

# Optimized Design of an LCL Filter for Grid Connected Photovoltaic System and Analysis of the Impact of Neighbors' Consumption on the System

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This paper presents an optimized design method for an LCL filter for a grid connected photovoltaic system. This method is based on the Fast Fourier Transform (FFT) of the current and voltage which provides the current ripples thus allowing to find the LCL filter passives elements. A trick which consists of inductances fragmentation is adopted in order to reduce the volume and the cost of the filter. Then, we do an analysis taking into account the impact of our neighbors consumption. This system is controlled by a decoupled active and reactive power control (PQ control) using a Phase Locked Loop (PLL) for the system's synchronization. Finally, we present and discuss the results of our simulation obtained by Matlab software (simulink and simpowersystems) in order to highlight the proposed study.

Keywords: Optimized design; LCL filter; grid connected photovoltaic system.

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### **1. Introduction**

In a grid connected photovoltaic (PV) system, an inverter between the PV source and the utility grid is required. It is necessary to insert a passive filter between the inverter and the utility grid in order to filter the harmonics produced by the inverter [1], [2].

There are three types of passive filter: the *L* filter, the *LC* filter and the *LCL* filter. Nowadays, the *LCL* filter is vastly used than the others because of its filtering efficiency as in [1], [2], [3], [4], [5], [6], [7], [8] and [11].

However, many authors impose simplifying hypotheses in which they connect the neutral of the utility grid to the midpoint of the *DC* bus and consider the inverter as a *DC/DC* converter to find the current ripple expression as a function of inductance, switching frequency, DC bus voltage and duty cycle. Knowing the ripple formula allows to find the inductance on the inverter side  $L_1$ . The value of the capacitor *C* is found using the formula of the reactive power generated by the capacitor. Very often, a variation of the reactive power lower than 5% of the active power is considered, as in [1], [2], [3] and [4]. Then, knowing  $L_1$  and *C*, and by using the transfer function of the *LCL* filter, it is easy to find the grid side inductance  $L_2$ .

This is practically the most common method for calculating *LCL* filter elements, but it is based on unrealistic assumptions. Indeed, in the case of the inverter, the duty cycle changes

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over time, the output voltage of the inverter is also a function of time and depends on the grid voltage. In addition, connecting the utility grid neutral to the midpoint of the *DC* bus makes easier the calculation by setting the common mode voltage to null; Despite its easiness, from an economical point of view, this solution is not desirable because it requires an additional cable. On the other hand, if the neutral is not connected to the midpoint, the expression of the current ripples becomes very complicated because it is necessary to take account of the common mode voltage [5].

The objectives of this paper are to design the LCL filter according to the requirements of the *IEEE*1547 [13], taking into account the common mode voltage, and using a design method based on the Fast Fourier Transform (*FFT*) of the currents and voltages on the one hand, and to analyze the system by taking into account the impact of the consumption of neighbors on our system on the other hand. In order to optimize the magnetic design of the filter inductances, we apply a trick consisting of dividing each inductance value and making it in several small inductances in series. This technique makes it possible to choose small inductances cores at low cost and less bulky. It is shown that there is a gain on the overall volume and on the manufacturing cost of these inductances.

A decoupled active and reactive power control (PQ control) will be used to control the current to be injected into the utility grid and to adjust the output voltage of the inverter. The synchronization of the system is done by a Phase-Locked Loop (PLL).

This paper is organized around the following sections: Section 2 describes the system, section 3 presents the modeling of the system, section 4 and 5 present the design of the *LCL* filter. Finally, section 6 presents the simulation results and discussion.

#### 2. Description of the system

The diagram of the grid connected PV system is shown in figure 1. It is composed of the photovoltaic generator (PVG), the three-phase inverter, the LCL filter and the utility grid. A damping resistance  $R_f$  is added in series with the filter capacitor in order to limit the resonance effects of the filter [6], [7], [8]. This resistance can also be connected in parallel with the capacitor. Moreover, there are other types of damping such as active damping or other types of passive damping, but we have chosen here the simplest case, namely the passive damping obtained by adding of the resistance in series with the capacitor. The RL load represents the consumption of our neighbors which are connected on the same grid as our system.

The *PVG* provides a continuous energy that will be converted into alternative form by the inverter before injecting it into the grid through the *LCL* filter. The *PVG* will not be studied here, it will therefore be replaced by a *DC* voltage source ( $V_{dc}$ ) which is the input voltage of the inverter. The system is controlled by a decoupled *PQ* control which is based on the Park transform, the current control in the Park frame, the decoupling of the direct and quadrature ( $I_{dq}$ ) components of the current and the grid voltage compensation. A Phase-Locked Loop (*PLL*) is used to synchronize the system with the utility grid. First, we are interested in the modeling and design of the *LCL* filter before returning to the analysis and control of the system.



Figure 1. Diagram of the grid-connected PV system and its control loop

#### 3. Modeling of the LCL filter

By replacing the *PVG* by the *DC* voltage ( $V_{dc}$ ), by ignoring the control scheme and the load RL, the diagram of figure 1 becomes that of figure 2. To simplify, we create a fictitious neutral "0" (midpoint) by dividing  $V_{dc}$ .



Figure 2. Simplified diagram of the system

The mathematical equations governing the behavior of this scheme are the following:

$$\begin{cases} V_{x0} = \frac{V_{dc}}{2}, \text{ if } K_{i} = 1 \text{ and } K_{i}^{'} = 0 \\ V_{x0} = -\frac{V_{dc}}{2}, \text{ if } K_{i} = 0 \text{ and } K_{i}^{'} = 1 \end{cases}$$
With  $x = a, b, c$  and  $i = 1, 2, 3$ 
(1)

## 4. Electrical design of the LCL filter

To simplify, we set :  $V_{xn} = V_1$ ,  $L_2 = L_{2f} + L_g$  et  $V_g = V_2$ . The simplified diagram of the *LCL* filter can be represented in single-phase as shown in figure 3. The internal resistances  $(R_1 \text{ and } R_2)$  are neglected in this diagram. Where,  $V_1$  is the line-to-phase inverter voltage and  $V_2$  is the line-to-phase grid voltage.



Figure 3. Topologie of the LCL filter

The transfer function of the LCL filter is given in (2) [6], which expresses the resonance pulsation ( $\omega_{res}$ ) and damping resistor  $R_f$  in (3).

$$H(s) = \frac{I_2(s)}{V_1(s)} = \frac{C_f R_f s + 1}{L_1 C L_2 s^3 + C(L_1 + L_2) R_f s^2 + (L_1 + L_2) s}$$
(2)

$$\begin{cases} \omega_{res} = \sqrt{\frac{L_1 + L_2}{L_1 C L_2}} \\ R_f = \frac{2z\omega_{res}L_1L_2}{L_1 + L_2} = \frac{2z}{\omega_{res}C} \end{cases}$$
(3)

Where  $\omega_{res}$  is the resonance pulsation  $(f_{res} = \frac{\omega_{res}}{2\pi})$ , z is the damping factor and s is the

Laplace variable.

In the literature, it is often mentioned that the resonant frequency must respect (4) in order for there to be stability of the system.

$$10 f < f_{res} < 0.5 f_{sw} \tag{4}$$

#### 4.1. Constraint of the reactive power variation and calculation of C

The value of the capacitor C is chosen so as to maximize the power factor [3]. For this purpose, the reactive power generated by this capacitor must be less than or equal to five percent of the rated active power of the installation  $(Q_c \leq 5\% \cdot P_n)$ . The reactive power formula is given in (5).

$$Q_{c} = C \cdot \omega \cdot U_{n}^{2}$$
Either the expression of a single capacitor:  

$$C_{max} = \frac{0.05 \cdot P_{n}}{2.2\pi f U_{n}^{2}}$$
(5)
(6)

Where  $P_n$  rated power, f grid frequency and  $U_n$  phase-to-phase grid rated voltage.

#### 4.2. Voltage drop constraint and determination of total inductance L

By neglecting the capacitor C, the voltage drop module is shown in (7).  $\Delta V_L = L \cdot \omega \cdot I$ (7)where L is the total inductance  $(L = L_1 + L_2)$ ,  $\Delta V_L$  is the voltage drop at this inductance, I the rated current and  $\omega$  is the grid pulsation ( $\omega = 2\pi f$ ). We admit  $\Delta V_L = 10\% \cdot V$  of voltage drop to satisfy the *IEEE*1547 standard [13].

$$I = \frac{P_n}{3 \cdot V}$$

$$L = \frac{10\% \cdot 3 \cdot V}{\omega \cdot P_n}$$
(8)
(9)

Where V is the line-to-phase grid rated voltage (V = 220 V).

#### 4.3. Constraints of current ripples

The maximum current ripple on the inverter side is generally chosen to be between 10% and 20% of the rated current, whereas the maximum grid ripple must be less than or equal to 0.3% [13].

$$10\% \cdot I \le \Delta I_{1m} \le 20\% \cdot I \tag{10}$$

$$\Delta I_{2m} \le 0.3\% \cdot I \tag{11}$$

In the simplified model, the three-phase grid voltage is denoted  $V_2$ . In reality, it is a three-phase voltage vector forming a balanced three-phase system that is regularly shifted by  $\frac{2\pi}{3}$ . If only one phase is considered (e.g. phase a), the formula of  $V_2$  is that of (12).  $V_2 = V\sqrt{2}\sin(\omega t)$  (12)

By considering (1), the curve of  $V_{a0}(t)$  is plotted in figure 4.



Figure 4. Evolution of the inverter voltage over time

The mean value of the inverter voltage is calculated in (13).  

$$V_{a0\_moy} = \frac{1}{T_{sw}} \int_0^{T_{sw}} V_{a0}(t) dt = \frac{V_{dc}}{2} [2 \cdot \alpha(t) - 1]$$
(13)  
The formula of the duty cycle is given in (14)  

$$\alpha(t) = \frac{1}{2} + \frac{m}{2} \sin(\omega t + \varphi)$$
(14)  
By injecting (14) into (13) we obtain (15).

$$V_{a0\_moy} = \frac{m \cdot v_{dc}}{2} \sin(\omega t + \varphi) \tag{15}$$

where  $\varphi$  is the phase shift between the grid voltage and the inverter voltage,  $T_{sw}$  is the switching period.

From (15), (16) is deduced.

$$V_{a0\_eff} = V_1 = \frac{V_m}{\sqrt{2}} = \frac{mV_{dc}}{2\sqrt{2}}$$
(16)

On the other hand, since the capacitor is very low  $(1.5 \,\mu\text{F})$ , the current passing through it  $(I_c)$  is negligible compared to current passing into the grid  $(I_2)$ . So by neglecting  $I_c$  in figure 3, the system can be represented in a Fresnel diagram as in figure 5  $(I_1 = I_2 = I)$ .



Figure 5. Fresnel diagram of the system connected to the network (phase a)

From figure 5, equation (17) can be written.

$$\underline{V_1} = \underline{V_2} + jL\omega I \tag{17}$$

$$|V_1| = V_1 = \sqrt{V_2^2 + (L\omega I)^2}$$
(18)  
Where  $V_2 = V$  is the rated grid voltage and j is the complex operator.

By using (16) and (18), we obtain (19).  

$$m = \frac{2\sqrt{2} \cdot \sqrt{V^2 + (L\omega I)^2}}{V_{dc}}$$
(19)

m is the depth of modulation.

By placing the expression of m of equation (19) in equation (15) we find (20).

$$\alpha(t) = \frac{1}{2} + \frac{2\sqrt{2} \cdot \sqrt{V^2 + (L\omega I)^2}}{2V_{dc}} \cdot \sin(\omega t + \varphi)$$

$$\varphi = \arctan\left(\frac{L\omega I}{V}\right)$$
(20)
(21)

We have already mentioned that we will opt for the calculation of current ripples by using the *FFT*. For this, figure 3 becomes figure 6 which takes account of admittances.



Figure 6. Modified diagram of the LCL (admittances)

By applying the Millman theorem, the formula of the common voltage  $(V_3)$  is given in (22).

$$V_3 = \frac{V_1 Y_1 + V_2 Y_2}{Y_1 + Y_2 + Y_3} \tag{22}$$

$$\begin{cases}
Y_1(\omega_h) = \frac{1}{jL_1\omega_h} \\
Y_2(\omega_h) = \frac{1}{jL_2\omega_h} \\
Y_3(\omega_h) = \frac{1}{R_f + \frac{1}{jC\omega_h}}
\end{cases}$$
(23)

Where  $\omega_h$  is the harmonic pulsation. The formula of currents ( $i_1$  and  $i_2$ ) taking into account all frequencies (fundamental and harmonics) are given in (24).

$$\begin{cases} i_{1}(\omega_{\rm h}) = \frac{V_{1} - V_{3}}{jL_{1}\omega_{\rm h}} \\ i_{2}(\omega_{\rm h}) = \frac{V_{3} - V_{2}}{jL_{2}\omega_{\rm h}} \end{cases}$$
(24)

The *FFT* of the current is done in (25).

$$\begin{cases} FFT(i_{1}) = \frac{FFT(V_{1}) - FFT(V_{3})}{jL_{1}\omega_{h}} \\ FFT(i_{2}) = \frac{FFT(V_{3}) - FFT(V_{2})}{jL_{2}\omega_{h}} \end{cases}$$
(25)

The system parameters are given in Table 1.

Symbol	Parameter	Value	Unit	
P <sub>n</sub>	Rated power	5.2	kVA	
I	Rated current	7.87	А	
V	Rated line-to-phase grid voltage	220	V	
Un	Rated phase-to-phase grid voltage	381	V	
V <sub>dc</sub>	DC voltage	750	V	
f <sub>sw</sub>	Switching frequency	20	kHz	
f	Grid frequency	50	Hz	
ω	Grid pulsation	$2\pi f = 100\pi$	rad/s	
$\Delta I_{1m}$	Maximum inverter current ripples	$20\% \cdot 7.87 = 1.57$	A	
$\Delta I_{2m}$	Maximum grid current ripples	$0.3\% \cdot 7.87 = 23.6$	mA	
$\Delta V_{Lm}$	Voltage drop	$\Delta V_{Lm} = 10\% \cdot 220 = 22$	V	
C <sub>m</sub>	Maximum capacitor	2	μF	
$L_T$	Total inductance	8.8	mН	
L <sub>1</sub>	Inverter side inductance	to be find	mH	
L <sub>2</sub>	Grid side inductance	to be find	mH	
Č	Optimal capacitor of the filter	to be find	μF	
R <sub>f</sub>	Damping resistance	to be find	Ω	

Table 1: Parameters of the grid connected PV system

In order to find the unknown elements of table 1, we must answer the following question. What are the optimal values of  $L_1$ ,  $L_2$  and C to respect the following constraints ?  $L = L_1 + L_2 \le 8.8$  mH,  $C \le 2$  µF,  $\Delta I_{1m} \le 1.57$  A et  $\Delta I_{2m} \le 23.6$  mA.

For this, we have written a Matlab program with which we plot the three-dimensional curves of the maximum grid current ripple ( $\Delta I_{2m}$ ) as a function of  $L_1$ ,  $L_2$  and C ( $R_f$  is neglected here), by varying  $L_1$  and  $L_2$  from 1mH to 8.8 mH for different values of C between 1 µF and 2 µF. Only the standardized values of unpolarized capacitors (*E*12) are considered here. The Matlab program indicates that the best case is where  $C = 1.5 \mu F$  and two symmetrical values of  $L_1$  and  $L_2$  (3 mH, 3.5 mH) or (3 mH, 3.5 mH) as shown in figure 7 (X corresponds to à  $L_1$ , Y corresponds to  $L_2$  and Z corresponds to  $\Delta I_{2m}$ ).



Figure 7. Grid current ripples  $\Delta I_{2m}$  vs  $L_1$ ,  $L_2$  and C

At this level, it is not possible to know which of  $L_1$  or  $L_2$  should be preferred. To find out, the curve of the maximum inverter current ripples  $(\Delta I_{1m})$  is plotted in figure 8 (here, X corresponds to  $L_1$ , Y corresponds to  $L_2$  and corresponds to  $\Delta I_{1m}$ ).



Figure .8 Inverter current ripples  $\Delta I_{1m}$  vs  $L_1$ ,  $L_2$  and C

According to figure 8, the maximum inverter current ripple is lower ( $\Delta I_{1m} = 1.492 \text{ A}$ ) when  $L_1 = 3.5 \text{ mH}$  and  $L_2 = 3 \text{ mH}$  than when  $L_1 = 3 \text{ mH}$  and  $L_2 = 3.5 \text{ mH}$  ( $\Delta I_{1m} = 1.743 \text{ A}$ ). On the other hand, the maximum grid current ripple is the same in both cases ( $\Delta I_{2m} = 22 \text{ mA}$ ). Therefore, the optimal values of the *LCL* filter parameters are :  $L_1 = 3.5 \text{ mH}$ ,  $L_2 = 3 \text{ mH}$  and  $C = 1.5 \mu\text{F}$ .

With these values, we find  $\omega_{res} = 20315 \text{ rad/s}$  and  $f_{res} = 3233 \text{ Hz}$ .

500Hz < 3233 Hz < 10000 Hz. The stability condition of equation (6) is satisfied.

To determine  $R_f$ , we vary z between [0, 1] using (3) and we find table 2.

Damping factor z	<b>Damping resistance</b> $R_f(\Omega)$
0	0
0.0588	3.86
0.166	10.89
0.707	46.4
1	65.63

Table	2:	Dam	ping	resistance	val	lue
	<b>-</b> ·		D			

Then, we tested these different values (see table 2) and we found that the optimal value of the damping resistance is  $R_f = 3.86 \Omega$ . Because this value does not modify the current ripples. Figures 9 and 10 show the ripples of the grid current and inverter current



respectively, when  $R_f$  is taken into account. We find practically the same values when we neglected  $R_f$ .

Figure 9. Grid current ripples  $\Delta I_{2m}$  vs  $L_1$ ,  $L_2$ , C and  $R_f$ 



Figure 10. Inverter current ripples  $\Delta I_{1m}$  vs  $L_1$ ,  $L_2$ , C and  $R_f$ 

The Bode diagram of the *LCL* filter is then shown in figure 11. Figure 11 shows that the insertion of the resistance  $R_f$  in series with the capacitor made it possible to suppress the peak due to the resonance phenomenon (curve in red).



Figure 11. Bode diagram of the undamped LCL filter ( $R_f = 0 \Omega$ ) and damped LCL filter ( $R_f = 3.86 \Omega$ )

#### 5. Magnetic design of the filter inductances

Knowing the values of the passive components  $L_1$  and  $L_2$ , we are interested in the magnetic design which consists in determining the magnetic core, the number of turns, the air gap, joules losses, iron losses and the temperature evaluation of each inductance. Our magnetic design method is based on the areas product method presented in [15]. The design method is summarized in the flowchart (see figure 12) gives the results of table 3. These results are obtained using a Matlab program.

Symbol	Parameter	Value	Unit	
N <sub>1</sub>	Number of turns of inductance $L_1$	81		
$N_1$	Number of turns of inductance $L_2$	71		
e <sub>1</sub>	Air gap of inductance $L_1$	4.3	mm	
e <sub>1</sub>	Air gap of inductance $L_2$	3.3	mm	
$P_{i1}$	Joule losses in inductance $L_1$	14.24	W	
P <sub>i1</sub>	Joule losses in inductance $L_2$	10.98	W	
$P_{f1}$	Iron losses in inductance $L_1$	11	kW	
$P_{f2}$	Iron losses in inductance $L_2$	10.9	kW	
R <sub>1</sub>	Winding resistance of $L_1$	0.46	Ω	
$R_1$	Winding resistance of $L_2$	0.36	Ω	
$\Delta T_1$	Temperature difference in $L_1$	57	C°	
$\Delta T_2$	Temperature difference in $L_2$	52	C°	

Tal	ble	53	3: ]	Inc	luctance	e pa	aram	neters	des	igı	1

In hot countries like Chad,  $T_{max} = 100$  °C and  $T_{amb} = 40$  °C can be considered. This gives  $\Delta T = 60$  °C.

According to table 3,  $L_1$  is designed to operate at ambient temperature  $T_{amb1} = 43$  °C  $(T_{amb1} = T_{max} - \Delta T_1)$  and  $L_2$  at the ambient temperature  $T_{amb2} = T_{max} - \Delta T_2 = 48$  °C. So these inductances are well designed to operate in Chad.

When we choose the cores for inductances  $L_1$  and  $L_2$ , we found that only the ferrite core *PM*114 [16] is suitable. Because it has a areas product ( $A_p = 1840400 \text{ }mm^4$ ) greater than

those calculated ( for  $L_1$ ,  $A_{pL1} = 829800 \text{ mm}^4$  and for  $L_2$ ,  $A_{pL2} = 640000 \text{ mm}^4$ ). However, this core costs too much (176.90 euros, at Distrelec) and are too bulky ( $V_{pm114} = 334000 \text{ mm}^3$ ). In order to reduce the manufacturing cost and the volume of the passive components ( $L_1$  and  $L_2$ ), we said why not split each inductance and realize it in several small inductances in series? In this case, the optimum in terms of volumes is found when each inductance is divided by two and two *PM*87 cores are chosen for  $L_1$  and two *PM*74 cores for  $L_2$  as shown in figure 13. On the other hand, the *PM*87 core costs 63 euros and the *PM*74 costs 68 euros. So by dividing the inductances and choosing two small cores, there is a gain of 50.9 euros for  $L_1$  and 34.9 euros for  $L_2$  for one inductance. For three phase *LCL* filter, the cost is multiplied by three.



Figure 12. Flowchart of the design procedure of  $L_1$  and  $L_2$ 



Figure 13. Impact of core choice on inductances volume

We can see in figure 13 that, at the optimum, the volume of the inductance  $L_1$  is equal to :  $Volume_1 = 2 \cdot V_{PM87} = 266000 \text{ mm}^3$  and the volume of  $L_2$  is equal to :  $Volume_2 = 2 \cdot V_{PM74} = 202000 \text{ mm}^3$  [16].

# 6. Simulations results and discussion6.1. Simulations results

Now that the *LCL* filter elements are known, we can look at the control of the system and its analysis taking into account the impact of the consumption of our neighbors. The system control diagram is shown in figure 1. It is reported that the photovoltaic generator (PVG) is not studied in this paper, it has been replaced by a continuous voltage  $(V_{dc})$  which is the supply voltage of the inverter. The parameter setting  $(k_p \text{ and } k_i)$  of the PI controllers are shown in [17].

To test the control, we impose an active power reference equal to five point two kilowatts ( $P^* = 5.2$  kW) and the reactive power reference is equal to zero ( $Q^* = 0$  VAR). The consumption of our neighbors is modeled here by a three-phase load RL which consumes active power.

Thus, the following profile is considered:

- at  $t \in [0 \ 0.5]s$ , the *RL* load does not consume any power of our system,
- at  $t \in [0.5 \ 1]s$ , the *RL* load consumes a part of power of our system.

The simulation results of the control are shown in figures 14, 15, 16, 17 and 18.





Figure 15. Reactive power variation





Waveform of the three phase injected current vs time 50 40 30 20 Current (A) 10 0 -10 -20 -30 -40 -50 L 0.1 0.2 0.3 0.4 0.5 0.6 0.7 0.8 0.9 1 Time (s)

Figure 17. Wave form of the injected grid current



Figure 18. Synchronization of the system by PLL

#### 6.2. Discussion

Figure 14 shows that when the active power of the load is equal to zero ( $P_{load} = 0 W$ ) in the time interval [0 0.5]s, the grid active power and the inverter active power are identical ( $P_{arid} = P_{inv} \approx 5.2$  kW). This means that all the power produced by our system is injected into the grid. But when the power of the RL load is not null ( $P_{load} = 3 \text{ kW}$ ) in the time interval [0.5 1]s, some of our power supplies the RL load and the rest of the power (2.2 kW) is injected into the grid. In figure 15, it can be seen that when the reactive power is equal to zero ( $Q_{load} = 0$  VAR) in the time interval  $[0 \ 0.5]s$ , our system does not inject any reactive power on the grid ( $Q_{grid} = Q_{inv} = 0$  VAR). But when the load consumes power, in the interval [0.5 1] s, it also generates reactive power that will be injected into the grid. This is why the reactive power of the grid is slightly negative ( $Q_{grid} < 0$ ) in this interval. Figures 16 and 17 show the grid voltage and current waveforms respectively. It can be noted that the voltage and current fluctuations due to the RL load are not too pronounced. Indeed, when the neighbors start to consume from our system (in the time interval [0.5 1] s), this results in a slight drop in voltage and a slight increase in the current in our system. However, the behavior of the transients at time t = 0.5 s is very interesting (so the LCL filter is well designed).

Figure 18 shows the superposition of the injected current on the grid  $(I_g = I_2)$  and the grid voltage (for one phase). It can be seen that the two curves are in phase and have the same frequency (50 Hz). Therefore, we say that our system is synchronized on the grid despite the interaction of the consumption of the neighbors on our system (at t = 0.5 s).

#### 7. Conclusion and perspectives

This paper dealt with an optimized design method of an *LCL* filter for grid connected *PV* system and an analysis of the impact of the neighbor's consumption on this system. Our design complies with the *IEEE*1547standard for interconnection to the grid in terms of voltage drop, current ripples, variation in power factor (variation in reactive power) and frequency variation. The used technique to fragment the inductances with two inductances in series seems to show a gain in volume and manufacturing cost of the filter. The used

control has fulfilled its function of tracking of the references and system synchronization, when the RL load varies.

However, even if our system doesn't generate reactive power to the grid, the used control currently cannot compensate the reactive power generated obviously by the neighbours. In the future, it would be interesting to imagine a smart system that could detect reactive power at the connection point and compensate it in order to participate in a system service.

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