Normalized thermal stresses analysis to design a thermal fatigue experiment

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This paper summarizes the thermal fatigue testing conditions that can be found in the literature about shape-forming tools. The importance of the local geometry of the tools is discussed. The key point of the study is to demonstrate that a reproduction of thermal fatigue conditions must take into account a size effect: the same apparent thermal shock does not have the same effect in a large, thick tool as it has in a small, thin laboratory specimen. This paper proposes a method to evaluate what kind of thermal shock to perform on the laboratory specimen to replicate a thermal shock observed in the large and thick tool. A global method of design of a thermal fatigue experiment is given for a cylindrical specimen, provided that the maximum temperature, maximum thermal stresses, and the corresponding time in the cycle have been previously determined. A method to determine the required data is proposed. A definition of the intensity of the thermal shocks is proposed and damages on specimen surfaces are illustrated with regard to that definition.

**Keywords** fatigue testing, thermal fatigue, thermal stresses, thermomechanical fatigue, tool steels, tools, transient heat transfer

Industrial tools, such as forging matrixes, casting dies, glass molds, or hot rolling rolls, are well known to suffer from repeated transient thermal loading and to damage under thermal fatigue mode. This results in the appearance of cracks on the surface of the tools. Depending on the forming process, these cracks may be left free to propagate deep into the bulk of the tool. For instance, tools for the glass pressing industry are no longer used as soon as a few cracks longer than a few millimeters appear on the surface. In the die casting industry, the tolerance of the process to crack development can be much larger and the die casters may wait until a biaxial network of cracks develops on a large scale of the surface. A network, as can be seen in Figure 1b, is called “heat checking.” Because forming processes are concerned
with shaping a part, the shape of the dies are usually not simple and one often finds uniaxial crack networks such as that shown in Figure 1a. These cracks, usually associated with a geometrical singularity that acts as a stress riser, can be avoided or at least delayed by a smart modification of geometrical features, such as fillet radius. Optimization of the design can be performed with CAD software, based on the reduction of thermomechanical loading during the forming operation. Nevertheless, forming tools still heat-check in their flat areas. It has been observed, for instance, that high-pressure die casting (HPDC) dies tend to form heat checking next to the gates and in the thickest cavities even when perfectly flat. The heat checking in these areas proves to be just as limiting as the geometrical singularities.

The present paper is, therefore, concerned with the investigation of heat checking in those flat areas of industrial tools. Because cracks interfere with the processes

Figure 1. Network of cracks, in (a) a cast iron gravity casting die and (b) an aluminum HPDC die.
at an early stage of their development, the life of tools is not necessarily limited by a crack propagating deep into a tool. A few millimeters depth is usually sufficient to create a defect on an aesthetic product or to reduce drastically the productivity of a machine. The study of the initiation stage of heat checking is, therefore, of industrial relevance as well as of scientific interest.

To study the initiation stage of a crack network on a die, a laboratory test must be performed. Since the late 1950s, many thermal fatigue (TF) tests have been proposed. The geometry of the specimen and the type of heating have varied considerably from one author to another as follows: square specimen [1,2], wedged specimen [3–8], cylindrical specimen [9–16]; inductive heating [6,13–16], fluidized bed [4,10], dip into an aluminum melt [1,2] or flame [8,17].

The size of the specimen and the heating capacity vary greatly from one author to the other and are basically dictated by the available facilities. As a consequence, the results can differ from one test to another (e.g., the classification of materials is different among [1,2,15,16]). One of the major issues is the comparison of the results from one laboratory to another and, more important, the comparison with the industrial tools. Our analysis shows that the thermomechanical loading is not comparable from one to another, and such a comparison has never been done. Indeed most of the papers on TF compare different materials in given conditions instead of evaluating the effect of process parameters on the thermal fatigue.

The reasons why tools or TF specimens alter are linked to temperature and to thermomechanical loading that are imposed to their heated surfaces. Since the study of quenching-induced stresses [18] reported by Boley and Weiner [19], it has been well known that thermal stresses strongly depend on the thickness of the quenched parts: the thicker the parts, the larger the thermal stresses for the same heat transfer condition (same quenching medium). One can talk about a size effect: the same thermal loading will induce different thermal stresses on a thick industrial tool compared to a thin experimental specimen. As a consequence, it is necessary to take into account this scale effect to design TF lab specimens in order to reproduce the TF of an industrial tool. This is the main topic of the present paper.

In the following it will be considered that a flat tool (say, a slab) is accurately instrumented (e.g., see [20–22]) to know the temperature field \( T(z,t) \) as a function of time \( t \) and depth \( z \). From this it is possible to evaluate the thermomechanical field of the tool \( \sigma(z,t) = \sigma_{xx}(z,t) = \sigma_{yy}(z,t) \), using either elastic body equations [19,23,24], elastoplastic, or even elastoviscoplastic equations. To design a TF rig (e.g., specimen in Figure 2) that will become damaged in the same manner as the reference tool, the same loading has to be reproduced. The loading on the surface should be relevant enough in a TF study on the crack initiation and propagation. In this investigation, the attention is focused on crack initiation and propagation on the surface. However, the definition of the loading remains delicate. The thermomechanical loading consists of both the temperature and stresses (or strains) as functions of the time. As far as temperature is concerned, the replication criterion is simple; a relevant test should reproduce the same temperature history of the surface \( T(z = 0, t) \) of the tool to the surface of the specimen (e.g., \( T(\phi_1, t) \) for the cylinder Figure 2). Where stresses or strains are concerned, the situation is far more complicated:
1. Which mechanical loading should be considered to simulate tool loading?
2. Simulate plastically relaxed stresses or the elastic body stresses?
3. Measure in terms of deformation, the total deformation, the elastic deformation, or the plastic deformation?
4. Or measure in terms of energy, the total loop energy, or the plastic loop energy?

The choice is delicate considering that the damage criteria (stress, strain, energy, etc.) are not yet a generally accepted rule in TF. The origin of all the stresses and mechanical strain is the incompatibility of thermal expansion when a part is heated or cooled with a nonuniform temperature. A lattice distortion of the crystal network is induced to accommodate the incompatibility of thermal expansion. The lattice distortion comes together with the so-called thermal stresses of the elastic body. However, the elastic-body thermal stresses are often high enough to push dislocations to motion, inducing some plastic deformation. Evidently, this event is favored if the temperature is high. (Dislocation flow is a function of the temperature, applied stress, etc. [25].) As a consequence, the elastic-body thermal stresses and the temperature taken together can be seen as the potential that measures the tendency of the material to deform plastically. In other words, they can be seen as the driving forces of the reaction of the material to the thermal loads, and to some extent of the damage of the tool.

As a consequence, the objective of a relevant TF rig design should be to reproduce the same driving forces (temperature and elastic-body thermal stresses) applied to the surface of the reference tool, on the surface of the TF specimen. To account for the size effect between the thick reference tool and the small laboratory specimen, normalization of the heat conduction and elastic-body thermal stress equations are needed. A discussion about the size effect and time follows along with a method for dimensioning a TF experiment.
NORMALIZED TRANSIENT THERMAL STRESSES IN SLAB AND CYLINDRICAL GEOMETRY

To account for the scale effect of the reference tool (slab) and of the lab specimen (see Figure 2), a normalization transformation of the heat transfer and of the equations for thermal stresses is a promising approach. General equations are addressed for a slab geometry and then for a cylindrical geometry. Hereafter the (\( + \)) indicates the normalized variables of the problem.

Normalized Thermal Stresses in a Slab

In a previous paper [23], the normalization of thermal stresses generated in a slab heated on one face and cooled down on the other face was proposed. The slab was considered an elastic body with constant physical properties and was free to buckle. The equations under concern were the heat conduction along the thickness \( z \) of the slab and the classical thermal stresses equation [19]. The heated face of the slab is subjected to a heat flux density \( \phi_{\text{max}} \) during a time \( \tau \), while the opposite face is cooled down by a cooling fluid characterized by the heat transfer coefficient \( h \) and its average temperature \( T_\text{fl} \) (set to zero as the initial temperature of the slab for the sake of simplicity). The normalization of the equations was made with the variables \( \phi_{\text{max}}, \tau \) and \( L \), where \( L \) is half the thickness of the slab. Equations (1)–(6) describe how the time, the depth into the slab, the heat flux density on the heated face, the heat transfer coefficient on the cooled face, the temperature, and the thermal stresses are transformed, respectively. It should be noticed that an equivalent temperature is used, based on the ratio \( \phi_{\text{max}} L / k \):

\[
\begin{align*}
t^+ &= \frac{\kappa t}{L^2} \quad & (1) \\
z^+ &= \frac{z}{L} \quad & (2) \\
h^+ &= \frac{hL}{k} \quad & (3) \\
\phi^+(t^+) &= \frac{\phi(t)}{\phi_{\text{max}}} \quad & (4) \\
T^+(z^+, t^+) &= \frac{T(z, t)}{\phi_{\text{max}} L} \quad & (5) \\
\sigma^+(z^+, t^+) &= \frac{\sigma(z, t)}{E z \phi_{\text{max}} L} \quad & (6)
\end{align*}
\]

where \( \kappa \) is the heat diffusivity of the slab, \( k \) is the heat conductivity of the slab, \( z \) denotes the ordinate along the thickness of the slab, \( L \) is half of the slab thickness,
\( h \) is the heat transfer coefficient at the back of the slab (cooled face), and \( \phi \) and \( \phi_{\text{max}} \) denote heat flux density input at the front of the slab.

With that set of transformed variables, the thermal stresses expression reduces to a single equation, Eq. (7), in which the only parameter is the heat transfer coefficient \( h^+ \):

\[
\sigma^+(z^+, t^+) = \left[ -T^+(z^+, t^+) + \frac{1}{2} \int_0^2 T^+(z^+, t^+) \, dz^+ \
+ \frac{3}{2}(z^+ + 1) \int_0^2 (z^+ + 1) T^+(z^+, t^+) \, dz^+ \right]
\]

(7)

More details about the equations and illustration of the effect of \( h^+ \) may be seen in the literature [23].

**Normalized Thermal Stresses in a Cylindrical Geometry**

The problem of thermal stresses in a cylinder is a classical plane-strain problem [19,24]. The heat conduction along the radius only is considered. The outer radius \( R_2 \) is subjected to a heat flux density \( \phi_{\text{max}} \) during a time \( \tau \). The inner radius \( R_1 \) is cooled down by contact with a cooling fluid characterized by the same couples \( h \) and \( T_{fl} \) (set to 0). The whole set of equations can be normalized with the same set of transformations: Eqs. (1)–(6). The characteristic length \( L \) can be chosen as the minimum radius \( R_1 \), the maximum radius \( R_2 \), the thickness \( Ep = R_2 - R_1 \), the average radius of the cylinder, and so on. In the following, the maximum radius \( R_2 \) will be chosen to be the characteristic length, because our practice with the specimen in Figure 2 is to modify the inner radius and keep the outer radius constant. This allows us to work with the same heating equipment from one specimen to the other.

After normalization, the transient thermal stresses can be written as follows:

\[
\sigma_{rr}^+(r^+, t^+) = -\frac{1}{r^{+2}} \left[ \frac{(1 - Ep^+)^2 - r^{+2}}{(1 - Ep^+)^2 - 1} \int_{1-Ep^+}^1 r^{+} T^+(r^+, t^+) \, dr^+ \
+ \int_{1-Ep^+}^{r^+} r^{+} T^+(r^+, t^+) \, dr^+ \right]
\]

(8)

\[
\sigma_{\theta\theta}^+(r^+, t^+) = \frac{(1 - Ep^+)^2 + r^{+2}}{r^{+2}} \int_{1-Ep^+}^1 r^{+} T^+(r^+, t^+) \, dr^+ 
+ \frac{1}{r^{+2}} \int_{1-Ep^+}^{r^+} r^{+} T^+(r^+, t^+) \, dr^+ - T^+(r^+, t^+)
\]

(9)

\[
\sigma_{zz}^+ = v \cdot (\sigma_{rr}^+ + \sigma_{\theta\theta}^+) - (1 - v) \cdot T^+
\]

(10)

which stands for the plane-strain condition \( \varepsilon_{zz}^+ = 0 \), where \( Ep^+ = Ep/R_2 \) is the normalized thickness of the cylinder.
Compared with the slab geometry, the normalized stresses depend on one more parameter: the thickness $E_p h$. Figure 3 shows the thermomechanical path $\sigma_{\theta \theta}$ and $\sigma_{zz}$ vs. $T^+$ for the heated surface for cylinders with different $E_p$ and $h^+$.

A few facts are worth noting with regard to the curves in Figure 3.

i. For the short times ($t^+ < 0.04$), the curves are all similar. Later, the evolution can follow three different tendencies:

Steady thermomechanical state: both the stress and the temperature reach a steady value, such as the $(\sigma_{\theta \theta}, T^+)$ curves for the large $h^+$.

Steady stress but transient temperature: the stress reaches a steady value while the temperature keeps increasing; see the $(\sigma_{\theta \theta}, T^+)$ curves for the small $h^+$.

In fact, the temperature field through the thickness of the cylinder stays the same but translates to higher temperatures, leading to a steady stress but not steady temperatures.

Transient temperature and stress; see the $(\sigma_{zz}, T^+)$ curves.

ii. The maximum of stresses (in absolute value) occurs at the different normalized times for the different thicknesses. The reason is that the maximum stresses are attained when the heat wave reaches the inner radius of the specimen ($R_1$), as explained by Dour [23]. This time is roughly proportional to $E_p^2/\kappa$, or $E_p^{+2}$ in terms of normalized time.

iii. The stress at the surface of the cylinder is not, strictly speaking biaxial for the long time ($t^+ > 0.04$) because $\sigma_{\theta \theta}$ and $\sigma_{zz}$ are not equal. This is clearly seen in Figure 3 when the temperature is high and $\sigma_{\theta \theta}$ reaches a steady value, whereas $\sigma_{zz}$ keeps increasing. This is understandable when one considers the plane-strain condition: the displacement in the $z$ direction is zero, leading to stresses roughly equal to $-E\kappa T(R_1)$ for the long times.

iv. There are two different regimes for the long times.

v. For large times (larger than 0.1), the stresses are strongly dependent on the heat transfer coefficient $h^+$, whereas for small times, the stresses are very similar.

From a practical point of view, this means that TF tests in the long time range must be performed with an accurate control of the cooling conditions. This is not an easy task, because it depends on the type of fluid flow, the surface roughness, and, moreover, the limestone deposition in “hard water” countries. On the contrary, a TF test working in the short time range can be performed with a less-accurate cooling control. It is, therefore, advisable to work in the short time conditions, where the heat transfer coefficient has a negligible influence on the applied driving forces.

APPLICATION OF THE NORMALIZATION TO THE DESIGN OF A TF TEST

Based on the normalized analysis of the first paragraph, two design examples are given. In the first, the geometry is kept the same (slab) and the design accounts for only the scale effect. The whole temperature and thermal stresses field replication
Figure 3. Thermal stresses history of the heated face of a cylinder. The dots correspond to times incremented every 0.02 units of normalized time.
is discussed. The second example consists of replicating the temperature and the thermal stresses of the working face of the reference tool on the outer radius of the specimen (Figure 2).

From a Slab Tool to a Slab Specimen: Pure Scale Effect

In the following, the thickness of the reference slab is $2L$ and the thickness of the laboratory specimen is $2L'$. The downscaling ratio is called $A$ and is defined as $L = A \cdot L'$, where $A$ is typically 10 to 100.

A perfect reproduction of both the temperature and the thermal stresses at the lab scale means obtaining stresses $\sigma'$ and temperatures $T'$ at a location $z'$ in depth and at the time $t'$ that satisfy the following:

$$\sigma'(z' = z/A, t' = t) = \sigma(z, t)$$

$$T'(z' = z/A, t' = t) = T(z, t)$$

Considering Eqs. (1) and (2), it is clear that the perfect replica is not possible. If the factor $A$ was applied to the thickness, the square root of $A$ should be automatically applied to the time. The only way to obtain a perfect reproduction is to set $A$ to 1.

The best way to reproduce the temperature and the thermal stresses involves changing the duration of the test, or the frequency of the fatigue test. This is what will be called the “homothetic” replica. When the slab thickness is reduced by a factor of $A$, the time is reduced by the factor $A^2$. Reproducing stress and temperature is then relatively easy if the heat flux density $\phi_{\text{max}}'$ is $A$ times $\phi_{\text{max}}$. The thickness $L$ and the heat flux density are indeed multiplied in Eqs. (5) and (6). Table 1 summarizes the conditions of the homothetic downscaling.

Such a reduction may seem easy to perform; however, multiplying the heat flux density may become a technical issue when one faces industrial scale (see, for instance, HPDC [26–29]) with 1 to 50 MW/m$^2$ during 100 ms. Applying 10 to 500 MW/m$^2$ for $A = 10$ during only 1–10 ms requires a huge and robust power supply (even for a few square centimeter test rig). As an example, for a rig with a surface area of 17 cm$^2$, a generator of 15–850 kW would be necessary. Moreover, it must be able to deliver its maximum power within a few milliseconds accurately. Technically speaking, this is not an easy task.

<table>
<thead>
<tr>
<th>Condition</th>
<th>Industrial scale</th>
<th>Laboratory scale</th>
</tr>
</thead>
<tbody>
<tr>
<td>Thickness, depth</td>
<td>$L$, $Z$</td>
<td>$L' = L/A$, $z' = z/A$</td>
</tr>
<tr>
<td>Heat flux density</td>
<td>$\phi_{\text{max}}$</td>
<td>$\phi_{\text{max}}' = A \cdot \phi_{\text{max}}$</td>
</tr>
<tr>
<td>Time</td>
<td>$t$</td>
<td>$t' = t/A^2$</td>
</tr>
<tr>
<td>Stress</td>
<td>$\sigma(t, z)$</td>
<td>$\sigma'(t', z') = \sigma(t, z)$</td>
</tr>
<tr>
<td>Temperature</td>
<td>$T(t, z)$</td>
<td>$T'(t', z') = T(t, z)$</td>
</tr>
</tbody>
</table>
From a Slab Tool to a Cylindrical Specimen

For practical reasons, it is often preferred to run a TF test on a cylindrical tube with induction heating. One of the reasons that hollow tubes are commonly used \[14,30,31\] is that the thickness is a parameter that influences the mechanical load. It is possible to adjust the mechanical loading without changing the temperature; it only requires changing the thickness. In our group we are now used to changing the inner radius of the specimen for a constant exterior radius (see Figure 2). Then none of the heating conditions have to be changed \[12\]. This is the reason we chose \(R_2\) as the characteristic length in Eqs. (8)–(10). Inductive heating is used because it is one of the most efficient ways to rapidly heat a metallic specimen on the scale of several square centimeters.

When the geometry is modified from the reference tool to the TF rig, it is obviously impossible to replicate the entire temperature and thermal stress field. The replication of the two driving forces has to be focused on the surface only. Nevertheless, the following equations show that it is possible to reproduce them at the same time, which prevents any frequency effect on the damage prediction when plastic fatigue condition prevails. In order to do so, the following method has been proposed:

i. Measure or collect information about the material’s key parameters (\(E, \alpha, \nu, \kappa, \kappa\)).

ii. It is assumed that the working conditions of the reference tool have been determined. In particular, the maximum stresses \(\sigma_{\text{max}}\) and maximum temperature \(T_{\text{max}}\) are recorded to occur at time \(\tau\).

iii. From Eqs. (5) and (6), the following equation is obtained:

\[
\frac{T^+(r^+, t^+)}{\sigma^+(r^+, t^+)} = \frac{T(r, t)}{\sigma(r, t)} \frac{E\alpha}{1 - \nu} \tag{11}
\]

This equation can be applied for \(r = R_2\) at the surface of the TF specimen (i.e., \(r^+ = 1\)) and for time \(\tau\) (the same as identified on the reference tool) when the driving forces must be at their peak values. The nonnormalized stresses and temperature should then be \(T_{\text{max}}\) and \(\sigma_{\text{max}}\) as identified on the reference tool:

\[
\frac{T_{\text{max}}^+}{\sigma_{\text{max}}^+} = \frac{T_{\text{max}}}{\sigma_{\text{max}}} \frac{E\alpha}{1 - \nu} \tag{12}
\]

iv. Identify the ratio \(T_{\text{max}}^+/\sigma_{\text{max}}^+\) on the chart in Figure 4 (see the horizontal line) using the second team of Eq. (12) with the maximum temperature, maximum stresses, and the materials data.

v. At that point it is necessary to choose the normalized thickness \(E\rho^+\) of the tube and the relative heat transfer coefficient \(h^+\). This means choosing one of the curves. Where the chosen curve crosses the horizontal line (when it does), the time \(\tau^+\) reads as the normalized time that should be used on the lab specimen to reproduce the real time \(\tau\) on the industrial tool.
Figure 4. Chart of the ratio $T^+/\sigma^+\text{vs.} \ t^+$ involving (a) the hoop stress $\sigma_{\theta\theta}$ and (b) the axial stress $\sigma_{zz}$ for a hollow tube.
vi. To obtain the same time on the lab specimen as on the actual part, the reference length $R_2$ must satisfy Eq. (1), which leads to Eq. (13):

$$R_2 = \sqrt{\frac{k\tau}{\tau^+}}$$  \hspace{1cm} (13)

vii. From the chart found in Figure 3, it is now possible to determine $T^+_{\max}$ and $\sigma_{\theta\theta}^+_{\max}$ at the instant $\tau^+$.

viii. The heat flux density that is needed to perform such a TF test is given by Eq. (14) and the power supply that is needed for a tube of length $Z$ is given by Eq. (15):

$$\phi_{\max} = \frac{T^+_{\max} k}{T^+_{\max} R_2} \quad \text{or} \quad \phi_{\max} = \frac{\sigma_{\max} 1 - \nu k}{E\alpha L}$$  \hspace{1cm} (14)

$$P = 2\pi R_2^2 Z \phi_{\max}$$  \hspace{1cm} (15)

From the chart in Figure 4, one may arrive at the following conclusions.

i. When the inner radius is thermally insulated ($h^+$ is small), the absolute ratios for the ortho-radial stress component continue to increase during heating. This is understandable, because Figure 3 shows that thermal stress $\sigma_{\theta\theta}^+$ tends to a steady value while the temperature keeps increasing. The trend is different for the ratio with the axial stress component, because the thermal stress tends to increase proportionally to the temperature.

ii. When $h^+$ is large, the curves $T^+/\sigma^+$ reach a steady value, because both stress and temperature tend to finite values. This applies for both axial and hoop stress components, but the limit values are not the same.

iii. The slopes at the origin are different if the thicknesses are different. This confirms that, in nonperfect contact condition, the size influences the thermal stresses.

iv. When the heat transfer coefficient $h^+$ is small, the absolute ratio is a decreasing function of the thickness $Ep^+$. The contrary applies when the heat transfer coefficient is large, at least for long times. This means that a classification of the TF results as a function of thickness can be changed whether the cylinder works in high or low internal heat transfer conditions and for long or short times. The reason for this reverse order can be understood in that, in high internal heat transfer, the global temperature gradient through the thickness is forced by $h^+$. In this condition, the thicker the tube, the lower the gradient and the smaller the stresses. On the contrary, when the transfer coefficient is small, the global temperature gradient is controlled by the thermal inertia of the tube. Thus, the thicker the tube, the larger the gradient and then the larger the thermal stresses.

v. The absolute ratio is always larger than 1. The value 1 appears as a limit value that can be obtained only for extremely short times, whatever the thickness of the tube. This fact corresponds to the limit case of no penetration of the heat wave, such as in the beginning of the perfect contact condition. It
follows from this that it will be impossible to set a stress larger than that of Eq. (16) at a given time. To achieve such a stress, an infinitely large heat flux density is required and the targeted temperature $T$ would be reached in an extremely short time. This corresponds to the situation described by the perfect contact between a part whose initial temperature is set to 0 and a perfectly stirred fluid at temperature $T$, as described by Boley and Weiner [19]. If fact, the inverse of the absolute ratio appears to be a measure of the intensity of the thermal shock:

$$\sigma_{\theta\theta,\text{lim}} = \sigma_{zz,\text{lim}} = -\frac{E\alpha}{1 - \nu} T$$

In conclusion, the cylindrical geometry will not be able to create stresses higher than the perfect contact thermal stresses. Therefore, thermal stresses due to geometrical singularities, where stress concentration factors apply, cannot be handled by such a test.

Table 2 presents results inspired from some examples that have been studied in the CROMeP research center. The lab specimen is 40 mm long. The material is the AISI H11 steel, whose physical properties are $E/(1 - \nu) = 260$ GPa and $\alpha = 1.3 \times 10^{-5}$ $\text{K}^{-1}$ and thermal properties are $k = 30 \text{Wm}^{-1}\text{K}^{-1}$ and $\kappa = 8 \times 10^{-6} \text{m}^{2}\text{s}^{-1}$ [12].

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Targeted values</th>
<th>Experimental conditions</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\Delta T$ ($^\circ\text{C}$) or $T^+$</td>
<td>400$^\circ\text{C}$</td>
<td>0.053</td>
</tr>
<tr>
<td>$\sigma$ (MPa) or $\sigma^+$</td>
<td>1 200 MPa</td>
<td>-0.047</td>
</tr>
<tr>
<td>$\tau$ ($\sigma$) or $\tau^+$</td>
<td>1 s</td>
<td>0.00269</td>
</tr>
<tr>
<td>$T^+/\sigma^+$ absolute ratio</td>
<td>1.126</td>
<td>1.126</td>
</tr>
<tr>
<td>$R_2$</td>
<td>54.5 mm</td>
<td>36 mm</td>
</tr>
<tr>
<td>$E_p$ (mm) or $E_p^+$</td>
<td>0.66</td>
<td>4.12 MWm$^{-2}$</td>
</tr>
<tr>
<td>$P$ (W)</td>
<td>56.4 kW</td>
<td></td>
</tr>
</tbody>
</table>

(a) Very strong thermal shock ($T^+/\sigma^+$ close to 1)

(b) Very weak thermal shock ($T^+/\sigma^+$ close to 3)

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Targeted values</th>
<th>Experimental conditions</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\Delta T$ ($^\circ\text{C}$) or $T^+$</td>
<td>500$^\circ\text{C}$</td>
<td>0.286</td>
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<tr>
<td>$\sigma$ (MPa) or $\sigma^+$</td>
<td>500 MPa</td>
<td>-0.0847</td>
</tr>
<tr>
<td>$\tau$ ($\sigma$) or $\tau^+$</td>
<td>1 s</td>
<td>0.060</td>
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<tr>
<td>$T^+/\sigma^+$ absolute ratio</td>
<td>3.38</td>
<td>3.38</td>
</tr>
<tr>
<td>$R_2$</td>
<td>11.5 mm</td>
<td>3.8 mm</td>
</tr>
<tr>
<td>$E_p$ (mm) or $E_p^+$</td>
<td>0.33</td>
<td>4.56 MWm$^{-2}$</td>
</tr>
<tr>
<td>$P$ (W)</td>
<td>13 kW</td>
<td></td>
</tr>
</tbody>
</table>
Figure 5. Evolution of microheat checking density and of macrocrack propagation on the surface of a specimen for different repeated thermal chocks.
CONCLUSIONS

We propose that a transient TF test should be designed to respect the same temperature and elastic body thermal stresses, so-called “driving forces” of the damaging process, as in a real tool. Most of the time it is impossible to reproduce a homothetic temperature and stress field in the laboratory specimen. However, as far as one intends to study the heat-checking initiation on the surface of the component, reproducing the driving forces on the surface of a hollow tube is sufficient and relevant.

We explain an original and rapid method to design a TF lab test based on the normalization of heat transfer and thermal stresses equations for a cylindrical geometry. This method requires that the designers know what set of driving forces they are seeking. Prior to any TF design attempt, measurement and simulation of the working condition of the real tool must be performed. From this point, using a chart and a limited amount of calculations, it is possible to design the whole geometry (inner radius, thickness) and the heating conditions (power supply, heating duration). It appears that, for a given set of driving forces to be reproduced, there is only one solution to the problem, provided that the thermal boundary condition $h^+$ and the $Ep/R^2$ ratio are previously chosen.

The ratio that is used in Figure 4 and Eq. (12) provides a way to rank the thermal shocks. The larger the absolute value of the ratio, the lower the thermal shock. The largest thermal shock that can be attained is given by the well-known Eq. (16). We propose to call the inverse ratio, $|\sigma^+_{\text{max}}/T^+_{\text{max}}|$, the intensity of a thermal shock.

The present method has been used recently on TF rigs such as that described in Figure 2. The parameter $\sigma^\text{max}$ was changed at constant $T^\text{max}$ simply by modifying the heating duration $\tau$ and the maximum heating capacity $\Phi^\text{max}$ with the same thickness of specimen. Different types of damage, such as the density of microcracks (or heat checking in the oxide scale) and the macrocrack propagation on the surface of the specimen, are shown in Figure 5 [32]. It is worth observing that the two criteria for the damage of the specimen are strongly dependent on the intensity of the thermal shock $|\sigma^+_{\text{max}}/T^+_{\text{max}}|$.

REFERENCES