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The SUrvey for Pulsars and Extragalactic Radio Bursts – II. New FRB discoveries and their follow-up

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ABSTRACT

We report the discovery of four Fast Radio Bursts (FRBs) in the ongoing SUrvey for Pulsars and Extragalactic Radio Bursts at the Parkes Radio Telescope: FRBs 150610, 151206, 151230 and 160102. Our real-time discoveries have enabled us to conduct extensive, rapid multimessenger follow-up at 12 major facilities sensitive to radio, optical, X-ray, gamma-ray photons and neutrinos on time-scales ranging from an hour to a few months post-burst. No counterparts to the FRBs were found and we provide upper limits on afterglow luminosities. None of the FRBs were seen to repeat. Formal fits to all FRBs show hints of scattering while their intrinsic widths are unresolved in time. FRB 151206 is at low Galactic latitude, FRB 151230 shows a sharp spectral cut-off, and FRB 160102 has the highest dispersion measure (DM = 2596.1 \pm 0.3 pc cm−3) detected to date. Three of the FRBs have high dispersion measures (DM > 1500 pc cm⁻³), favouring a scenario where the DM is dominated by contributions from the intergalactic medium. The slope of the Parkes FRB source counts distribution with fluences >2 Jy ms is $\alpha = -2.2^{+0.6}_{-1.2}$ and still consistent with a Euclidean distribution ($\alpha = -3/2$). We also find that the all-sky rate is $1.7^{+1.5}_{-0.9}$ × 10³FRBs/(4 π sr)/day above ∼2 Jy ms and there is currently no strong evidence for a latitude-dependent FRB sky rate.

Key words: radiation mechanisms: general – methods: data analysis – methods: observational – surveys – intergalactic medium – radio continuum: general.

1 INTRODUCTION

High-time resolution studies of the radio Universe have led to the discovery of Fast Radio Bursts (FRBs). First seen in 2007 in archival Parkes radio telescope data (Lorimer et al. 2007), FRBs have dispersion measures (DMs) which can exceed the Milky Way contribution by more than an order of magnitude (Petroff et al. 2016) and typically have durations of a few milliseconds. In the past couple of years, the discovery rate has accelerated – including those reported here, there are now 31 FRBs known – which include discoveries from the Green Bank Telescope (GBT), the Parkes radio telescope, the Arecibo Observatory, the upgraded Molonglo synthesis telescope (UTMOST) and the Australian SKA Pathfinder (Lorimer et al. 2007; Keane et al. 2012; Thornton et al. 2013; Burke-Spolaor & Bannister 2014; Spitler et al. 2014; Masui et al. 2015; Petroff et al. 2015a, 2017; Ravi, Shannon & Jameson 2015; Champion et al. 2016; Keane et al. 2016; Ravi et al. 2016; Caleb et al. 2017; Bannister et al. 2017).

The origin of these bursts is currently unknown, with leading theories suggesting giant flares from magnetars (Thornton et al. 2013; Pen & Connor 2015), compact objects located in young expanding supernovae (Connor, Sievers & Pen 2016; Piro 2016) and supergiant pulses from extragalactic neutron stars (Cordes & Wasserman 2016) as possible progenitors. Other theories involve cataclysmic models including neutron star mergers (Totani 2013) and 'blitzars' occurring when a neutron star collapses to a black hole (Falcke & Rezzolla 2014).

Independent of the physical mechanism/process, an FRB may leave an afterglow through interaction with the surrounding medium. Yi, Gao & Zhang (2014) have estimated FRB afterglow

luminosities, using standard Gamma Ray Burst (GRB) afterglow models in radio, optical and X-ray bands, assuming a plausible range of total kinetic energies and redshifts. Lyutikov & Lorimer (2016) have discussed possible electromagnetic counterparts for FRBs; searching for such counterparts is thus one strategy for localizing FRB host galaxies. Chatterjee et al. (2017) directly localized the repeating FRB 121102 (Spitler et al. 2016) using the Karl G. Jansky Very Large Array (VLA) Telescope and identified its host to be a dwarf galaxy at a redshift *z* ∼ 0.2 (Tendulkar et al. 2017). The host is co-located with a persistent variable radio source. Additionally, the radio follow-ups of FRB 131104 (Shannon & Ravi 2017) and FRB 150418 (Keane et al. 2016; Johnston et al. 2017) have shown the presence of variable radio emission from active galactic nuclei (AGNs) in the fields of FRBs.

The SUrvey for Pulsars and Extragalactic Radio Bursts (SUPERB) is currently ongoing at the Parkes radio telescope and is described in the detail in Keane et al. (2018, hereafter Paper 1). Initial results from the SUPERB survey have already been published elsewhere – this includes investigations into radio frequency interference (RFI) at the Parkes site (Petroff et al. 2015b), the discovery of FRB 150418 (Keane et al. 2016) and the discovery of new pulsars (Paper 1). Here, we report further results from the survey, in particular the discovery of four new FRBs –150610, 151206, 151230 and 160102 – as well as the multimessenger follow-up of the four FRBs. In Section 2, we provide an overview of the observations and techniques for the FRB search. Next, we present the new FRB discoveries and their properties in Section 3. FRB multimessenger follow-up observations and their results are described in Section 4. Finally, in Sections 5 and 6 we present our conclusions and discuss the implications of our results.

Figure 1. The pulse profiles of the four new FRBs de-dispersed to their best-fitting DM values: clockwise from top left FRB 150610, FRB 151206, FRB 160102 and FRB 151230. The top panel shows the time series, frequency averaged to one channel and the bottom panel shows the spectrum of the pulse. The data have been time averaged to 1, 0.6, 0.8 and 0.5 ms per sample for FRB 150610, FRB 151206, FRB 160102 and FRB 151230, respectively. The flux density scale in the upper panel of individual pulses is derived from the radiometer equation. See Table 1 for the dispersion smearing times within a single channel for each FRB.

2 OBSERVATIONS AND TECHNIQUES

The full details of the SUPERB observing system and analysis setup can be found in Paper 1; here, we briefly summarize the key points relevant to this work. Real-time searches are conducted for both transient and periodic signals in the incoming data. These data are also searched offline through a more rigorous process which operates slower than real time. These two streams are called the 'Fast' (F) and 'Thorough' (T) pipelines, respectively. For the single pulse pipeline, data are acquired in the form of a time, frequency and total intensity matrix. These are fed to the transient detection pipeline, $HEMDALL¹$, which applies sliding boxcar filters of various widths and performs a threshold search. This produces candidate detections that are classified as FRBs if they meet the following criteria:

$$
DM \ge 1.5 \times DM_{\text{Galaxy}}
$$

\n
$$
S/N \ge 8
$$

\n
$$
N_{\text{beams,adj}} \le 4
$$

\n
$$
W \le 262.14 \text{ ms}
$$

\n
$$
N_{\text{events}}(t_{\text{obs}} - 2s \to t_{\text{obs}} + 2s) \le 5,
$$
 (1)

where DM and DM_{Galaxy} are the dispersion measures of the candidate and the Milky Way contribution along the line of sight, respectively. The latter is estimated using the NE2001 model (Cordes & Lazio 2002). S/N is the peak signal-to-noise ratio of the candidate, $N_{\text{beams, adj}}$ is the number of adjacent beams in which the candidate is detected and *W* is the width of the boxcar. The final criterion measures the number of candidates detected within a 4 s window centred on the time of occurrence of the pulse. If there are too many candidates in a time region around the candidate of interest, it is flagged as RFI. These criteria are followed by the T-pipeline, and for the purposes of keeping the processing to real-time, for the F-pipeline, we raise the detection threshold to $S/N > 10$ and only search for pulses with widths $W \leq 8.192$ ms. When a candidate meets these criteria, an alert email is issued and an astronomer evaluates a series of diagnostic plots to determine the validity of the candidate. If the candidate is deemed credible, multiwavelength follow-up is triggered. Upon detection of a candidate matching the above criteria, 8-bit full-Stokes data are saved to disc for further offline processing.

3 FRB DISCOVERIES

The individual pulse profiles for the FRBs are shown in Fig. 1 and Table 1 presents their measured and derived properties. The FRBs were detected in single beam of the Parkes multibeam receiver. Each FRB has a positional uncertainty with a radius of 7.5 arcmin.

¹ <https://sourceforge.net/projects/heimdall-astro/>

Table 1. The observed and inferred (model-dependent) properties for FRBs 150610, 151206, 151230 and 160102. The model-dependent properties are derived using the YMW16 model (Yao et al. 2017) of the electron density in the Milky Way. For the cosmological parameters, we use CosmoCalc (Wright 2006), adopting $H_0 = 69.9$ km s⁻¹ Mpc⁻¹, $\Omega_M = 0.286$ and $\Omega_{\Lambda} = 0.714$. The error in the isotropic energy estimate is dominated by the error in the fluence.

The inferred properties including redshift, energy, comoving and luminosity distance are derived using the YMW16 model (Yao, Manchester & Wang 2017) of the electron density in the Milky Way. Our results are consistent within the uncertainties if we adopt the NE2001 model (Cordes & Lazio 2002) instead. To measure the scattering properties of the bursts, the procedure adopted in Champion et al. (2016) was applied. The resulting scattering time was scaled to a standard frequency of 1 GHz, using a spectral index of −4. In the fitting process, we varied the assumed intrinsic width of the burst and find in all cases that the best fit is given by a burst duration that is solely determined by a combination of DM smearing across the filterbank channels and interstellar scattering. Hence, due to the high DM of the FRBs reported here, all four FRBs are unresolved in width. We note that the estimated isotropic energies of the FRBs at source had an incorrect redshift correction in Caleb et al. (2016). The FRBs analysed at that time were mainly at redshifts $z < 1$, and the conclusions of the paper are unaffected. In this paper, three of the reported FRBs have DM >1500 pc cm⁻³, for which cosmological effects become important. We follow Hogg (2000) and estimate the in-band intrinsic energies of the FRBs as

$$
E(J) = \frac{\mathcal{F}_{\text{obs}} \times BW \times 4\pi D_{\text{L}}^2 \times 10^{-29}}{(1+z)^{1+\alpha}}
$$
 (2)

where \mathcal{F}_{obs} is the observed fluence for FRBs in Jy ms, *BW* is the bandwidth at Parkes in Hz, D_L is the luminosity distance in metres, *z* is the inferred redshift of FRBs and α is the spectral index of the source. Note that the denominator incorporates both the *k*-correction for the spectral index and the time-dilation correction. Since we generally assume the spectral index to be flat and thus $\alpha = 0$, there is no *k*-correction in practice.

FRB 150610 was not detected in the F-pipeline. The reason for this was the final selection criterion described in equation (1). At the time of observation, the number of events detected in a 4 s window did not make a distinction *by beam* and as such was overly harsh. In this case, one beam (beam 10) had a large number of RFI events in the time window, which resulted in all other (unrelated) beams being flagged. This criterion has since been corrected in the

F-pipeline. FRB 150610 was discovered in the T-pipeline which makes less severe cuts to generated candidates. Since this burst was found in the offline processing, no prompt follow-up observations could be performed upon detection. The burst is slightly scattered but unresolved.² We determine the frequency dependence of the observed dispersion, $t_{\text{delay}} \propto \text{DM} \times v^{-\beta}$, to be $\beta = 2.000 \pm 0.008$, perfectly consistent with a cold-plasma law.

FRB 151206 fell *just* between search trials in the F-pipeline, placing it slightly below the detection threshold. However the T-pipeline (which samples DM parameter space more completely) identified it soon after. As a result, the full-Stokes data were not retained and no polarization information is available. The burst is unresolved and slightly scattered. The limited signal-to-noise ratio prevents a fit for the DM index. The trigger was issued only 25 h after the time of occurrence and 11 telescopes observed the Parkes position over the following days to months. Observations and results from each of these telescopes are described in Section 4.

FRB 151230 shows peak intensity near the centre of our observing band, similar to some of the events described in Spitler et al. (2016) for FRB 121102. The FRB is bright in the upper 200 MHz of the band and disappears at the lower frequencies in the band, below 1300 MHz. The burst is unresolved and shows scattering, possibly partly responsible for the non-detection at the lowest frequencies. We can determine the DM index to be $\beta = 2.00 \pm 0.03$. This burst was discovered by the F-pipeline, an alert was raised, and a trigger was issued to telescopes after an hour of the detection. This burst was followed up by 12 telescopes ranging from radio to gamma-ray wavelengths.

FRB 160102 is the highest DM FRB yet observed with DM = 2596.1 \pm 0.3 pc cm⁻³, and has an inferred luminosity distance of 17 Gpc, assuming the nominal redshift $z = 2.1$ from the models of Ioka (2003) and Inoue (2004) for the observed DM excess. We find indications of scattering and determine the DM index to be

 $2 \text{ In the lowest subbands a second peak is visible, but statistical tests suggest}$ that it is not significant and caused by noise fluctuations.

Figure 2. Multimessenger follow-up campaign for FRBs 151206, 151230 and 160102. The black line represents a part of the search for neutrino counterparts with ANTARES over the window $[T_0 - 1]$ d; $T_0 + 1$ d], where T_0 is the event time. No high energy follow-up was performed for FRB 151206 as it was Sun-constrained. Also, due to the delayed detection of FRB 150610 the multimessenger follow-up was restricted to an ANTARES search alone.

 $\beta = 2.000 \pm 0.007$. For this FRB, a trigger was issued approximately 1 h after the event and this burst was followed up by eight telescopes spanning radio to gamma-ray wavelengths.

4 FOLLOW-UP STUDIES

Follow-up observations of each FRB's field were carried out with four optical telescopes, nine radio telescopes, one high-energy telescope and the ANTARES neutrino detector. Fig. 2 shows the summary of observations performed on each field. Imaging observations with radio and optical telescopes were performed in order to search for any variable or transient sources that might be associated with the FRBs. Radio follow-up also included searching for repeat pulses from each FRB location. A complete record of all observations performed is included in Tables A1–A4 in the Appendix.

4.1 Radio follow-up for repeat bursts

Follow-up observations were performed with the Parkes telescope using the Berkeley Parkes Swinburne Recorder (BPSR) observing set-up (Keith et al. 2010) immediately after the discovery of each real-time FRB. The Sardinia radio telescope (SRT; Bolli et al. 2015) observed the FRB fields in single pulse search mode at a centre frequency of 1548 MHz with a bandwidth of 512 MHz. Observations were also performed by the Lovell and Effelsberg radio telescopes (Lovell 1985; Hachenberg, Grahl & Wielebinski 1973) in *L* band (1.4 GHz) and single pulse searches were performed with PRESTO (Ransom, Eikenberry & Middleditch 2002) around the DM of the FRB. The UTMOST telescope (Bailes et al. 2017) also observed three of the FRB fields (all except FRB 150610). The UTMOST observations were performed at 843 MHz with a bandwidth of 31 MHz in fan beam mode with 352 fan beams covering $4° \times 2°$.8 (see Caleb et al. 2017 for the details of this observing mode). The

Table 2. The time spent by the Parkes, SRT, Effelsberg, Lovell and UTMOST radio telescopes on the field of SUPERB FRBs to search for repeating pulses. None of the observations showed repeated bursts.

details of the time spent on each FRB field are listed in Table 2. None of the observations showed repeated bursts from their respective FRB fields.

4.2 Radio interferometric follow-up for possible counterparts

Radio imaging observations were performed using the Australia Telescope Compact Array (ATCA; Wilson et al. 2011), VLA, the Giant Metrewave Radio Telescope (GMRT; Ananthakrishnan 1995) and the e-Merlin radio telescope (Garrington et al. 2004), spanning 4–8 GHz and 1–1.4 GHz. The details of the observations, data analysis and variability criteria are listed in Appendix B. Here, we present the results of the follow-ups and the implications of the variability are discussed in Section 5.

FRB 151206 : ATCA observed the field of FRB 151206 on 2015 December 9, 3 d after the burst. Visibilities were integrated for 3 h yielding a radio map with an rms noise of 50 μ Jy beam⁻¹ at 5.5 GHz and 60 μ Jy beam⁻¹ at 7.5 GHz. The declination of the FRB field $(\delta = -04°)$ was not favourable for ATCA observations, therefore no subsequent observations were performed and no variability analysis was conducted on these data.

Table 3. Radio variable sources in the field of FRB 151206 and FRB 160102. The errors in RA and Dec. are in arcseconds and are presented in brackets. Columns 4 and 5 list χ^2 and χ^2_{thresh} values. The χ^2_{thresh} values are upper-tail critical values of chi-square distribution with *N* − 1 degrees of freedom. Columns 6 and 7 list m_d and ΔS values. These variability indices are defined in Appendix B.

Figure 3. Left-hand panel: the light curves over 92 d of two sources in the field of FRB 151206 found to vary significantly in the VLA observations: 1921–0414 (top panel) and 1921–0412 (bottom panel). Right-hand panel: the light curve of the significant variable source 2238–3011 in the field of FRB 160102. The fluxes and errors on fitting are derived from the task IMFIT in MIRIAD. Note that the data have not been calibrated to the same absolute flux scale, and there may be systematic differences between different instruments. However, the data are self-consistent for variability analysis for each instrument.

This field was observed for eight epochs with the VLA starting from 2015 December 8. The radio images reached an rms of ¹⁰ [−] ²⁵μJy beam−1. Observations at epoch 3 were severely affected by RFI and hence excluded from the analysis. To form mosaic images, each of the seven single pointings were stitched together for every epoch and were deconvolved using the CLEAN algorithm (Högbom 1974). Two significantly variable sources were detected in this field, details of which are listed in Table 3. Fig. 3(a) shows their light curves. No non-radio counterpart was identified for either of the sources.

Observations were performed with the GMRT on 2015 December 9. The field was observed for 4 h and the map yielded an rms of 30 μ Jy beam⁻¹. No subsequent observations were performed and no variability analysis was conducted on these data.

The field was also observed with e-Merlin on 2015 December 7 and 8. Observations ran from 14:00–19:30 UTC on December 7 and 09:30–19:30 on December 8. A total of 1945 overlapping fields were imaged and then combined using the AIPS task FLATN. The combined image covered a circular area of 10 arcmin diameter and has an rms of 34 μ Jy beam⁻¹ (beam size =171 \times 31 mas, $PA = 19.4$). At the declination of the source, snapshot imaging is

quite challenging for e-Merlin, so the combined full sensitivity image from 1.5 runs was searched for significant detections with SEXTRACTOR and nothing significant ($> 6\sigma$) was found.

FRB 151230 : ATCA was triggered ∼1 d after the event and visibilities were recorded for 8 h. Subsequent observations were performed on 2016 January 11 and February 24 for 9.5 and 4.5 h, respectively. We performed a variability analysis of all compact sources at 5.5 and 7.5 GHz. Following the criteria described in Appendix B, we conclude that there are no significant variable sources present in the field of FRB 151230.

Observations were performed using the VLA on 2016 February 29 and March 4 and images were produced at the centre frequency of 5.9 GHz with an rms of \sim 15 µJy beam⁻¹. All ATCA sources were detected. None of the compact sources were found to be significantly variable.

GMRT observations were performed on 2016 January 6, February 17 and March 3. The integration times of 4 h yielded an rms of [∼]³⁰ ^μJy beam−¹ at 1.4 GHz. None of the sources showed any significant variability.

FRB 160102 : ATCA observed the FRB 160102 field on 2016 January 3, January 11 and February 24. The best map yielded an rms

Table 4. The results of the radio follow-up performed using the ATCA, VLA and GMRT on the fields of SUPERB FRBs. *N*_{total} denotes the total number of sources detected above 6σ and *N*analysis is the number of sources used in the variability analysis. This excludes extended sources in the field of respective FRBs. *N*variable denotes the number of significant variable sources detected in each field.

Telescope	ATCA				VLA				GMRT			
Centre freq.		5.5 GHz			7.5 GHz			5.9 GHz			$1.4\,\mathrm{GHz}$	
	N_{total}	N_{analysis}	N_{variable}	N_{total}	N_{analysis}	N_{variable}	N_{total}	N_{analysis}	N_{variable}	N_{total}	N_{analysis}	N_{variable}
FRB 151206		$\overline{}$	$\overline{}$		$\overline{}$	$\overline{}$	10	10		13	$\overline{}$	
FRB 151230		₀				$\left($	25	20		27	18	
FRB 160102	12	10		12	10	Ω	21	19		48	$\overline{}$	

of ~40 μ Jy beam⁻¹ at 5.5 GHz and ~50 μ Jy beam⁻¹ at 7.5 GHz. The search for sources was performed over an area of sky that is twice the region of the localization error, i.e. a radius of 15 arcmin because this FRB was detected in the outer beam of the Parkes telescope.

The final variability analysis was performed on 10 compact sources. Source 2238−3011 was found to vary significantly at 5.5 GHz but not at 7.5 GHz. We identify it to the quasar 2QZ J223831.1−301152 from the 'Half a Million Quasar Survey' (Flesch 2015) at $z = 1.6$. This source is also present in the *GALEX* survey (Bianchi et al. 2011, *GALEX* J223831.1−301152) and has a DSS (Eisenstein et al. 2011) optical counterpart. Table 3 and Fig. 3(b) list the details and light curve of the source 2238−3011. The flux density of the source was observed to be rising at ATCA epochs at 5.5 GHz.

The VLA observations were performed on 2016 February 26 and March 4. Flux densities were derived from mosaics with the best rms being [∼]¹⁰ ^μJy beam−1. ATCA source 2238−3011 showed a low level variability with the fractional change (defined in Appendix B), $\Delta S \sim 20$ per cent (< 50 per cent). None of the remaining sources were found to vary significantly at 5.9 GHz.

The field was also observed with the GMRT on 2016 February 6. The integration of 4 h yielded an rms of \sim 30 µJy beam⁻¹. This GMRT epoch was used to cross-check sources detected in the ATCA and VLA images and no variability analysis was performed on these data.

The results of the radio follow-up are summarized in Table 4.

4.3 Follow-up at non-radio frequencies

We have carried out optical and high-energy follow-up and searched for neutrino counterparts to these four SUPERB FRBs. The results are presented in this section and the details of the observations and magnitude limits are listed in Appendix C.

4.3.1 Thai National Telescope (FRB 151206)

The observations were performed with ULTRASPEC on the Thai National Telescope (TNT) on the night of 2015 December 7. Four optically variable sources were found in the field of FRB 151206. The change in magnitude Δ mag provides a measurement of the variability of a given source in the field, such that Δ mag > 0 reflects a dimming source. The only source detected with a negative Δ mag is also bright at infrared wavelengths, with $J = 9.38$, $H = 8.31$, $K = 7.93$, respectively, from 2MASS (Skrutskie et al. 2006). Further photometric observations of the four variable sources were obtained using the 0.5-m robotic telescope 'pt5m' (Hardy et al. 2015). In all cases, the variability seen for these sources can be explained by stellar variability, either eclipsing, ellipsoidal or stochastic (accretion, flaring etc.).

4.3.2 Subaru Telescope (FRB 151230)

We performed follow-up imaging observations of the field of FRB 151230 in the *g*, *r* and *i* bands on 2016 January 7, 10 and 13, with Subaru/Hyper Suprime-Cam that covers a 1.5◦ diameter field-ofview. The images taken on January 13 were used as the reference images and were subtracted from the images of January 7 and 10 using the HSC pipeline (Bosch et al. 2017). 97 variable source candidates with either positive or negative flux difference were detected in the error circle of FRB 151230 on the differential images. These candidates were examined by eye, and approximately half of them appear to be real objects while the other half are artefacts by subtraction failure. Most of the real variable sources are likely to be either Galactic variable stars (point sources without host galaxy) or AGNs (variable sources located at centres of galaxies). There are three objects associated with galaxies and offset from galaxy centres, which are most likely supernovae. This number is consistent with those detected outside the FRB error region considering the area difference, and also consistent with a theoretically predicted number of supernovae with the depth and cadence of our observations (Niino, Totani & Okumura 2014). No object shows evidence for an association with the FRB, although we cannot exclude the possibility that one of them is associated. The nature of the variable objects will be investigated and discussed in detail in a forthcoming paper (Tominaga et al. in preparation).

4.3.3 DECam (FRB 151230)

We obtained Dark Energy Camera (DECam) *u-g-r-i* dithered images centred on the coordinates of FRB 151230, with observations taken approximately 14 h after the detection at Parkes. The field was also re-observed with the *g* filter ∼ 39 h after the FRB detection. We searched these *g*-band images for transient sources $(>10\sigma$ significance) between the two consecutive nights, within the localization error region of 15 arcmin, using MARY pipeline (Andreoni et al., 2017). We detected five variable sources and four of them were catalogued³ as small bodies, i.e. Main-belt asteroids. A fifth object was detected at a magnitude $g = 22.51 \pm 0.08$ on 2016 January 1, which had not been detected on the previous night, 2015 December 31 ($g < 23.37$ at 5σ confidence). This transient is located at RA = 9:40:56.34, Dec. = $-3:27:38.29$ (J2000) and is not present in the NASA/JPL small body catalogue but is most likely to be an asteroid unrelated to FRB. However, it is not detected in the *u-g-r-i* images taken on 2015 December 31. All other transient events were rejected as bona fide transients due to poor local subtraction and bad pixels after a visual inspection of the residuals.

³ NASA/JPL SB identification system: ssd.jpl.nasa.gov.

We have also compared the radio sources detected in the GMRT and ATCA images with the DECam images to look for optical counterparts; more details are given in Appendix C.

4.3.4 The Zadko telescope (FRB 151230)

On 2015 December 30, the Zadko telescope was shadowing the Parkes telescope at the time of the discovery of FRB 151230. However, due to technical difficulties, the first science images were taken at 18:03:20.6 UTC, i.e. ∼1 h after the FRB event. Following this initial imaging, a series of 19 images of 5 tiles each were obtained during about 2 h through to the end of the night. Each image had an exposure time of 60 s in the *r* band. The localization error region (15 arcmin) around FRB 151230 is completely covered by the central image of the tiles and partly contained (∼33 per cent) in the peripheral images.

We analysed the individual images to search for new optical or variable sources in the field of FRB 151230. We particularly focused on the central image of the tile that fully covers the error radius around the FRB position. We found no convincing new or variable optical sources.

4.3.5 High-energy follow-up (FRB 151230, FRB 160102)

We acquired follow-up observations with *Swift* on FRB 151230 burst on 2015 December 30 at 23:14:45 UTC, about 7 h after the FRB for a duration of 2.05 ks. No sources were detected above a 2.5 σ limit in the X-ray image. The data were analysed using the tools available at the *Swift* website (Evans et al. 2007, 2009) on an observation-by-observation basis. Count rates were converted to X-ray flux assuming a GRB-like spectral index of −2.0 and Galactic H_I column density estimates from the HEASOFT tool 'nH'.

We acquired three epochs on the field of FRB 160102 with the *Swift* XRT of durations 3.5, 3.3 and 1.8 ks, respectively. No sources were detected above a 2.5σ limit in any of the images. We did not trigger *Swift* for FRB 150610 (due to the delay in its detection), nor FRB 151206 (as it was Sun constrained for 31 d after the FRB).

No *Swift*-BAT REALTIME triggers were issued for shortduration gamma-ray transients during the follow-up observations for each FRB field.

4.3.6 ANTARES follow-up (all FRBs)

Multimessenger observations with high-energy neutrino telescopes can help to constrain the FRB origin and offer a unique way to address the nature of the accelerated particles in FRBs. The ANTARES telescope (Ageron et al. 2011) is a deep-sea Cherenkov neutrino detector, located 40 km off Toulon, France, in the Mediterranean Sea and dedicated to the observation of neutrinos with $E_v \gtrsim 100 \,\text{GeV}$. ANTARES aims primarily at the detection of neutrino-produced muons that induce Cherenkov light in the detector. Therefore, by design, ANTARES mainly observes the Southern sky $(2\pi$ steradian at any time) with a high duty cycle. Searches for neutrino signals from the four detected FRBs have been performed within two different time windows around the respective FRB trigger time, *T*0, within a 2◦ radius region of interest (ROI) around the FRB position [3σ ANTARES point spread function (PSF) for the online track reconstruction method]. The first time window $\Delta T_1 = [T_0 - 500 \text{ s};$ T_0+500 s] is short and was defined for the case where FRBs are associated with short transient events, e.g. short Gamma-Ray Bursts (Baret et al. 2011). A longer time window $\Delta T_2 = [T_0 - 1 \text{ d}; T_0 + 1 \text{ d}]$

is then used to take into account longer delays between the neutrino and the radio emission. The number of atmospheric background events within the ROI is directly estimated from the data measured in the visible southern sky using a time window $\Delta T_{\text{back}} = [T_0 - 12 \text{ h};$ T_0+12 h]. The stability of the counting rates has been verified by looking at the event rates detected in time slices of 2 h within ΔT_{back} . Within ΔT_1 and ΔT_2 , no neutrino events were found in correlation with FRB 150610, FRB 151206, FRB 151230 or FRB 160102.

5 RESULTS AND DISCUSSION

5.1 Cosmological implications of high DM FRBs

Assuming FRBs are extragalactic, the DM may be divided into contributions along the line of sight from the ISM in the Milky Way (DM_{Galaxy}), the intergalactic medium (DM_{IGM}), a host galaxy (DM_{host}) and the circumburst medium (DM_{source}) :

$$
DM_{FRB} = DM_{Galaxy} + DM_{IGM} + DM_{host} + DM_{source}.\tag{3}
$$

For all the FRBs reported here, the DM_{Galaxy} contribution is minor (< 10 per cent of the total observed DM). It is currently difficult to disentangle the DM contributions of the remaining DM terms for these bursts. Xu & Han (2015) showed the DM_{host} to peak in the range of 30–300 pc cm⁻³ for different inclination angles of a spiral galaxy and average DM_{host} to be 45 and 37 pc cm^{−3} for a dwarf and an elliptical galaxy, respectively. In such cases, the remaining DM is expected to arise from the IGM if the sources are cosmological in nature.

If the DM of our FRBs is indeed dominated by the IGM contribution, then we are potentially probing the IGM at redshifts beyond $z \gtrsim 2$. If we can find FRBs with DM $\gtrsim 3000 \,\text{pc cm}^{-3}$, we could begin to probe the era in which the second helium reionization in the Universe occurred (Fialkov & Loeb 2016), which is important for determining the total optical depth to reionization of the cosmic microwave background (CMB), τ_{CMB} . We note that we discovered FRB 160102 soon after our pipelines were modified to allow for DM searches above 2000 pc cm^{-3} (the current upper limit is 10 000 pc cm−3). Even in the absence of scattering being a dominant factor higher sensitivity instruments will likely be needed to probe such high redshifts.

5.2 FRB latitude dependence revisited

With an ever increasing sample of FRBs detected with the BPSR backend, it is worthwhile to revisit the Galactic latitude dependence in FRB detectability first examined in Petroff et al. (2014). Table 5 summarizes the data from SUPERB, as well as several other projects using BPSR that have each observed the sky with essentially the same sensitivity to FRBs resulting in the total of 19 bursts. We consider three regions on the sky, delineated in Galactic latitude as follows: $|b| \le 19.5$, $19.5 < |b| < 42°$ and $42° \le |b|$. The time on sky in each of these regions and the updated FRB rate at the 95 per cent confidence level are presented in the table. Fig. 4 shows these FRBs on an Aitoff projection in the Galactic coordinate frame. For the studies considered here, Parkes has spent ∼28 per cent of the total time in the lowest Galactic latitude region (this is mostly driven by pulsar searches and/or continued monitoring studies). Despite this, only 4 of the 19 bursts have been found in this range. At the highest latitudes, nine FRBs have been detected in ∼41 per cent of the total time. We performed a Kolmogorov–Smirnov test (K-S) between the expected cumulative distribution of |*b*| for isotropically distributed FRBs based on the integration-time-weighted Galactic latitudes of

Table 5. Time on sky in the three latitude bins for recent surveys conducted at the Parkes telescope: the High Time Resolution Universe survey (HTRU; Keith et al. 2010), observations of rotating radio transients, FRB follow-up, the SUPERB survey and observations of young pulsars for *Fermi* timing. All surveys made, or make, use of the multibeam receiver and have equivalent field of view and sensitivity limits. The FRB sky rates for respective latitude bins are quoted with 95 per cent confidence.

Galactic latitude b (deg)	HTRU medlat (h)	HTRU hilat (h)	RRAT search (h)	FRB follow-up (h)	SUPERB (h)	Fermi timing (h)	Misc time (h)	Total time (h)	$N_{\rm FRBs}$	$R_{\rm FRB}$ $FRBs$ sky ⁻¹ d ⁻¹
$ b \le 19.5$	1157	402	483		700	281		3024	4	$2.4^{+3.1}_{-1.5} \times 10^{3}$
$19.5 < b < 42^{\circ}$		942	28	50	1115	10	100	2245	6	$4.8^{+4.6}_{-2.7} \times 10^3$
$42^{\circ} \le b \le 90^{\circ}$		982	39	60	907		90	2088	$\mathbf Q$	$7.8^{+5.8}_{-3.7} \times 10^3$

Figure 4. An Aitoff projection of the sky distribution of all published FRBs. The shaded regions show the three Galactic latitude bins in Table 5. The bold black line shows the horizon limit of the Parkes radio telescope.

the combined HTRU-SUPERB survey pointings, and the observed cumulative distribution of the 15 FRBs (see Fig. 5). We obtain the K-S statistic *D* and *p* values of 0.29 and 0.10, respectively, and conclude that departure from isotropy is not significant. Thus, any disparity in the FRB rate with Galactic latitude has low significance $(< 2\sigma$) in our now larger sample of 15 FRBs. If such a disparity exists, it could be explained by diffractive scintillation boosting at high Galactic latitudes as discussed in Macquart & Johnston (2015).

5.3 FRB populations and distributions

Sources with constant space density in a Euclidean Universe yield an integral source counts, N , as a function of fluence, \mathcal{F} , the so-called logN–log $\mathcal F$ relation, with a slope of $-3/2$. The relation flattens in Λ cold dark matter cosmologies, depending on the redshift distribution of the sources being probed, and depends to some extent on the luminosity function of the sources, and observational factors like the effects that DM smearing have on the S/N of events (Caleb et al. 2016; Vedantham et al. 2016; CHIME Scientific Collaboration 2017).

Figure 5. The observed cumulative distribution of Galactic latitude |*b*| of FRBs detected in HTRU and SUPERB and the expected integration-timeweighted cumulative distribution of Galactic latitude |*b*| for isotropically distributed FRBs. A K-S test indicates that the FRB distribution does not deviate significantly from isotropy.

Figure 6. Left-hand panel: the source count distribution of Parkes FRBs. The sky rate is indicated on the right, normalized to rate of 1.7 [×] 103 FRBs sky−¹ ^d−¹ for ^F > 2 Jy ms (see Section 5.4). Right-hand panel: the slope ^α of the integral source counts obtained using the maximum-likelihood method (Crawford et al. 1970). We obtain a slope of $\alpha = -2.2^{+0.6}_{-1.2}$ for FRBs above a fluence completeness limit of 2 Jy ms in our updated sample of 19 FRBs. The vertical dashed line indicates the fluence completeness limit and the horizontal dashed line indicates $\alpha = -3/2$, the slope expected for constant space density sources distributed in a Euclidean Universe.

In Fig. $6(a)$, we present the FRB source count distribution as a function of fluence, for FRBs found with the BPSR instrument at Parkes. The sample consists of 10 FRBs found in the HTRU survey (Thornton et al. 2013; Champion et al. 2016; Petroff et al. in preparation), 5 FRBs found with SUPERB (Keane et al. 2016, FRB 150418) and this paper, and 4 FRBs found at Parkes with the same instrumentation and search technique (Petroff et al. 2015a, 2017; Ravi et al. 2015, 2016).

We note the following caveats about the $logN - logF$ distribution. First, the fluences are lower limits, as most of the FRBs are poorly localized within the Parkes beam pattern. Secondly, all FRB surveys are incomplete below some fluence, due to the effects of DM smearing, scattering and the underlying width distribution of the events (see Section 5.4 and Fig. 7). Although both these affect the shape of logN–log F , simulations performed by Caleb et al. (2016) show that the slope of the relation is mainly set by cosmological effects. They found $\alpha = -0.9 \pm 0.3$ for the nine HTRU FRBs.

We measure a slope of the integral source counts using the maximum likelihood method (Crawford, Jauncey & Murdoch 1970) and obtain $\alpha = -2.2^{+0.6}_{-1.2}$ for FRBs above a fluence limit of 2 Jy ms as shown in Fig. 6(b). This is consistent with the source count slope for Parkes FRBs found by Macquart & Ekers (2018), who find $\alpha = -2.6^{+0.7}_{-1.3}$. The large uncertainty in α is due to the small sample size. Similarly to Macquart & Ekers (2018), we are unable to rule out that the source counts are not Euclidean ($\alpha = -3/2$).

5.4 Parkes sky rates

With the increased number of FRBs, we update the all-sky rate estimates for Parkes. The all-sky lower limit on the rate is $4.7^{+2.1}_{-1.7} \times 10^3$ FRBs/(4π sr)/day. This is based on the observed rate of 19 events in 306 d of observing with BPSR, assuming the events occur within the full-width-half-power field-of-view of the receiver, and extrapolating this to the entire sky. The quoted uncertainties are 95 per cent

Figure 7. The observed peak flux density and observed width for all known FRBs. The sensitivity limits and fluence completeness region for BPSR Parkes events are indicated. These do not apply to other events which are shown for reference only.

Poisson uncertainties (Gehrels 1986). Additionally, we update the fluence complete rate, which is a more useful quantity when scaling FRB rates to other telescopes and/or frequencies. Fig. 7 shows the observed peak flux density and observed widths of the FRB population, with Parkes sensitivity and completeness regions highlighted. Following Keane & Petroff (2015) and considering those FRBs in the fluence complete region, we estimate a rate above ∼2 Jy ms of $1.7^{+1.5}_{-0.9} \times 10^3$ FRBs/(4 π sr)/day.

Figure 8. Left-hand panel: the density of significantly variable radio sources as a function of flux density in surveys made at ∼5 and 3 GHz by Bell et al. (2015), this work, Becker et al. (2010) and Mooley et al. (2016). The density of significantly variable sources is consistent within a 1σ Poisson error for surveys done in the past. Right-hand panel: the density of transient radio sources in surveys conducted at 1.4 GHz (Frail et al. 1994; Carilli, Ivison & Frail 2003; Croft et al. 2011; Thyagarajan et al. 2011; Mooley et al. 2013), 3 GHz (Bower et al. 2010; Croft, Bower & Whysong 2013; Mooley et al. 2016, CNSS pilot, CNSS, VLSS), 4.9 GHz (Bower et al. 2007; Ofek et al. 2011), and 5.5 GHz (this work, Bell et al. 2015) as a function of flux density. The dashed blue line shows $\rho_t \propto$ *S*^{−3/2}. This is the relation for a Euclidean population.

5.5 Variable and transient source densities in the field of FRBs

We essentially performed a targeted survey to search for significantly variable and transient radio sources in the three of our FRB fields. We covered \sim 0.15 deg² of sky for all fields with VLA at a sensitivity of \sim 100 µJy and \sim 0.3 deg² of sky for all fields with ATCA at a sensitivity of ∼300 μJy from 4 to 8 GHz. We detected two sources in the VLA images of the field of FRB 151206 and one source in the ATCA images of the field of FRB 160102 to vary significantly.

However, no radio transients were detected. The significant variable source surface density for our survey is $\rho_v = 10^{+9.7}_{-5.4}$ deg⁻² (1*o*) Poisson error). The Poisson uncertainties are calculated following Gehrels (1986). The upper limits on the transient source density for zero detections at 95 per cent confidence is given by $\rho_t < 0.56 \text{ deg}^{-2}$ above the flux limit of 100 μ Jy. (Fig. 8b).

Bell et al. (2015) performed a search for variable sources in \sim 0.3 deg² with comparable flux limits and at similar frequencies as our search. They reported $\rho_v = 3.3^{+7.5}_{-2.7} \text{ deg}^{-2}$ (1 σ Poisson error) for significant variable sources. We also compared our ρ _v with Becker et al. (2010) and Mooley et al. (2016). The results are presented in Fig. 8(a). The flux density limit (S_{min}) and ρ_{v} for Mooley et al. (2016) were scaled from 5.5 to 3 GHz using the relation $S_{\text{min}} \propto v^{\alpha}$ and $\rho_v \propto S_{\text{min}}^{-1.5}$, where v is the frequency and α is the spectral index (which is assumed to be -0.7). We find that the surface density of significant variable sources is consistent within the uncertainty estimates with surveys done in the past in non-FRB fields. Consequently, we find no strong evidence that the FRBs reported here are associated with the highly variable sources in the fields, subject to the caveats that somewhat different variability search criteria, different frequencies and different sensitivity limits were used in the comparison surveys.

The probability of detecting *N* variable sources in an area *A* is given by

$$
P(N) = \int_0^\infty P(N \mid \sigma) P(\sigma) d\sigma,\tag{4}
$$

where σ is the variable source density, $P(\sigma)$ is the prior probability for that variable, normalized such that $\int_0^\infty P(\sigma) d\sigma = 1$. We calculate the prior probability using Bell et al. (2015) as our control survey, which is given by

$$
P(\sigma) = C\sigma^{N_0} e^{-\sigma A_0},\tag{5}
$$

where *C* is the normalization constant, N_0 and A_0 are the number of highly variable source and the area covered in the control survey, respectively. We use results from our VLA observations of FRB fields to compare with the control survey because of their comparable sensitivities and found that the probability of detecting two highly variable sources in a \sim 0.15 deg² area of sky is 14.8 per cent. Currently with the available data, we lack sufficient information to conclusively associate any of these variable sources with FRB 151206 or FRB 160102. However, the detection of a known variable quasar in the field of FRB 160102, the presence of variable AGNs in the field of FRB 150418 (Johnston et al. 2017), FRB 131104 (Shannon & Ravi 2017) and the persistent variable radio source in the field of FRB 121102 (Chatterjee et al. 2017) hint that FRBs might be related to AGN activity in the host galaxy; however, in the absence of a large FRB population and their localization, this remains speculative.

6 SUMMARY AND CONCLUSIONS

We report the discoveries of four new FRBs in the SUPERB survey being conducted with the Parkes radio telescope: FRB 150610, 151206, 151230 and 160201. We have performed multimessenger follow-up of these using 2, 11, 12 and 8 telescopes, respectively. No repeating radio pulses were detected in 103.1 h of radio follow-up. We continue to follow all SUPERB and bright HTRU FRBs in our ongoing SUPERB observations.

A comparison of the repeating FRB with the published nonrepeating FRBs has been performed by Palaniswamy & Zhang (2017), who present evidence that there are two distinct populations of FRBs – repeating and non-repeating – based on the distribution of pulse fluences and the amount of follow-up time for each

Table 6. Comparison of the properties of the FRBs detected in SUPERB and the repeating FRB 121102. SUPERB FRBs are unresolved in time and show scattering unlike the repeater.

Property	FRB 121102	SUPERB FRBs
\sim 100 MHz spectral features	Yes	1 of 5 sources
Time resolved	Yes	N ₀
Range of spectral index	-15 to $+10$	~ 0
Scattering	N ₀	Yes
Width	$3-9$ ms	$< 0.8 - 4$ ms

source. The FRBs reported here differ from FRB121102 (the repeating FRB) in a number of ways, as shown in Table 6. The pulses from the repeater are time resolved and their pulse widths vary from 3 to 9 ms, whereas the SUPERB FRBs are unresolved (in time): the width is instead dominated by the effects of DM smearing and scattering. This appears to provide further support for the two-source population conclusion of Palaniswamy & Zhang (2017).

With our larger sample of FRBs detected at Parkes, we have revisited the FRB event rate and derived an updated all-sky FRB rate of $1.7^{+1.5}_{-0.9} \times 10^3$ FRBs/(4 π sr)/day above a fluence of ~2 Jy ms. We have also computed the volumetric rate of FRBs for the 19 FRB sample using the fluence complete rate as our basis. We get volumetric rates in the range 2000–7000 Gpc⁻³ yr⁻¹ out to a redshift of *z* ∼ 1. This is consistent with volumetric rates for a range of transients [e.g. low-luminosity long GRBs, short GRBs, NS–NS mergers and supernovae (CC, Type Ia, etc.)] (Totani 2013; Kulkarni et al. 2014).

Our follow-up campaign of the reported FRBs yielded no multiwavelength or multimessenger counterparts and we have placed upper limits on their detection. We have also concluded that variability in the optical/radio images alone does not provide a reliable association with the FRBs. We encourage wide-field and simultaneous multiwavelength observations of FRBs. In future, the detection of FRBs with an interferometer would be able to provide a robust host galaxy association.

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APPENDIX A: FRB FOLLOW-UP SUMMARY

Tables A1 to A4 below summarize all of the follow-up observations that have been performed for the four FRBs presented in this paper.

> **Table A1.** Multiwavelength follow-up of FRB 150610 at ANTARES and Parkes. The sensitivity limits are specified for 10σ events with a width of 1 ms at Parkes.

Telescope	UTC	$T_{\text{post-burst}}$	$T_{\rm obs}$ (s)	Sensitivity limit
ANTARES	2015-06-10 05:26:58	$T_{\rm FRB}$	$T_{\rm FRB}$ – day; $T_{\rm FRB}$ + day	Ref. Table C5
Parkes	2017-06-08 03:22:10	728 d. 21:55:12	7200	466 mJy at 1.4 GHz
Parkes	2017-06-08 05:26:02	728 d, 23:59:04	7200	466 mJy at 1.4 GHz
Parkes	2017-06-08 07:38:43	729 d. 2:11:45	7200	466 mJy at 1.4 GHz
Parkes	2017-06-08 09:43:47	729 d. 4:16:49	7200	466 mJy at 1.4 GHz
Parkes	2017-06-08 11:48:30	729 d, 6:21:32	7200	466 mJy at 1.4 GHz

Table A2. Multiwavelength follow-up of FRB 151206 at 11 telescopes. The sensitivity limits are specified for 10σ events with a width of 1 ms at Parkes, SRT, Lovell, Effelsberg and UTMOST.

Table A3. Multiwavelength follow-up of FRB 151230 at 12 telescopes. The sensitivity limits are specified for 10σ events with a width of 1ms at Parkes, SRT, Lovell and UTMOST.

Telescope	UTC	$T_{\text{post-burst}}$	T_{obs} (s)	Sensitivity limit
ANTARES	2015-12-30 17:03:26	$T_{\rm FRB}$	$T_{\text{FRB}} - \text{day}$; $T_{\text{FRB}} + \text{day}$	Ref. Table C5
Zadko	2015-12-30 18:03:21	00:59:55	7457	r < 19.8
Parkes	2015-12-30 18:03:30	01:00:04	3616.01	466 mJy at 1.4 GHz
Parkes	2015-12-30 19:32:28	02:29:02	3618.11	466 mJy at 1.4 GHz
SWIFT	2015-12-30 23:14:45	06:11:19	2056.5	1.918×10^{13} erg ⁻¹ cm ² s ⁻¹
DECam	2015-12-31 07:11:17	14:07:51	900	u < 21.5
DECam	2015-12-31 07:28:42	14:25:16	375	g < 22.5
DECam	2015-12-31 07:37:22	14:33:56	200	r < 23.8
DECam	2015-12-31 07:43:06	14:39:40	750	i < 24.1
ATCA	2015-12-31 14:15:45	21:12:19	28 800	288 μ Jy at 5.5 GHz
				348 µJy at 7.5 GHz
Lovell	2016-01-01 00:44:43	1 d, $7:41:17$	7200	350 mJy at 1.5 GHz
DECam	2016-01-01 07:44:44	1 d, 14:41:18	200	g < 22.6
Parkes	2016-01-01 13:42:56	1 d, 20:39:30	3619.95	466 mJy at 1.4 GHz
Parkes	2016-01-01 14:43:39	1 d, 21:40:13	3617.06	466 mJy at 1.4 GHz
Parkes	2016-01-01 15:44:19	1 d, 22:40:53	3617.06	466 mJy at 1.4 GHz
Parkes	2016-01-01 16:45:09	1 d, 23:41:43	3617.06	466 mJy at 1.4 GHz
Parkes	2016-01-01 17:45:49	2 d, 0:42:23	3617.06	466 mJy at 1.4 GHz
Parkes	2016-01-01 18:46:28	2 d, 1:43:02	3618.11	466 mJy at 1.4 GHz
Parkes	2016-01-01 19:47:09	2 d, 2:43:43	3617.06	466 mJy at 1.4 GHz
Parkes	2016-01-02 14:20:00	2 d, 21:16:34	3616.01	466 mJy at 1.4 GHz
Parkes	2016-01-02 15:20:38	2 d, 22:17:12	3618.11	466 mJy at 1.4 GHz
Parkes	2016-01-02 16:21:18	2 d, 23:17:52	3618.11	466 mJy at 1.4 GHz
Parkes	2016-01-02 17:22:10	3 d, 0:18:44	3616.01	466 mJy at 1.4 GHz
Parkes	2016-01-02 18:22:47	3 d, 1:19:21	3618.9	466 mJy at 1.4 GHz
Parkes	2016-01-02 19:23:28	3 d, 2:20:02	3618.11	466 mJy at 1.4 GHz
Parkes	2016-01-03 13:32:51	3 d, 20:29:25	3624.93	466 mJy at 1.4 GHz
Parkes	2016-01-03 14:33:38	3 d, 21:30:12	3618.11	466 mJy at 1.4 GHz
Parkes	2016-01-03 15:34:19	3 d, 22:30:53	3617.06	466 mJy at 1.4 GHz
Parkes	2016-01-03 16:35:09	3 d, 23:31:43	3617.06	466 mJy at 1.4 GHz
Parkes	2016-01-03 17:35:48	4 d, 0:32:22	3618.11	466 mJy at 1.4 GHz
Lovell	2016-01-03 22:41:31	4 d, 5:38:05	5580	350 mJy at 1.5 GHz
Lovell	2016-01-04 00:16:07	4 d, 7:12:41	1596	350 mJy at 1.5 GHz
Parkes	2016-01-04 14:54:30	4 d, 21:51:04	3616.01	466 mJy at 1.4 GHz
Parkes	2016-01-04 15:55:10	4 d, 22:51:44	3616.01	466 mJy at 1.4 GHz
Parkes	2016-01-04 16:56:00	4 d, 23:52:34	3616.01	466 mJy at 1.4 GHz
Parkes	2016-01-04 17:58:08	5 d, 0:54:42	3618.11	466 mJy at 1.4 GHz
Parkes	2016-01-04 18:58:49	5 d, 1:55:23	1258.03	466 mJy at 1.4 GHz
Parkes	2016-01-04 19:20:18	5 d, 2:16:52	3618.11	466 mJy at 1.4 GHz
Parkes	2016-01-05 14:40:00	5 d, 21:36:34	3616.01	466 mJy at 1.4 GHz
Parkes	2016-01-05 15:40:39	5 d, 22:37:13	3617.06	466 mJy at 1.4 GHz
Parkes	2016-01-05 16:41:42	5 d, 23:38:16	3623.88	466 mJy at 1.4 GHz
Parkes	2016-01-05 17:43:03	6 d, 0:39:37	3623.09	466 mJy at 1.4 GHz
Parkes	2016-01-05 18:52:06	6 d, 1:48:40	3619.95	466 mJy at 1.4 GHz
Parkes	2016-01-06 14:41:36	6d, 21:38:10	3619.95	466 mJy at 1.4 GHz
Parkes	2016-01-06 15:42:16	6 d, 22:38:50	3619.95	466 mJy at 1.4 GHz
Parkes	2016-01-06 16:43:10	6 d, 23:39:44	3616.01	466 mJy at 1.4 GHz
Parkes	2016-01-06 17:43:47	7 d, 0:40:21	3618.9	466 mJy at 1.4 GHz
Parkes	2016-01-06 18:48:33	7 d, 1:45:07	3623.09	466 mJy at 1.4 GHz
GMRT	2016-01-06 18:30:00	7 d, 1:26:34	15588	180 μ Jy at 1.4 GHz
Parkes	2016-01-06 19:53:13	7 d, 2:49:47	1900.28	466 mJy at 1.4 GHz
Subaru	2016-01-07 11:23:19	7d, 18:19:53	4200	Refer table C ₂
Subaru	2016-01-07 13:17:22	7d, 20:13:56	3150	Refer table C2
Subaru	2016-01-07 15:12:39	7d, 22:09:13	4200	Refer table C2
Subaru	2016-01-10 11:11:39	10 d, 18:08:13	3600	Refer table C ₂
Subaru	2016-01-10 13:03:29	10 d, 20:00:03	3600	Refer table C ₂
Subaru	2016-01-10 15:07:20	10 d, $22:03:54$	4080	Refer table C ₂
ATCA	2016-01-11 11:36:55	11 d, 18:33:29	34 4 4 0	288 µJy at 5.5 GHz
				390 µJy at 7.5 GHz
Subaru	2016-01-13 11:21:54	13 d, 18:18:28	3600	Refer table C ₂
UTMOST	2016-01-13 12:13:48	13 d, 19:10:22	27 000	11 Jy at 843 MHz
Subaru	2016-01-13 13:12:52	13 d, 20:09:26	3600	Refer table C ₂
Subaru	2016-01-13 15:13:35	13 d, 22:10:09	3600	Refer table C2

Table A3. – *continued*

Telescope	UTC	$I_{\text{post-burst}}$	$T_{\rm obs}$ (s)	Sensitivity limit
Lovell	2016-01-14 00:03:12	14 d, 6:59:46	7200	350 mJy at 1.5 GHz
Lovell	2016-01-30 00:32:04	30 d, 7:28:38	7200	350 mJy at 1.5 GHz
GMRT	2016-02-17 19:30:00	49 d, 2:26:34	14400	180 µJy at 1.4 GHz
ATCA	2016-02-24 09:48:15	55 d, 16:44:49	16500	240 μ Jy at 5.5 GHz
				$252 \mu Jy$ at 7.5 GHz
VLA	2016-02-29 06:42:11	60 d, 13:38:45	4353	105 μ Jy at 5.9 GHz
GMRT	2016-03-03 13:30:00	63 d, 20:26:34	14400	$180 \mu Jy$ at 1.4 GHz
VLA	2016-03-04 06:26:25	64 d, 13:22:59	4353	84 µJy at 5.9 GHz
Lovell	2016-03-18 18:34:51	79 d, 1:31:25	1965	350 mJy at 1.5 GHz
SRT	2016-05-10 17:58:43	132 d, 0:55:17	10350	1.7 Jy at 1.5 GHz

Table A4. Multiwavelength follow-up of FRB 160102 at eight telescopes. The sensitivity limits are specified for 10σ events with a width of 1 ms at Parkes, SRT and UTMOST.

APPENDIX B: INTERFEROMETRIC OBSERVATIONAL DETAILS AND VARIABILITY CRITERIA

Table B1 summarizes the observations performed by the ATCA, VLA and GMRT on the field of SUPERB FRBs. For all detected sources, the following statistics were used to test for variability using a method very similar to Bell et al. (2015). First, the chi-square χ^2 probability that the source is not variable is estimated with

$$
\chi^{2} = \sum_{i=1}^{n} \frac{(S_{i} - \overline{S}_{\text{wt}})^{2}}{\sigma_{i^{2}}},
$$
(B1)

where S_i is the flux value in an epoch i, σ_i is the inverse of individual error in the flux measurement and \overline{S}_{wt} is the weighted mean flux. Using χ^2 distribution tables for *n* − 1 degrees of freedom, a source is classified as variable if $P < 0.001$, where P is the probability that χ^2 is produced by chance. Additionally, the de-biased modulation index is calculated using

$$
m_{\rm d} = \frac{1}{\overline{S}} \sqrt{\frac{\sum_{i=1}^{n} (S_i - \overline{S})^2 - \sum_{i=1}^{n} \sigma_i^2}{n}},
$$
(B2)

where \overline{S} is the mean flux density. Lastly, the fractional variability is computed using

$$
\Delta S = \frac{S_{\text{max}} - S_{\text{min}}}{\bar{S}},\tag{B3}
$$

where S_{max} and S_{min} are the maximum and minimum flux densities for a source over *n* epochs. A source is regarded to be a significant variable if the χ^2 is greater than threshold χ^2_{thresh} and $\Delta S > 50$ per cent, similar to Bell et al. (2015).

B1 The Australia Telescope Compact Array

The follow-up of three of the FRB fields was performed with the ATCA, using compact array broad-band backend (Wilson

ATCA VLA GMRT No. of epochs Area PC and SC No. of epochs Area PC and SC No. of epochs Area PC and SC (deg^2) (deg²) (deg²) FRB 151260 1 0.05 1934−638 1937−101 8 0.05 3C286 J2355+4950 1 0.05 3C286 2011−067 FRB 151230 3 0.05 1934−638 0941−080 2 0.05 3C138 J0943−0819 3 0.05 3C48 0943−083 FRB 160102 3 0.2 1934−638 2240−260 2 0.05 3C48 J2248−3235 1 0.2 3C48 3C286

Table B1. Radio imaging observations performed with the ATCA, VLA and GMRT on the field of SUPERB FRBs. The table lists the number of epochs, area covered and primary and secondary calibrators used for these observations.

et al. 2011) with a bandwidth of 2 GHz each centred at 5.5 and 7.5 GHz to search for radio afterglows or variable sources associated with FRBs. The observations were done in a 42-pointing mosaic mode encompassing the localization error radius of 75 arcmin. The data were reduced following the standard steps of imaging in MIRIAD (Sault, Teuben & Wright 1995). AEGEAN (Hancock et al. 2012) was used as a source finding and flux estimation software along with MIRIAD tasks IMSAD and IMFIT. The images were searched for sources down to the threshold of 6σ in all ATCA data and a variability analysis (described above) was performed to identify variable sources.

B2 The Karl G. Jansky VLA

The VLA observations were performed in the 4 to 8 GHz band with a centre frequency of 5.9 GHz. A seven-pointing mosaic was done to encompass Parkes localization error radius of 75 arcmin. The data reduction was performed using CASA (McMullin et al. 2007). All sources detected above 7σ were monitored between the epochs to search for variable sources. We note here that the flux density scale using wide-band VLA mosaics is unreliable due to poorly constrained primary beam shape over the wide frequency band; however, the flux scale is stable between epochs such that although the absolute flux scale of the mosaic images is wrong, the variability analysis will be correct.

B3 The Giant Metrewave Radio Telescope

The GMRT (Ananthakrishnan 1995) observed the FRB fields at the centre frequency of 1.4 GHz and bandwidth of 120 MHz. The data reduction was performed using the data reduction software AIPS (Wells 1985). AEGEAN was used as source finding algorithm and a search for sources was performed down to 6σ noise level.

B4 e-Merlin radio telescope

The follow-up of FRB 151206 was also conducted by the e-Merlin telescope (Garrington et al. 2004) with a bandwidth of 512 MHz centred on 5072.3 MHz. The data reduction was done using software AIPS (Wells 1985) and a search for sources was performed down to 6σ noise limit.

APPENDIX C: OBSERVATIONAL DETAILS AND MAGNITUDE LIMITS FOR NON-RADIO FOLLOW-UPS.

C1 Thai National Telescope

Optical follow-up imaging was conducted on the field of FRB 151206 with the 2.4-m TNT, using the ULTRASPEC camera, with field of view $8' \times 8'$ (Dhillon et al. 2014). Four tilings

Table C1. Optical variable sources detected by the TNT in the field of FRB 151206.

were observed on the night of 2015 December 7. Each tile observation consisted of 6 r' -band images with exposure times of 60 s. The same four tiles were repeated 4 d later, enabling a comparative analysis of sources. The effective overlapping area observed on both occasions was $15' \times 15'$, centred on 19:21:27, -04:07:35 (J2000). The estimated 5 σ detection limits for both epochs were $r' = 22.0$. The variable sources detected are presented in Table C1.

C2 Subaru Telescope

The Hyper Suprime-Cam (HSC) data are reduced using HSC pipeline version 4.0.5 (Bosch et al. 2017), which is developed based on the LSST pipeline (Ivezić et al. 2008; Axelrod et al. 2010 ; Jurić et al. 2015), in the usual manner including bias subtraction, flat-fielding, astrometry, flux calibration, mosaicking, warping, coadding and image subtraction. The astrometric and photometric calibration is made relative to the Pan-STARRS1 (Chambers et al. 2016) with a 4.0 (24 pixel) aperture diameter.

For transient finding, the HSC pipeline adopts the frequently used image subtraction algorithm developed by Alard (2000) and Alard & Lupton (1998); an image with narrower PSFs is convolved with spatially varying kernels to match the wider PSFs of the other image, and the image subtraction is made for the PSF-matched images. In the analysis, we set the images taken on January 13 as the reference images and are subtracted from the science images taken on January 7 and 10. The 5σ limiting magnitude on the variability are estimated by 1000–4000 apertures with a diameter being twice as large as the FWHM size of PSF. The apertures are randomly sampled from positions without any detection in the science and reference images and are locally sky subtracted.

Since the detected sources include many fakes, transient candidates are further selected using their measured properties and the spatially varying PSF and elongation of the difference images. We select the transient candidates detected at least twice with the following detection criteria; (1) the detection significance is higher than 5σ , (2) the PSF size is between 0.8 and 1.3 of PSF size of the difference image, (3) the elongation is larger than 0.65 of elongation of the difference image and (4) the residual of the subtraction of the PSF kernel from the detected source is less than 3σ . The limiting magnitudes for Subaru observations are listed in Table C2.

Table C2. Limiting magnitudes for Subaru observations of FRB 151230 field.

Band	$2016 - 01 - 07 - 2016 - 01 - 13$	$2016 - 01 - 10 - 2016 - 01 - 13$
$HSC-G$	>26.1	>26.3
$HSC-R$	>25.8	>25.8
$HSC-I$	>26.00	>26.1

Table C3. Details of the follow-up of FRB 151230 performed with DE-Cam, including the date and time of the observation, the filter used, the individual exposure time and the number of exposures $N_{\rm exp}$ taken with a regular dithering pattern.

Obs. time (UTC)	Filter	Exp(s)	$N_{\rm exp}$
2015-12-31, 07:11:17.1		180	
2015-12-31, 07:28:42.5		75	
2015-12-31, 07:37:22.2	g	40	
2015-12-31, 07:43:06.8	\mathcal{U}	150	
2016-01-01, 07:44:44.4	g	40	

Table C4. Detection limits (AB magnitudes) for sources detected in the DECam images for the field of FRB 151230 with significance reported in the last column. Refer to Table C_3 for more details about the observations.

C3 DECam

The DECam (Dark Energy Survey Collaboration 2012; Flaugher et al. 2012) is a wide-field optical imager mounted at the primary focus of the 4-m Blanco telescope at CTIO. Tables C3 and C4 summarizes the details of these observations and the limiting magnitudes

The radio sources in ATCA and GMRT images for the FRB 151230 field were compared with DECam optical image to look for optical counterparts. Optical sources present above 5σ of the background noise are considered to be a detection in each *u*-*g*-*r*-*i* filter. We found that 52 per cent of the radio sources have an optical counterpart in at least one filter, for a search radius of 3 arcsec. This result of radio-to-optical source association is consistent with the work of Huynh et al. (2005).

C4 The Zadko Telescope

The Zadko Telescope (Coward et al. 2017) is a 1-m f/4 Cassegrain telescope situated in the state of Western Australia. The Zadko telescope has a moderate field of view of $23' \times 23'$, so the complete shadowing of the Parkes multibeam receiver required five-tile images.

C5 The ANTARES neutrino detector

Searches for up-going track events in the ANTARES data have been optimized to give a 3σ discovery potential for one neutrino event in a search time window of $\Delta T = [T_0 - 6 \text{ h}; T_0 + 6 \text{ h}]$ within the ROI. For the four FRBs, the expected background event rate in an ROI of 2° is of the order of $R_µ$ ~ 5 × 10⁻⁸events⁻¹. Thus, the Poisson probability of observing zero event, knowing the background event rate, is ≥ 99 per cent for any of the four FRBs. Hence, the null result is compatible with the background expectation.

The non-detection of neutrino counterparts allows us to derive upper limits at 90 per cent confidence level on the neutrino fluence of the four FRBs based on the instantaneous acceptance of ANTARES at the FRB trigger time: $F_{v,90}$ per cent $\lt \int_{E_{\text{min}}}^{E_{\text{max}}} dN/dE_v E_v dE_v$ Two generic neutrino energy spectra were considered and defined by a power-law function $dN/dE_v \propto E_v^{-\Gamma}$ with spectral indices $\Gamma = 1$ and 2. The limits are then computed using a dedicated Monte Carlo simulation that takes into account the response of the detector at the FRB trigger time. The energy range $[E_{\min}; E_{\max}]$ corresponds to the 5–95 per cent range of the energy distribution of the events in the optimized data set. The results on the neutrino fluence upper limits for the two considered neutrino spectra are given in Table C5. Constraints on the isotropic energy released in neutrinos can be set depending on the distance of the considered FRB: $E_{\nu,90}^{\text{iso}}$ per cent = $4\pi D^2 F_{\nu,90}$ per cent/(1 + z), where *D* is the effective distance travelled by the neutrinos. For the E_{ν}^{-2} spectral model, three FRB distance scenarios have been tested: a galactic environment with $D = 50$ kpc ($z \sim 0$), a nearby extragalactic distance with $D = 100$ Mpc ($z \sim 0.02$) and a cosmological scenario with $D =$ $D(z)$ depending on the cosmological parameters and the maximum *z* inferred from DM as listed in Table 1. The cosmological distance, $D(z)$, travelled by the neutrinos from each FRB was computed from the equation 4 of Adrian-Martínez et al. (2017) and found to be $D(z) = 6.61, 6.75, 3.67$ and 10.17 Gpc, respectively. For the four FRBs, the ANTARES constraints given by $E_{\nu,90}^{iso}$ per cent are at the level of $E_{\nu,90}^{iso}$ per cent $\sim 10^{45}$, 10^{52} and 10^{55} erg, respectively, for the three distance scenarios. In particular, if these four FRBs are

Table C5. Upper limits on the neutrino fluence, $F_{\nu,90}$ per cent, estimated for the four FRBs according to the instantaneous ANTARES sensitivity. The limits are given in the energy range [*E*min–*E*max] where 90 per cent of the neutrino signal is expected.

FRB	$\frac{dN}{dE_v} \propto E_v^{-2}$		$\frac{dN}{dE_v} \propto E_v^{-1}$		
	$F_{\nu,90}$ per cent $erg \text{ cm}^{-2}$ (GeV cm ⁻²)	$[E_{\min}; E_{\max}]$ $log_{10}(GeV)$	$F_{\nu,90}$ per cent $\text{erg cm}^{-2}(\text{GeV cm}^{-2})$	$[E_{\min}; E_{\max}]$ $log_{10}(GeV)$	
150610	3.2×10^{-2} (20)	[3.4; 6.8]	2.54(1600)	[5.8; 7.9]	
151206	1.8×10^{-2} (11)	[3.6; 6.9]	0.41(250)	[5.8; 8.0]	
151230	1.8×10^{-2} (11)	[3.2; 6.8]	0.76(470)	[5.8; 8.0]	
160102	2.6×10^{-2} (16)	[3.6; 7.0]	0.47(290)	[5.8; 8.0]	

associated with neutrino emission following an E_v^{-2} spectrum and with $E_{\nu,90}^{iso}$ per cent $\gtrsim 10^{52}$ erg, ANTARES excludes their origin at distance within 100 Mpc.

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