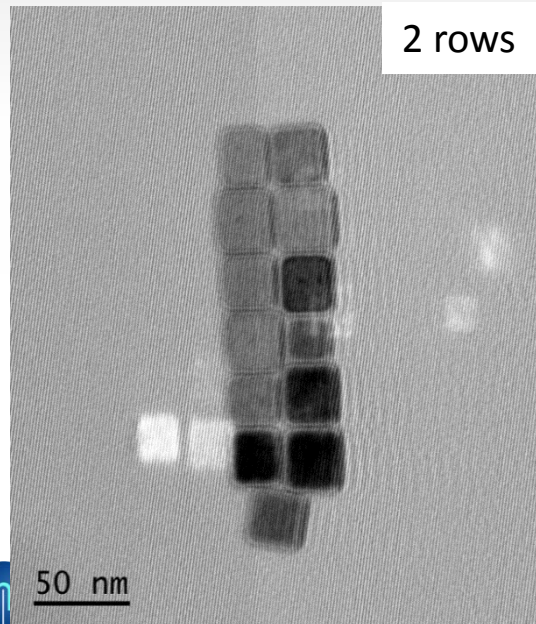
Hologram



Magnetic Phase Shift

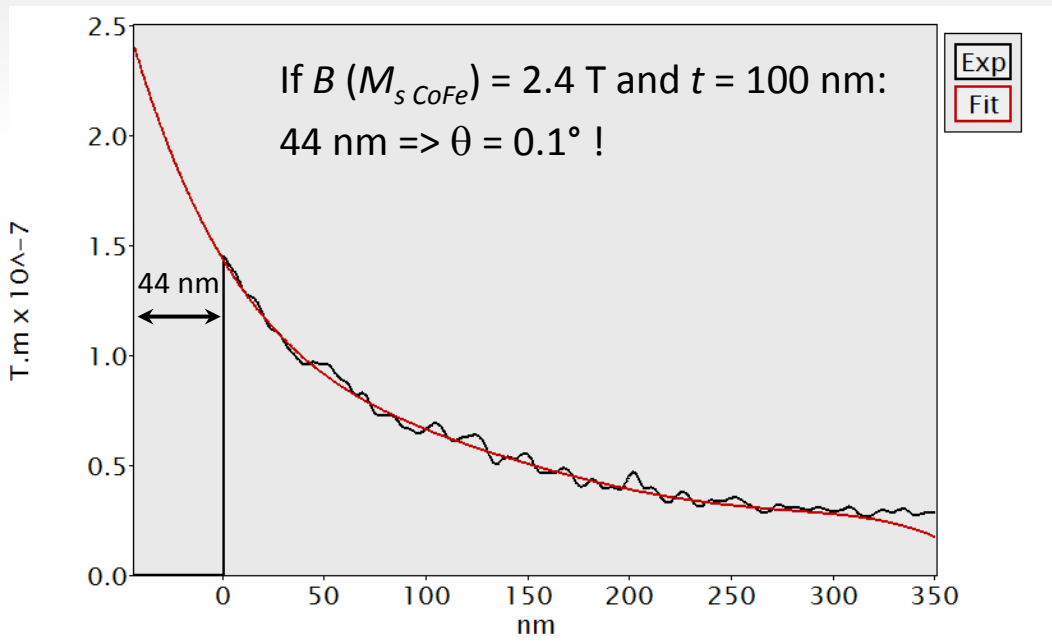
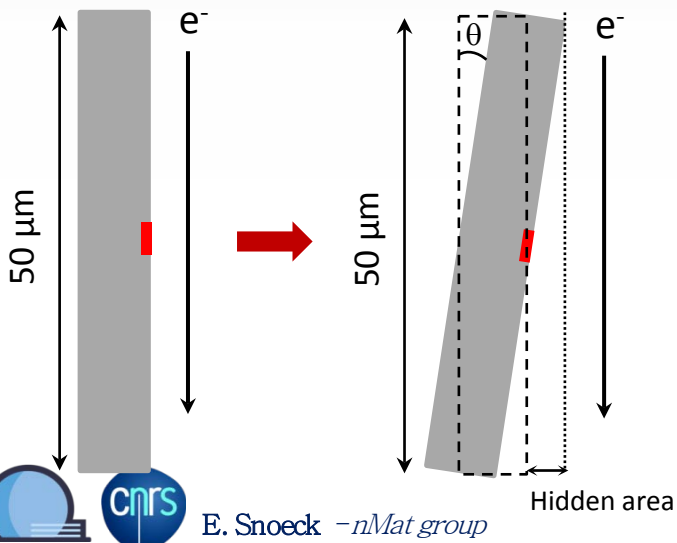
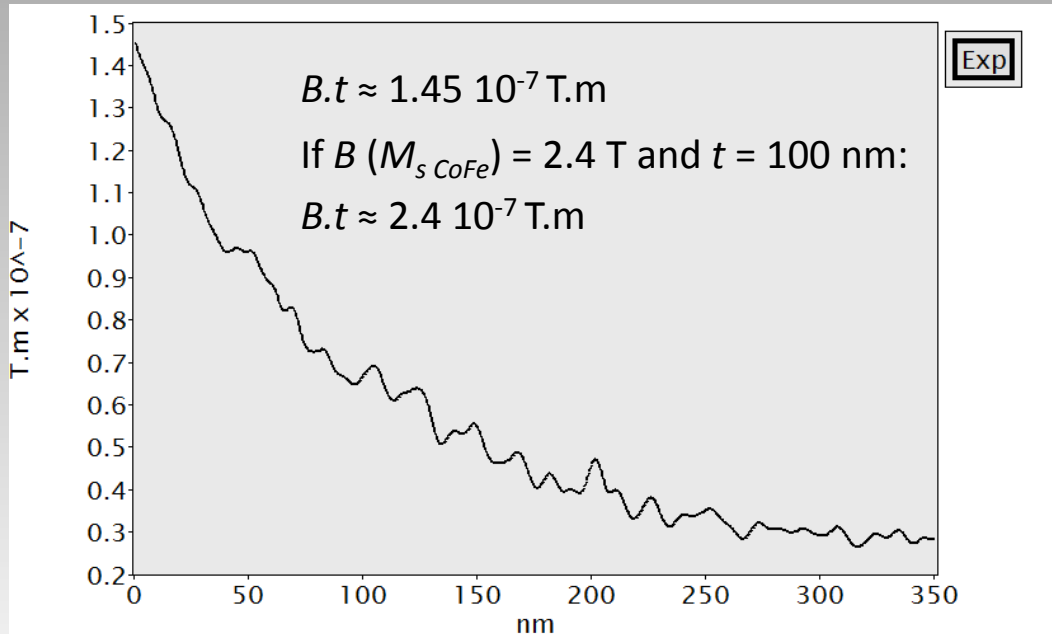
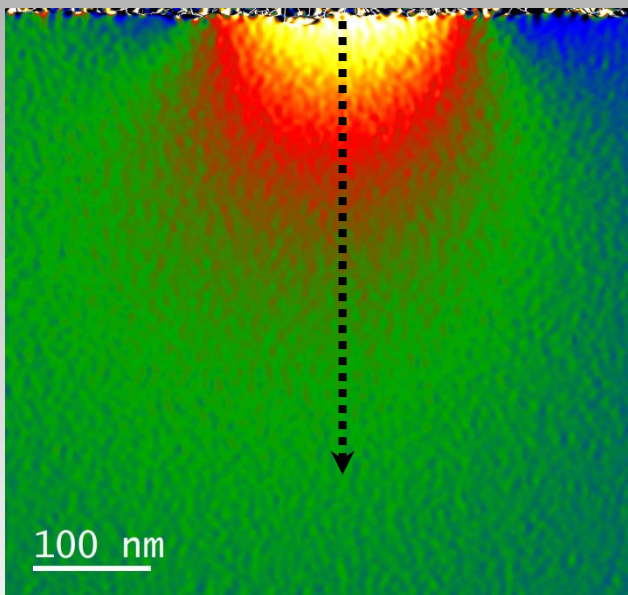


Cosine of Magnetic Phase



# Induction profile and tilt problem

Y component, D dataset, -60 mA



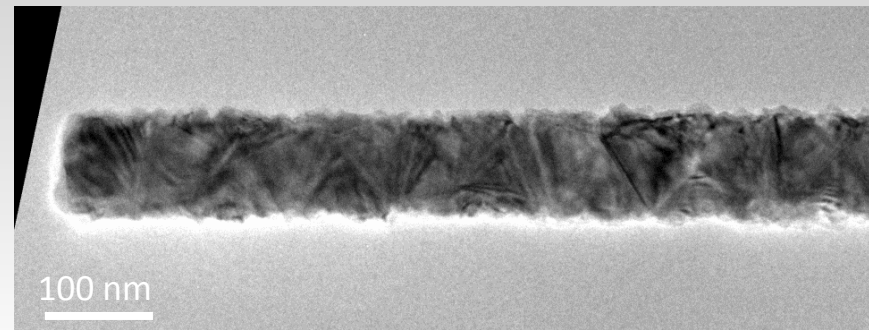
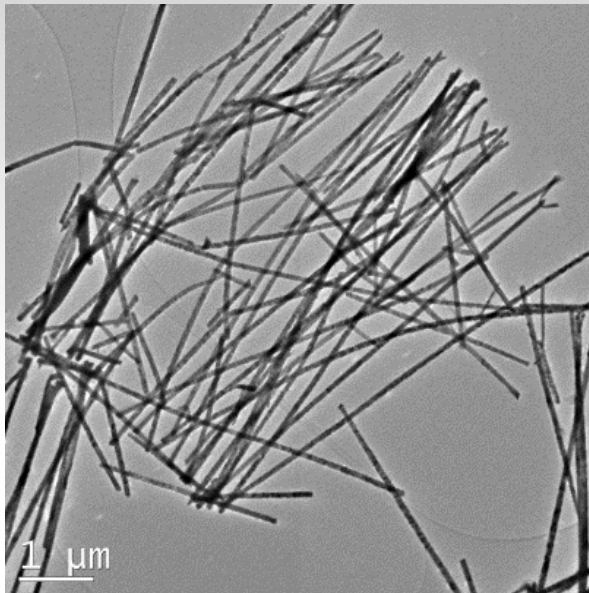
# Domain wall imaging in Ni Nanowire

- Studying transition between vortex to transverse walls as a function of diameter
- Concept of « massless » DW [1,2]

Cylindrical symmetry => High propagation velocity of TW

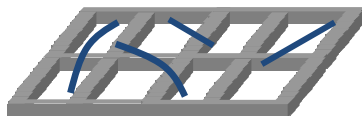
=> Interest for spintronic logic devices

- Very few experimental observations of DW in cylinders

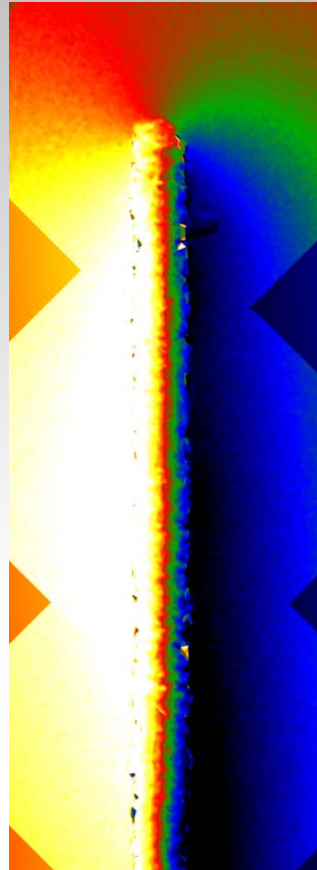
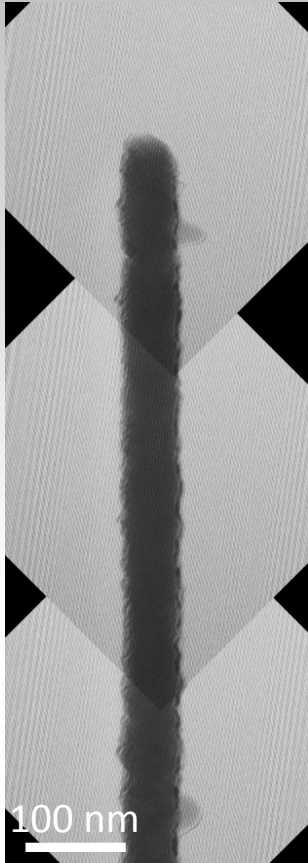


- Electro-deposition in commercial Poly-Carbonate (PC) membranes Polycrystalline nanocylinder
- Easy and low cost
- Mean diameter : 50, 80 or 110 nm
- Hundreds of nanowires on a TEM grid

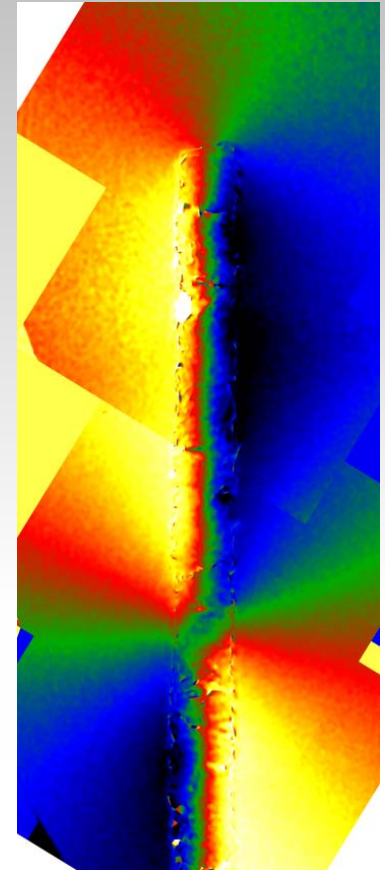
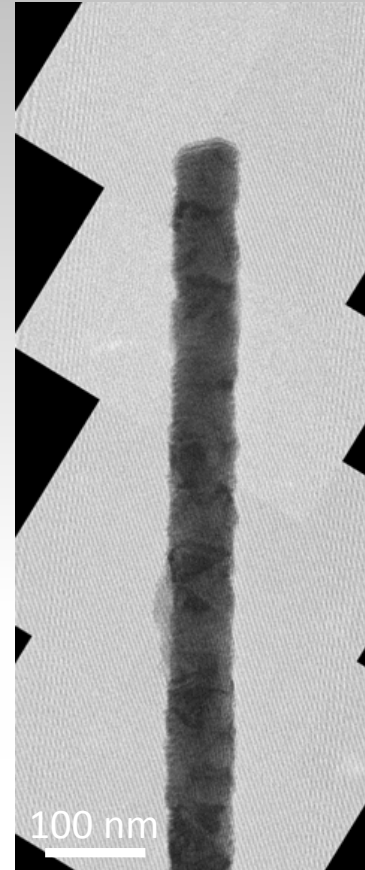
$$\mu_0 H_0 = 1T$$



Without DW



With DW



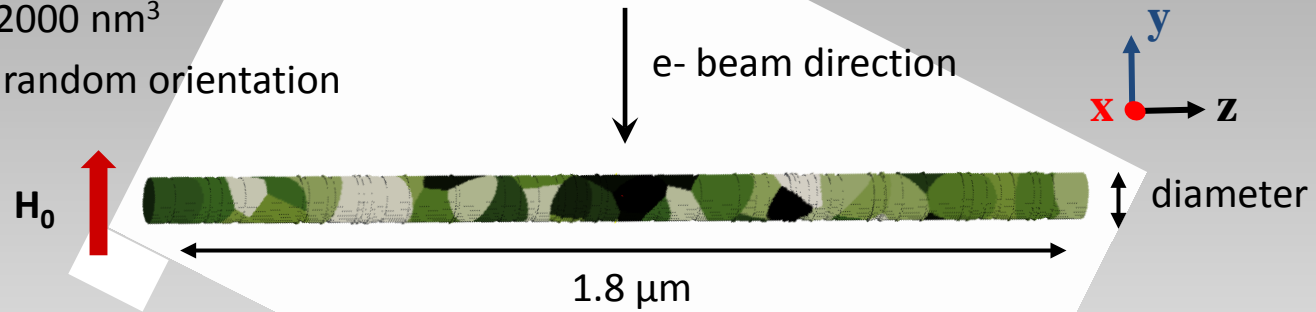
Local field lines outside the nanowire + asymmetry inside  
=> Presence of a DW

# Domain wall imaging in Ni Nanowire

3D OOMMF software: Cell size  $2.5 \times 2.5 \times 2.5 \text{ nm}^3$

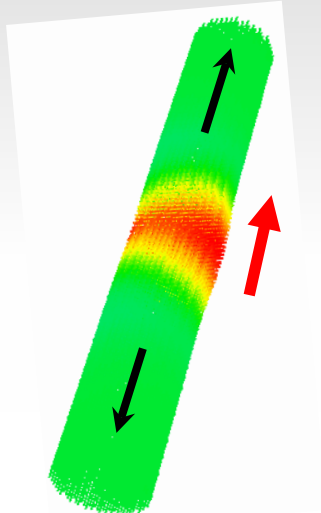
Universe size  $500 \times 500 \times 2000 \text{ nm}^3$

Generation of grains with random orientation

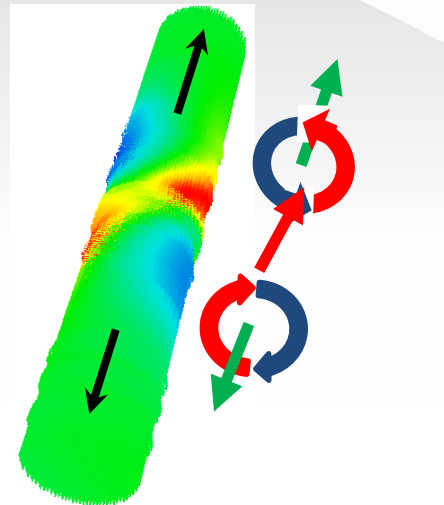


$M_y$  component

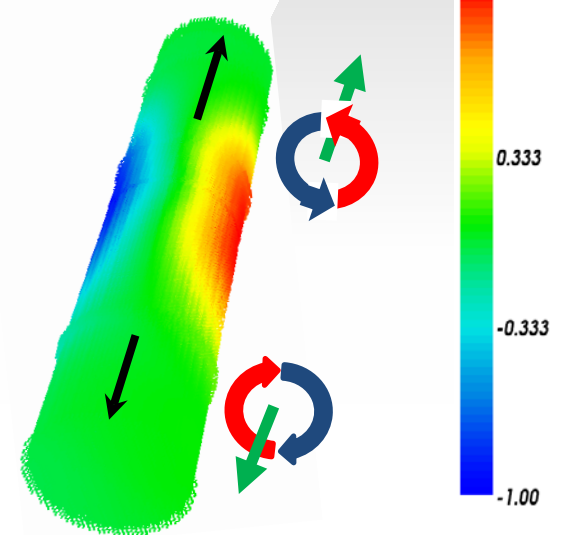
$\phi = 48 \text{ nm}$



$\phi = 85 \text{ nm}$



$\phi = 92 \text{ nm}$



Tranverse

Hybrid

Vortex

diameter

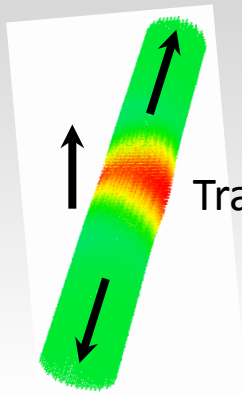
# Domain wall imaging in Ni Nanowire

Phase

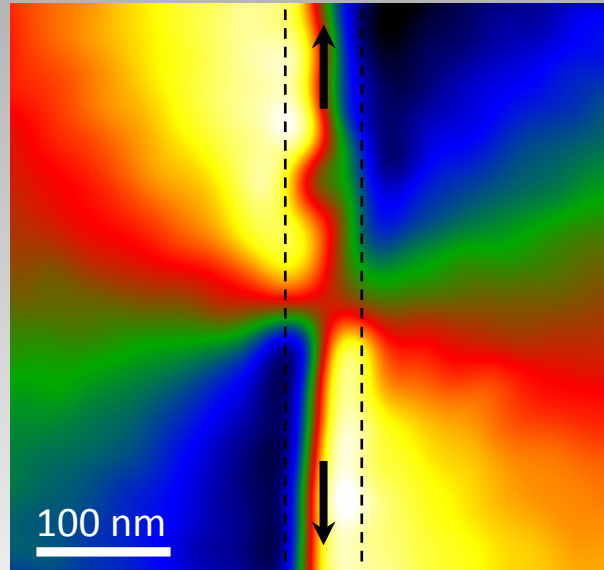
Cos(phase)

Experimental phase

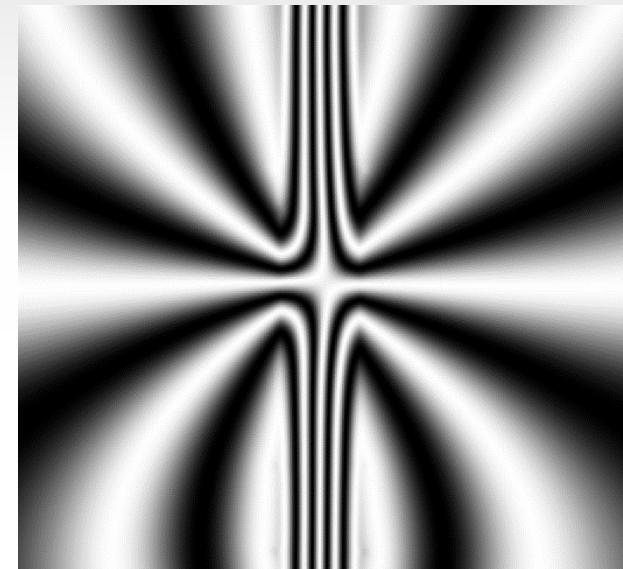
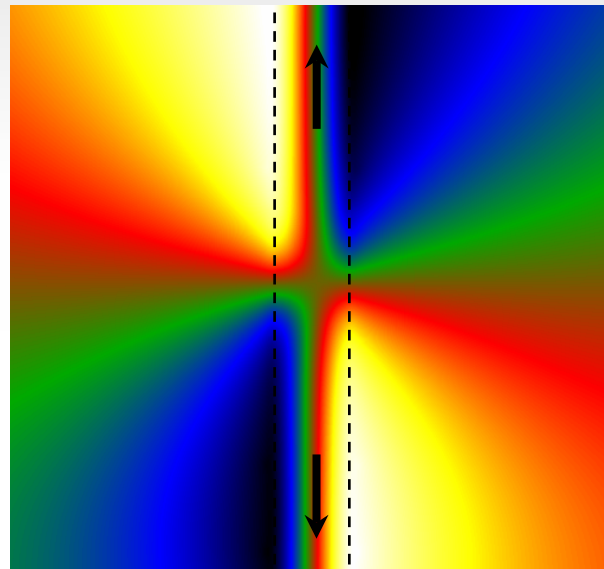
Diameter = 55 nm



Transverse wall



Simulated phase



Very good agreement between simulation and experiments

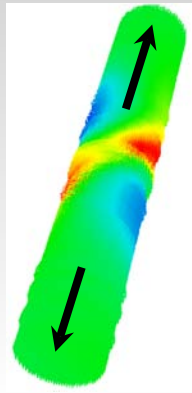
# Domain wall imaging in Ni Nanowire

Phase

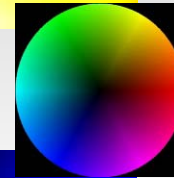
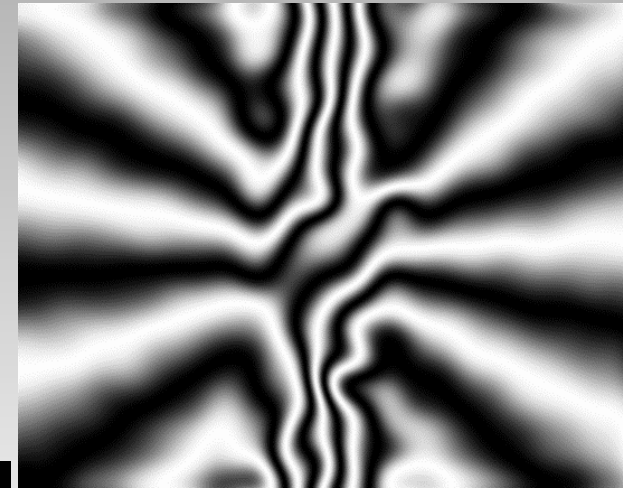
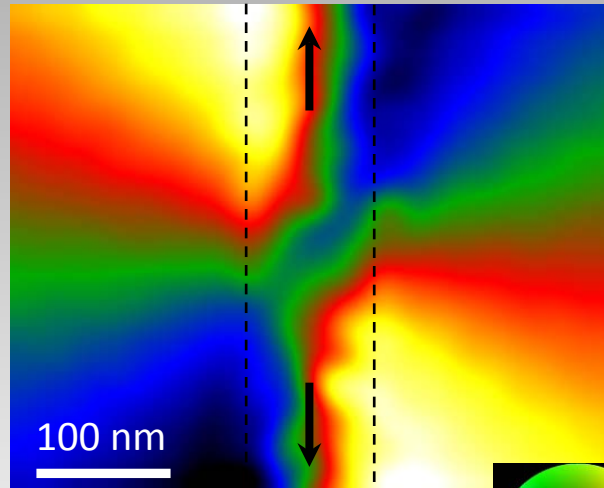
$\text{Vec}(\cos(\alpha))$

Experimental phase

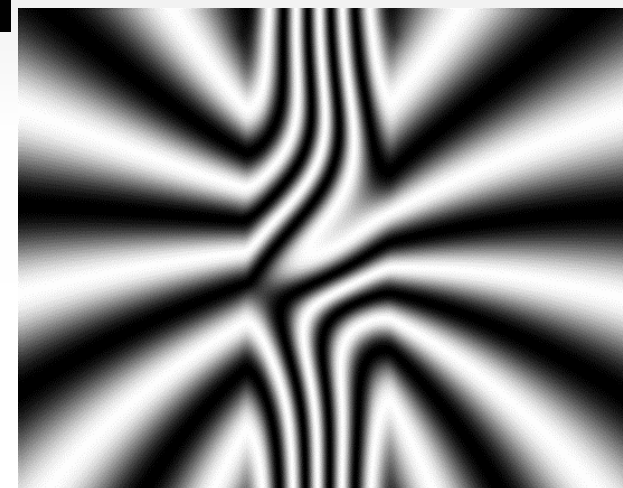
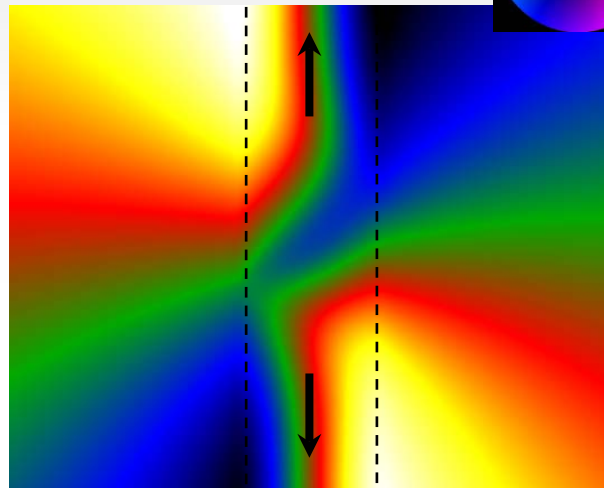
Diameter = 85 nm



Hybrid wall

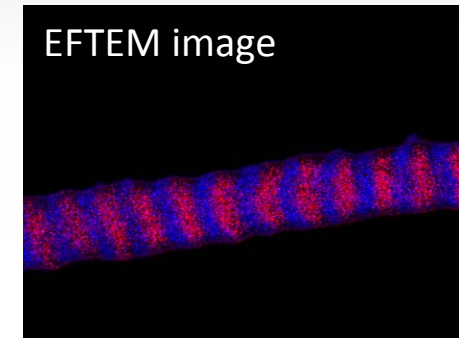
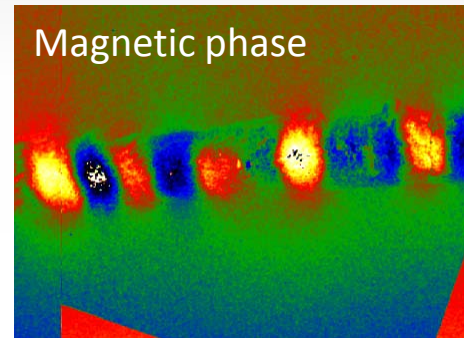
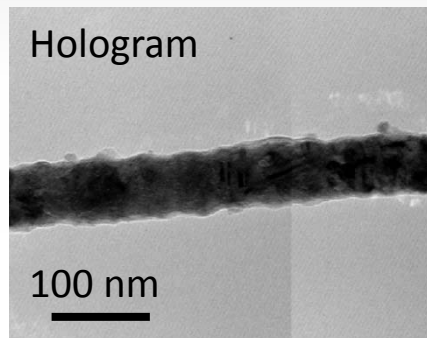


Simulated phase



Very good agreement between simulation and experiments

- Need to combine experimental phase and micromagnetic simulations  
=> Determination of the magnetic configuration inside nano-objets
- New Hitachi I2TEM => Study of Fe Nanocubes (and other particles) with smaller dimensions. Next step: Study of the superparamagnetic transition
- Magnetic transition: function of the size, but possibility to change the temperature, to inject a current
- For nanowires: different domain walls have been observed. In future, study of nanowires with Co/Cu multilayers



Special acknowledgments to ESTEEM2 Project  
and MIMETIS Equipex

E. Snoeck - *nMat* group





# I2TEM: Spatial Resolution

Observation modes	Aberration	Stage	Focusing	Cs	Cc	Resolution	Mag. at SA	Dark field
OBJ off observation Lorentz mode	Uncorrected	Standard	Int 1	770 mm	50 mm	1.0 nm	-	NA
	Corrected (Aplanatic)	Standard	TL11	0 mm	164 mm	0.56 nm	8.8	NA
Double stage (single focus Lorentz mode)	Uncorrected	Upper	Objective (weak)	3.2 m	63 mm	1.43 nm	3.8	NA
	Corrected (Aplanatic)	Upper	Objective (weak)	0 m	115 mm	0.48 nm		
Double stage (double focus Lorentz mode)	Uncorrected	Upper	Objective (strong)	241 m	1.1 m	4.2 nm	4.1	Available
	Corrected (Aplanatic)	Upper	Objective (strong)	0 m	1.7 m	1.8 nm	3.8	Available
High resolution mode	Uncorrected	Standard	Objective	2.3 mm	2.4 mm	0.24 nm	61	Available
	Corrected (Aplanatic)	Standard	Objective	0 mm	3.7 mm	0.084 nm	99 (Changeable)	Available

Accelerating voltage : 300kV  
Pole piece : Wide gap

- ✓ 3 corrected Lorentz mode
- ✓ Various resolution and object magnification on the hologram
- ✓ 0.8A resolution in standard mode despite wide pole piece gap

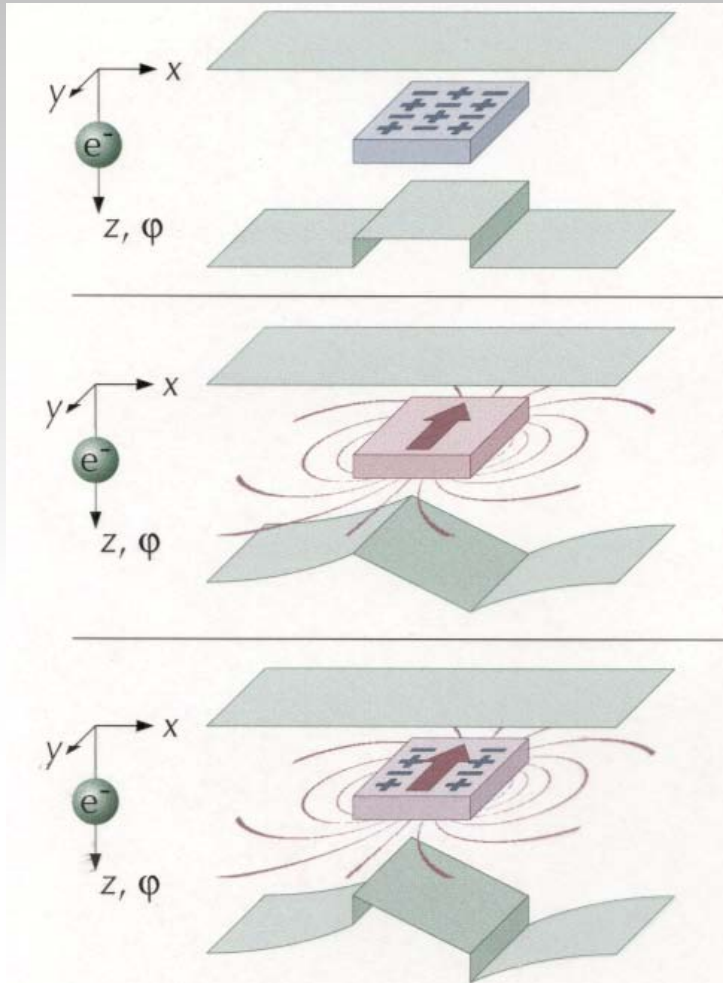
# Aharonov-Bohm effect: Phase shift of the beam due to the electromagnetic field

W. Ehrenberg, R.E. Siday, *Proc. Phys. Soc.* **B62**, 8 (1949)

Y. Aharonov, Y. D. Bohm, *Phys. Rev.* **115**, 485 (1959)

Y. Aharonov, Y. D. Bohm, *Phys. Rev.* **123**, 1511 (1961)

A. Tonumora *et al.*, *Phys. Rev. Letter* **48**, 1443 (1982)



Phase shift introduced by the local electrostatic potential

$$\phi_{MIP, Elec}(\mathbf{R}) = C_E \int V(\mathbf{r}) dz$$

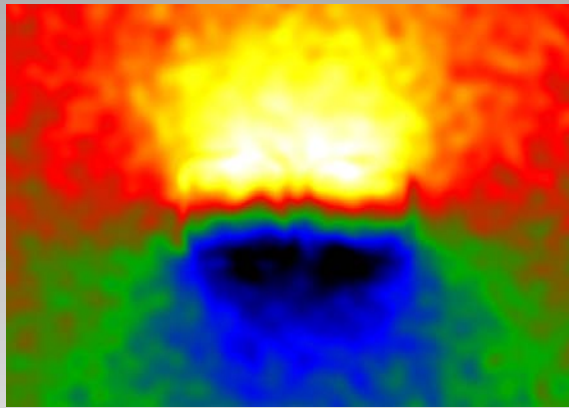
Phase shift introduced by the magnetic field

$$\begin{aligned} \phi_{Mag}(\mathbf{R}) &= -\frac{e}{\hbar} \int A_z(\mathbf{r}, z) dz \\ &= -\frac{e}{\hbar} \iint \mathbf{B}_R(\mathbf{R}_\perp, z) dR dz \end{aligned}$$

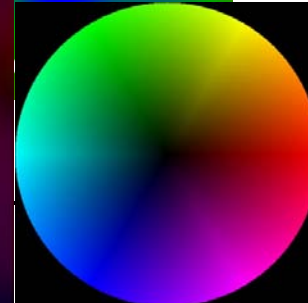
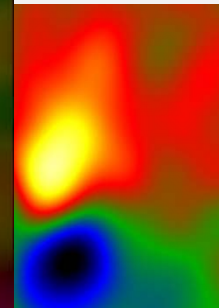
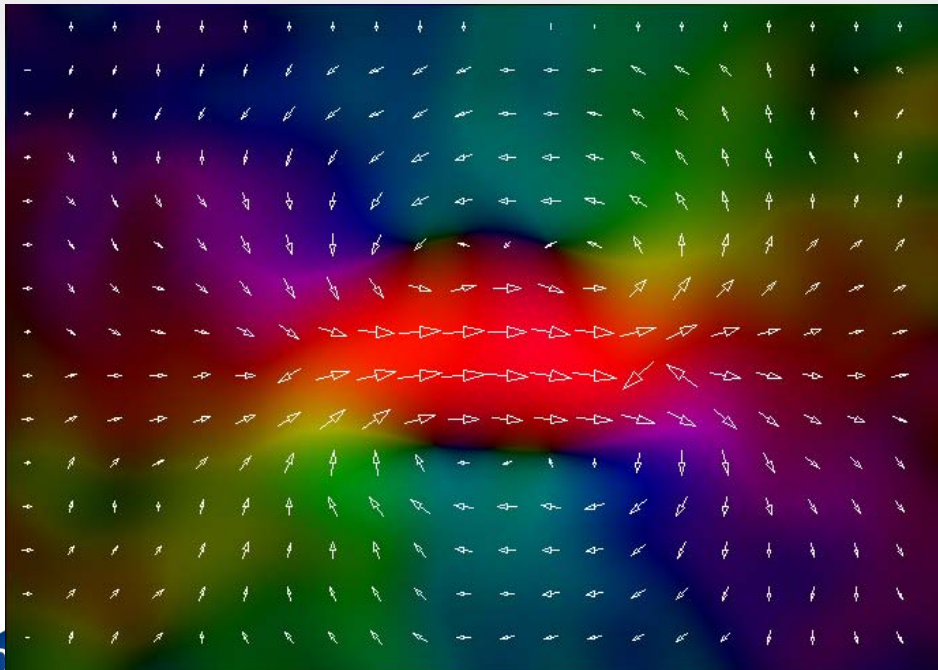
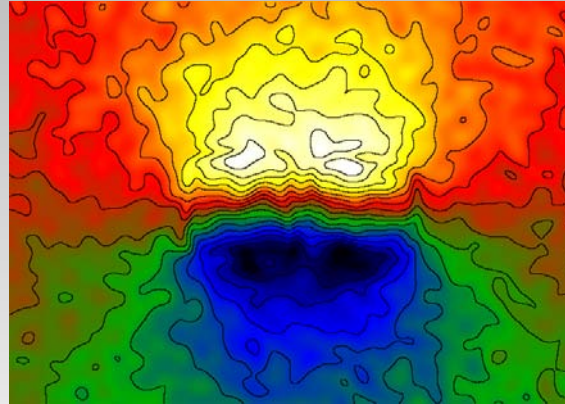
Total phase shift

$$\phi_{Total}(\mathbf{R}) = \phi_{MIP, Elec}(\mathbf{R}) + \phi_{Mag}(\mathbf{R})$$

*Integration of the projected potential*

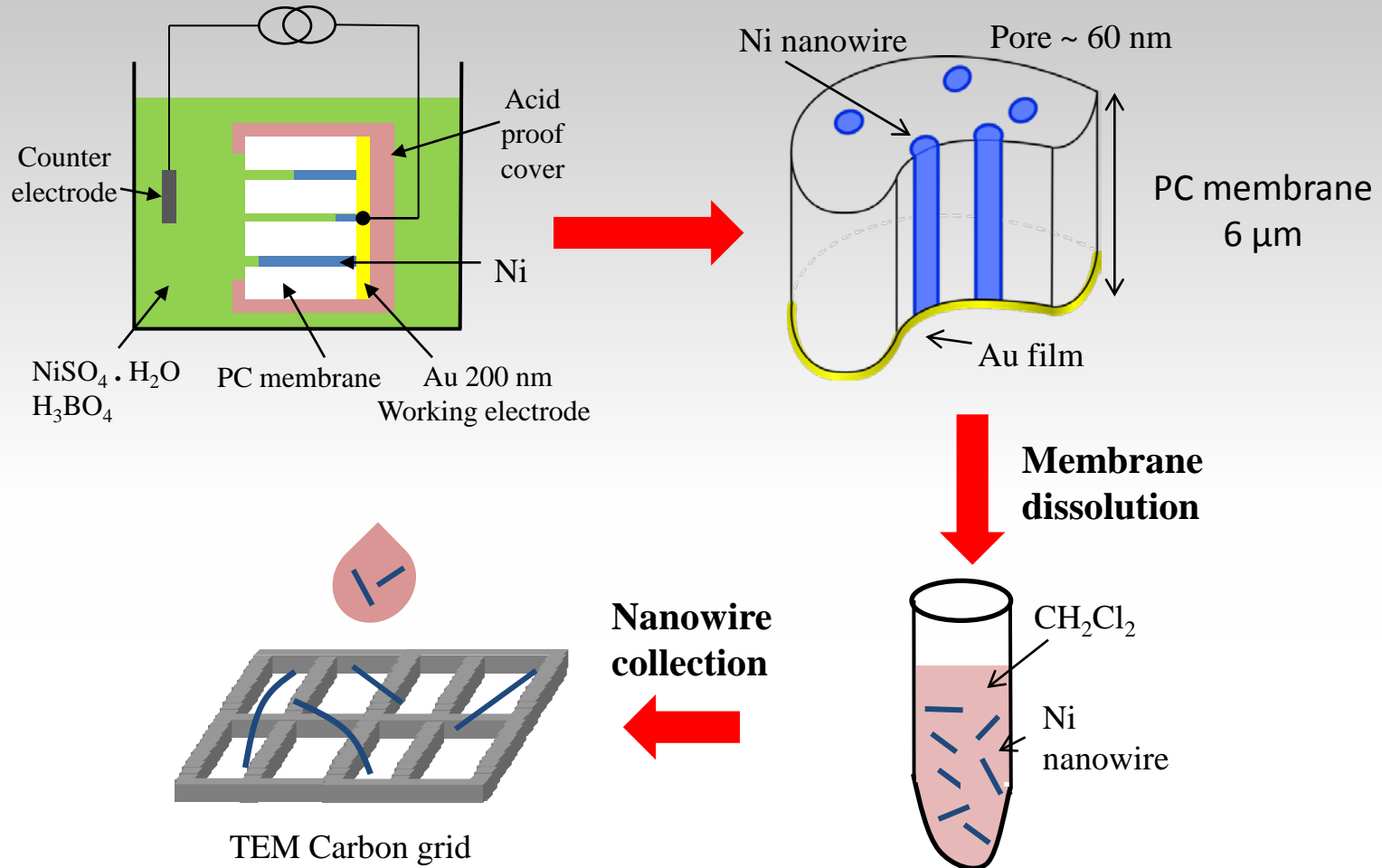


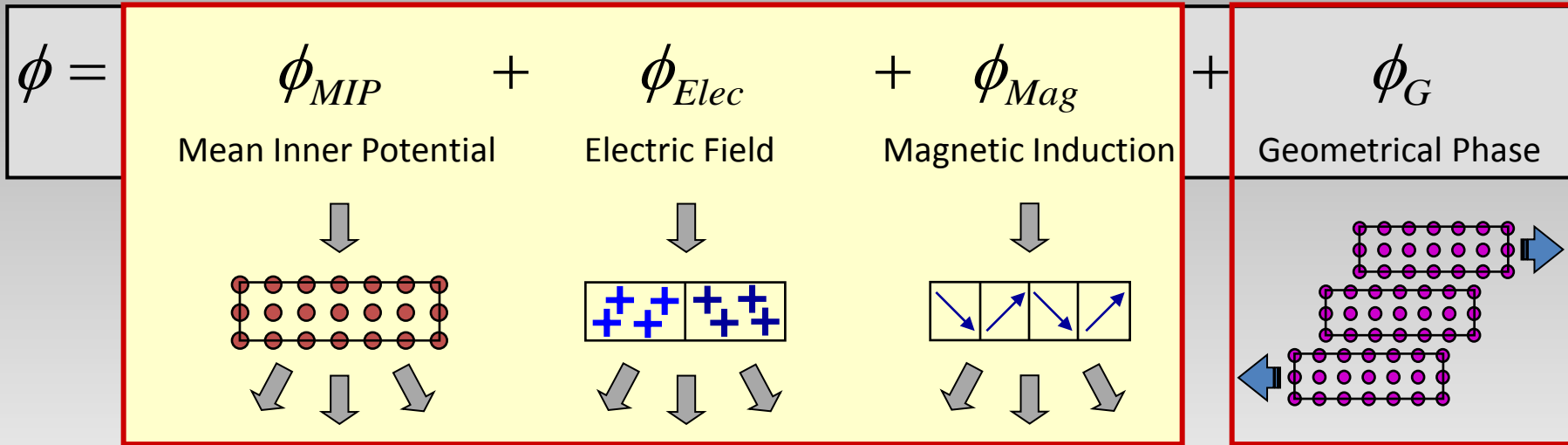
- Phase gradient proportional to the component in the plane of  $\mathbf{B}$   
=> Isophase contours correspond to B direction



- Only planar induction can be studied !
- Complicated data treatment

## Electro-deposition in commercial Poly-Carbonate (PC) membranes



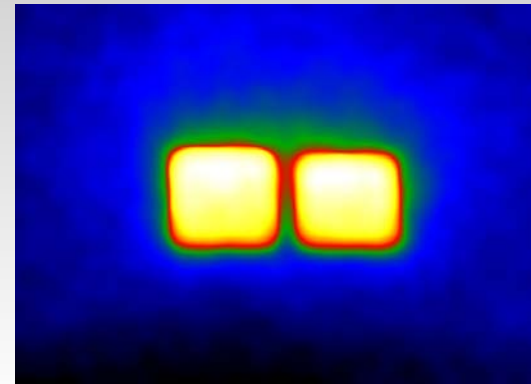
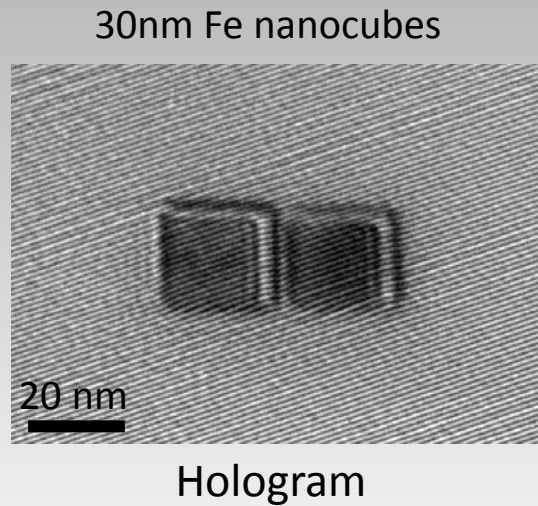


$$\phi_{MIP}(\mathbf{R}) = C_E \int V_{MIP}(\mathbf{r}) dz \quad \text{with} \quad C_E = \left( \frac{2\pi}{\lambda} \right) \left( \frac{E + E_0}{E(E + 2E_0)} \right)$$

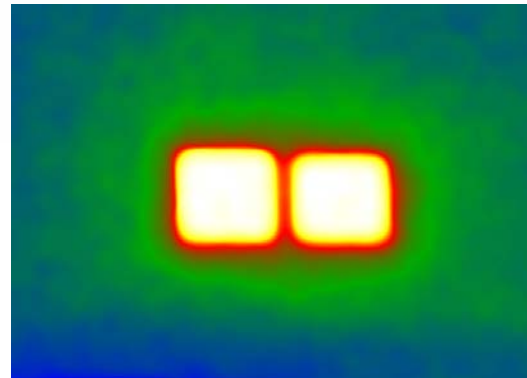
$$\phi_{Elec}(\mathbf{R}) = C_E \int V_{Elec}(\mathbf{r}) dz = C_E \iint E(\mathbf{r}) dS \quad (\text{Samples with charges or Ferroelectric materials})$$

$$\phi_{Mag}(\mathbf{R}) = -\frac{e}{\hbar} \int A_z(\mathbf{r}, z) dz = -\frac{e}{\hbar} \iint \mathbf{B}_R(\mathbf{R}_\perp, z) dR dz \quad (\text{Aharonov-Bohm effect})$$

For  $\phi_G$  : peculiar case due to the periodic arrangement of atoms

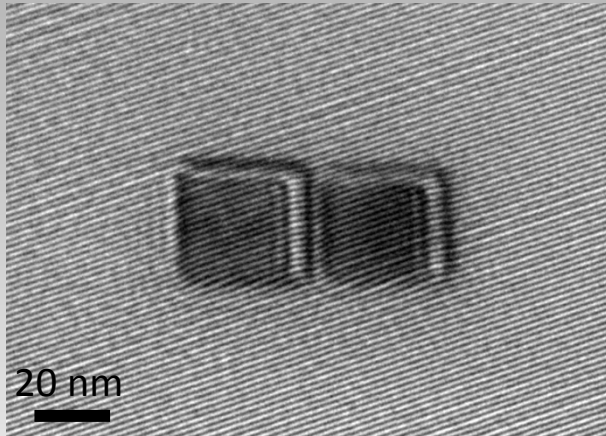


- Different methods to separate the contributions
- Need to record many holograms



$$\phi_{MIP, Elec}(\mathbf{R}) = C_E \int V(\mathbf{r}) dz \quad \phi_{Mag}(\mathbf{R}) = -\frac{e}{h} \iint \mathbf{B}_R(\mathbf{R}_\perp, z) dR dz$$

30nm Fe nanocubes

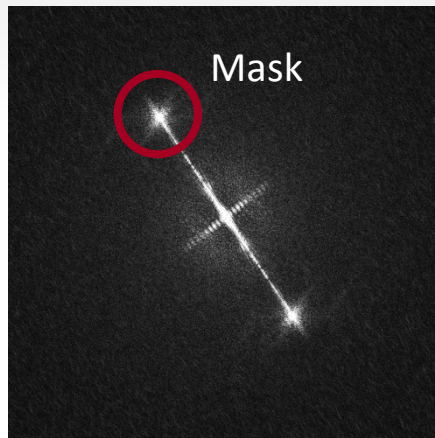


Hologram Image

Interference between a reference wave and the wave through the sample



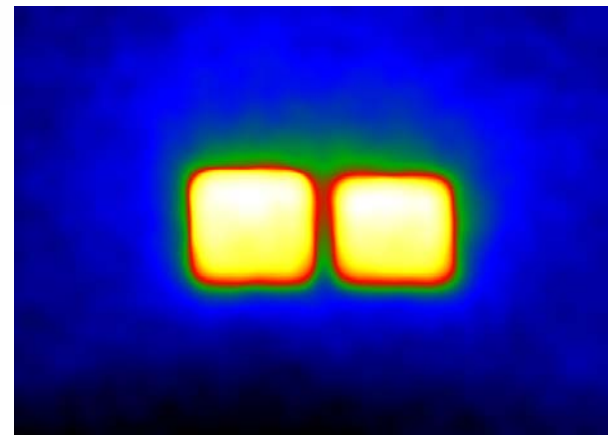
FFT



FFT<sup>-1</sup>



Amplitude image



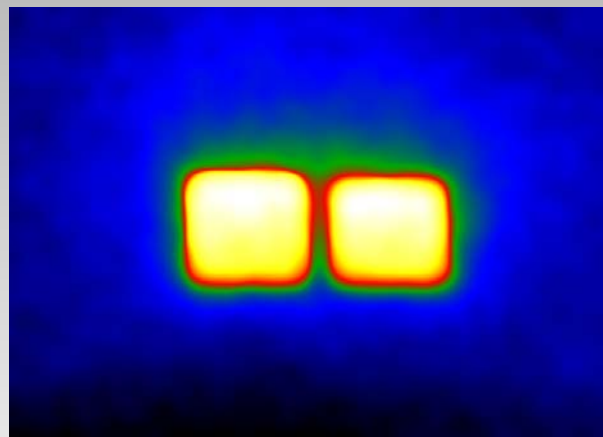
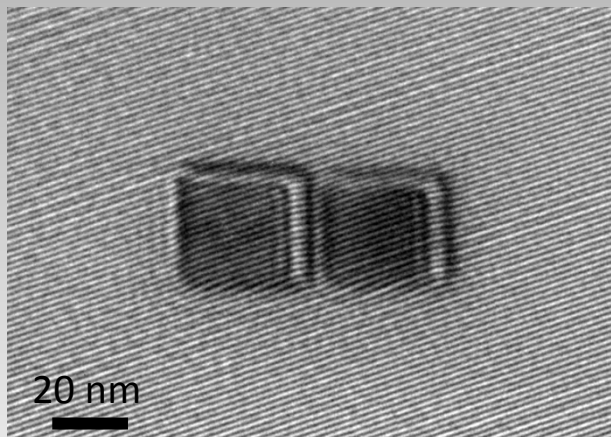
Phase image



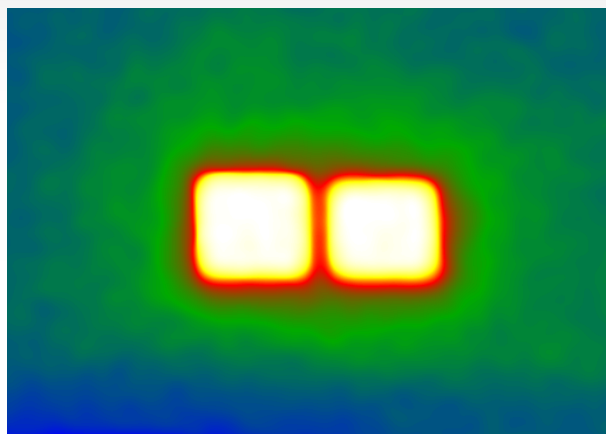
# Phase shift extraction and different contributions

30nm Fe nanocubes

$$\phi(\mathbf{R}) = \phi_{MIP,Elec}(\mathbf{R}) + \phi_{Mag}(\mathbf{R})$$



- Different methods to separate the contributions
- Need to record many holograms



$$\phi_{MIP,Elec}(\mathbf{R}) = C_E \int V(\mathbf{r}) dz$$



$$\phi_{Mag}(\mathbf{R}) = -\frac{e}{h} \iint \mathbf{B}_R(\mathbf{R}_\perp, z) dR dz$$

Incident beam

$$\psi_0 = \exp(i\mathbf{k}\cdot\mathbf{r})$$



After the sample

$$\psi(\mathbf{r}) = A(\mathbf{R}) \exp i((\mathbf{k}\cdot\mathbf{r}) + \phi(\mathbf{R}))$$



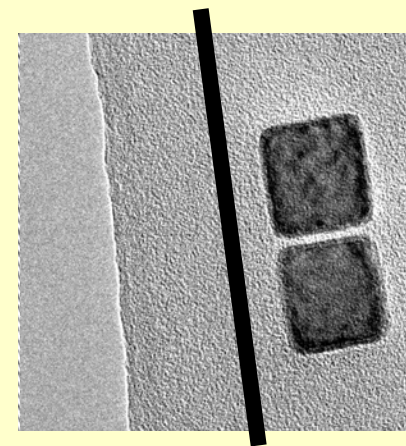
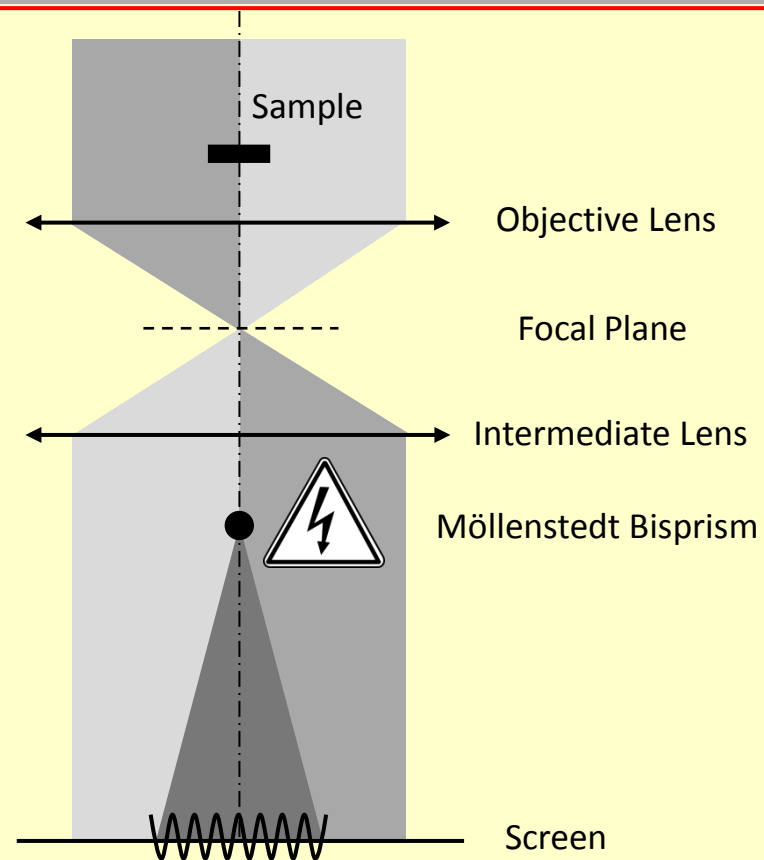
After the objective lens

$$\Psi(\mathbf{r}) = A_S(\mathbf{R}) \exp i((\mathbf{k}\cdot\mathbf{r}) + \phi_S(\mathbf{R}))$$

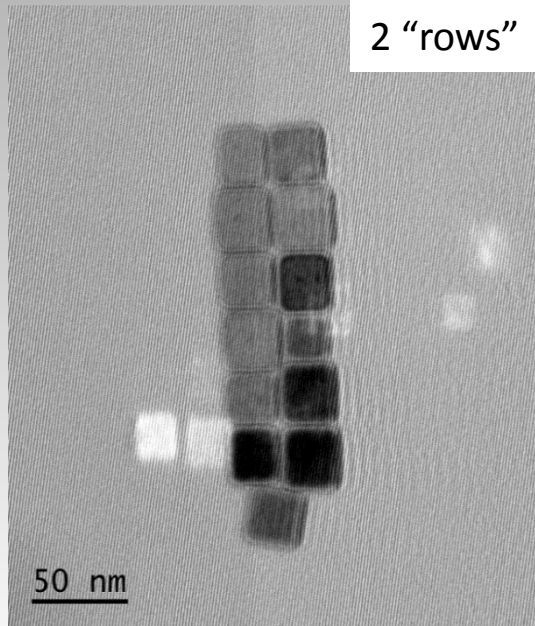
Image intensity

~~$I(\mathbf{R}) \propto |\Psi|^2 \propto A_S^2(\mathbf{R})$~~   $\rightarrow$   $\phi(\mathbf{R})$  is lost !

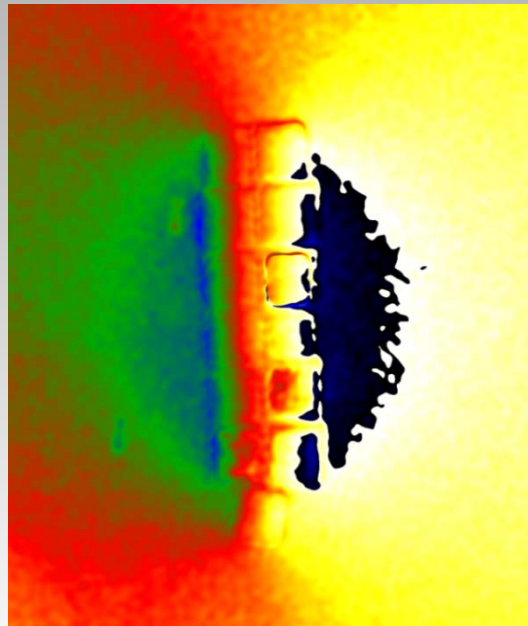
$$\begin{aligned}
 I_{Holo} &= |\Psi_0 + \Psi^*|^2 + \text{background} \\
 &= 1 + A_S^2(\mathbf{R}) \\
 &\quad + 2A_S(\mathbf{R}) \cdot \cos(2\pi R_0 \cdot x + \phi_S(\mathbf{R})) \\
 &\quad + I_{Inelast}(\mathbf{R})
 \end{aligned}$$



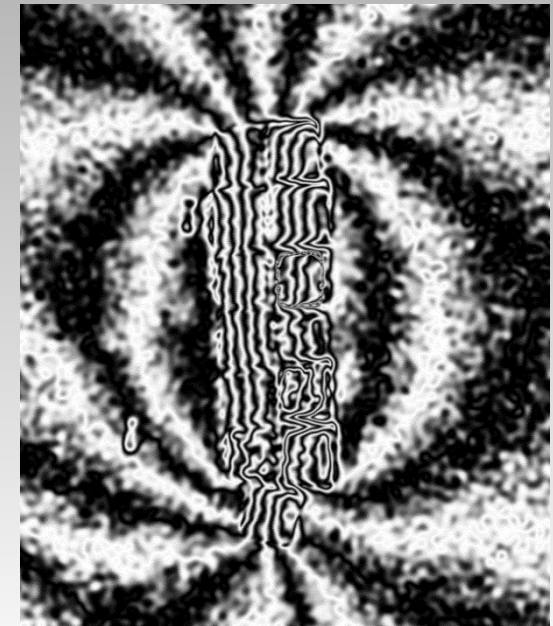
Several configurations of nanocubes: Study of their dipolar interactions



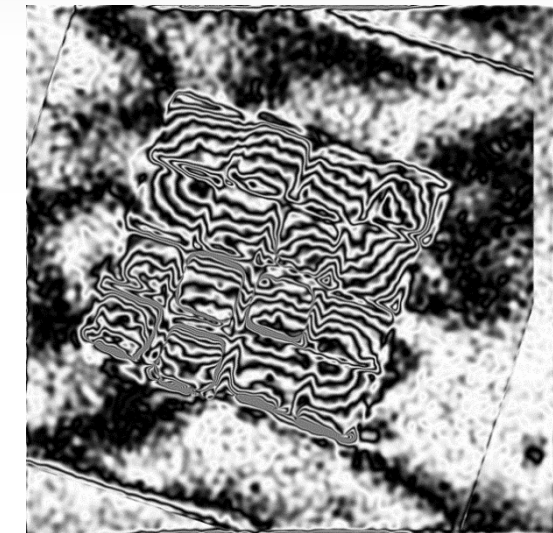
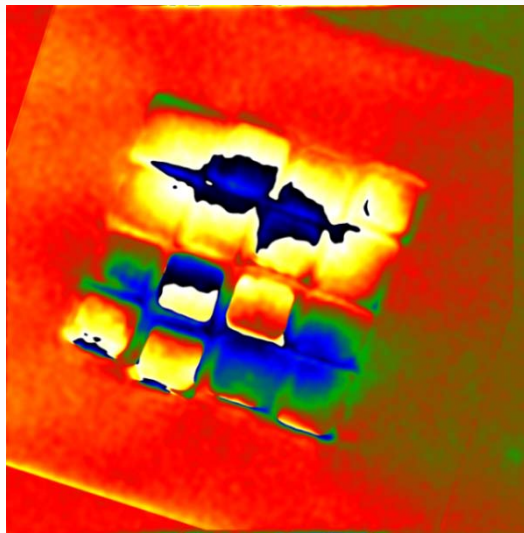
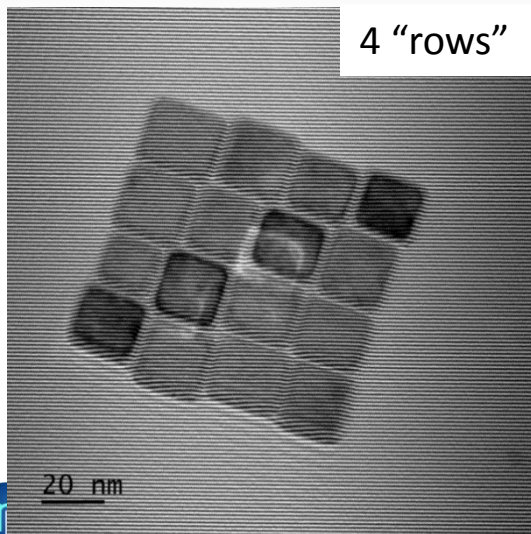
Hologram



Magnetic Phase Shift



Cosine of Magnetic Phase



Variation of the radiated regions located at 5 nm in front of the pole as a function of the applied current

Angular spread

